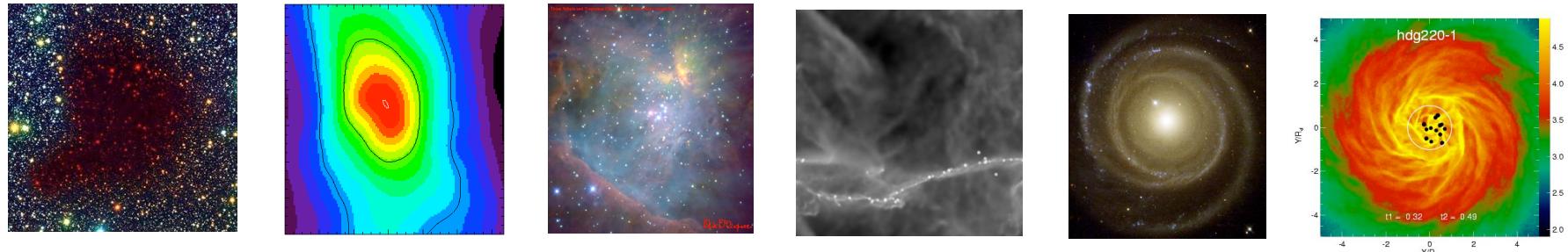


Star Formation



Ralf Klessen

Zentrum für Astronomie der Universität Heidelberg
Institut für Theoretische Astrophysik



ISM fragmentation: star formation

- theoretical approach to star formation
(historic overview + recent developments)
- interplay between turbulence and gravity
(properties of interstellar turbulence)
- application to star formation in Galactic molecular clouds

the questions

The star formation process

- *How* do stars form?
- What determines *when* and *where* stars form?
- What *regulates* the process and determines its *efficiency*?
- How do *global* properties of the galaxy influence star formation (a *local* process)?
- Are there different *modes* of SF?
(Starburst galaxies vs. *LSBs*, *isolated* SF vs. *clustered* SF)

→ *What physical processes initiate and control the formation of stars?*

historic overview

Early dynamical theory

- *Jeans (1902):* Interplay between self-gravity and thermal pressure

- stability of homogeneous spherical density enhancements against gravitational collapse
- dispersion relation:

$$\omega^2 = c_s^2 k^2 - 4\pi G \rho_0$$



Sir James Jeans, 1877 - 1946

- instability when $\omega^2 < 0$

- minimal mass:

$$M_J = \frac{1}{6} \pi^{-5/2} G^{-3/2} \rho_0^{-1/2} c_s^3 \propto \rho_0^{-1/2} T^{3/2}$$

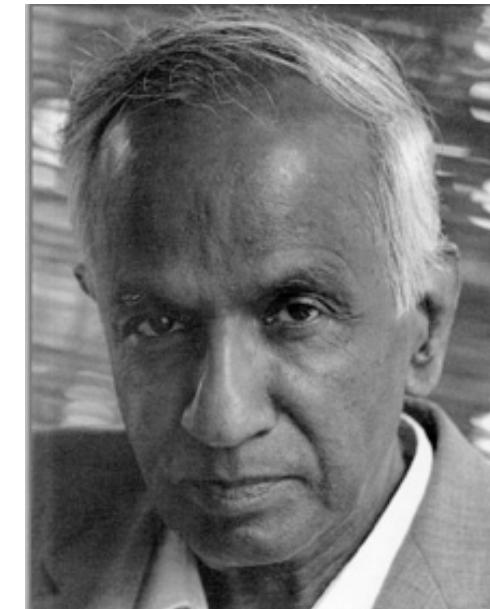
First approach to turbulence

- von Weizsäcker (1943, 1951) and Chandrasekhar (1951): concept of **MICROTURBULENCE**

- BASIC ASSUMPTION: separation of scales between dynamics and turbulence
 $\ell_{\text{turb}} \ll \ell_{\text{dyn}}$
- then turbulent velocity dispersion contributes to effective soundspeed:

- $C_s^2 \mapsto C_s^2 + \sigma_{rms}^2$
→ Larger effective Jeans masses → more stability
- BUT: (1) *turbulence depends on k*:

$$(2) \text{ supersonic turbulence} \rightarrow \text{usually} \quad \Omega_{rms}^2(k)$$



S. Chandrasekhar, 1910 - 1995

$$\sigma_{rms}^2(k) \gg C_s^2$$

Properties of IMS turbulence

ISM turbulence is:

- Supersonic (rms velocity dispersion \gg sound speed)
- Anisotropic (shocks & magnetic field)
- Driven on large scales (power in mol. clouds always dominated by largest-scale modes)

Microturbulent approach is
NOT valid in ISM

- No closed analytical/statistical formulation known --> necessity for numerical modeling

Problems of early dynamical theory

- Molecular clouds are *highly Jeans-unstable*
Yet, they do *NOT* form stars at high rate
and with high efficiency.
(the observed global SFE in molecular clouds is $\sim 5\%$)
→ *something prevents large-scale collapse.*
- All throughout the early 1990's, molecular clouds
had been thought to be long-lived quasi-equilibrium
entities.
- Molecular clouds are *magnetized.*

Magnetic star formation

- *Mestel & Spitzer (1956)*: Magnetic fields can prevent collapse!!!

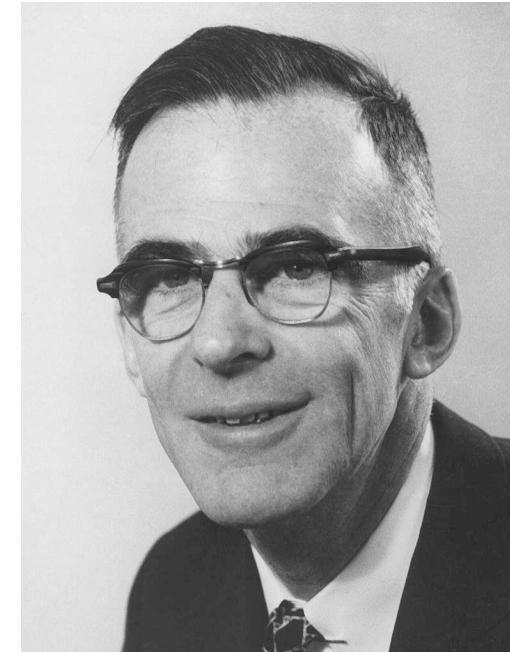
- Critical mass for gravitational collapse in presence of B-field

$$M_{cr} = \frac{5^{3/2}}{48\pi^2} \frac{B^3}{G^{3/2} \rho^2}$$

- Critical mass-to-flux ratio (Mouschovias & Spitzer 1976)

$$\left[\frac{M}{\Phi} \right]_{cr} = \frac{\zeta}{3\pi} \left[\frac{5}{G} \right]^{1/2}$$

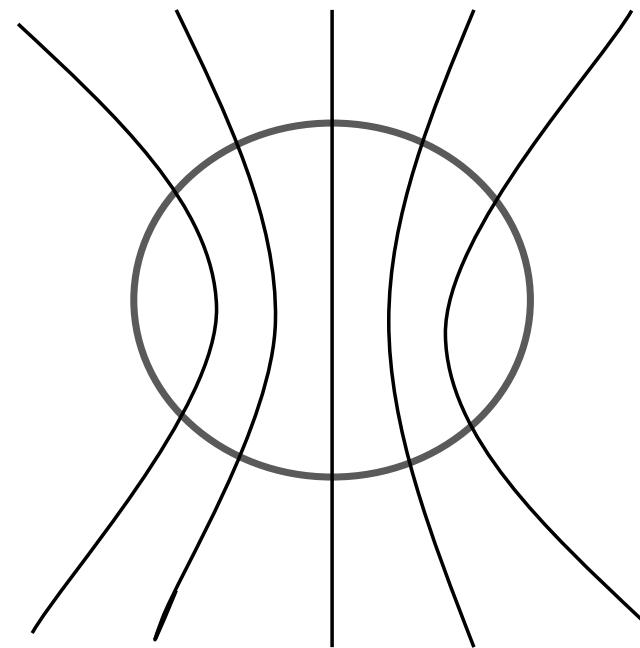
- Ambipolar diffusion can initiate collapse



Lyman Spitzer, Jr., 1914 - 1997

The "standard theory" of star formation:

- BASIC ASSUMPTION: Stars form from magnetically highly subcritical cores
- Ambipolar diffusion slowly increases (M/Φ): $\tau_{AD} \approx 10\tau_{ff}$
- Once $(M/\Phi) > (M/\Phi)_{crit}$:
dynamical collapse of SIS
 - Shu (1977) collapse solution
 - $dM/dt = 0.975 c_s^3/G = \text{const.}$
- Was (in principle) only intended for isolated, low-mass stars



Problems of magnetic SF

- Observed B-fields are weak, at most marginally critical (Crutcher 1999, Bourke et al. 2001)
- Magnetic fields cannot prevent decay of turbulence (Mac Low et al. 1998, Stone et al. 1998, Padoan & Nordlund 1999)
- Structure of prestellar cores (Bacman et al. 2000, e.g. Barnard 68 from Alves et al. 2001)
- Strongly time varying dM/dt (e.g. Hendriksen et al. 1997, André et al. 2000)
- More extended infall motions than predicted by the standard model (Williams & Myers 2000, Myers et al. 2000)

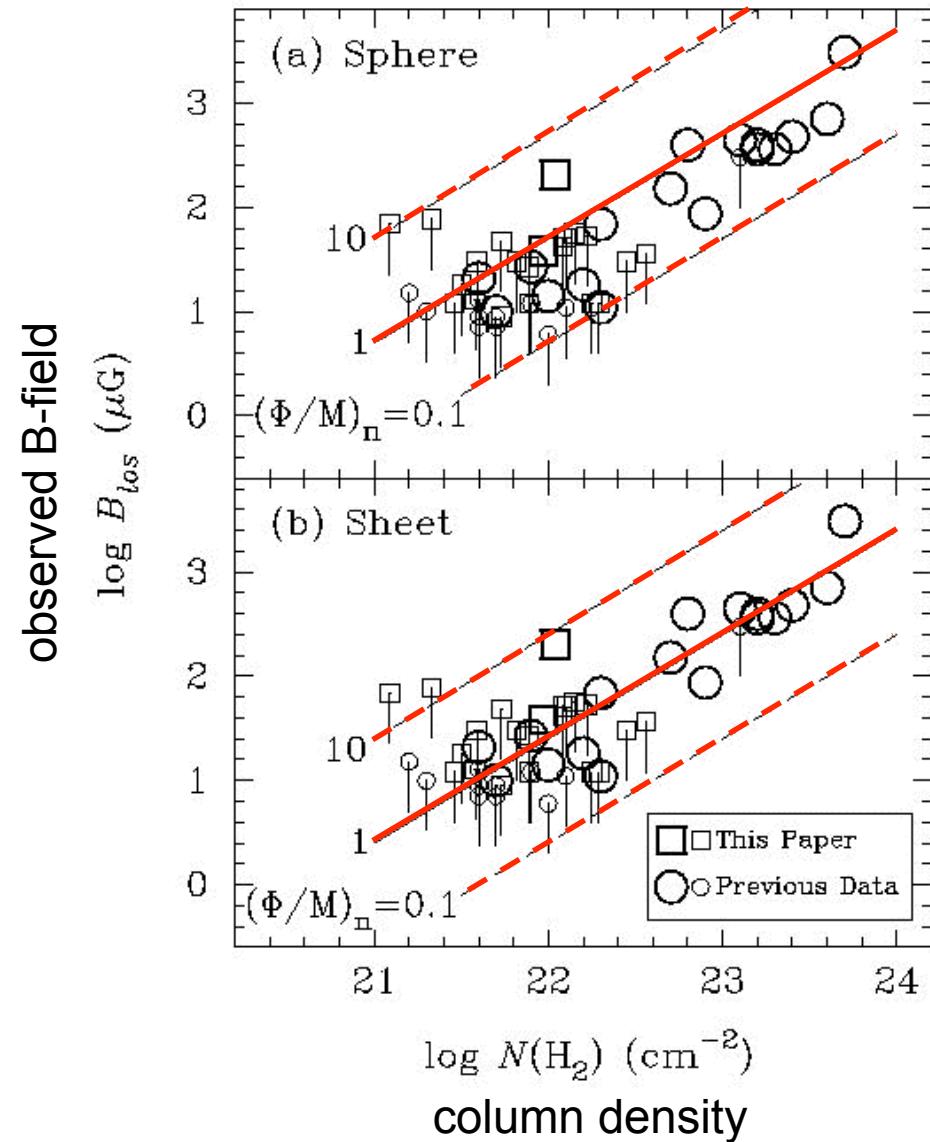
Observed B-fields are weak

B versus $N(H_2)$ from
Zeeman measurements.

(from Bourke et al. 2001)

→ cloud cores are
magnetically
supercritical!!!

$(\Phi/M)_n > 1$ no collapse
 $(\Phi/M)_n < 1$ collapse

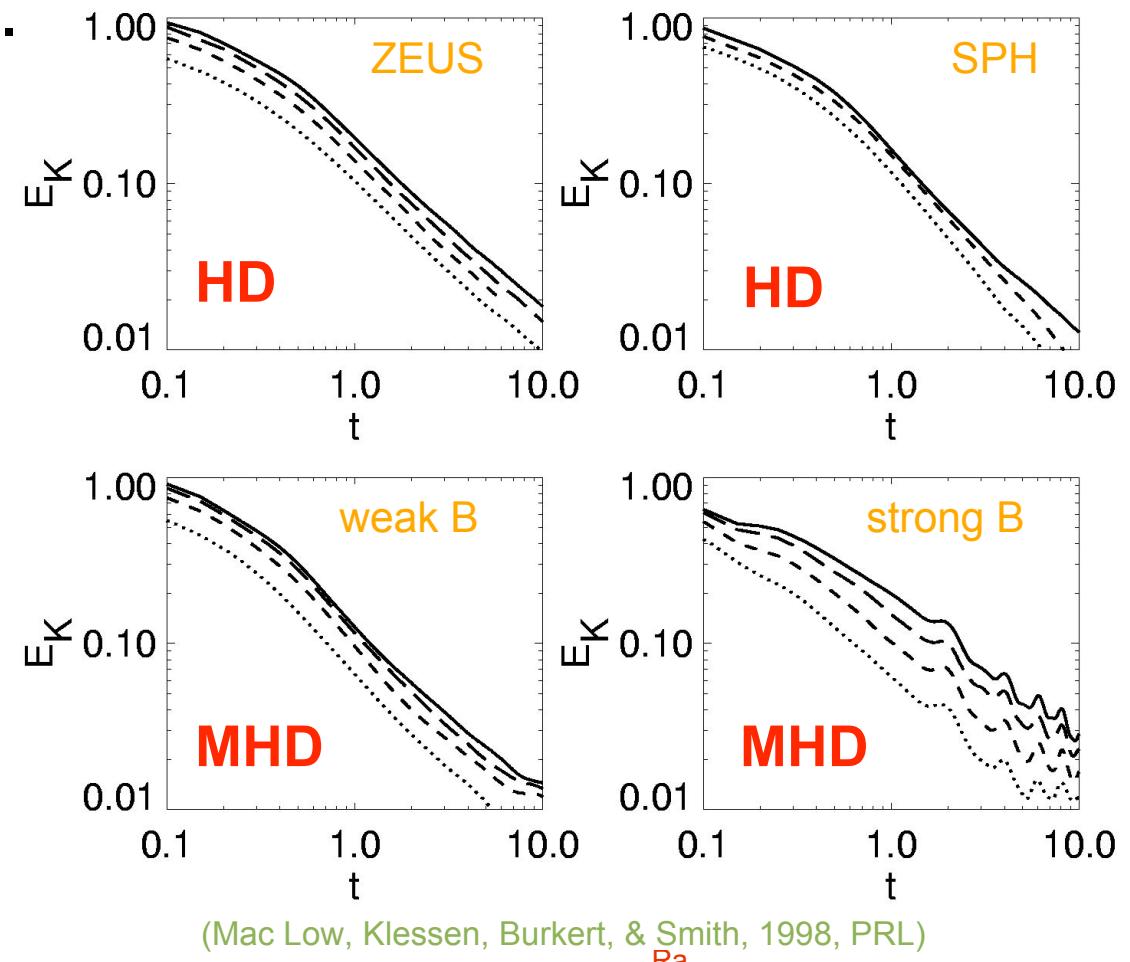


Molecular cloud dynamics

- Timescale problem: Turbulence *decays* on timescales *comparable to the free-fall time* τ_{ff} ($E \propto t^{-\eta}$ with $\eta \approx 1$).

(Mac Low et al. 1998,
Stone et al. 1998,
Padoan & Nordlund 1999)

- Magnetic fields (static or wave-like) *cannot* prevent loss of energy.



Problems of magnetic SF

- As many prestellar cores as protostellar cores in SF regions (e.g. André et al 2002)
- Molecular cloud clumps seem to be chemically young
(Bergin & Langer 1997, Pratap et al 1997, Aikawa et al 2001)
- Stellar age distribution small ($\tau_{\text{ff}} \ll \tau_{\text{AD}}$)
(Ballesteros-Paredes et al. 1999, Elmegreen 2000, Hartmann 2001)
- Strong theoretical criticism of the SIS as starting condition for gravitational collapse
(e.g. Whitworth et al 1996, Nakano 1998, as summarized in Klessen & Mac Low 2004)
- Most stars form as binaries

modern ideas

Graviturbulent star formation

- Idea:

*Star formation is controlled
by interplay between
gravity and
supersonic turbulence!*

- Dual role of turbulence:

- *stability on large scales*
- *initiating collapse on small scales*

(e.g., Larson, 2003, Rep. Prog. Phys., 66, 1651;
or Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125)

Ralf Klessen: Lecture 2: 27.12.2006

Graviturbulent star formation

- Idea:

*Star formation is controlled
by interplay between
gravity and
supersonic turbulence!*

- Validity:

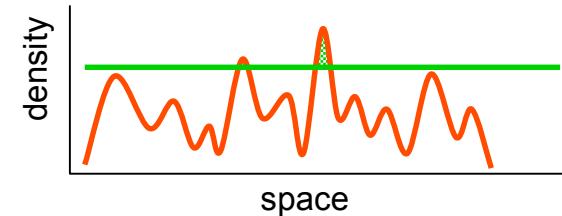
This hold on *all* scales and applies to build-up of stars and star clusters within molecular clouds as well as to the formation of molecular clouds in galactic disk.

