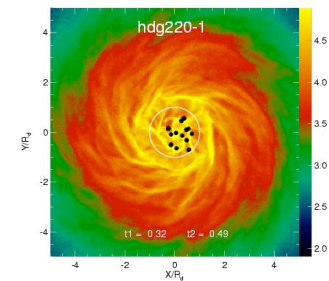
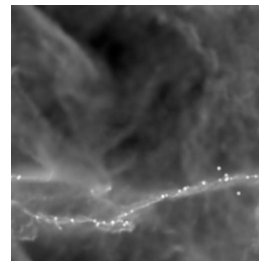
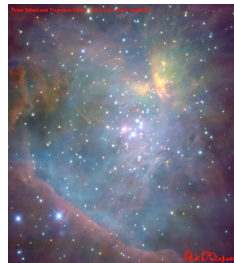
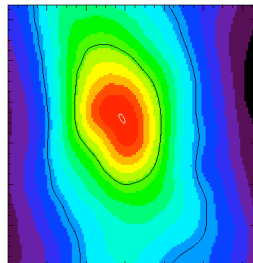
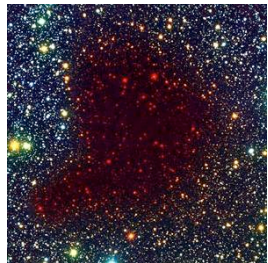


# star formation in disk galaxies



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Institut für Theoretische Astrophysik



en  
Mac Low  
Mac Low



# agenda

- phenomenology
  - stars
  - gas
- interplay between gravity and turbulence
- examples and predictions
  - transient cloud structure
  - stellar initial mass function

stars

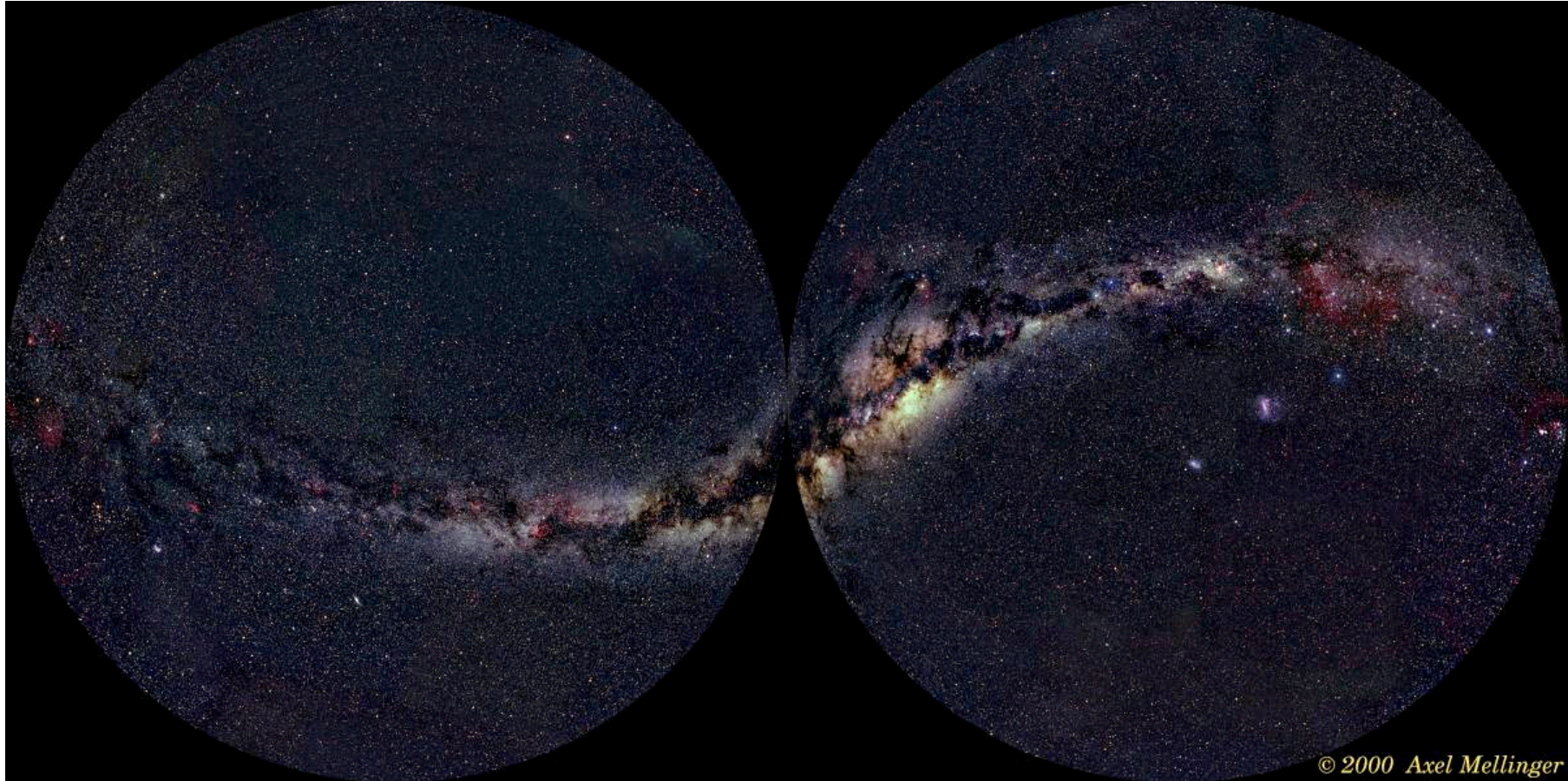
# young stars in spiral galaxies



(NGC 4622 from the Hubble Heritage Team)

- Star formation *always* is associated with *clouds of gas and dust*.
- Star formation is essentially a *local phenomenon* (on  $\sim$ pc scale)
- **HOW** is star formation is *influenced* by *global* properties of the galaxy?

# young stars in the Milky Way

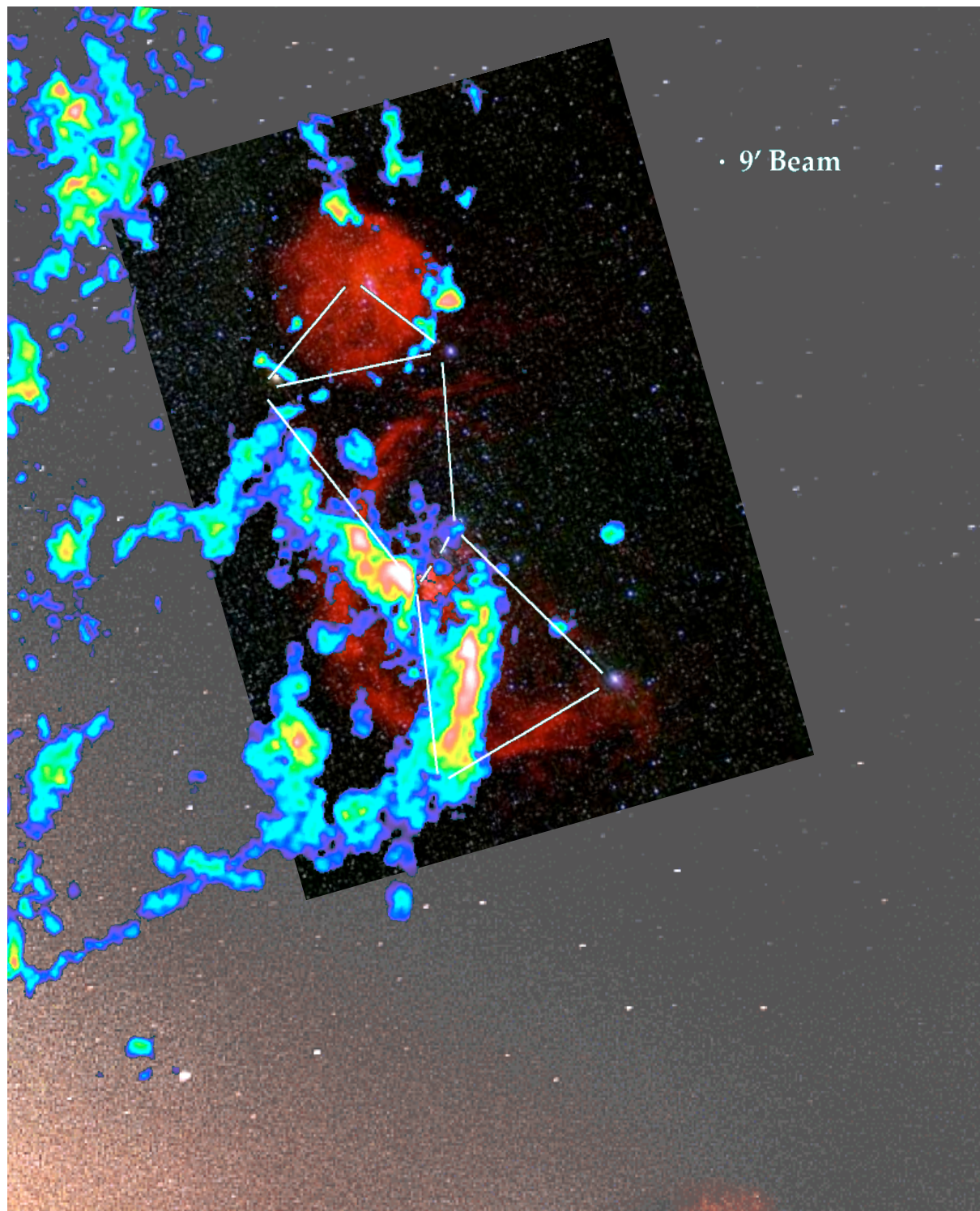


On the night sky, you see **stars** and **dark clouds**:

The brightest stars are massive and therefore young.

→ Star formation is important for understanding the structure of our Galaxy

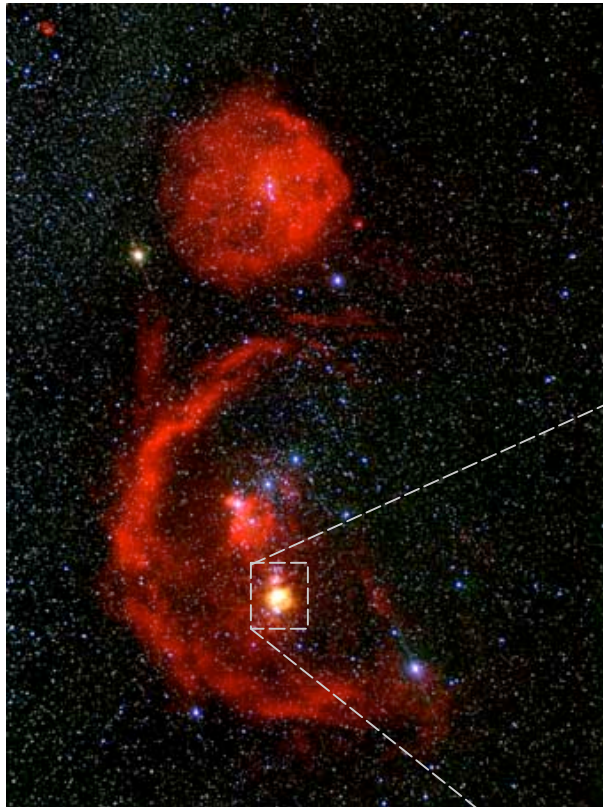
# star formation in Orion



We see

- *Stars* (in visible light)
- Atomic hydrogen (in  $H\alpha$  -- red)
- Molecular hydrogen  $H_2$  (radio emission -- color coded)

# local star forming region: ONC - Orion nebula cluster



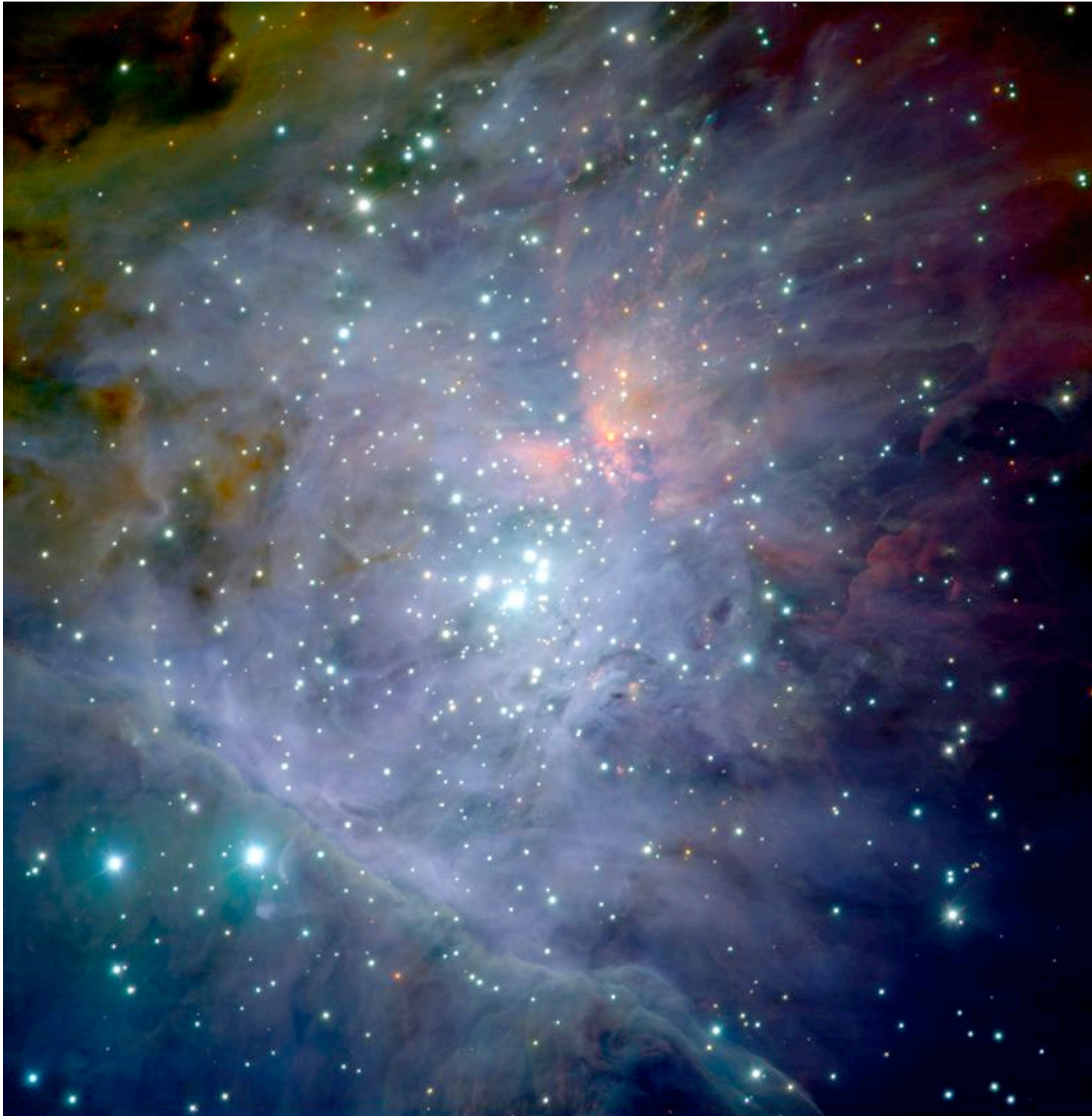
Orion molecular cloud

The Orion molecular cloud is the birth- place of several young embedded star clusters.

The Trapezium cluster is only visible in the IR and contains about 2000 newly born stars.



Trapezium cluster



## ONC (detail)

- stars form in **clusters**
- stars form in **molecular clouds**
- (proto)stellar **feedback** is important

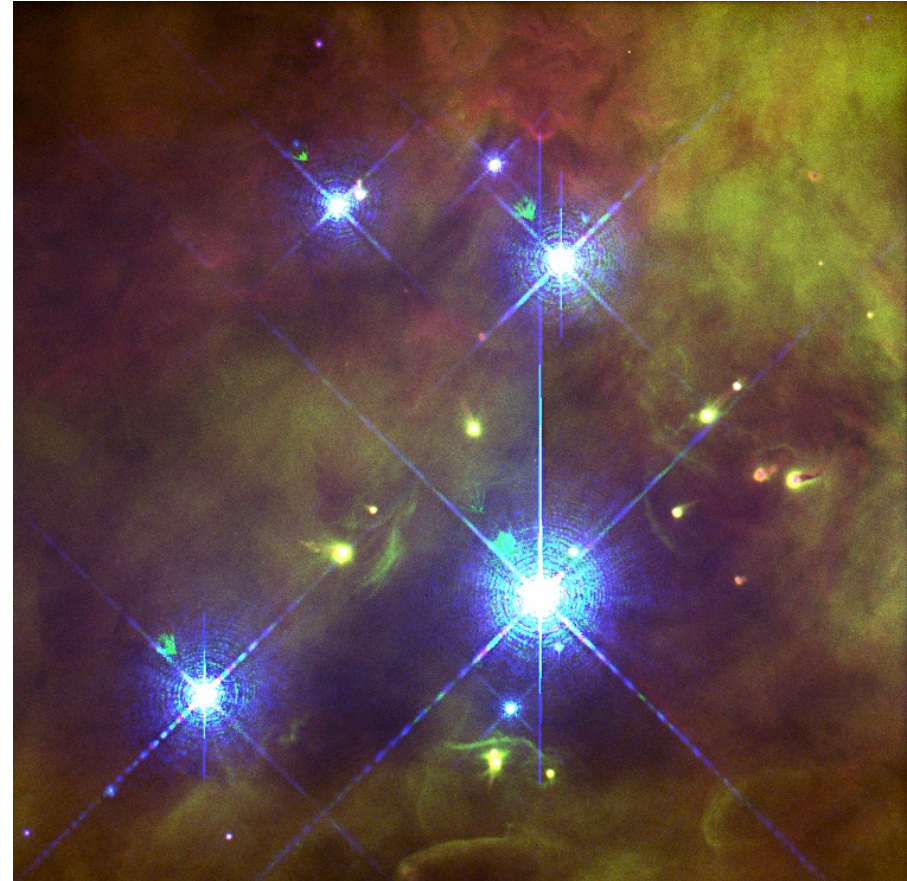
(color composite J,H,K  
by M. McCaughrean,  
VLT, Paranal, Chile)



# center of ONC: the trapezium



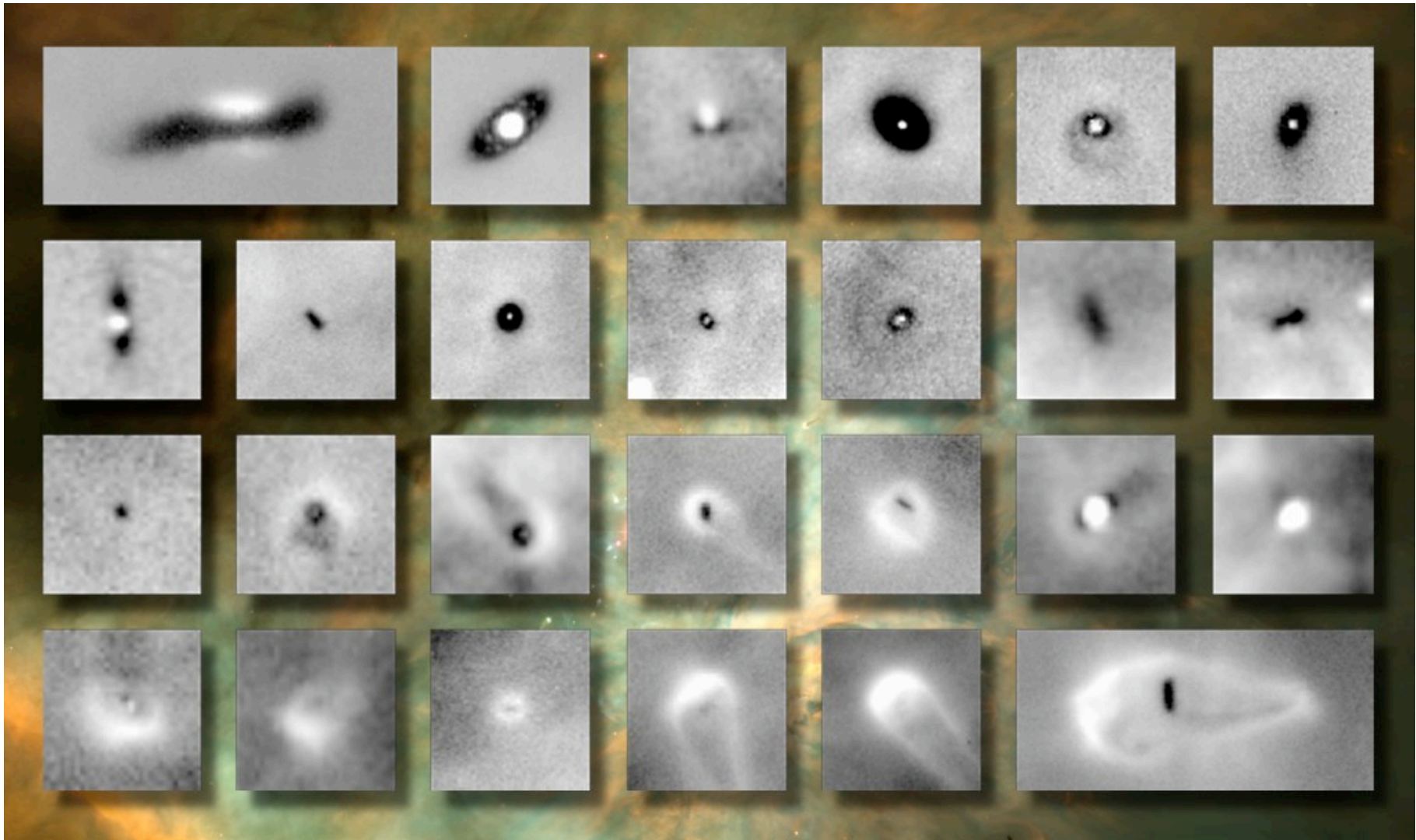
Ionizing radiation from central star  
**Θ1C Orionis**



**Proplyds:** Evaporating ``protoplanetary`` disks  
around young low-mass protostars

(images: Doug Johnstone et al.)

# silhouette disks in Orion



protostellar disks: dark shades in front of the photodissociation region in the background. Each image is 750 AU x 750 AU.

(data: Mark McCaughrean)

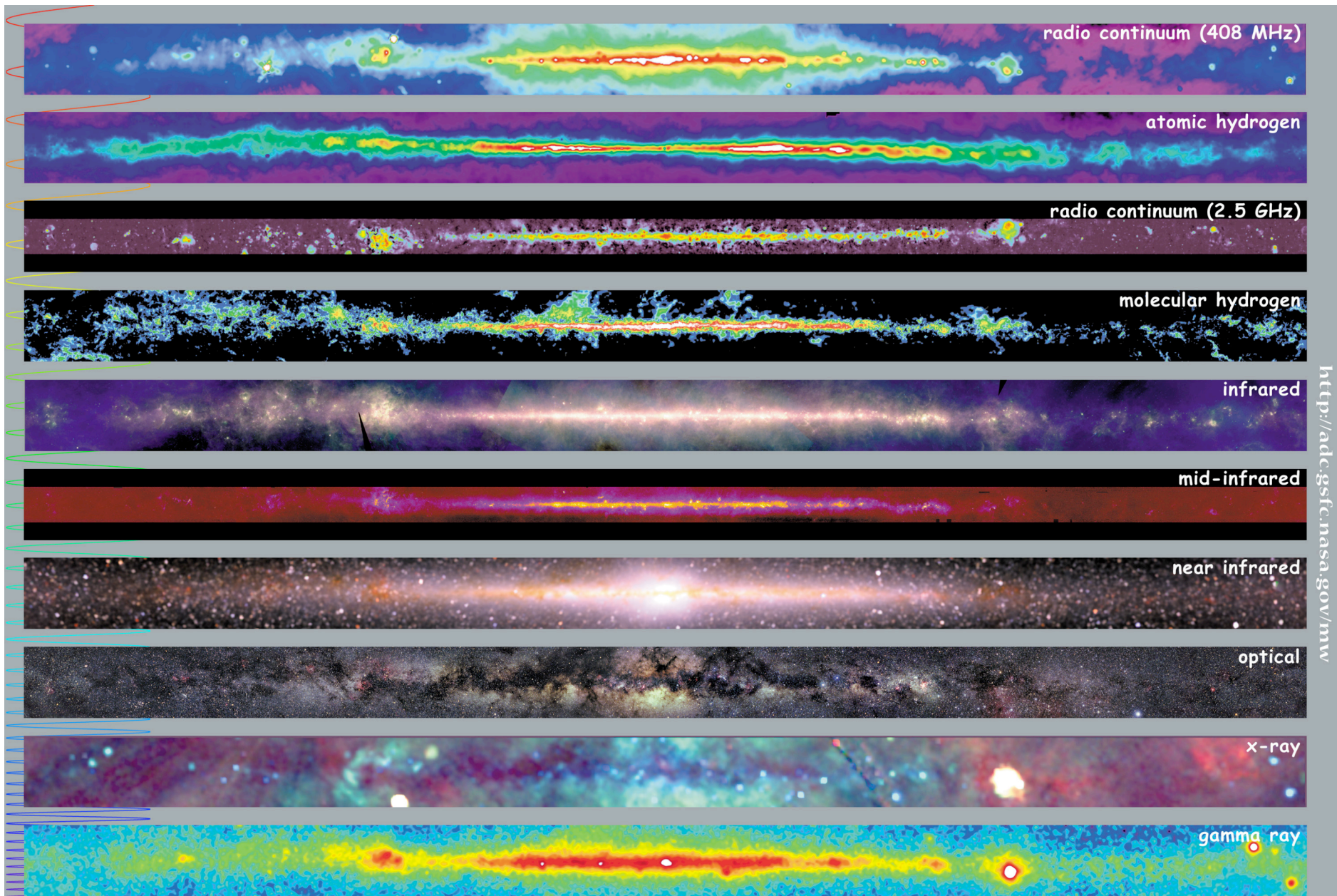
gas

# how to observe star forming clouds?

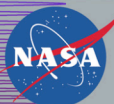
Different wavelength give different information.

