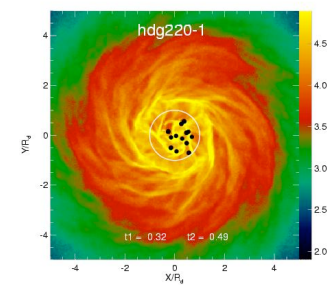
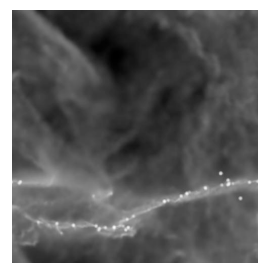
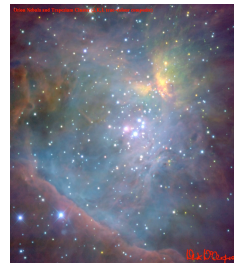
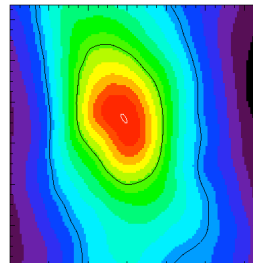
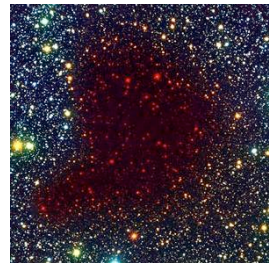


Star Formation in the Turbulent Interstellar Gas



Ralf Klessen

Zentrum für Astronomie der Universität Heidelberg
Institut für Theoretische Astrophysik



Agenda

- phenomenology
 - from large to small scales
- interplay between gravity and turbulence
- examples and predictions
 - star cluster formation: dynamics
 - star cluster formation: thermodynamics
 - > stellar initial mass function

phenomenology

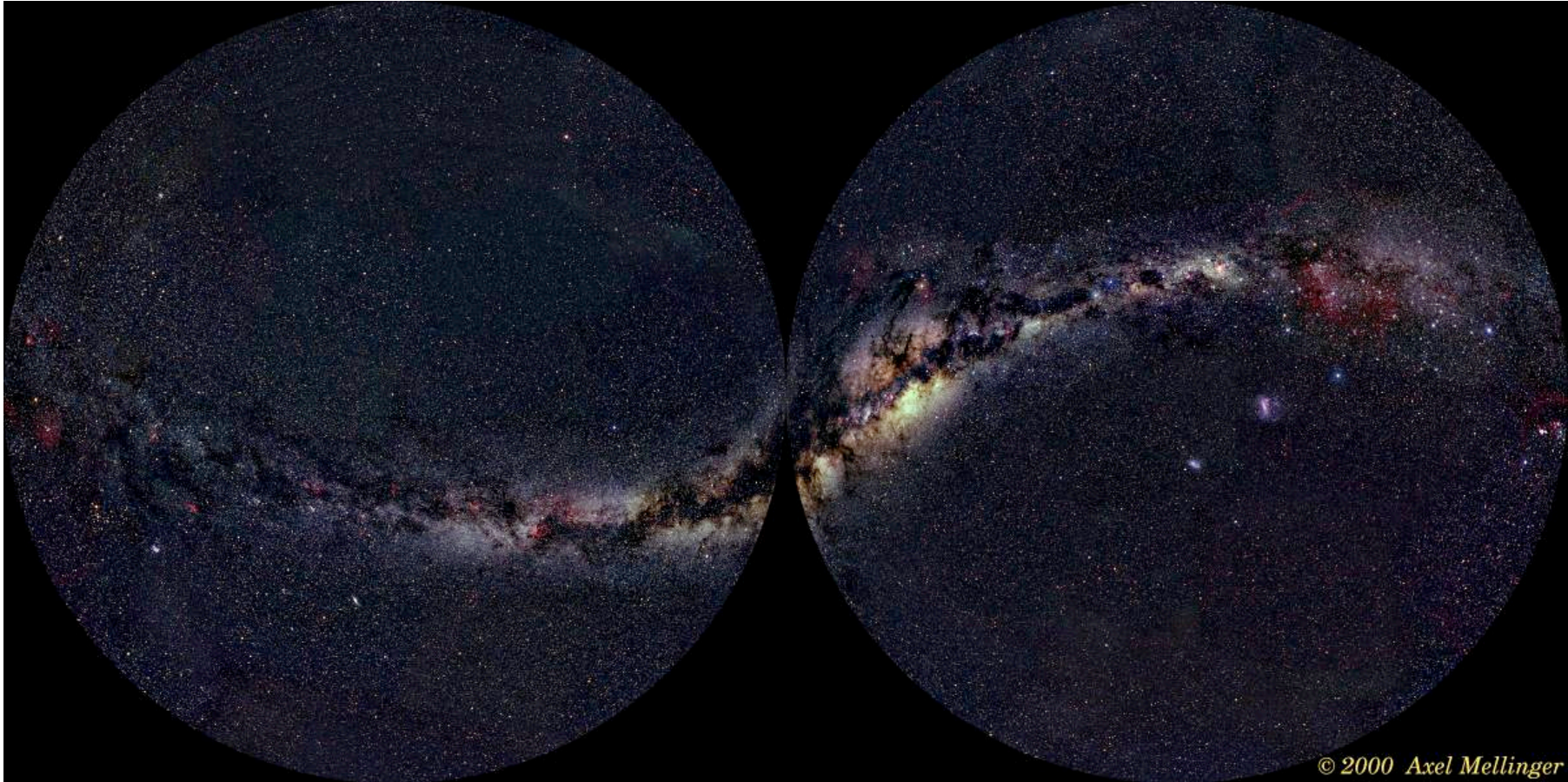
young stars in spiral galaxies



(NGC 4622 from the Hubble Heritage Team)

- Star formation *always* is associated with *clouds of gas and dust*.
- Star formation is essentially a *local phenomenon* (on \sim pc scale)
- **HOW** is star formation is *influenced* by *global* properties of the galaxy?

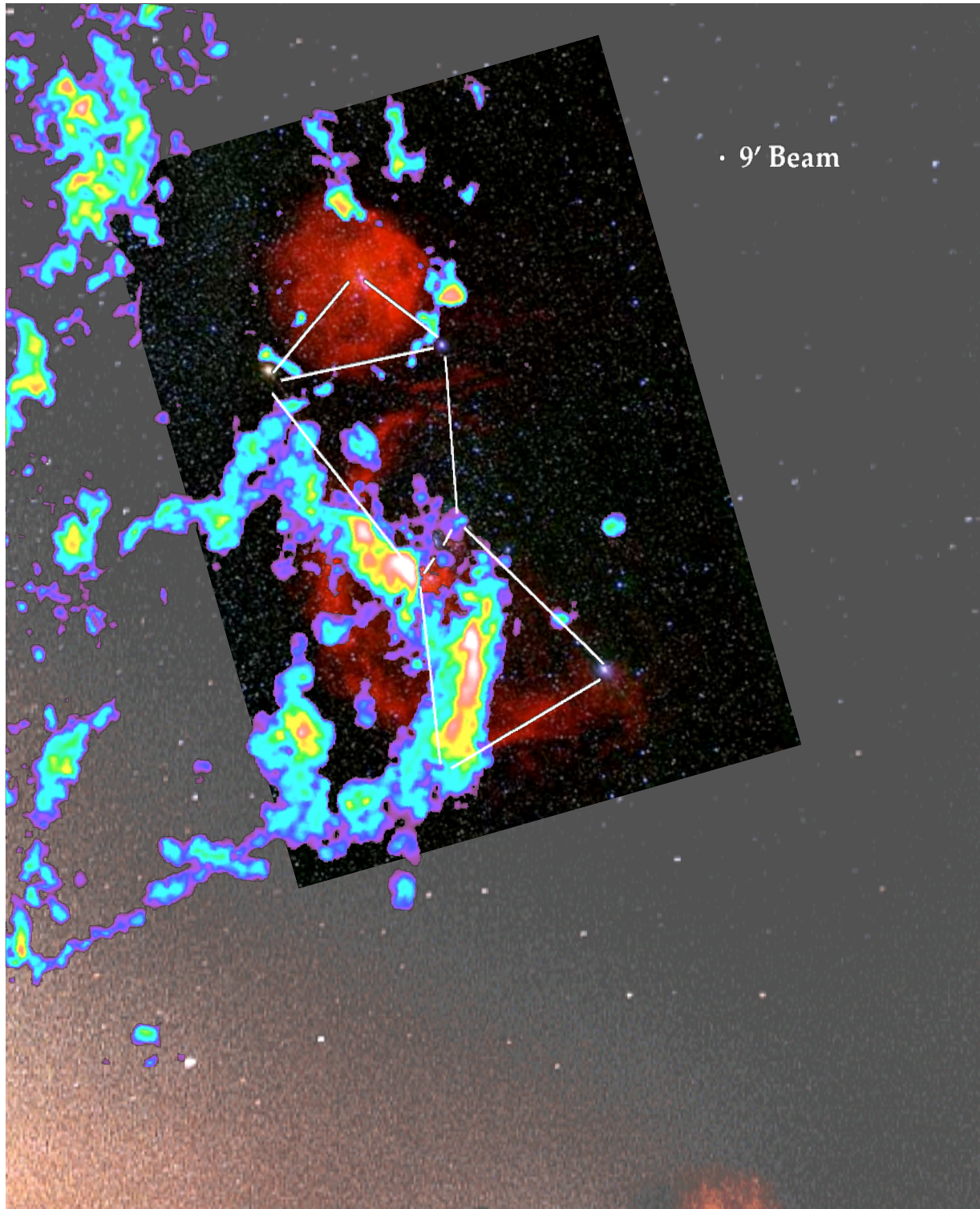
young stars in the Milky Way



On the night sky, you see **stars** and **dark clouds**:

The brightest stars are massive and therefore young.

→ Star formation is important for understanding the structure of our Galaxy

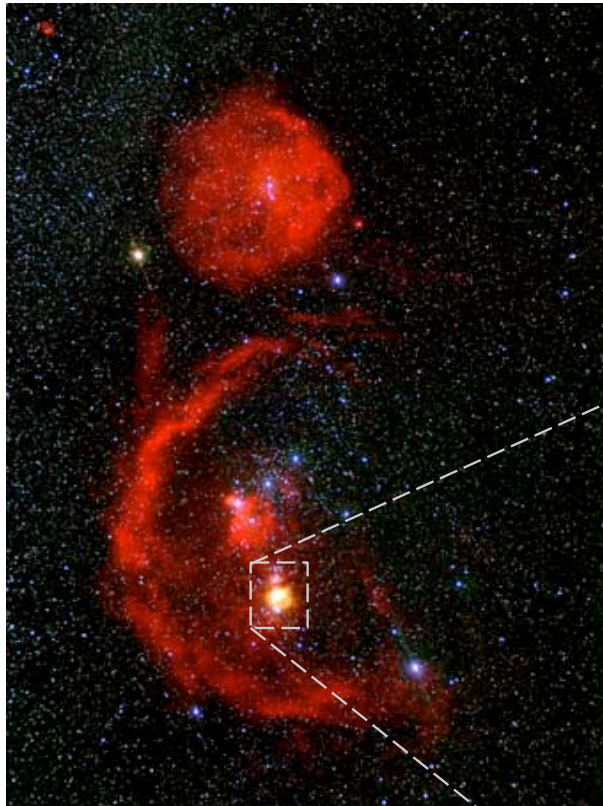


Star formation in Orion

We see

- *Stars* (in visible light)
- Atomic hydrogen (in $H\alpha$ -- red)
- Molecular hydrogen H_2 (radio emission -- color coded)

Local star forming region: The Trapezium Cluster in Orion



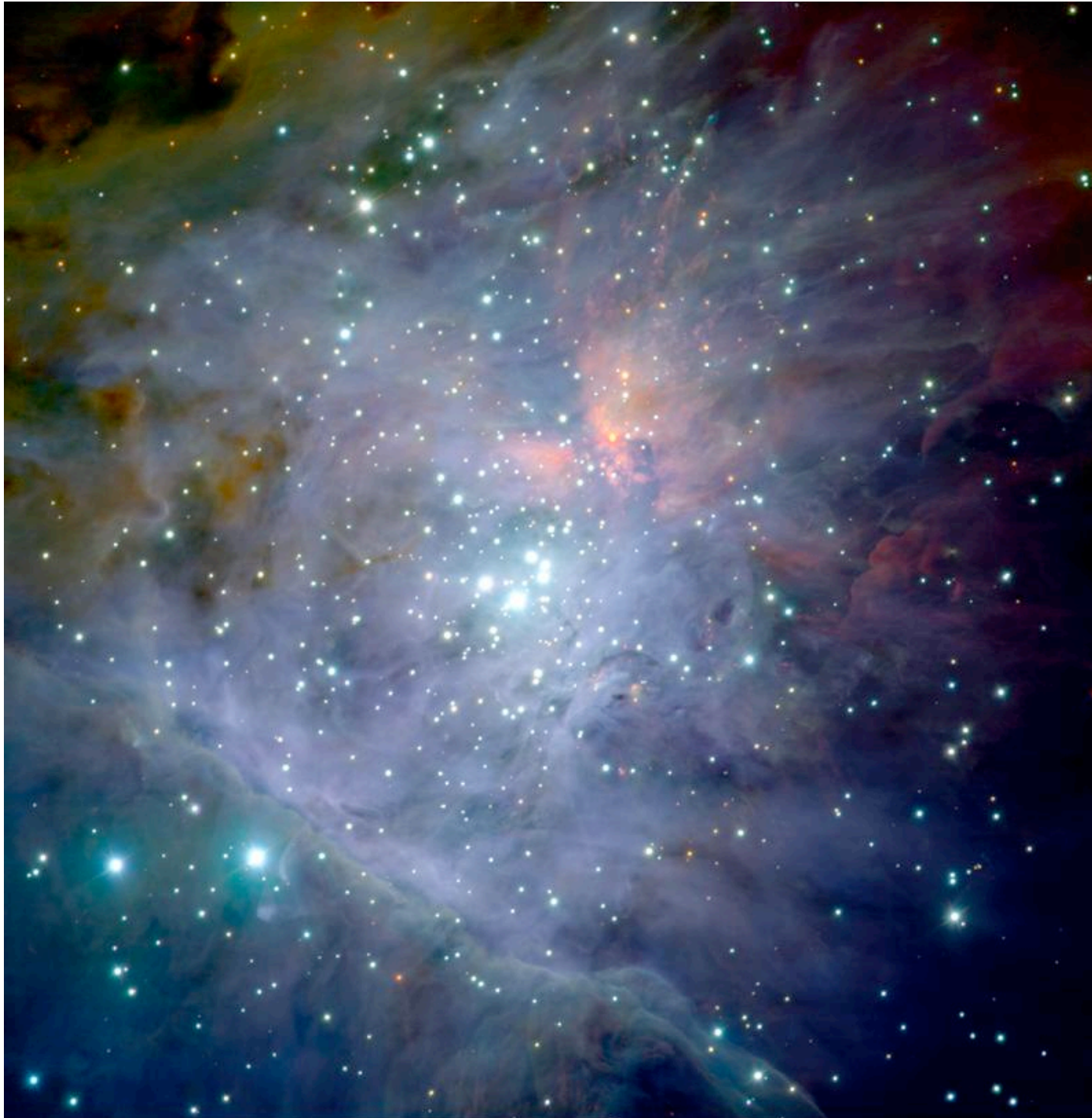
Orion molecular cloud

The Orion molecular cloud is the birth- place of several young embedded star clusters.

The Trapezium cluster is only visible in the IR and contains about 2000 newly born stars.



Trapezium cluster



Trapezium Cluster (detail)

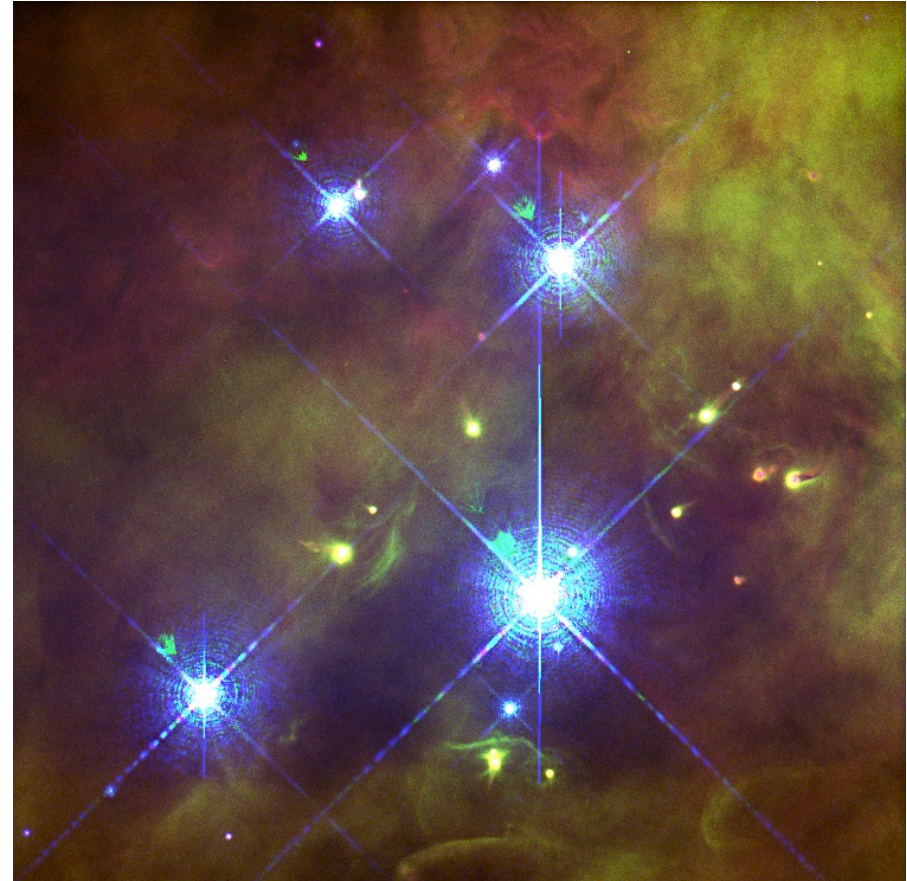
- stars form in **clusters**
- stars form in **molecular clouds**
- (proto)stellar **feedback** is important

(color composite J,H,K
by M. McCaughrean,
VLT, Paranal, Chile)

Trapezium Cluster: Central Region

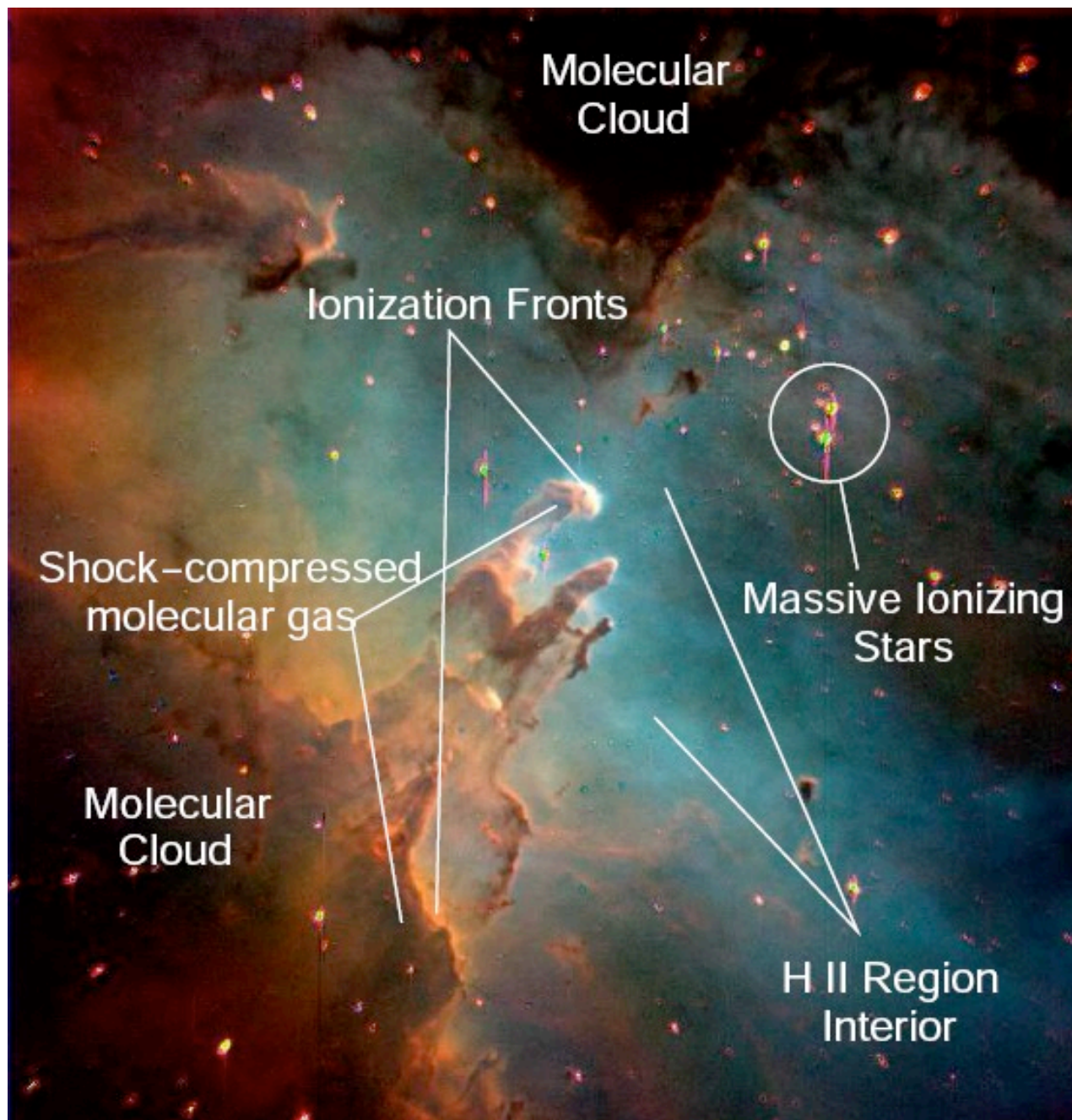


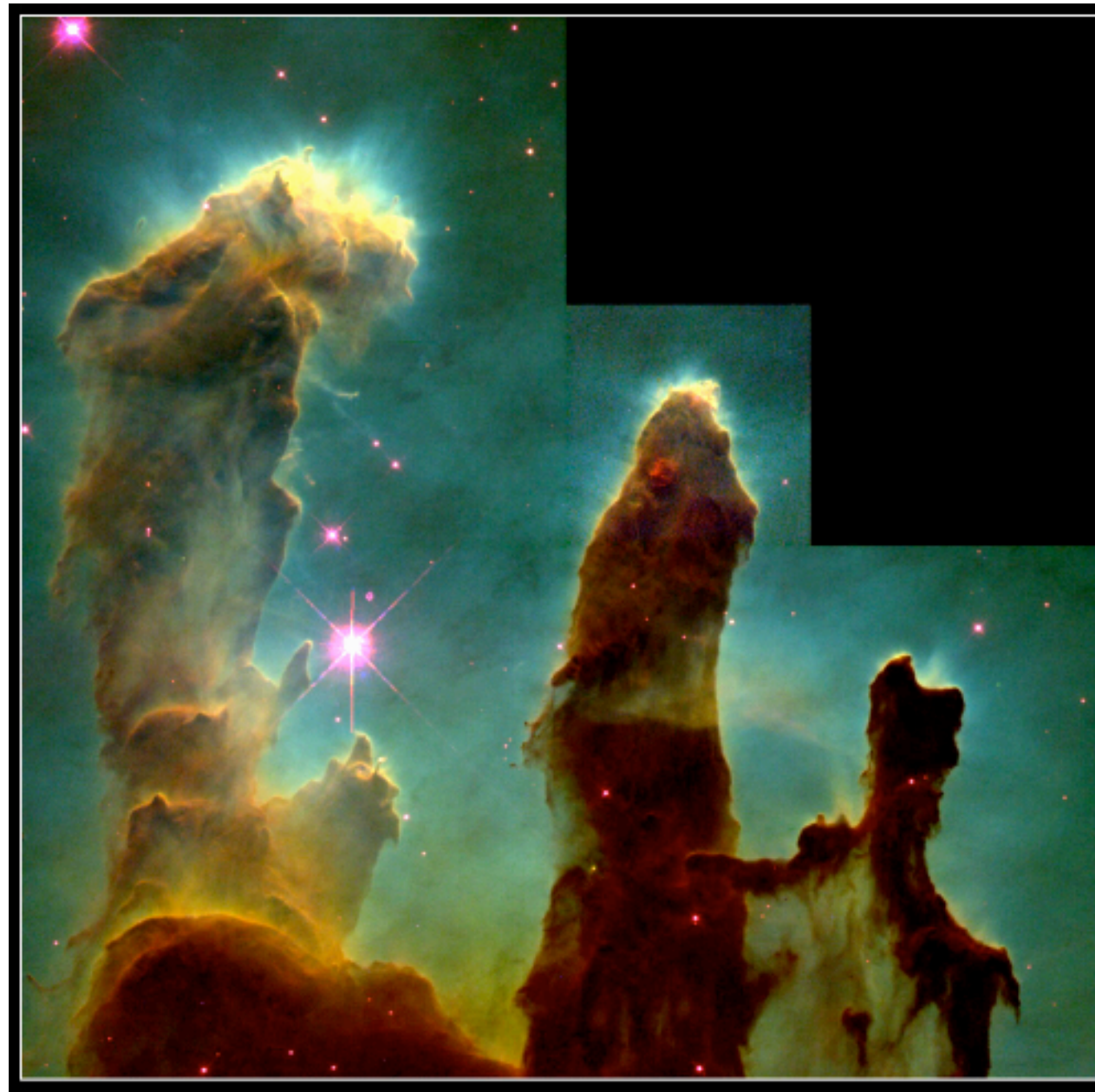
Ionizing radiation from central star
Theta 1C Orionis



Proplyds: Evaporating ``protoplanetary`` disks
around young low-mass protostars

alles in einem Bild

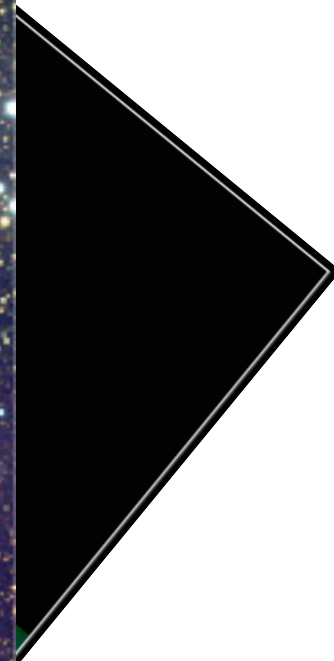




HST Aufnahme

Pillars of God (in Eagle Nebula): Formation of small groups of young stars in the tips of the columns of gas and dust

Infrared
observation





IR observation with ESO-VLT

Head of Column No.1 in Eagle Nebula (IR-View)
(VLT ANTU + ISAAC)

ESO PR Photo 37c/01 (20 December 2001)

© European Southern Observatory



Pillars of God (in Eagle Nebula): Formation of small groups of young stars in the tips of the columns of gas and dust



IR observation with ESO-VLT

Head of Column No.2 in Eagle Nebula (IR-View)
(VLT ANTU + ISAAC)

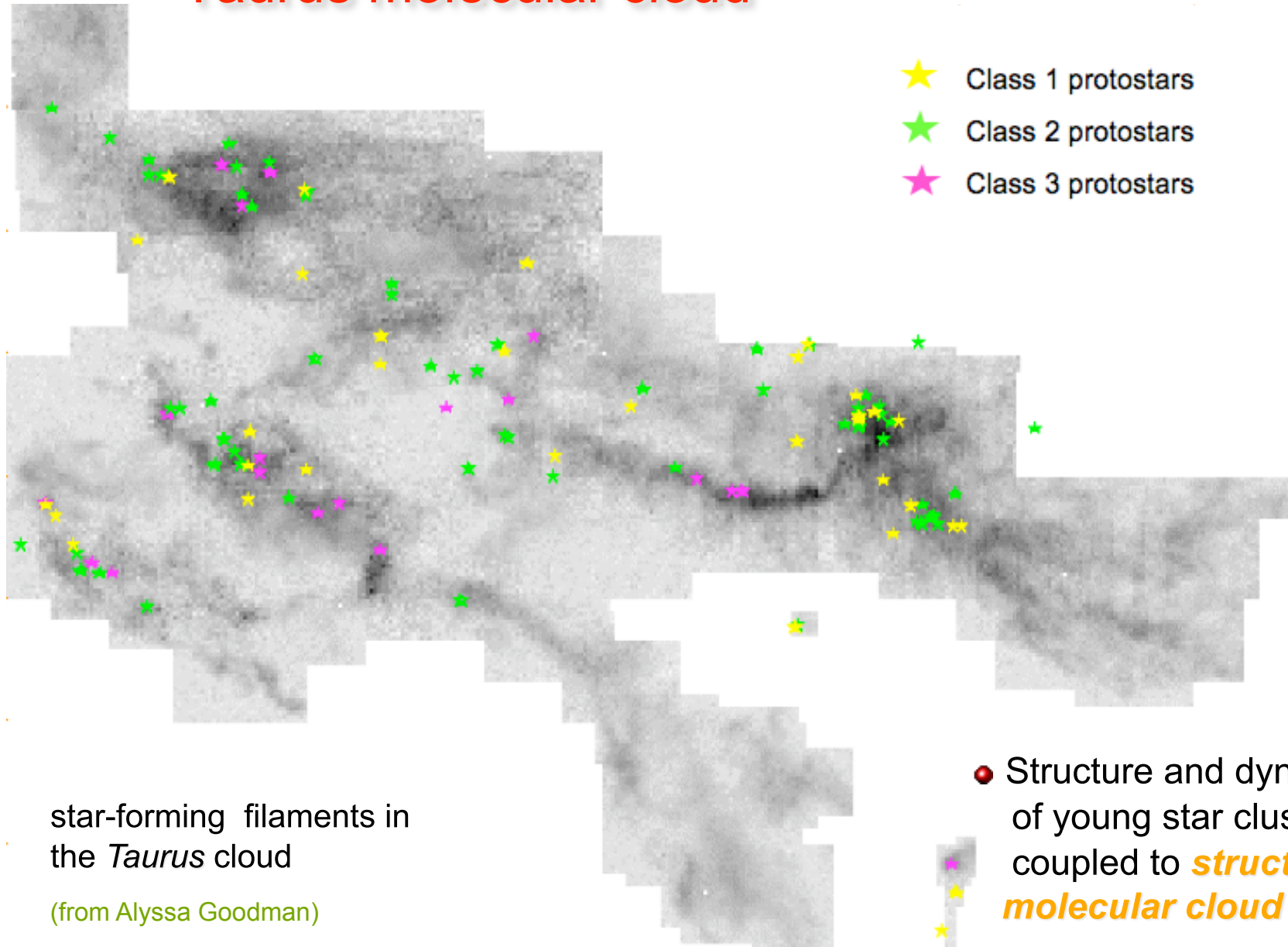
ESO PR Photo 37d/01 (20 December 2001)

© European Southern Observatory



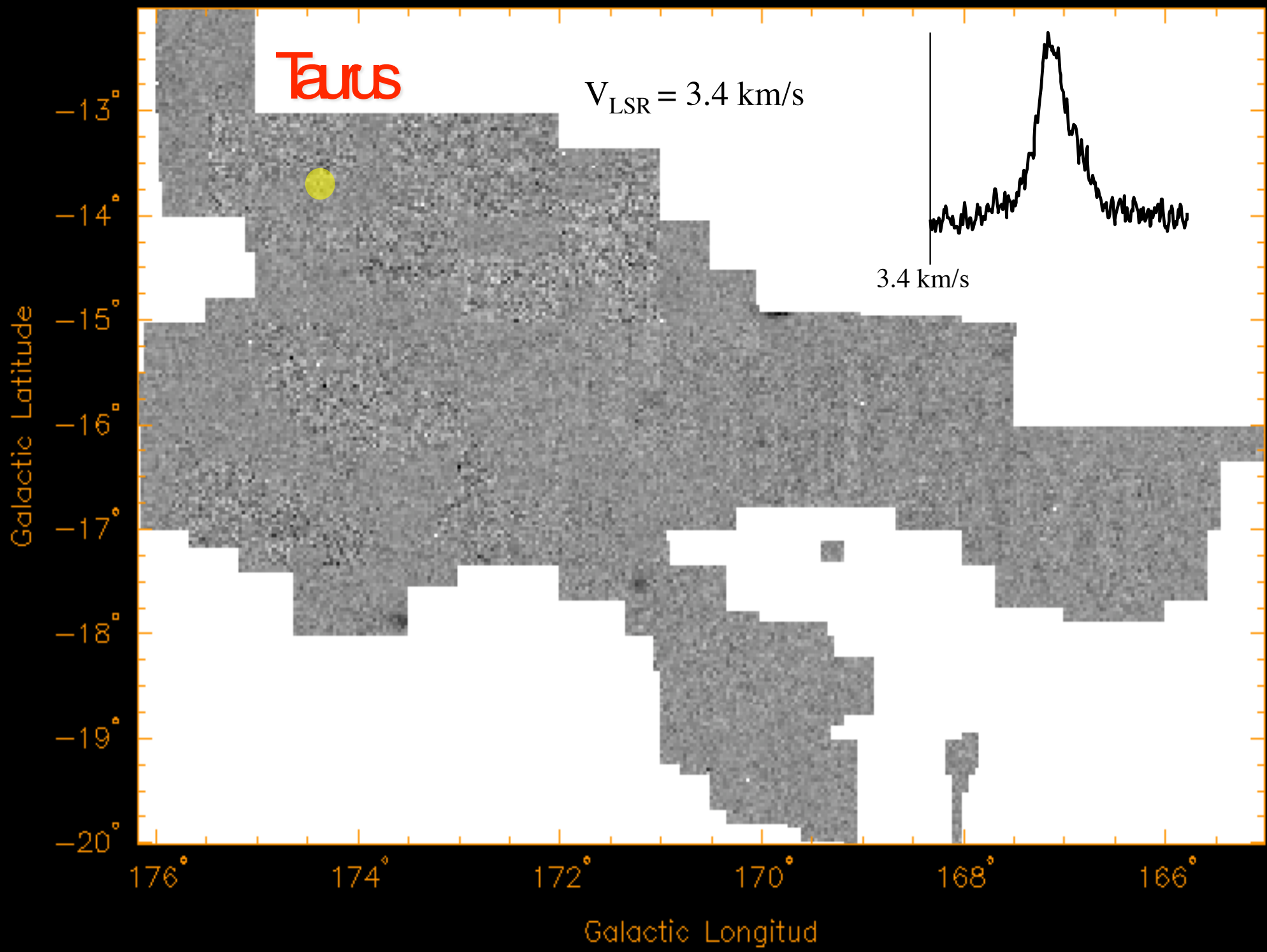
Pillars of God (in Eagle Nebula): Formation of small groups of young stars in the tips of the columns of gas and dust