(e.g., Larson, 2003, Rep. Prog. Phys., 66, 1651;
or Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125)

Ralf Klessen: Lecture 2: 27.12.2006

Graviturbulent star formation

- interstellar gas is highly *inhomogeneous*
 - *thermal instability*
 - *gravitational instability*
 - *turbulent compression* (in shocks $\delta p/p \propto M^2$; in atomic gas: $M \approx 1\dots 3$)
- cold *molecular clouds* can form rapidly in high-density regions at *stagnation points* of convergent large-scale flows
 - chemical *phase transition*: atomic \rightarrow molecular
 - process is *modulated* by large-scale *dynamics* in the galaxy
- inside *cold clouds*: turbulence is highly supersonic ($M \approx 1\dots 20$)
→ *turbulence* creates large density contrast,
gravity selects for collapse



GRAVOTURBULENT FRAGMENTATION

- *turbulent cascade*: local compression *within* a cloud provokes collapse
→ formation of individual *stars* and *star clusters*

turbulence

Properties of turbulence

- laminar flows turn *turbulent* at *high* Reynolds numbers

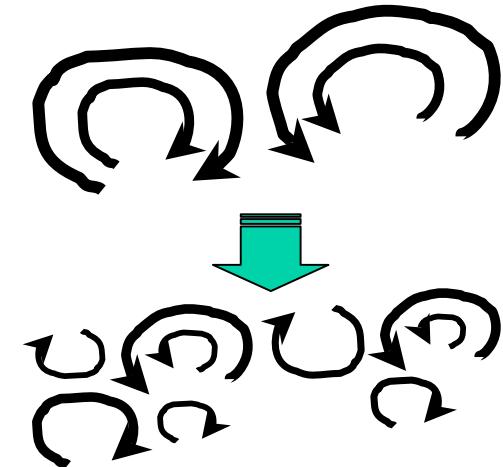
$$Re = \frac{\text{advection}}{\text{dissipation}} = \frac{VL}{\nu}$$

V = typical velocity on scale L , ν = viscosity, $Re > 1000$

- *vortex stretching* --> turbulence
is *intrinsically anisotropic*

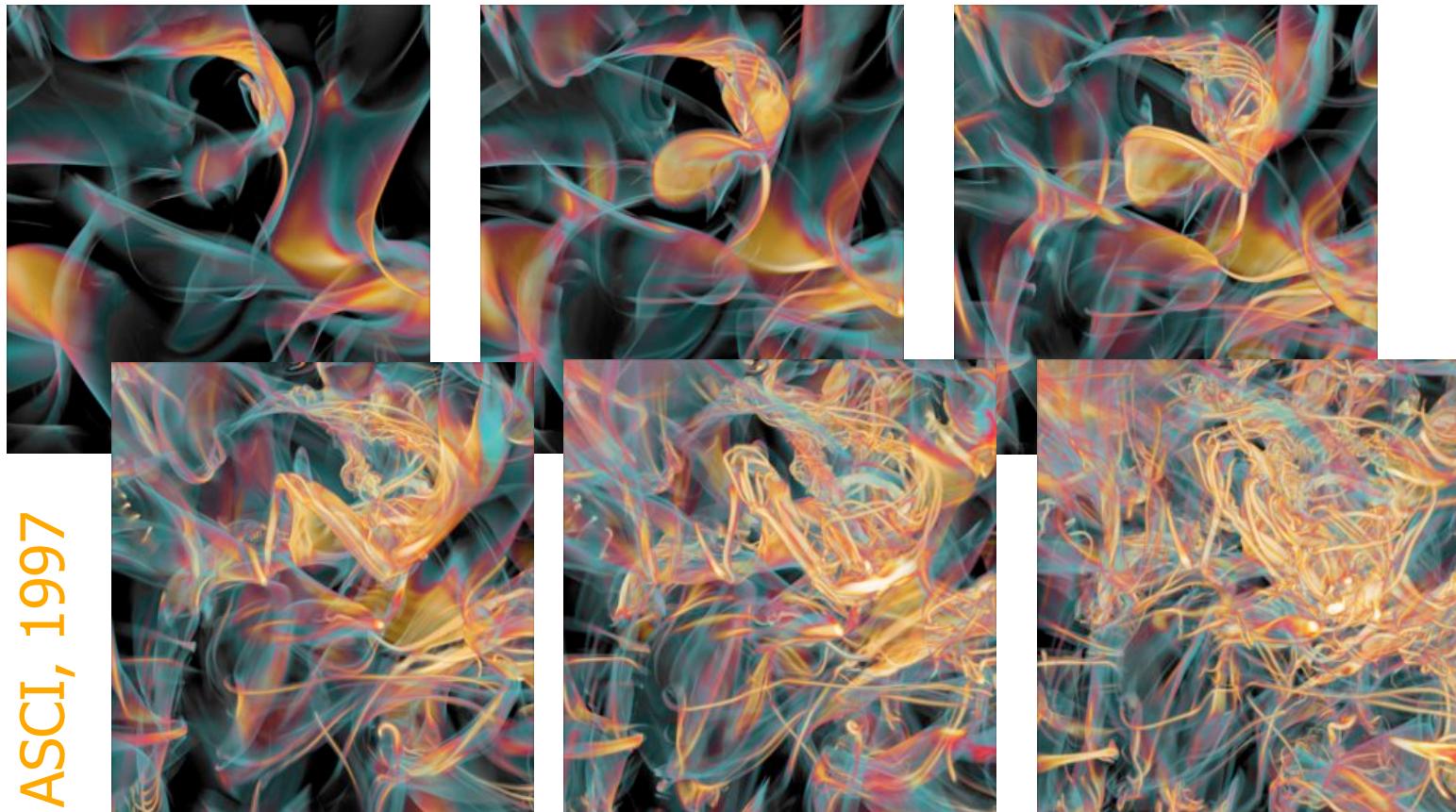
(only on large scales you *may* get
homogeneity & isotropy in a statistical sense;
see Landau & Lifschitz, Chandrasekhar, Taylor, etc.)

(ISM turbulence: shocks & B-field cause
additional inhomogeneity)



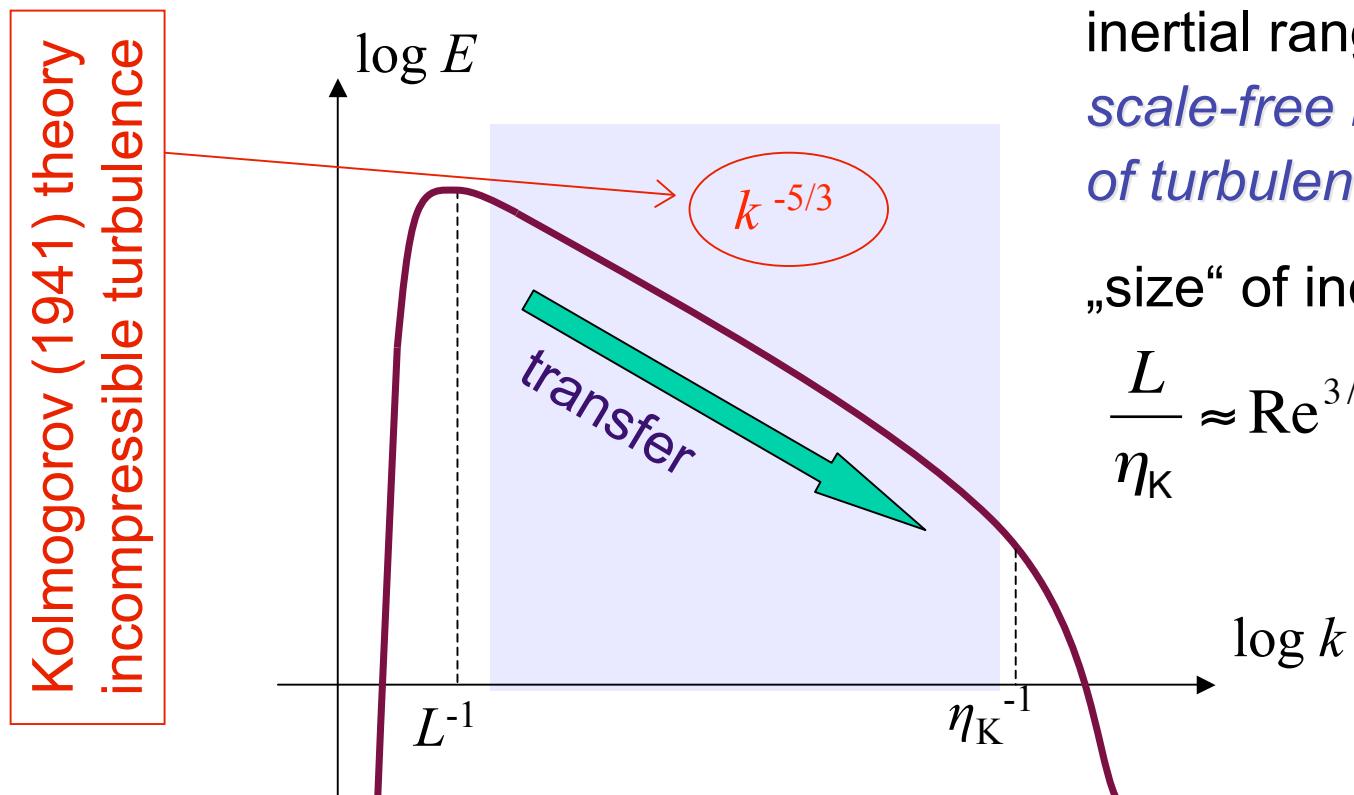
Vortex Formation

Porter et al.
ASCI, 1997



Vortices are stretched and folded in three dimensions

Turbulent cascade



energy
input
scale

energy
dissipation
scale

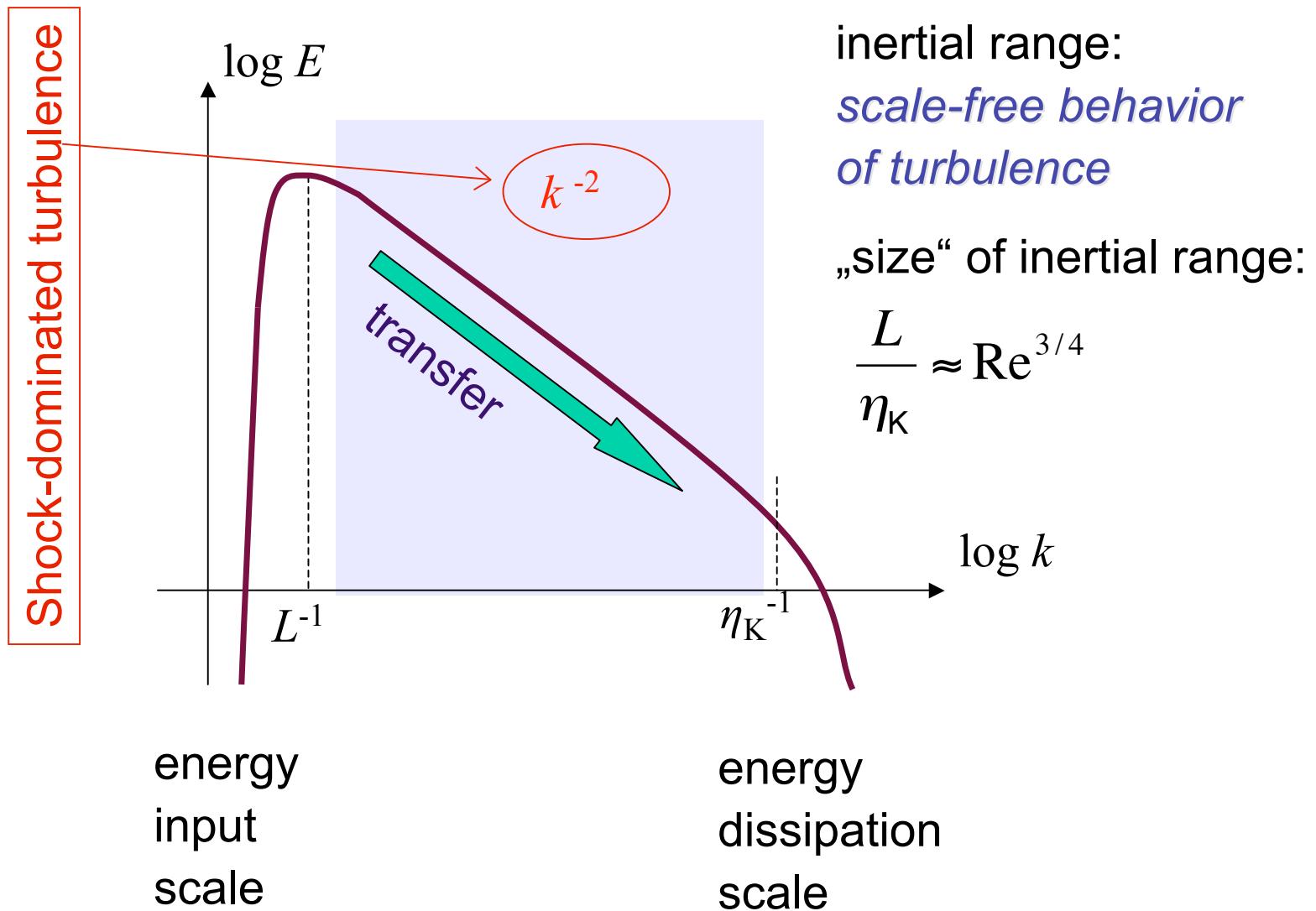
inertial range:
*scale-free behavior
of turbulence*

„size“ of inertial range:

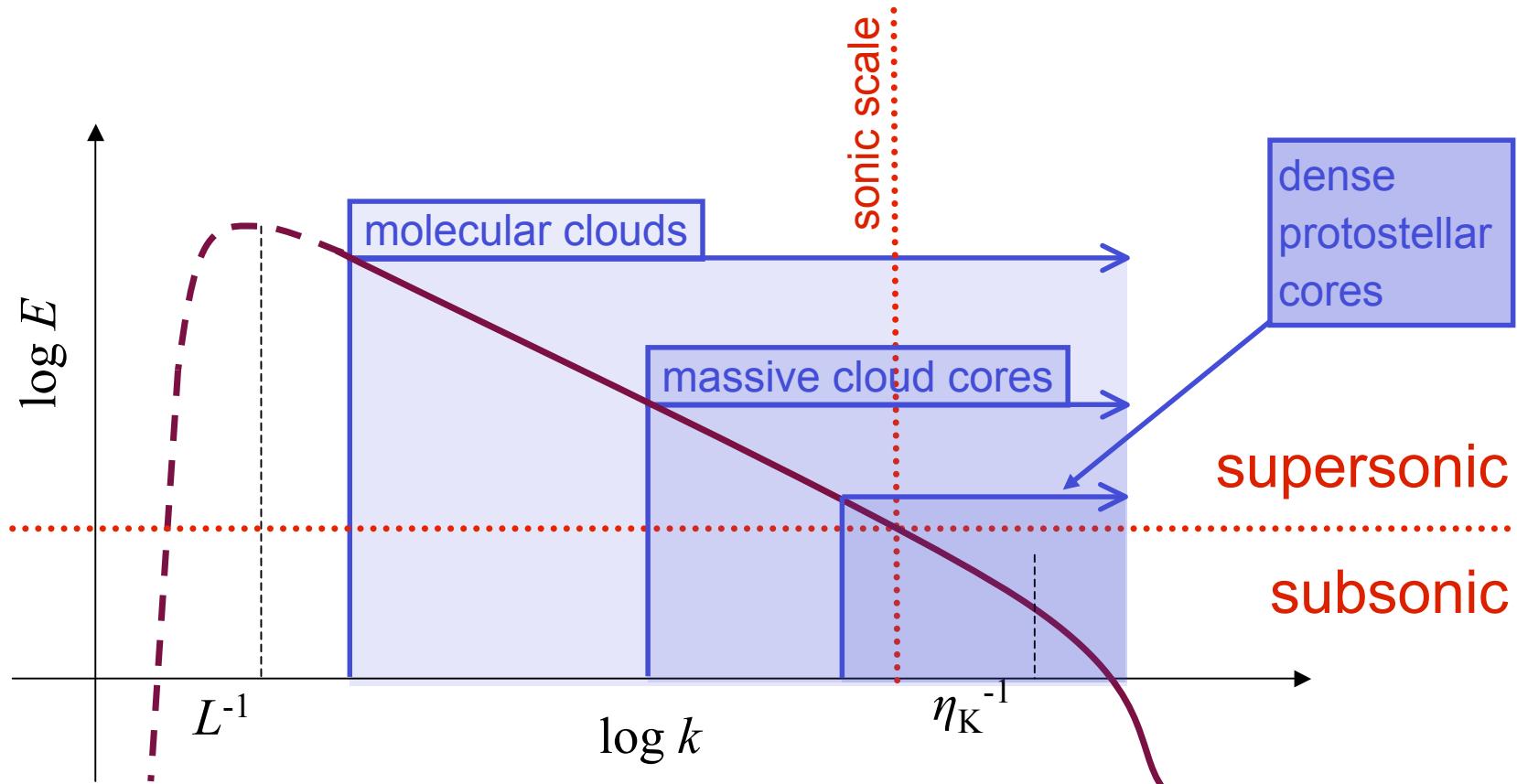
$$\frac{L}{\eta_K} \approx \text{Re}^{3/4}$$

$\log k$

Turbulent cascade



Turbulent cascade in ISM

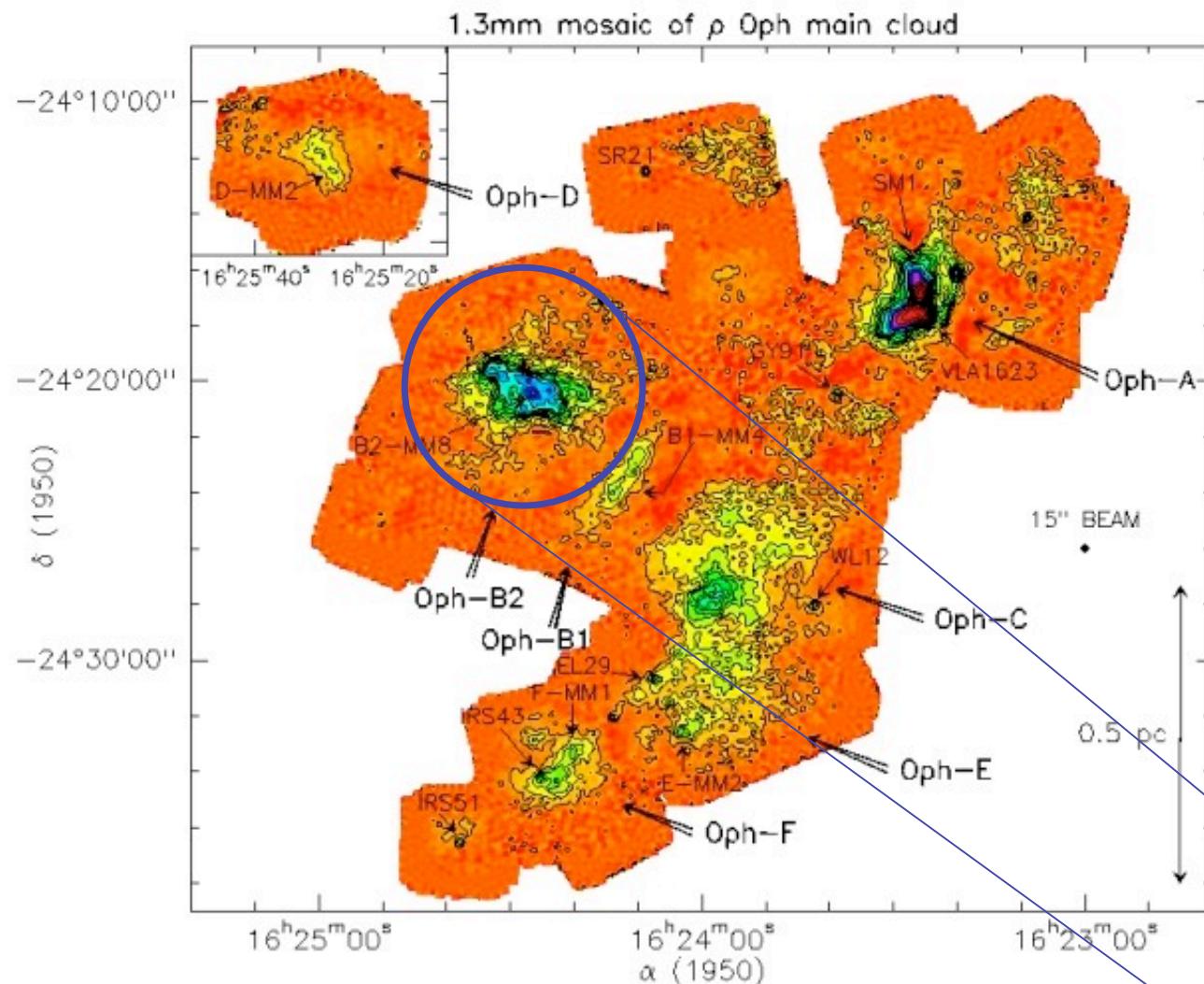


energy source & scale
NOT known
 (supernovae, winds,
 spiral density waves?)