→astronomer use the full electromagnetic spectrum

- **Radio:** interstellar gas  
(line emission -> velocity information)
- **sub-mm range:** dust (thermal emission)
- **infrared & optical:** stars
- **x-rays:** stars (coronae), supernovae remnants (very hot gas)
- **γ-rays:** supernovae remnants (radioactive decay, e.g.  $^{26}\text{Al}$ ), compact objects, merging of neutron stars (γ-ray burst)



<http://adc.gsfc.nasa.gov/mw>



# Multiwavelength Milky Way

# interstellar matter: ISM

Abundances, scaled to 1.000.000 H atoms

element atomic number abundance

Wasserstoff	H	1	1.000.000
Deuterium	${}_1\text{H}^2$	1	16
Helium	He	2	68.000
Kohlenstoff	C	6	420
Stickstoff	N	7	90
Sauerstoff	O	8	700
Neon	Ne	10	100
Natrium	Na	11	2
Magnesium	Mg	12	40
Aluminium	Al	13	3
Silicium	Si	14	38
Schwefel	S	16	20
Calcium	Ca	20	2
Eisen	Fe	26	34
Nickel	Ni	28	2

Hydrogen is by far the most abundant element (more than 90% in number).

# phases of the ISM

Because hydrogen is the dominating element, the classification scheme is based on its chemical state:

*ionized atomic hydrogen*

$HII (H^+)$

*neutral atomic hydrogen*

$HI (H)$

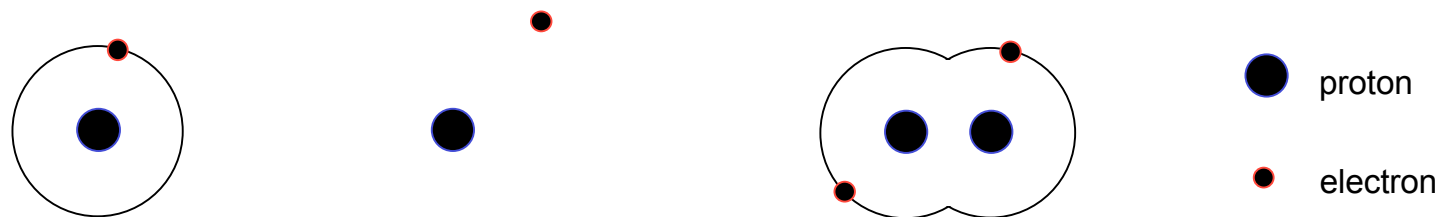
*molecular hydrogen*

$H_2$

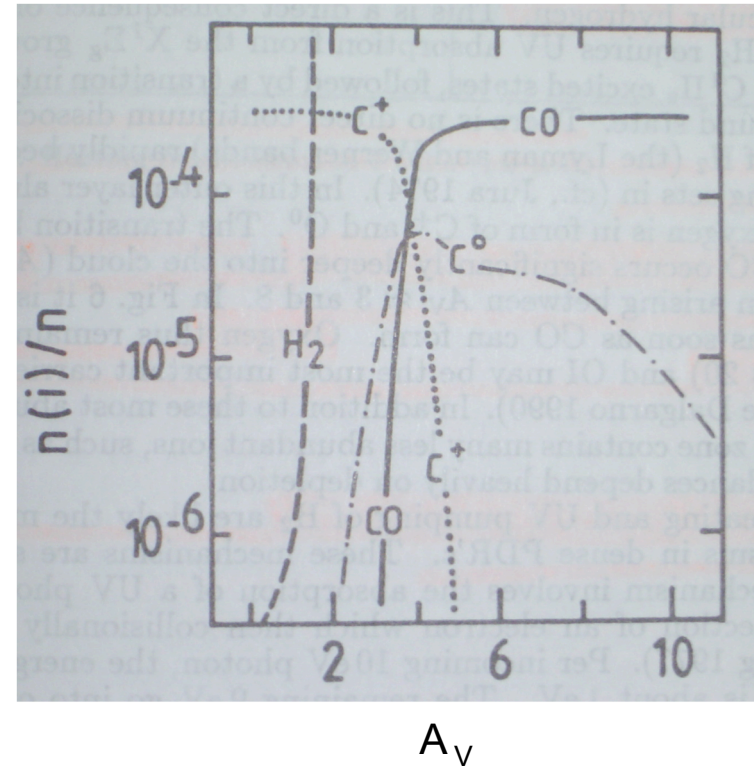
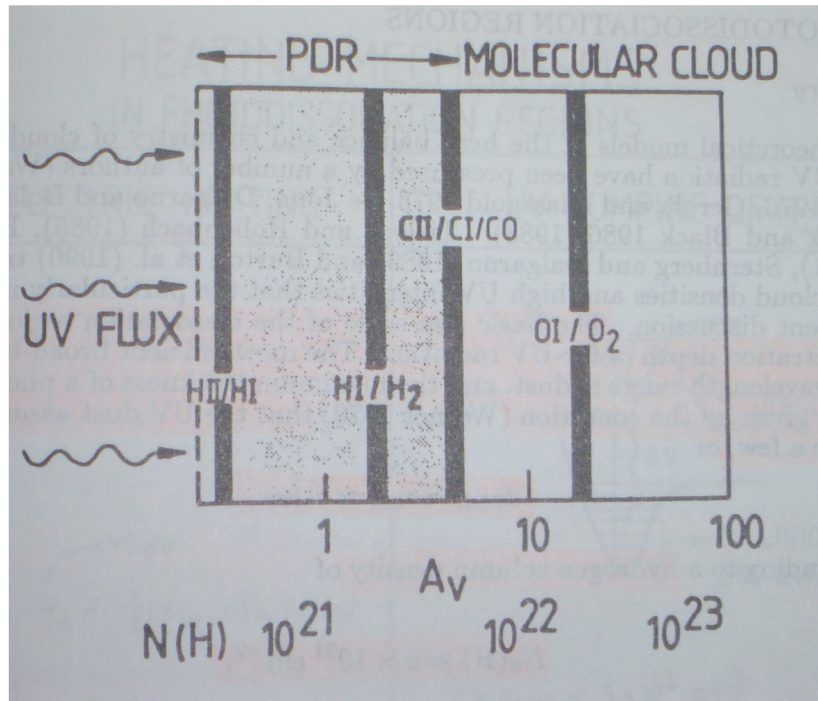
 Ionisation  
Phasenübergang

different regions consist of almost 100% of the appropriate phase, the transition regions between  $HII$ ,  $H$  and  $H_2$  are very thin.

star formation always takes place in dense and cold molecular clouds.



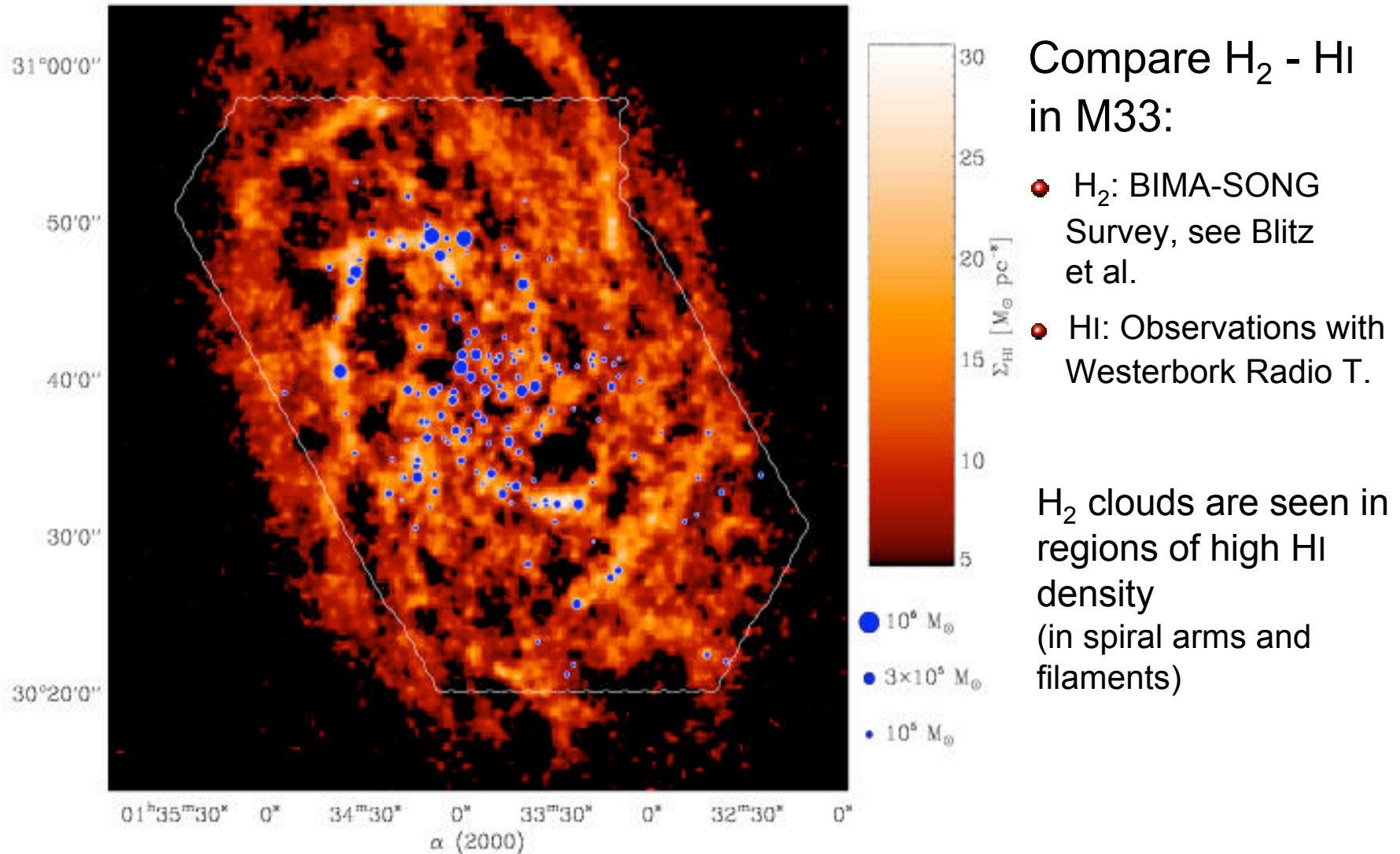
# phases of the ISM



$A_V$  bezeichnet die Extinktion, dh. die Abschwächung der einfallenden Strahlung.

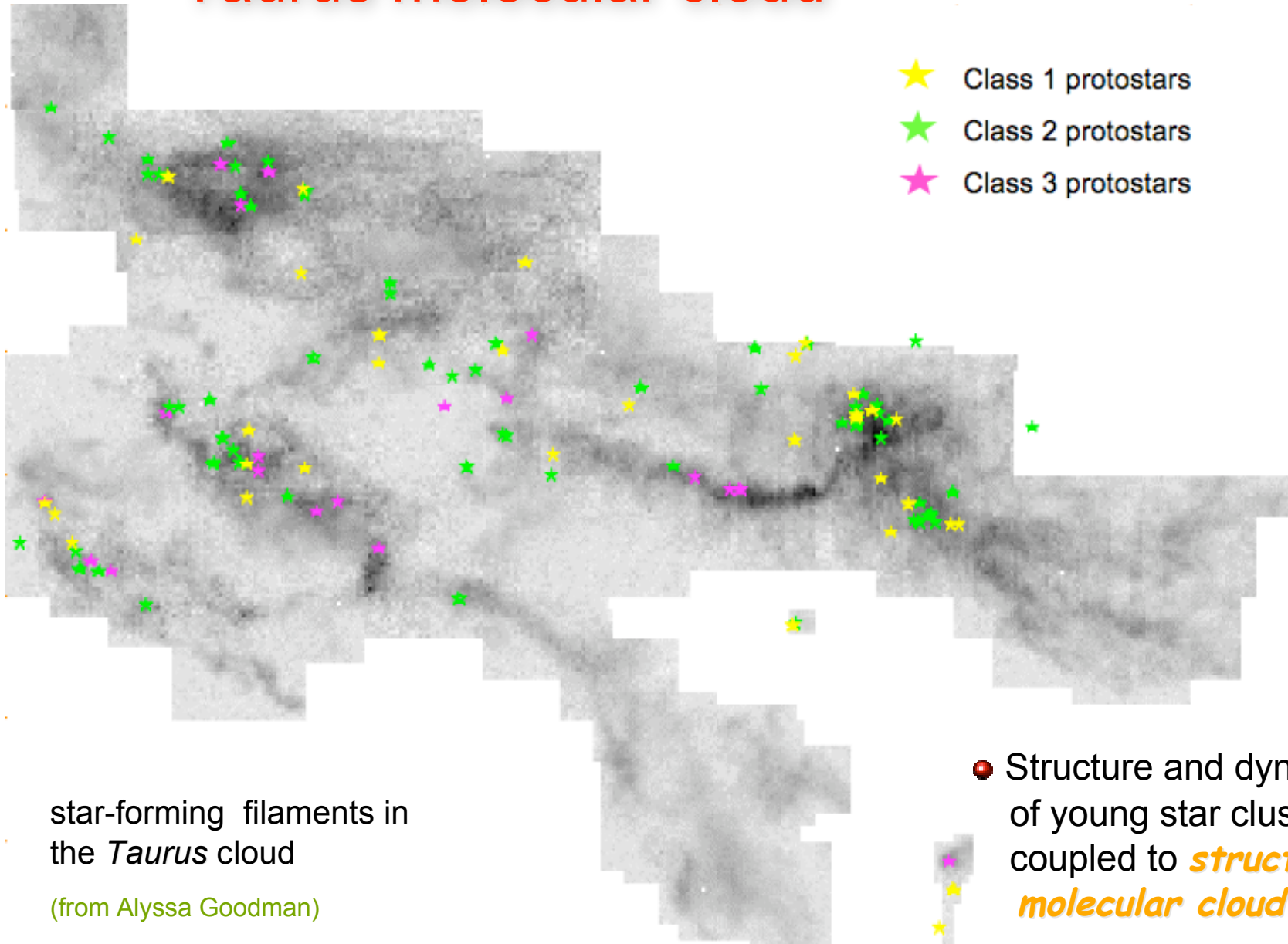


# correlation between H<sub>2</sub> and HI



(Deul & van der Hulst 1987, Blitz et al. 2004)

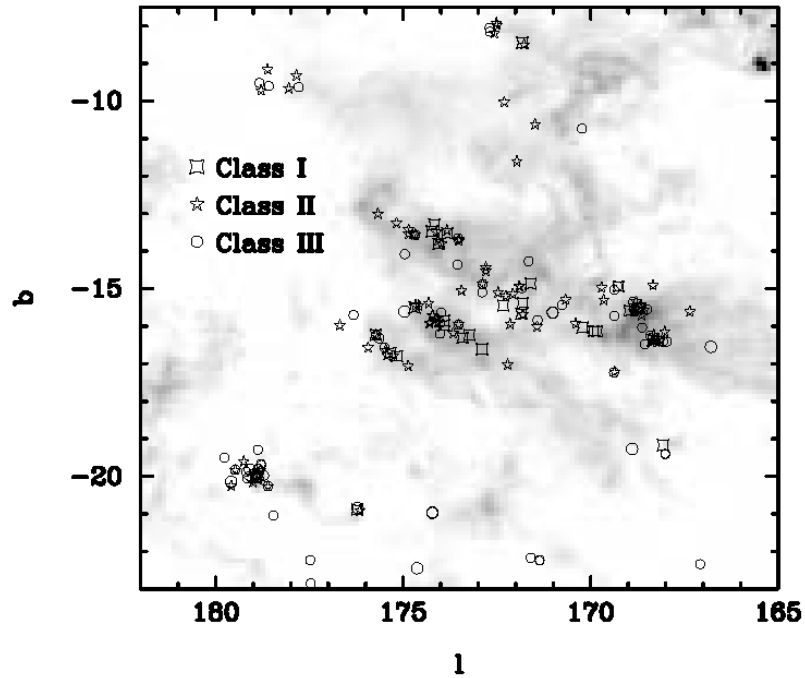
# Taurus molecular cloud



# Taurus molecular cloud

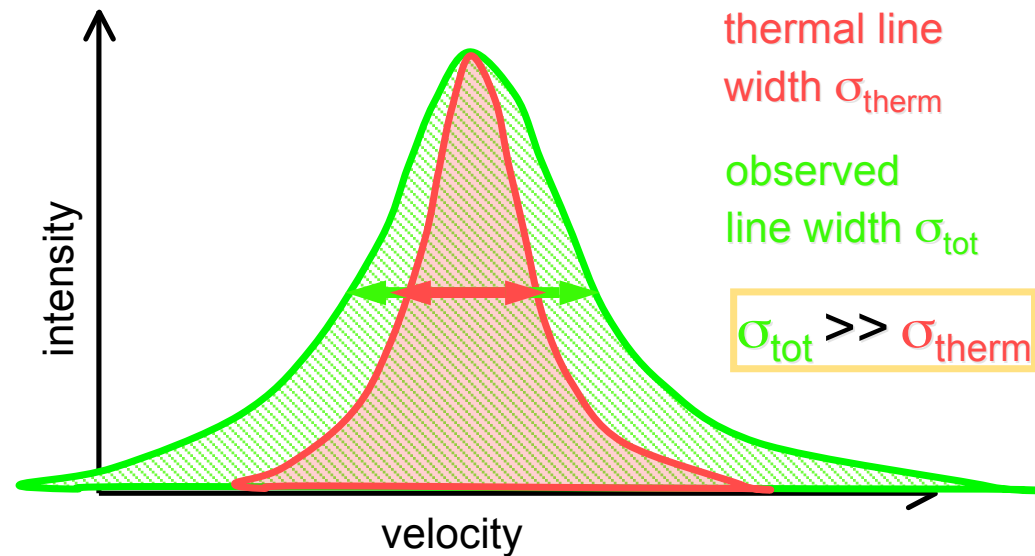
Star-forming filaments in *Taurus* cloud

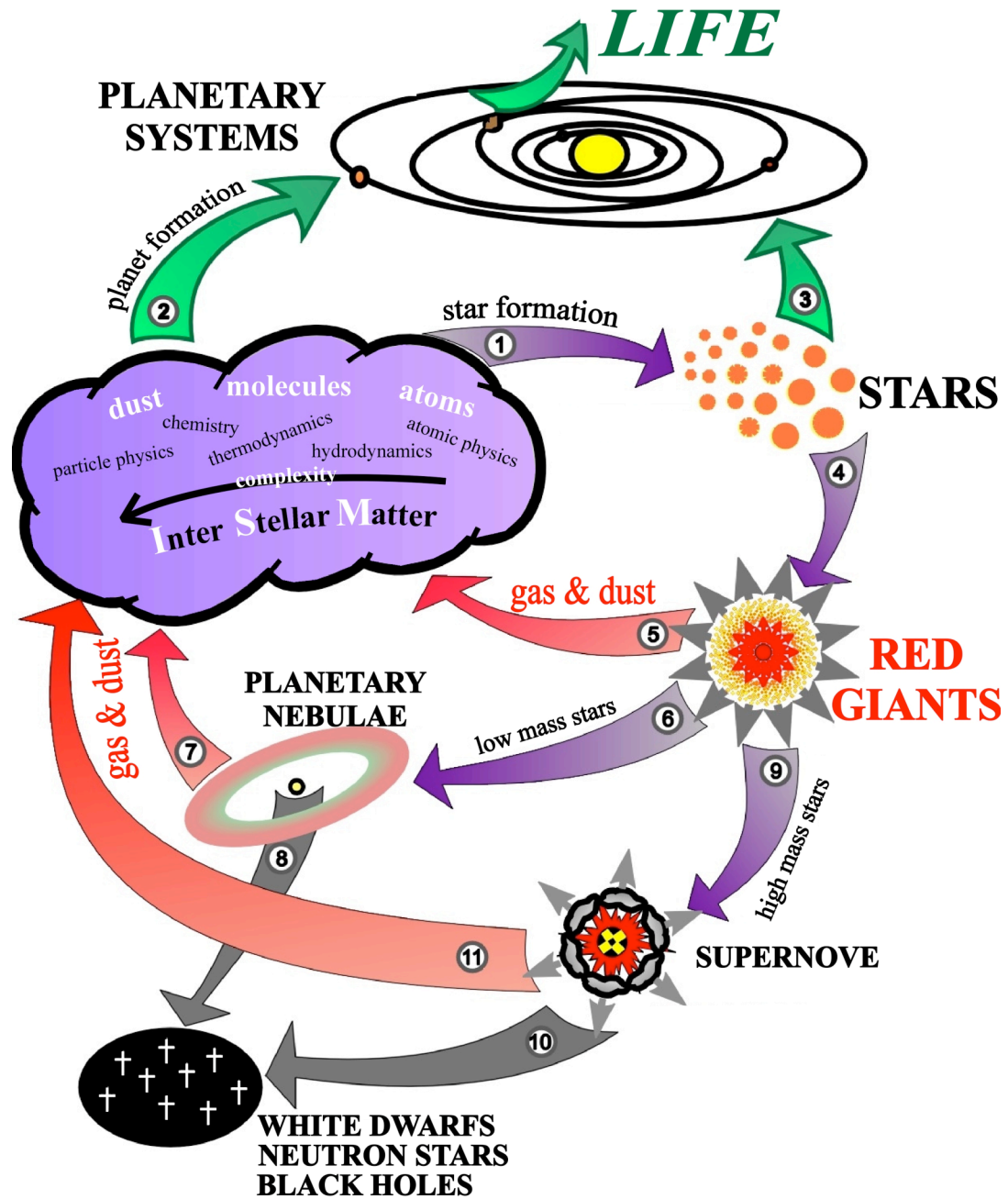
(from Hartmann 2002)

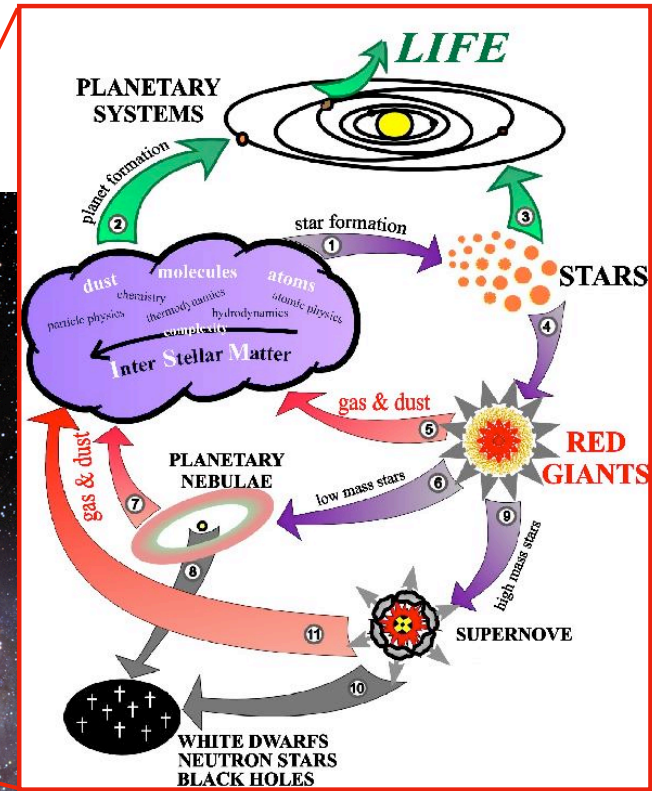
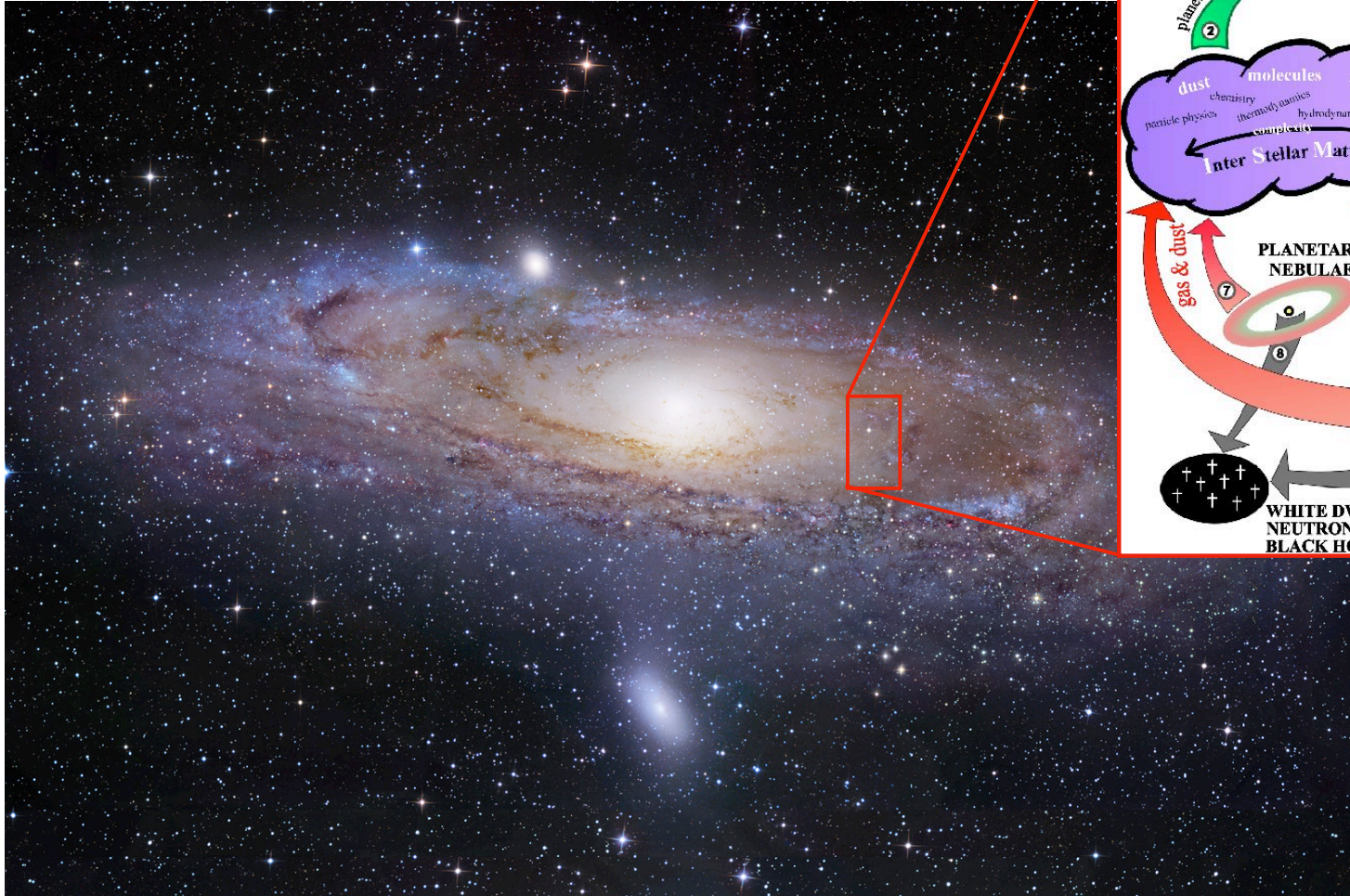


- Structure and dynamics of young star clusters is coupled to *structure of molecular cloud*

- Structure and dynamics of *molecular cloud* is determined by *supersonic turbulence*







idea

# gravoturbulent star formation

- idea:

*Star formation is controlled  
by interplay between  
gravity and  
supersonic turbulence!*

- dual role of turbulence:

- *stability on large scales*
- *initiating collapse on small scales*

(e.g., Larson, 2003, Rep. Prog. Phys, 66, 1651;  
or Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125)

# gravoturbulent star formation

- idea:

*Star formation is controlled  
by interplay between  
gravity and  
supersonic turbulence!*

- validity:

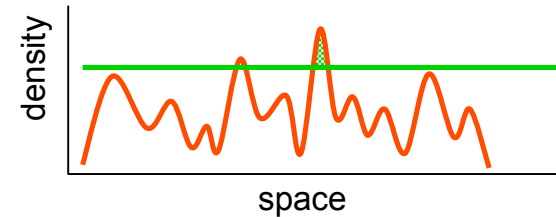
This hold on *all* scales and applies to build-up of stars and star clusters within molecular clouds as well as to the formation of molecular clouds in galactic disk.