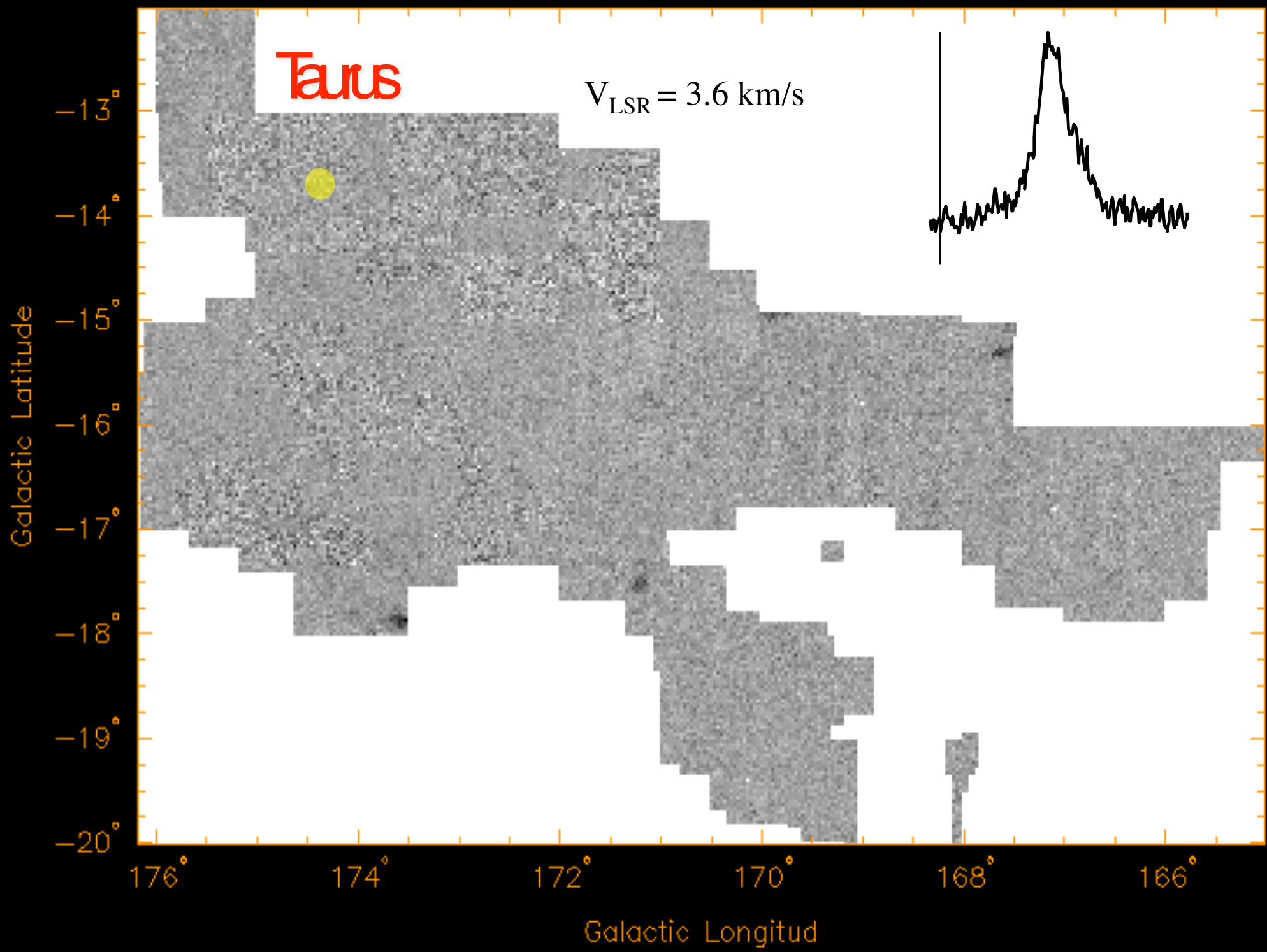
Taurus molecular cloud

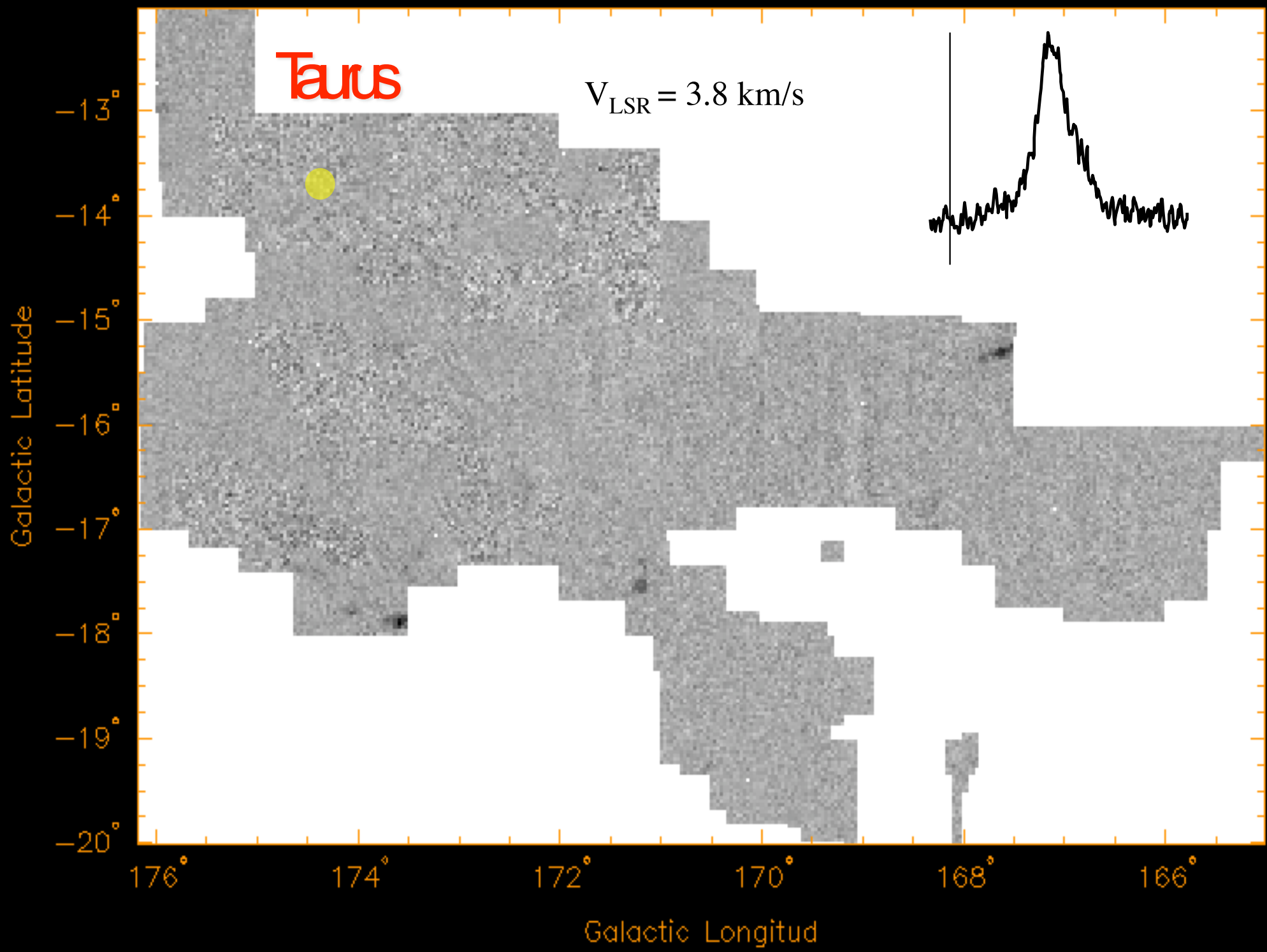


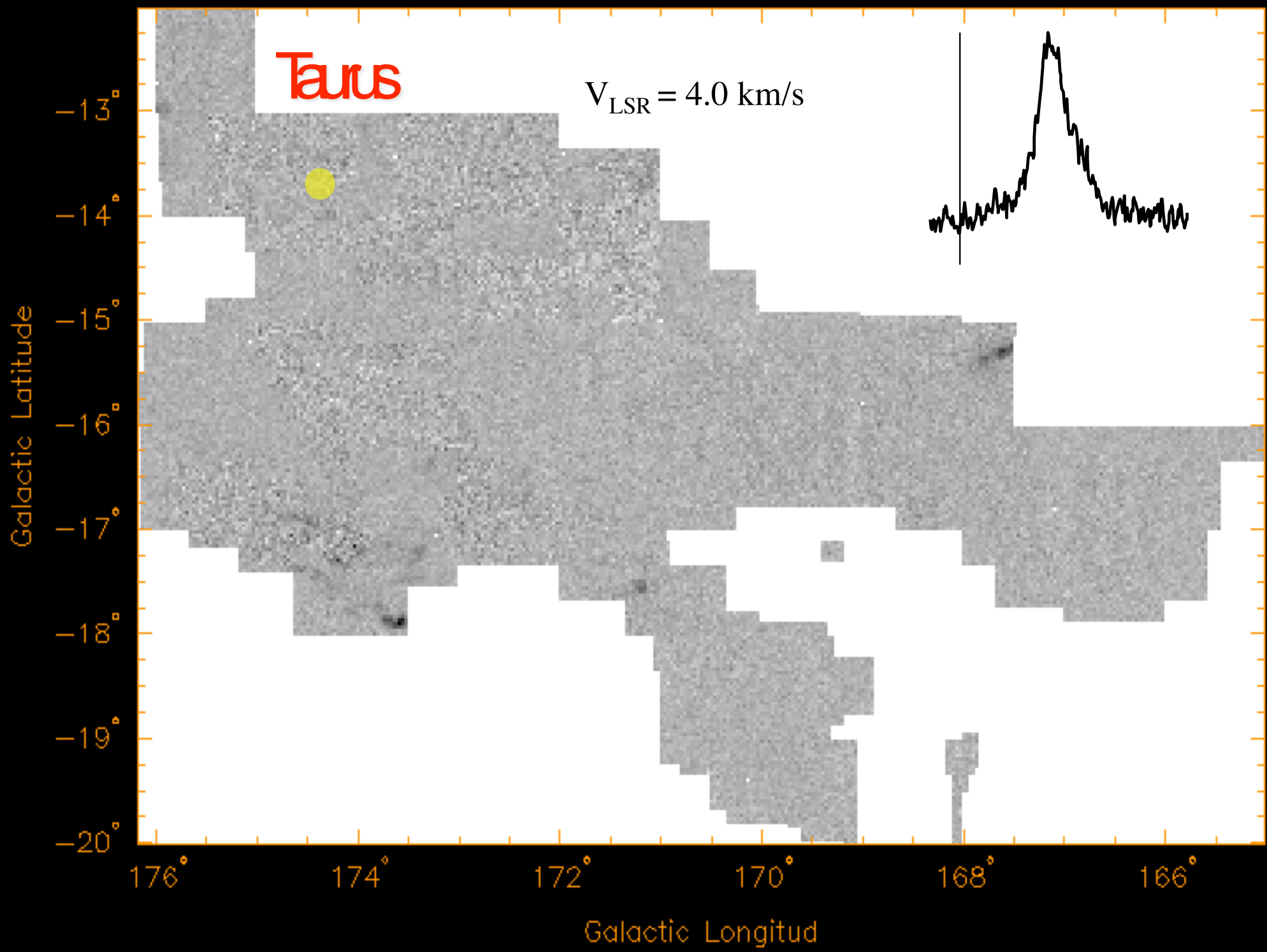
star-forming filaments in the *Taurus* cloud

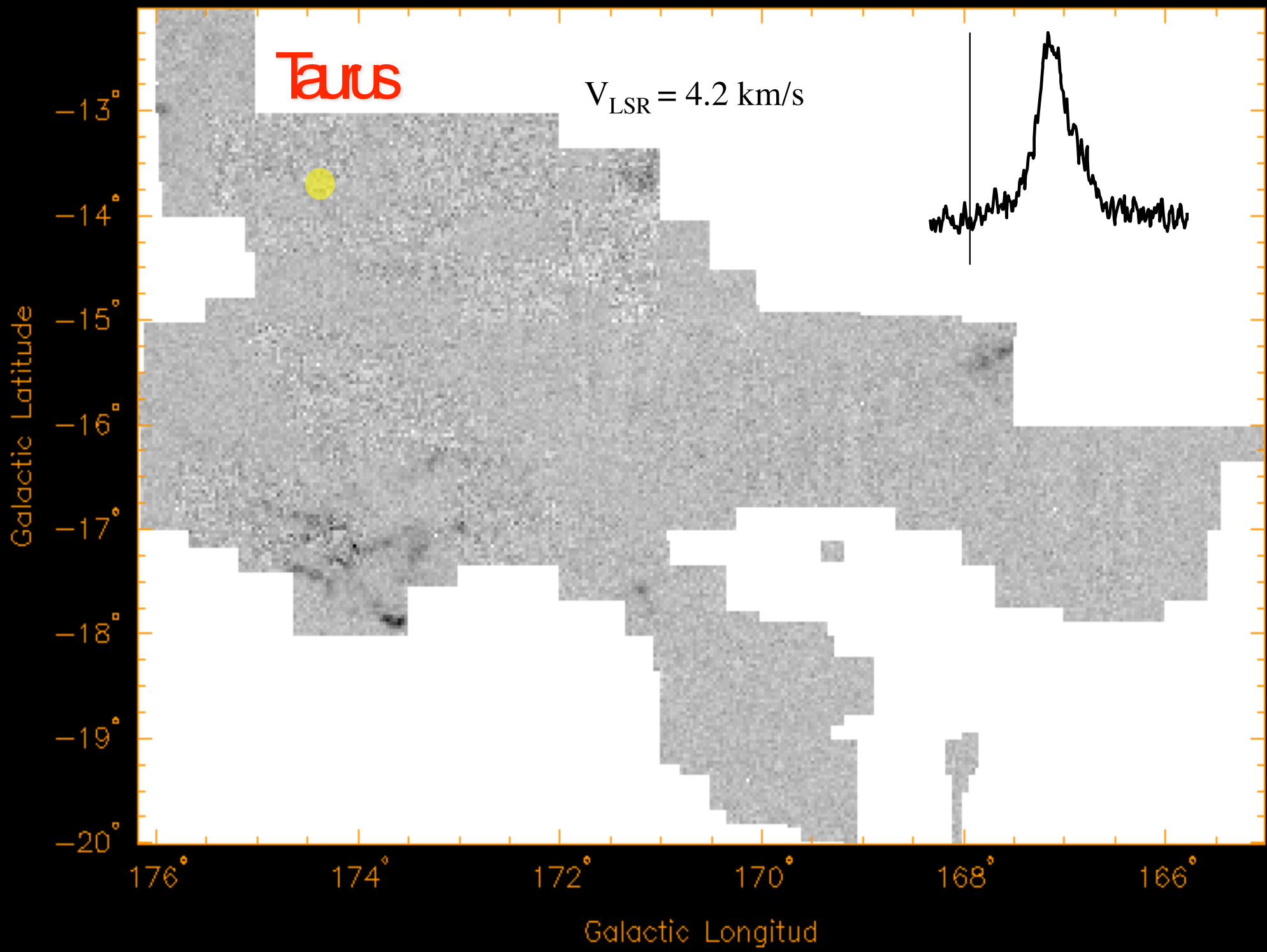
(from Alyssa Goodman)