$\sigma_{\text{rms}} \ll 1 \text{ km/s}$
 $M_{\text{rms}} \leq 1$
 $L \approx 0.1 \text{ pc}$

dissipation scale not known
 (ambipolar diffusion,
 molecular diffusion?)

Density structure of MC's



(Motte, André, & Neri 1998)

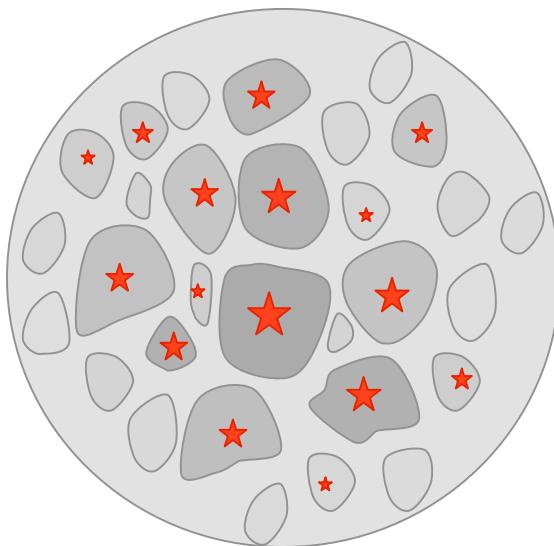
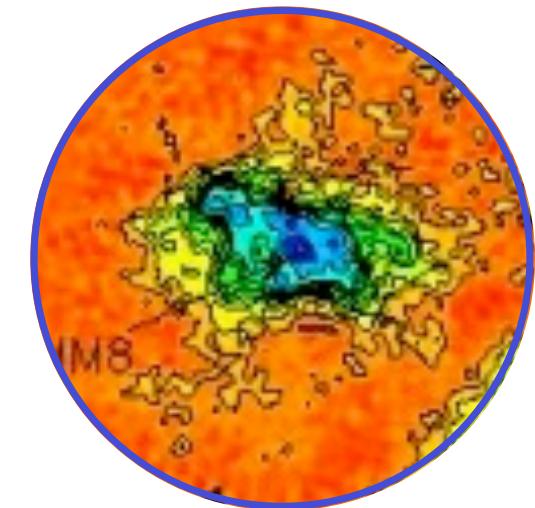
molecular clouds
are highly
inhomogeneous

stars form in the
densest and
coldest parts of
the cloud

ρ -Ophiuchus
cloud seen in dust
emission

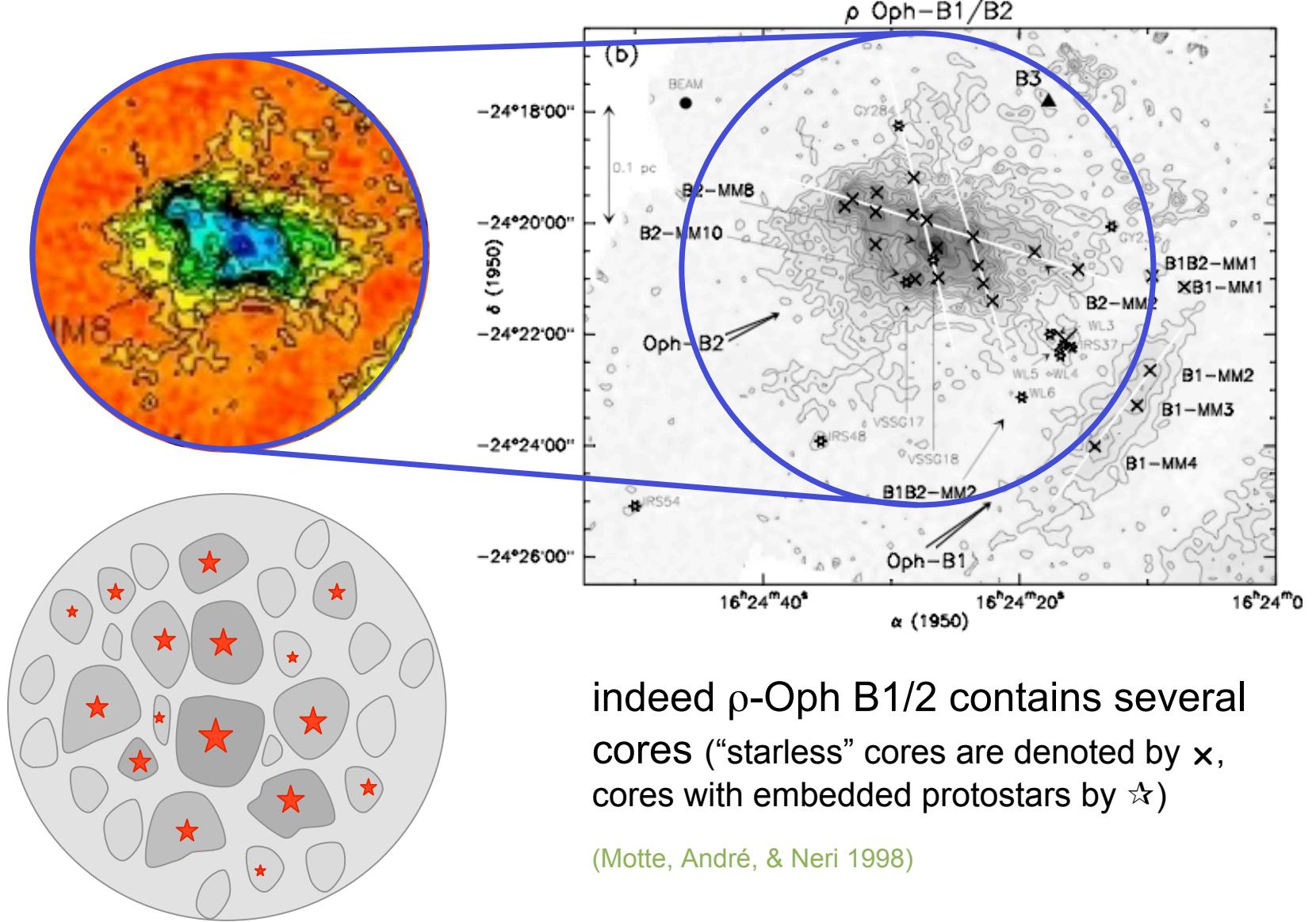
let's focus on
a cloud core
like this one

Evolution of cloud cores



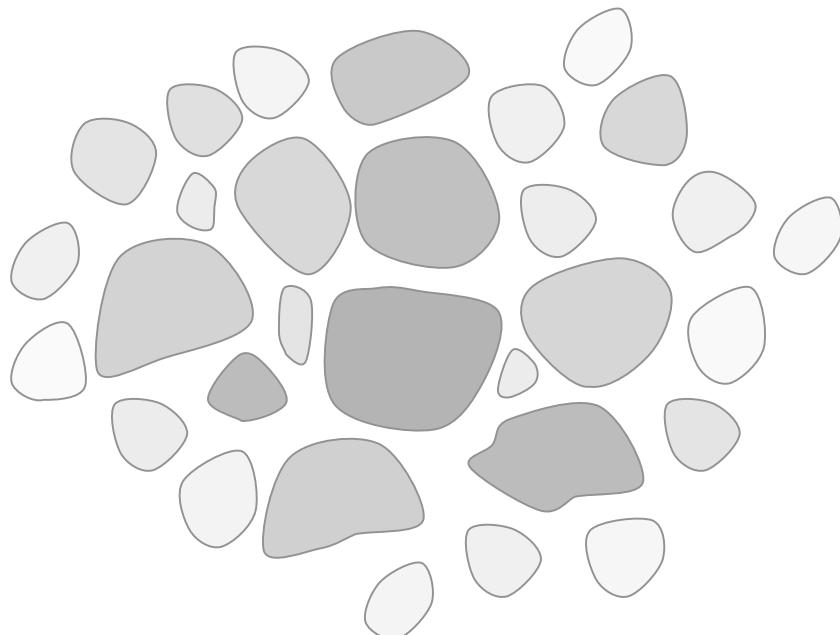
- How does this core evolve?
Does it form one single massive star or cluster with mass distribution?
- Turbulent cascade „goes through“ cloud core
 - > NO scale separation possible
 - > NO effective sound speed
- Turbulence is supersonic!
 - > produces strong density contrasts:
 $\delta\rho/\rho \approx M^2$
 - > with typical $M \approx 10$ --> $\delta\rho/\rho \approx 100!$
- many of the shock-generated fluctuations are Jeans unstable and go into collapse
- --> expectation: *core breaks up and forms a cluster of stars*

Evolution of cloud cores



Formation and evolution of cores

What happens to distribution
of cloud cores?



Two extreme cases:

(1) turbulence dominates energy budget:

$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| > 1$$

--> individual cores do *not* interact

--> *collapse of individual cores*
dominates *stellar mass growth*

--> *loose cluster of low-mass stars*

(2) turbulence decays, i.e. gravity

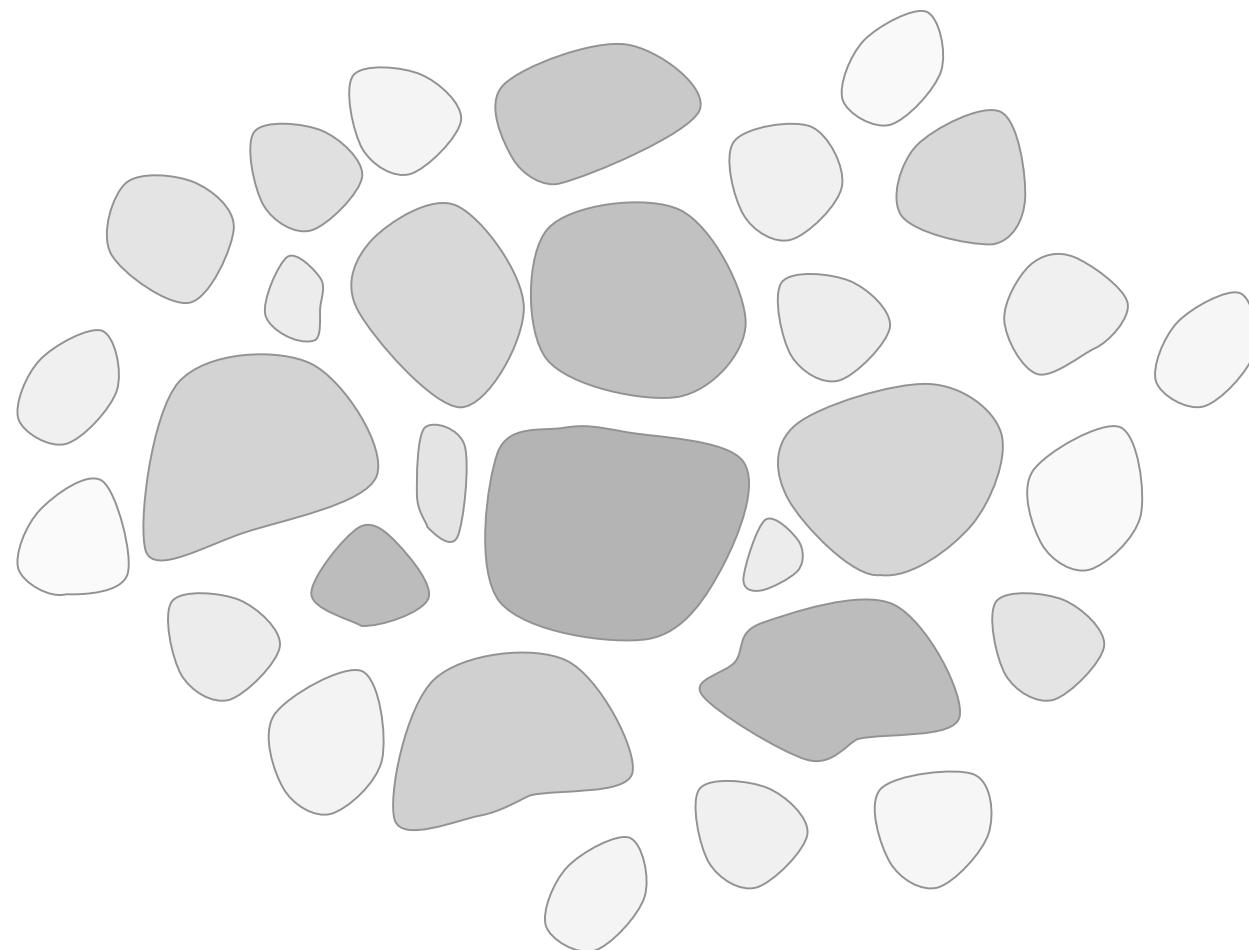
$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

--> *global contraction*

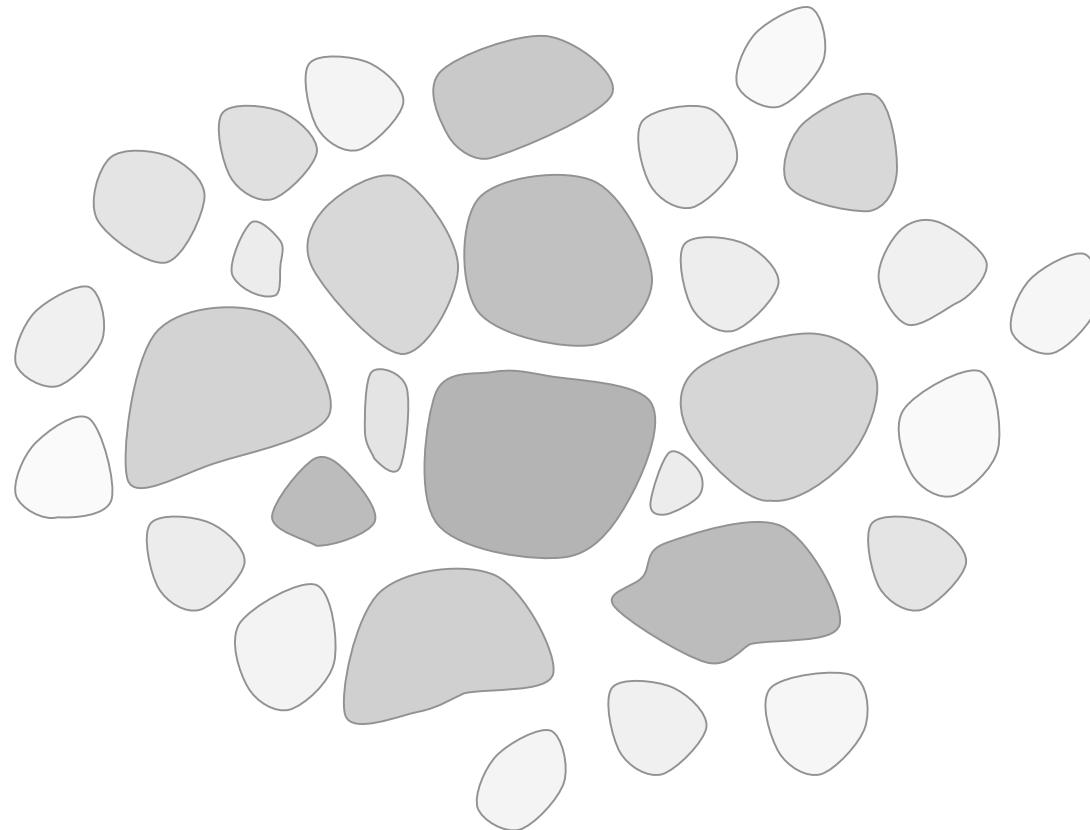
--> cores do *interact* while collapsing

--> *competition influences mass growth*

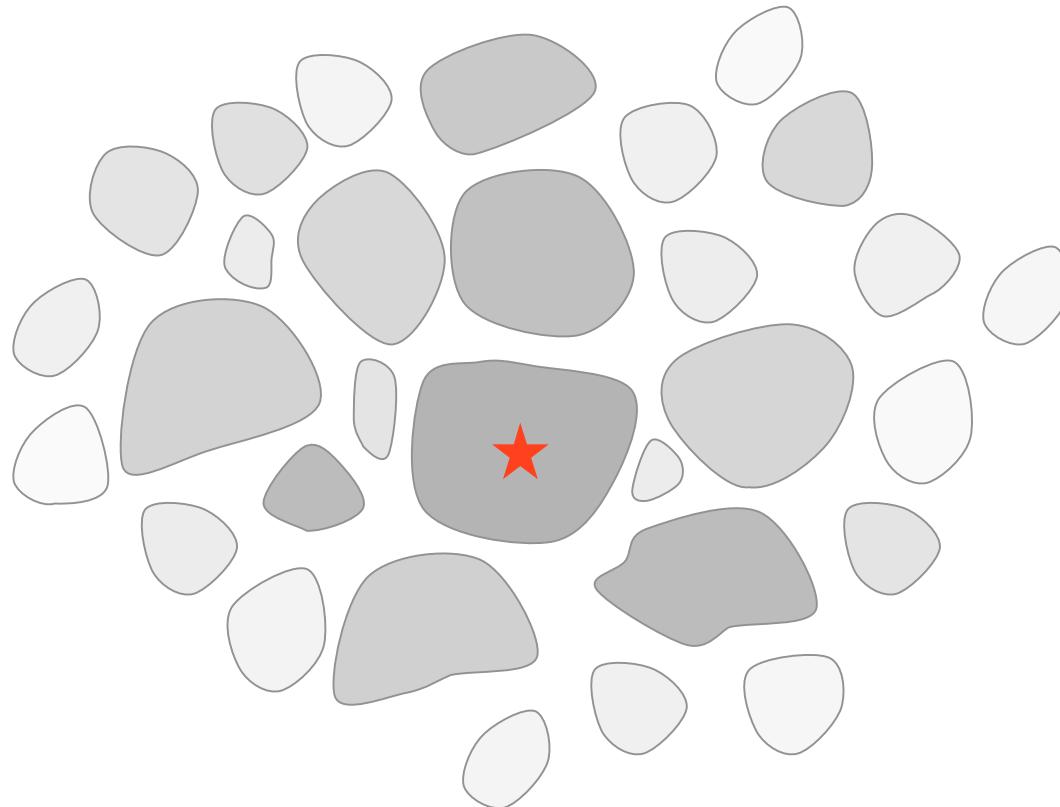
--> *dense cluster with high-mass stars*