(e.g., Larson, 2003, Rep. Prog. Phys, 66, 1651;  
or Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125)



# gravoturbulent star formation

- interstellar gas is highly *inhomogeneous*
  - *thermal instability*
  - *gravitational instability*
  - *turbulent compression* (in shocks  $\delta\rho/\rho \propto M^2$ ; in atomic gas:  $M \approx 1...3$ )
- cold *molecular clouds* can form rapidly in high-density regions at *stagnation points of convergent large-scale flows*
  - chemical *phase transition*: atomic  $\rightarrow$  molecular
  - process is *modulated* by large-scale *dynamics* in the galaxy
- inside *cold clouds*: turbulence is highly supersonic ( $M \approx 1...20$ )  
 $\rightarrow$  *turbulence* creates large density contrast,  
*gravity* selects for collapse

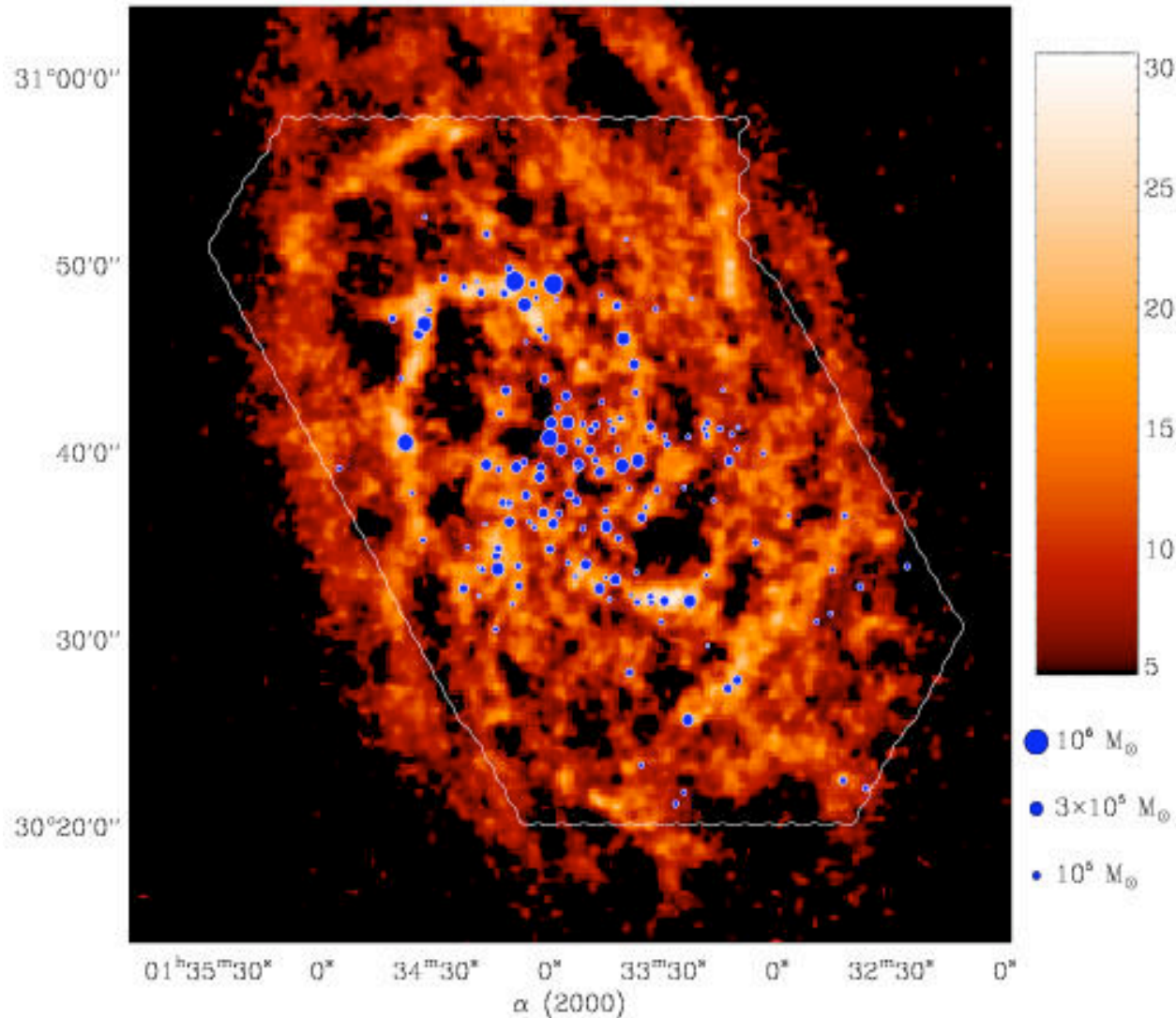


—————→ **GRAVOTUBULENT FRAGMENTATION**

- *turbulent cascade*: local compression *within* a cloud provokes collapse  $\rightarrow$  formation of individual *stars* and *star clusters*

# modeling large scales

# molecular cloud formation

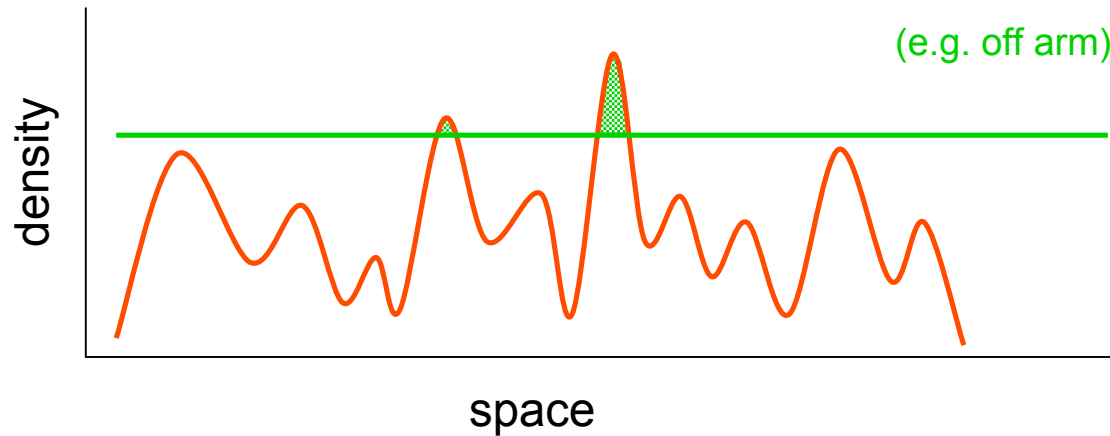


Thesis:

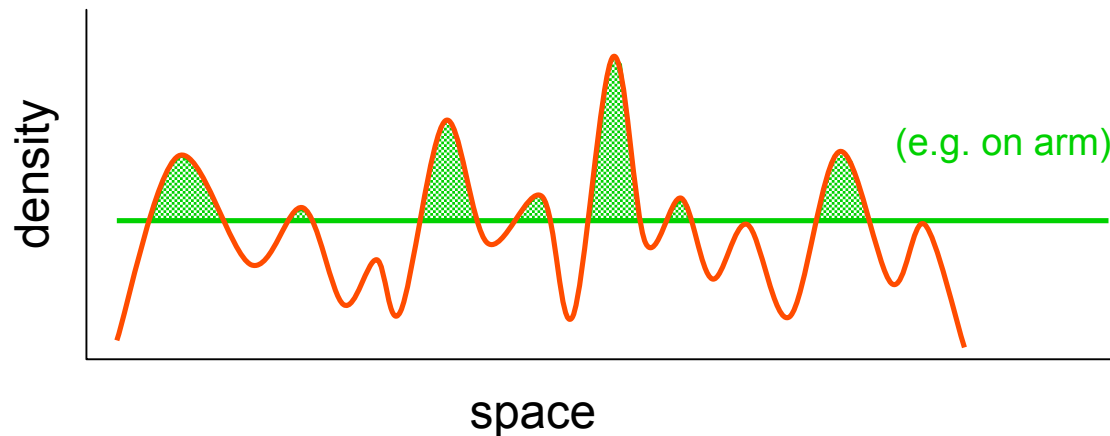
Molecular clouds form at *stagnation points* of large-scale convergent flows, mostly triggered by global (or external) perturbations.

(Deul & van der Hulst 1987, Blitz et al. 2004)

# correlation with large-scale perturbations



*density/temperature fluctuations* in warm atomic ISM are caused by *thermal/gravitational instability* and/or *supersonic turbulence*



some fluctuations are *dense* enough to *form  $H_2$*  within “*reasonable time*”

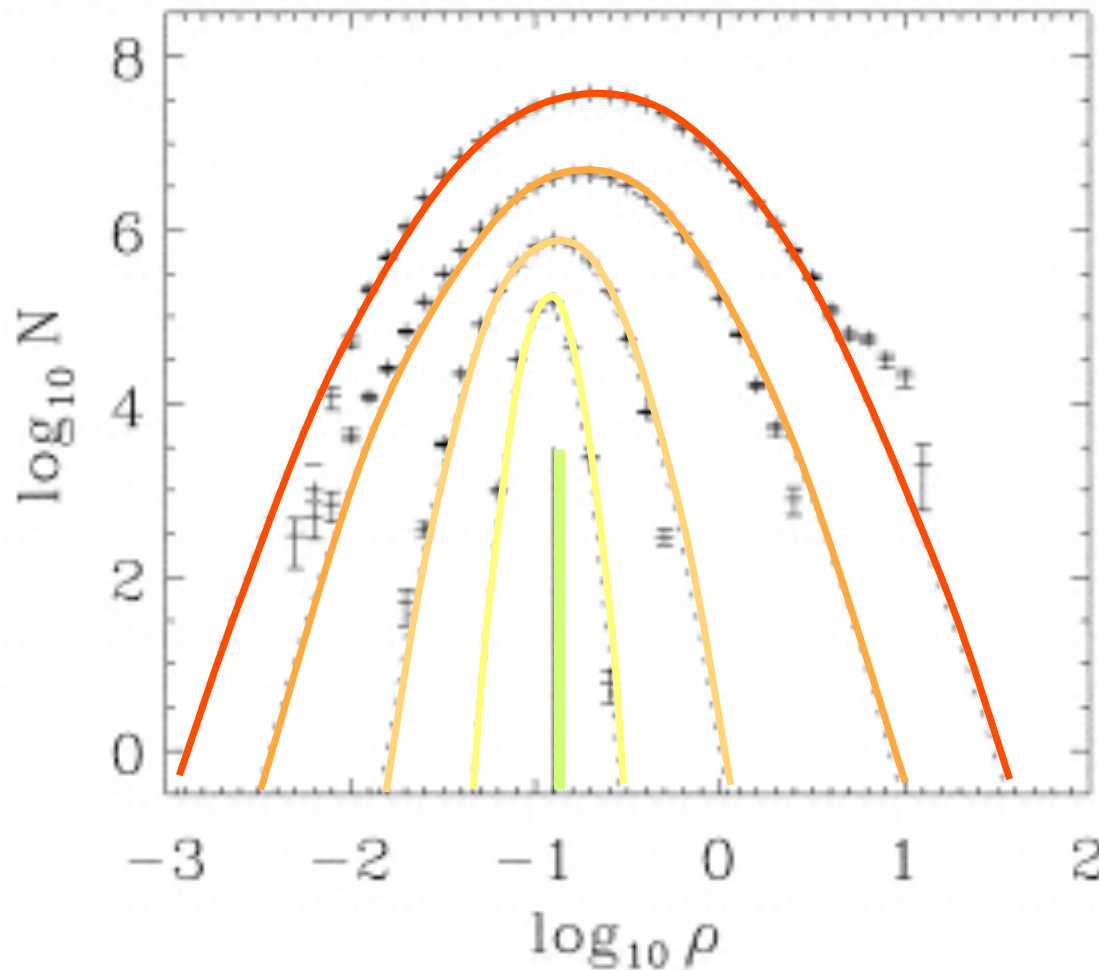
→ *molecular cloud*

(Glover & Mac Low 2007a,b)

*external perturbations* (i.e. potential changes) *increase* likelihood

(Dobbs & Bonnell 2006)

# star formation on *global* scales



probability distribution  
function of the density  
( $\rho$ -pdf)

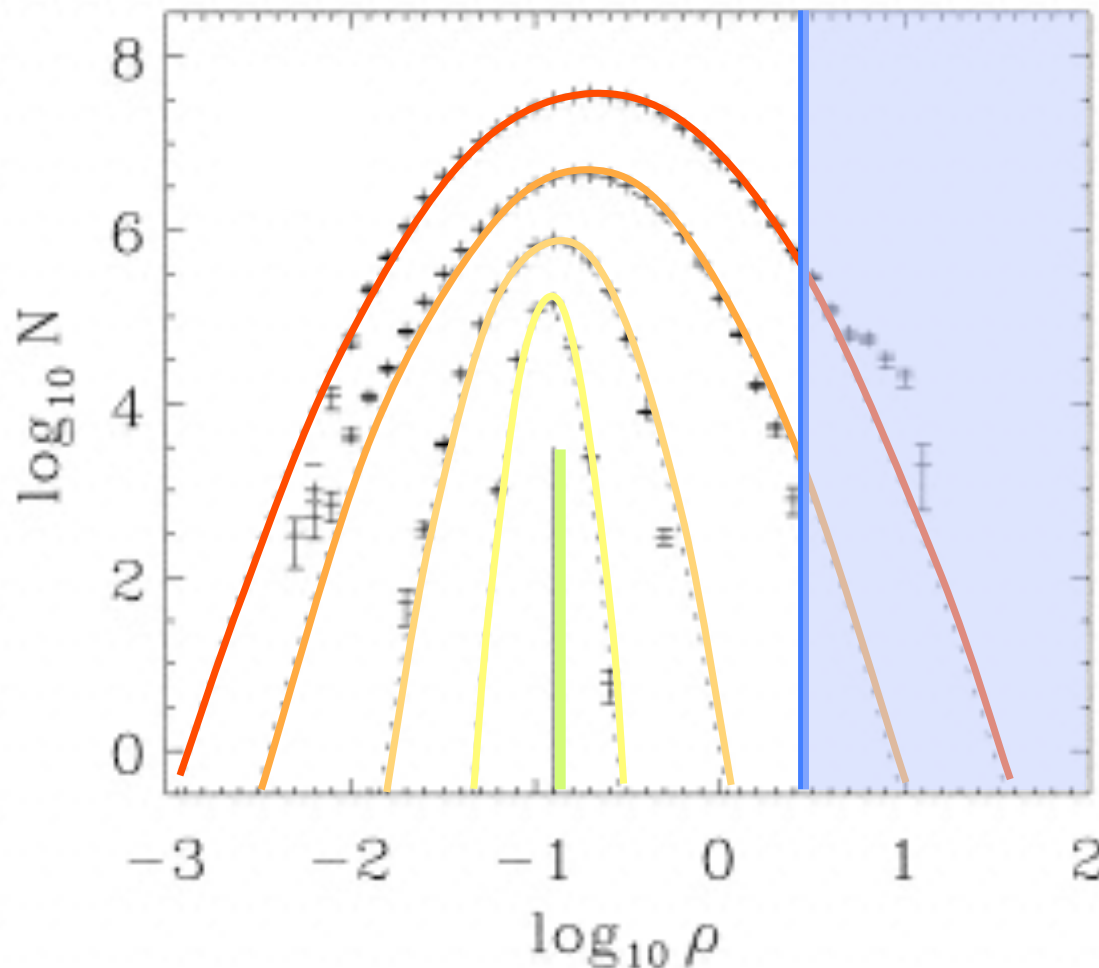
varying rms Mach  
numbers:

**M1** > **M2** >  
**M3** > **M4** > 0

mass weighted  $\rho$ -pdf, each shifted by  $\Delta \log N = 1$

(from Klessen, 2001; also Gazol et al. 2005, Mac Low et al. 2005)

# star formation on *global* scales



mass weighted  $\rho$ -pdf, each shifted by  $\Delta \log N = 1$

(rate from Hollenback, Werner, & Salpeter 1971)

H<sub>2</sub> formation rate:

$$\tau_{\text{H}_2} \approx \frac{1.5 \text{ Gyr}}{n_{\text{H}} / 1 \text{ cm}^{-3}}$$

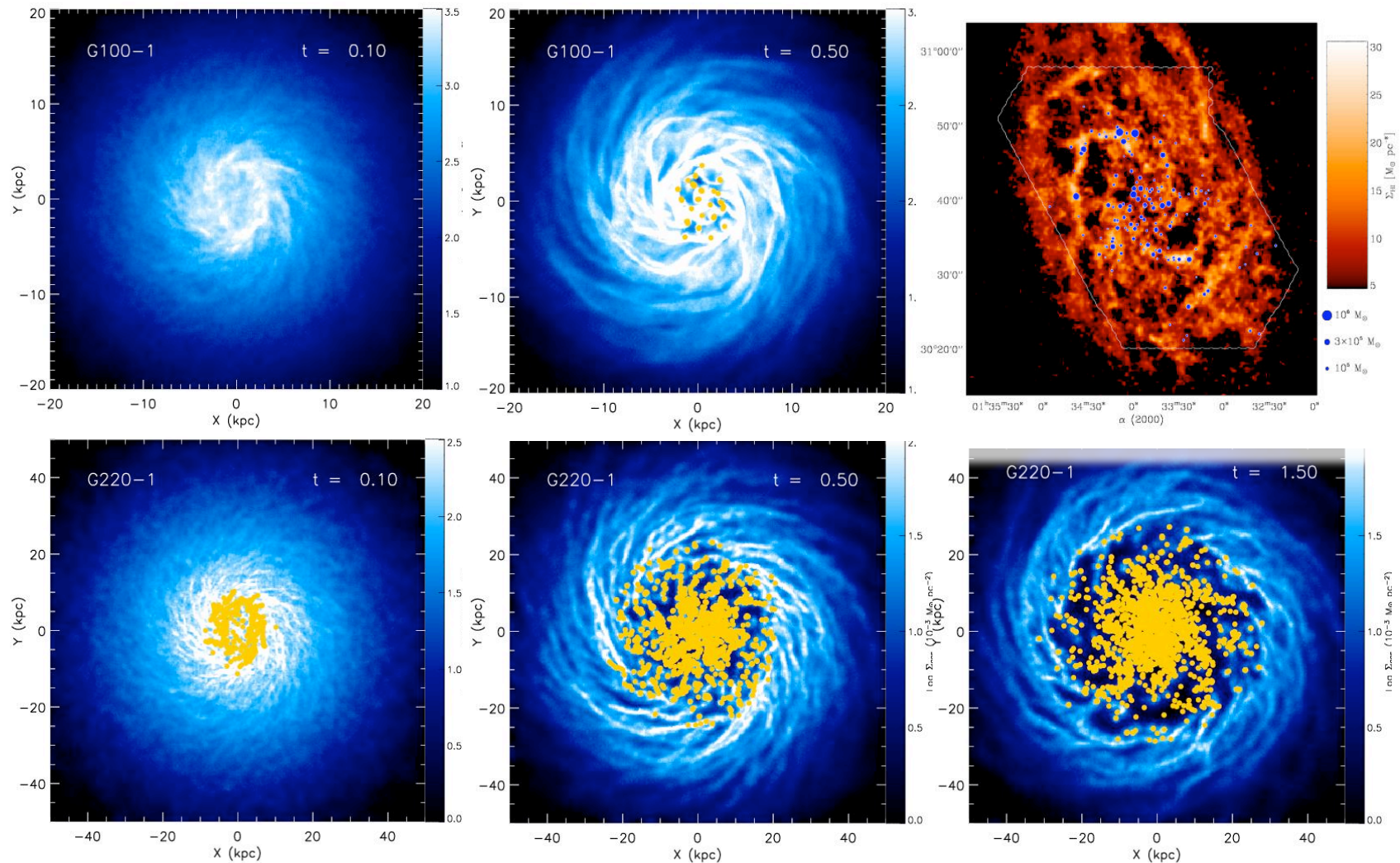
for  $n_{\text{H}} \geq 100 \text{ cm}^{-3}$ , H<sub>2</sub> forms within 10 Myr, this is about the lifetime of typical MC's.

in turbulent gas, the H<sub>2</sub> fraction can become very high on short timescale

(for models with coupling between cloud dynamics and time-dependent chemistry, see Glover & Mac Low 2007a,b)

# modeling galactic SF

SPH calculations of self-gravitating disks of stars and (isothermal) gas in dark-matter potential, sink particles measure local collapse --> star formation



# Modeling galactic SF

- Evolution of 42 isolated disk galaxies
  - DM halo, stellar disk & gas disk
  - SPH code GADGET with accretion particles  
(resolution:  $5 \times 10^5$  to  $3 \times 10^6$  gas particles)
  - $50 \text{ km/s} \leq v_{\text{circ}} \leq 250 \text{ km/s}$
  - fraction of disk mass:  $m_d = 5\% - 10\%$
  - gas fraction in disk:  $f_d = 20\%, 50\%, \& 90\%$
  - total mass:  $4.15 \times 10^{10} M_{\odot} \leq M_{200} \leq 357.14 \times 10^{10} M_{\odot}$   
(corresponds to mass resolution of  $138 M_{\odot} \leq M_{\text{SPH}} \leq 10^5 M_{\odot}$  in models with  $3 \times 10^6$  gas particles)

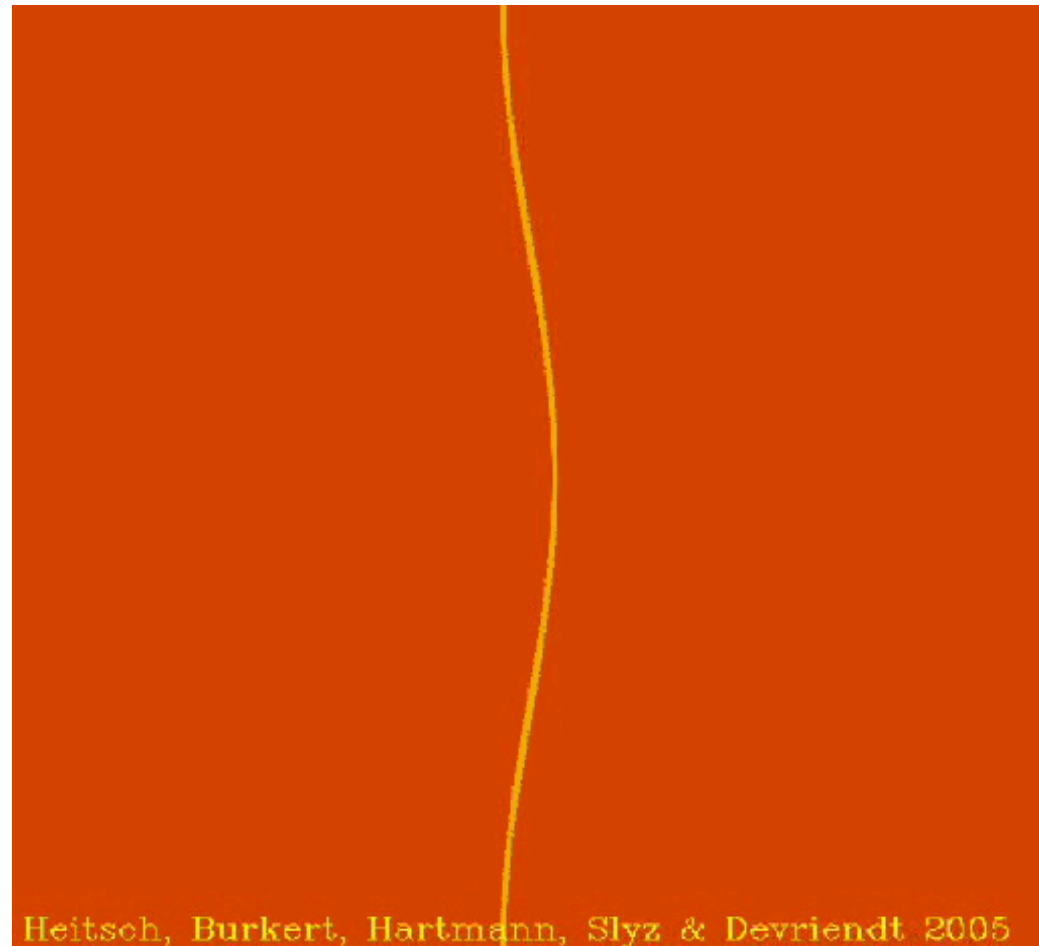


# Molecular cloud formation

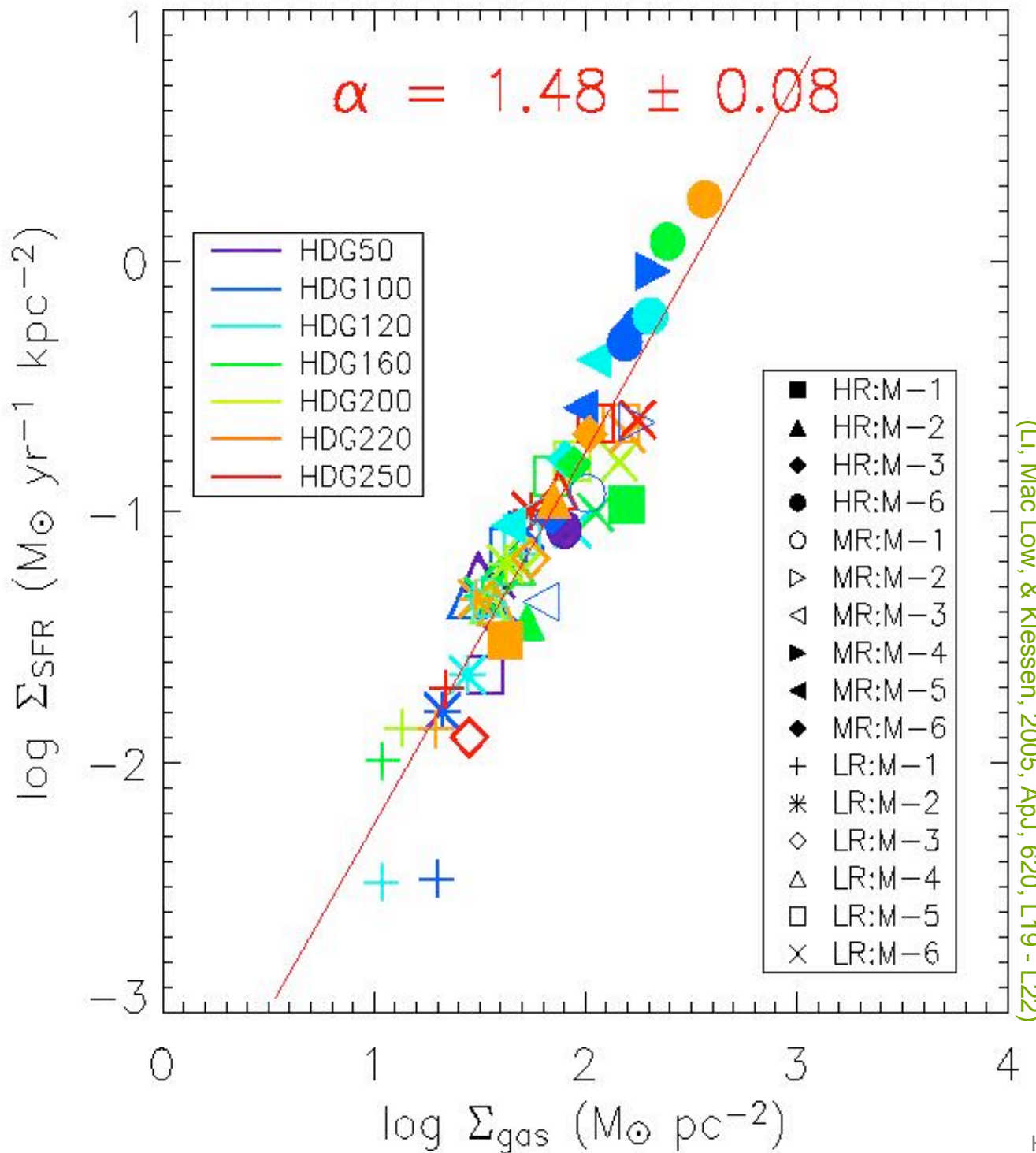
... in *convergent large-scale flows*

... setting up the *turbulent cascade*

- Mach 3 colliding flow
- Vishniac instability + thermal instability
- compressed sheet *breaks up* and builds up *cold, high-density* „blobs“ of gas
- --> molecular cloud formation
- cold cloud motions correspond to supersonic turbulence