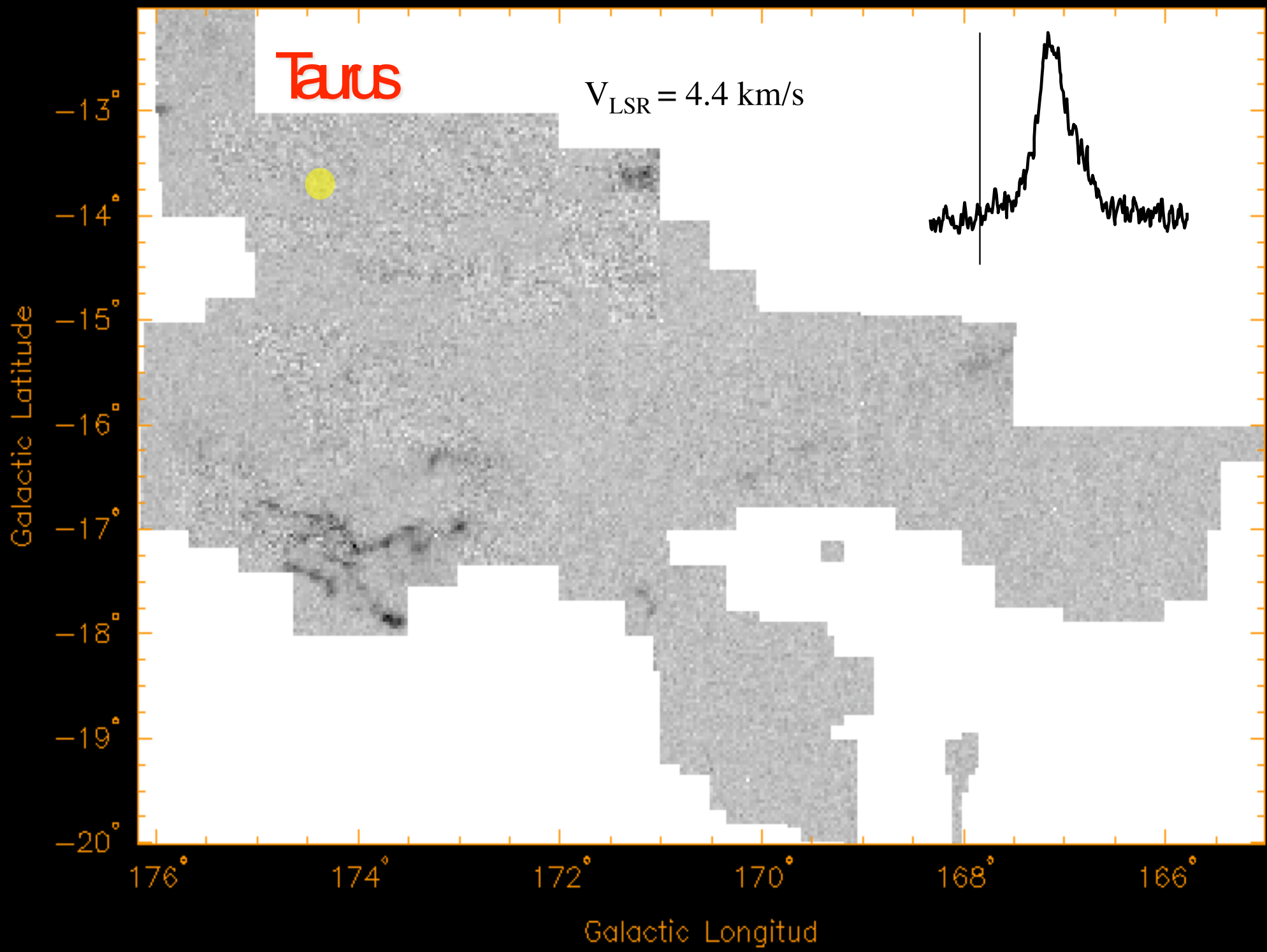


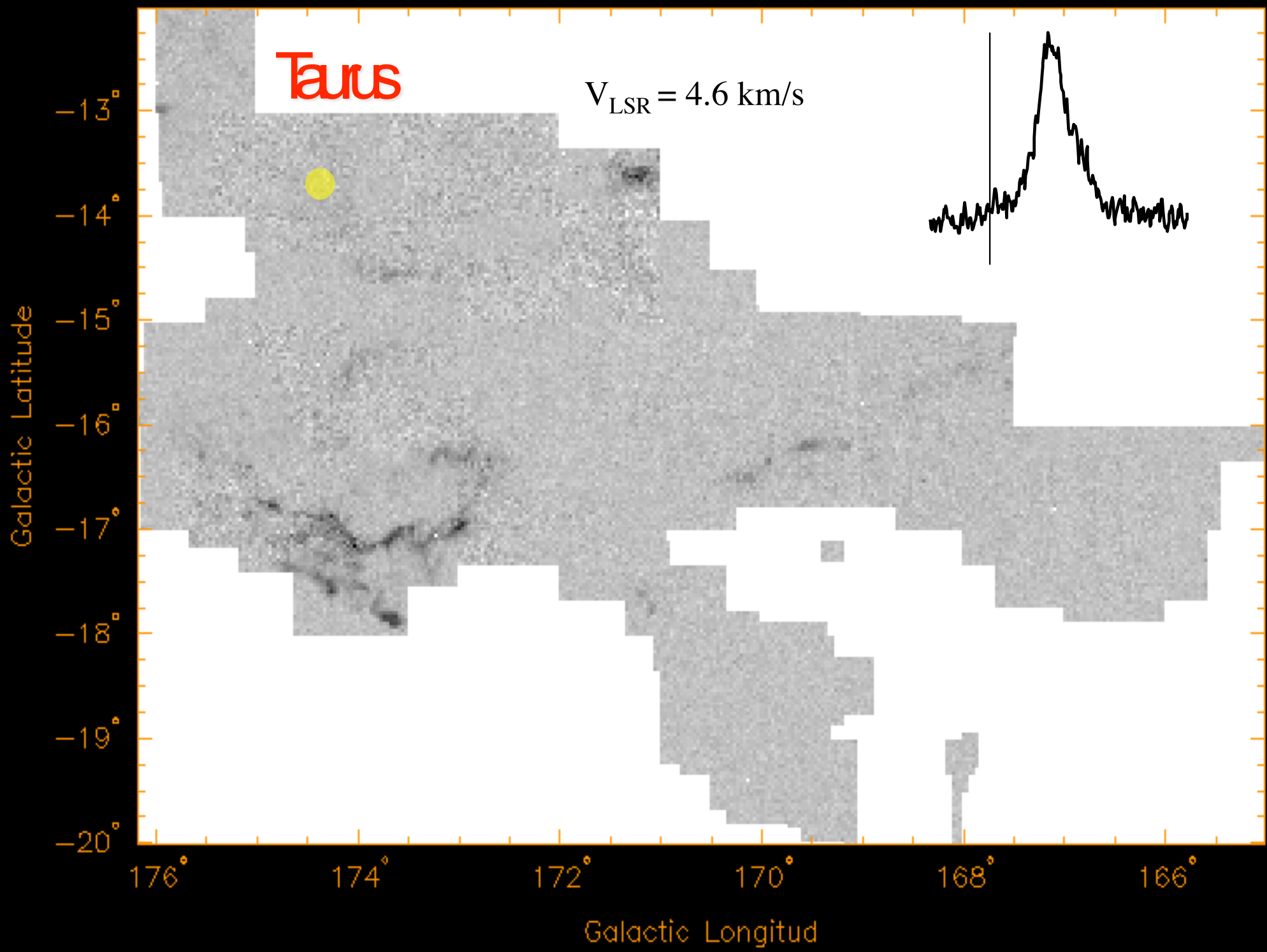


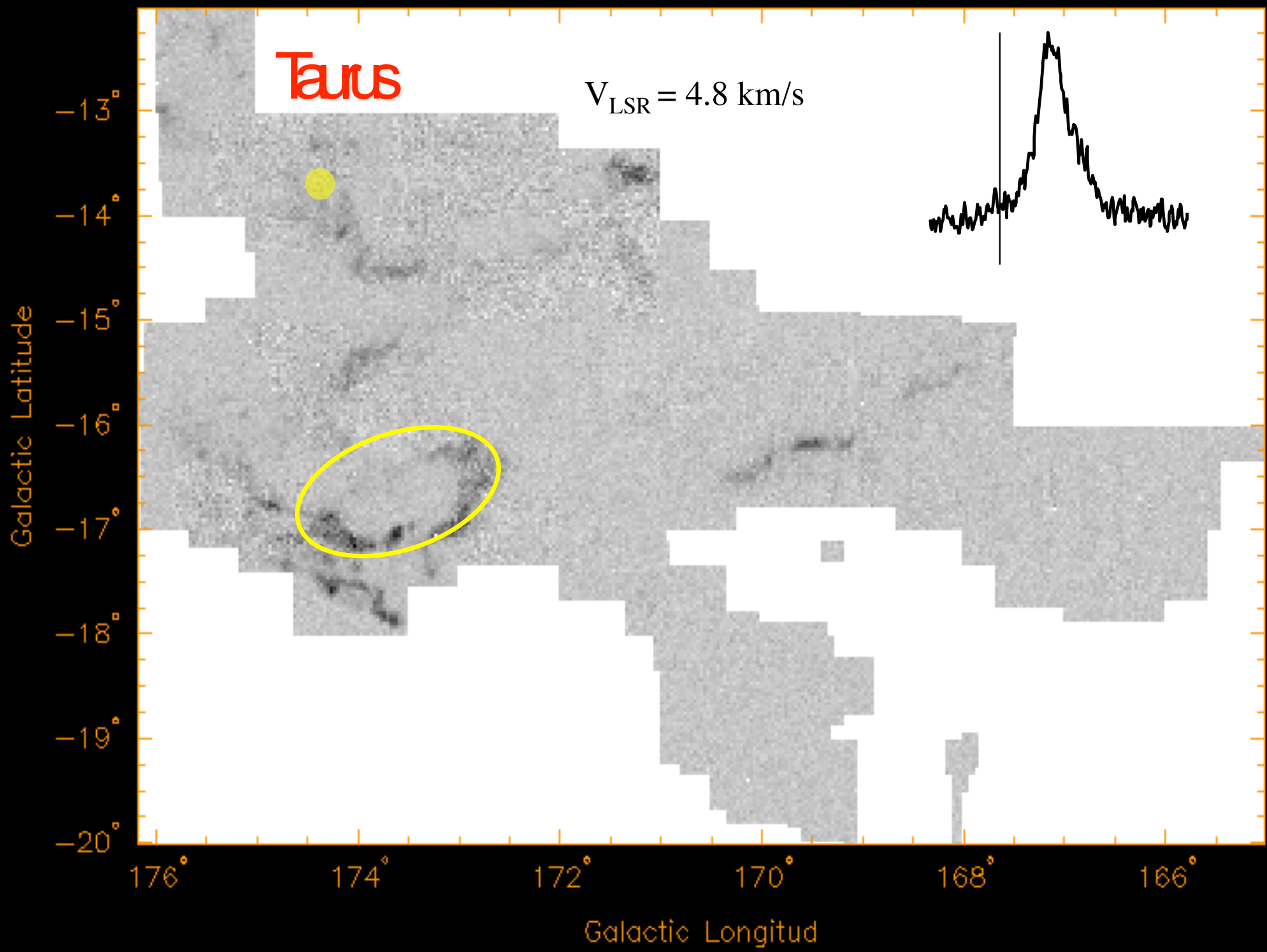


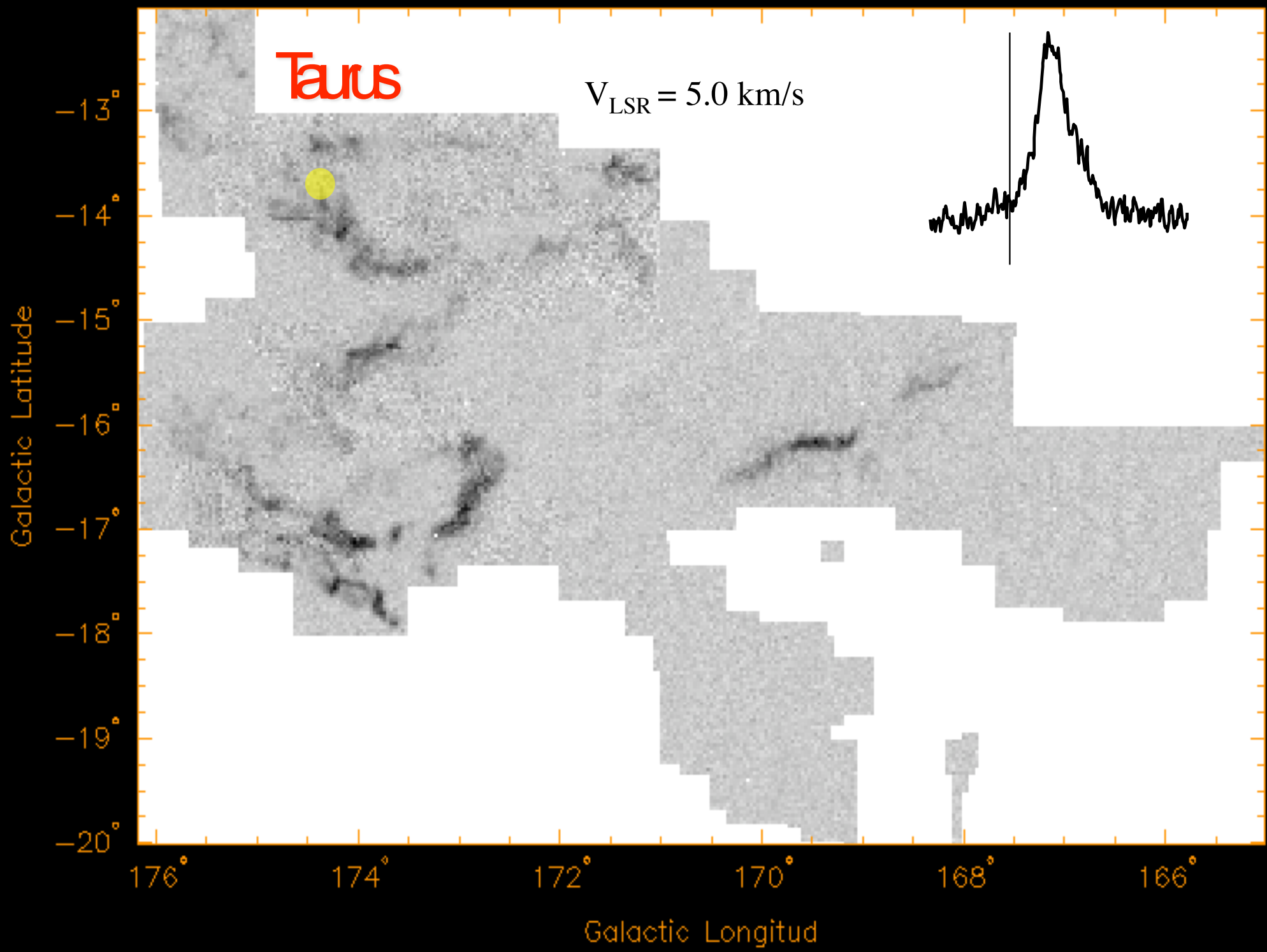


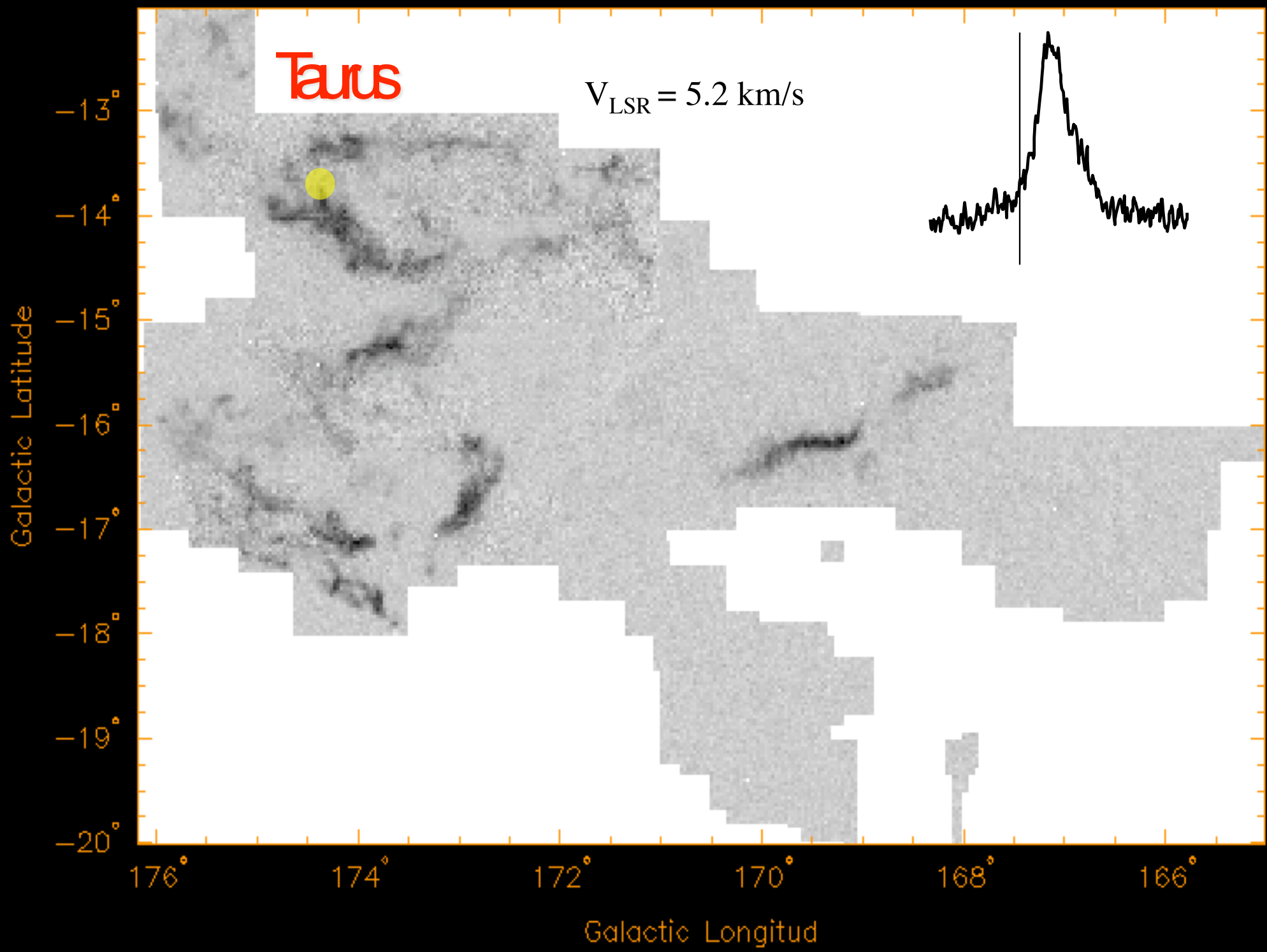


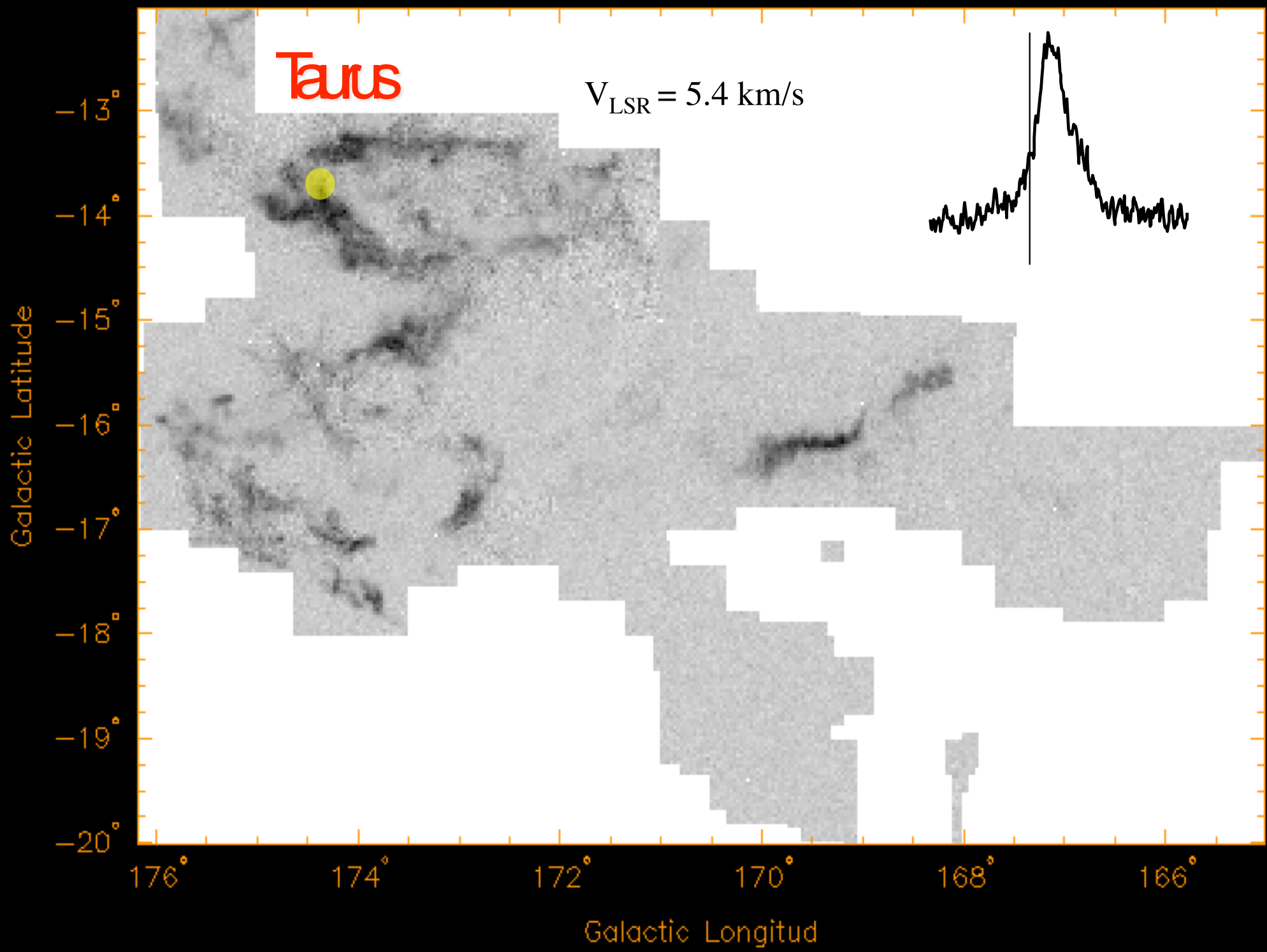


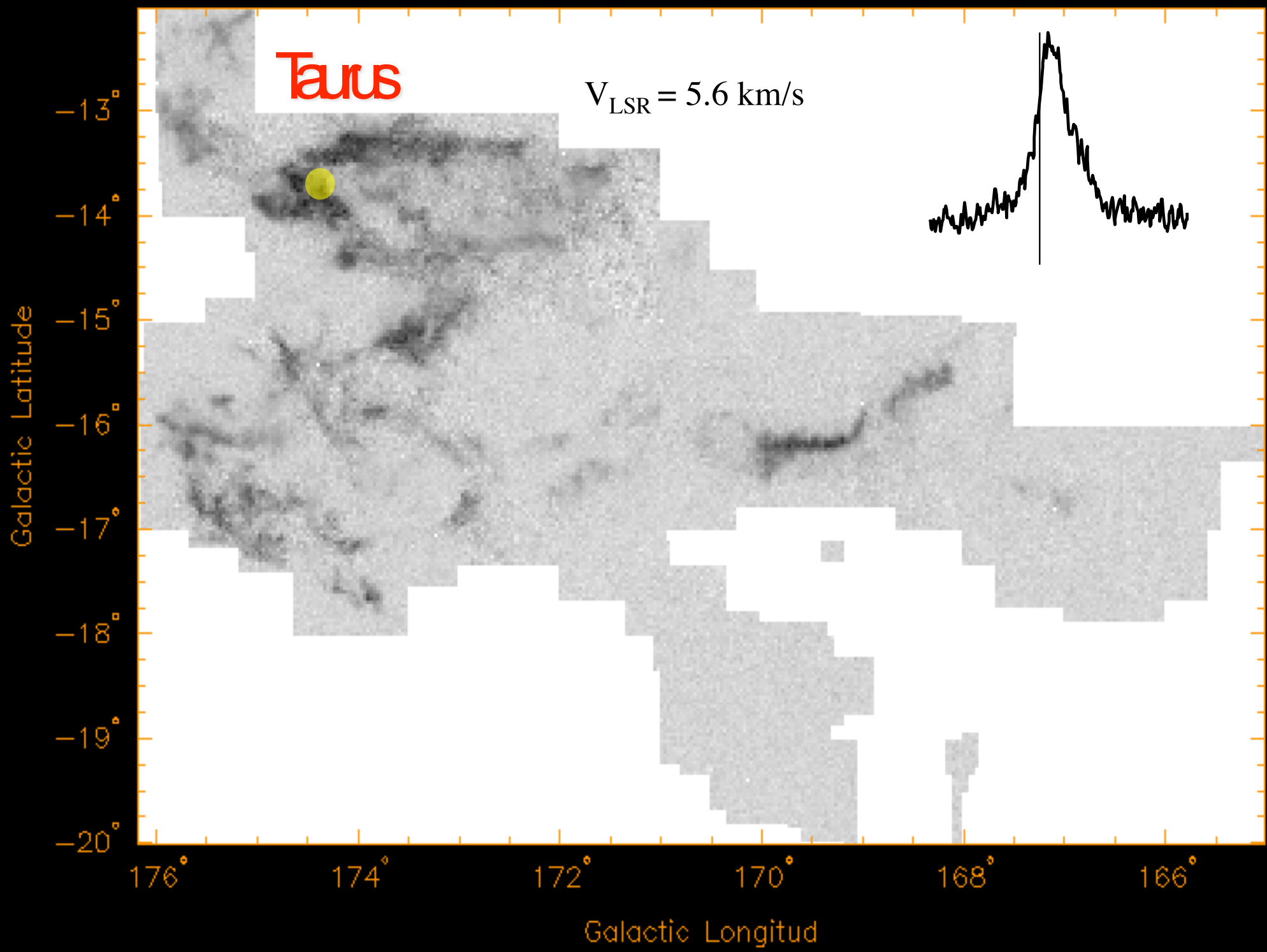


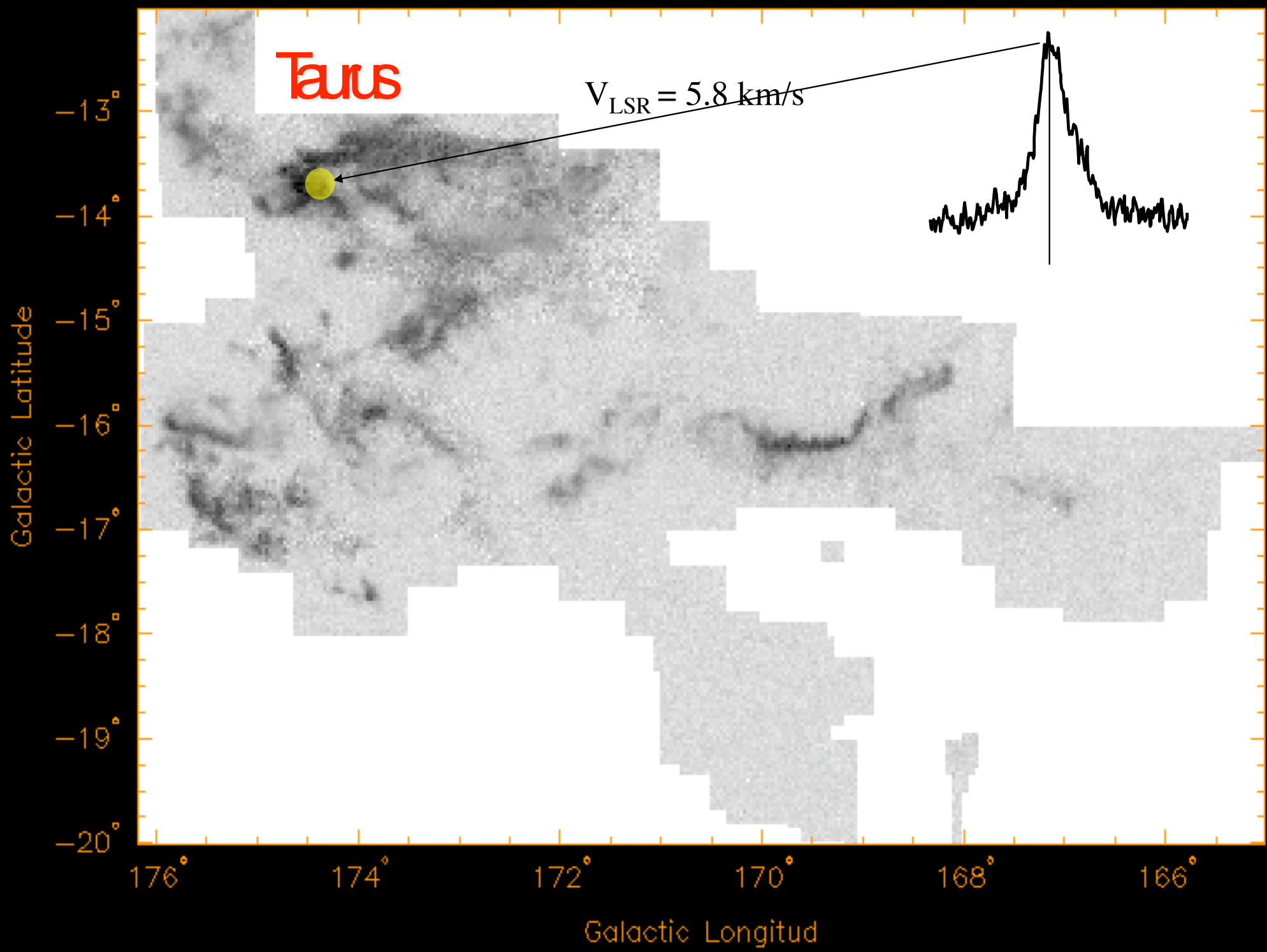


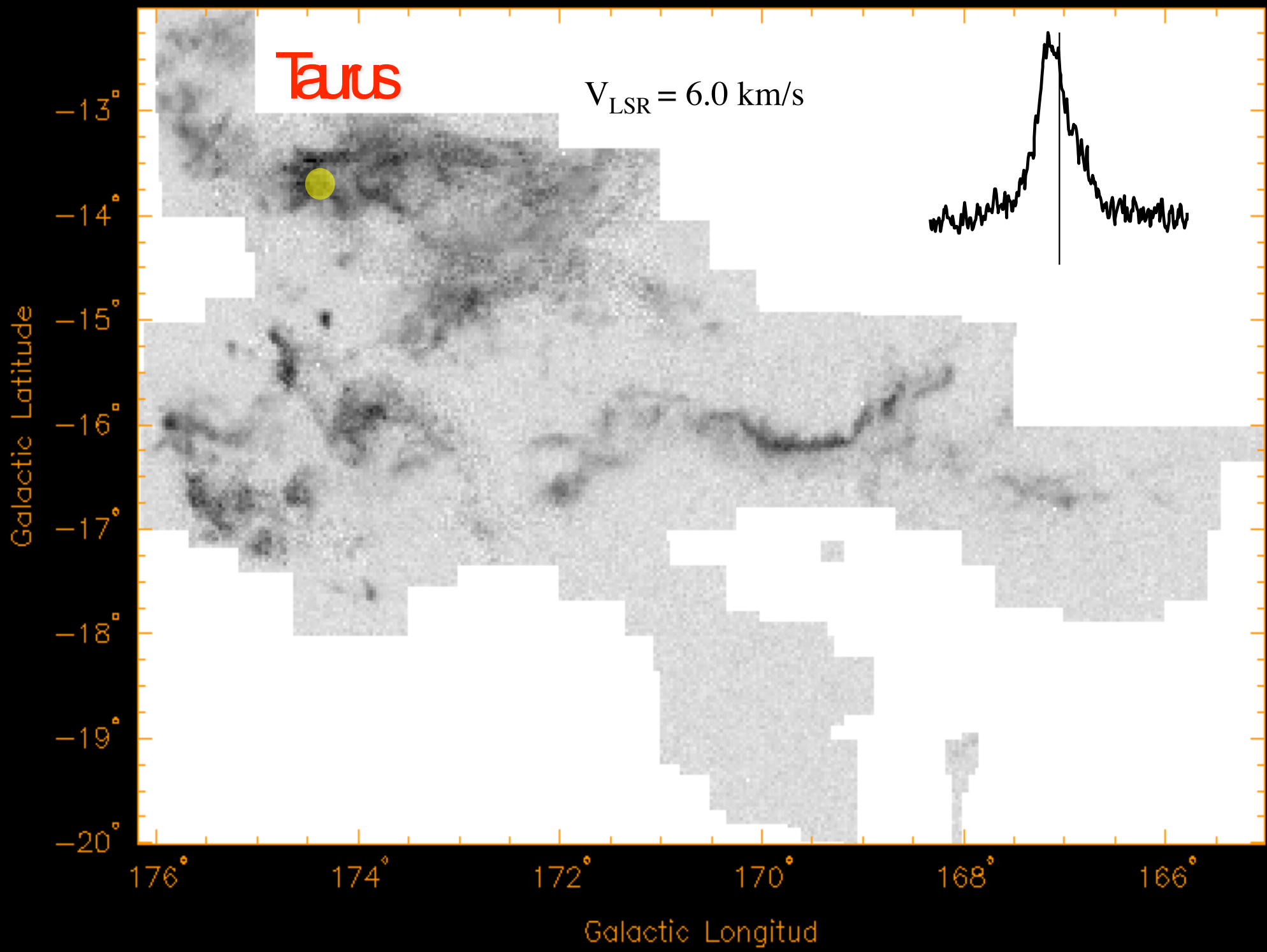


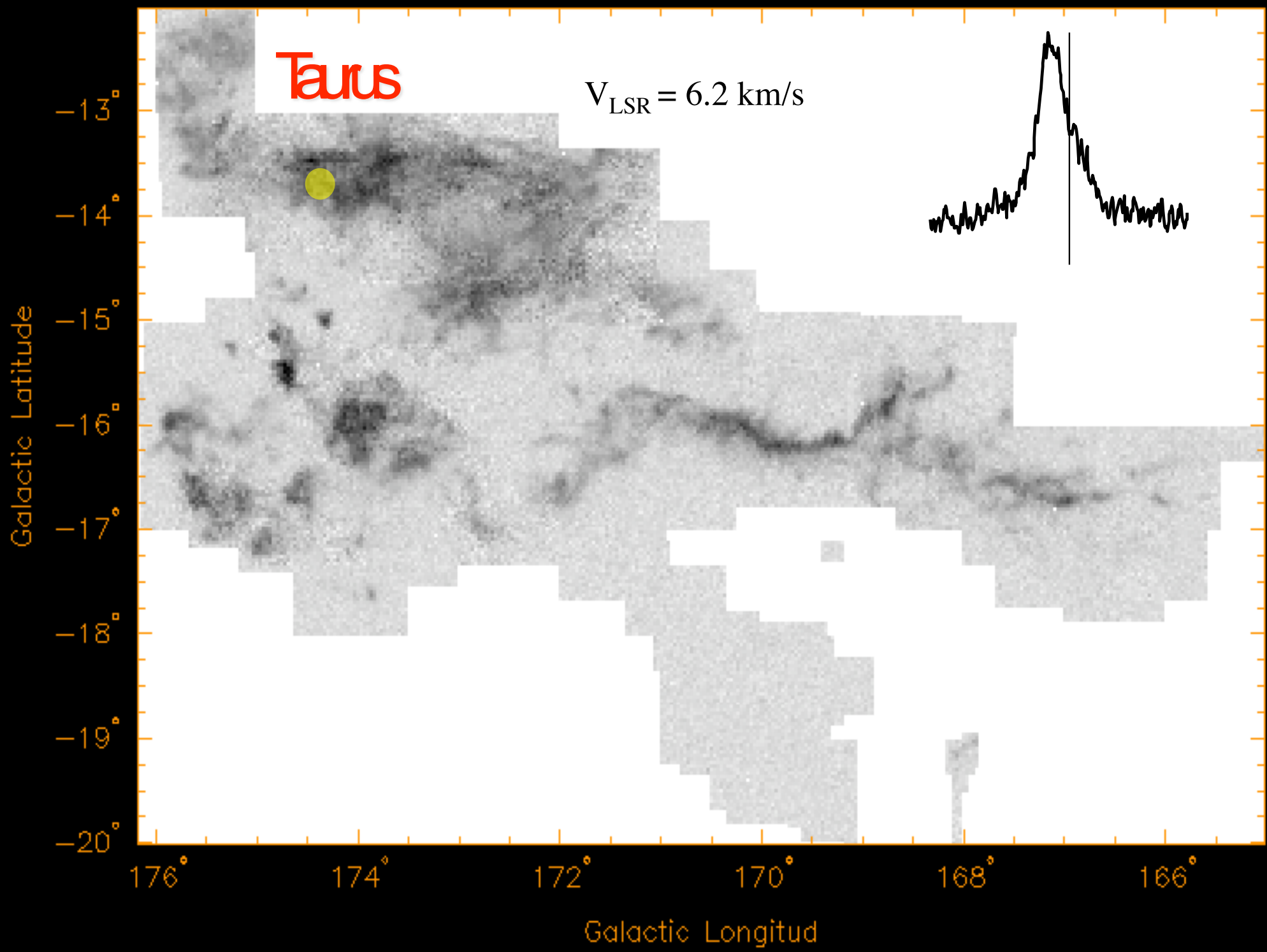


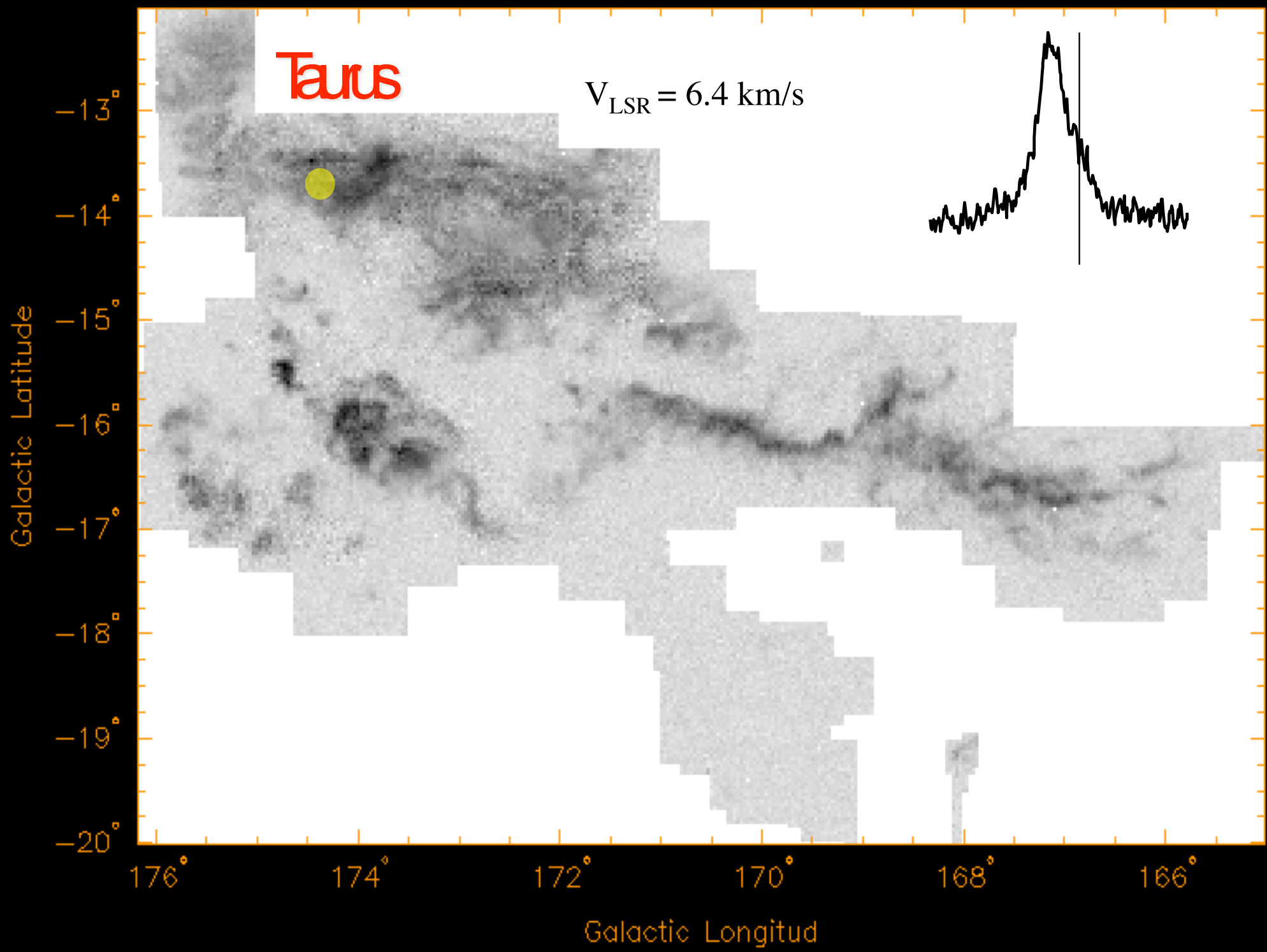


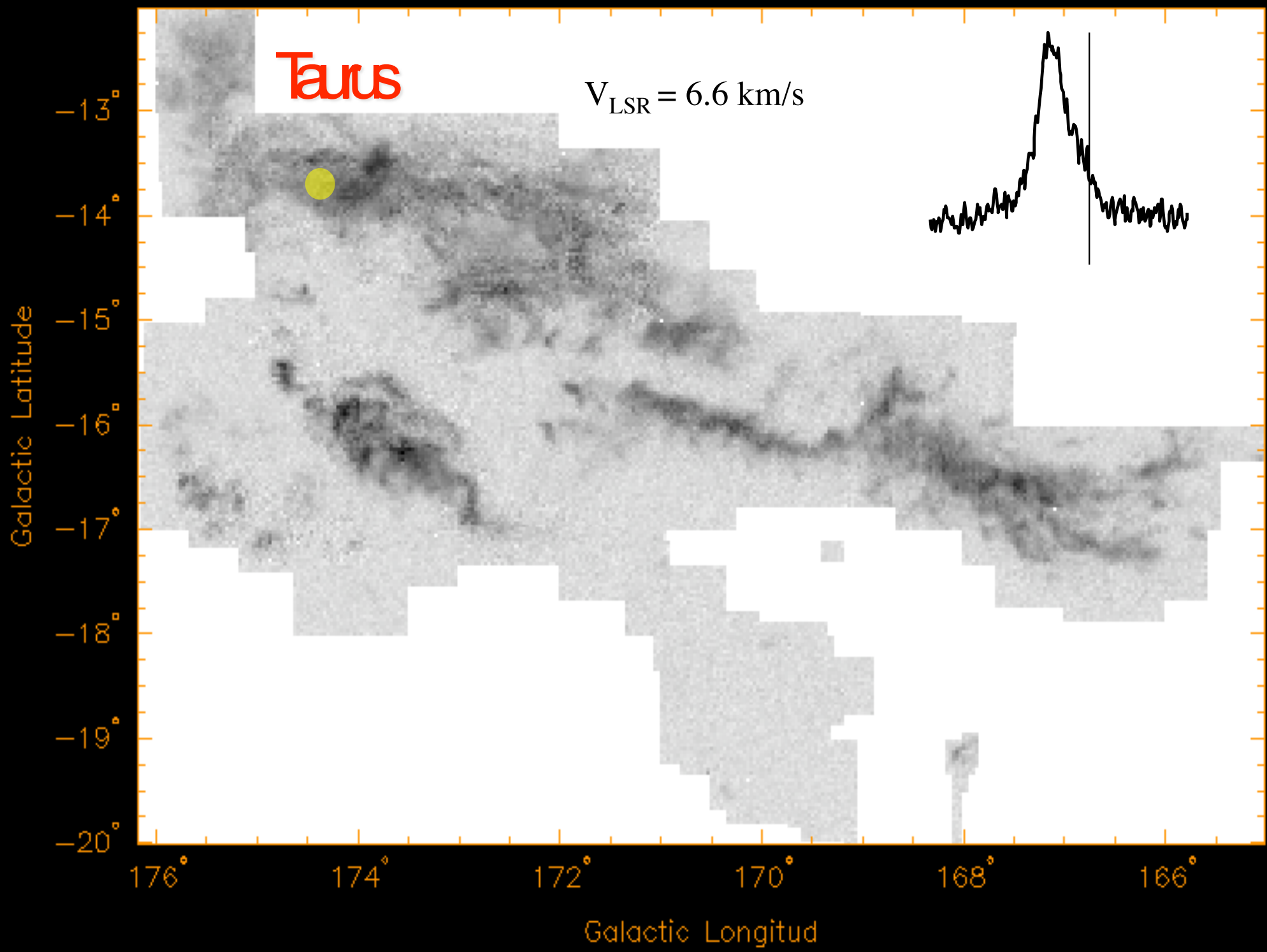


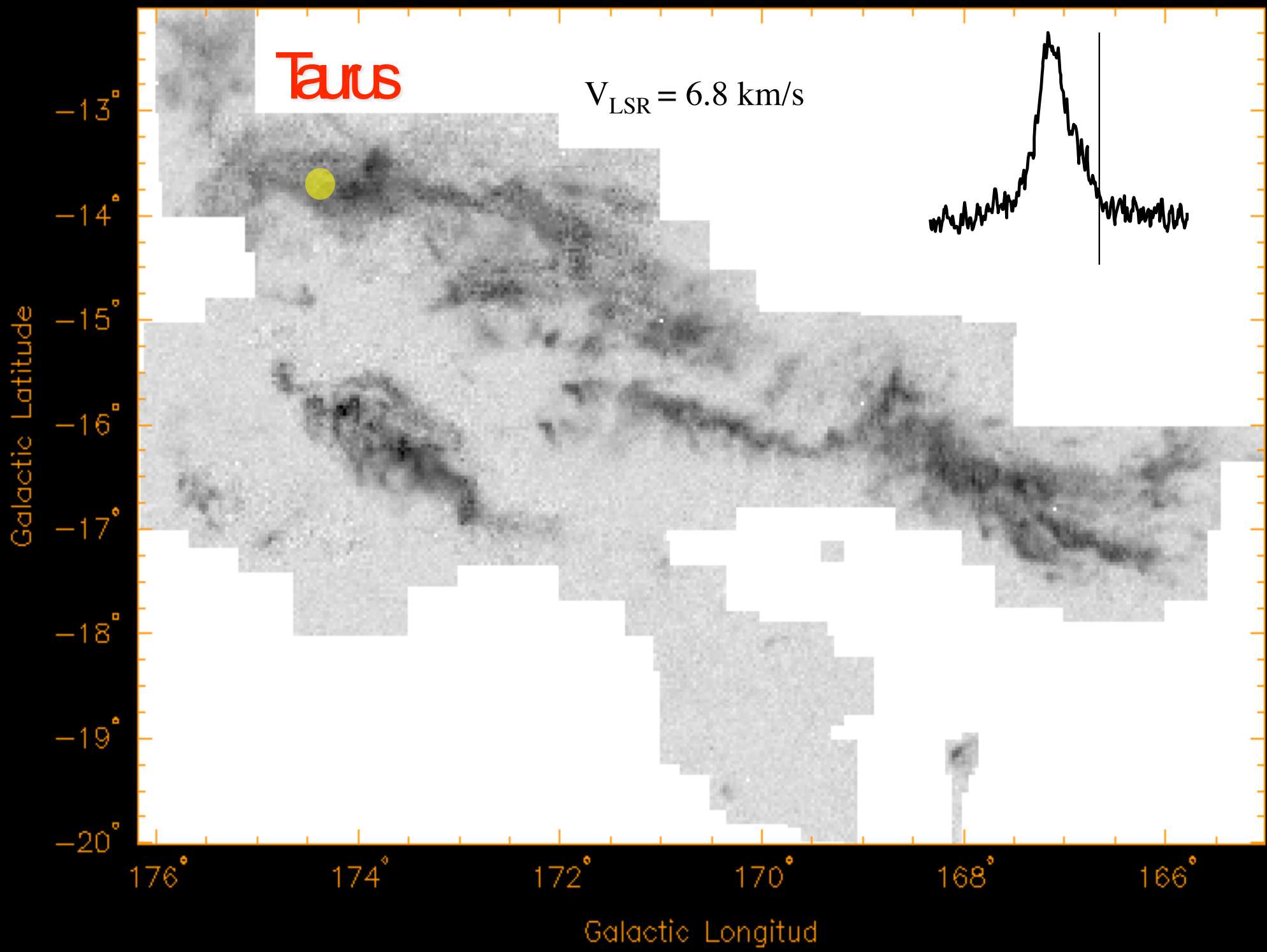


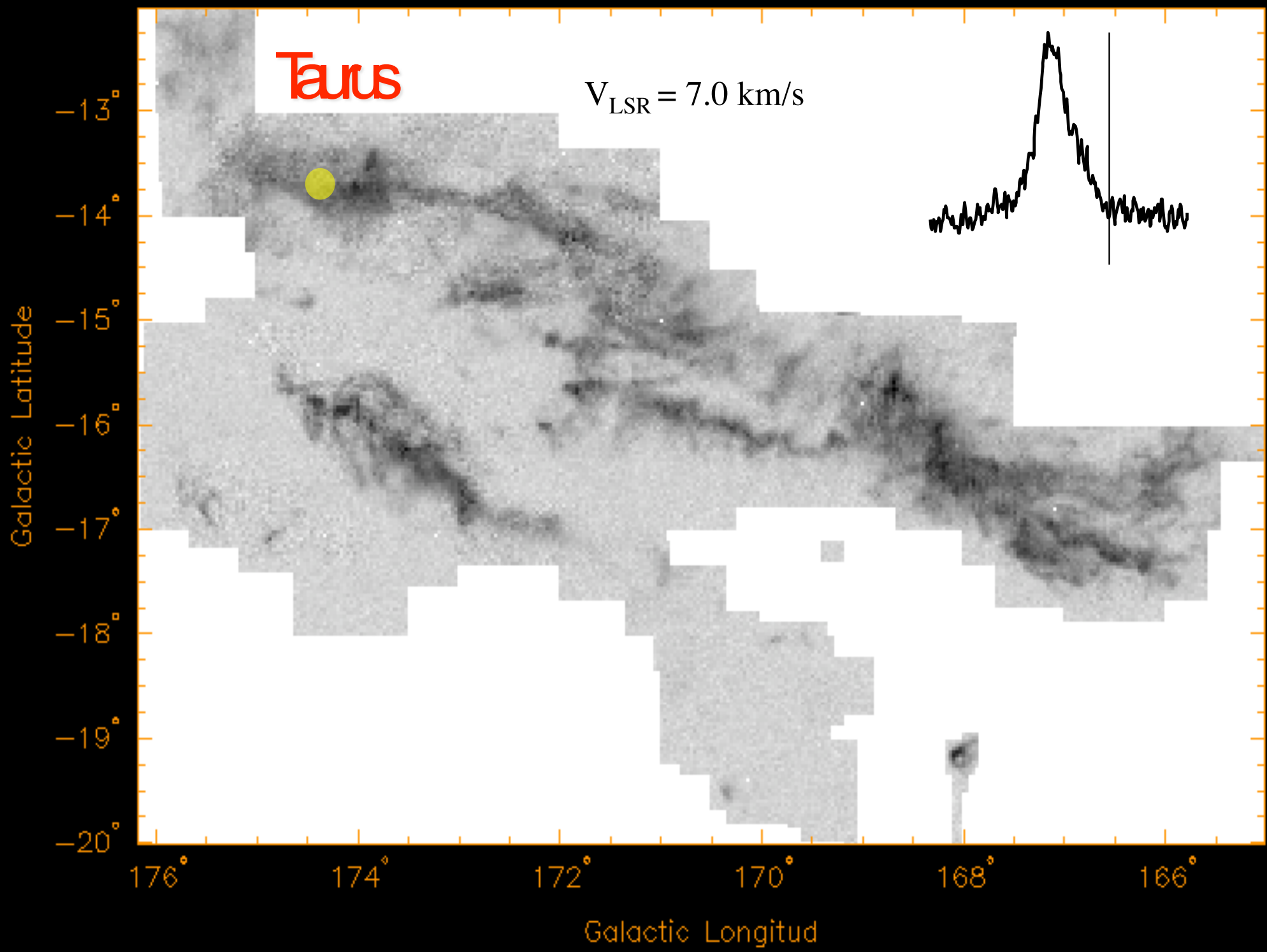










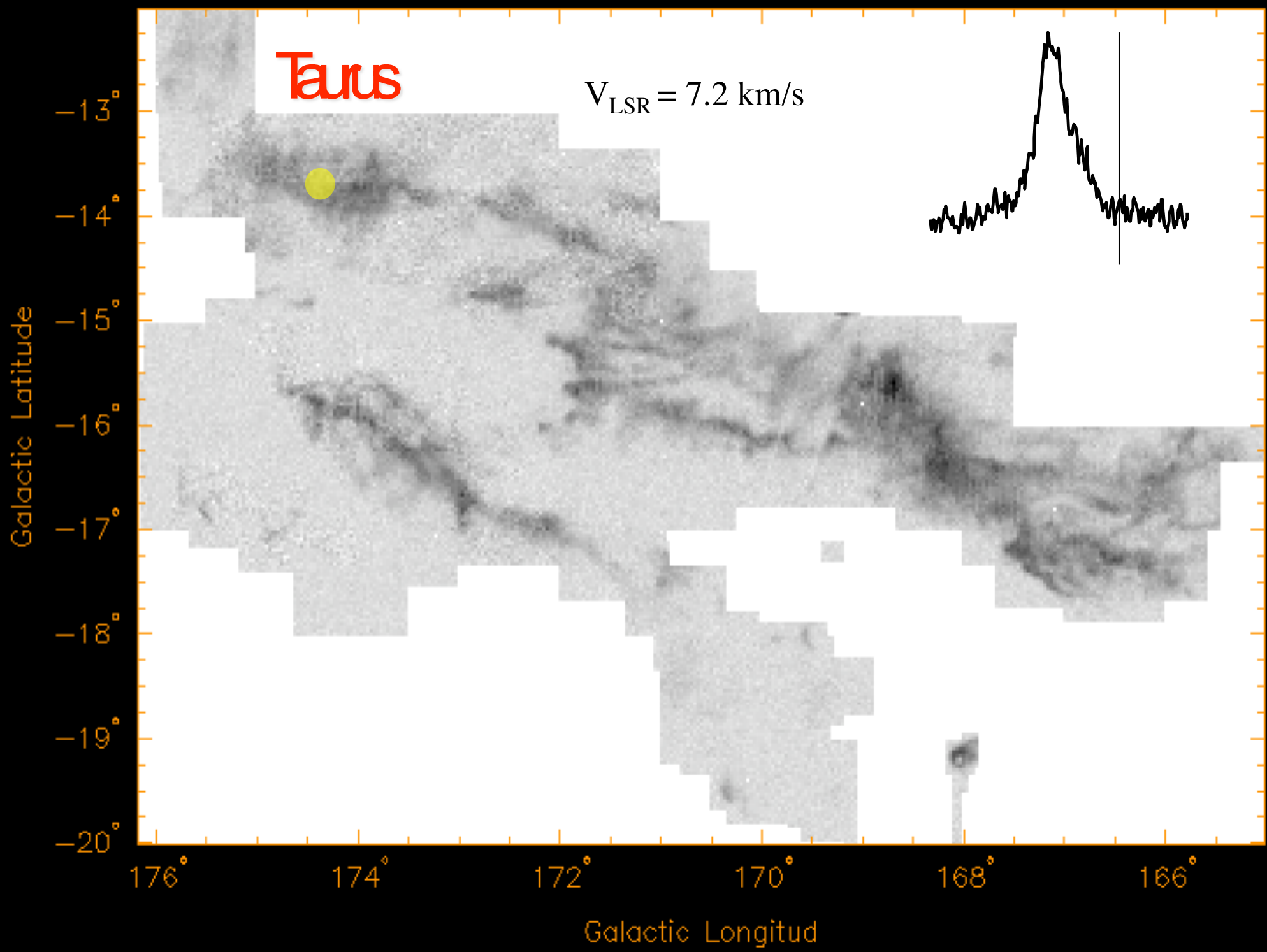


Taurus

$V_{\text{LSR}} = 7.0 \text{ km/s}$

Galactic Latitude

Galactic Longitud

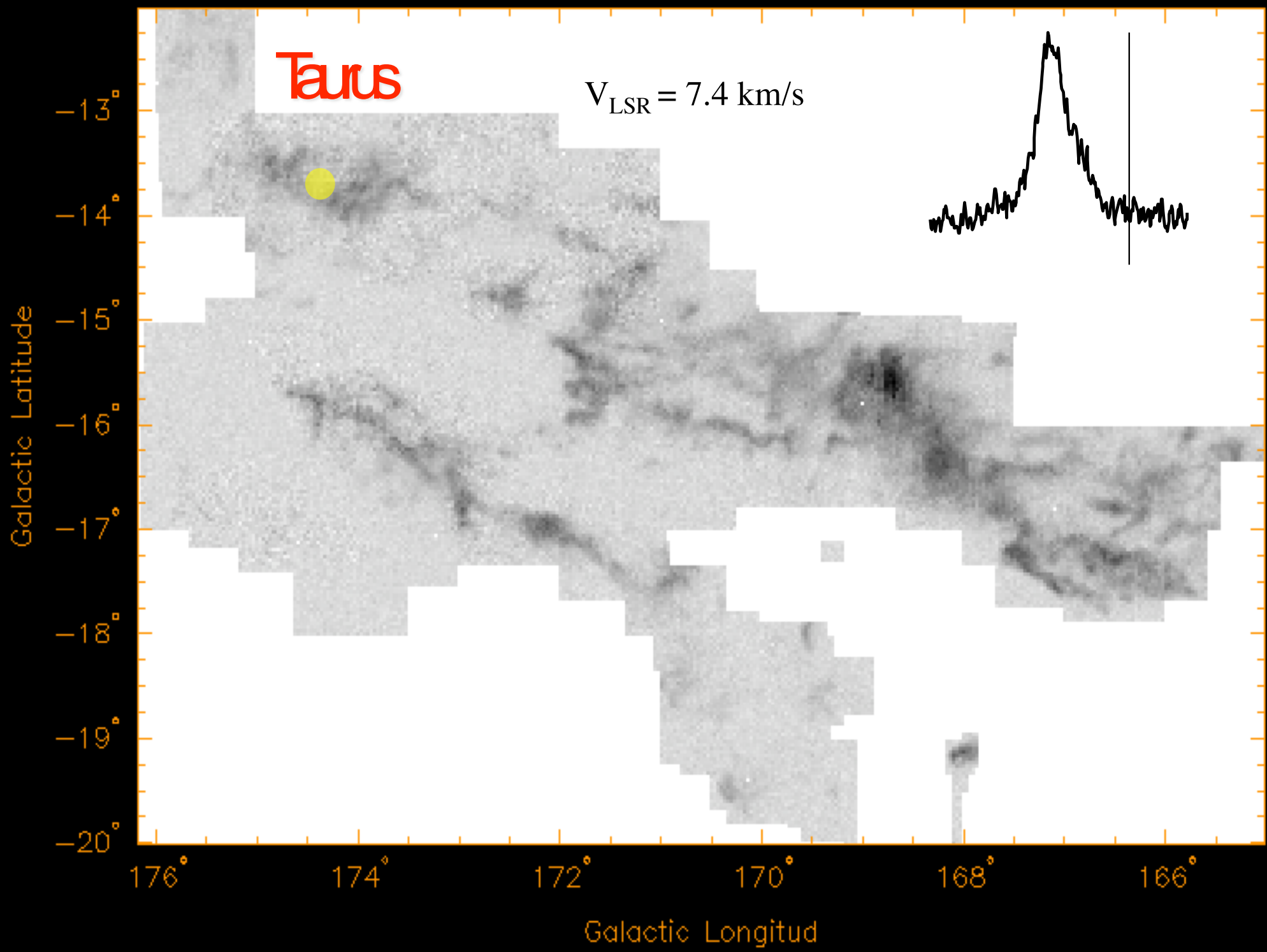


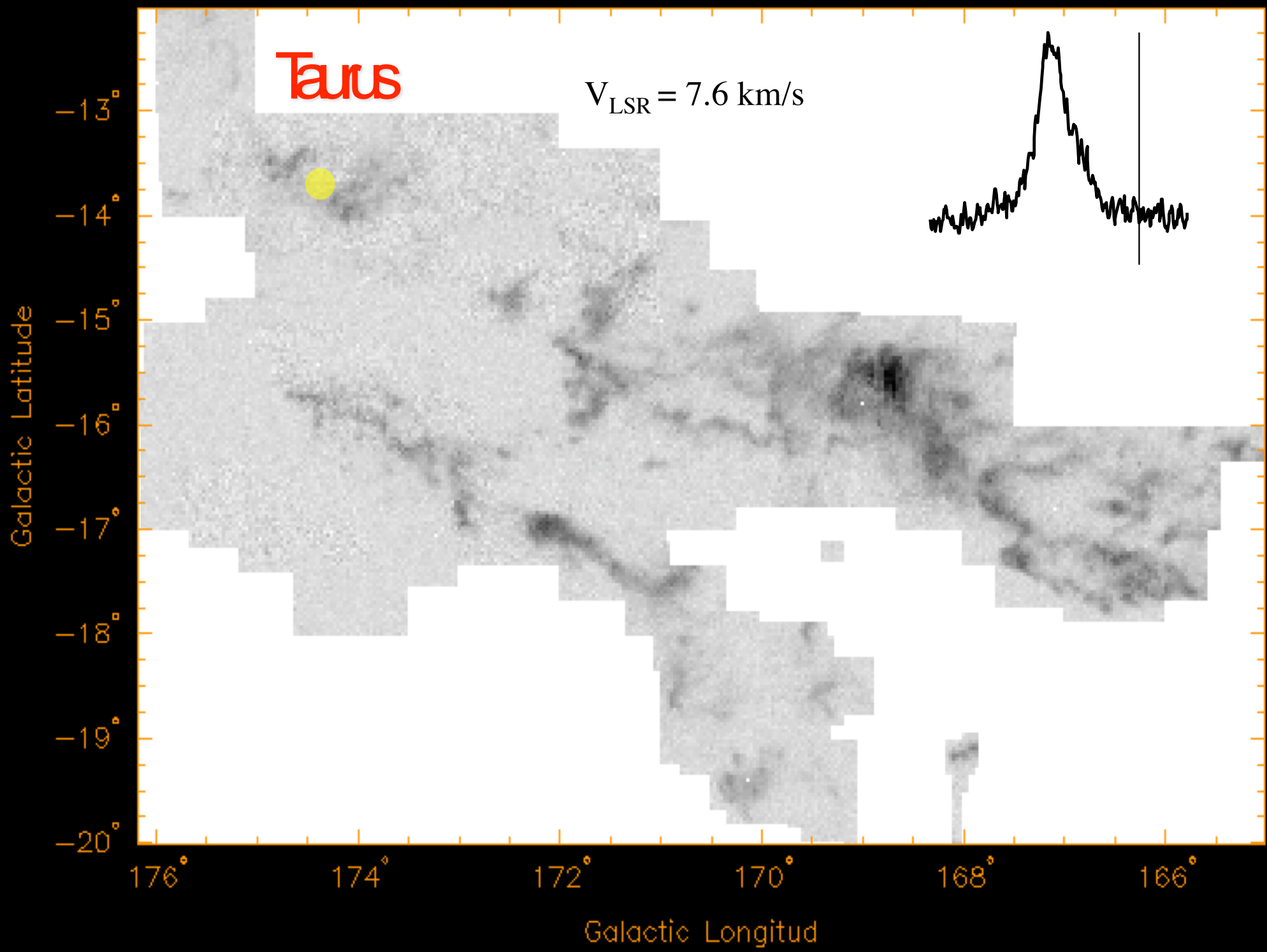
Taurus

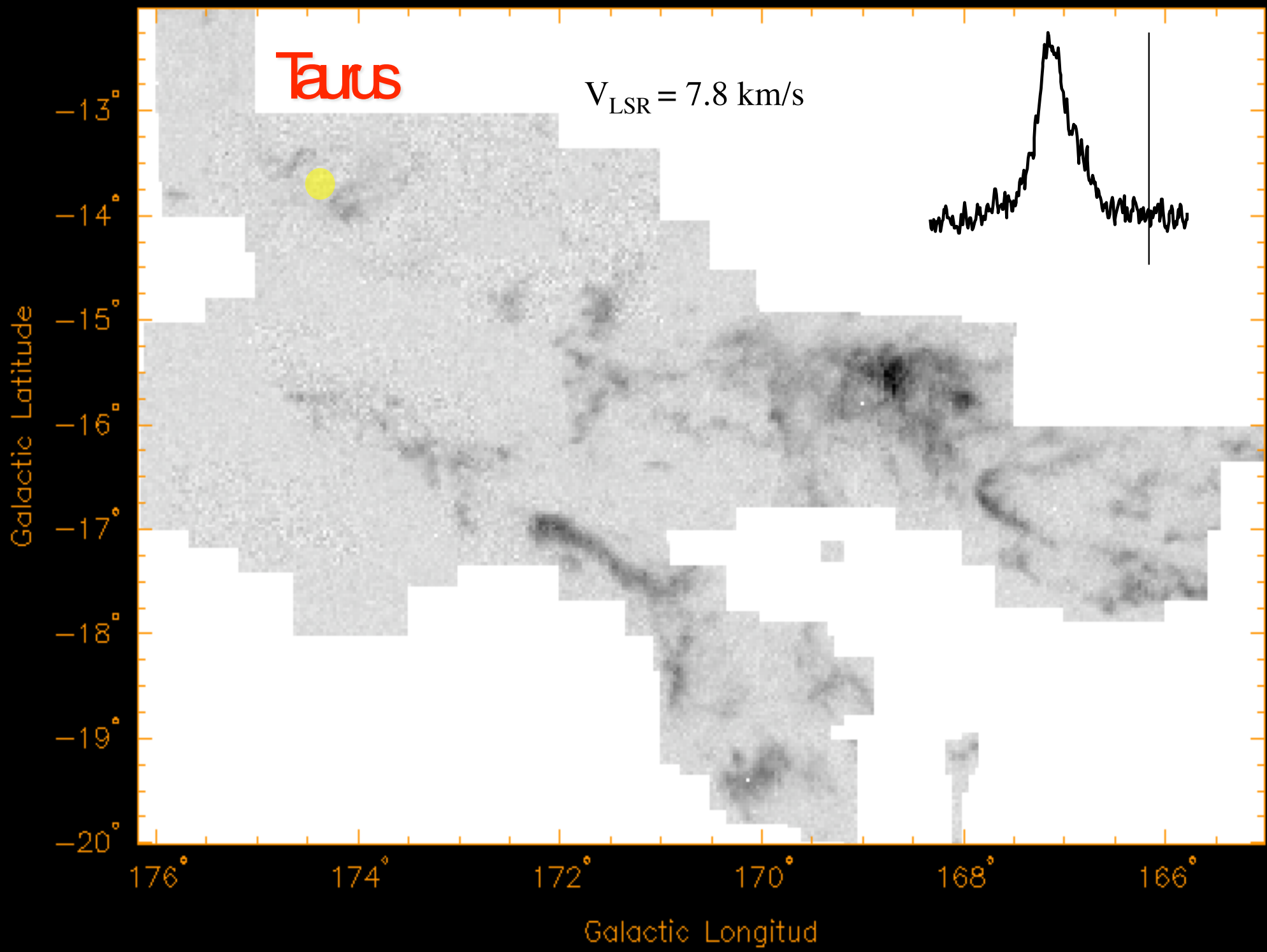
$V_{\text{LSR}} = 7.2 \text{ km/s}$

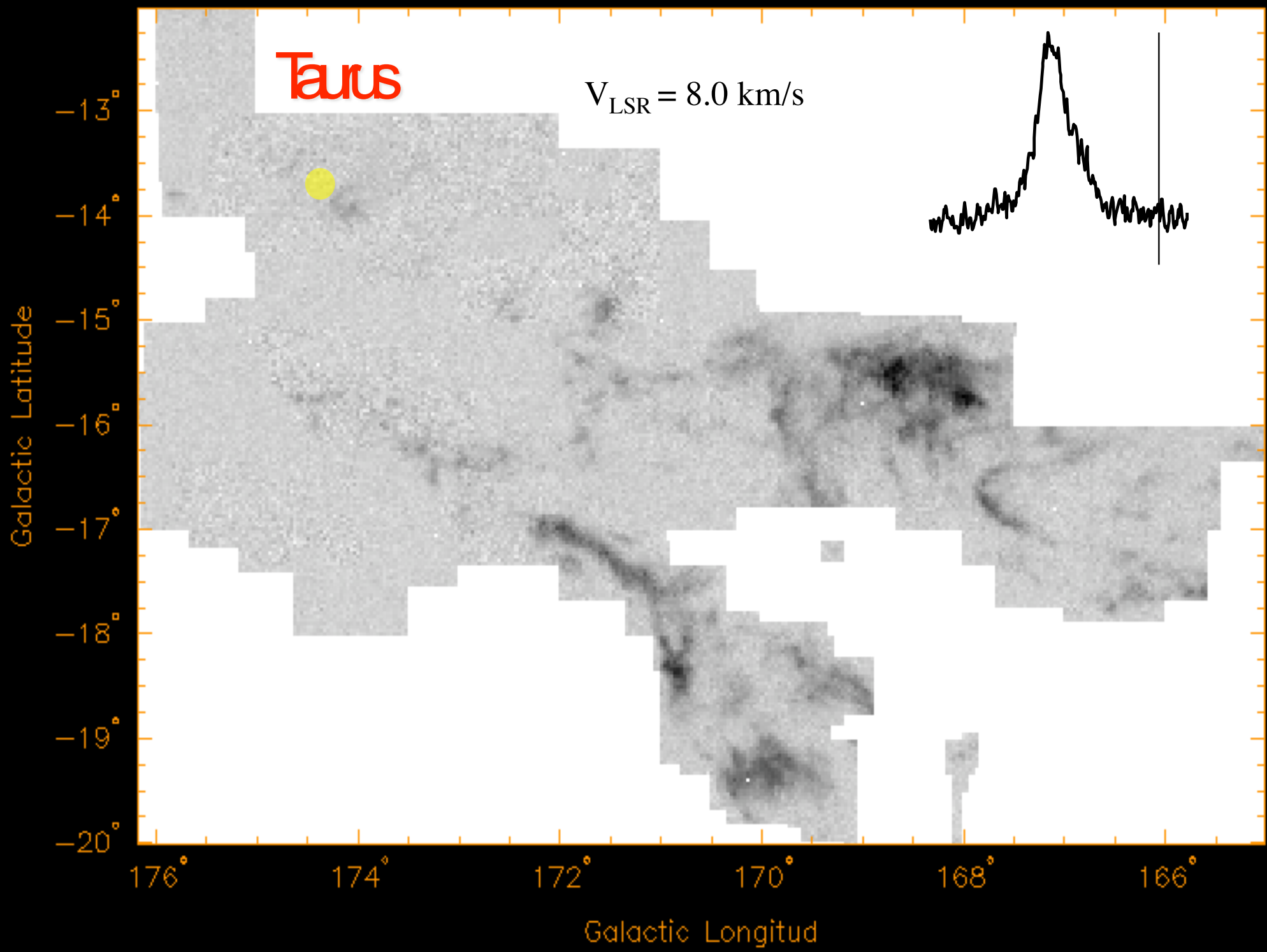
Galactic Latitude

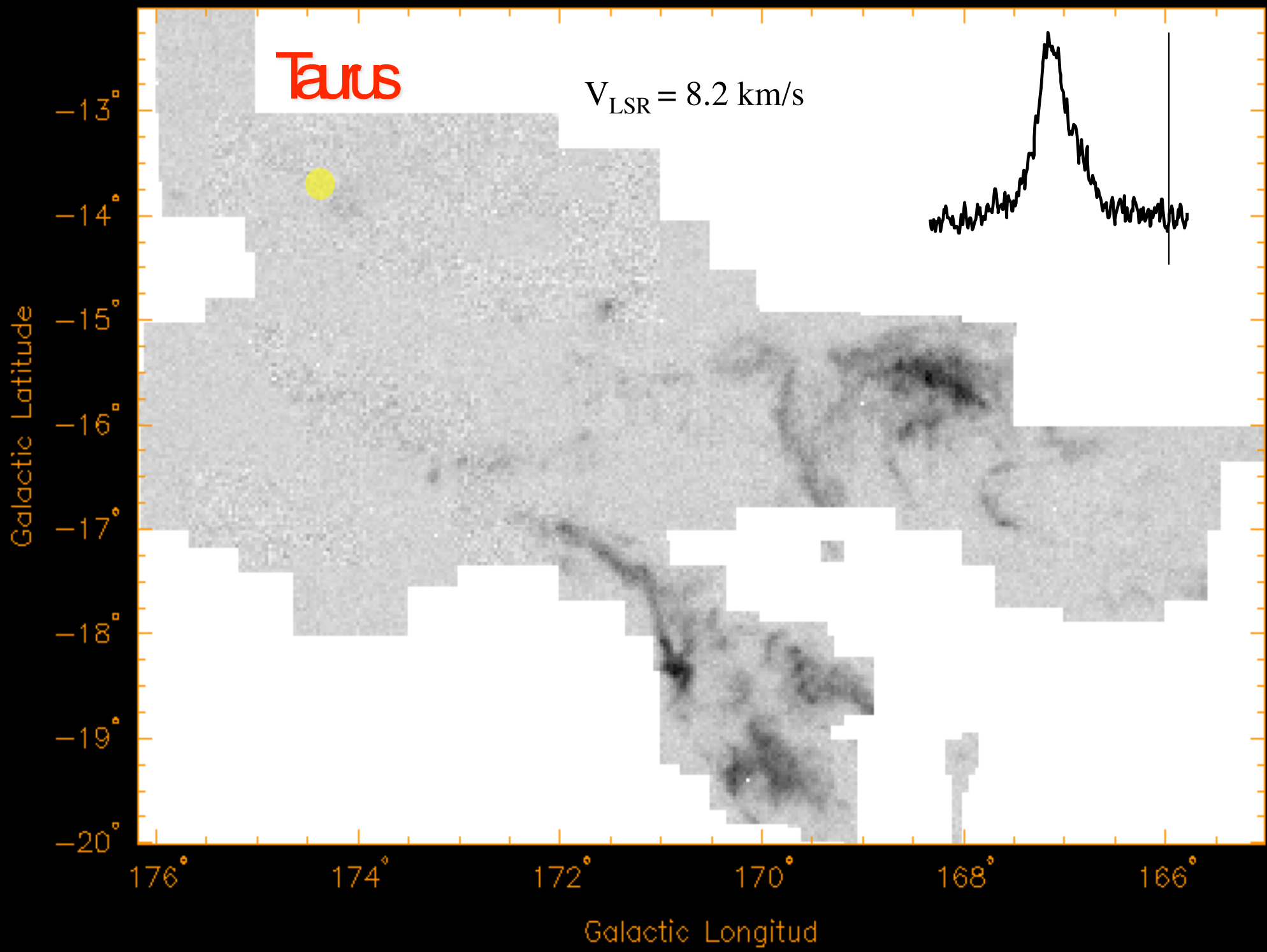
Galactic Longitud

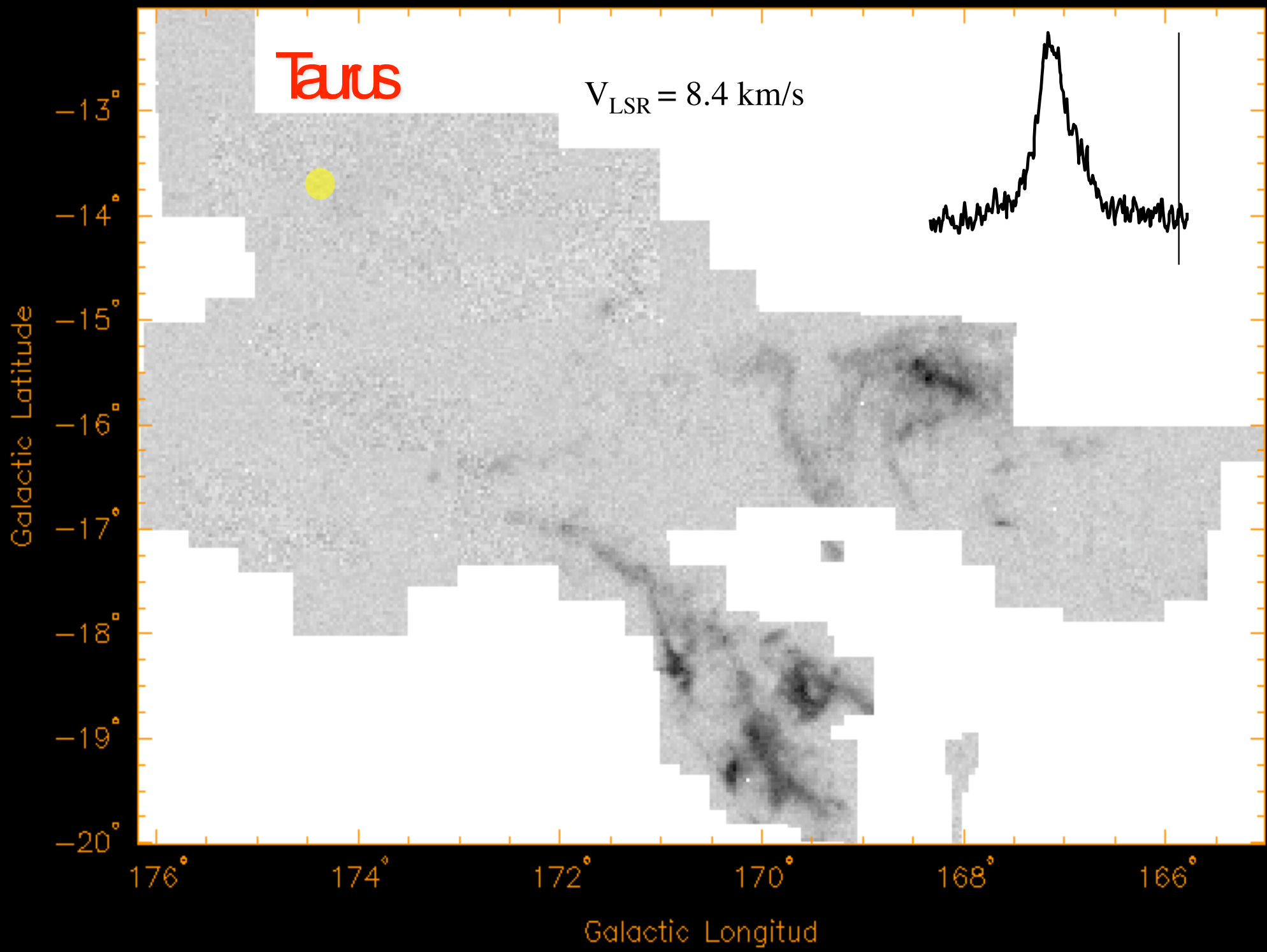