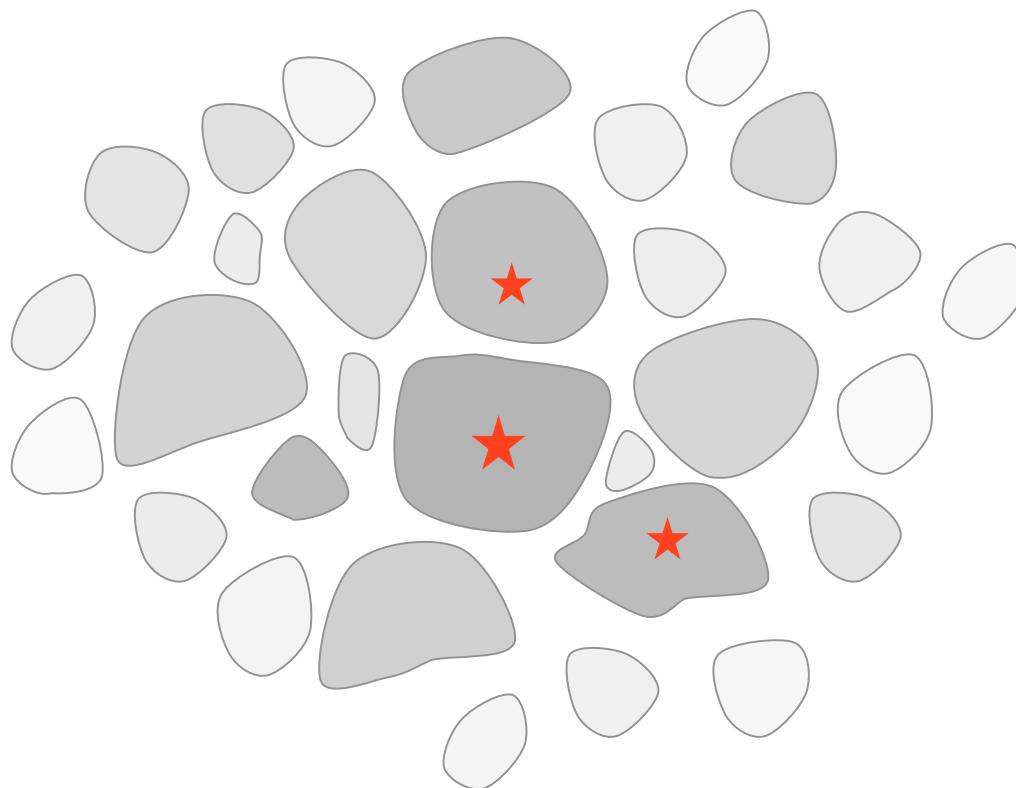
turbulence creates a hierarchy of clumps



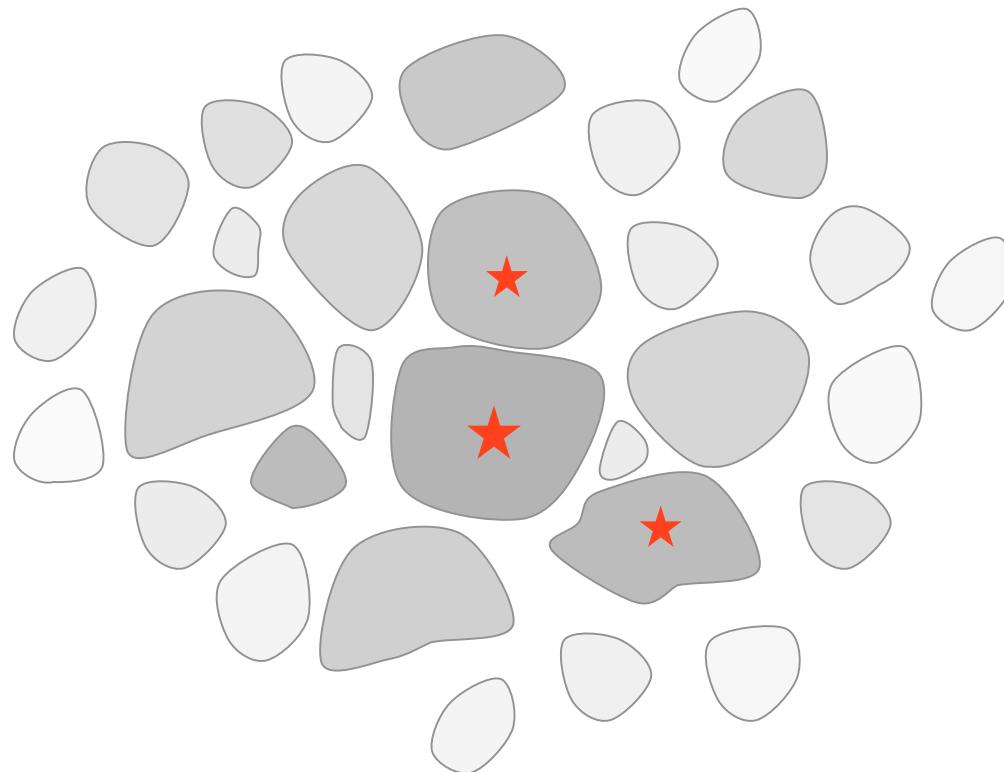
while region contracts, individual clumps collapse to form stars



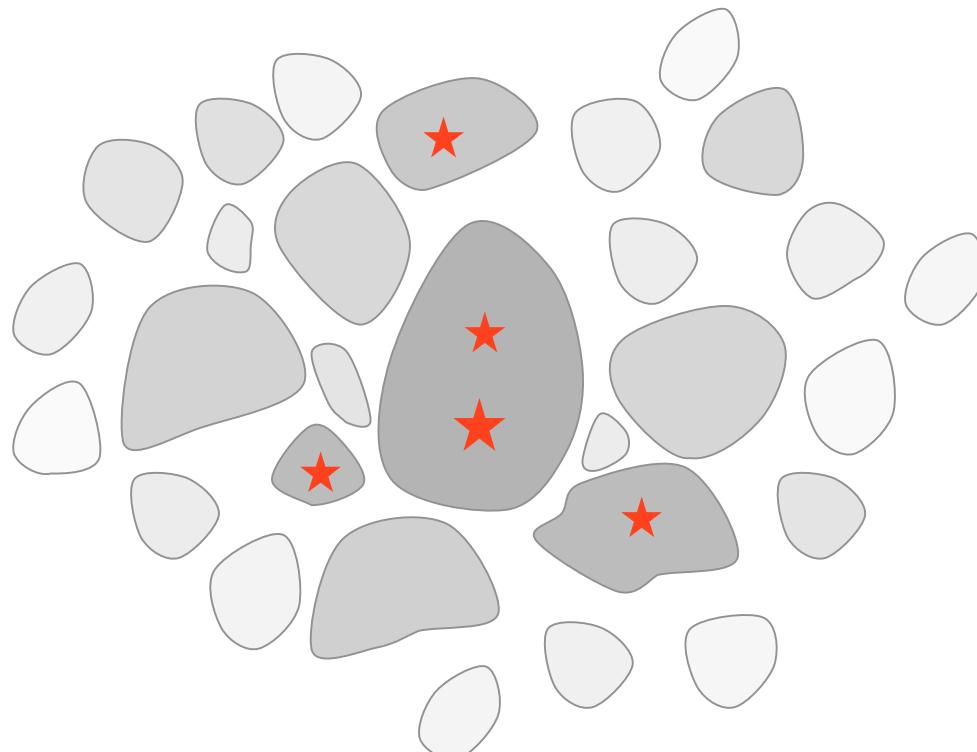
while region contracts, individual clumps collapse to form stars



individual clumps collapse to form stars

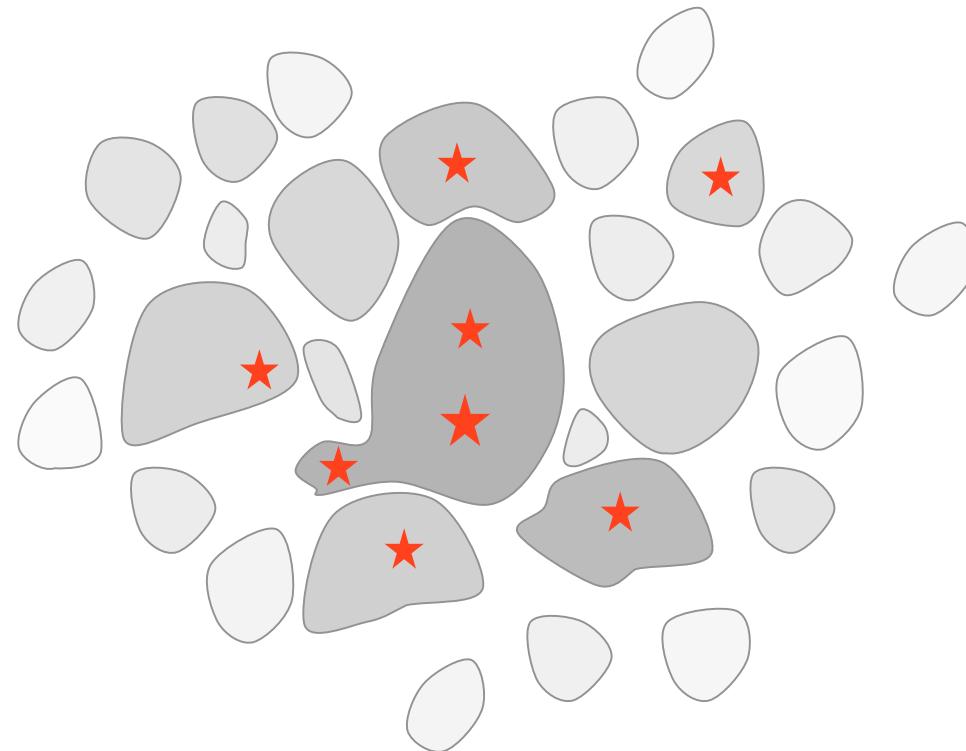


individual clumps collapse to form stars

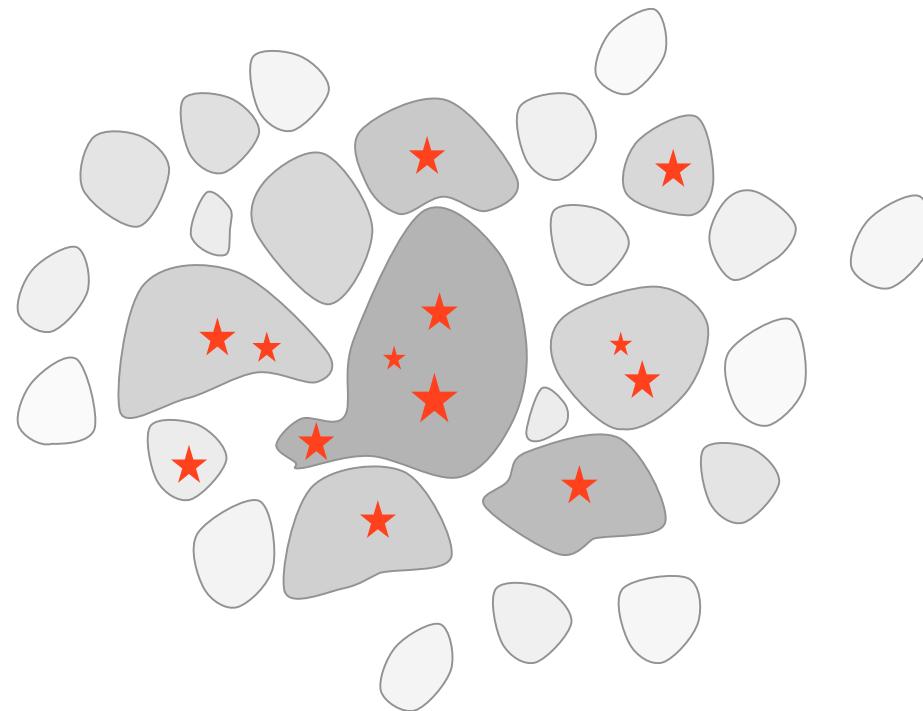


$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

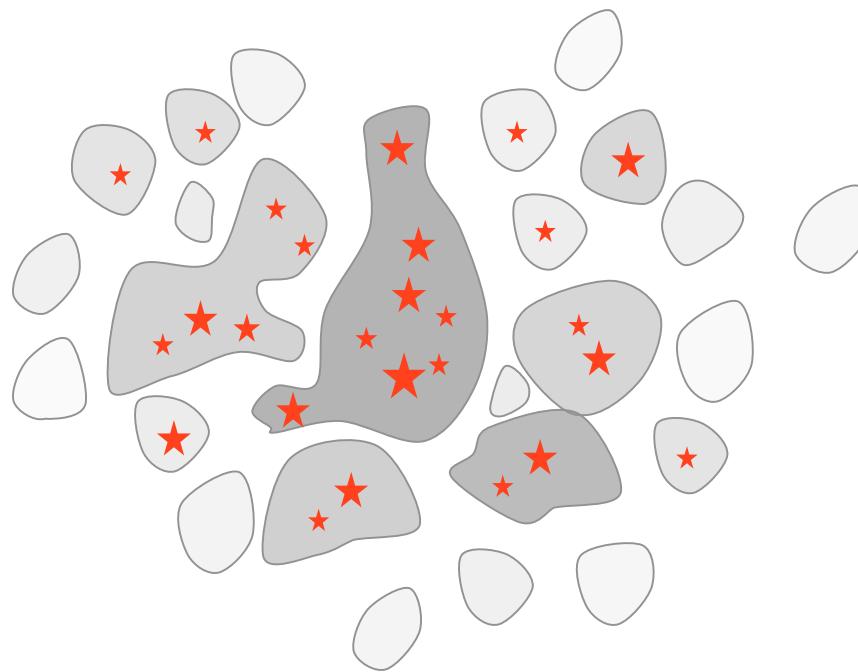
in *dense clusters*, clumps may merge while collapsing
--> then contain multiple protostars



in *dense clusters*, clumps may merge while collapsing
--> then contain multiple protostars



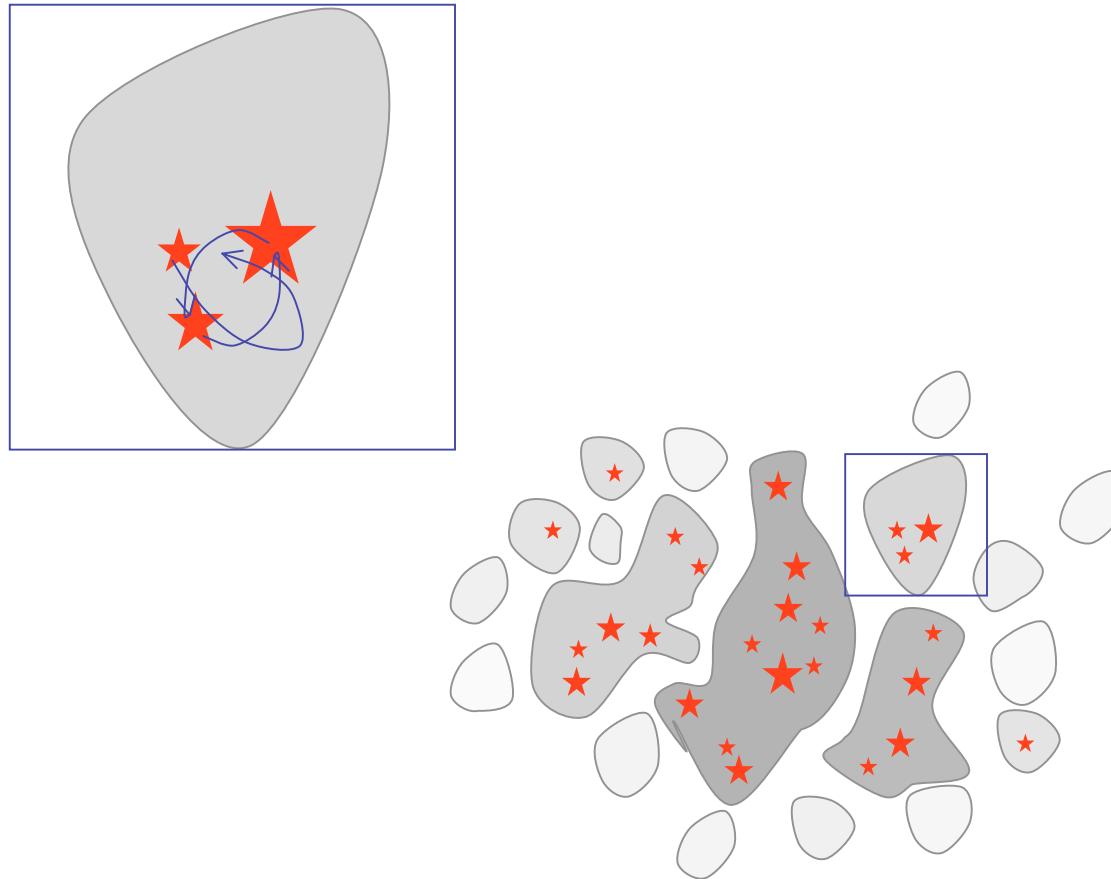
in *dense clusters*, clumps may merge while collapsing
--> then contain multiple protostars



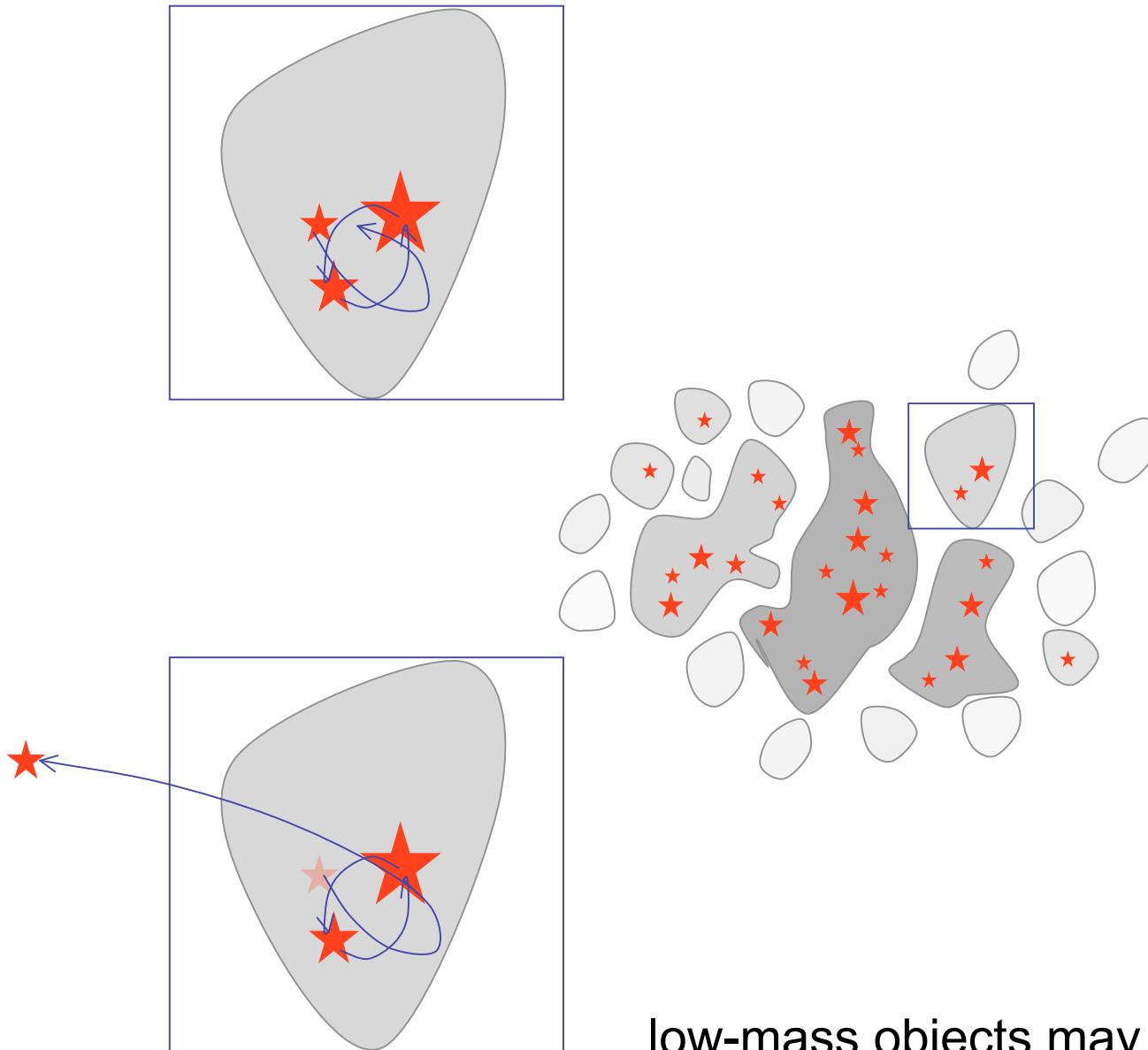
*in dense clusters, competitive mass growth
becomes important*