(e.g. Koyama & Inutsuka 2002, Heitsch et al., 2005, Vazquez-Semadeni et al. 2004;  
also posters 8577, 8302)

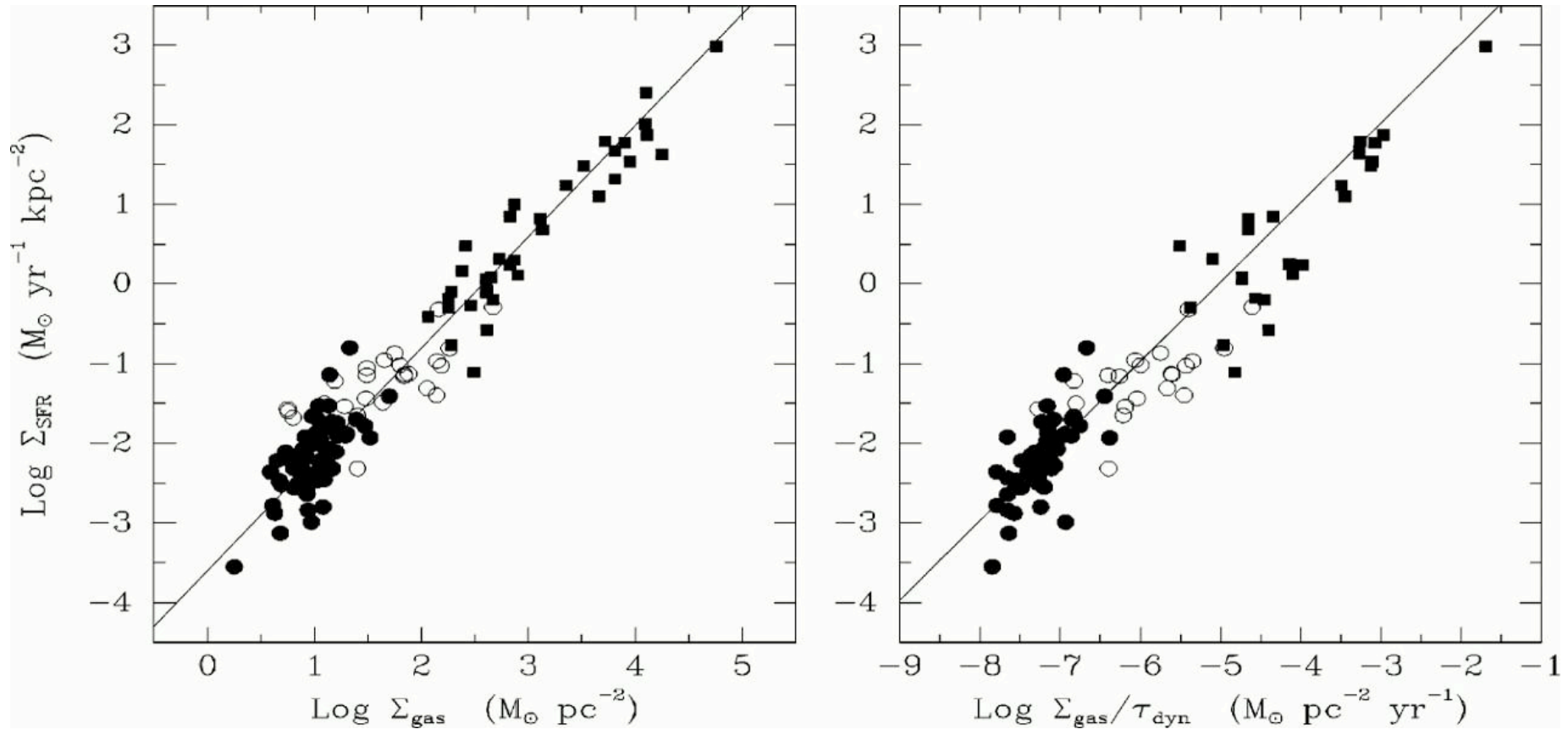


We find correlation between *star formation rate* and *gas surface density*:

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^{1.5}$$

*global Schmidt law*

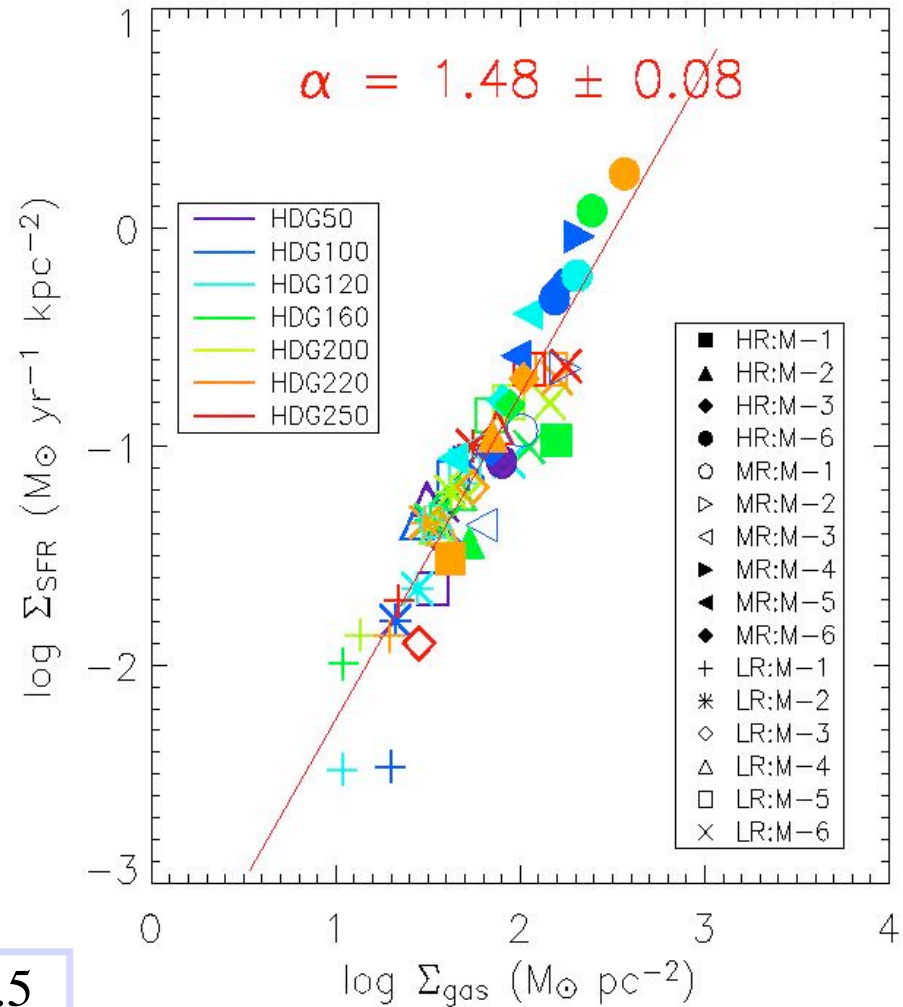
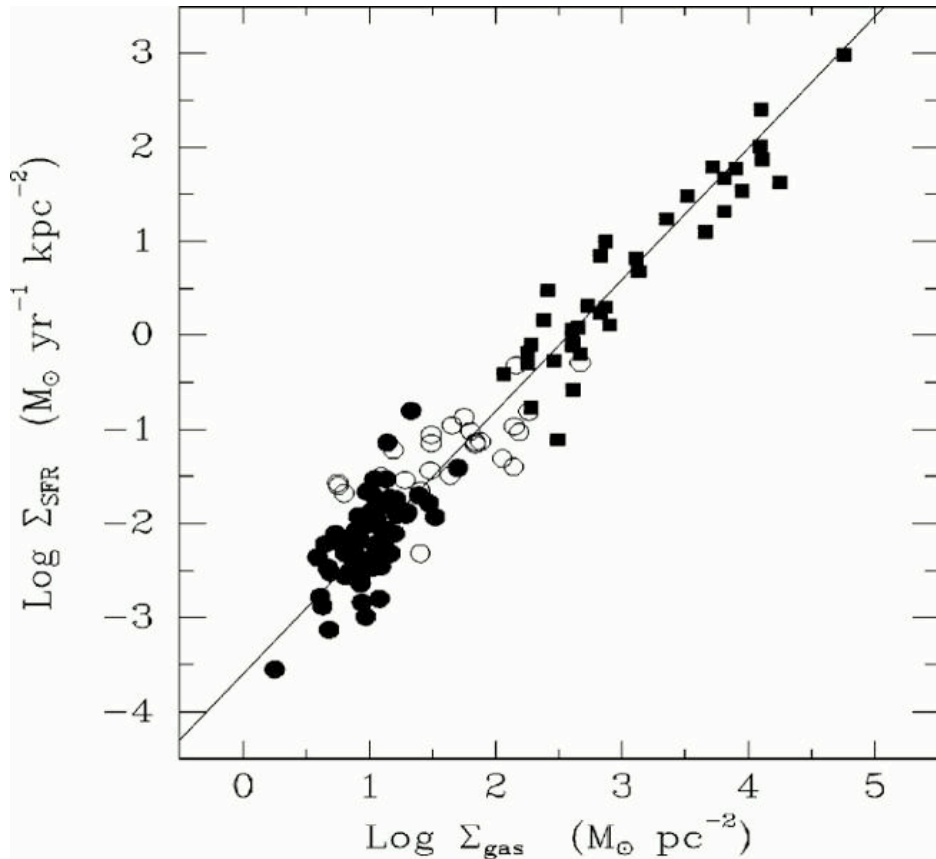
# Observed Schmidt law



$$\Sigma_{\text{SFR}} = (2.5 \pm 0.7) \times 10^{-4} \left( \frac{\Sigma_{\text{gas}}}{1 M_{\odot} \text{ pc}^{-2}} \right)^{1.4 \pm 0.15} M_{\odot} \text{ year}^{-1} \text{ kpc}^{-2},$$

(from Kennicutt 1998)

# observed Schmidt law



in both cases:

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^{1.5}$$

(from Kennicutt 1998)

# modeling small scales

# Properties of turbulence

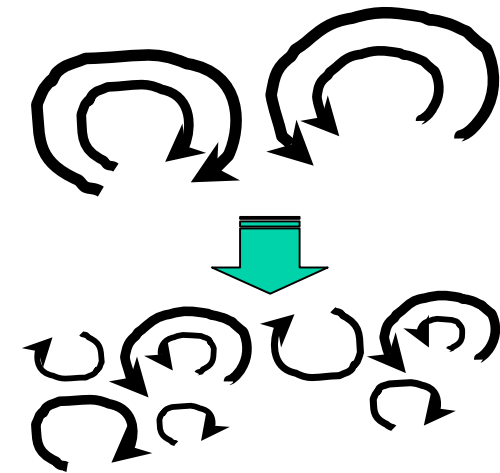
- laminar flows turn *turbulent* at *high Reynolds* numbers

$$\text{Re} = \frac{\text{advection}}{\text{dissipation}} = \frac{VL}{\nu}$$

$V$  = typical velocity on scale  $L$ ,  $\nu$  = viscosity,  $\text{Re} > 1000$

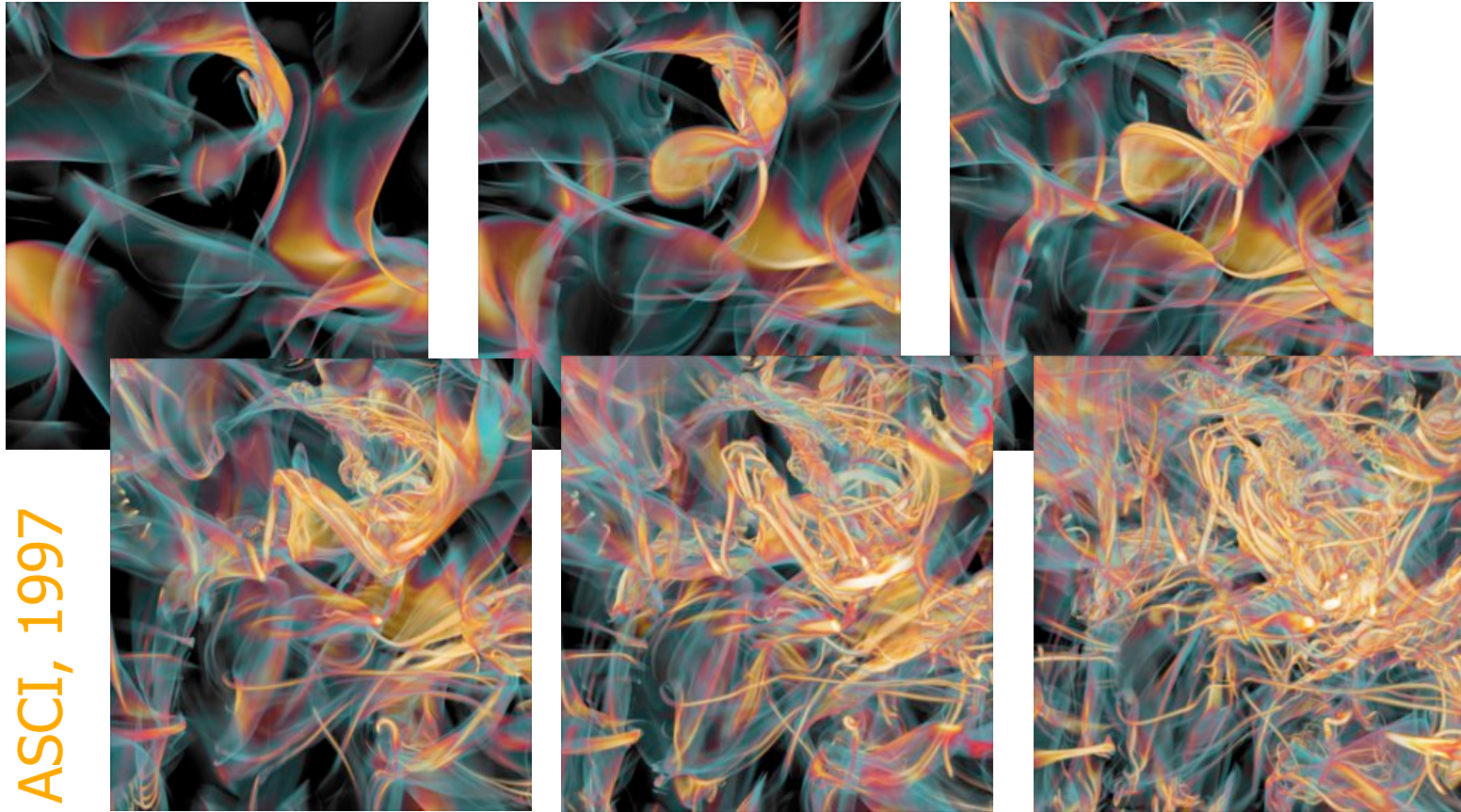
- *vortex stretching* --> turbulence is *intrinsically anisotropic* (only on large scales you *may* get homogeneity & isotropy in a statistical sense; see Landau & Lifschitz, Chandrasekhar, Taylor, etc.)

(ISM turbulence: shocks & B-field cause additional inhomogeneity)



# Vortex Formation

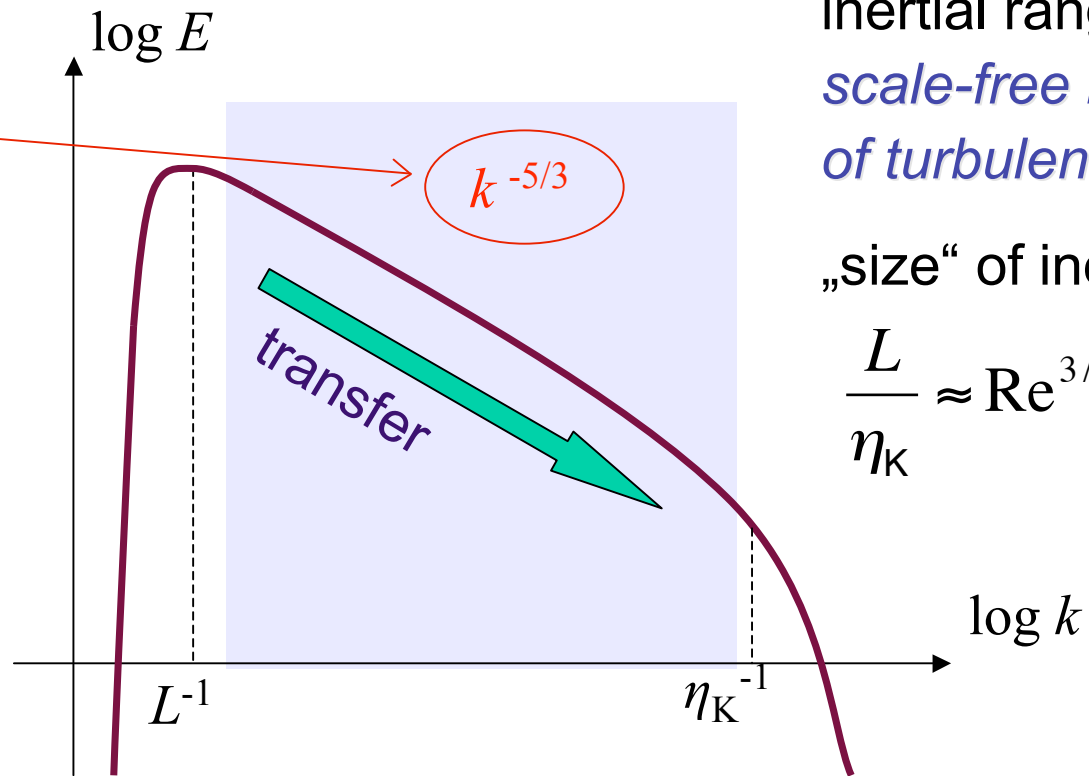
Porter et al.  
ASCI, 1997



Vortices are stretched and folded in **three dimensions**

# turbulent cascade

Kolmogorov (1941) theory  
incompressible turbulence



inertial range:  
*scale-free behavior  
of turbulence*

„size“ of inertial range:

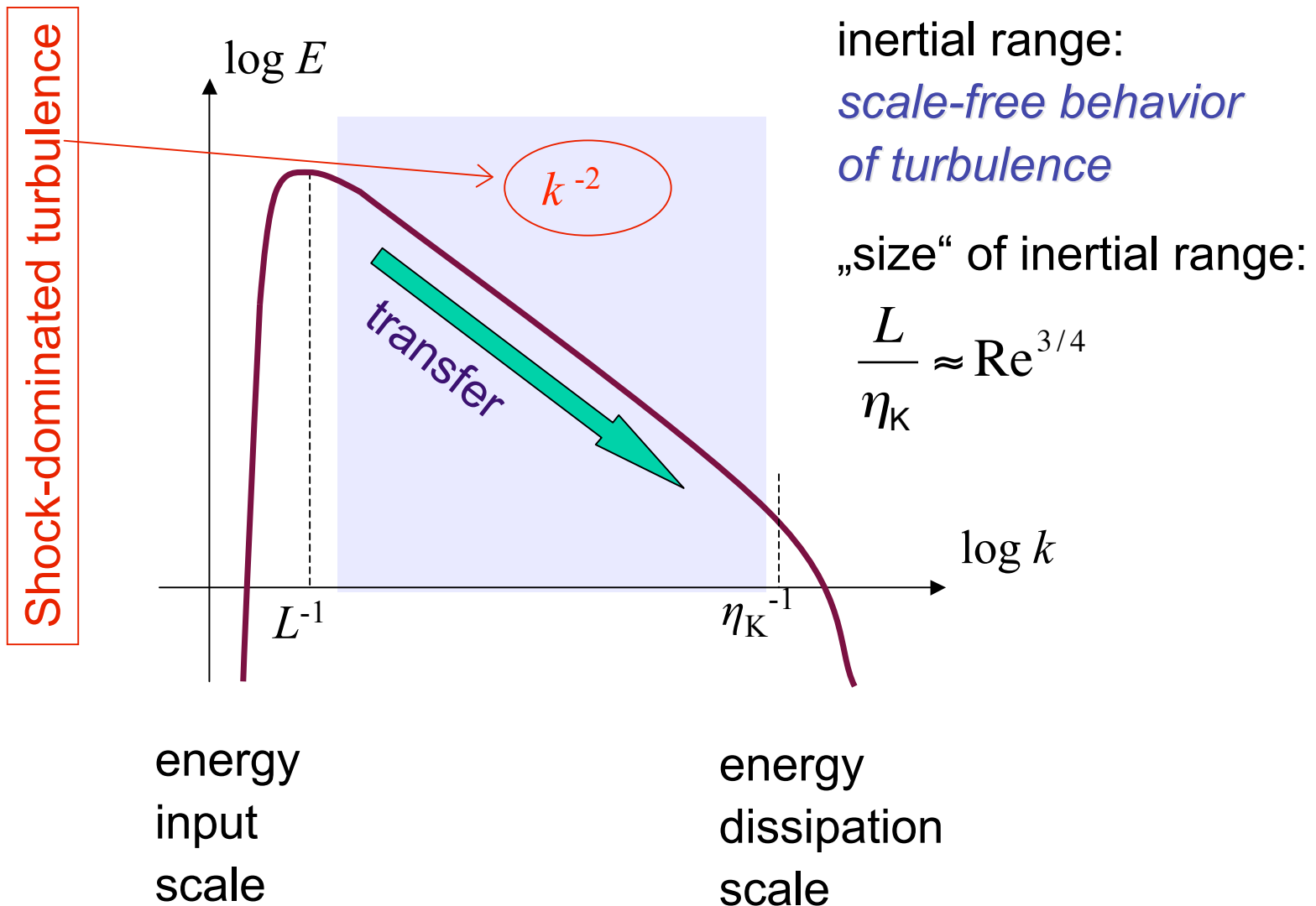
$$\frac{L}{\eta_K} \approx \text{Re}^{3/4}$$

energy  
input  
scale

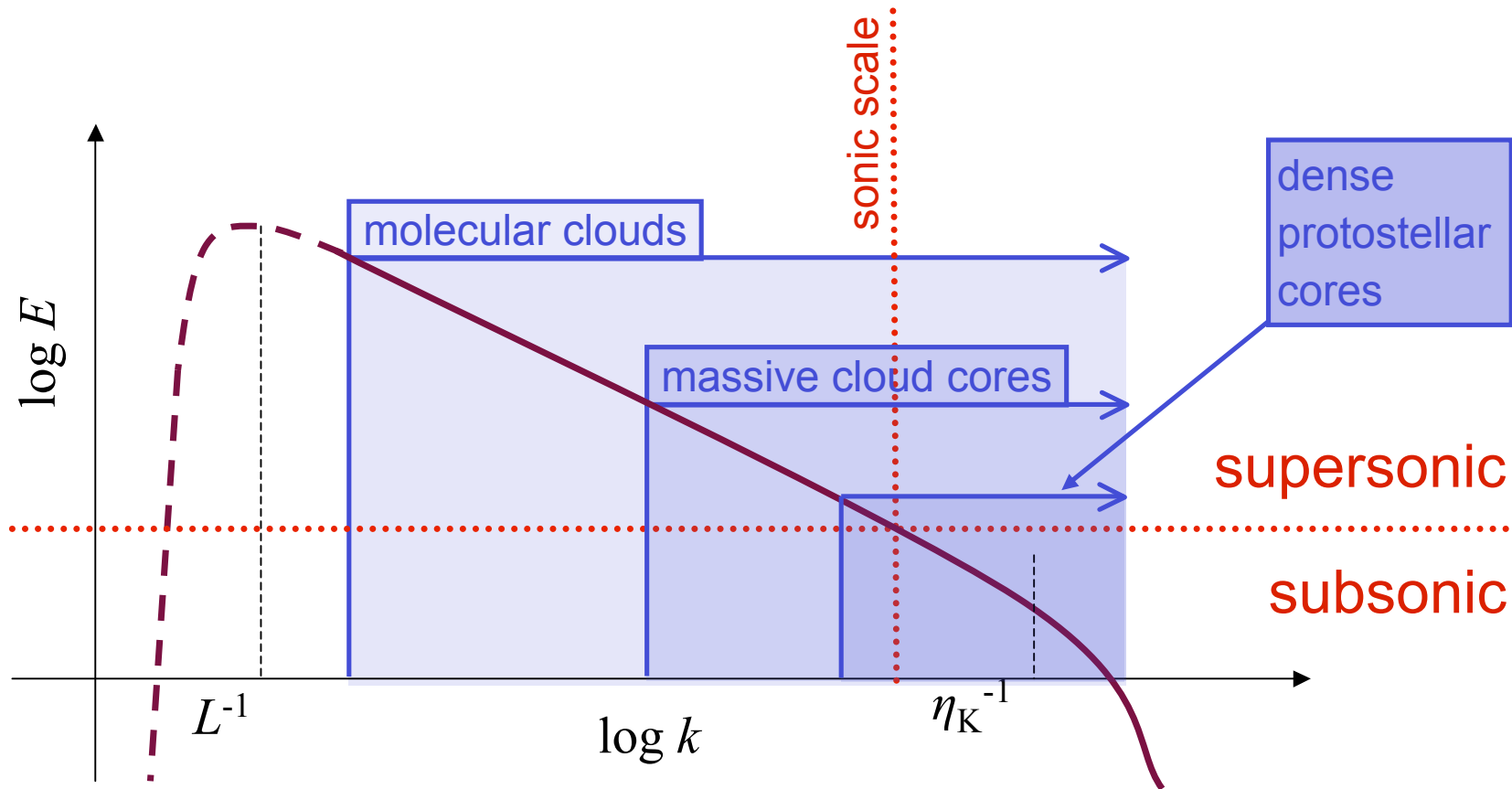
energy  
dissipation  
scale



# turbulent cascade



# turbulent cascade in ISM



energy source & scale  
*NOT known*  
 (supernovae, winds,  
 spiral density waves?)