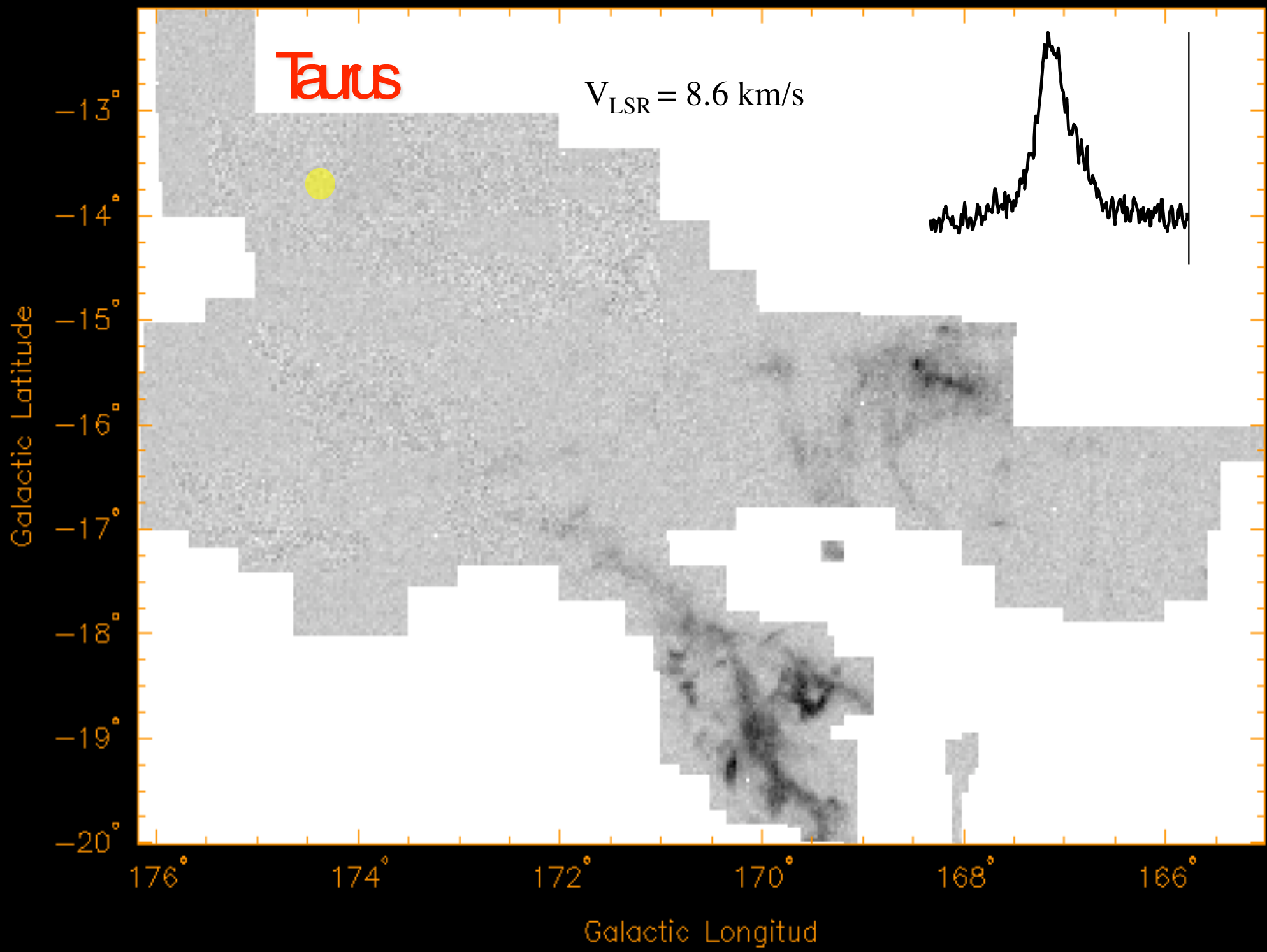


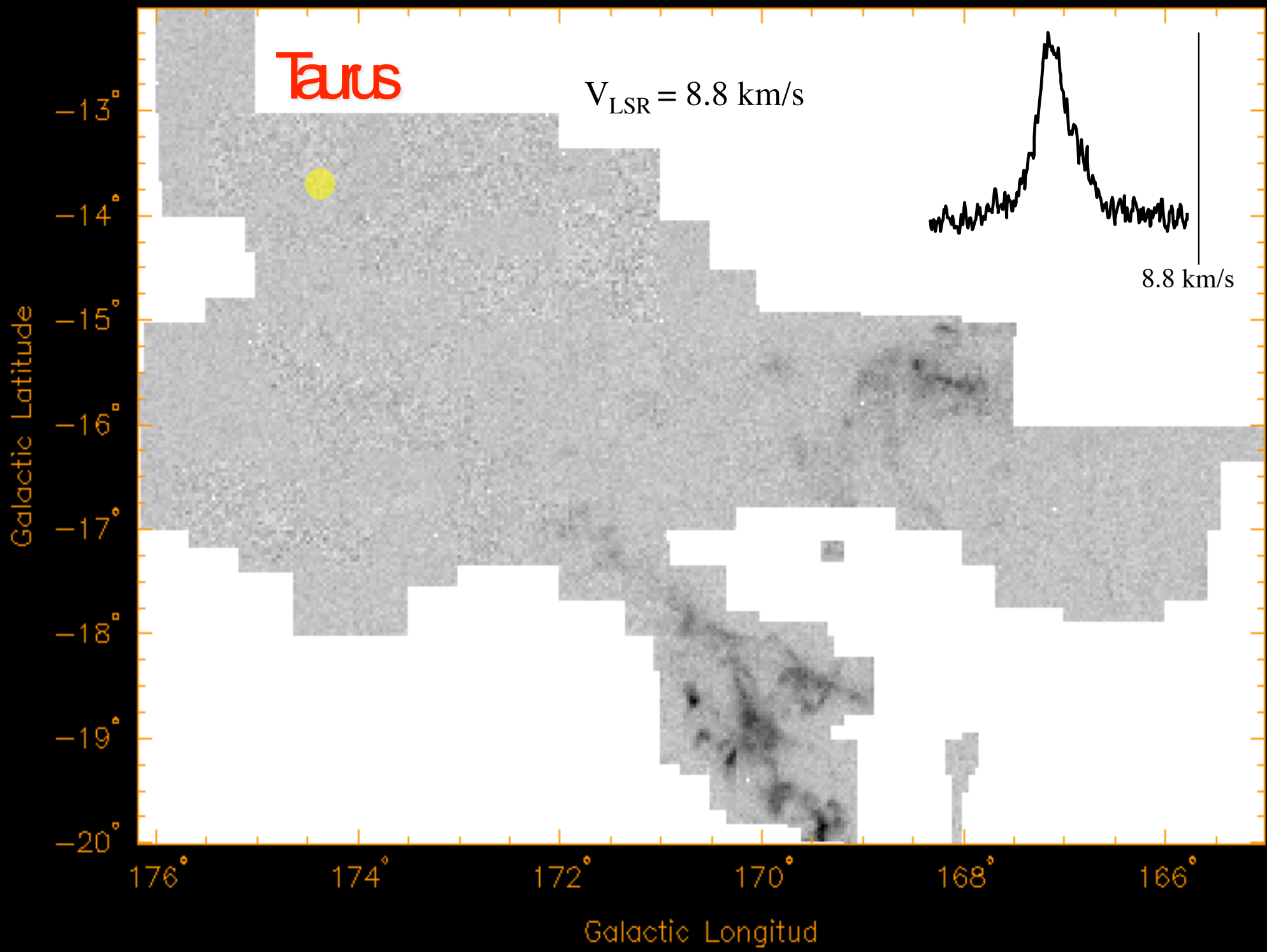


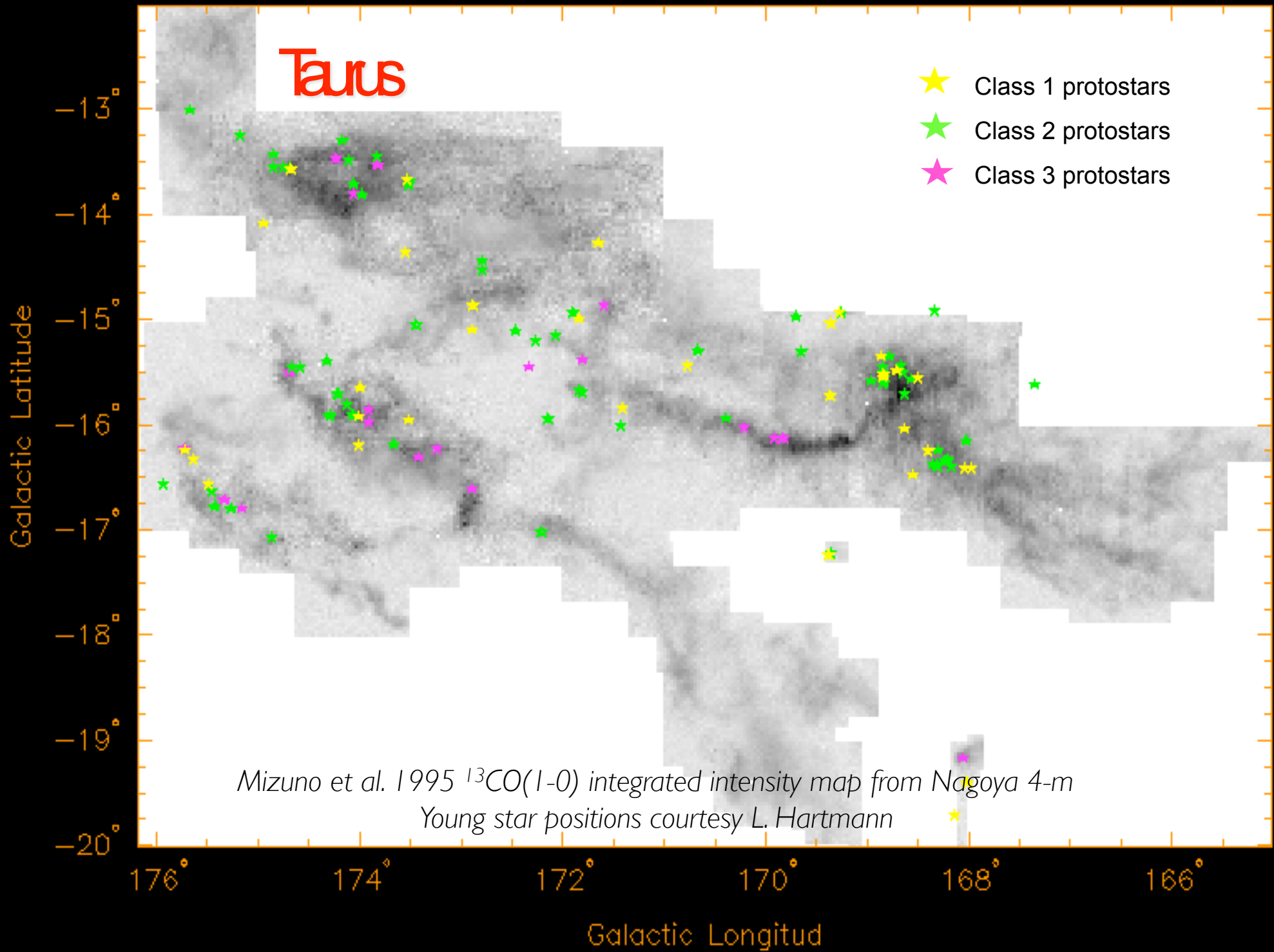












Taurus

- ★ Class 1 protostars
- ★ Class 2 protostars
- ★ Class 3 protostars

Mizuno et al. 1995 $^{13}\text{CO}(1-0)$ integrated intensity map from Nagoya 4-m
Young star positions courtesy L. Hartmann

theoretical
approach

Gravoturbulent star formation

- Idea:

***Star formation is controlled
by interplay between
gravity and
supersonic turbulence!***

- Dual role of turbulence:

- *stability on large scales*
- *initiating collapse on small scales*

(e.g., Larson, 2003, Rep. Prog. Phys, 66, 1651;
or Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125)

Gravoturbulent star formation

- Idea:

***Star formation is controlled
by interplay between
gravity and
supersonic turbulence!***

- Validity:

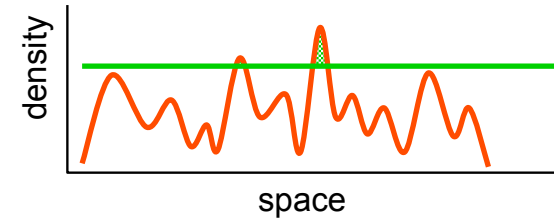
This hold on *all* scales and applies to build-up of stars and star clusters within molecular clouds as well as to the formation of molecular clouds in galactic disk.