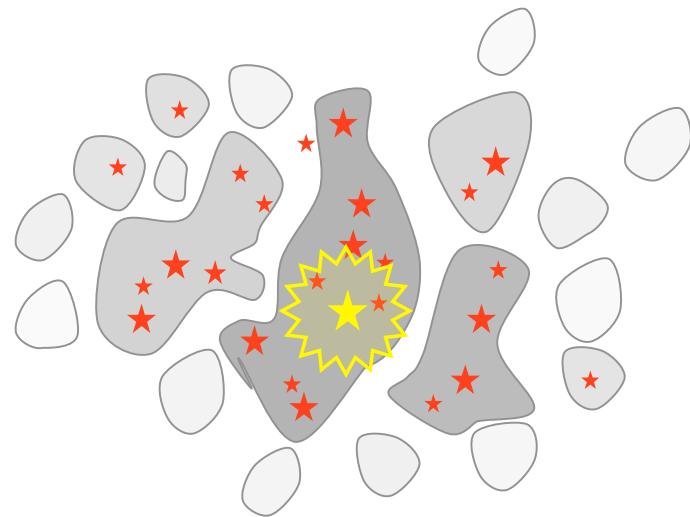
in dense clusters, competitive mass growth becomes important



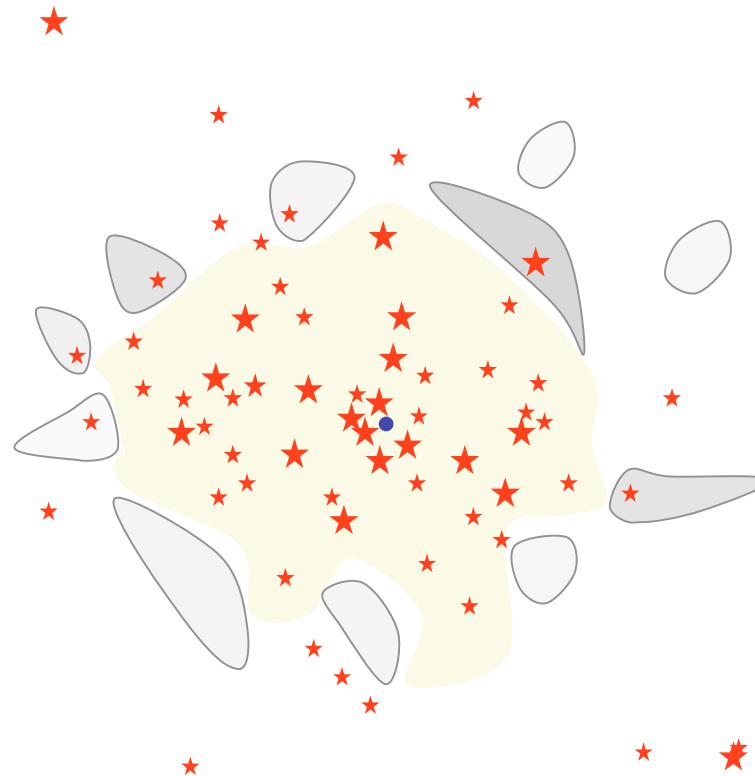
in dense clusters, N-body effects influence mass growth



low-mass objects may
become ejected --> accretion stops



feedback terminates star formation



result: *star cluster*, possibly with HII region

predictions

Predictions

- *global properties* (statistical properties)
 - SF efficiency and timescale
 - stellar mass function -- IMF
 - dynamics of young star clusters
 - description of self-gravitating turbulent systems (pdf's, Δ -var.)
 - chemical mixing properties
- *local properties* (properties of individual objects)
 - properties of individual clumps (e.g. shape, radial profile, lifetimes)
 - accretion history of individual protostars (dM/dt vs. t , j vs. t)
 - binary (proto)stars (eccentricity, mass ratio, etc.)
 - SED's of individual protostars
 - dynamic PMS tracks: $T_{\text{bol}}\text{-}L_{\text{bol}}$ evolution

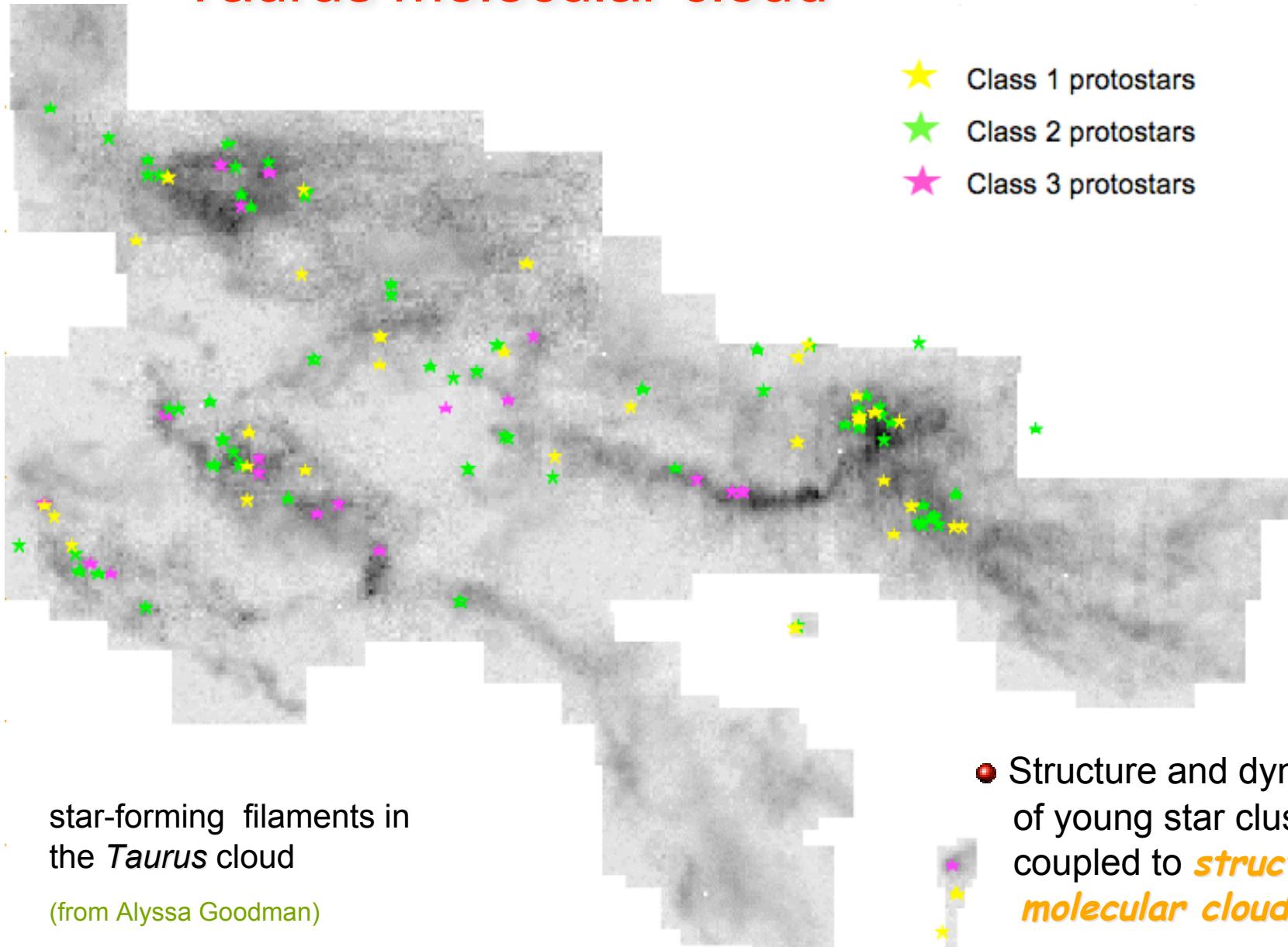
Examples and predictions

example 1: fragmentation and formation of star clusters

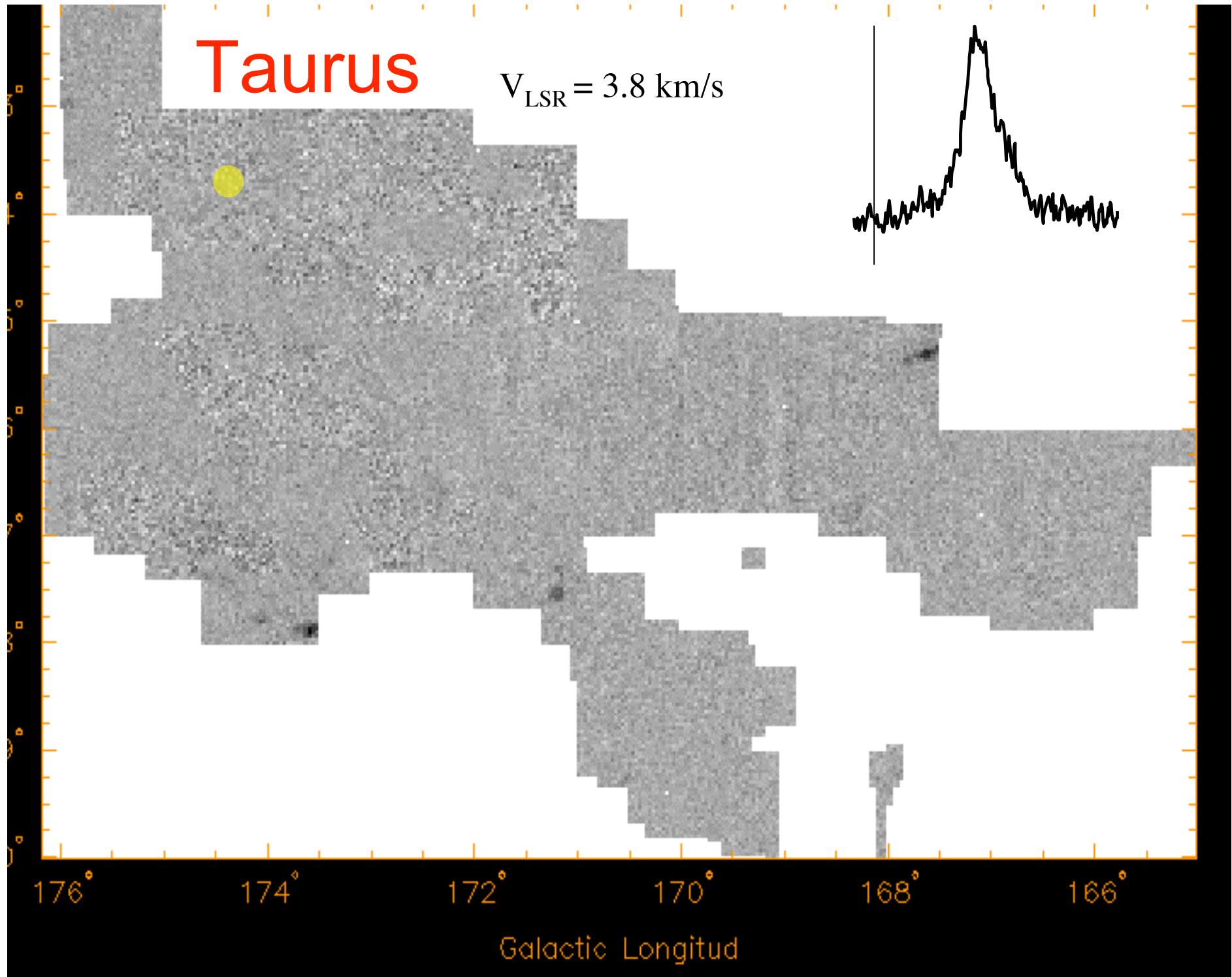
example 2: speculations on the origin of the stellar mass spectrum (IMF)