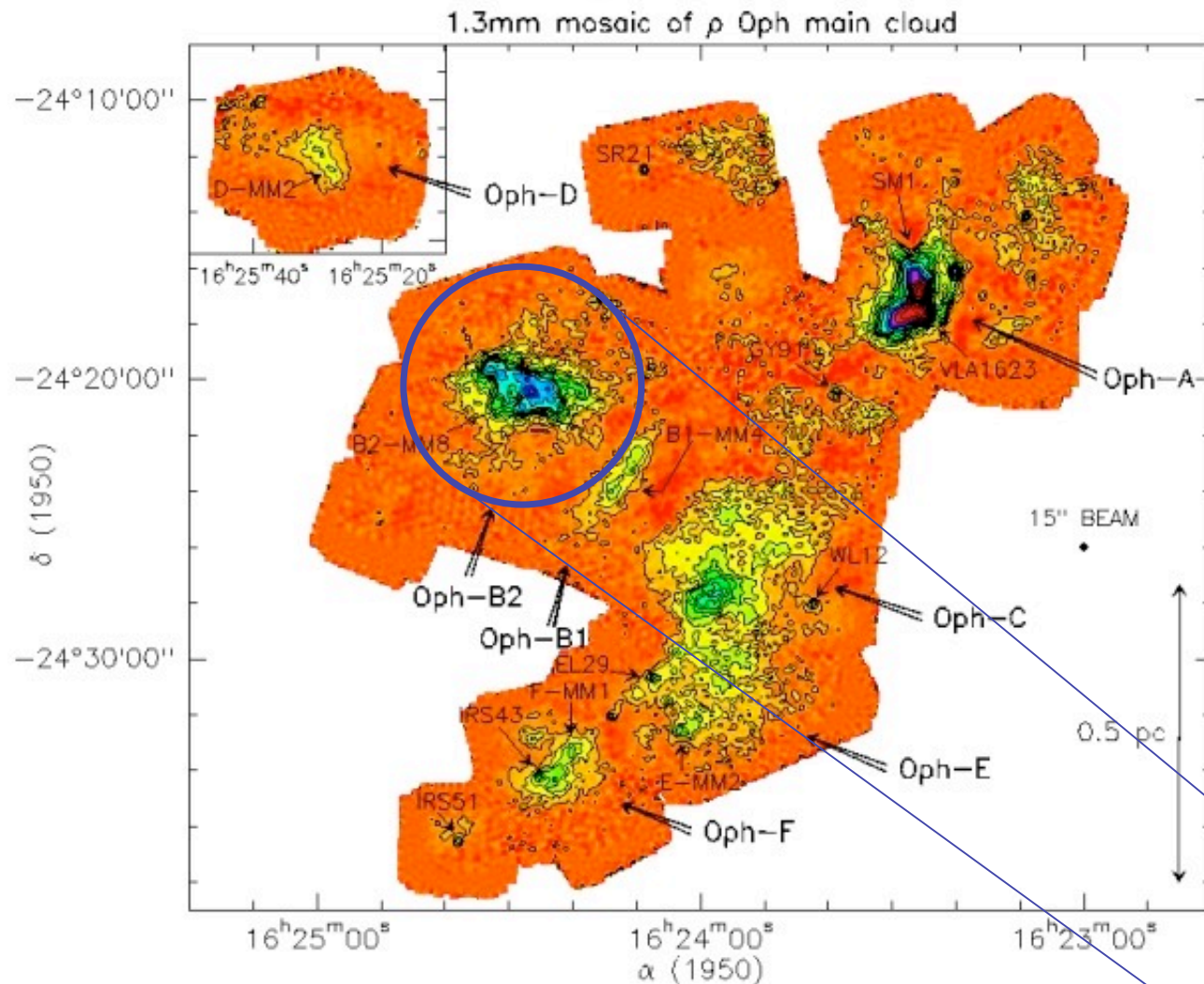
$$\sigma_{\text{rms}} \ll 1 \text{ km/s}$$

$$M_{\text{rms}} \leq 1$$

$$L \approx 0.1 \text{ pc}$$

dissipation scale not known  
 (ambipolar diffusion,  
 molecular diffusion?)

# density structure of MCs



molecular clouds are highly inhomogeneous

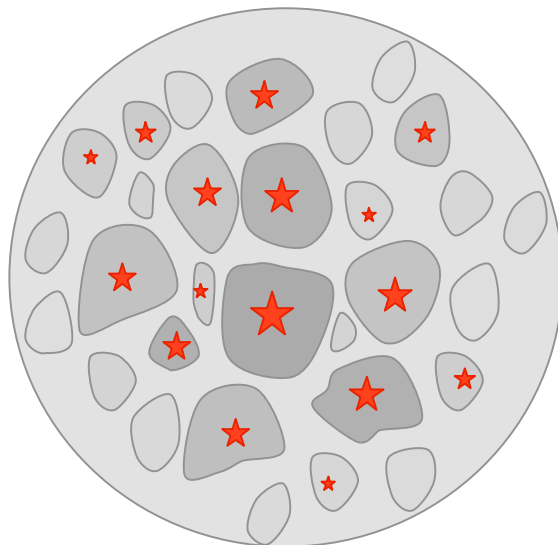
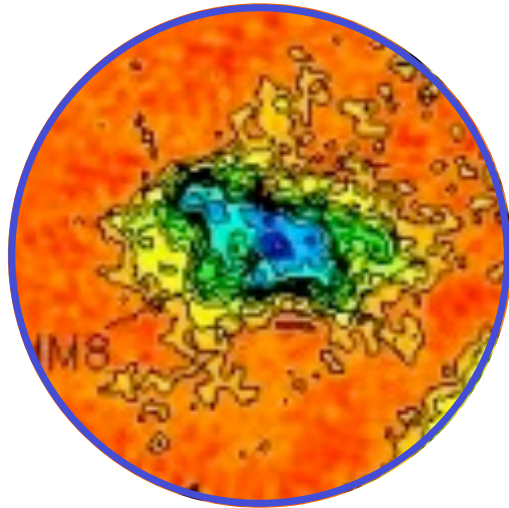
stars form in the densest and coldest parts of the cloud

$\rho$ -Ophiuchus cloud seen in dust emission

let's focus on a cloud core like this one

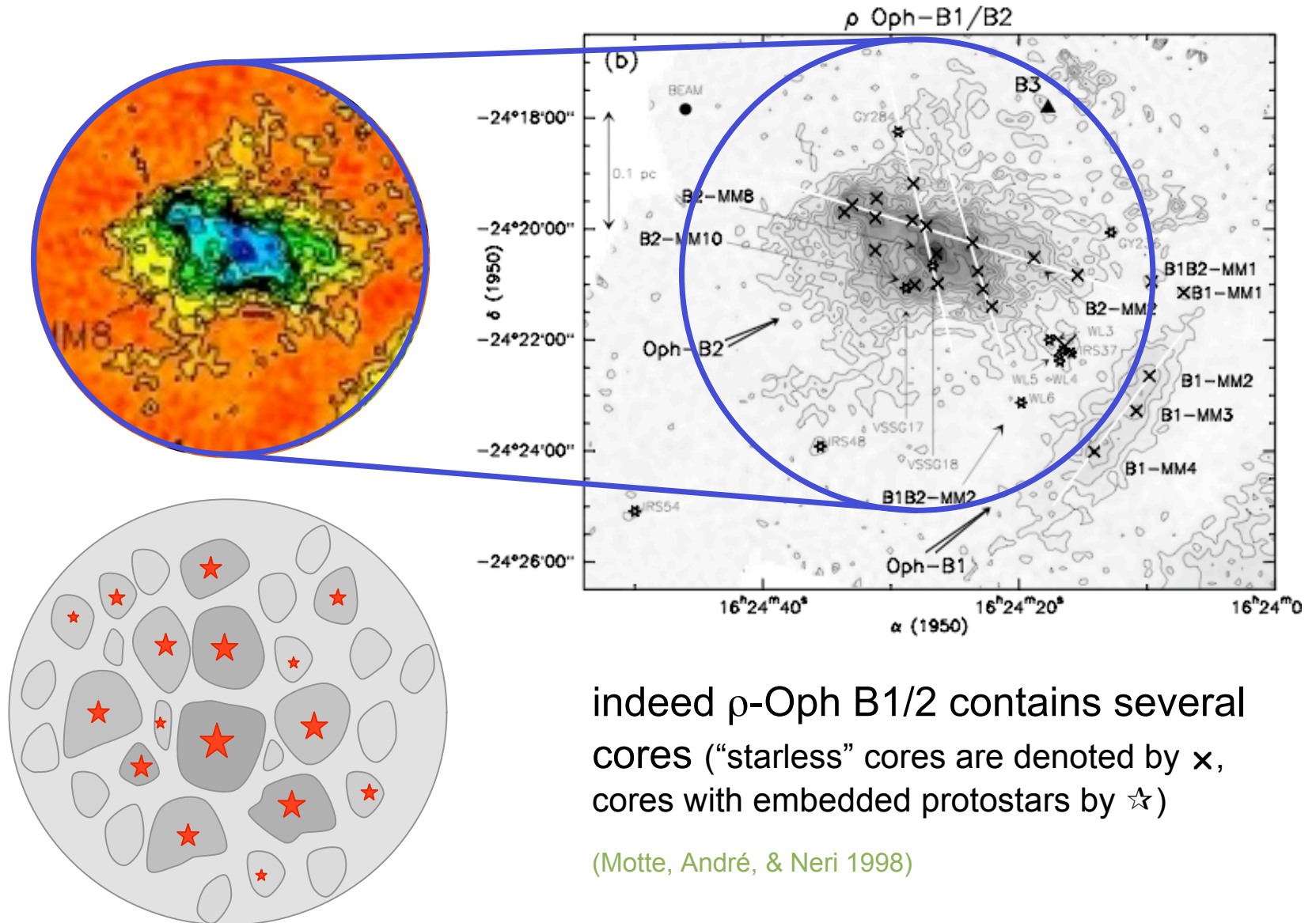
(Motte, André, & Neri 1998)

# evolution of cloud cores



- Does core form single massive star or cluster with mass distribution?
- Turbulent cascade „goes through“ cloud core  
--> NO *scale separation* possible  
--> NO *effective sound speed*
- Turbulence is supersonic!  
--> produces strong density contrasts:  
 $\delta\rho/\rho \approx M^2$   
--> with typical  $M \approx 10$  -->  $\delta\rho/\rho \approx 100!$
- many of the shock-generated fluctuations are Jeans unstable and go into collapse
- --> *core breaks up and forms a cluster of stars*

# evolution of cloud cores

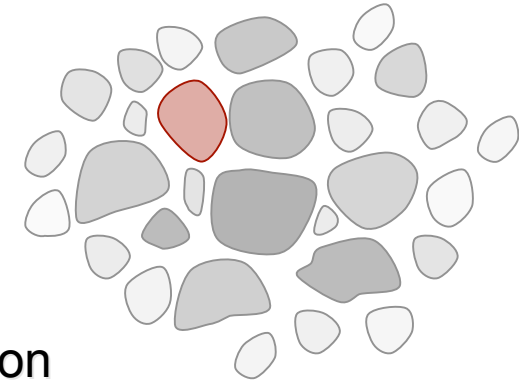


indeed  $\rho$ -Oph B1/2 contains several cores ("starless" cores are denoted by  $\times$ , cores with embedded protostars by  $\star$ )

(Motte, André, & Neri 1998)

# formation and evolution of cores

- protostellar cloud cores form at the *stagnation points* of *convergent turbulent flows*
- if  $M > M_{\text{Jeans}} \propto \rho^{-1/2} T^{3/2}$ : collapse and star formation
- if  $M < M_{\text{Jeans}} \propto \rho^{-1/2} T^{3/2}$ : reexpansion after external compression fades away



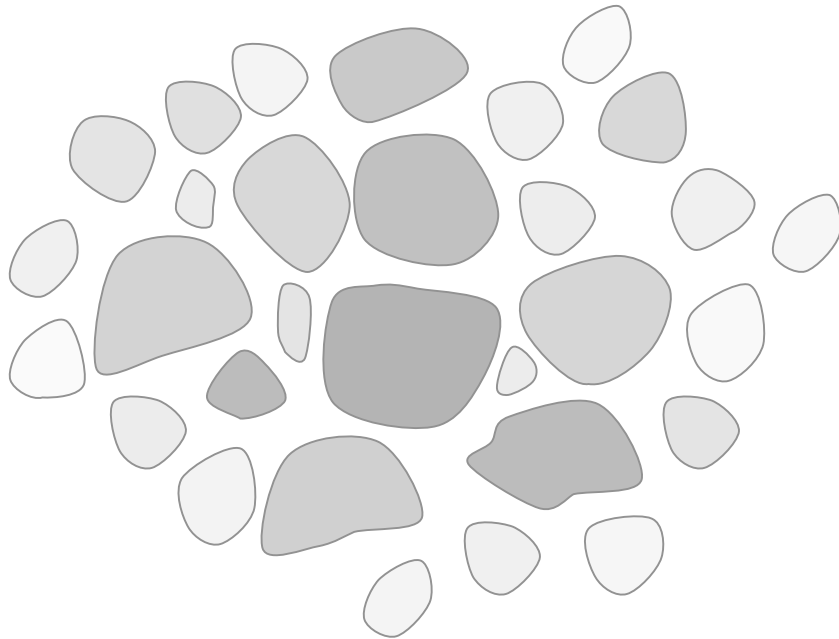
(e.g. Vazquez-Semadeni et al 2005)

- typical timescales:  $t \approx 10^4 \dots 10^5$  yr
- because *turbulent* ambipolar diffusion time is *short*, this time estimate still holds for the presence of magnetic fields, in *magnetically critical cores*

(e.g. Fatuzzo & Adams 2002, Heitsch et al. 2004)

# formation and evolution of cores

What happens to distribution of cloud cores?



Two extreme cases:

(1) turbulence dominates energy budget:

$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| > 1$$

--> individual cores do *not* interact

--> *collapse of individual cores*  
dominates *stellar mass growth*

--> *loose cluster of low-mass stars*

(2) turbulence decays, i.e. gravity

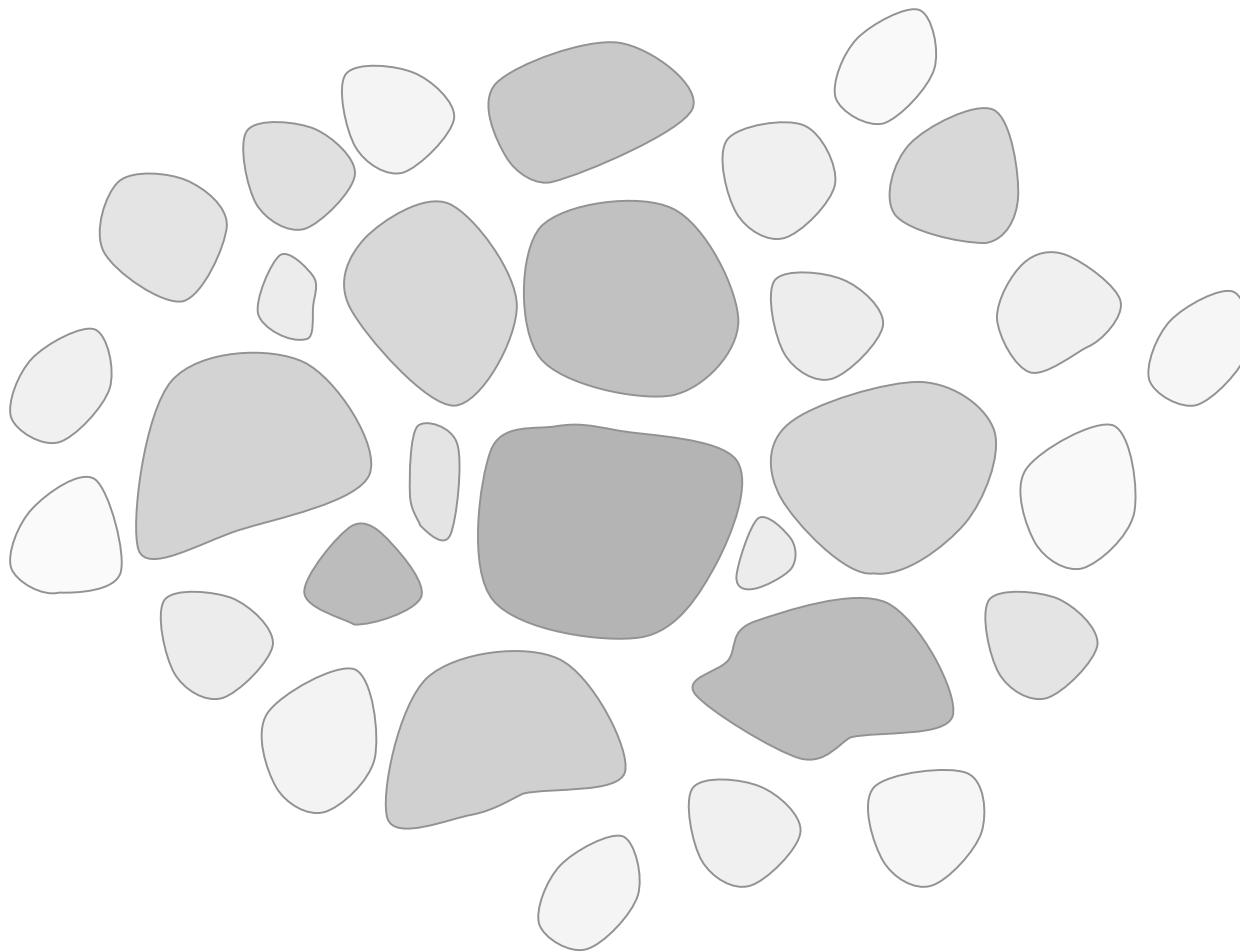
dominates:  $\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$

--> *global contraction*

--> core do *interact* while collapsing

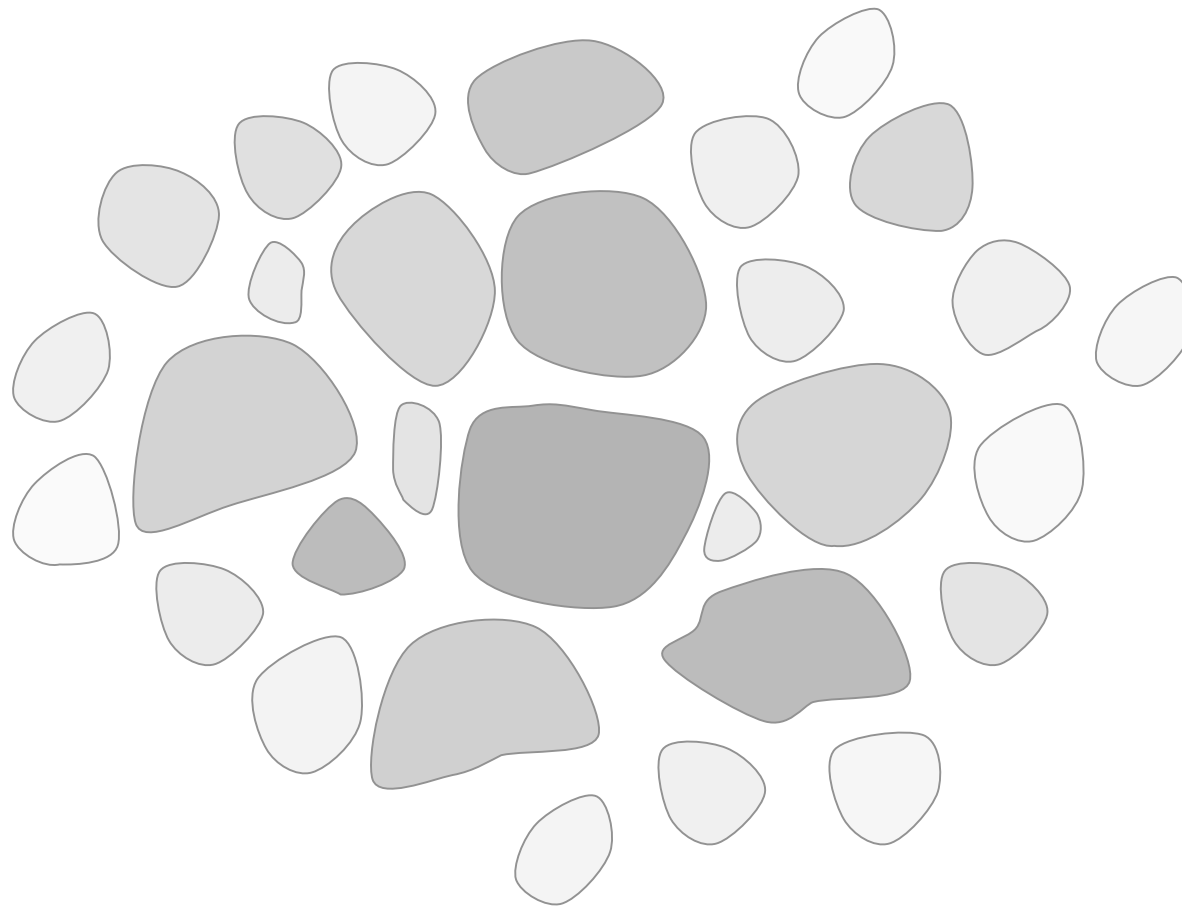
--> *competition* influences *mass growth*

--> *dense cluster with high-mass stars*



**turbulence creates a hierarchy of clumps**

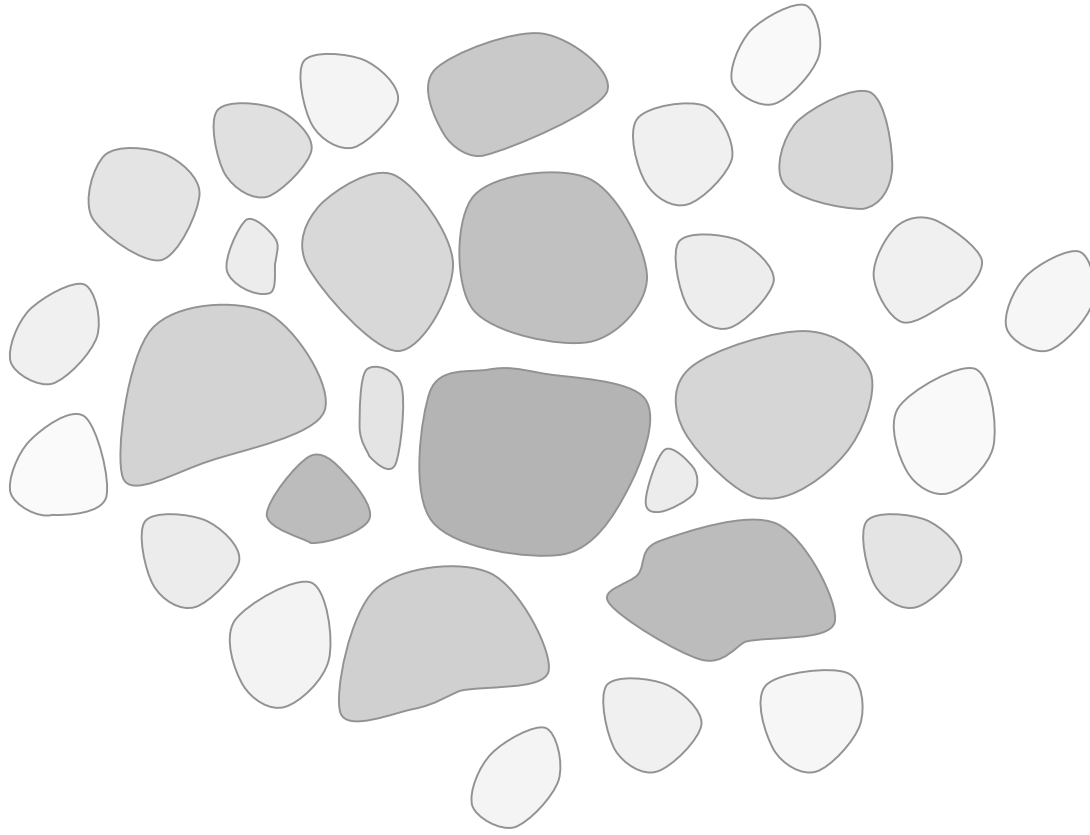




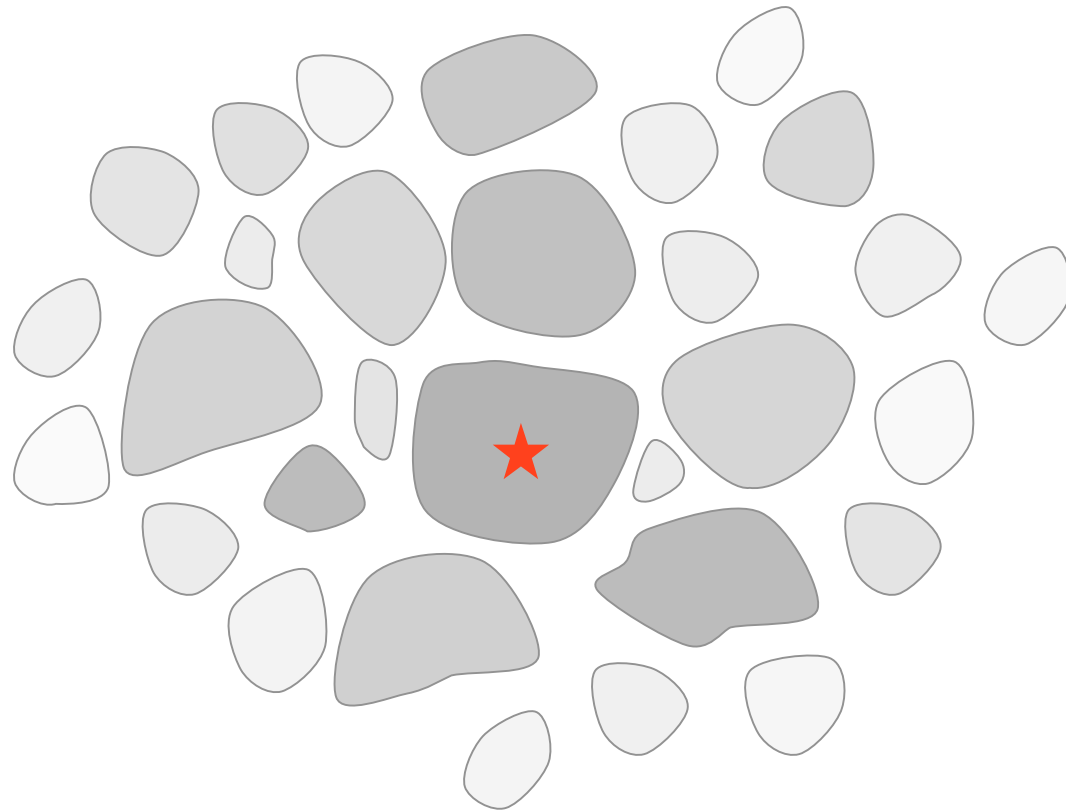
as turbulence decays locally, contraction sets in