(e.g., Larson, 2003, Rep. Prog. Phys, 66, 1651;
or Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125)

Gravoturbulent star formation

- interstellar gas is highly *inhomogeneous*
 - *thermal instability*
 - *gravitational instability*
 - *turbulent compression* (in shocks $\delta\rho/\rho \propto M^2$; in atomic gas: $M \approx 1...3$)
- cold *molecular clouds* can form rapidly in high-density regions at *stagnation points of convergent large-scale flows*
 - chemical *phase transition*: atomic \rightarrow molecular
 - process is *modulated* by large-scale *dynamics* in the galaxy
- inside *cold clouds*: turbulence is highly supersonic ($M \approx 1...20$)
 \rightarrow *turbulence* creates large density contrast,
gravity selects for collapse

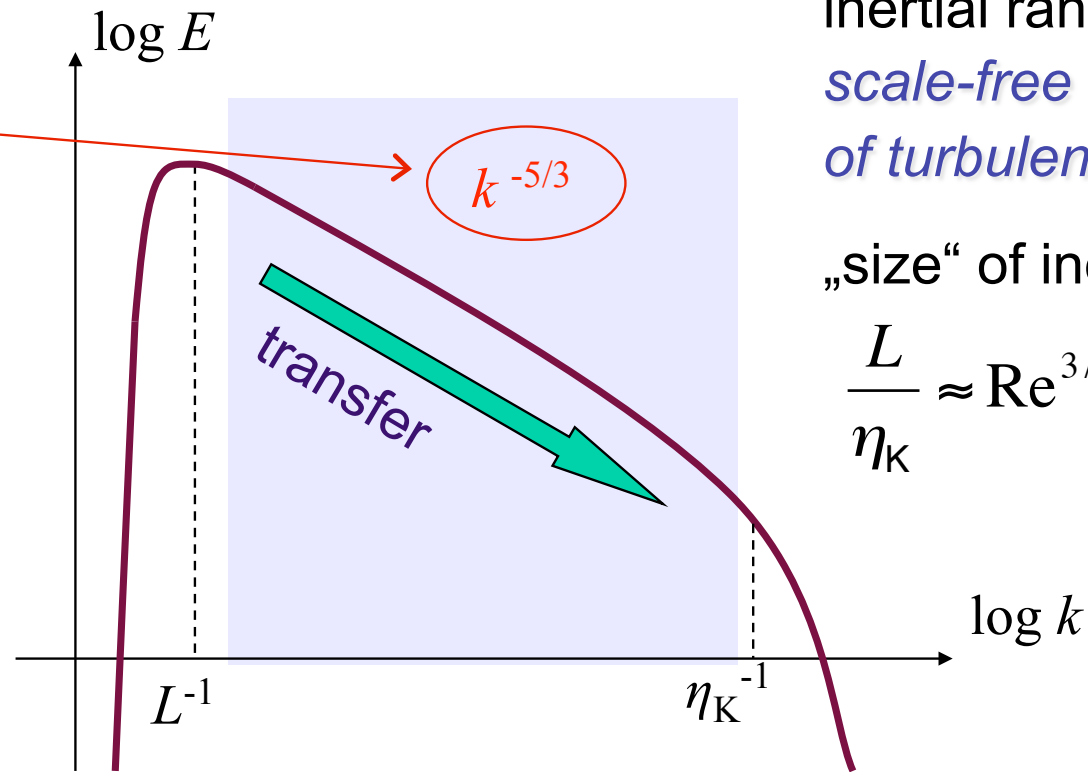
 \longrightarrow **GRAVOTUBULENT FRAGMENTATION**
- *turbulent cascade*: local compression *within* a cloud provokes collapse
 \rightarrow formation of individual *stars* and *star clusters*



turbulence

Turbulent cascade

Kolmogorov (1941) theory
incompressible turbulence



inertial range:
*scale-free behavior
of turbulence*

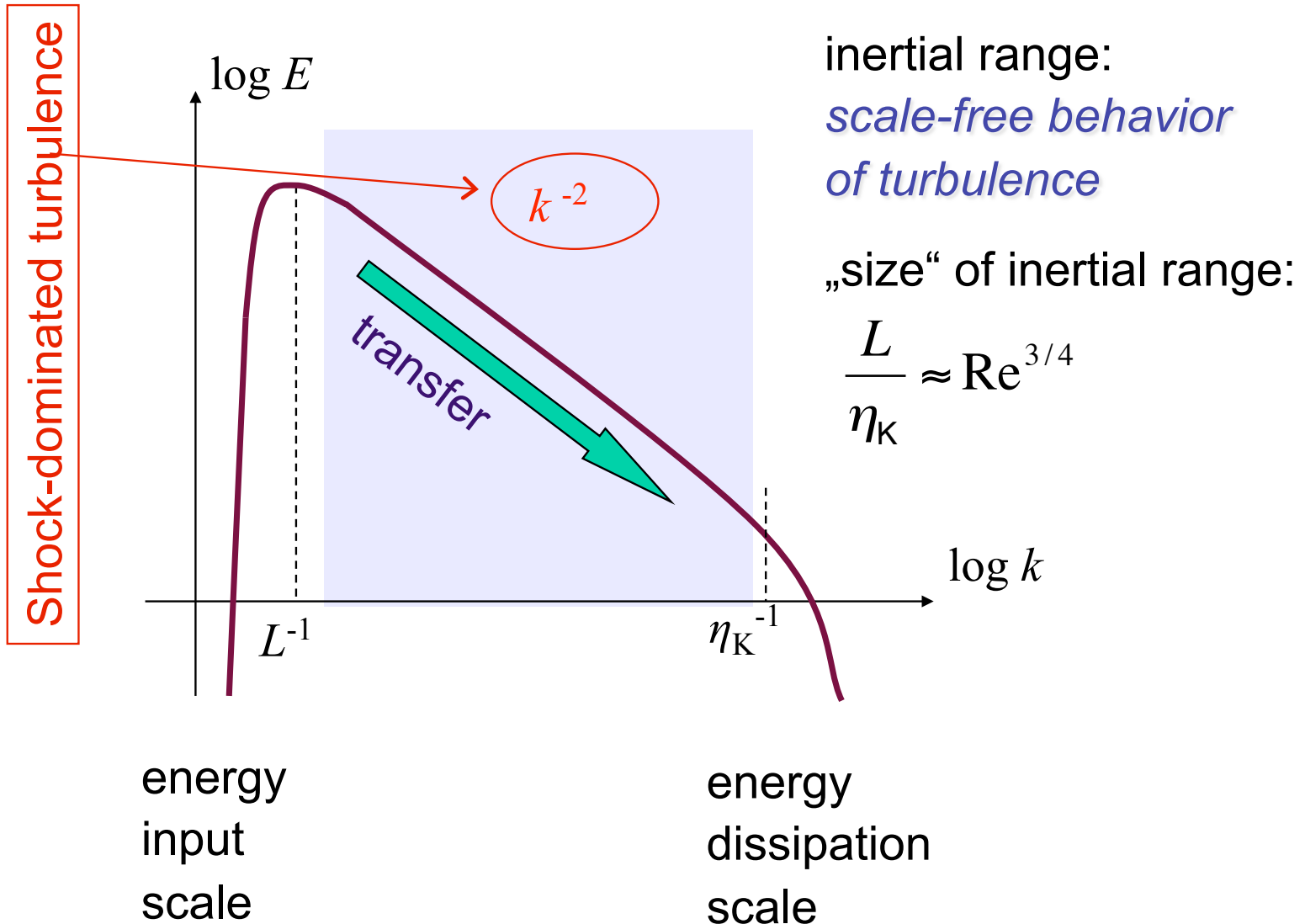
„size“ of inertial range:

$$\frac{L}{\eta_K} \approx \text{Re}^{3/4}$$

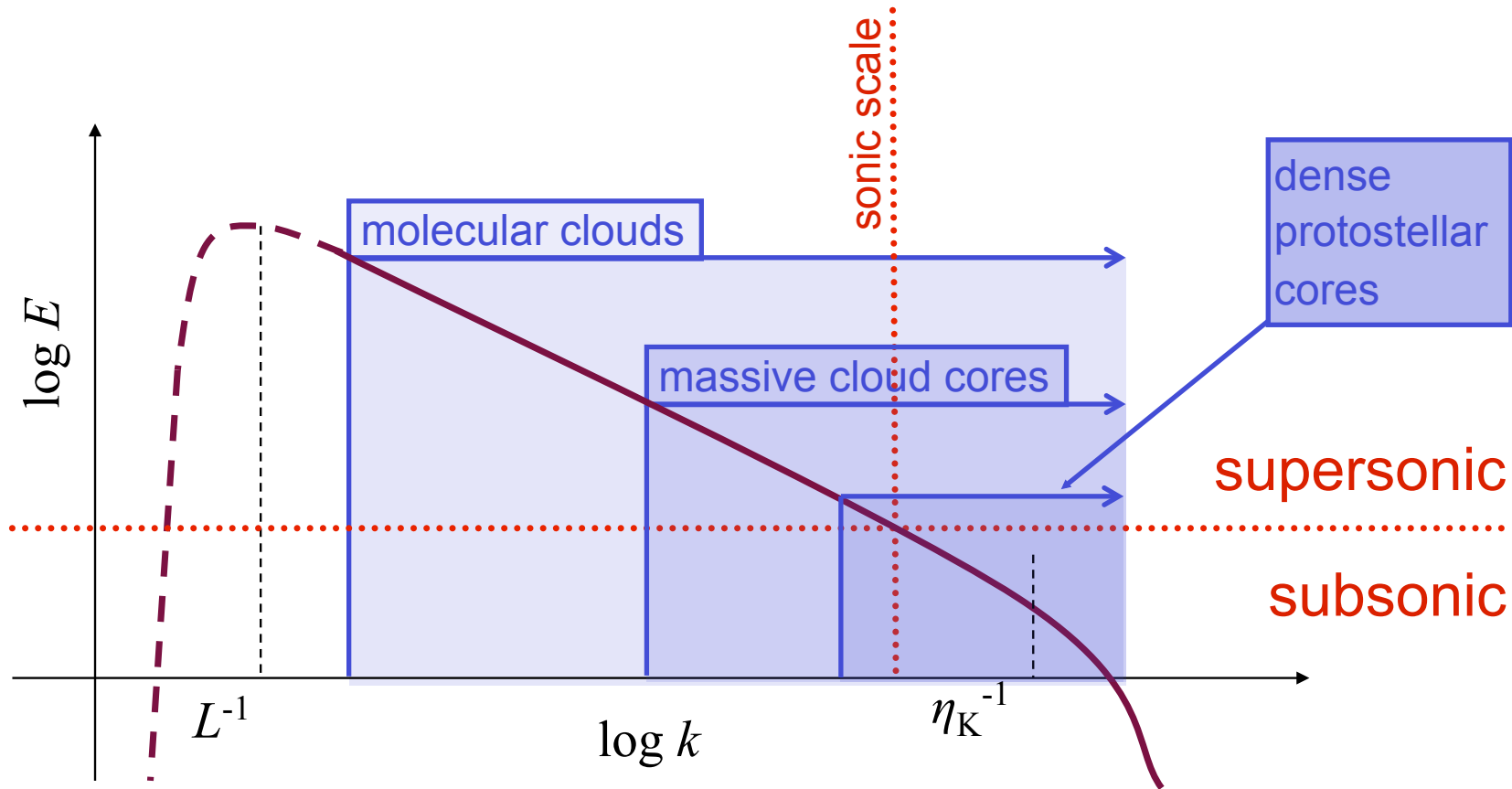
energy
input
scale

energy
dissipation
scale

Turbulent cascade



Turbulent cascade in ISM



energy source & scale
NOT known
 (supernovae, winds,
 spiral density waves?)

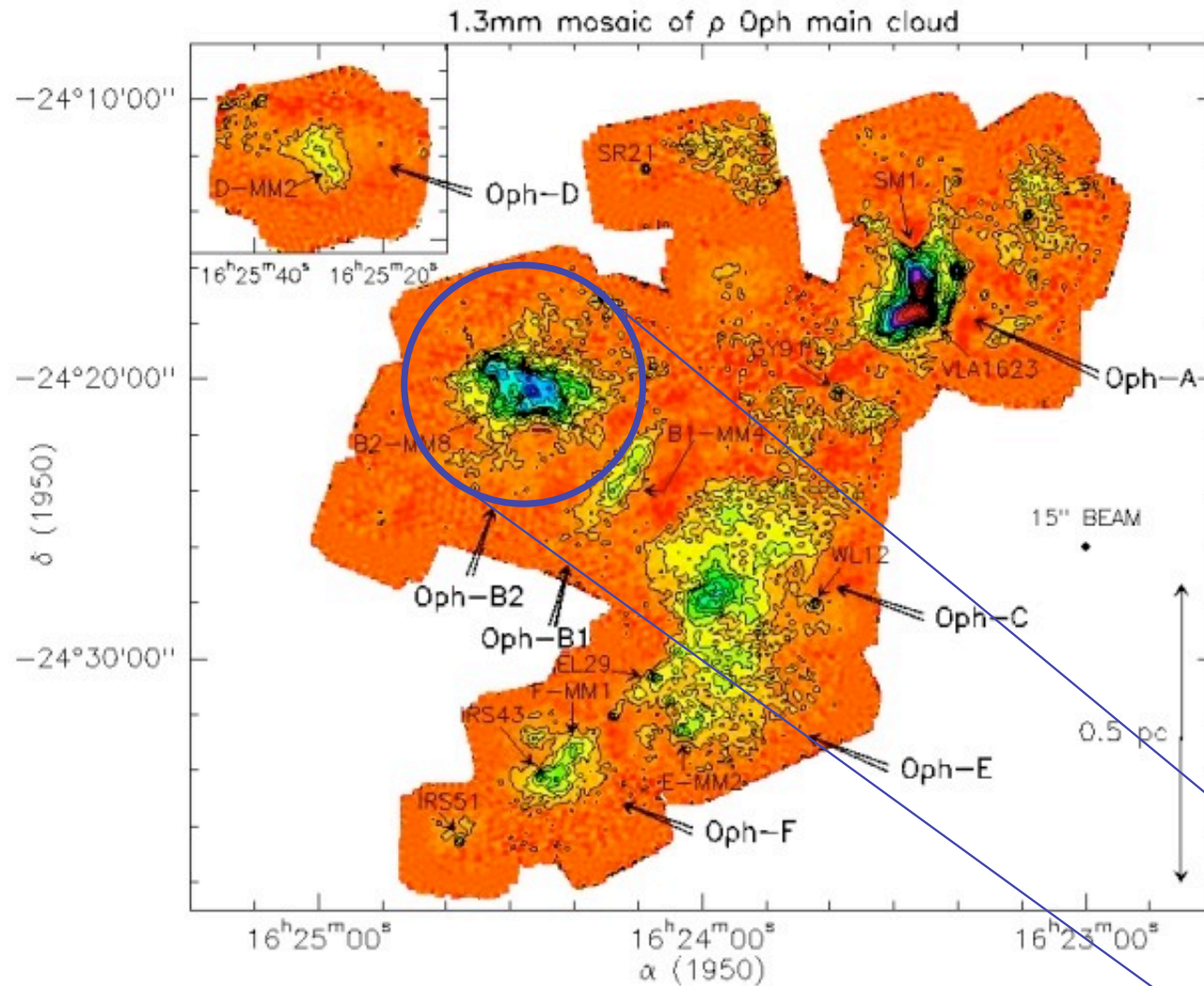
$$\sigma_{\text{rms}} \ll 1 \text{ km/s/s/m/s}$$

$$M_{\text{rms}} \leq 1$$

$$L \approx 0.1 \text{ pc}$$

dissipation scale not known
 (ambipolar diffusion,
 molecular diffusion?)

Density structure of MC's



molecular clouds
are highly
inhomogeneous

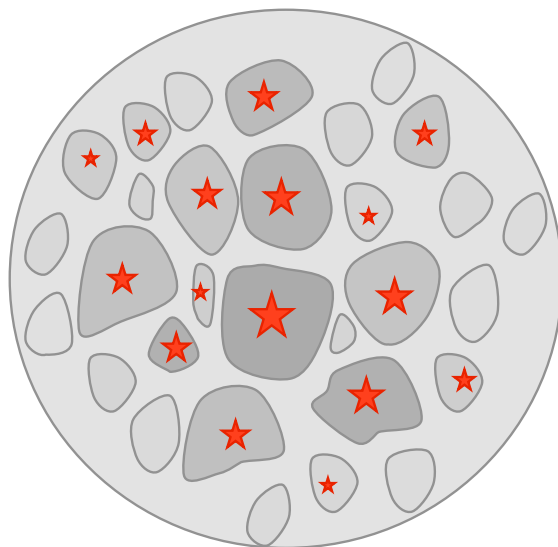
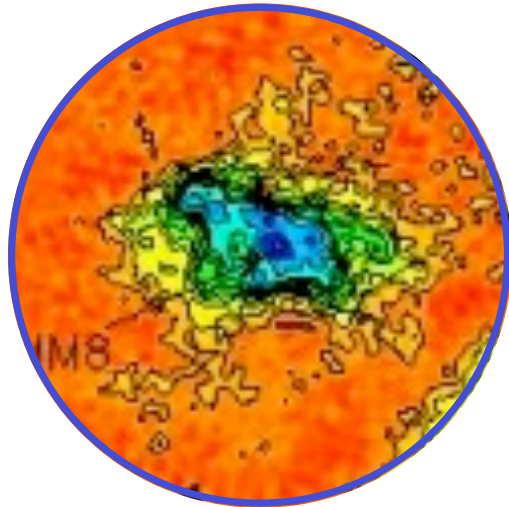
stars form in the
densest and
coldest parts of
the cloud

ρ -Ophiuchus
cloud seen in dust
emission

let's focus on
a cloud core
like this one

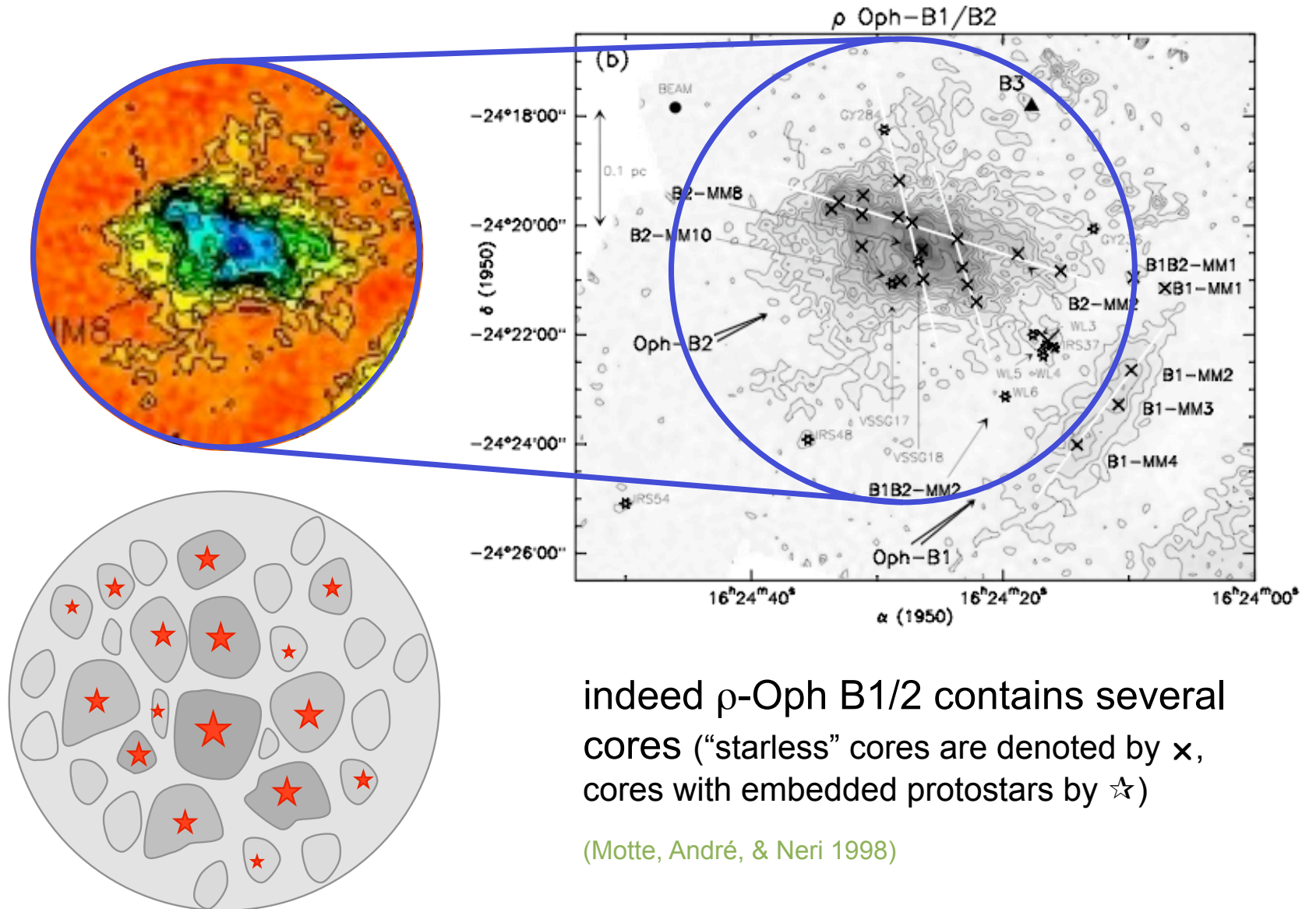
(Motte, André, & Neri 1998)

Evolution of cloud cores



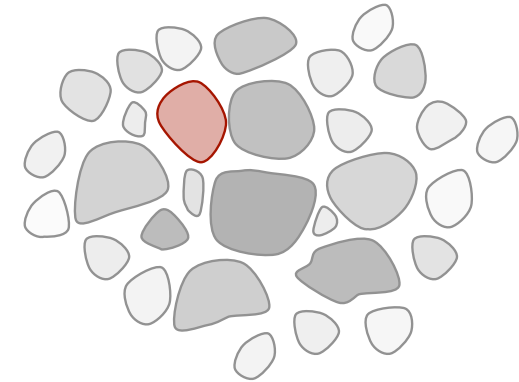
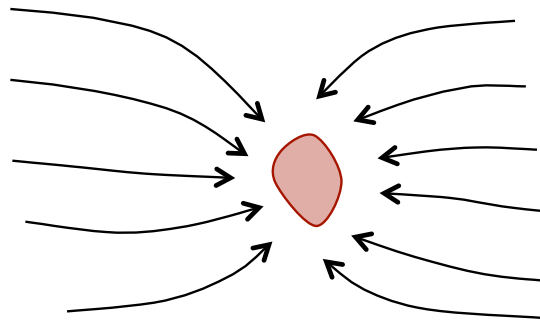
- How does this core evolve?
Does it form one single massive star or cluster with mass distribution?
- Turbulent cascade „goes through“ cloud core
--> NO *scale separation* possible
--> NO *effective sound speed*
- Turbulence is supersonic!
--> produces strong density contrasts:
 $\delta\rho/\rho \approx M^2$
--> with typical $M \approx 10$ --> $\delta\rho/\rho \approx 100!$
- many of the shock-generated fluctuations are Jeans unstable and go into collapse
- --> expectation: *core breaks up and forms a cluster of stars*

Evolution of cloud cores



Formation and evolution of cores

- protostellar cloud cores form at *stagnation point* in *convergent turbulent flows*

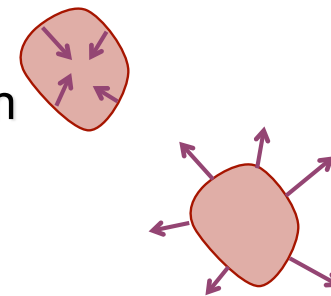


- if $M > M_{\text{crit}} \propto \rho^{-1/2} T^{3/2}$: collapse & star formation

- if $M < M_{\text{crit}} \propto \rho^{-1/2} T^{3/2}$: reexpansion after end of external compression

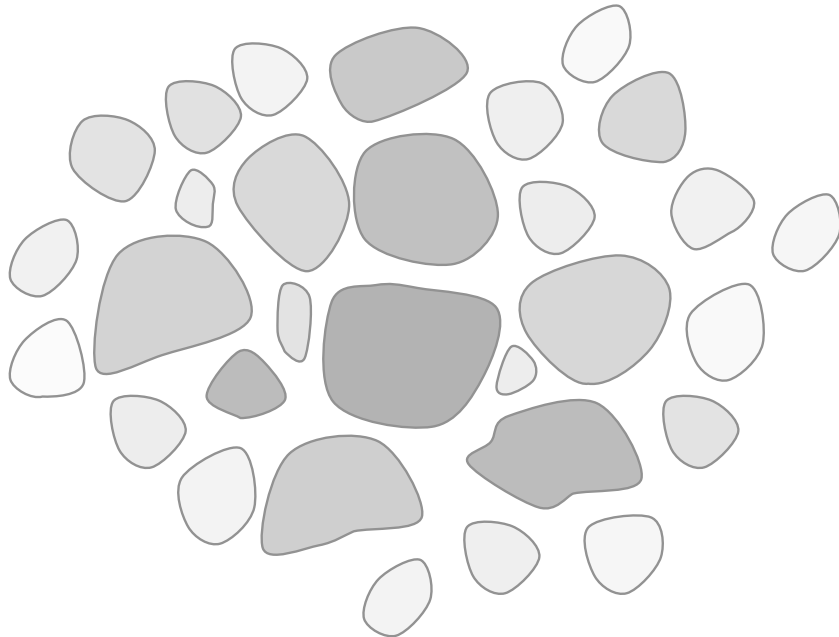
(e.g. Vazquez-Semadeni et al 2005)

- typical timescale: $t \approx 10^4 \dots 10^5$ yr



Formation and evolution of cores

What happens to distribution of cloud cores?



Two extreme cases:

(1) turbulence dominates energy budget:

$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| > 1$$

--> individual cores do *not* interact

--> *collapse of individual cores dominates stellar mass growth*

--> *loose cluster of low-mass stars*

(2) turbulence decays, i.e. gravity

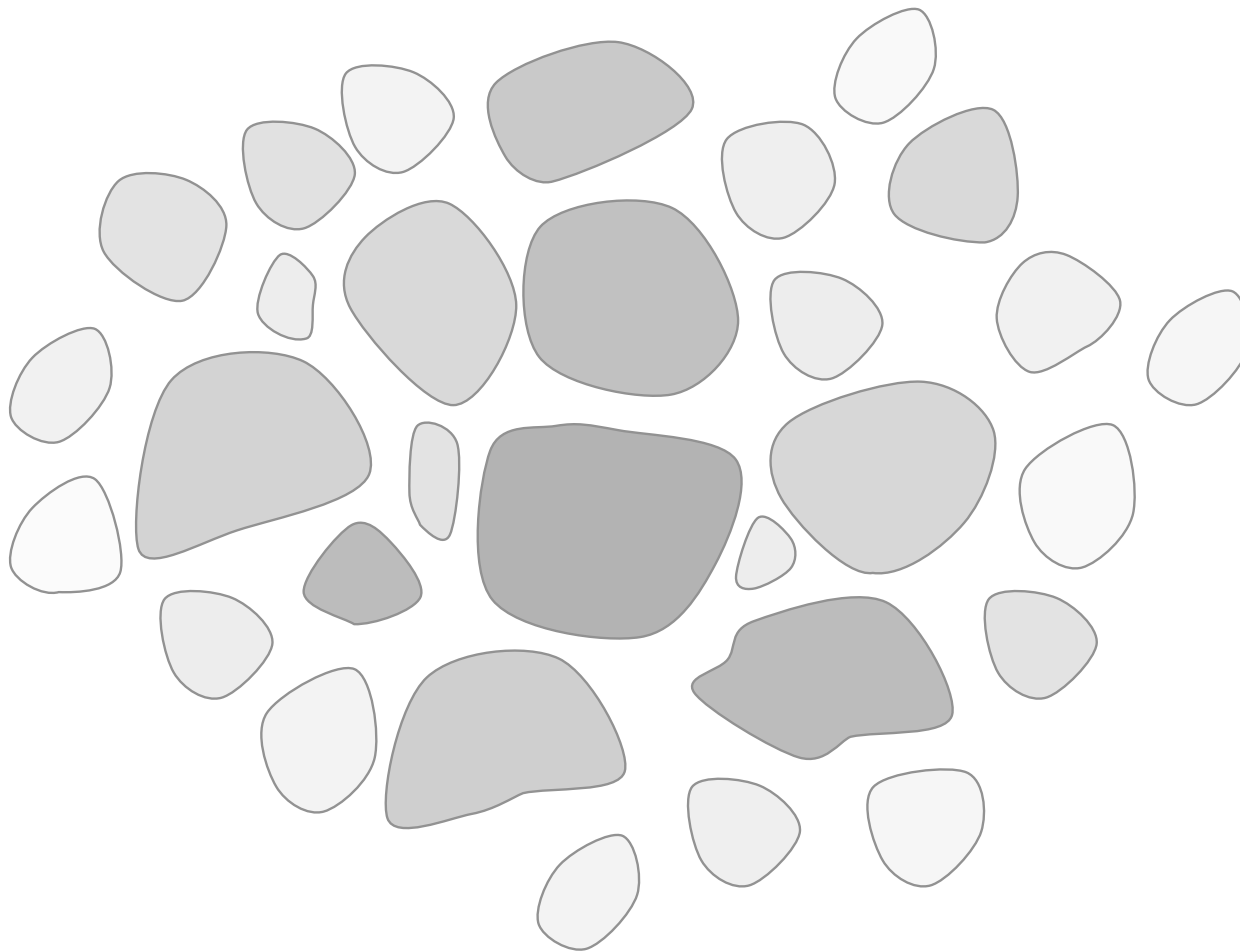
dominates: $\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$

--> *global contraction*

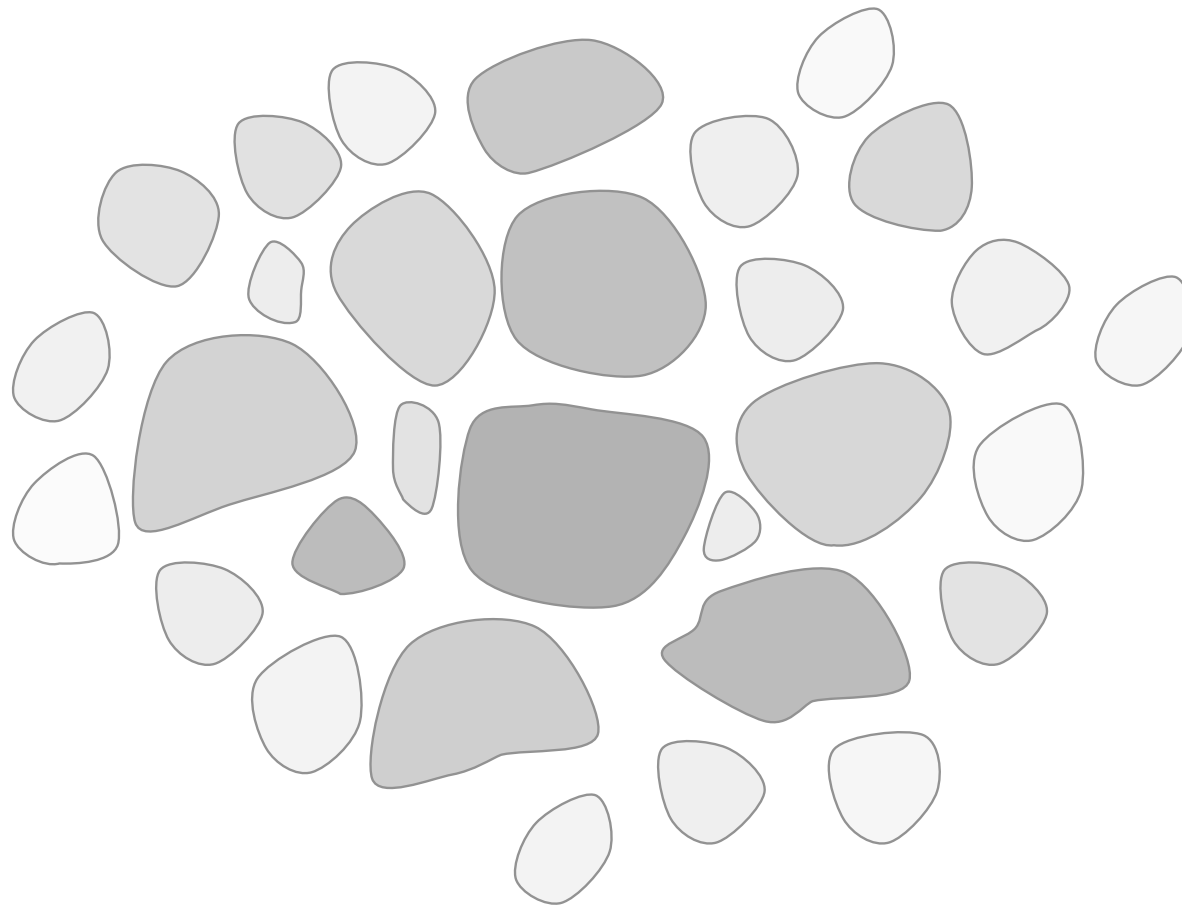
--> *core do interact while collapsing*

--> *competition influences mass growth*

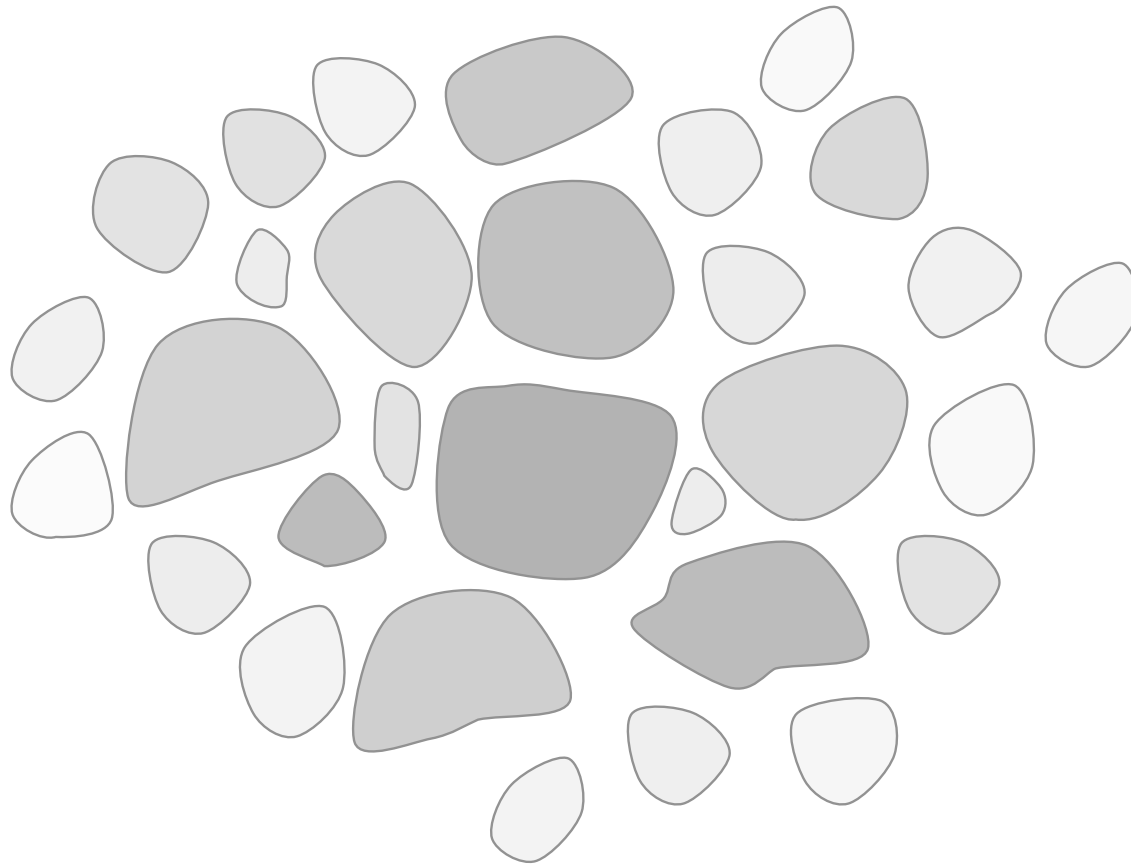
--> *dense cluster with high-mass stars*



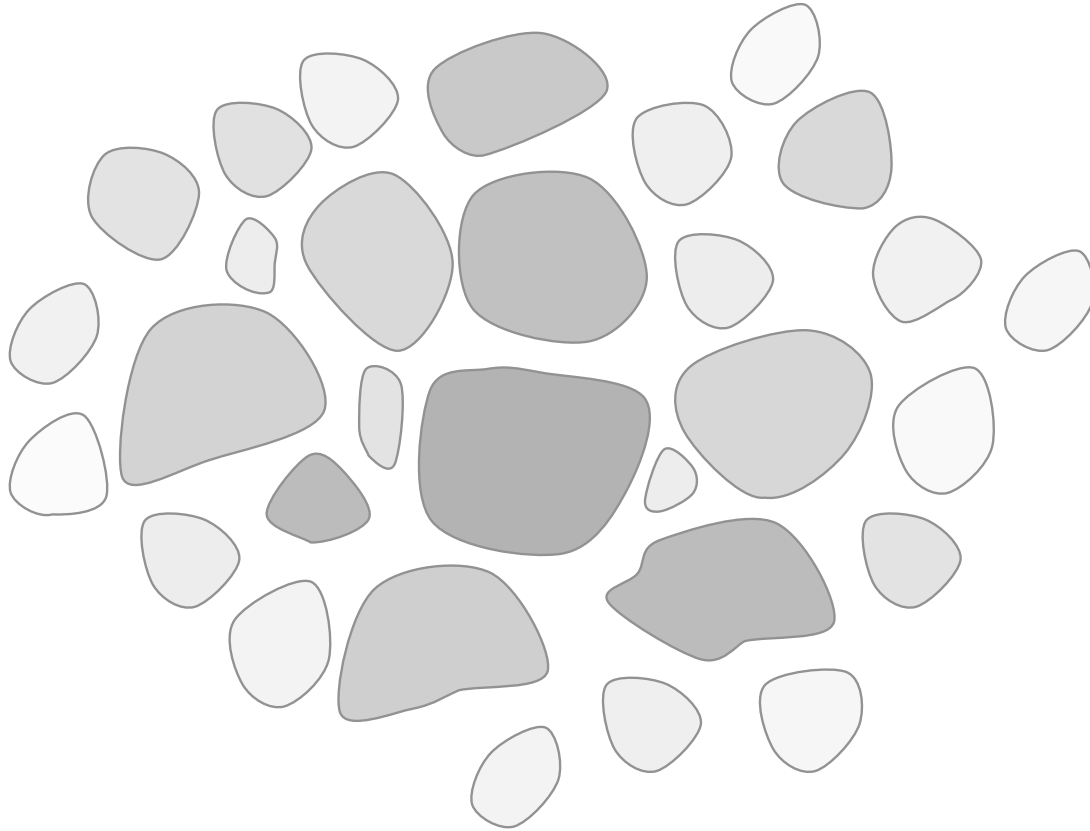
turbulence creates a hierarchy of clumps



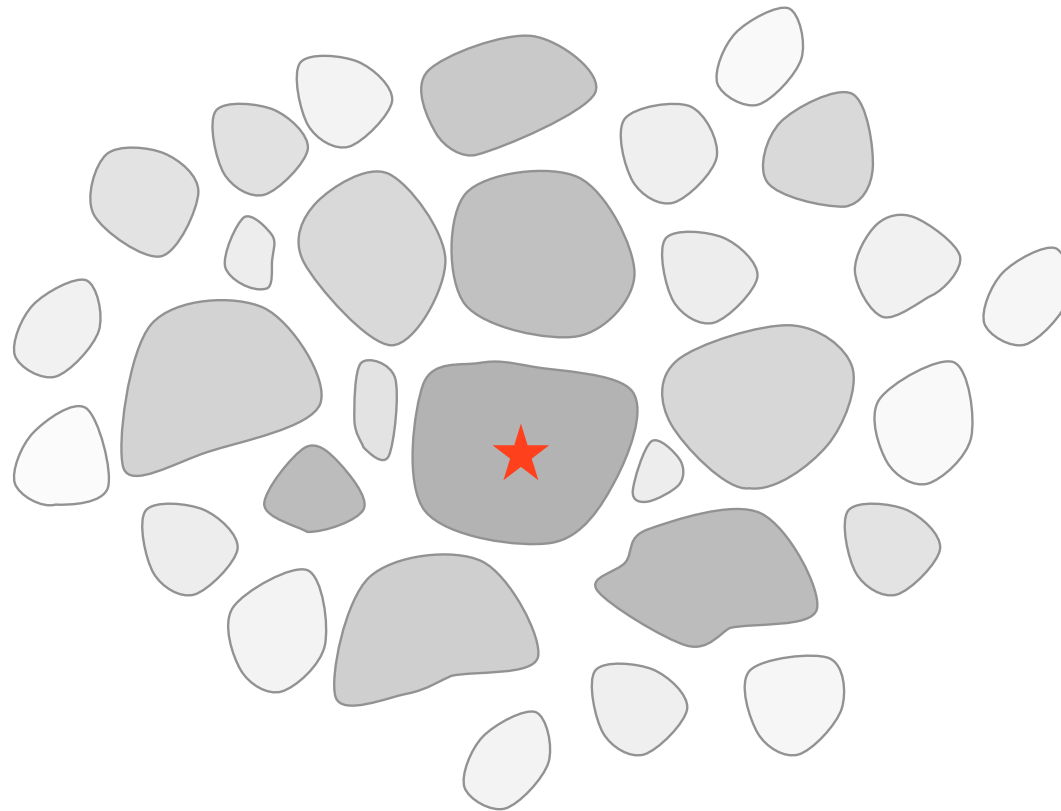
as turbulence decays locally, contraction sets in