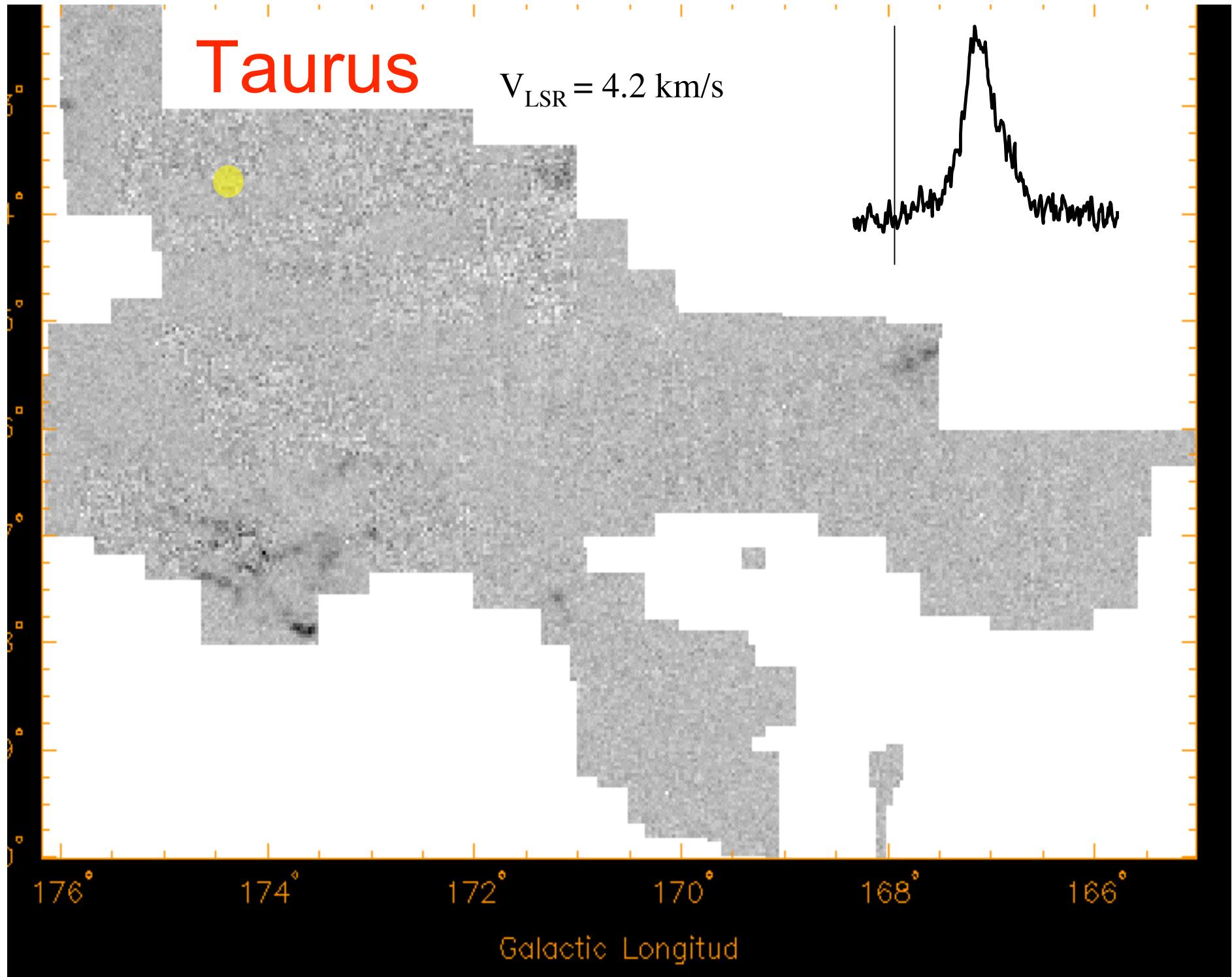
example¹

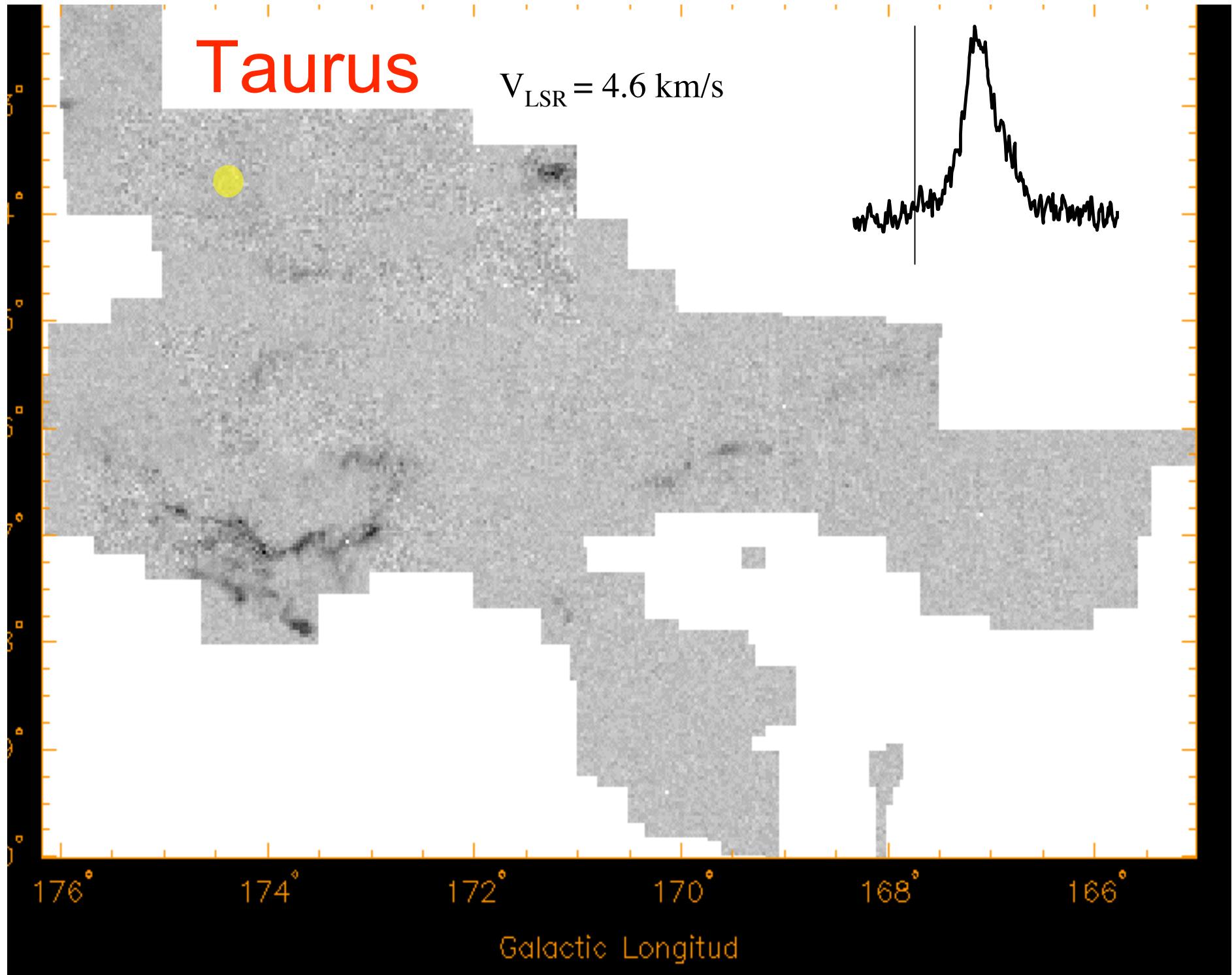
Taurus molecular cloud

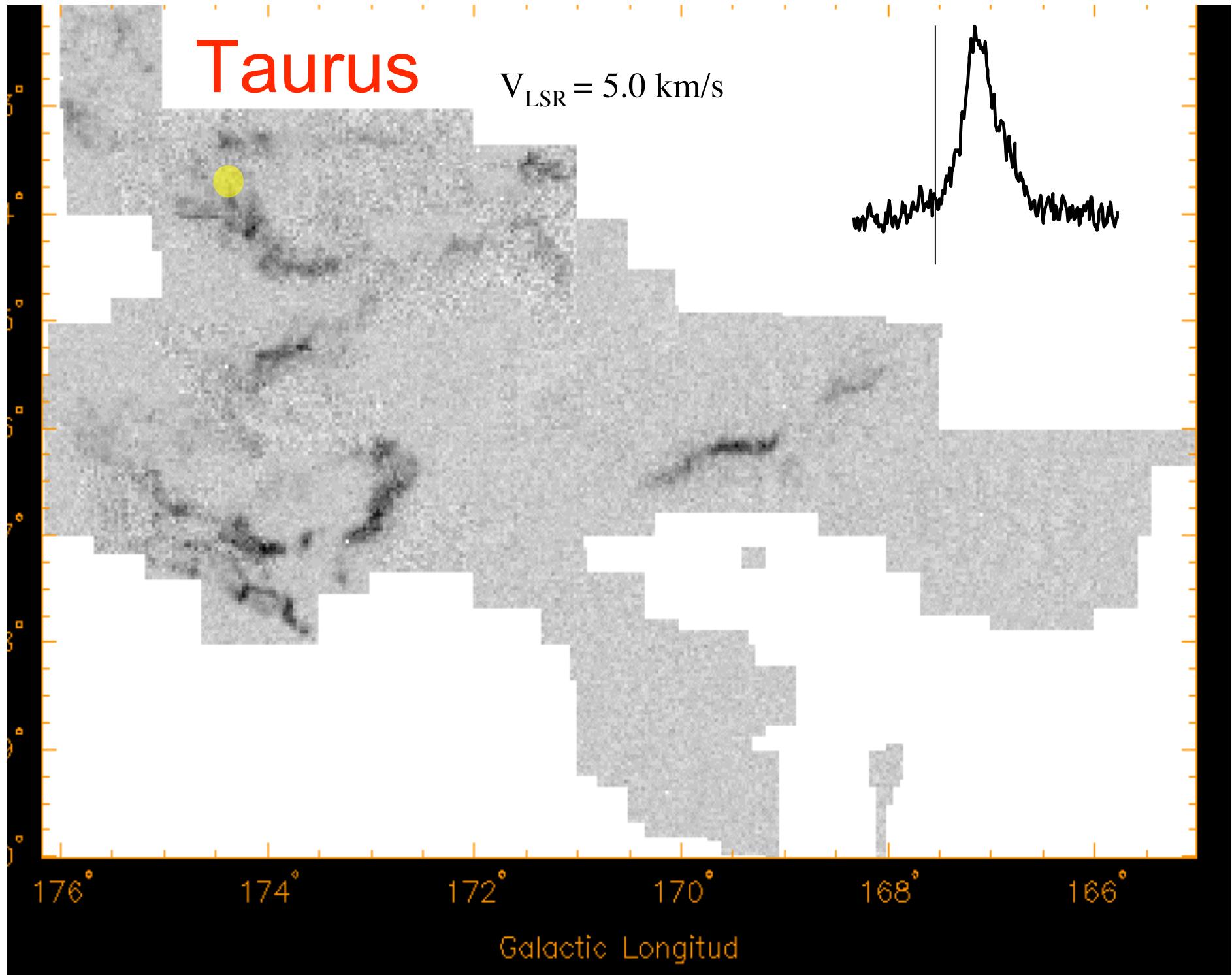


- Structure and dynamics of young star clusters is coupled to *structure of molecular cloud*