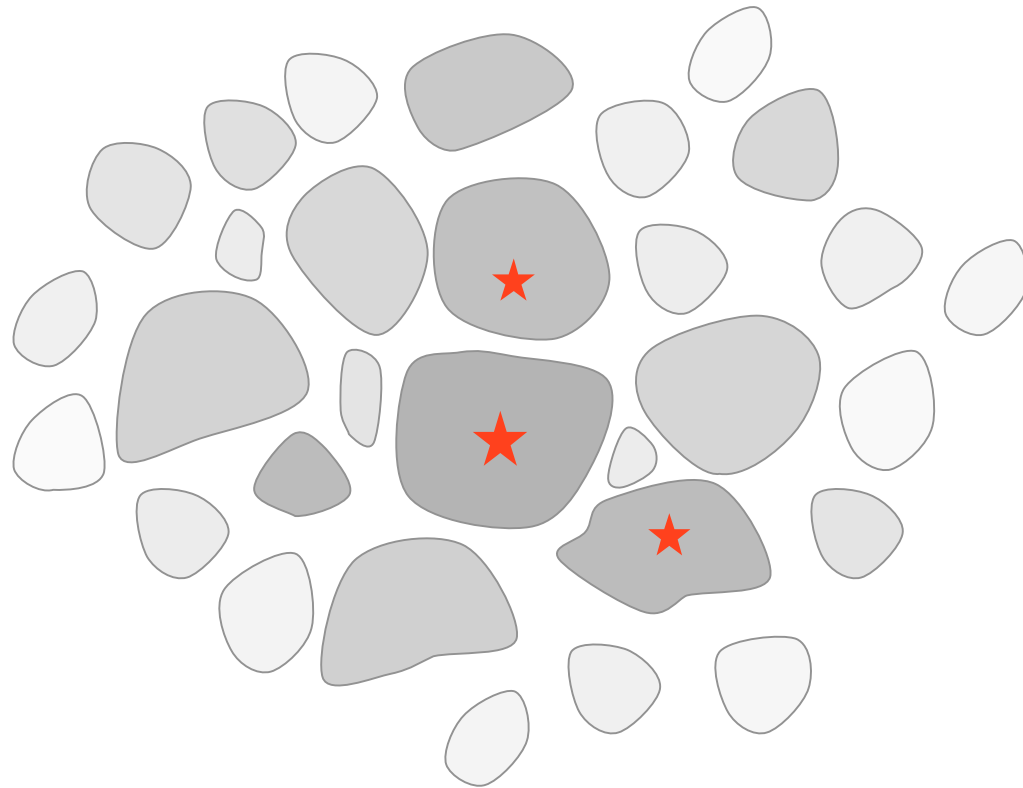
as turbulence decays locally, contraction sets in



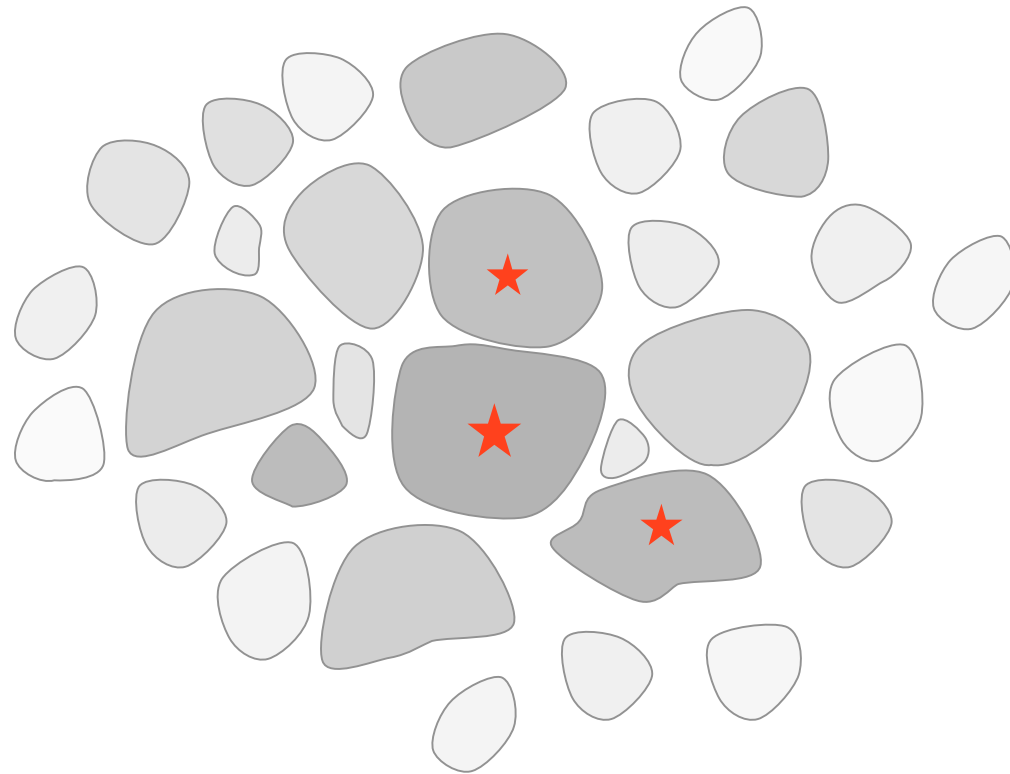
while region contracts, individual clumps collapse to form stars



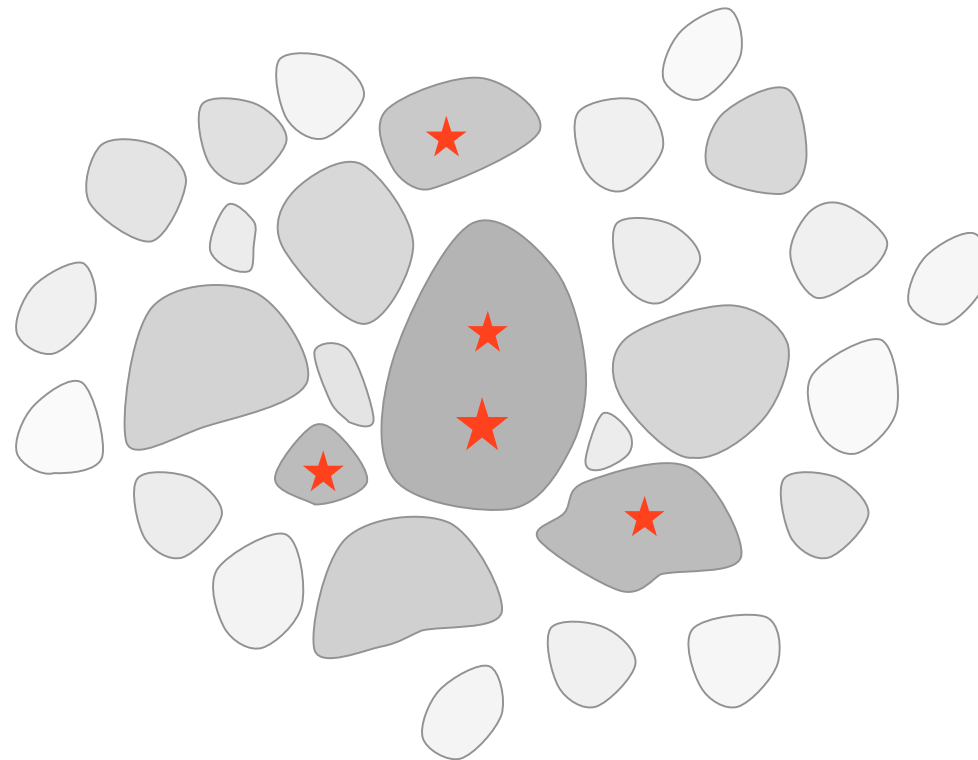
while region contracts, individual clumps collapse to form stars



individual clumps collapse to form stars

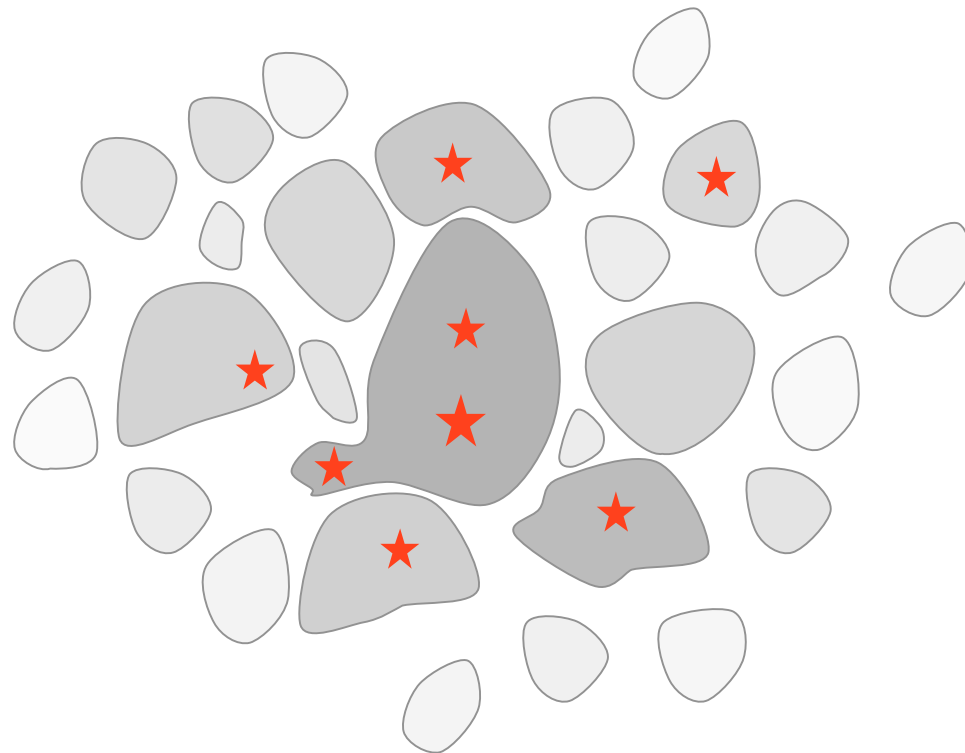


individual clumps collapse to form stars



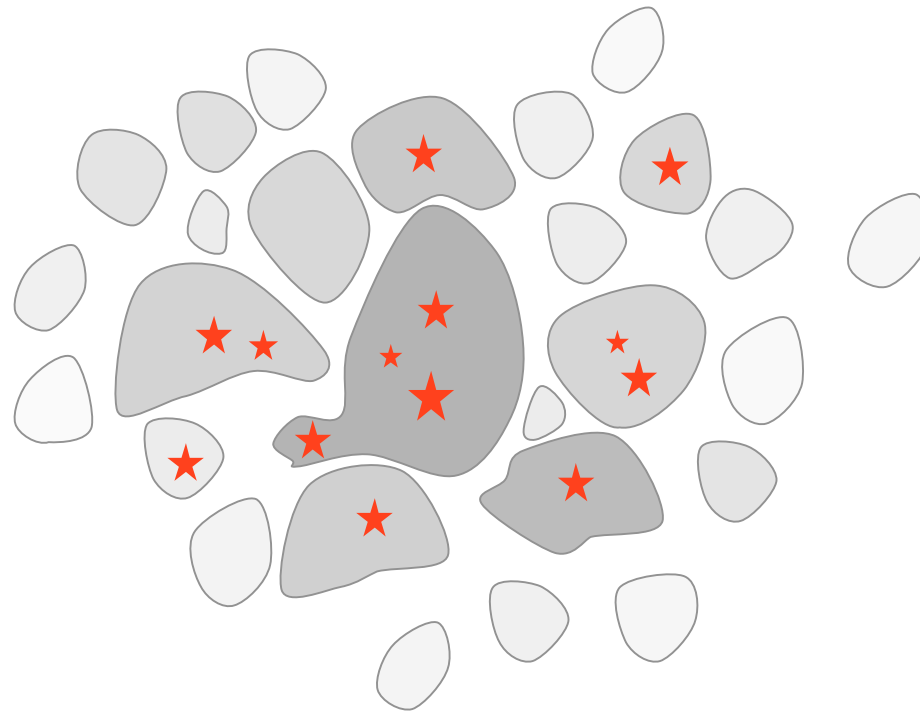
$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

in *dense clusters*, clumps may merge while collapsing  
--> then contain multiple protostars

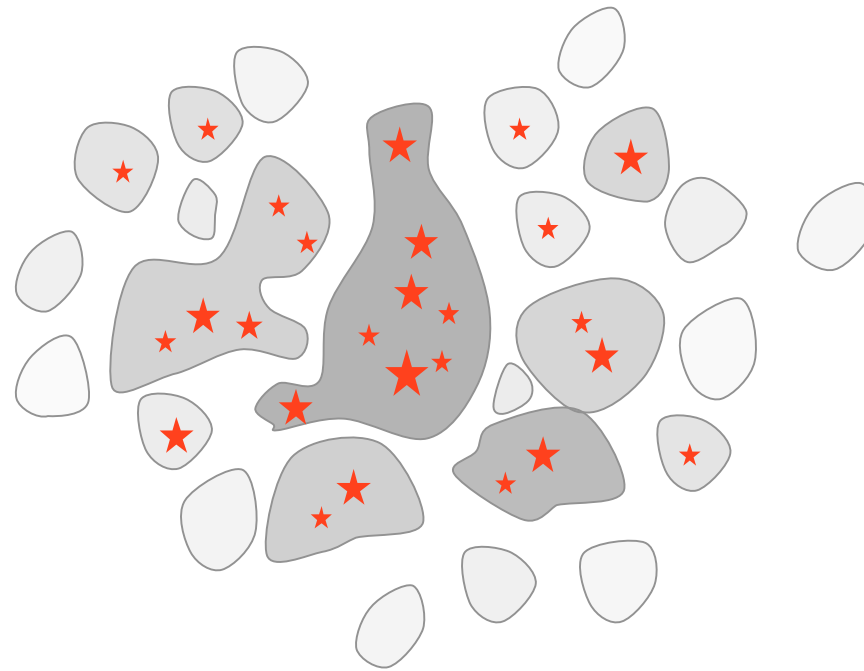


in *dense clusters*, clumps may merge while collapsing  
--> then contain multiple protostars

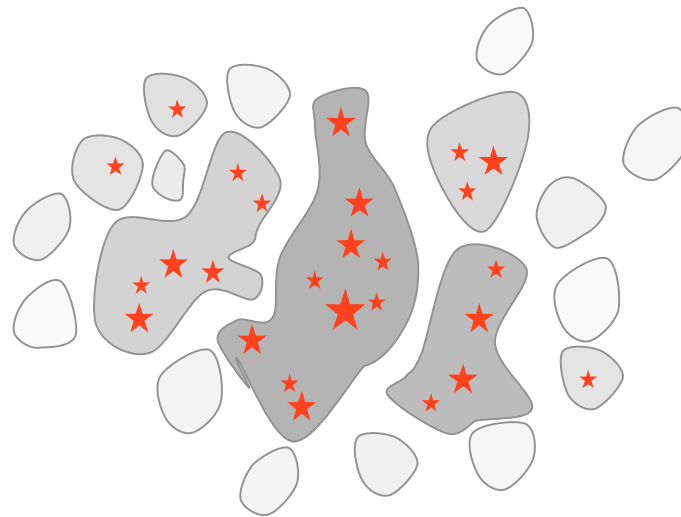




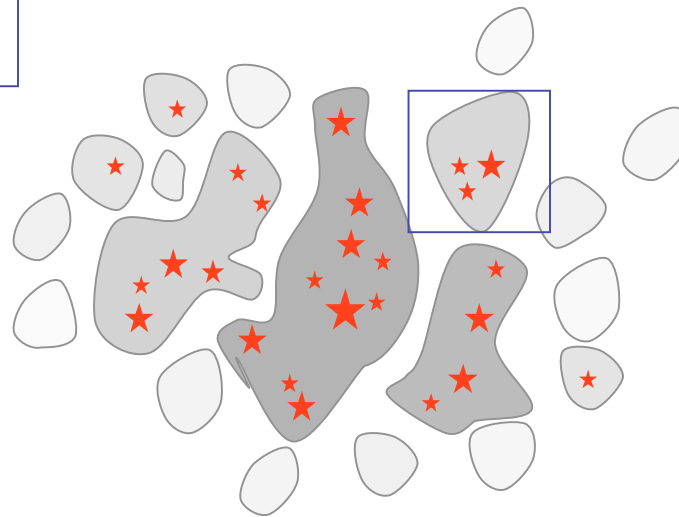
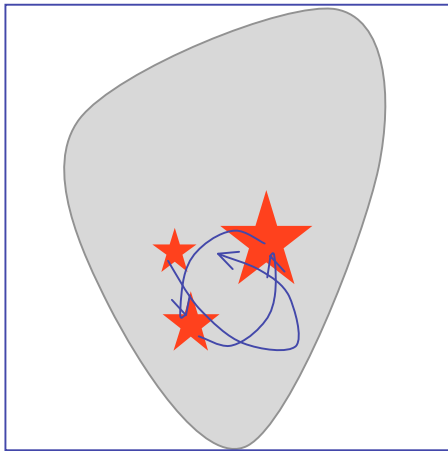
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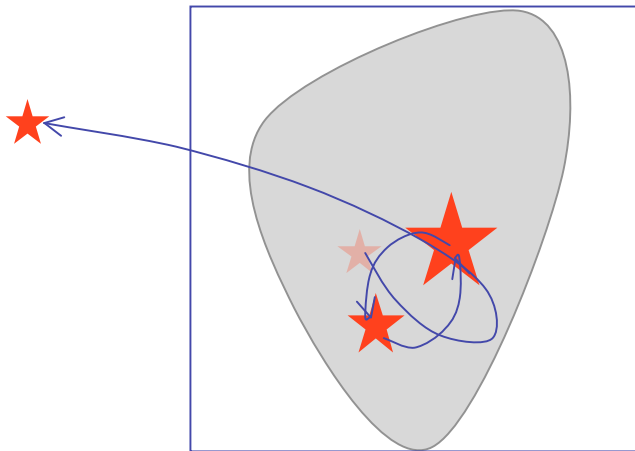
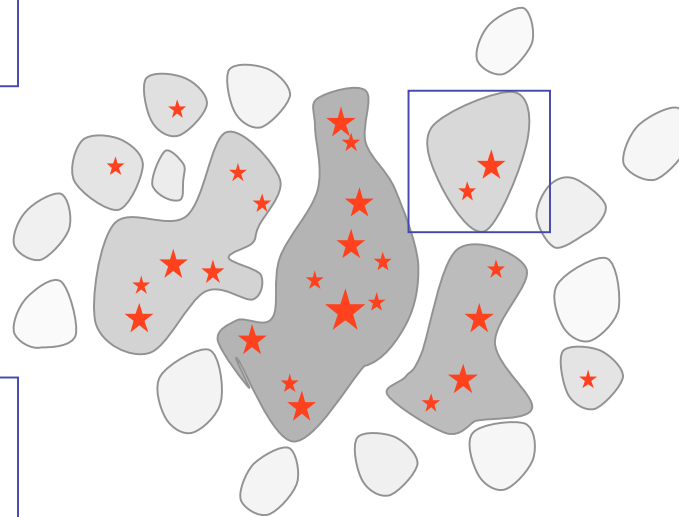
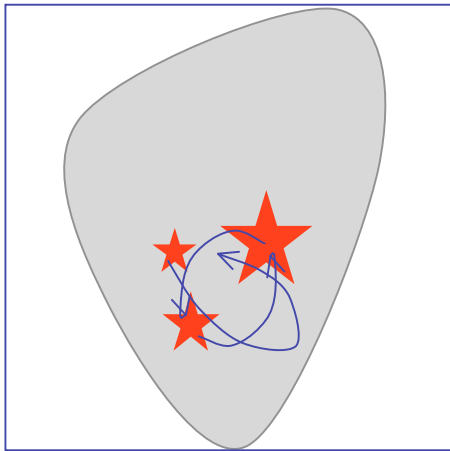
in *dense clusters*, competitive mass growth becomes important



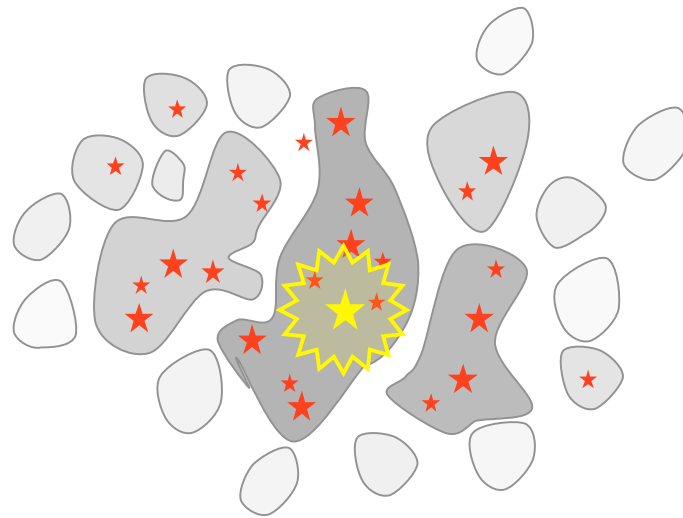
in *dense clusters*, competitive mass growth  
becomes important



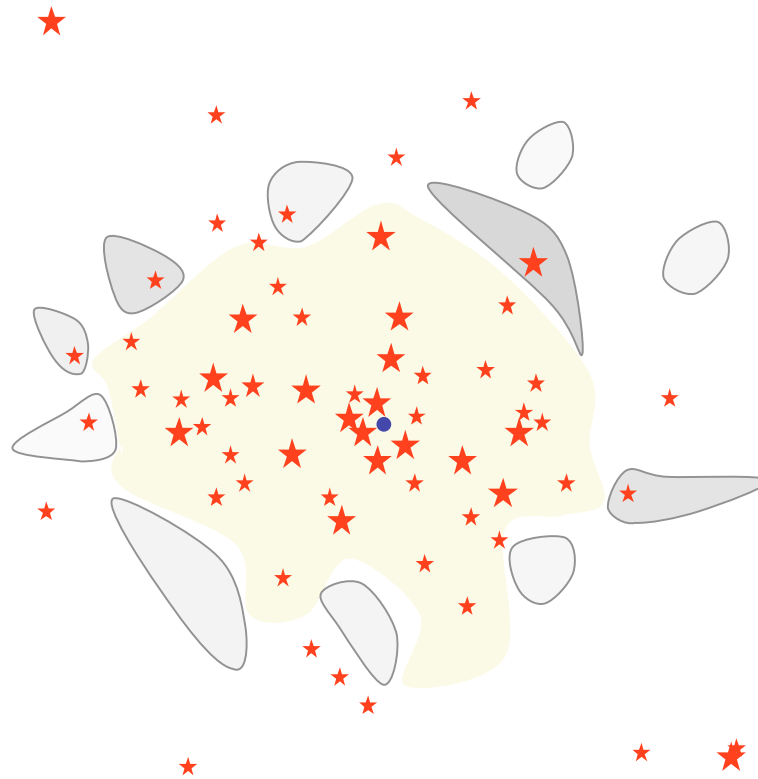
in *dense clusters*,  $N$ -body effects influence mass growth



low-mass objects may  
become ejected --> accretion stops



feedback terminates star formation



result: *star cluster*, possibly with H II region

predictions



# predictions

- *global properties* (statistical properties)
  - SF efficiency and timescale
  - stellar mass function -- IMF
  - dynamics of young star clusters
  - description of self-gravitating turbulent systems (pdf's,  $\Delta$ -var.)
  - chemical mixing properties
- *local properties* (properties of individual objects)
  - properties of individual clumps (e.g. shape, radial profile, lifetimes)
  - accretion history of individual protostars ( $dM/dt$  vs.  $t$ ,  $j$  vs.  $t$ )
  - binary (proto)stars (eccentricity, mass ratio, etc.)
  - SED's of individual protostars
  - dynamic PMS tracks:  $T_{\text{bol}}-L_{\text{bol}}$  evolution

# examples and predictions

*example 1:* transient structure of turbulent clouds

*example 2:* speculations on the origin of the stellar mass spectrum (IMF)