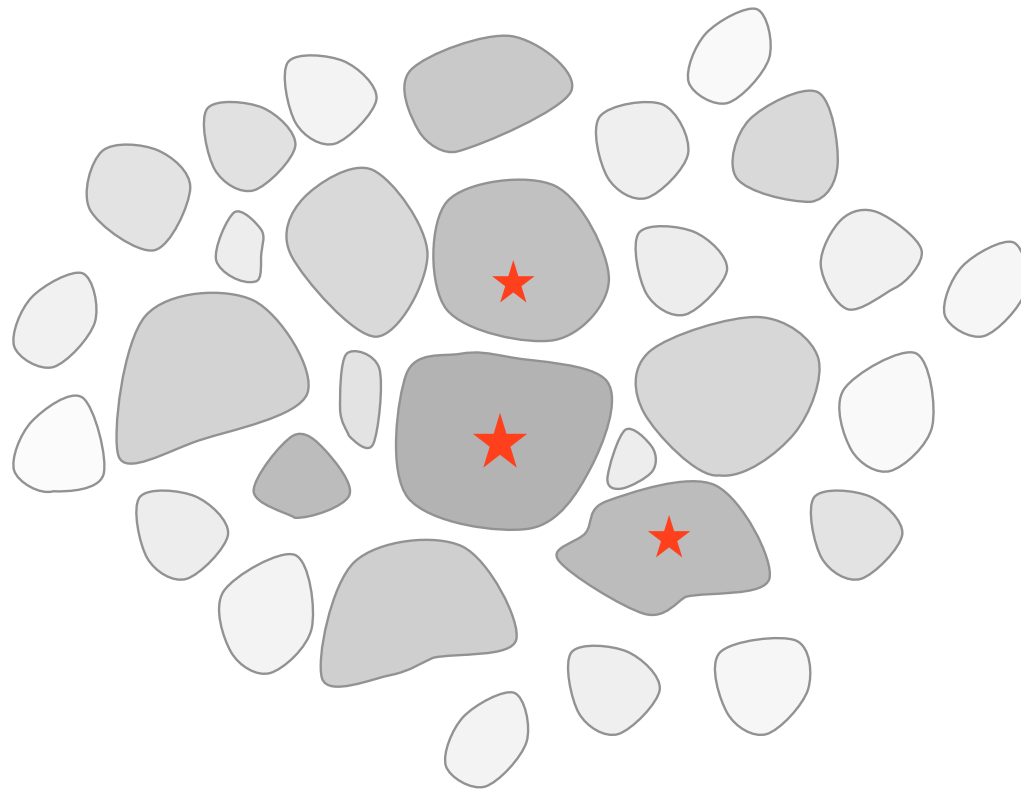
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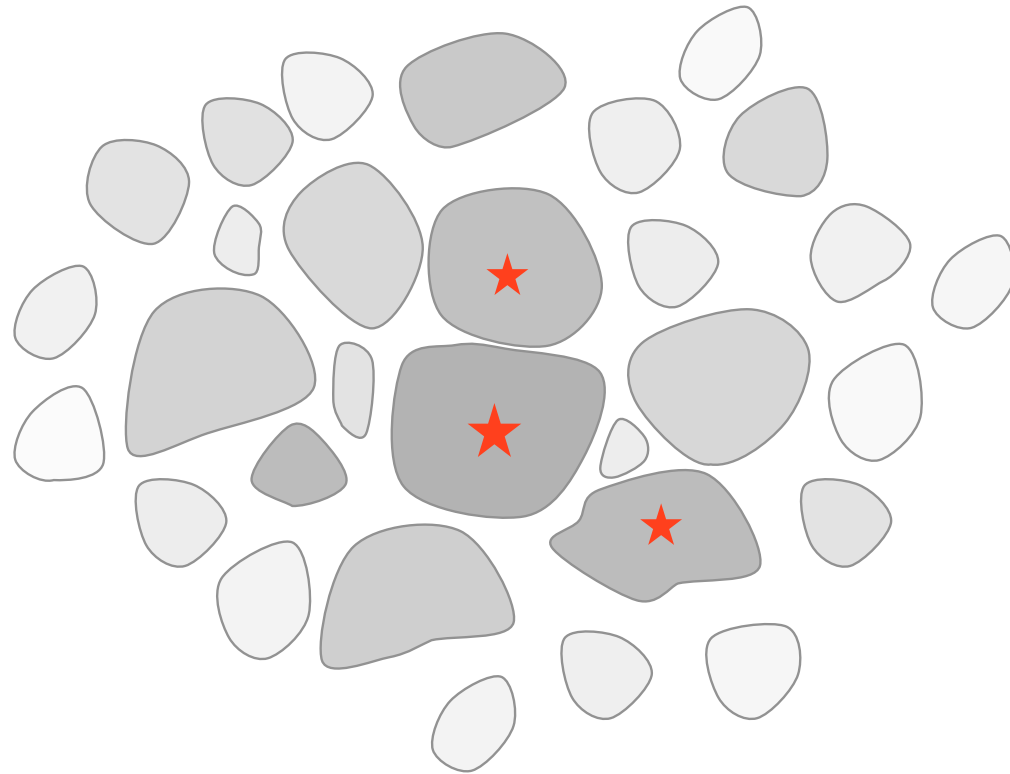
while region contracts, individual clumps collapse to form stars



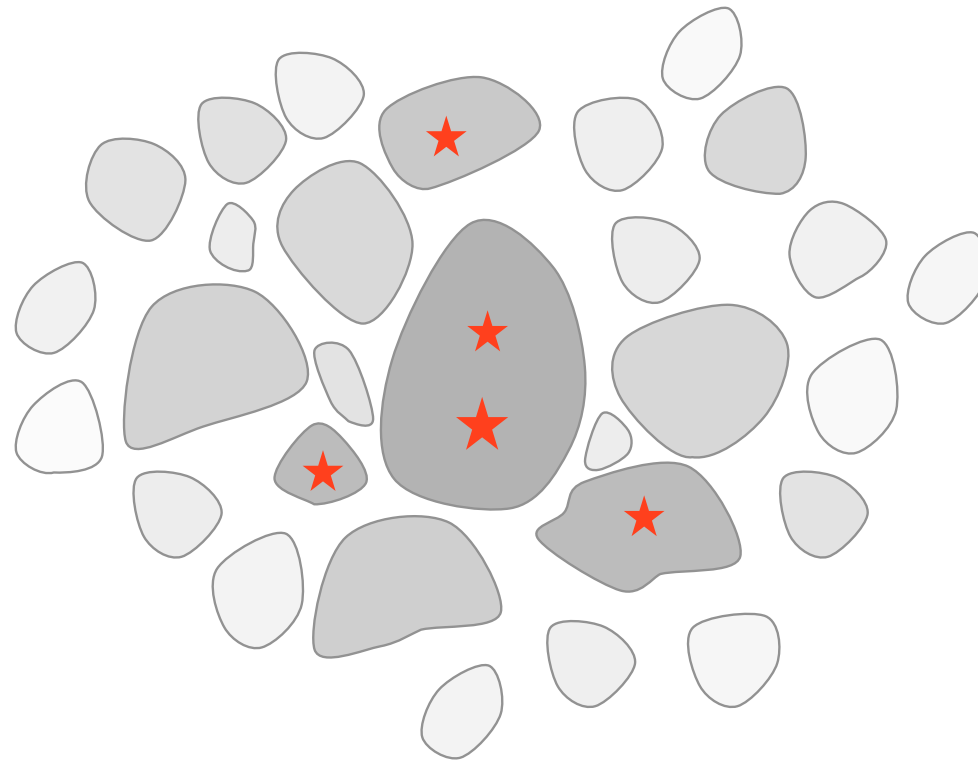
while region contracts, individual clumps collapse to form stars



individual clumps collapse to form stars

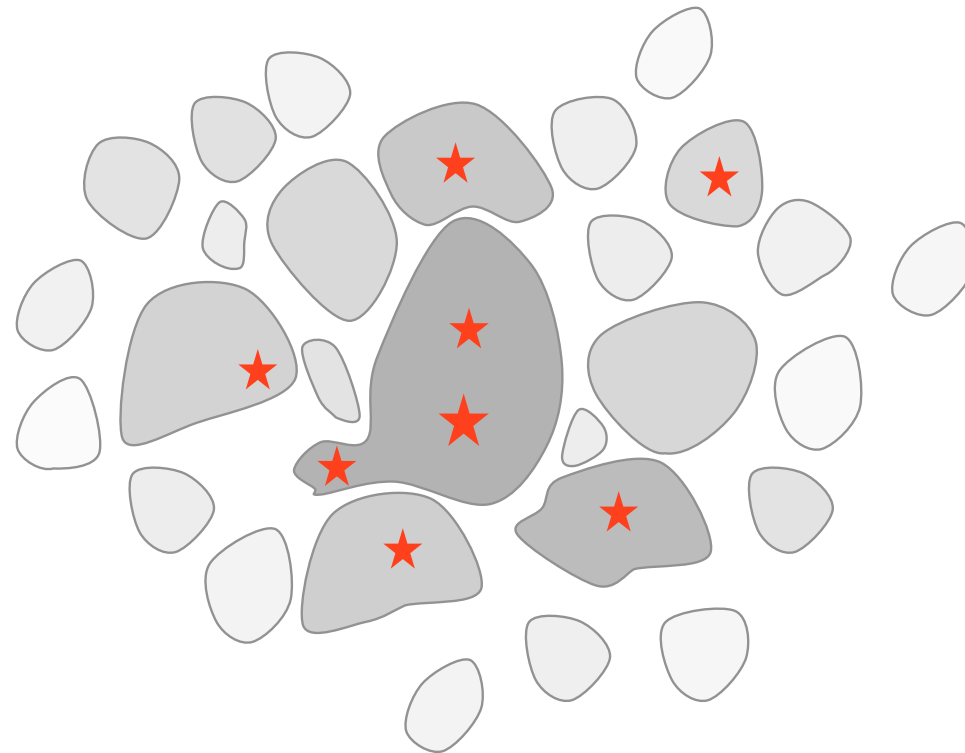


individual clumps collapse to form stars

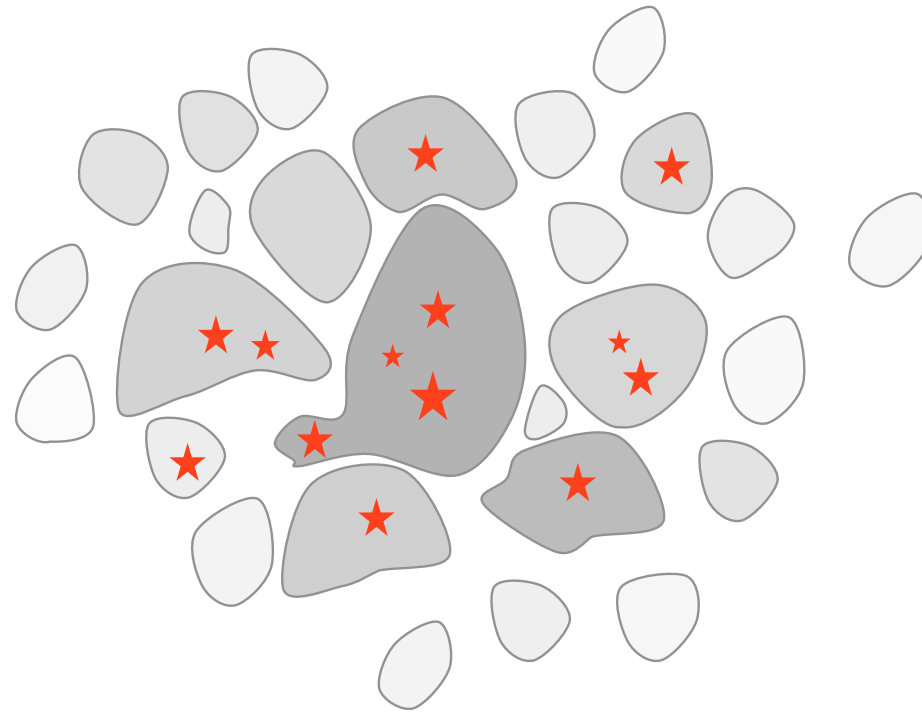


$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

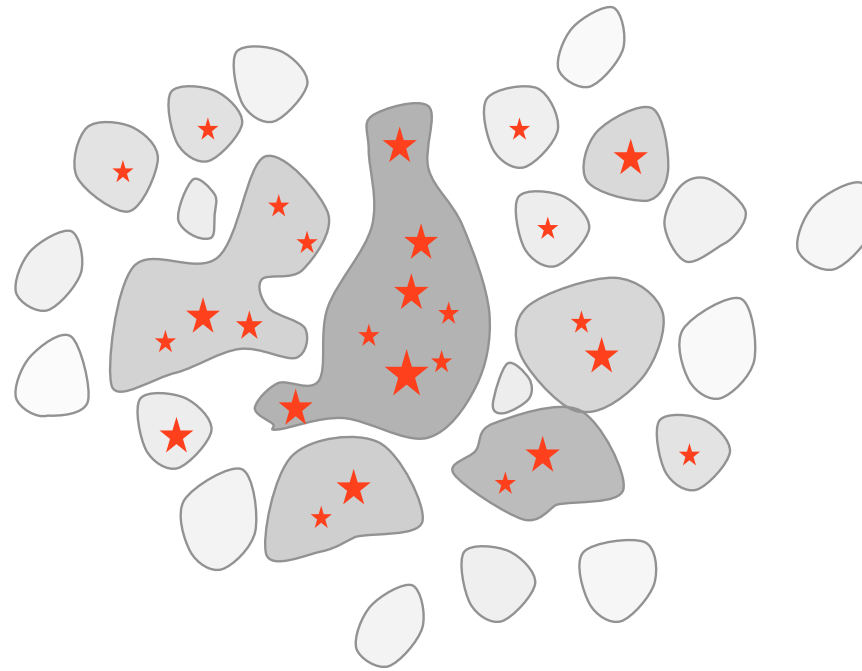
in *dense clusters*, clumps may merge while collapsing
--> then contain multiple protostars



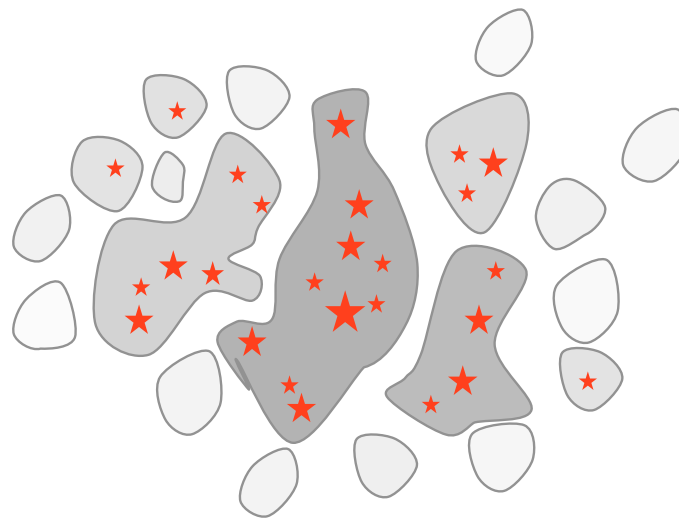
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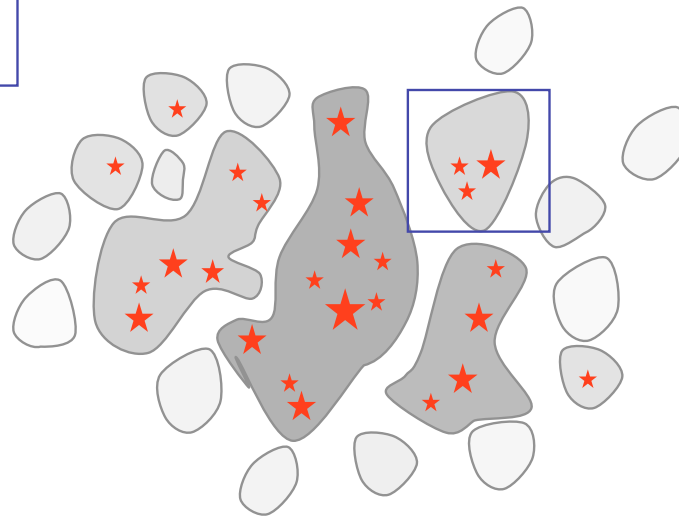
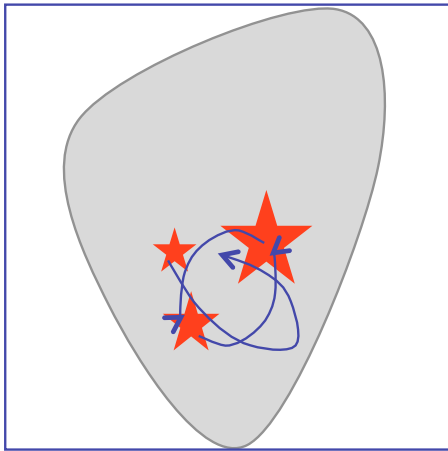
in *dense clusters*, clumps may merge while collapsing
--> then contain multiple protostars



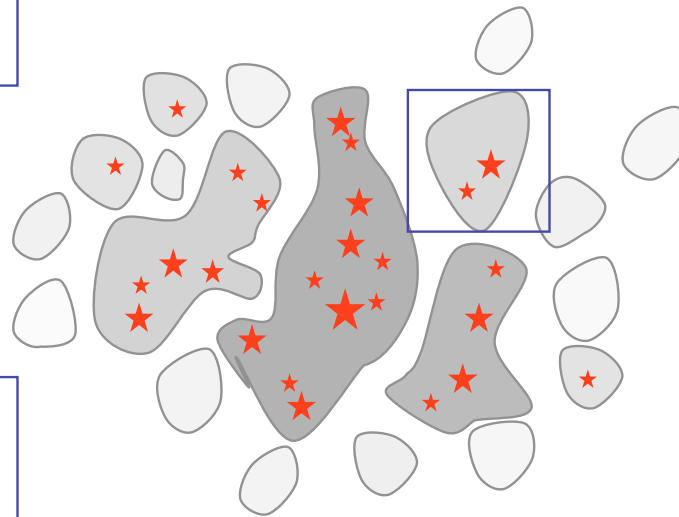
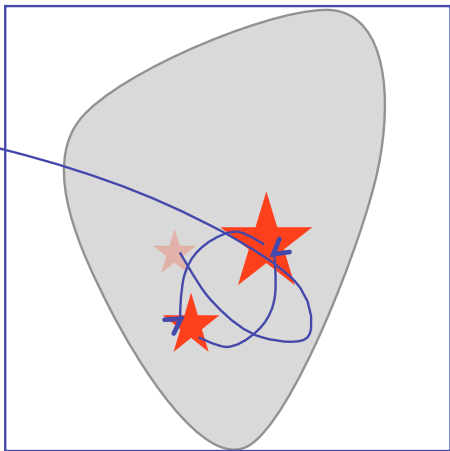
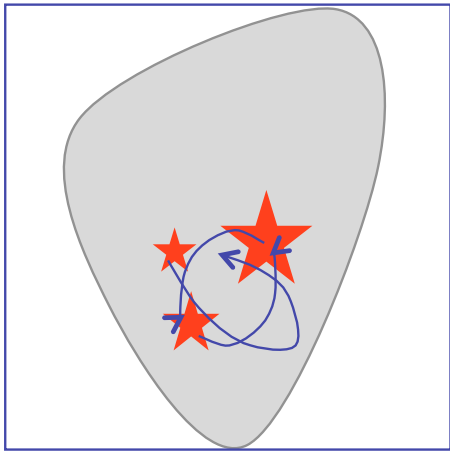
in *dense clusters*, competitive mass growth becomes important



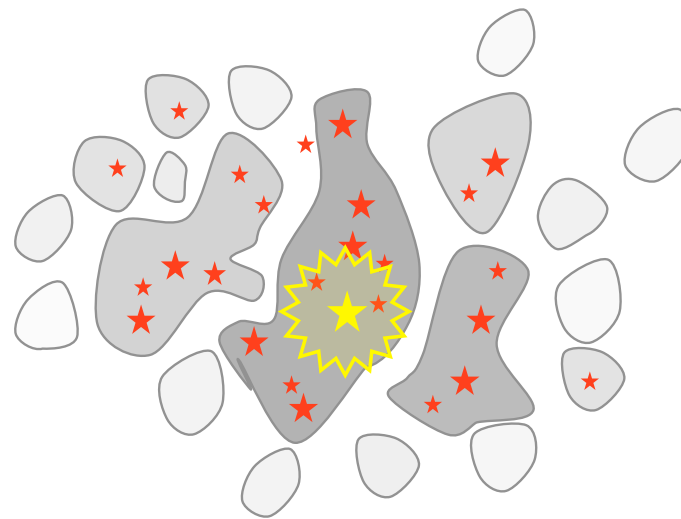
in *dense clusters*, competitive mass growth becomes important



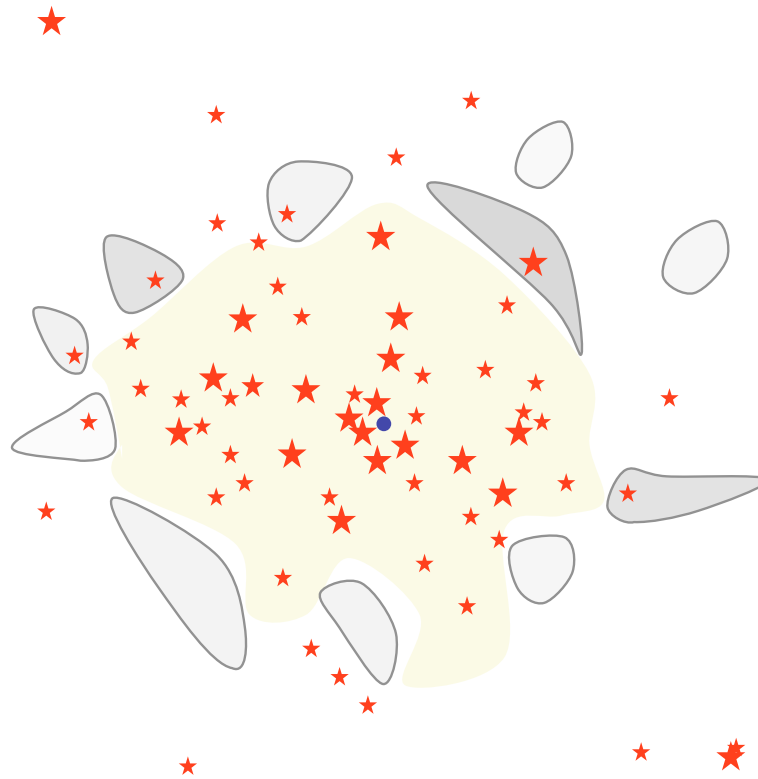
in *dense clusters*, N -body effects influence mass growth



low-mass objects may
become ejected --> accretion stops



feedback terminates star formation



result: *star cluster*, possibly with HII region

predictions

Predictions

- *global properties* (statistical properties)
 - SF efficiency and timescale
 - stellar mass function -- IMF
 - dynamics of young star clusters
 - description of self-gravitating turbulent systems (pdf's, Δ -var.)
 - chemical mixing properties
- *local properties* (properties of individual objects)
 - properties of individual clumps (e.g. shape, radial profile, lifetimes)
 - accretion history of individual protostars (dM/dt vs. t , j vs. t)
 - binary (proto)stars (eccentricity, mass ratio, etc.)
 - SED's of individual protostars
 - dynamic PMS tracks: $T_{\text{bol}}-L_{\text{bol}}$ evolution

Examples and predictions

example 1: star cluster formation: *dynamics*

example 2: star cluster formation: *thermodynamics*
--> speculations on the origin of the stellar
mass spectrum (IMF)

example 1

Example: model of Orion cloud

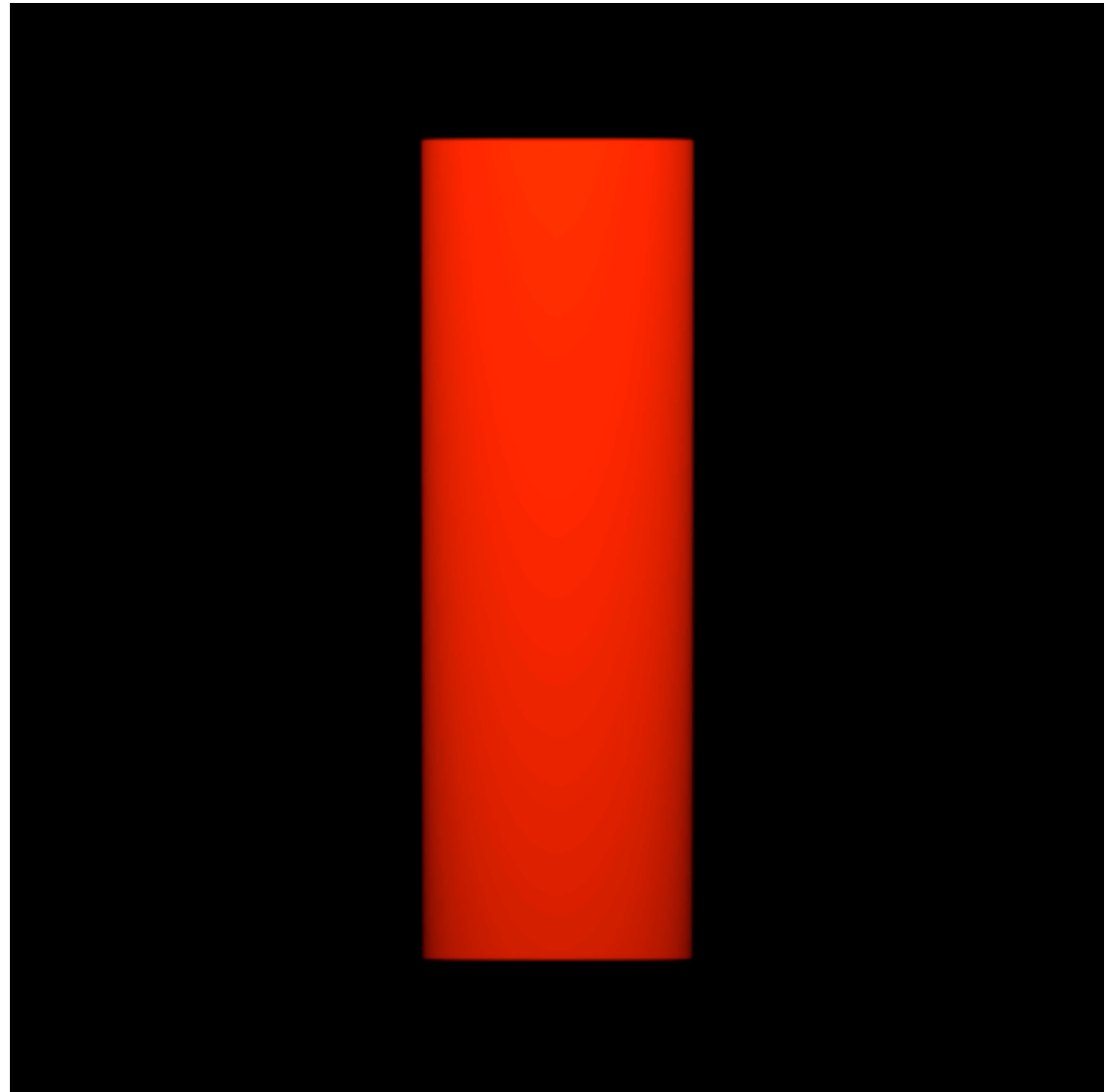
„model“ of Orion cloud:
15.000.000 SPH particles,
 $10^4 M_{\text{sun}}$ in 10 pc, mass
resolution $0,02 M_{\text{sun}}$, forms
~2.500 „stars“ (sink particles)

isothermal EOS, top bound,
bottom unbound

has clustered as well as
distributed „star“ formation

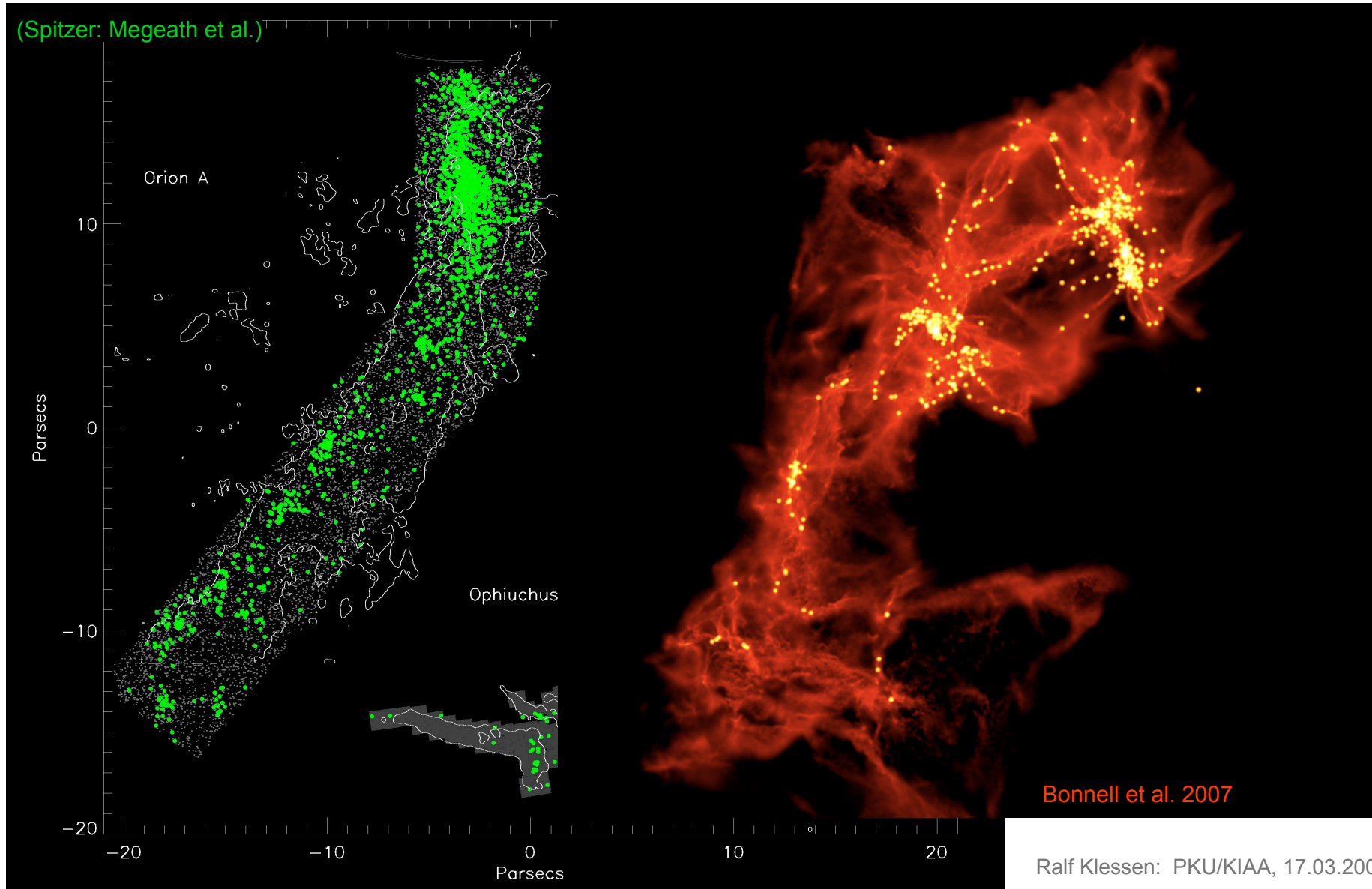
efficiency varies from 1% to
20%

develops full IMF
(distribution of sink particle masses)



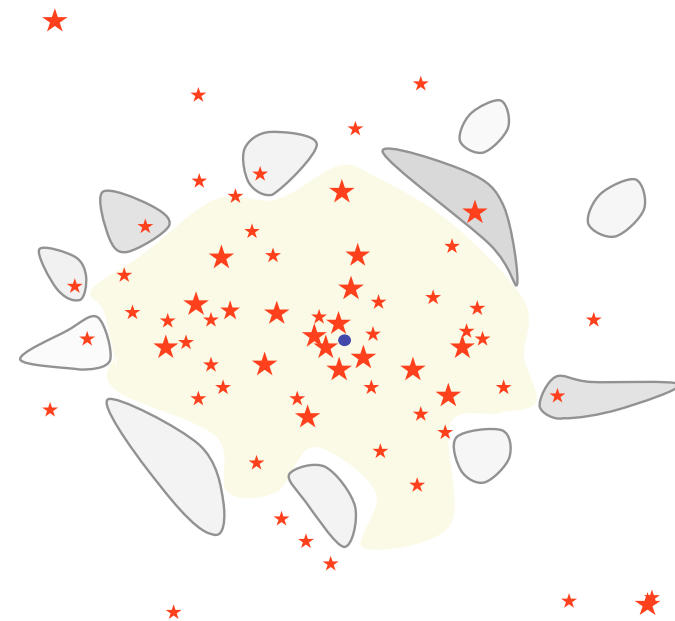
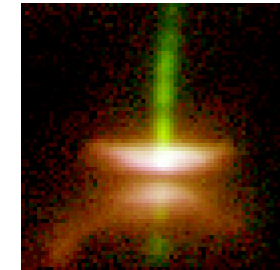
(Bonnell et al. 2007)

Example: model of Orion cloud



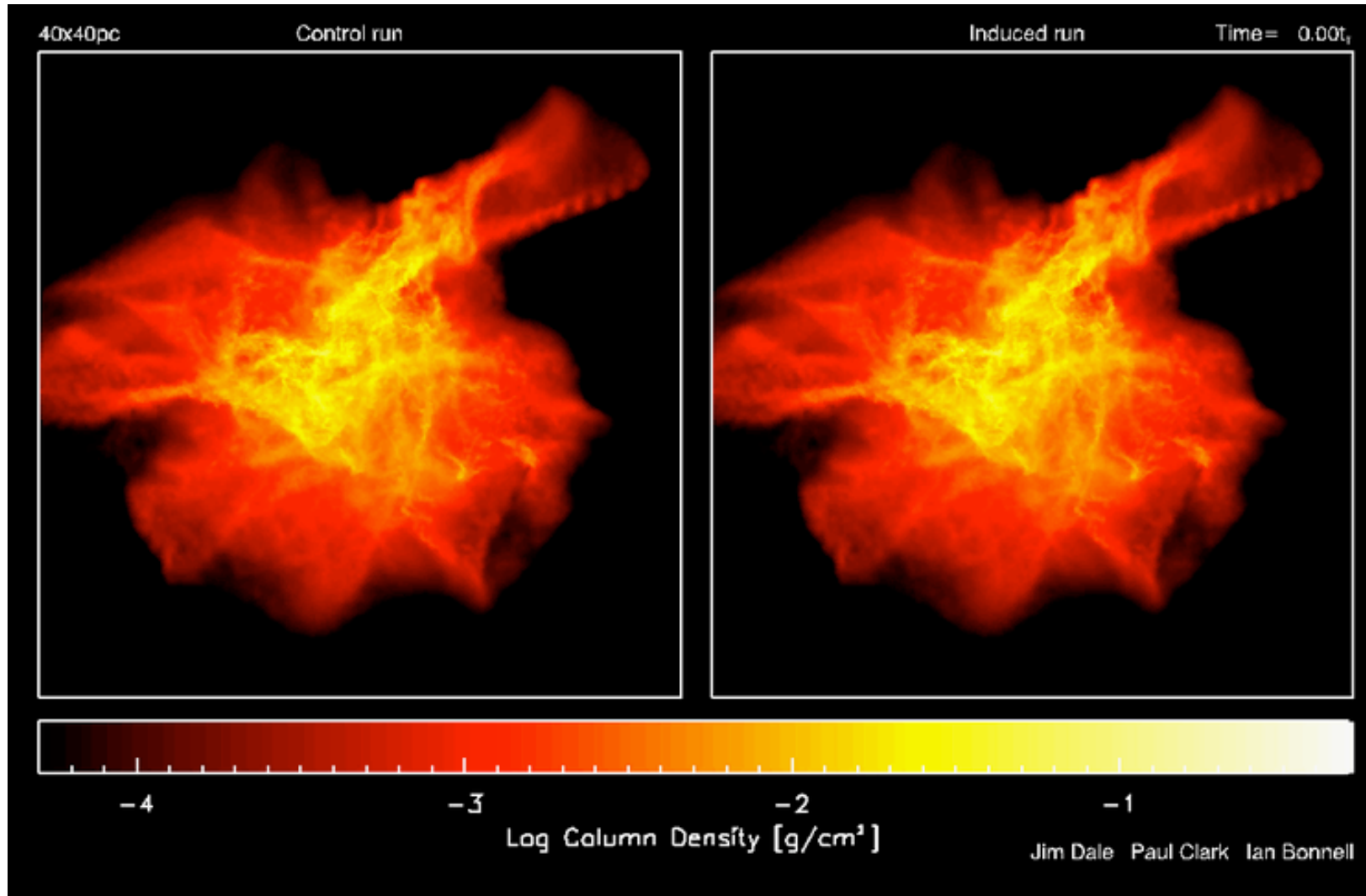
Models of star cluster formation

- dynamics:
basic properties are probably okay
- BUT: no feedback
(outflows, radiation, etc.)
- *how much detail are we missing?*
 - how does that change properties like *IMF*, *boundedness*, *efficiency*?