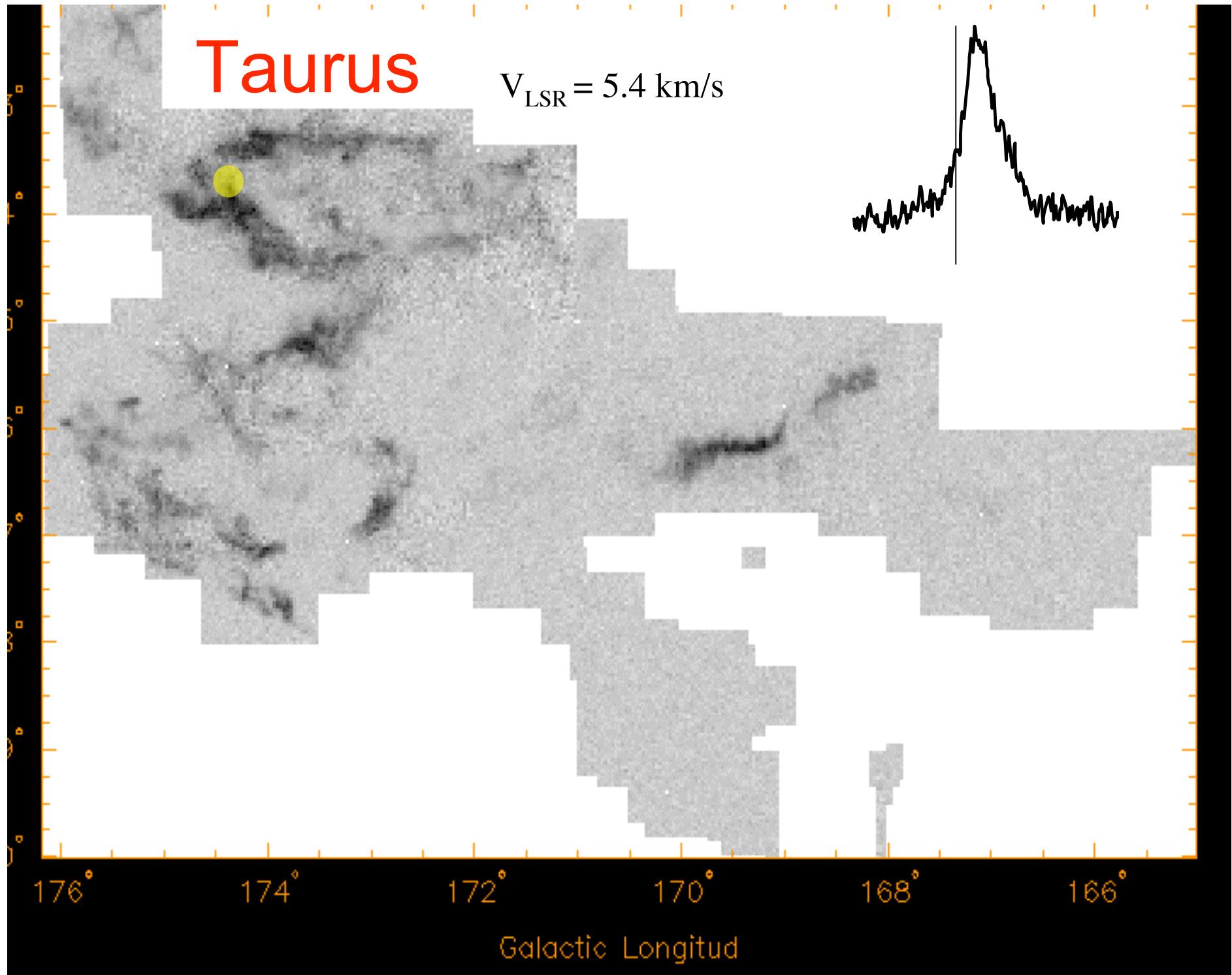


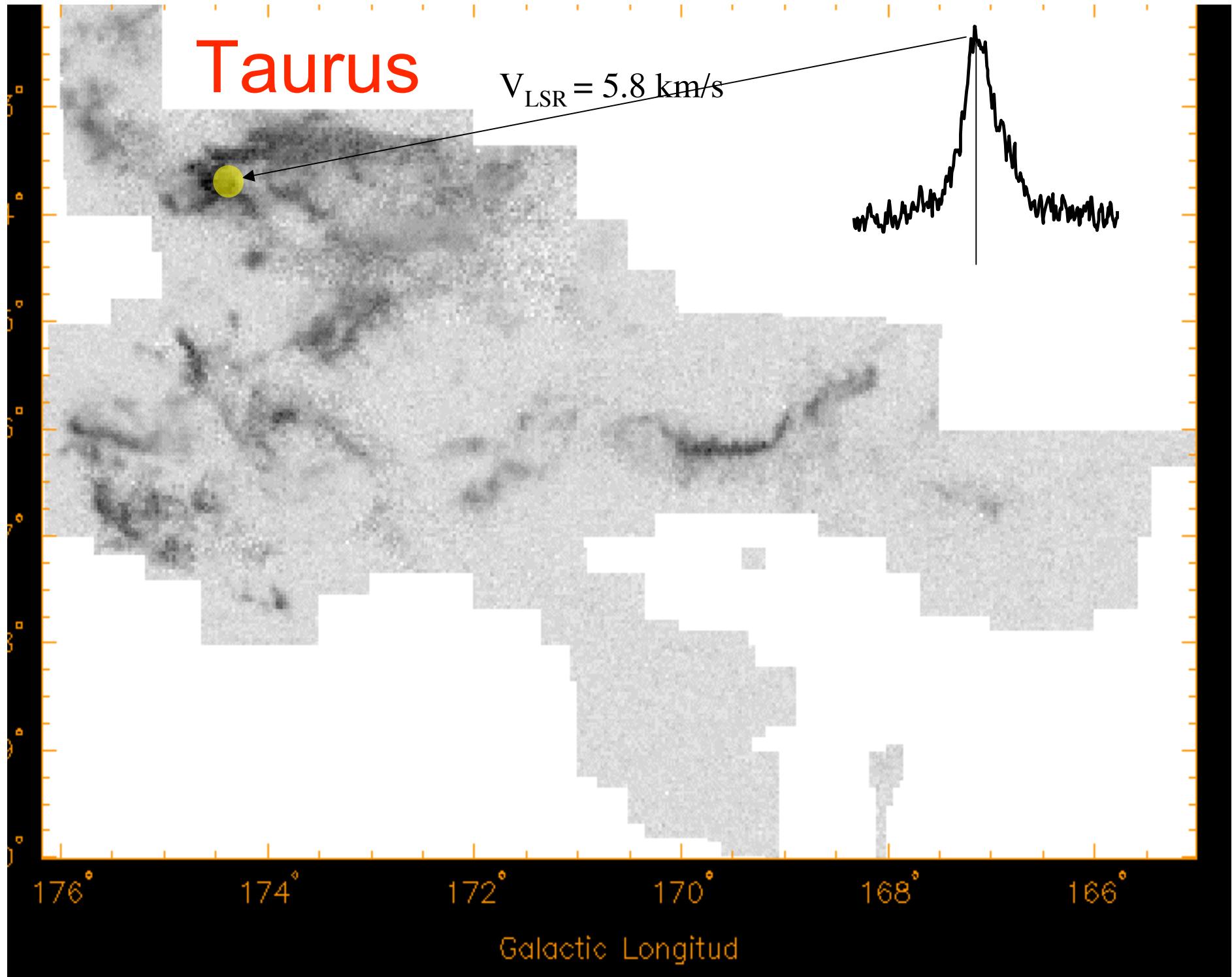


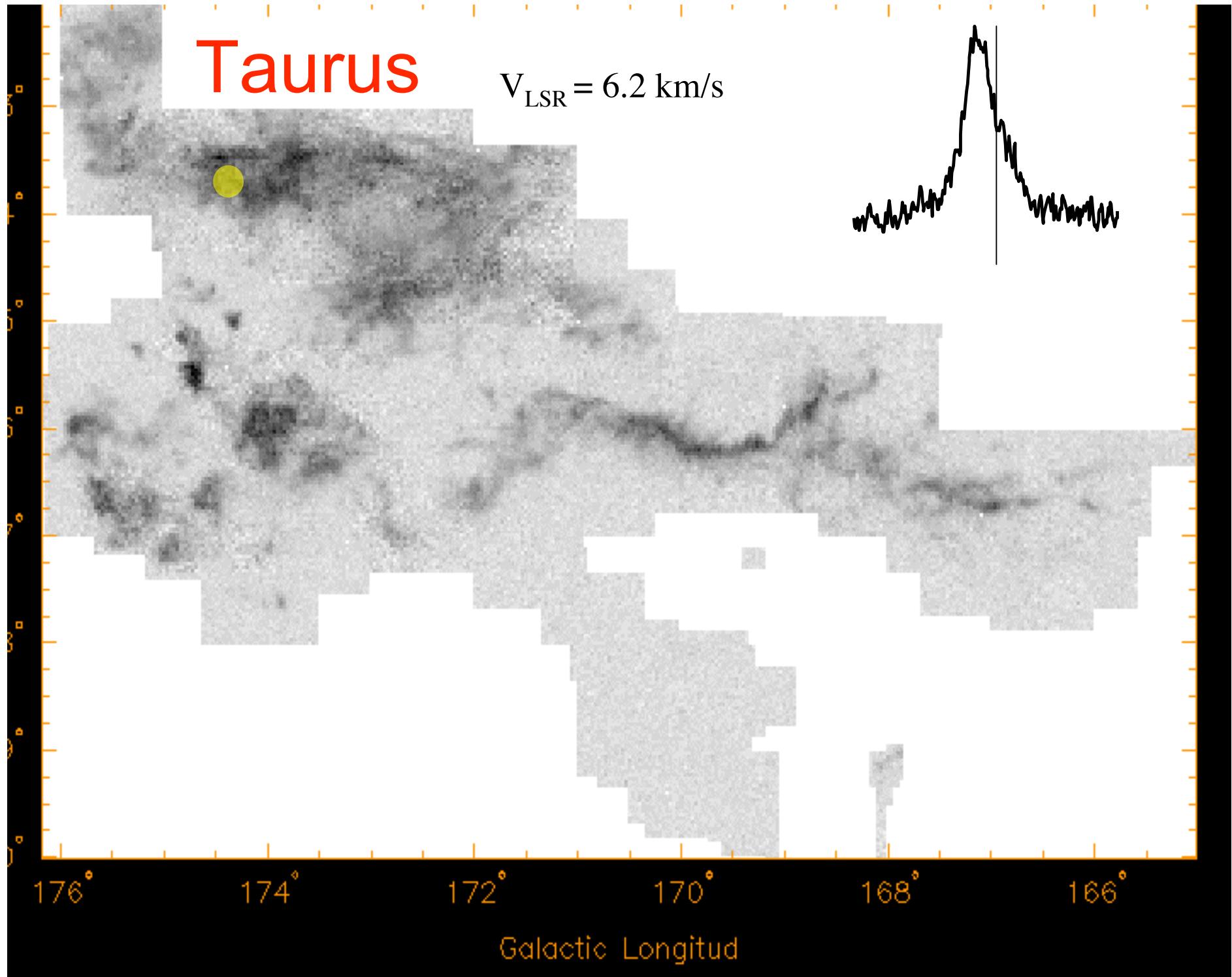


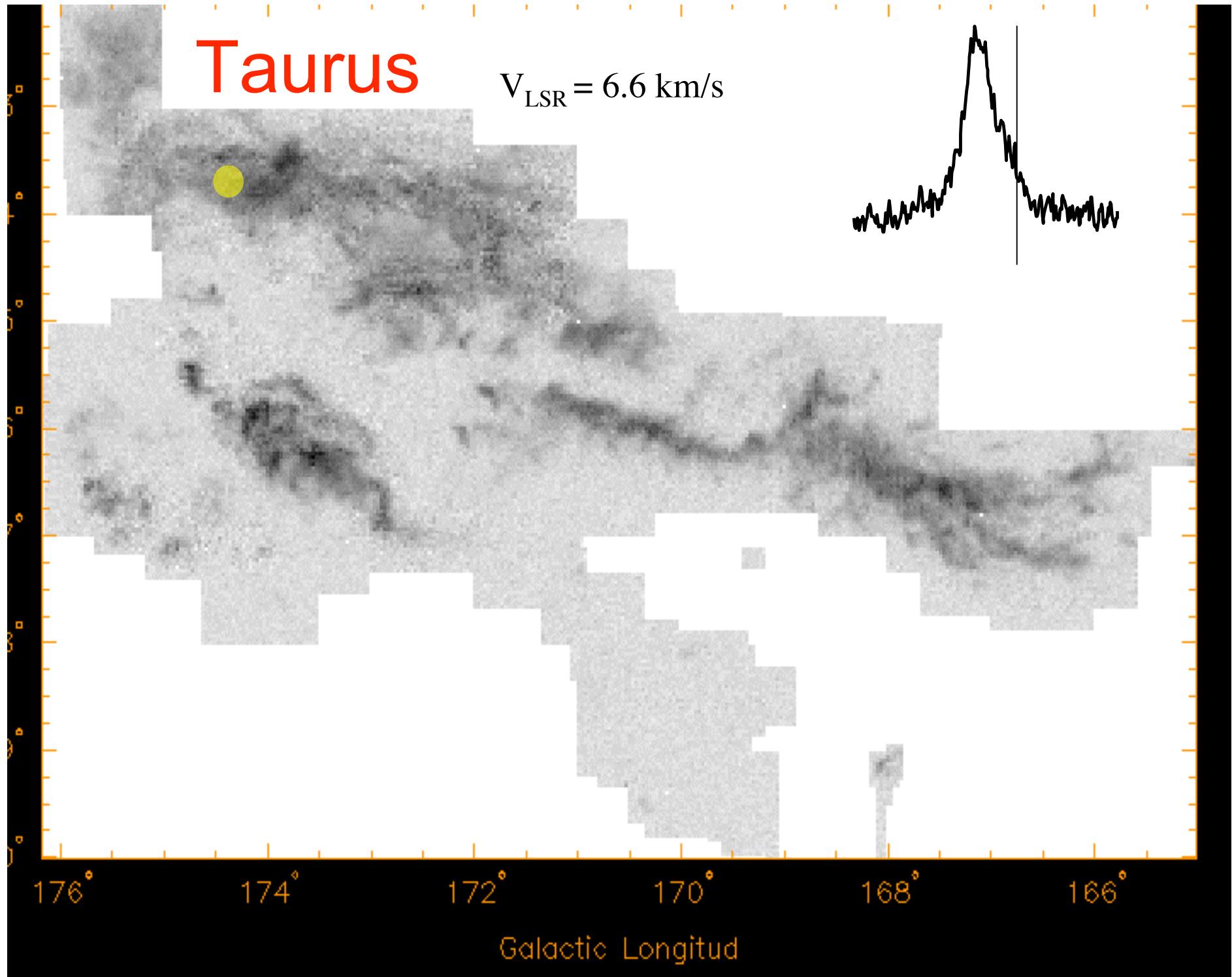
Taurus

$$V_{\text{LSR}} = 5.0 \text{ km/s}$$



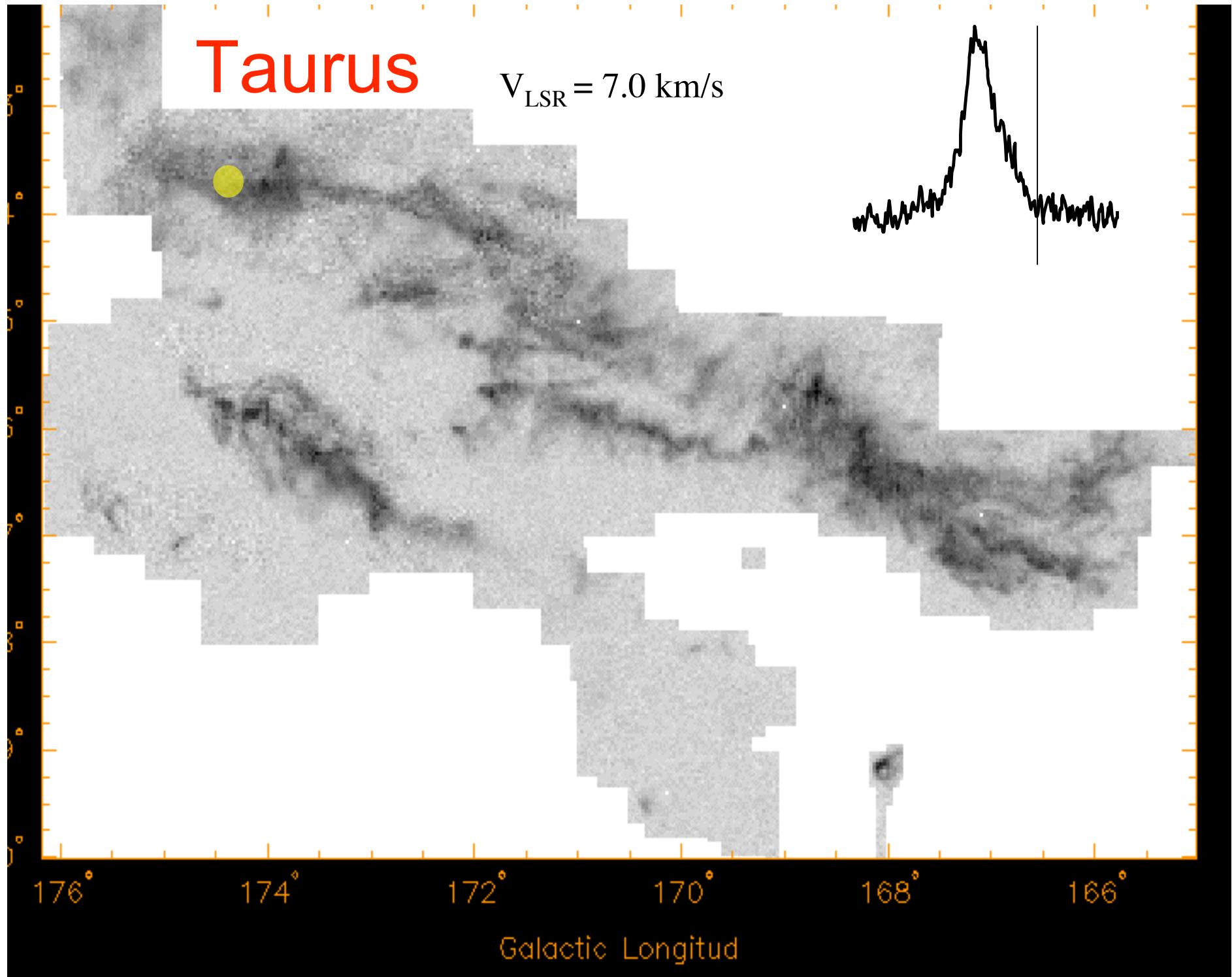






Taurus

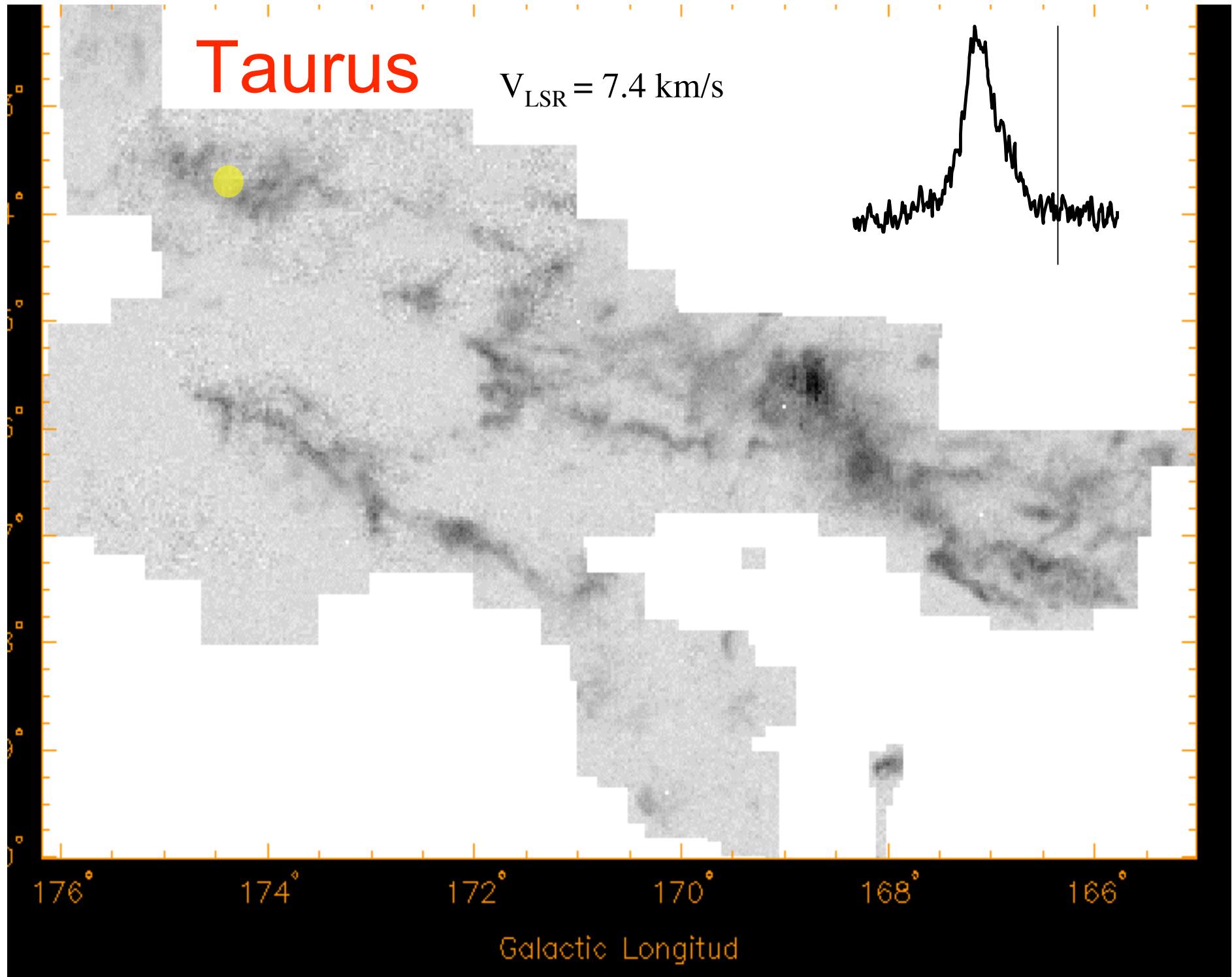
$V_{\text{LSR}} = 6.6 \text{ km/s}$

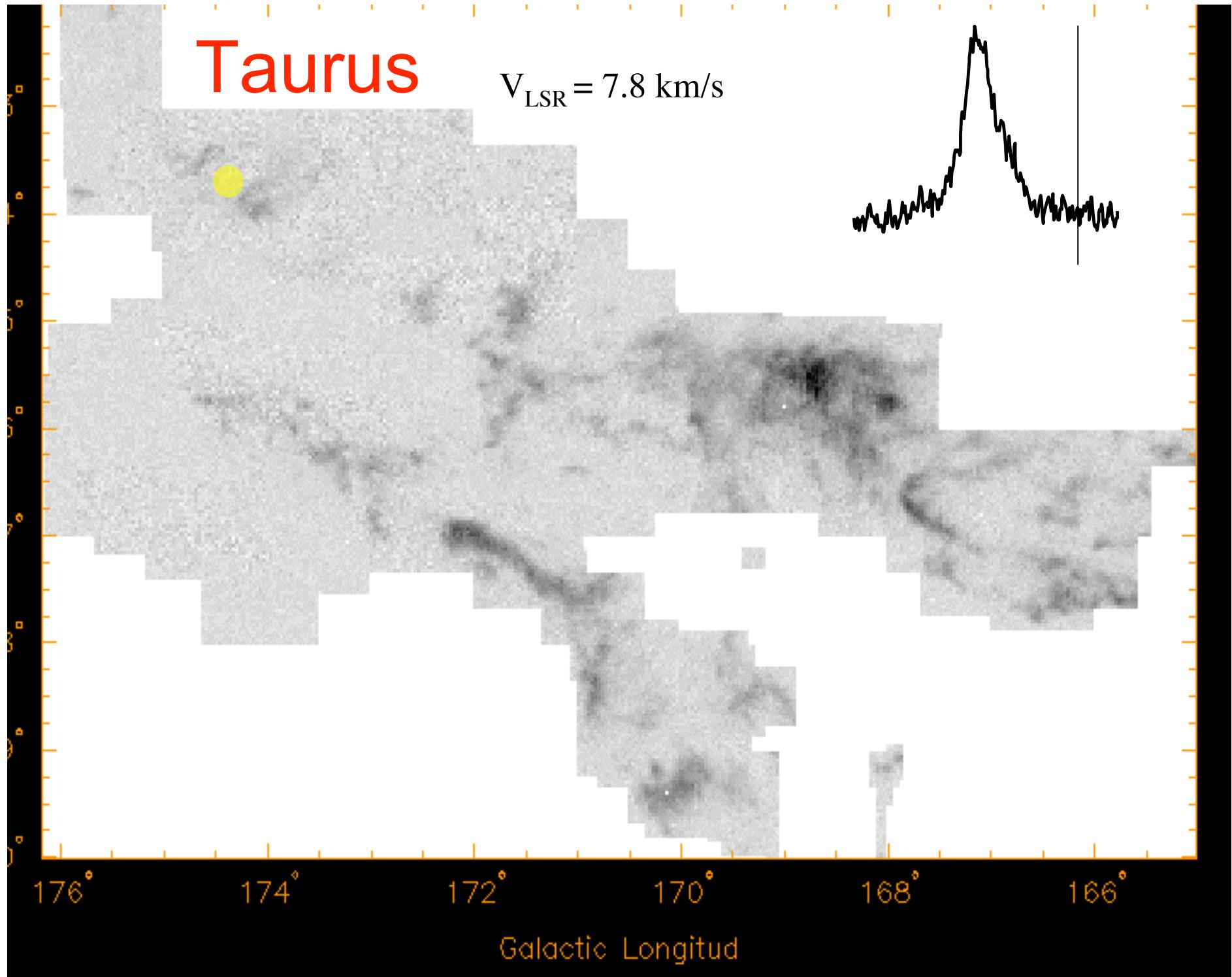


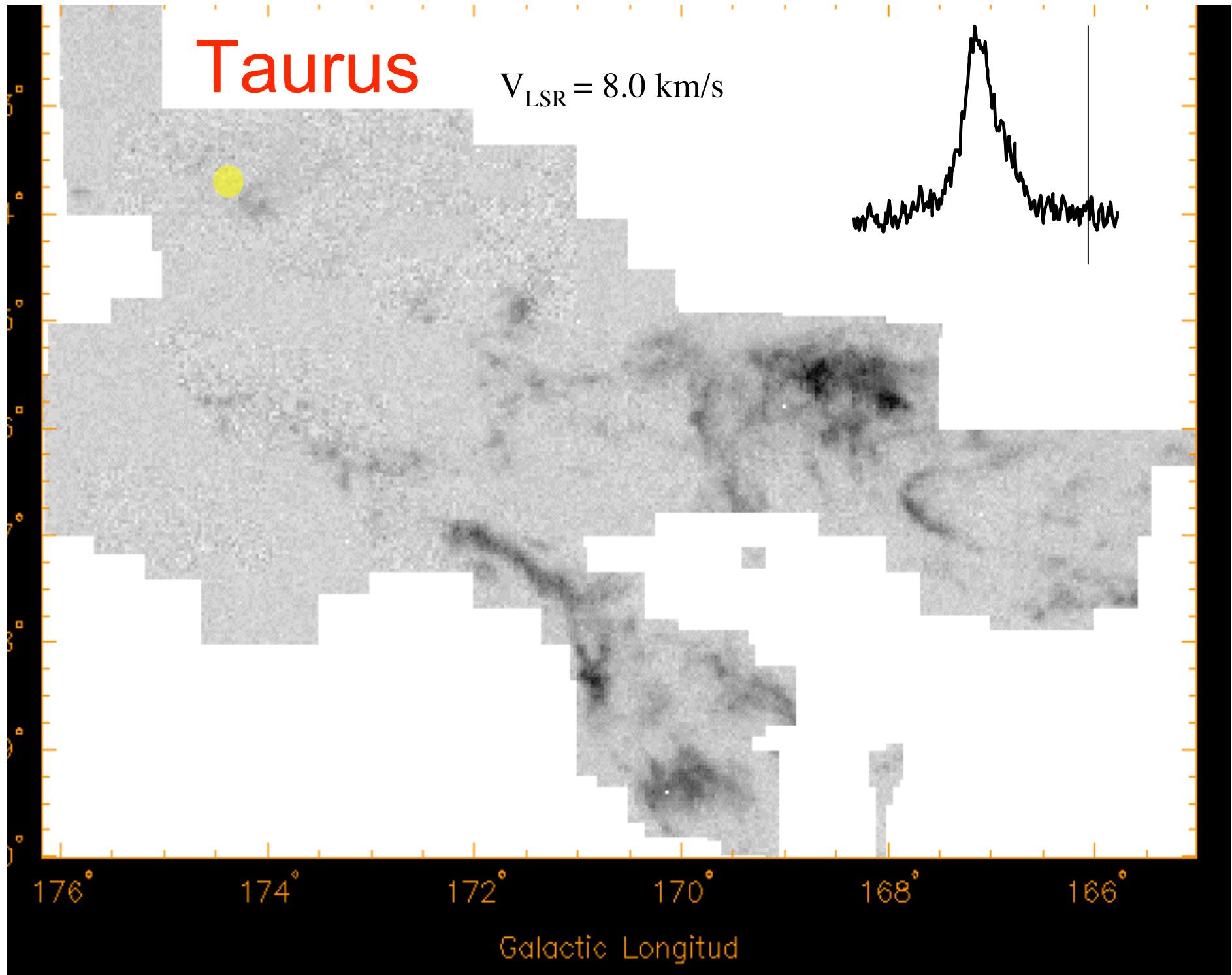
Taurus

$$V_{\text{LSR}} = 7.0 \text{ km/s}$$

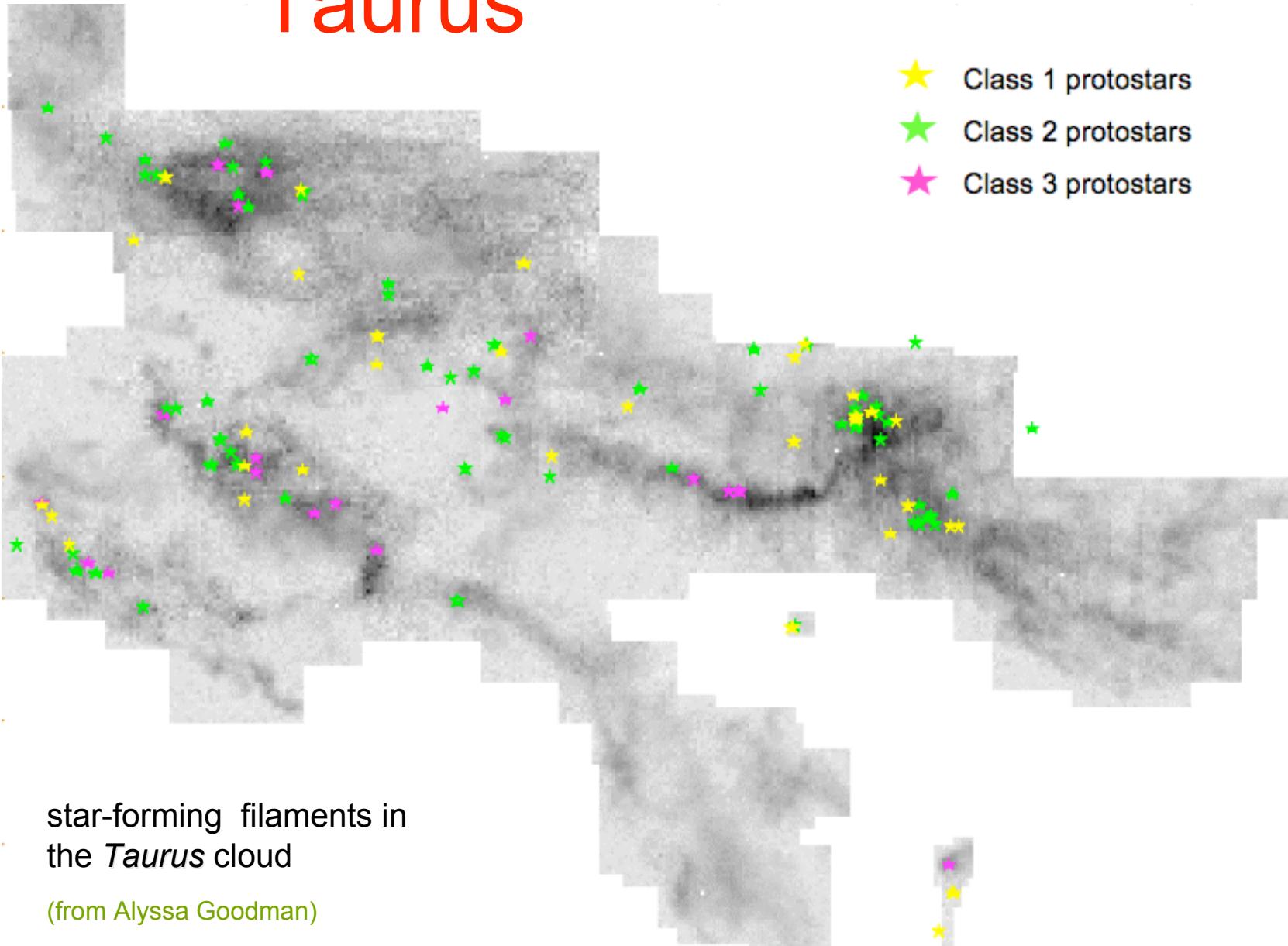
Galactic Longitud



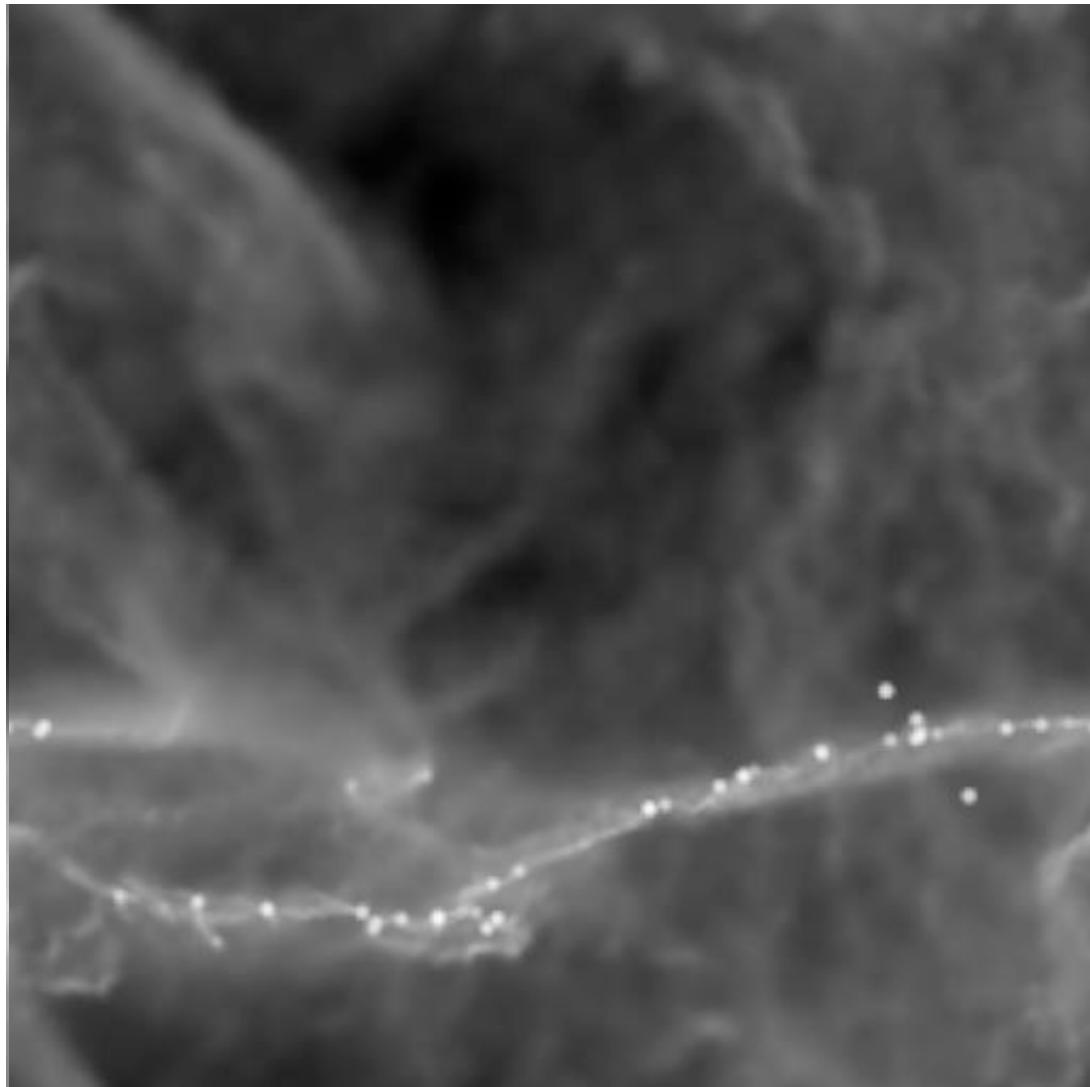




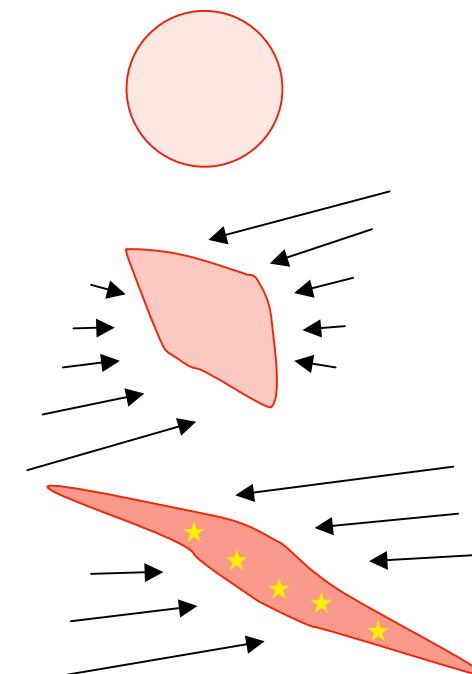
Taurus



Graviturbulent fragmentation



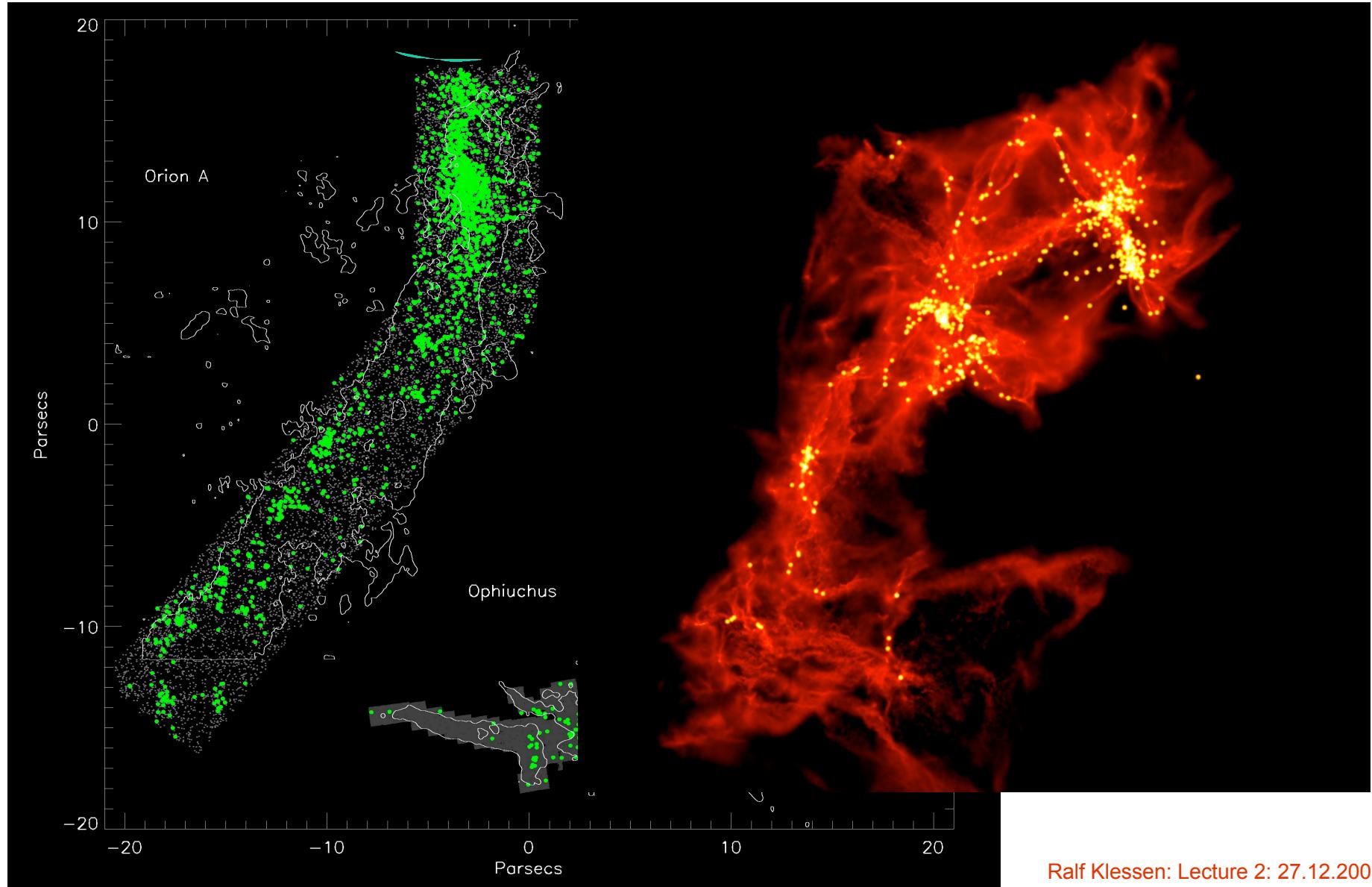
Filament generated by combination of compression and local shear:



“Taurus”:

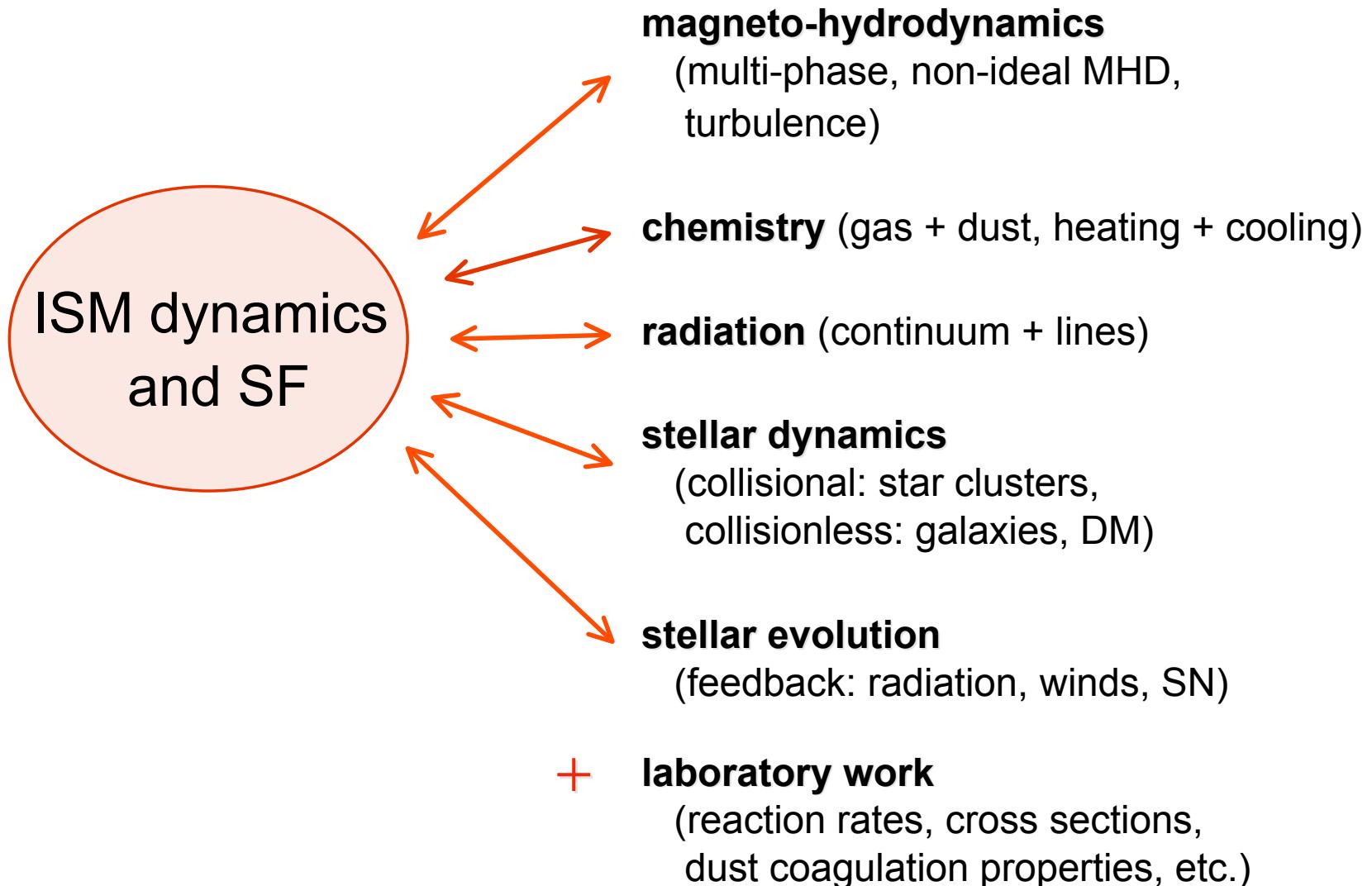
- density $n(H_2) \approx 10^2 \text{ cm}^{-3}$
- $L = 6 \text{ pc}$, $M = 5000 M_\odot$

Gravitational collapse within MCs



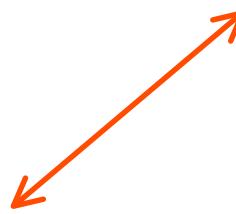
improvements

What do we need to study ISM?



What do we need to study ISM?

- massive parallel codes
- particle-based: SPH with improved algorithms (XSPH with turb. subgrid model, GPM, particle splitting, MHD-SPH?)
- grid-based: AMR (FLASH, ENZO, RAMSES, Nirvana3, etc), subgrid-scale models (FEARLESS)
- BGK methods



magneto-hydrodynamics

(multi-phase, non-ideal MHD, turbulence)

chemistry (gas + dust, heating + cooling)

radiation (continuum + lines)

stellar dynamics

(collisional: star clusters, collisionless: galaxies, DM)

stellar evolution

(feedback: radiation, winds, SN)

What do we need to study ISM?

- ever increasing chemical networks
- working reduced networks for time-dependent chemistry in combination with hydrodynamics
- improved data on reaction rates (laboratory + quantum mechanical calculations)



magneto-hydrodynamics

(multi-phase, non-ideal MHD, turbulence)

chemistry (gas + dust, heating + cooling)

radiation (continuum + lines)

stellar dynamics

(collisional: star clusters, collisionless: galaxies, DM)

stellar evolution

(feedback: radiation, winds, SN)

What do we need to study ISM?

- continuum vs. lines
- Monte Carlo,
characteristics
- approximative
methods
- combine with hydro



magneto-hydrodynamics