# example 1

# Transient cloud structure

*Gravoturbulent fragmentation of turbulent self-gravitating clouds*



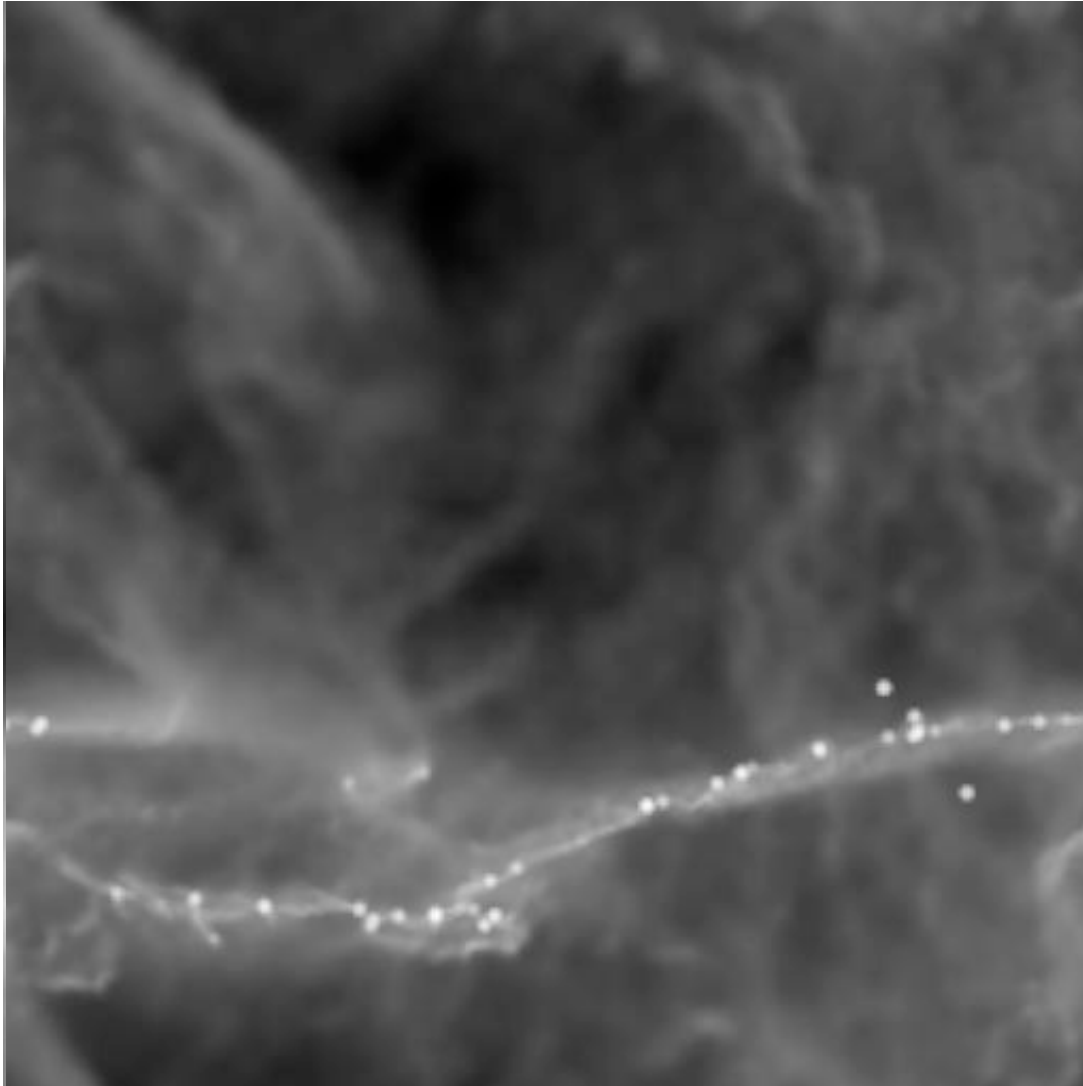
*xy projection*

*xz projection*

*yz projection*

- SPH model with  $1.6 \times 10^6$  particles
- large-scale driven turbulence
- Mach number  $\mathcal{M} = 6$
- periodic boundaries
- physical scaling: “Taurus”

# Gravoturbulent fragmentation



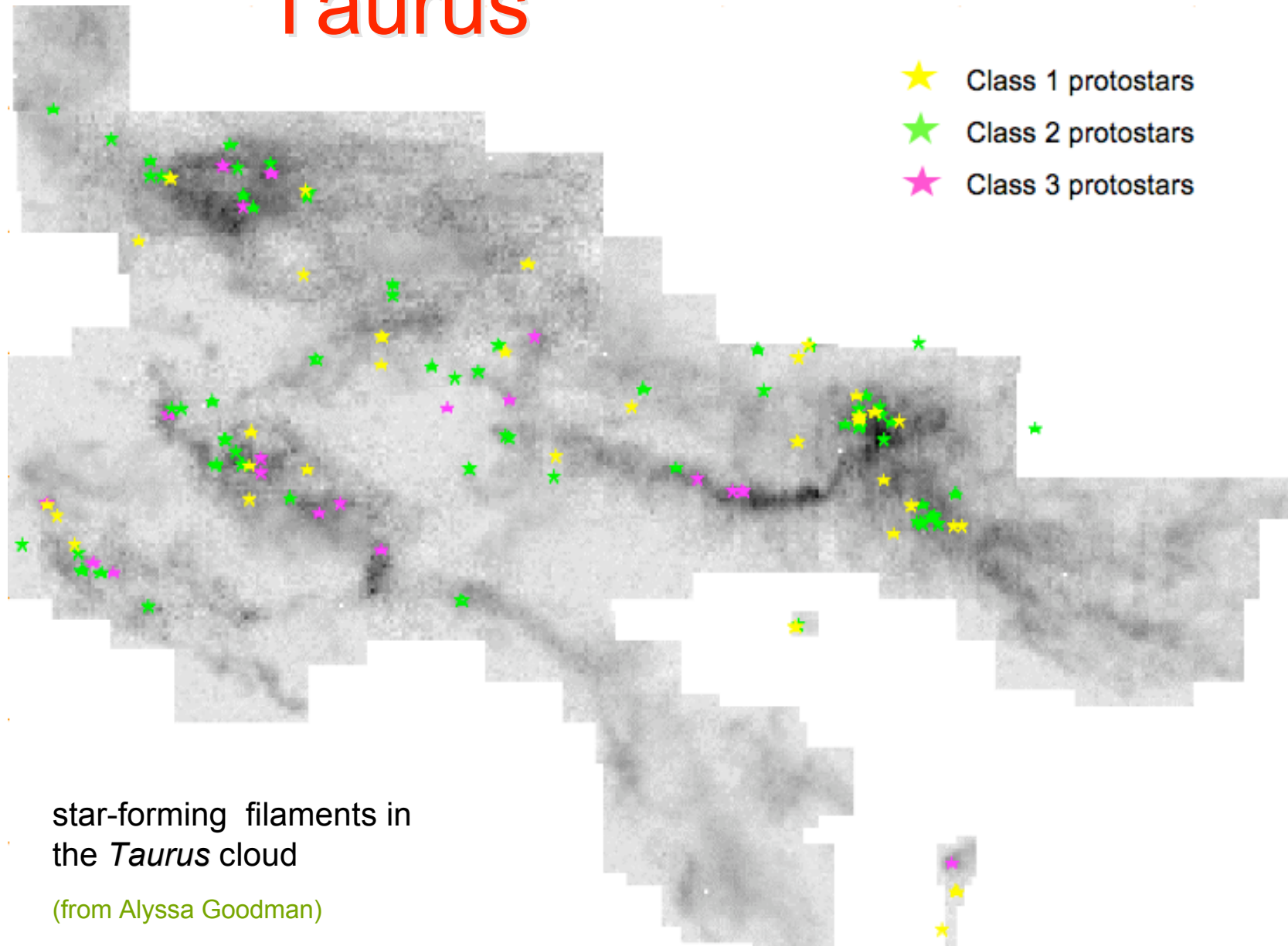
## Gravoturbulent fragmentation in molecular clouds:

- SPH model with  $1.6 \times 10^6$  particles
- large-scale driven turbulence
- Mach number  $\mathcal{M} = 6$
- periodic boundaries
- physical scaling:

### “Taurus”:

- density  $n(\text{H}_2) \approx 10^2 \text{ cm}^{-3}$
- $L = 6 \text{ pc}$ ,  $M = 5000 M_{\odot}$

# Taurus





# example 2

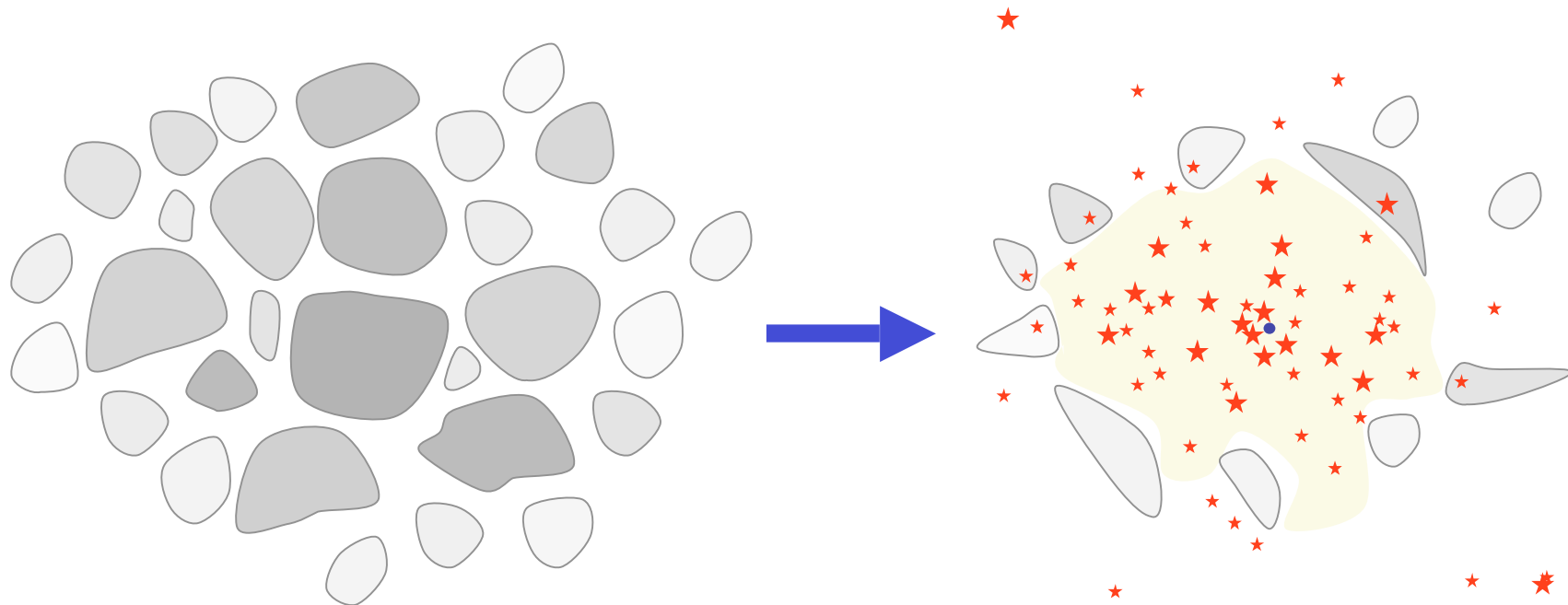


# IMF

- distribution of stellar masses depends on
  - turbulent initial conditions
    - > mass spectrum of prestellar cloud cores
  - collapse and interaction of prestellar cores
    - > competitive accretion and  $N$ -body effects
  - thermodynamic properties of gas
    - > balance between heating and cooling
    - > EOS (determines which cores go into collapse)
  - (proto) stellar feedback terminates star formation
    - ionizing radiation, bipolar outflows, winds, SN

# Star cluster formation

Most stars form in clusters → *star formation = cluster formation*

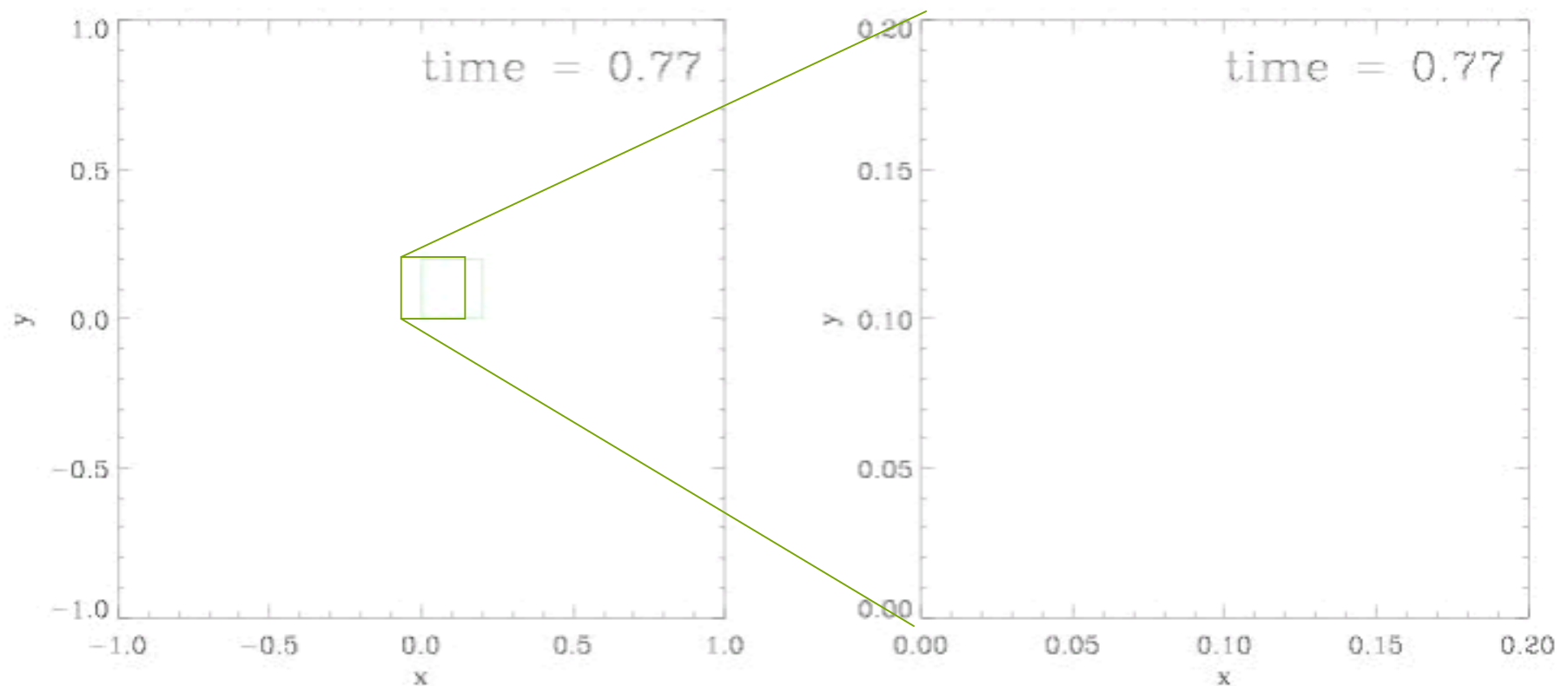


How to get from **cloud cores** to **star clusters**?

How do the stars **acquire mass**?

# Star cluster formation

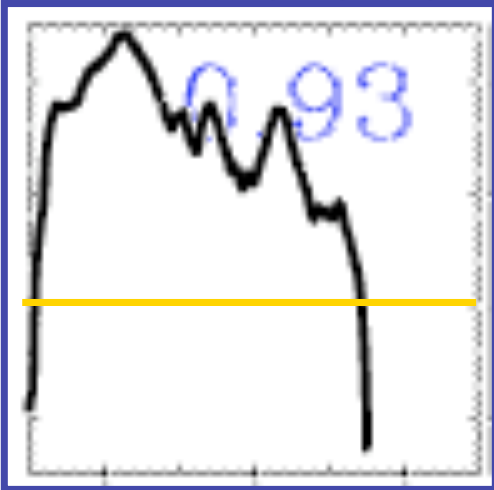
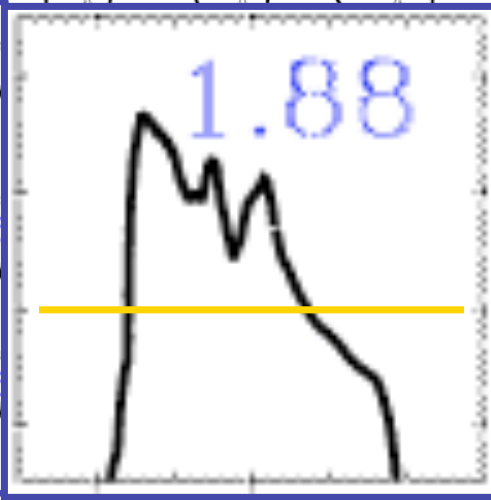
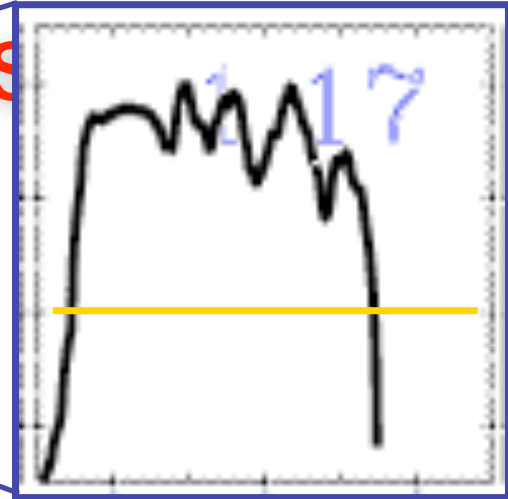
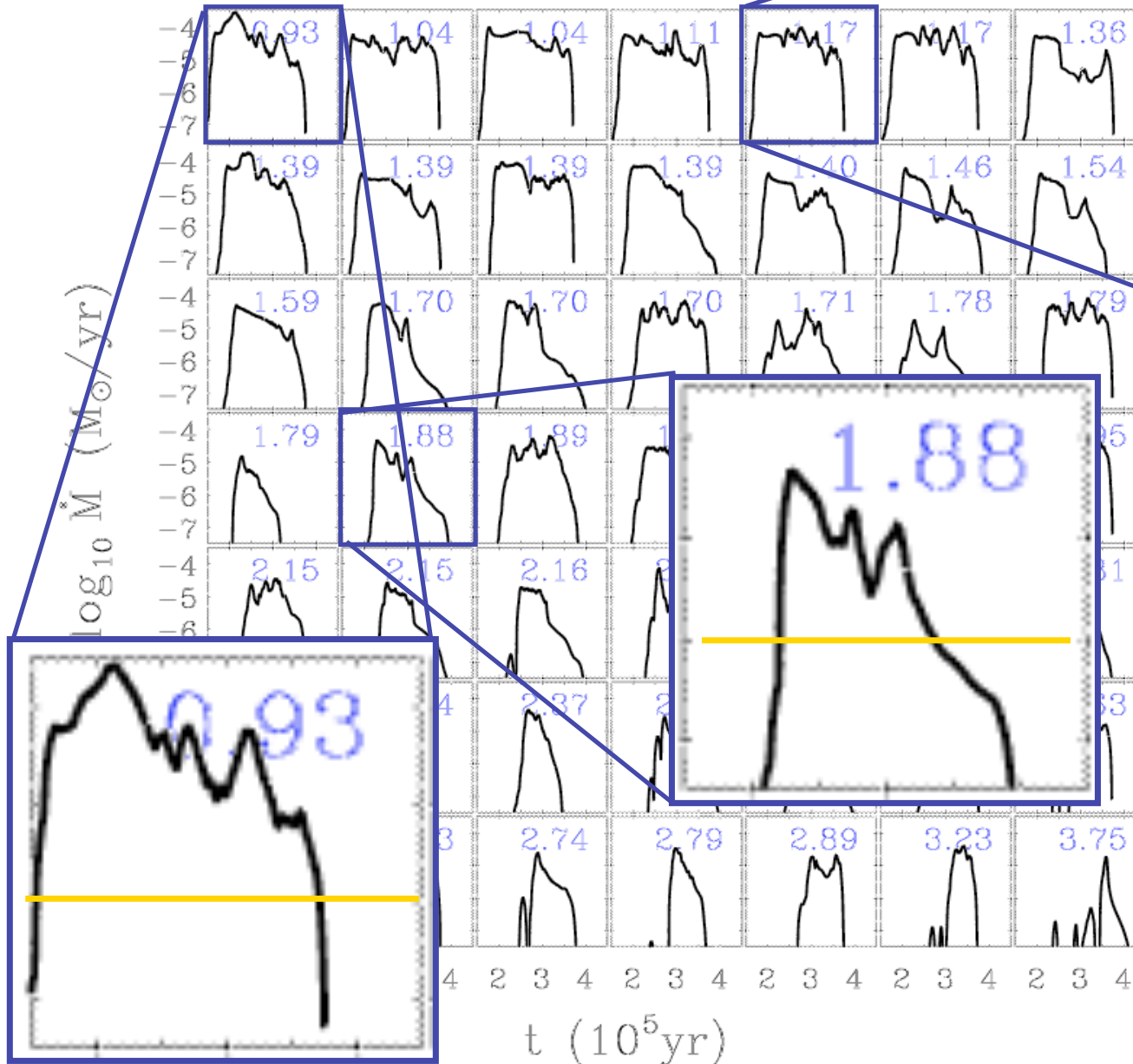
in dense clusters protostellar interaction may become important!



Trajectories of protostars in a nascent dense cluster created by gravoturbulent fragmentation

(from Klessen & Burkert 2000, *ApJS*, 128, 287)

# accretion rates in clus



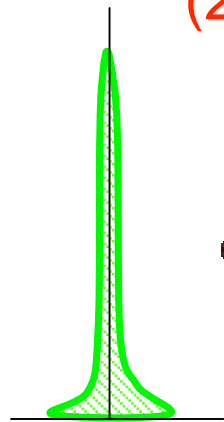
Mass accretion rates *vary with time* and are strongly *influenced* by the *cluster environment*.

(Klessen 2001, ApJ, 550, L77; also Schmeja & Klessen, 2004, A&A, 419, 405)

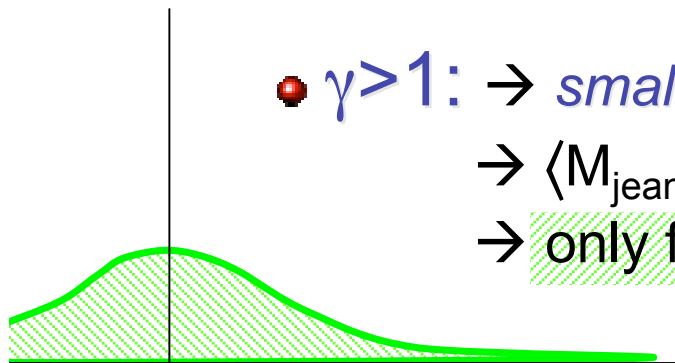
# fragmentation depends on EOS

$$(1) \quad p \propto \rho^\gamma \quad \rightarrow \quad \rho \propto p^{1/\gamma}$$

$$(2) \quad M_{\text{jeans}} \propto \gamma^{3/2} \rho^{(3\gamma-4)/2}$$

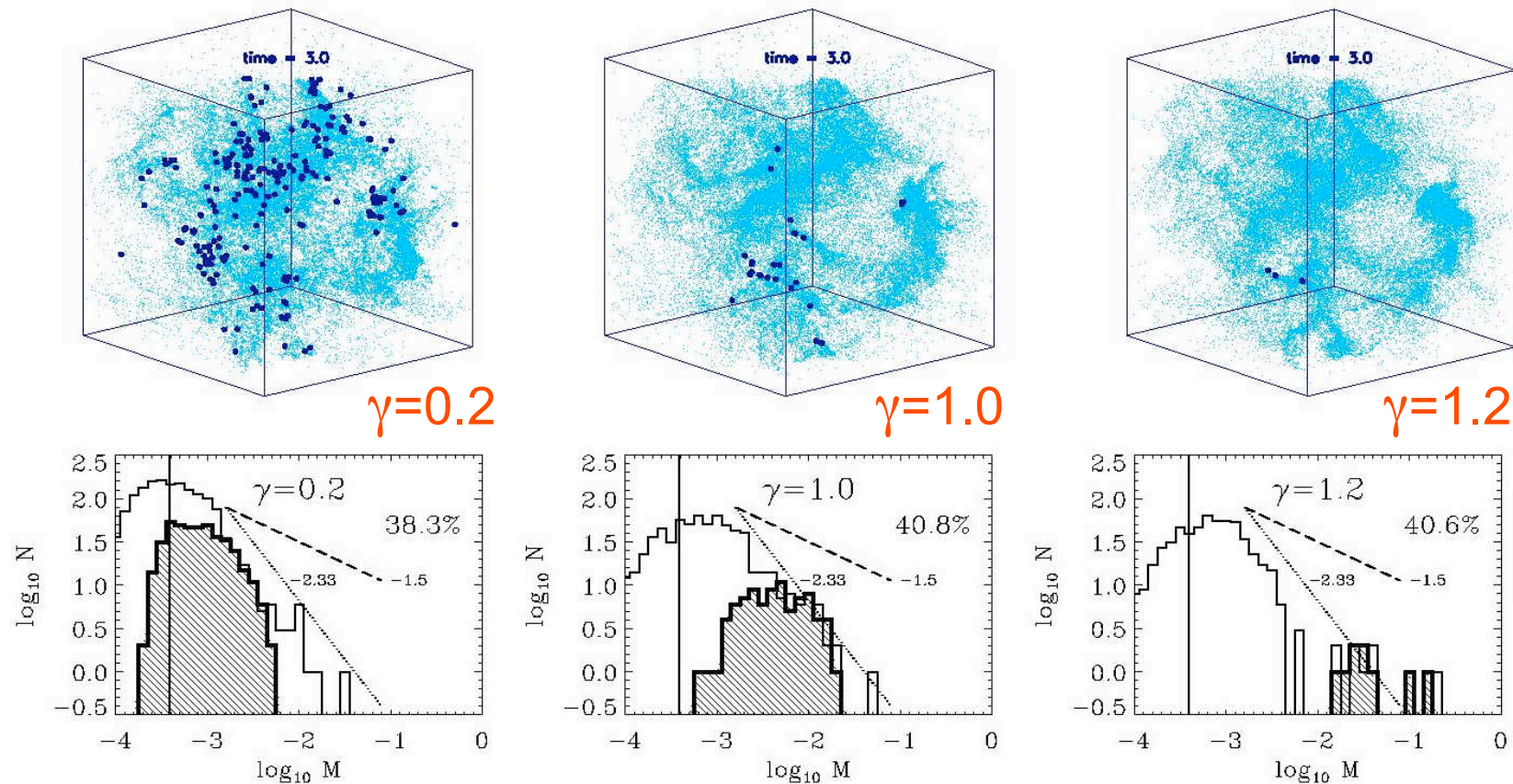


- $\gamma < 1$ :  $\rightarrow$  *large* density excursion for given pressure  
 $\rightarrow$   $\langle M_{\text{jeans}} \rangle$  becomes small  
 $\rightarrow$  number of fluctuations with  $M > M_{\text{jeans}}$  is large