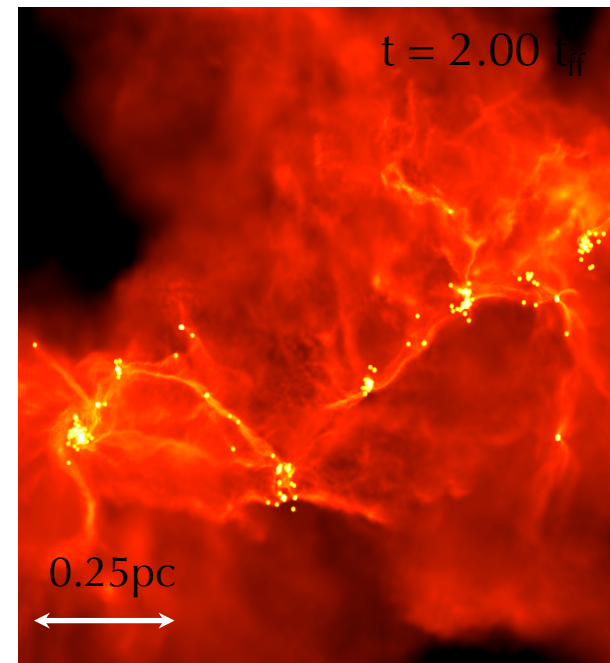
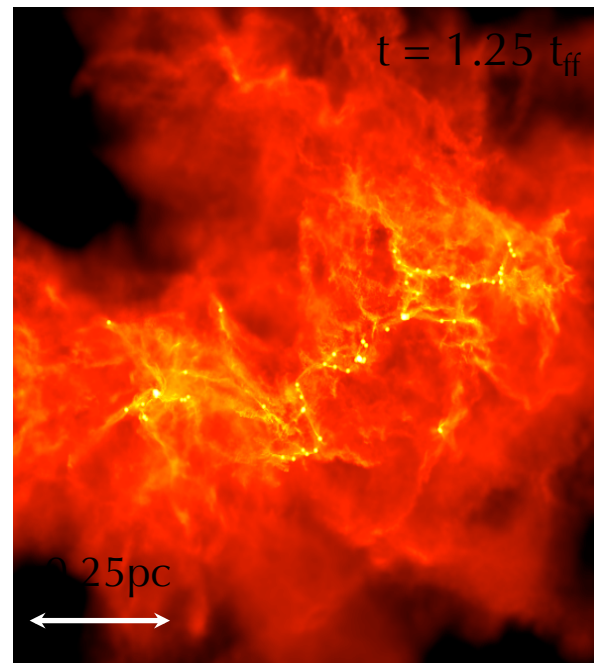
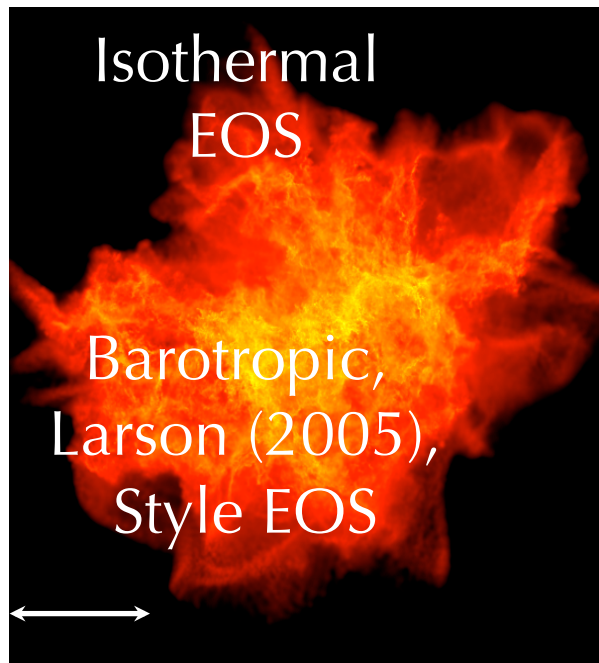
Model with ionizing feedback

SPH with radiation feedback: first calculations of star-cluster formation with ionization



Unbound clouds

KE = 2 x PE (initially), 1000 solar masses, 0.5pc



No global collapse:

local $t_{ff} <$ global interaction time
-scale

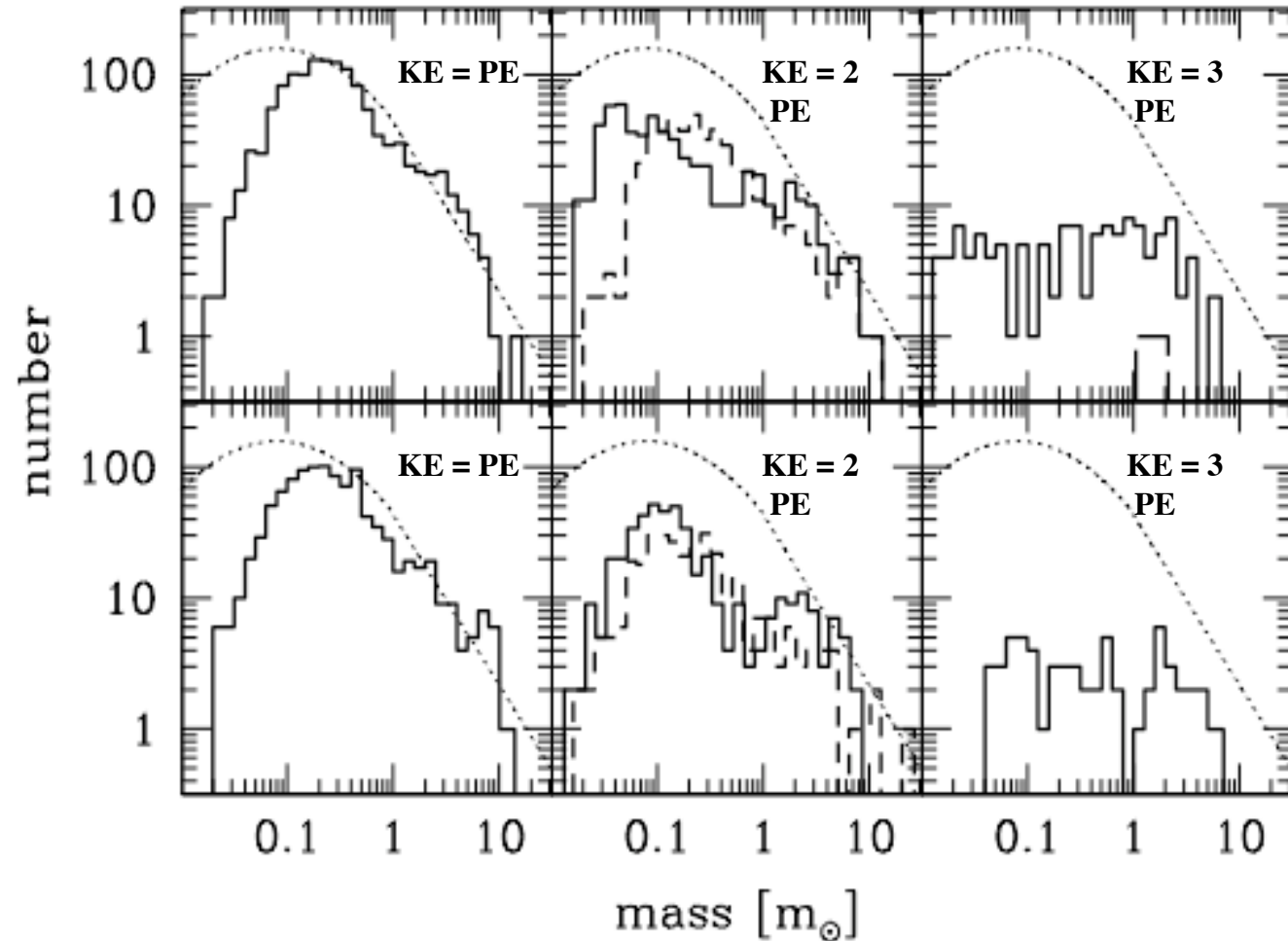
$$t_{ff} \sim 2 \times 10^5 \text{ years}$$

Clark, Bonnell & Klessen (2007)

Mass functions

Isothermal
EOS

Barotropic,
Larson
(2005), Style
EOS



Clark, Bonnell & Klessen (2007)

example 2

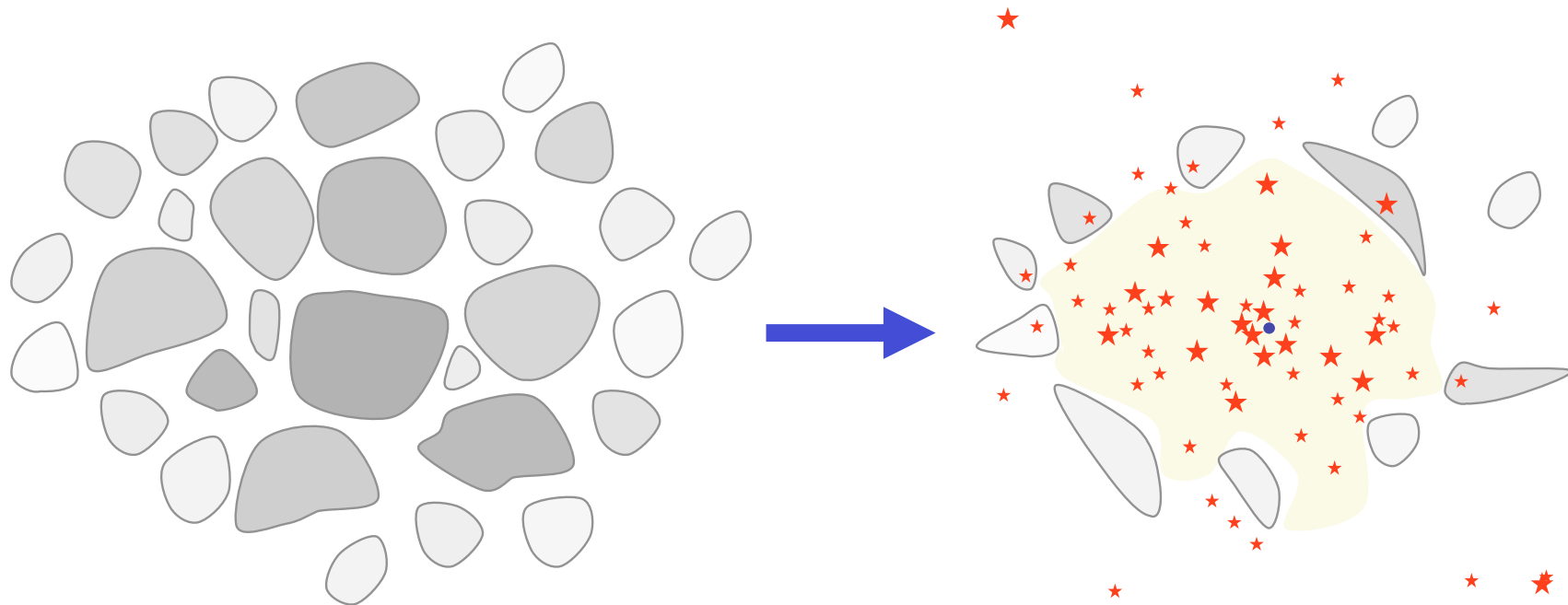
IMF

- distribution of stellar masses depends on
 - turbulent initial conditions
 - > mass spectrum of prestellar cloud cores
 - collapse and interaction of prestellar cores
 - > competitive accretion and N -body effects
 - thermodynamic properties of gas
 - > balance between heating and cooling
 - > EOS (determines which cores go into collapse)
 - (proto) stellar feedback terminates star formation
 - ionizing radiation, bipolar outflows, winds, SN

(e.g. Larson 2003, Prog. Rep. Phys.; Mac Low & Klessen, 2004, Rev. Mod. Phys, 76, 125 - 194)

Star cluster formation

Most stars form in clusters → *star formation = cluster formation*



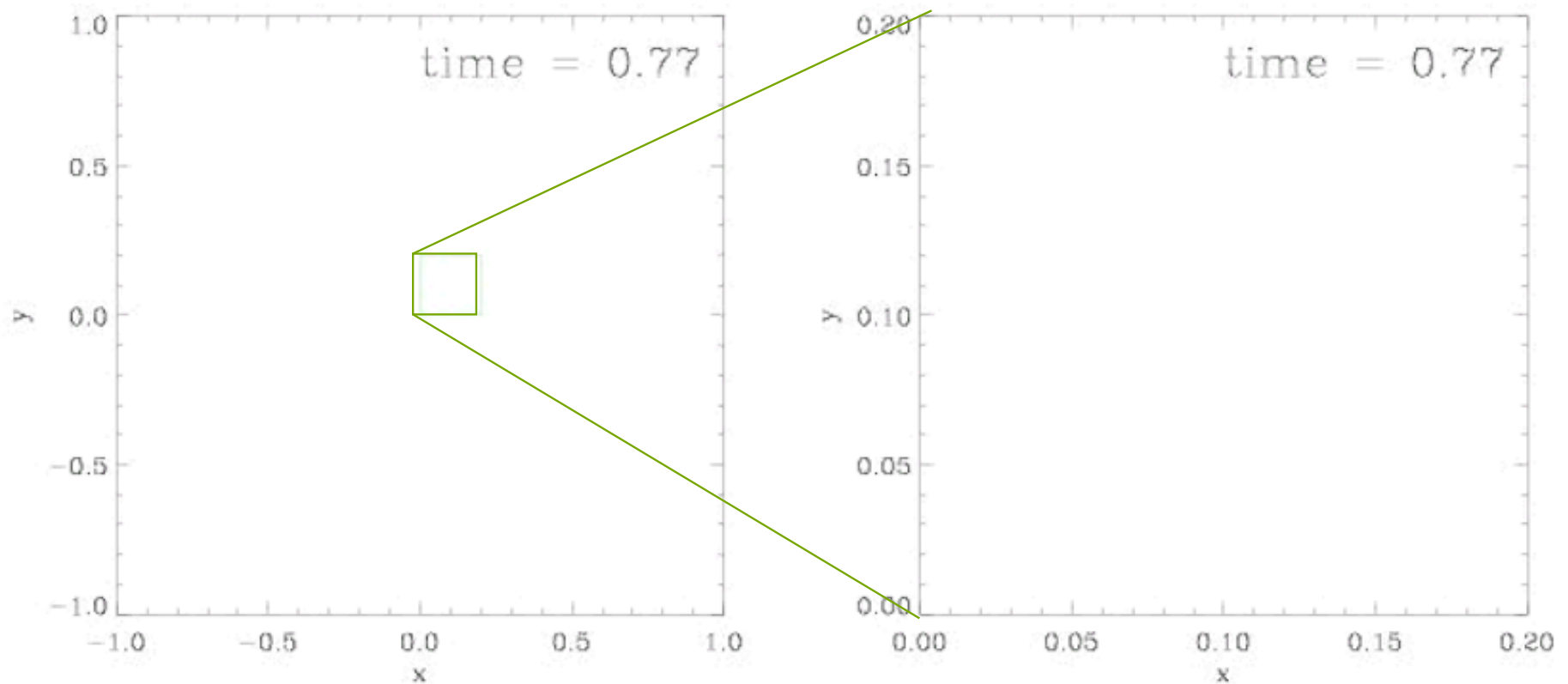
How to get from **cloud cores** to **star clusters**?

How do the stars **acquire mass**?

(e.g. Larson 2003, Prog. Rep. Phys.; Mac Low & Klessen, 2004, Rev. Mod. Phys, 76, 125 - 194)

Dynamics of nascent star cluster

in dense clusters protostellar interaction may be come important!

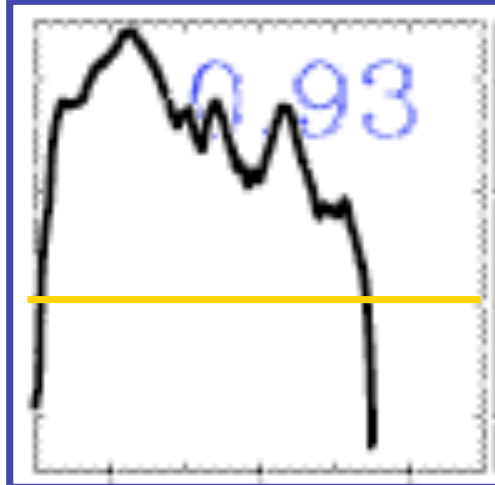
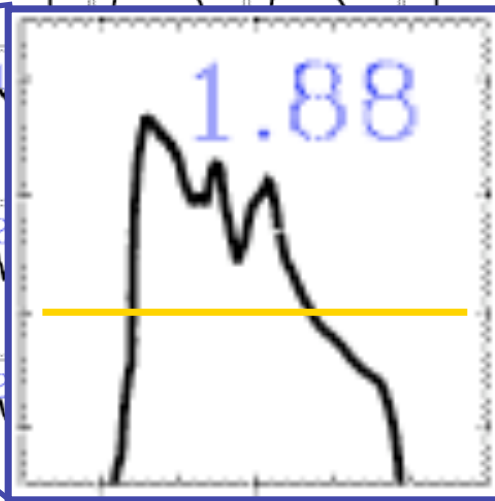
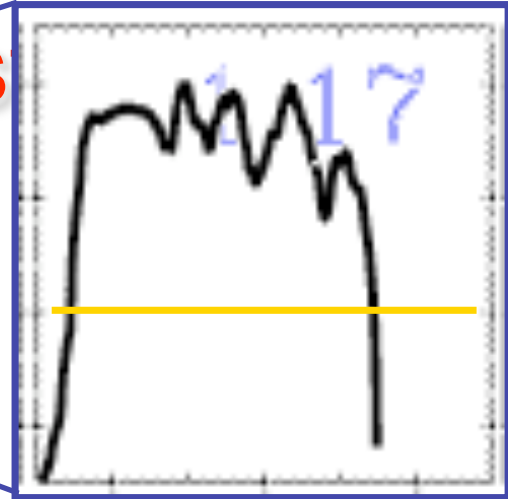
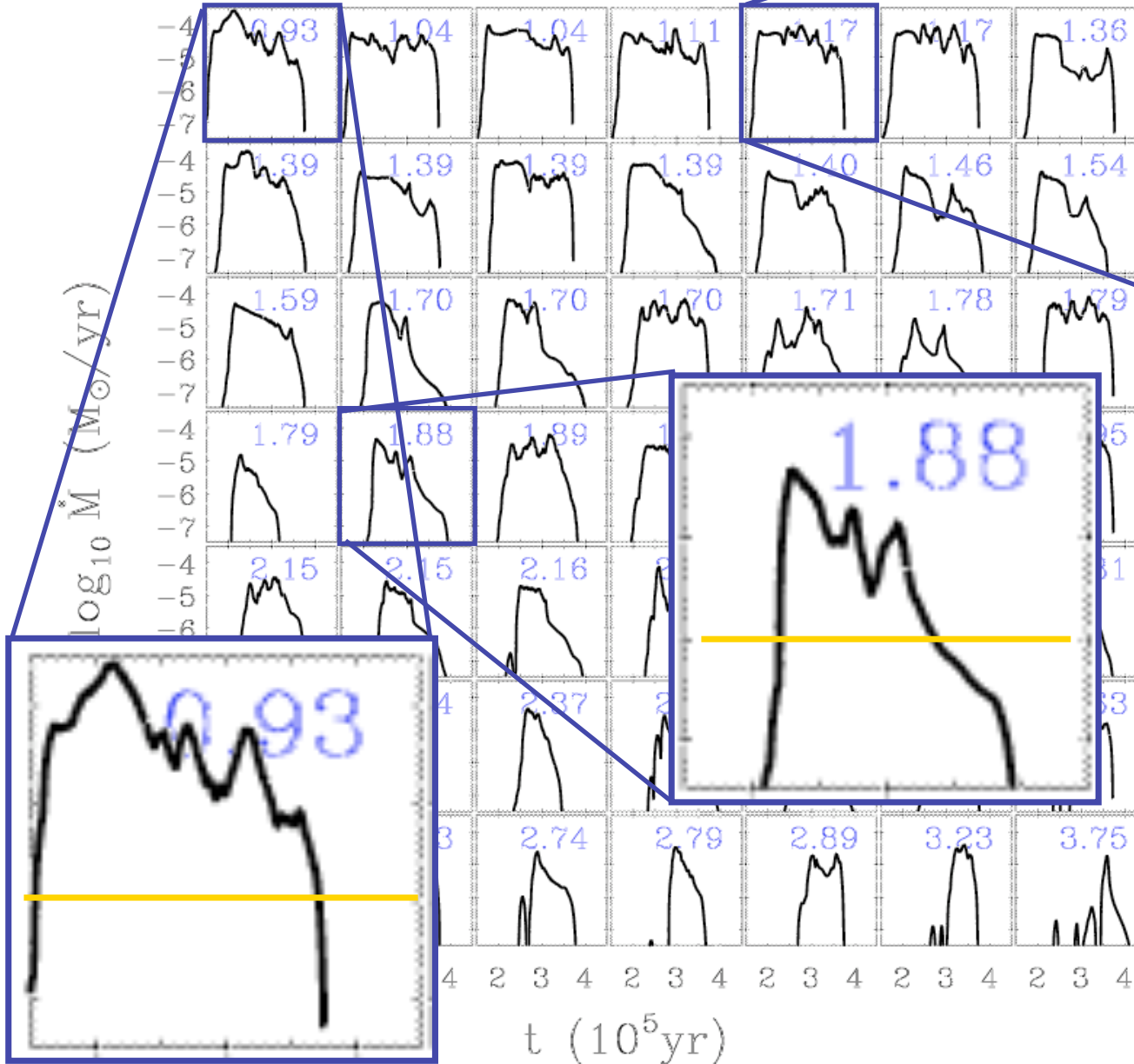


Trajectories of protostars in a nascent dense cluster created by gravoturbulent fragmentation

(from Klessen & Burkert 2000, ApJS, 128, 287)

Ralf Klessen: PKU/KIAA, 17.03.2008

Accretion rates in clus



Mass accretion rates *vary with time* and are strongly *influenced* by the *cluster environment*.

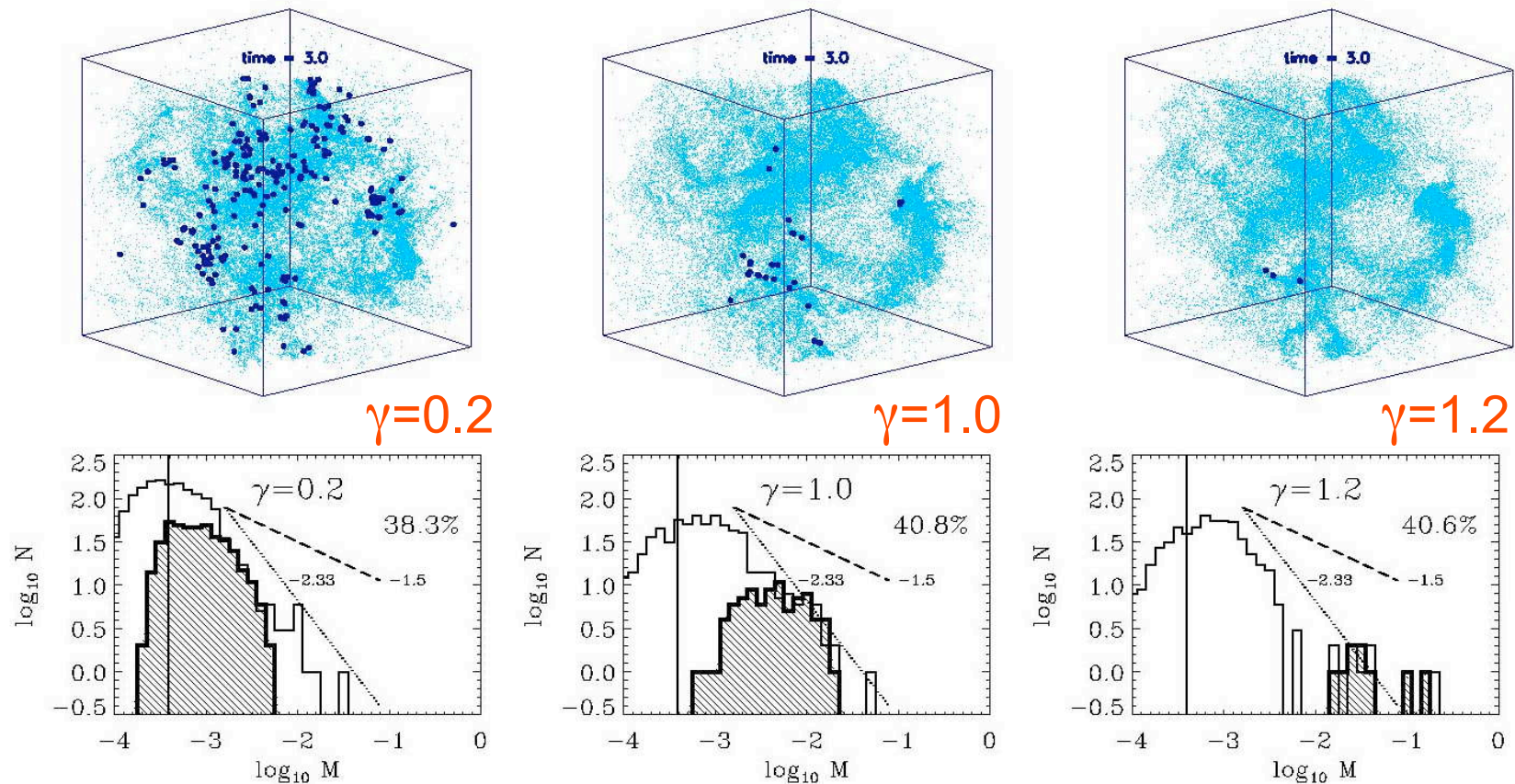
(Klessen 2001, ApJ, 550, L77;
also Schmeja & Klessen,
2004, A&A, 419, 405)

Dependency on EOS

- degree of fragmentation depends on *EOS!*
- polytropic EOS: $p \propto \rho^\gamma$
- $\gamma < 1$: dense cluster of low-mass stars
- $\gamma > 1$: isolated high-mass stars

(see Li, Klessen, & Mac Low 2003, ApJ, 592, 975; also Kawachi & Hanawa 1998, Larson 2003)

Dependency on EOS



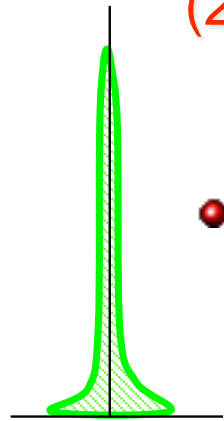
for $\gamma < 1$ fragmentation is enhanced \rightarrow *cluster of low-mass stars*
 for $\gamma > 1$ it is suppressed \rightarrow formation of *isolated massive stars*

(from Li, Klessen, & Mac Low 2003, ApJ, 592, 975)

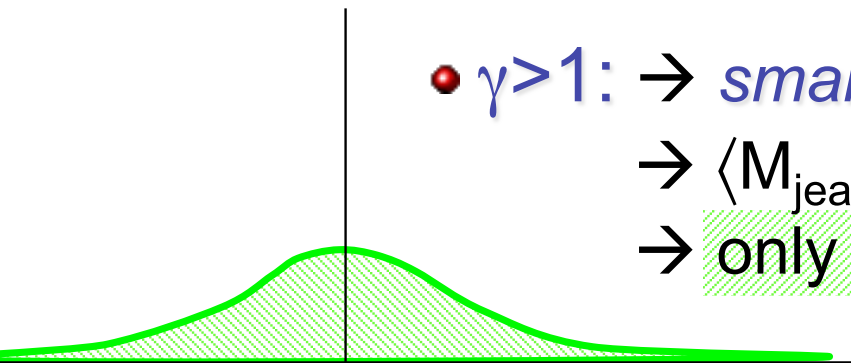
How does that work?

$$(1) \mathbf{p} \propto \rho^\gamma \quad \rightarrow \quad \rho \propto \mathbf{p}^{1/\gamma}$$

$$(2) \mathbf{M}_{\text{jeans}} \propto \gamma^{3/2} \rho^{(3\gamma-4)/2}$$



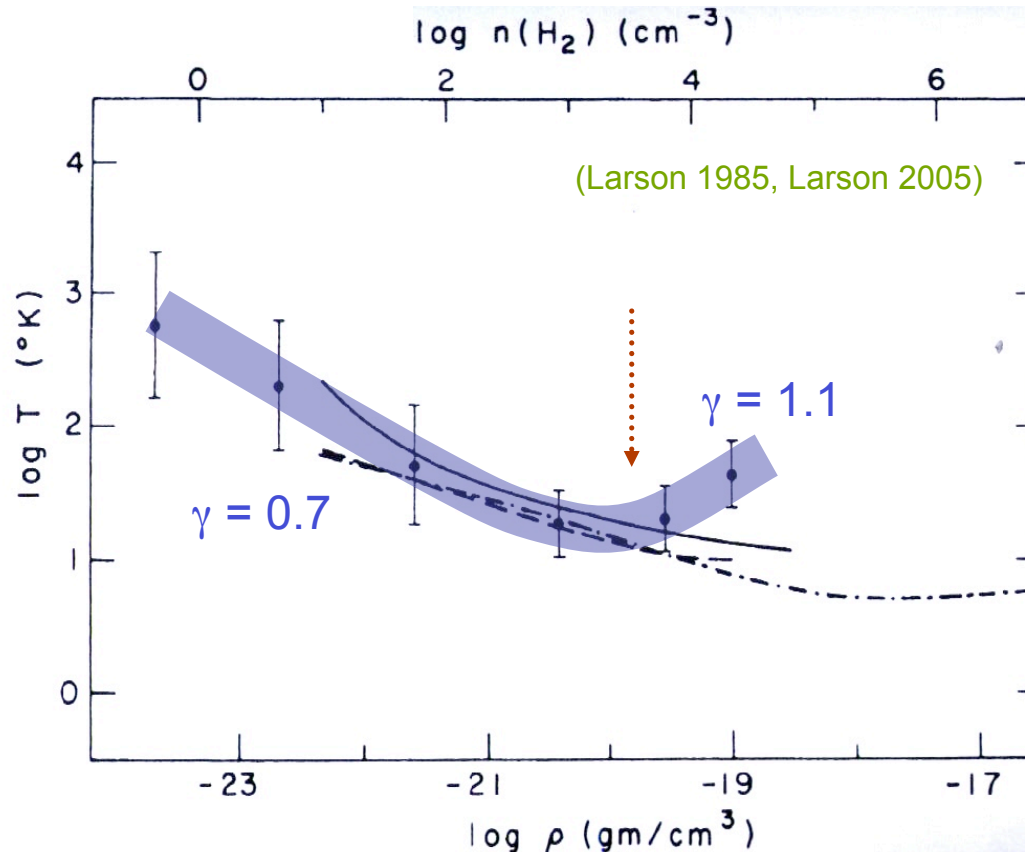
- $\gamma < 1$: \rightarrow *large* density excursion for given pressure
 \rightarrow $\langle M_{\text{jeans}} \rangle$ becomes small
 \rightarrow number of fluctuations with $M > M_{\text{jeans}}$ is large



- $\gamma > 1$: \rightarrow *small* density excursion for given pressure
 \rightarrow $\langle M_{\text{jeans}} \rangle$ is large
 \rightarrow only few and massive clumps exceed M_{jeans}

EOS for solar neighborhood

below $10^{-18} \text{ gcm}^{-3}$: $\rho \uparrow \Rightarrow T \downarrow$
 above $10^{-18} \text{ gcm}^{-3}$: $\rho \uparrow \Rightarrow T \uparrow$



$$P \propto \rho^\gamma$$

$$P \propto \rho T$$

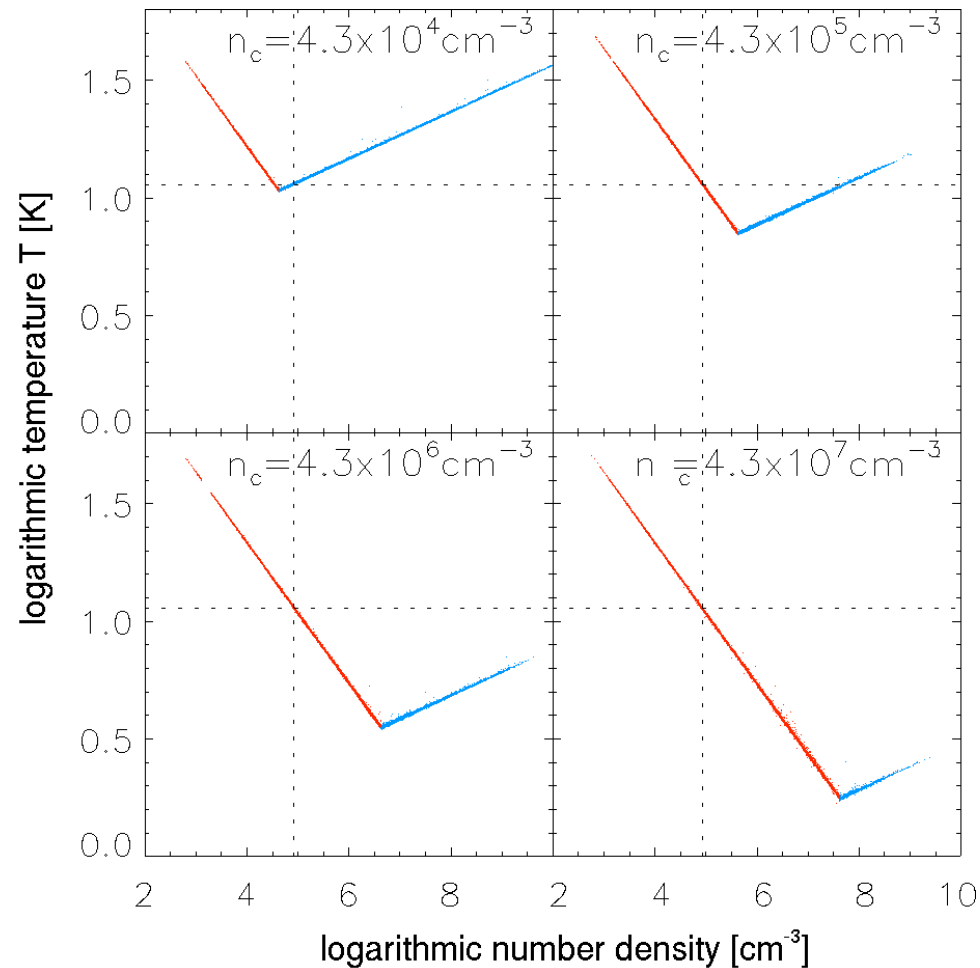
$$\rightarrow \gamma = 1 + d \ln T / d \ln \rho$$