(multi-phase, non-ideal MHD,
turbulence)

chemistry (gas + dust, heating + cooling)

radiation (continuum + lines)

stellar dynamics

(collisional: star clusters,
collisionless: galaxies, DM)

stellar evolution

(feedback: radiation, winds, SN)

What do we need to study ISM?

- statistics: number of stars (collisional: 10^6 , collisionless: 10^{10})
- transition from gas to stars
- binary orbits
- long-term integration



magneto-hydrodynamics

(multi-phase, non-ideal MHD,
turbulence)

chemistry (gas + dust, heating + cooling)

radiation (continuum + lines)

stellar dynamics

(collisional: star clusters,
collisionless: galaxies, DM)

stellar evolution

(feedback: radiation, winds, SN)

What do we need to study ISM?

- very early phases (pre main sequence tracks)
- massive stars at late phases
- role of rotation
- primordial star formation

magneto-hydrodynamics

(multi-phase, non-ideal MHD,
turbulence)

chemistry (gas + dust, heating + cooling)

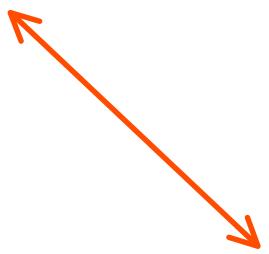
radiation (continuum + lines)

stellar dynamics

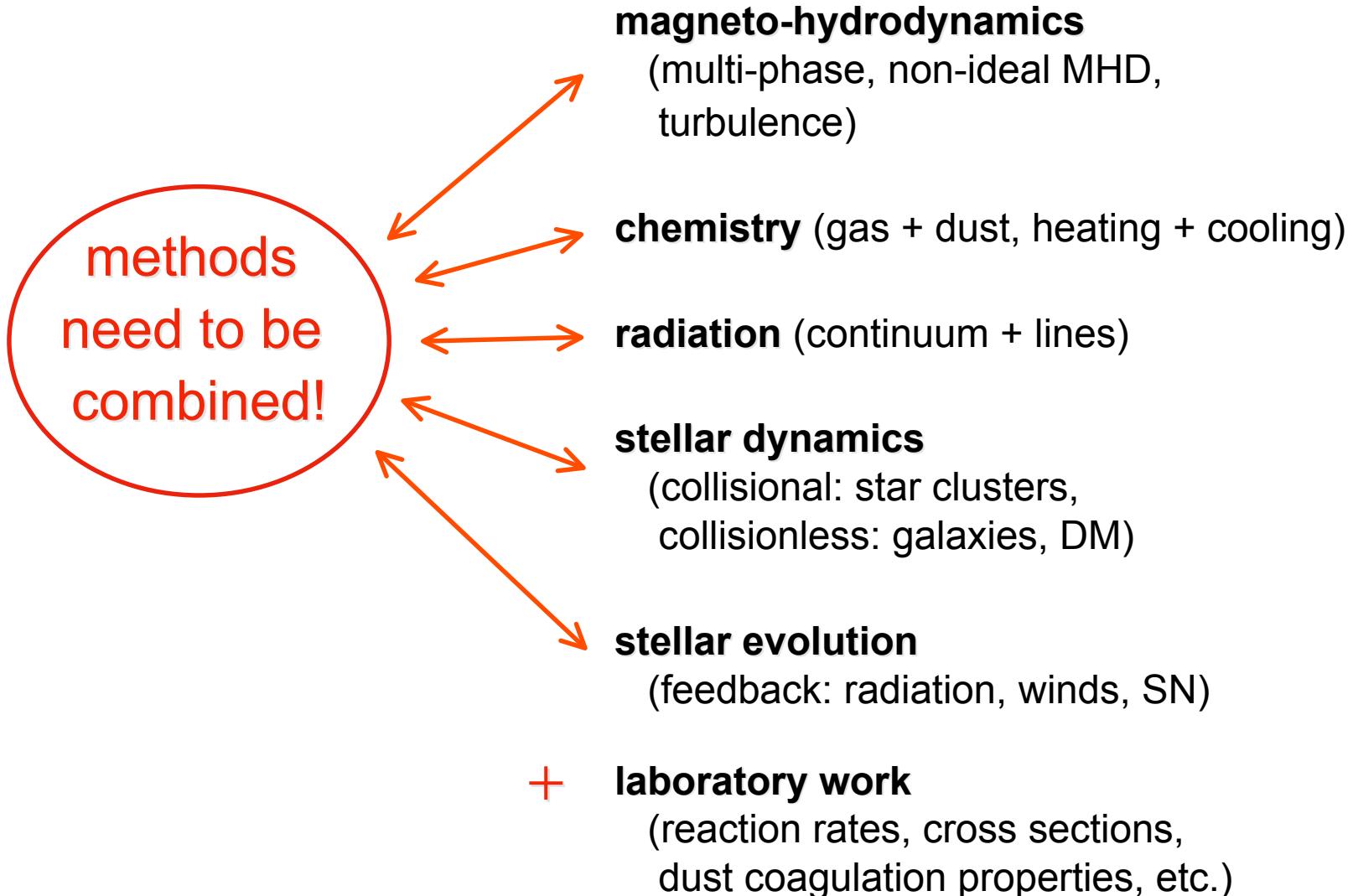
(collisional: star clusters,
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What do we need to study ISM?



Summary

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- interstellar gas is highly inhomogeneous
 - *thermal instability*
 - *gravitational instability*
 - *turbulent compression* (in shocks $\delta\rho/\rho \approx M^2$; in atomic gas: $M \approx 1\dots 3$)
- cold *molecular clouds* form rapidly in high-density regions
 - chemical *phase transition*: atomic \rightarrow molecular
 - process is *modulated* by large-scale *dynamics* in the galaxy
- inside *cold clouds*: turbulence is highly supersonic ($M \approx 1\dots 20$)
→ *turbulence* creates density structure, *gravity* selects for collapse

GRAVOTUBULENT FRAGMENTATION
- *turbulent cascade*: local compression *within* a cloud provokes collapse
- individual *stars* and *star clusters* form through *sequence* of highly *stochastic* events:
 - *collapse* of cloud cores in turbulent cloud (cores change during collapse)
 - plus mutual *interaction* during collapse (importance depends on ratio of potential energy to turbulent energy) (buzz word: *competitive accretion*)

Thanks!