- $\gamma > 1$ :  $\rightarrow$  *small* density excursion for given pressure  
 $\rightarrow$   $\langle M_{\text{jeans}} \rangle$  is large  
 $\rightarrow$  only few and massive clumps exceed  $M_{\text{jeans}}$

# fragmentation depends on EOS



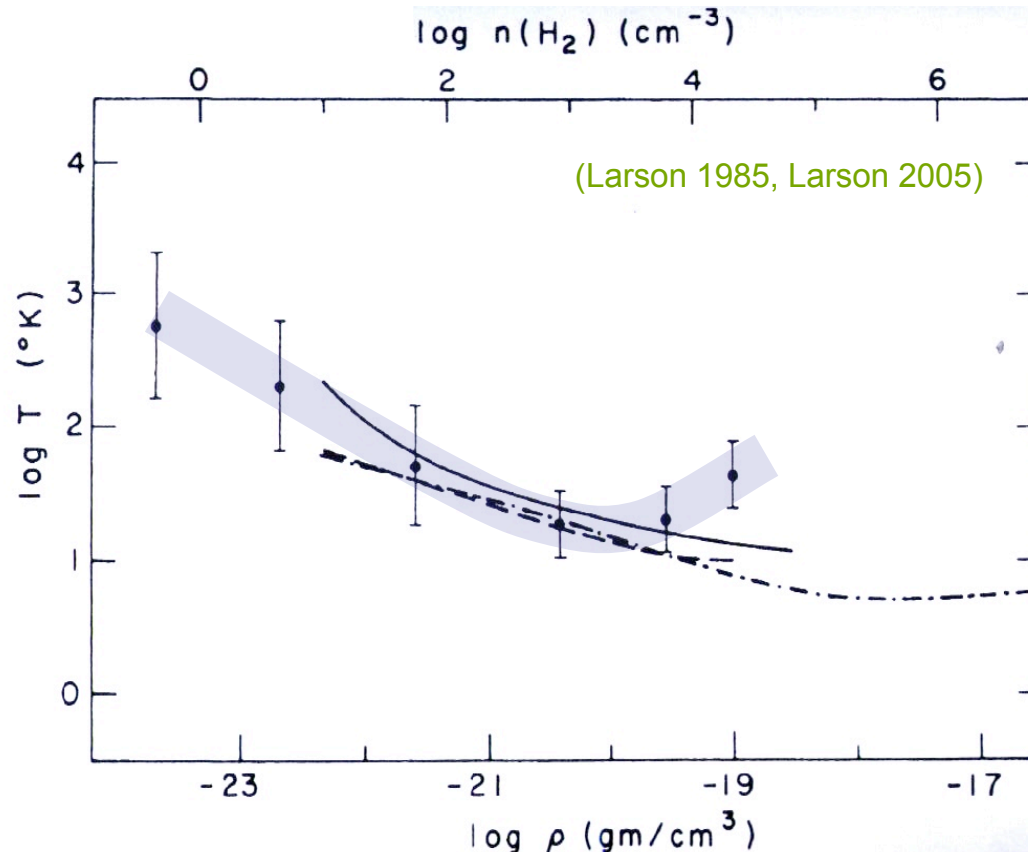
for  $\gamma < 1$  fragmentation is enhanced  $\rightarrow$  *cluster of low-mass stars*  
for  $\gamma > 1$  it is suppressed  $\rightarrow$  formation of *isolated massive stars*

(from Li, Klessen, & Mac Low 2003, ApJ, 592, 975)

# EOS for solar neighborhood

below  $10^{-18} \text{ gcm}^{-3}$ :  $\rho \uparrow \Rightarrow T \downarrow$

above  $10^{-18} \text{ gcm}^{-3}$ :  $\rho \uparrow \Rightarrow T \uparrow$

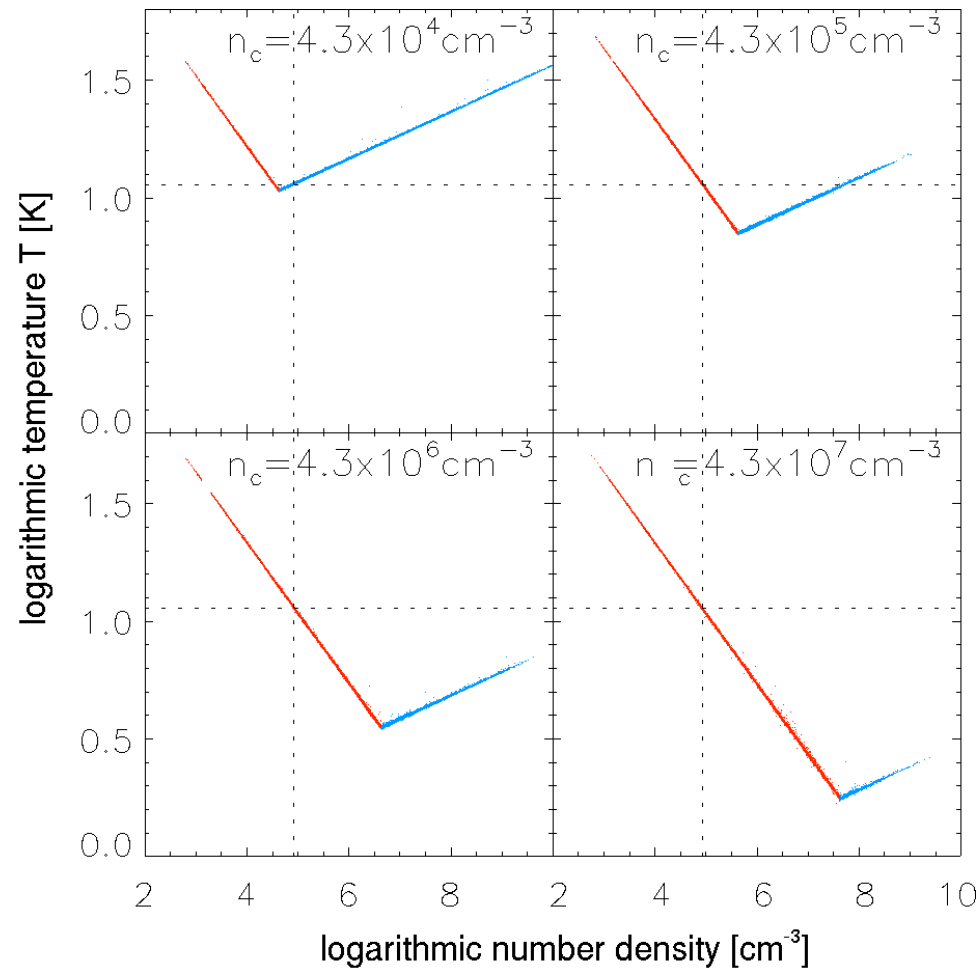


# IMF from simple piece-wise polytropic EOS

$$\gamma_1 = 0.7$$

$$\gamma_2 = 1.1$$

$$T \sim \rho^{\gamma-1}$$

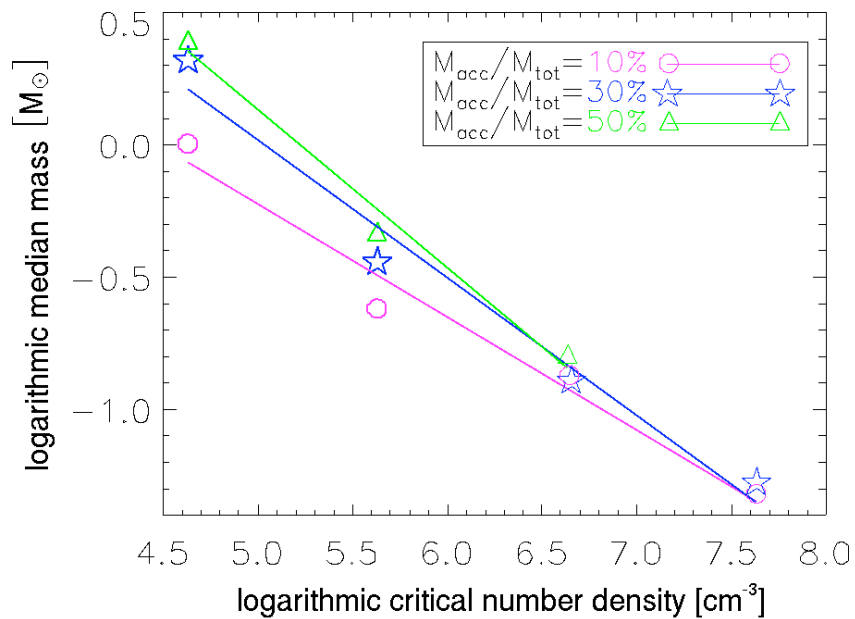


(Jappsen et al. 2005)

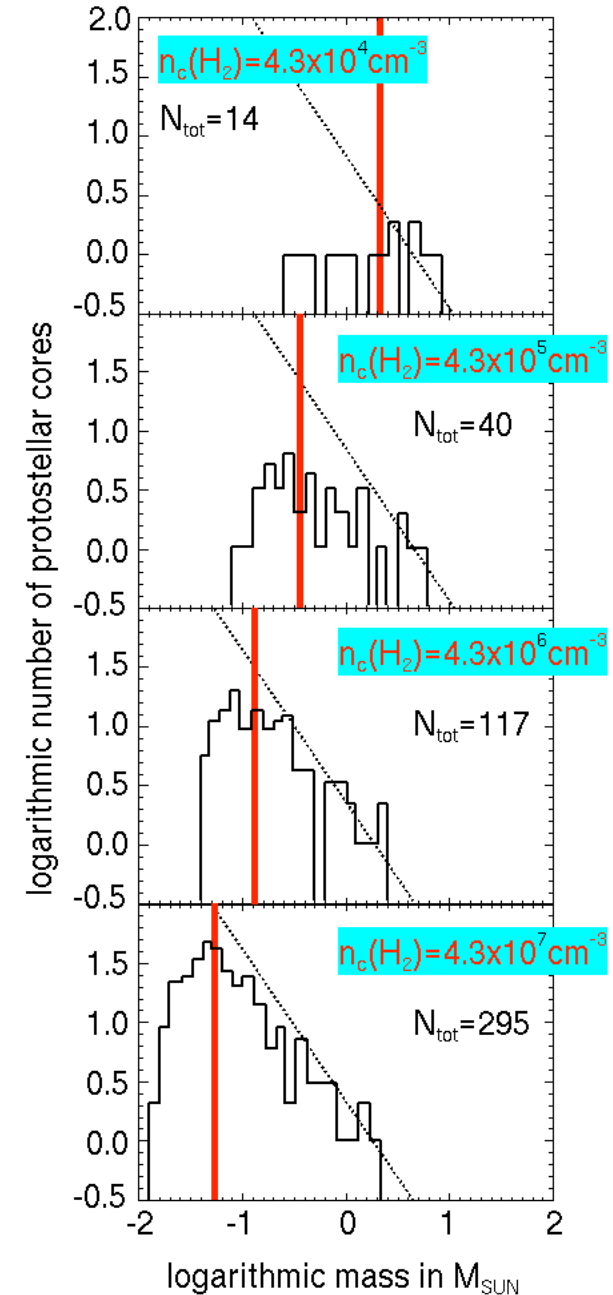


# IMF from simple piece-wise polytropic EOS

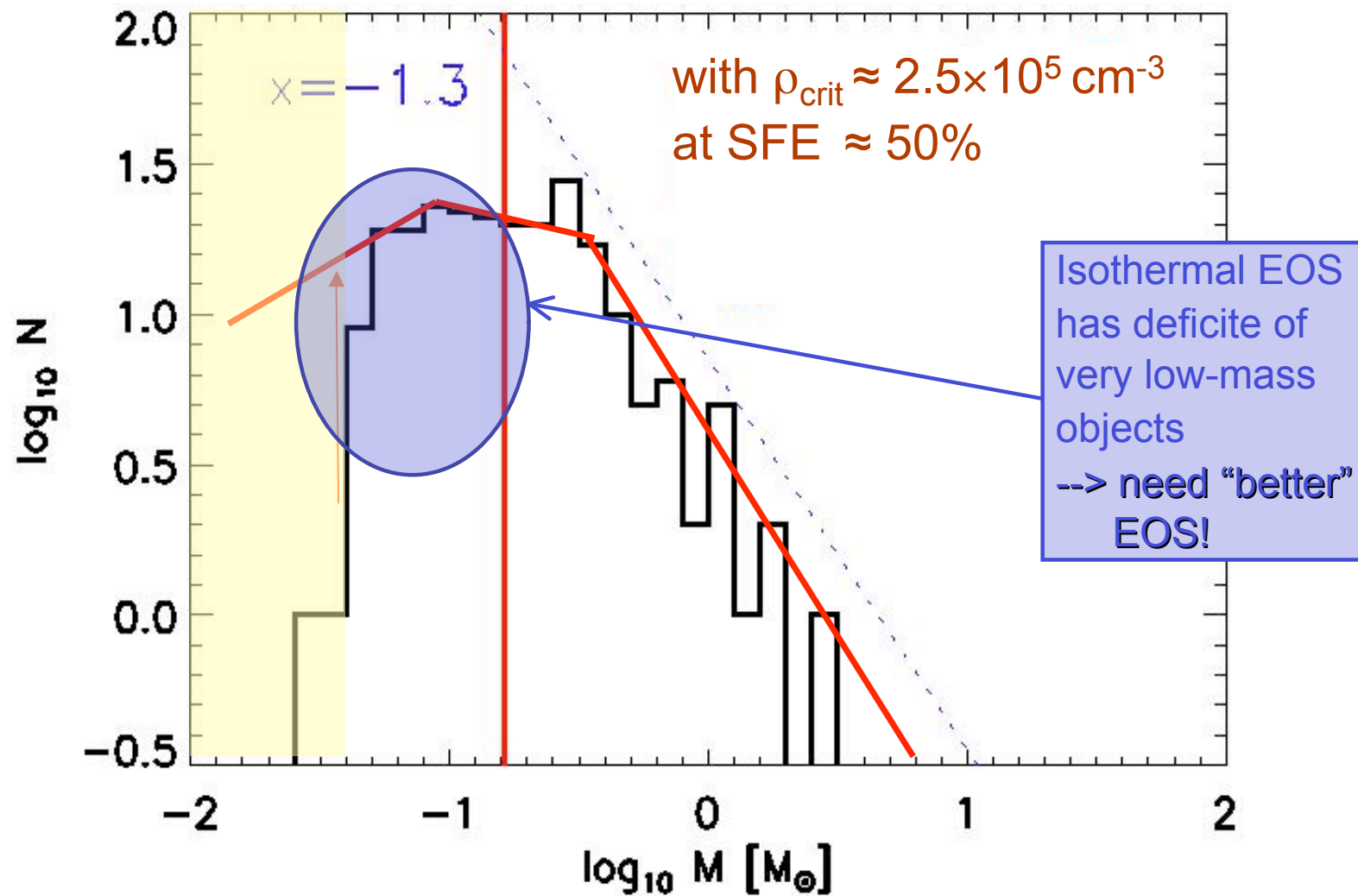
critical density  $\uparrow$   $\Rightarrow$  median mass  $\downarrow$



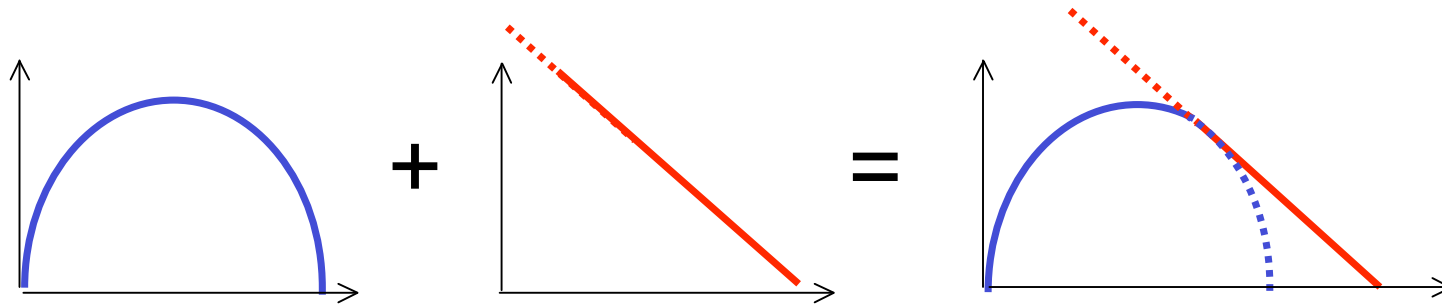
(Jappsen et al. 2005)



# IMF in nearby molecular clouds



# Plausibility argument for shape



- Supersonic turbulence is scale free process

→ *POWER LAW BEHAVIOR*

- *But also:* turbulence and fragmentation are highly stochastic processes → central limit theorem

→ *GAUSSIAN DISTRIBUTION*

# Summary

# summary

- interstellar gas is highly inhomogeneous
  - *thermal instability*
  - *gravitational instability*
  - *turbulent compression* (in shocks  $\delta\rho/\rho \approx M^2$ ; in atomic gas:  $M \approx 1...3$ )
- cold *molecular clouds* form rapidly in high-density regions
  - chemical *phase transition*: atomic  $\rightarrow$  molecular
  - process is *modulated* by large-scale *dynamics* in the galaxy
- inside *cold clouds*: turbulence is highly supersonic ( $M \approx 1...20$ )  
 $\rightarrow$  *turbulence* creates density structure, *gravity* selects for collapse  
 $\longrightarrow$  **GRAVOTUBULENT FRAGMENTATION**
- *turbulent cascade*: local compression *within* a cloud provokes collapse
- individual *stars* and *star clusters* form through *sequence* of highly *stochastic* events:
  - *collapse* of cloud cores in turbulent cloud (cores change during collapse)
  - plus mutual *interaction* during collapse (importance depends on ratio of potential energy to turbulent energy) (buzz word: *competitive accretion*)

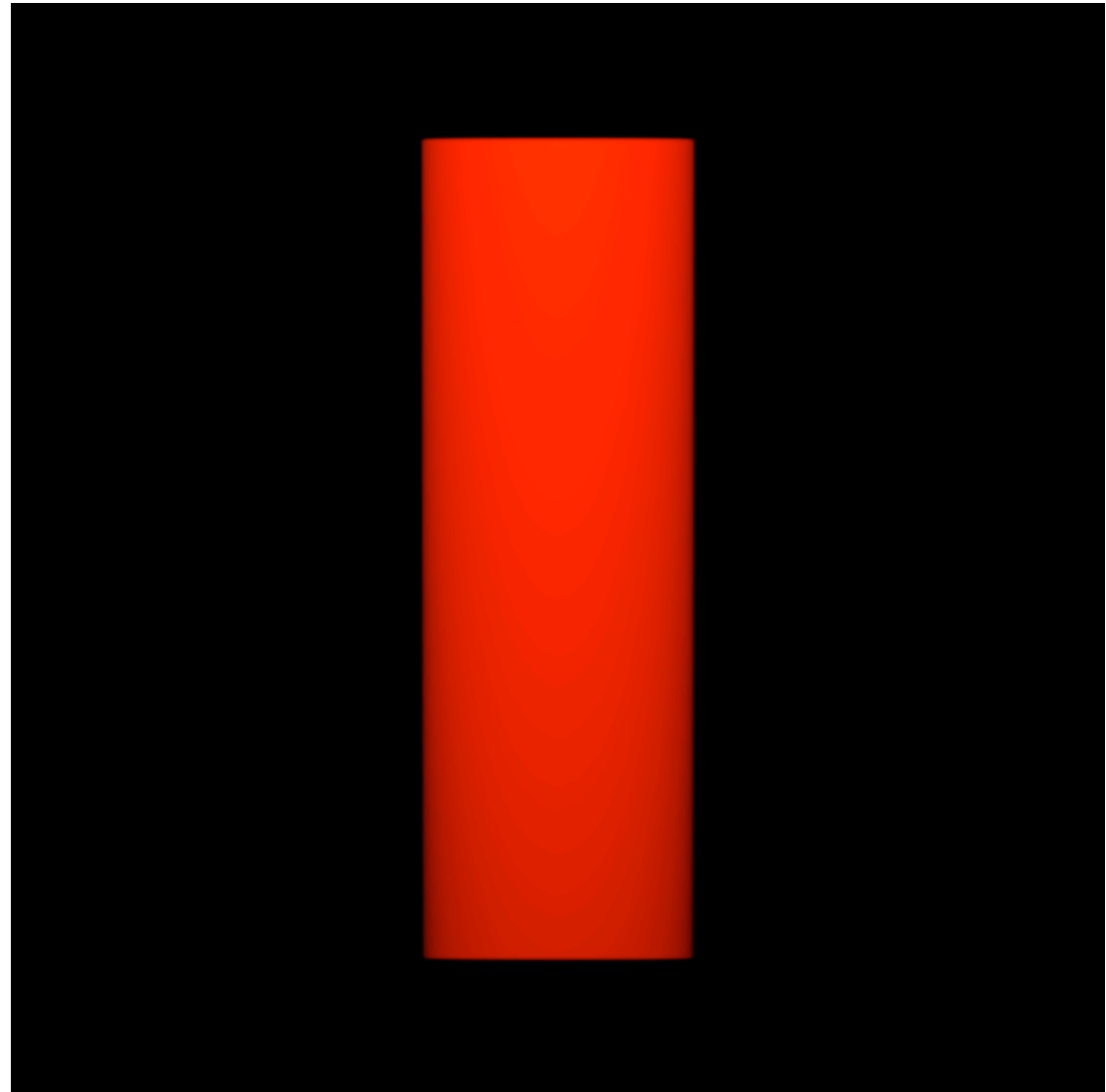
Thanks!

# Gravitational collapse within MCs

today: SPH with  
 $N > 10^7$  particles

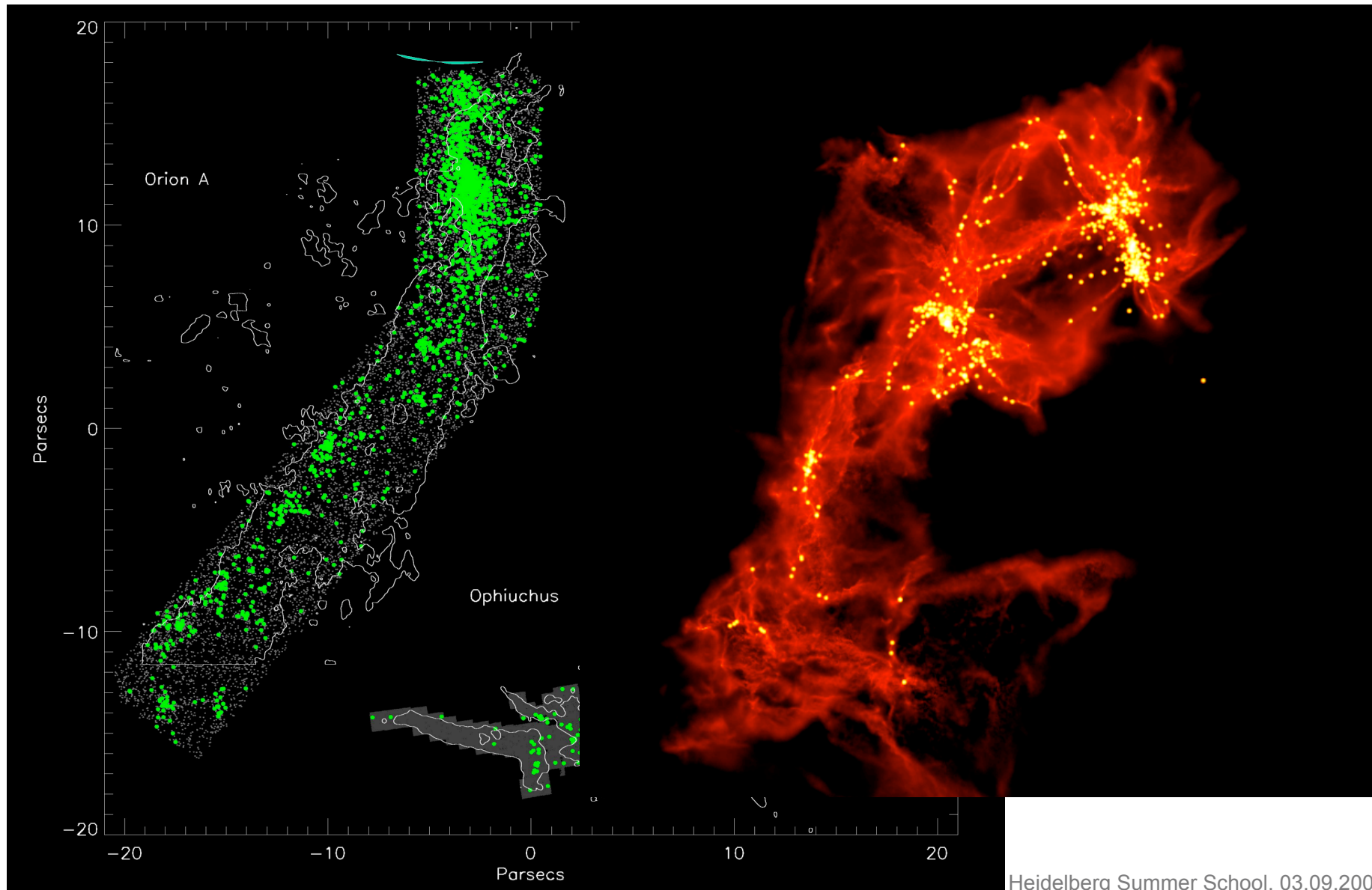
model for the Orion cloud:  
 $M = 10^4 M_{\text{sun}}$ , isothermal  
EOS

still no *chemistry*, no  
*stellar feedback*, no  
*radiation*



(Bonnell et al. 2006)

# Gravitational collapse within MCs





# Gravitational collapse within MCs

immediate future: SPH with radiation feedback (first validation runs)