IMF from simple piece-wise polytropic EOS

$$\gamma_1 = 0.7$$

$$\gamma_2 = 1.1$$

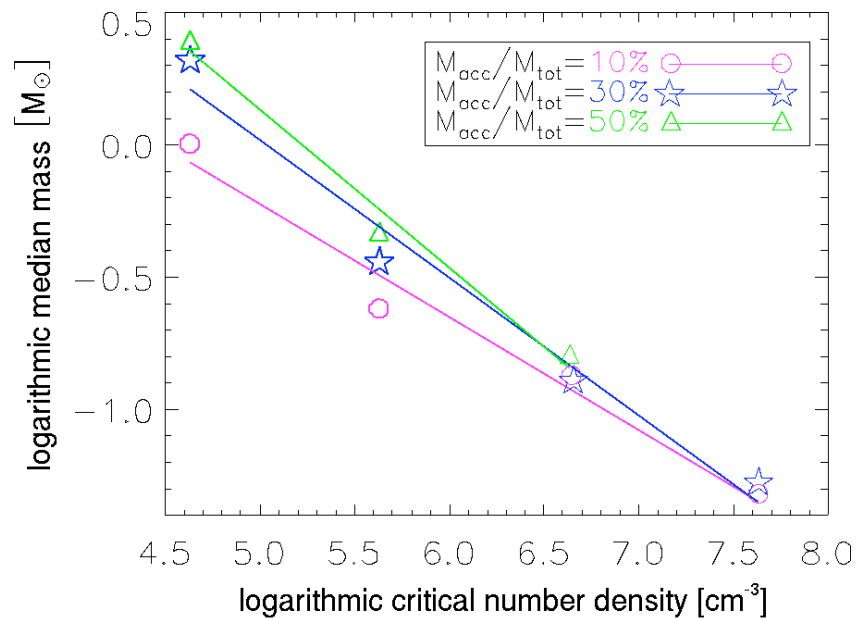
$$T \sim \rho^{\gamma-1}$$



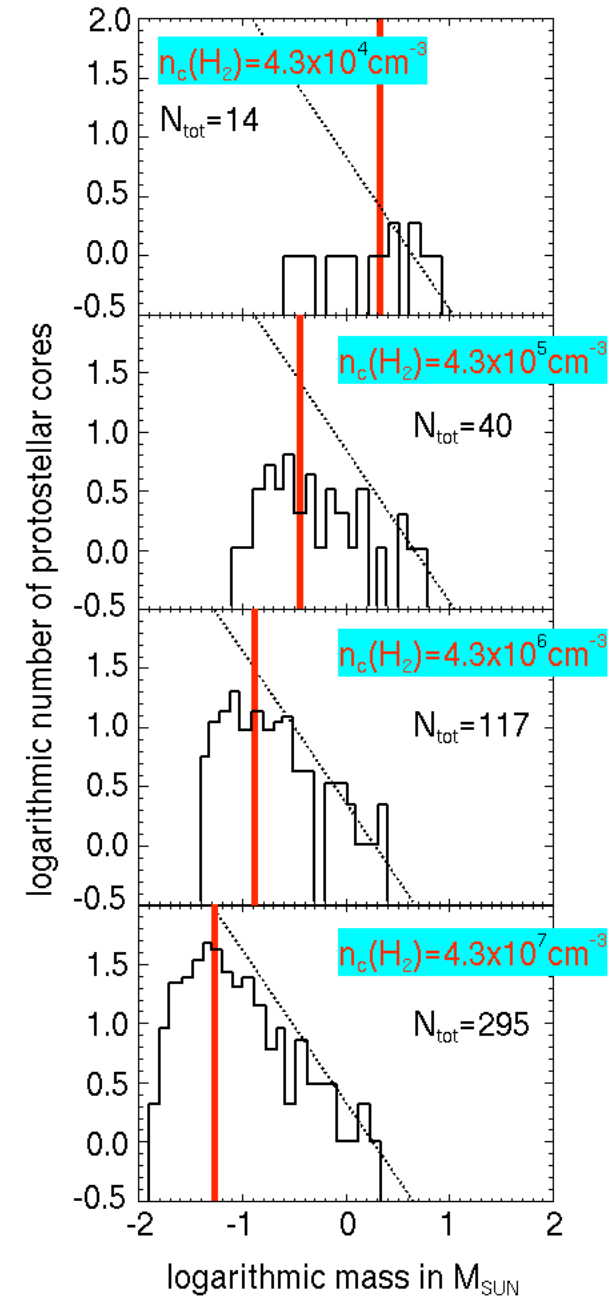
(Jappsen et al. 2005)

IMF from simple piece-wise polytropic EOS

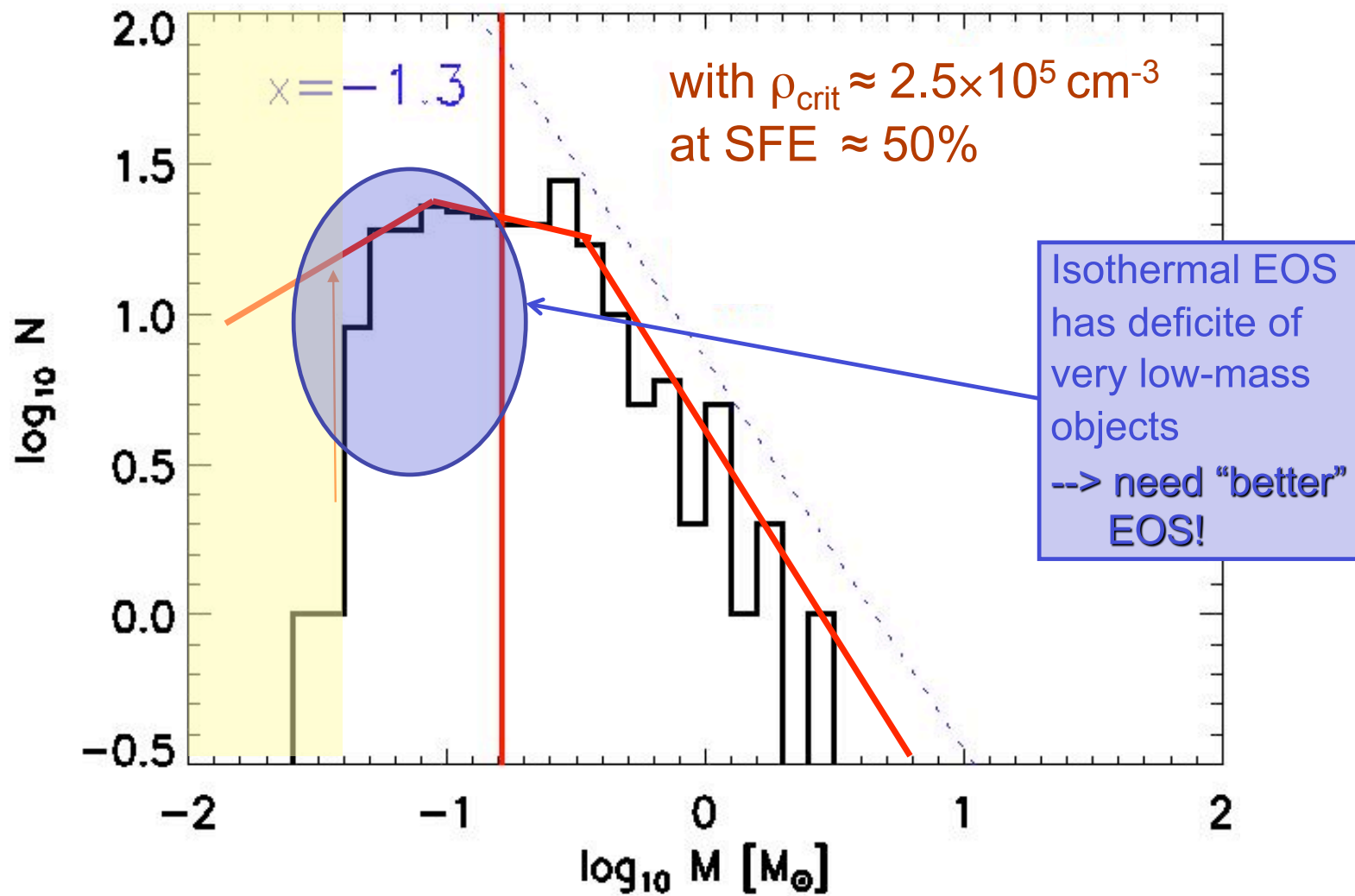
critical density \uparrow \Rightarrow median mass \downarrow



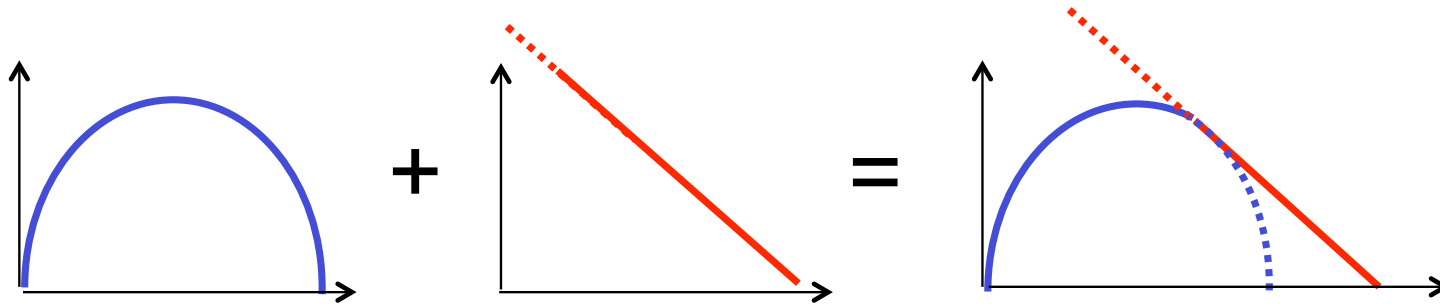
(Jappsen et al. 2005)



IMF in nearby molecular clouds



Plausibility argument for shape



- Supersonic turbulence is scale free process

→ *POWER LAW BEHAVIOR*

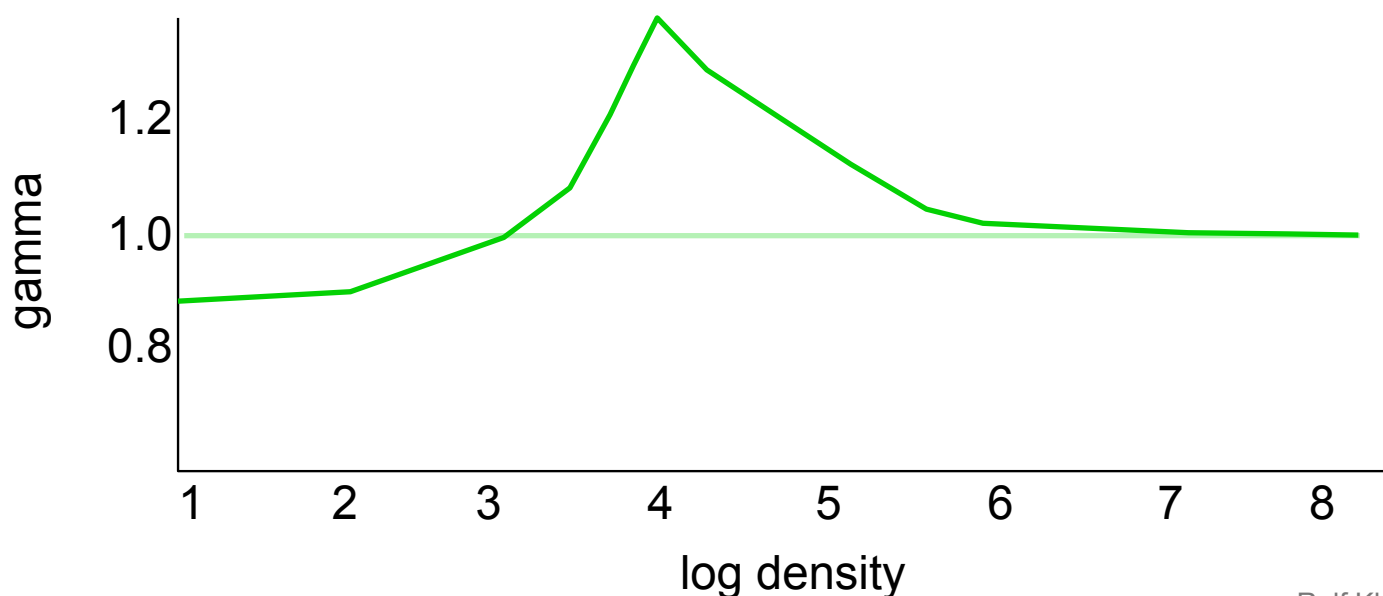
- *But also:* turbulence and fragmentation are highly stochastic processes → central limit theorem

→ *GAUSSIAN DISTRIBUTION*

IMF in starburst galaxies

- Nuclear regions of starburst galaxies are extreme:
 - hot dust, large densities, strong radiation, etc.
- Thermodynamic properties of star-forming gas differ from Milky Way --> Different EOS!

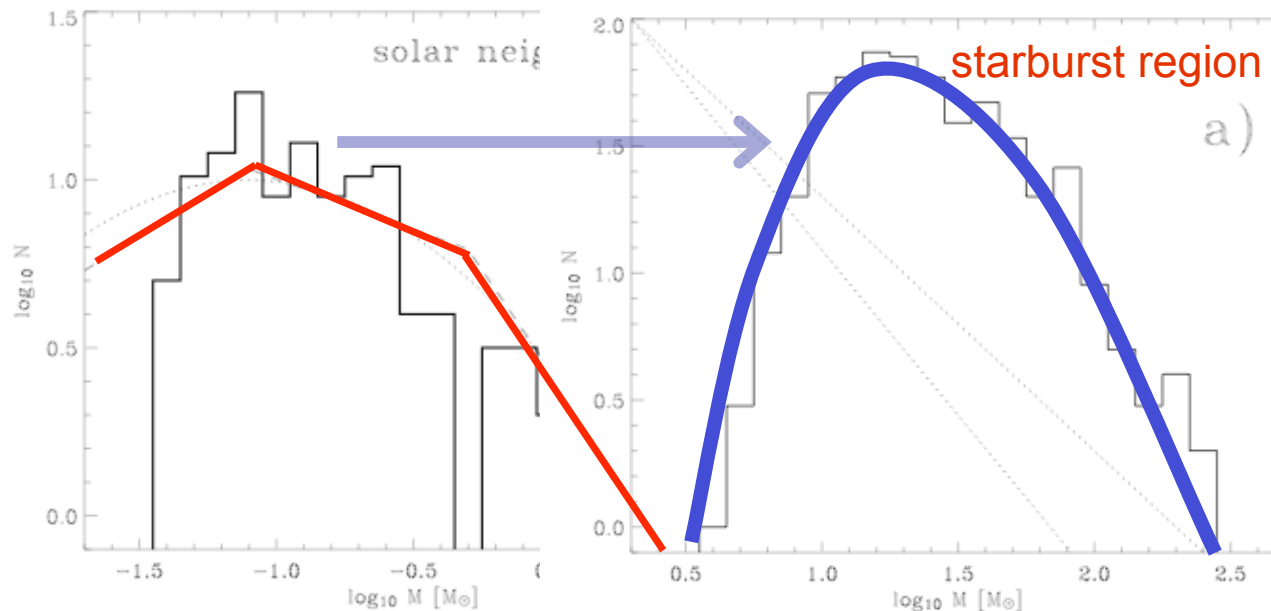
(see Spaans & Silk 2005)



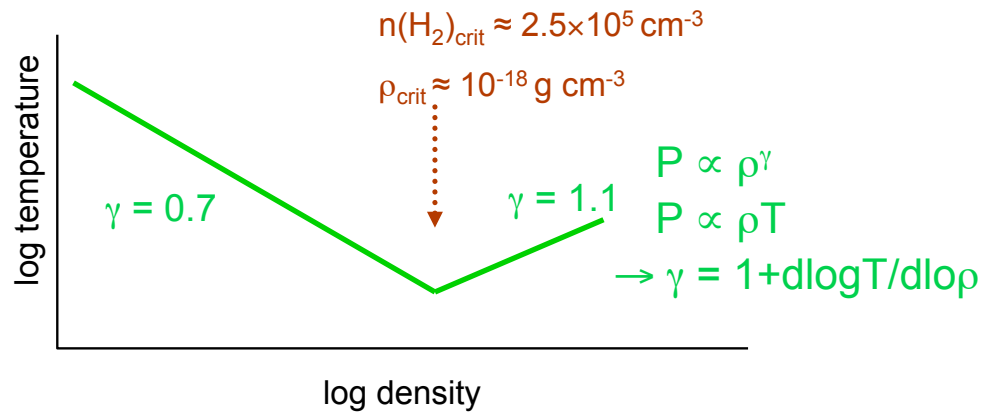
IMF in starburst galaxies

- Starburst EOS --> top-heavy IMF

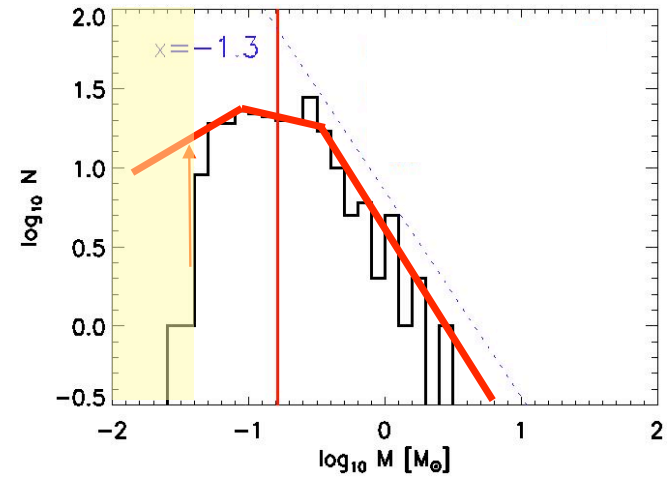
(Klessen, Spaans, Jappsen, 2007)



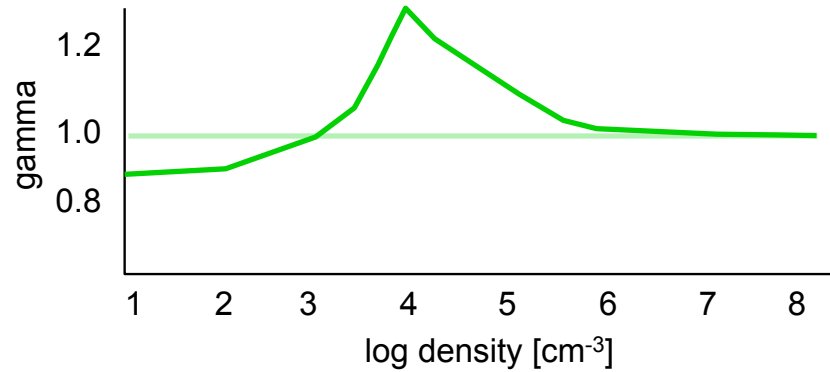
fragmentation depends on EOS



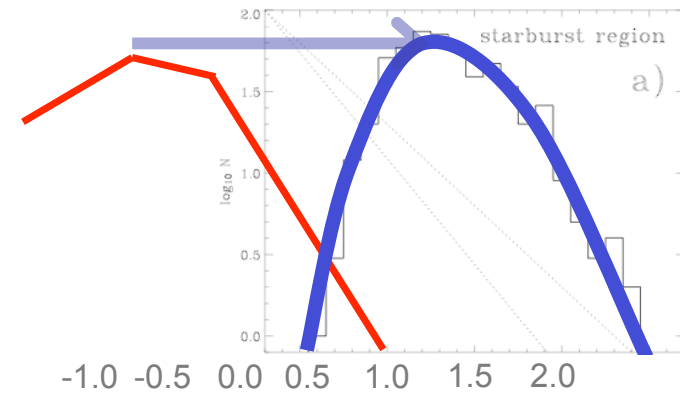
(Larson 2005)



(Jappsen et al. 2005)

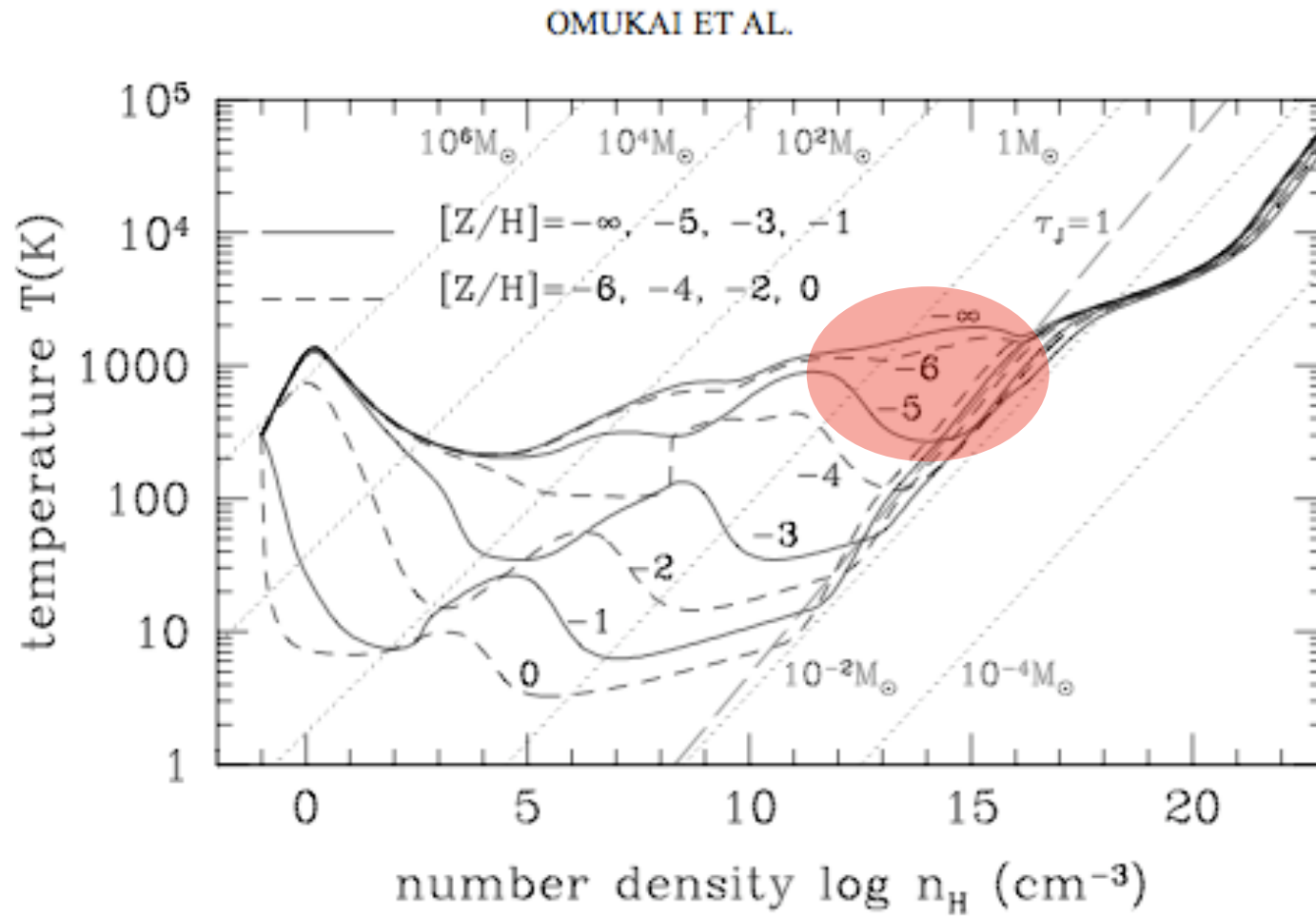


(Spaans & Silk 2005)



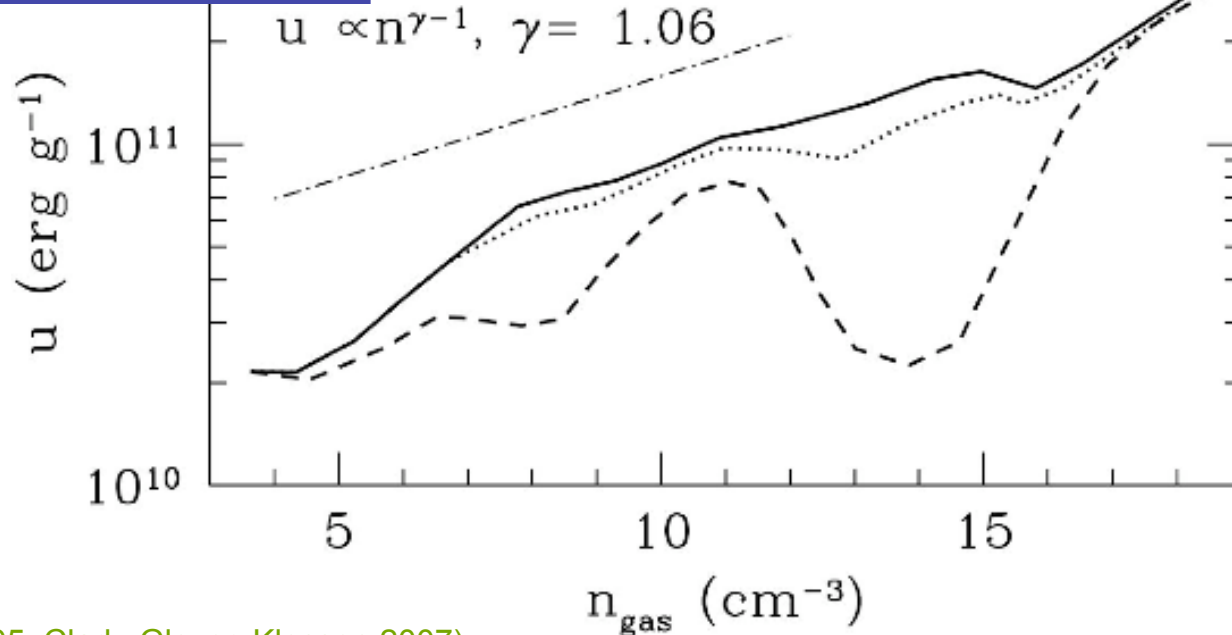
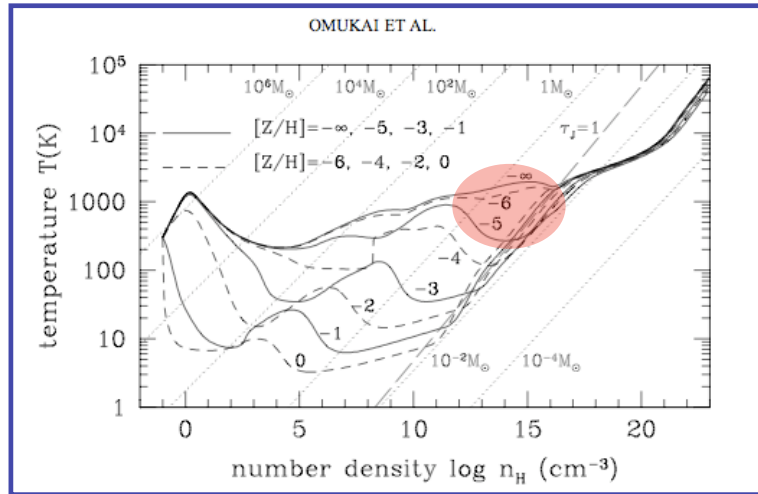
(Klessen et al. 2007)

transition: Pop III to Pop II.5



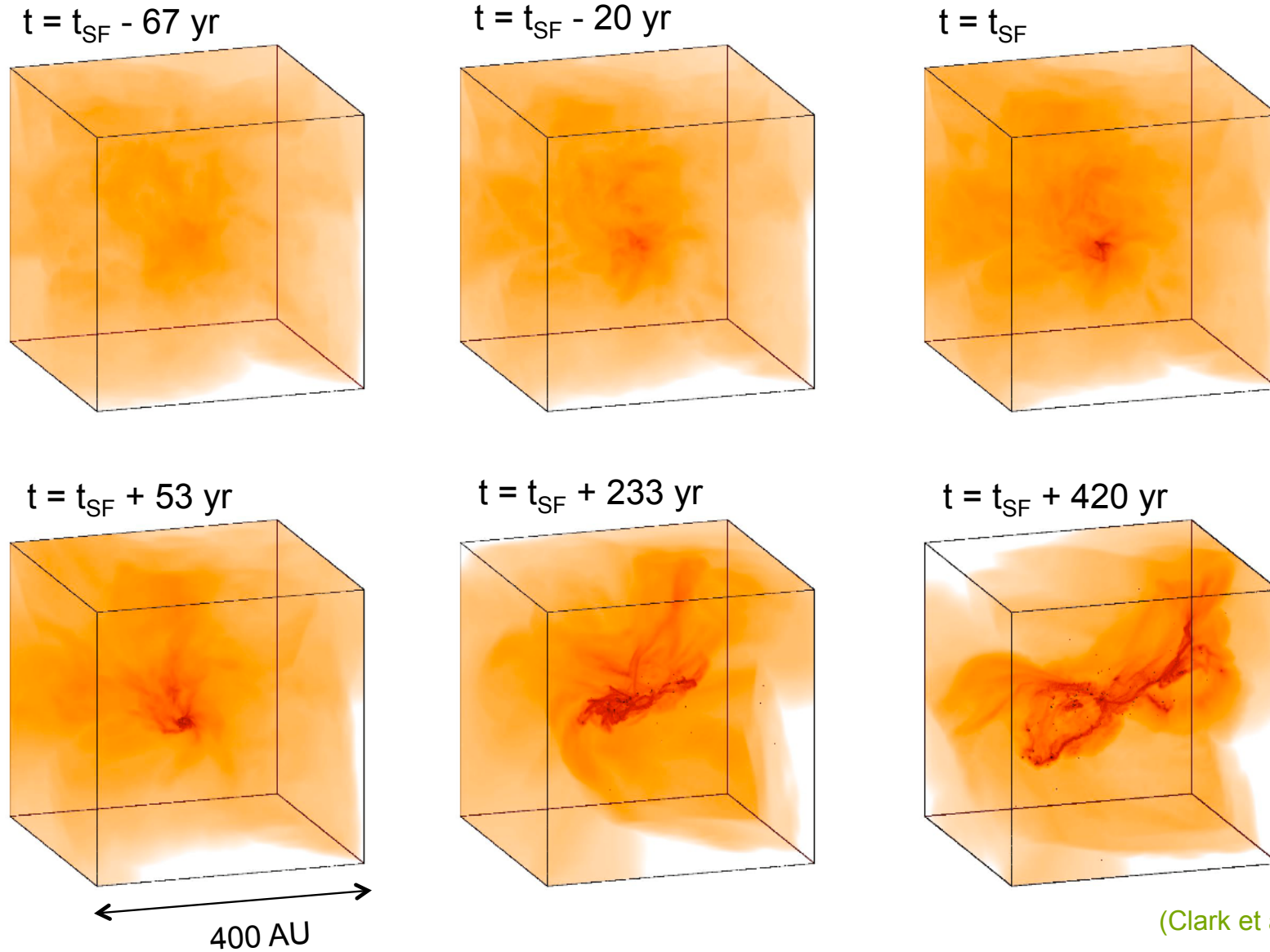
(Omukai et al. 2005)

transition: Pop III to Pop II.5



(Omukai et al. 2005, Clark, Glover, Klessen 2007)

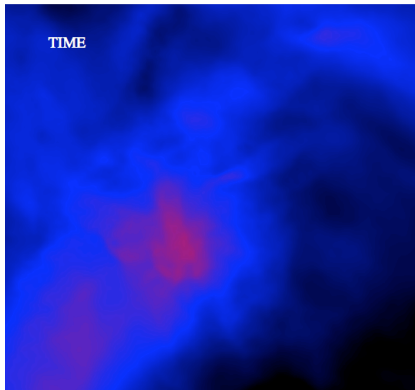
dust induced fragmentation at $Z=10^{-5}$



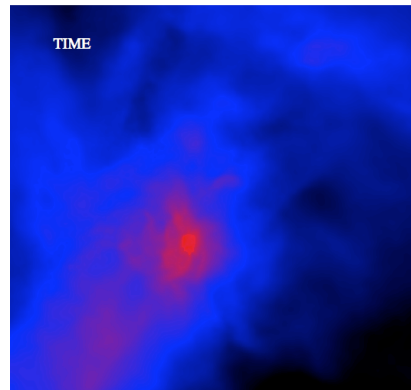
(Clark et al. 2007)

dust induced fragmentation at $Z=10^{-5}$

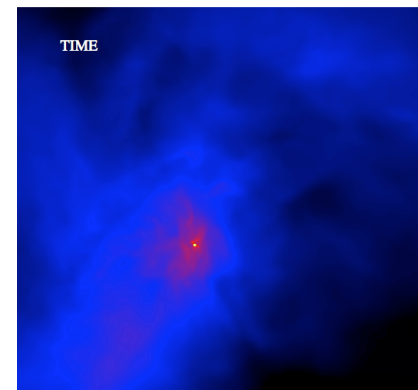
$t = t_{\text{SF}} - 67 \text{ yr}$



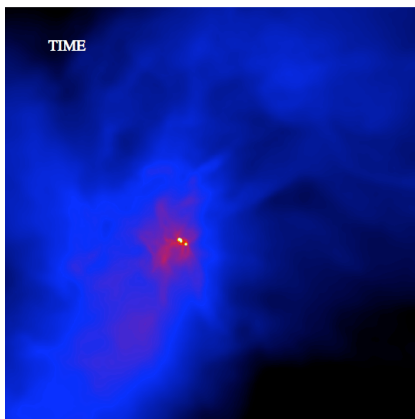
$t = t_{\text{SF}} - 20 \text{ yr}$



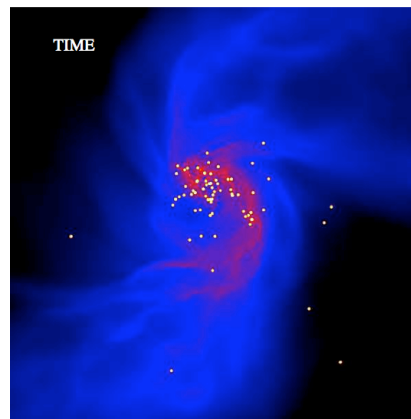
$t = t_{\text{SF}}$



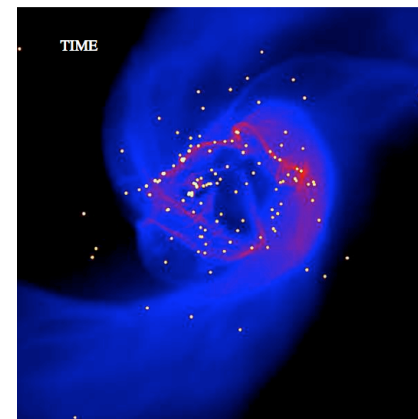
$t = t_{\text{SF}} + 53 \text{ yr}$



$t = t_{\text{SF}} + 233 \text{ yr}$

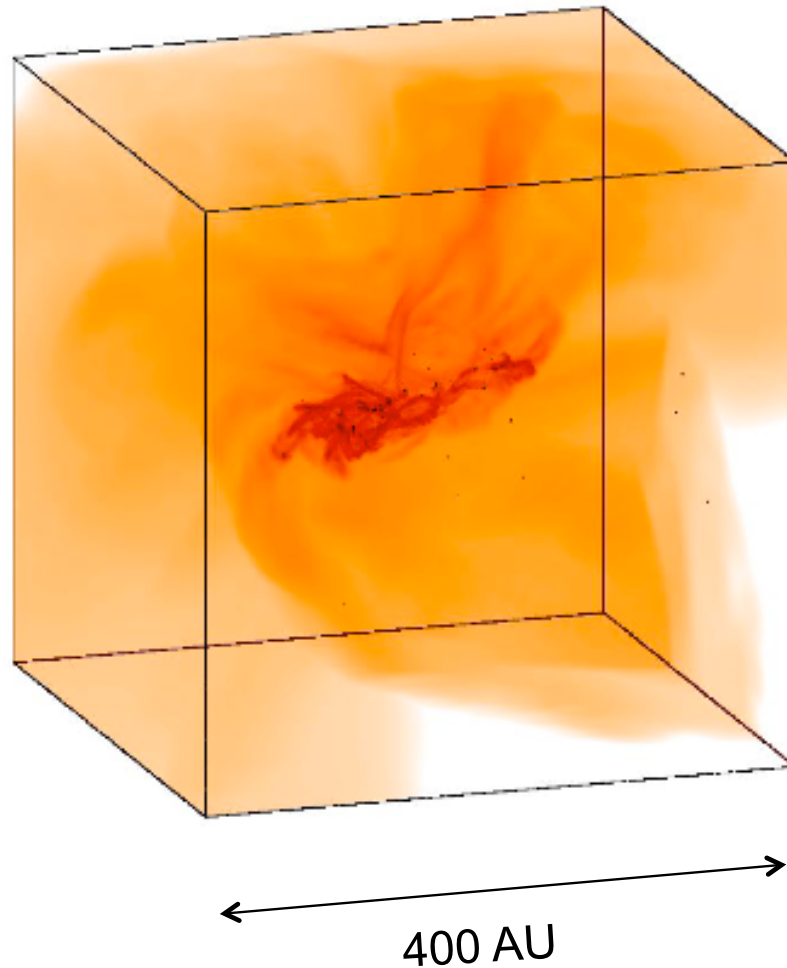


$t = t_{\text{SF}} + 420 \text{ yr}$



(Clark et al. 2007)

dust induced fragmentation at $Z=10^{-5}$



dense cluster of low-mass protostars builds up:

- mass spectrum peaks below $1 M_{\text{sun}}$
- cluster VERY dense
 $n_{\text{stars}} = 2.5 \times 10^9 \text{ pc}^{-3}$
- fragmentation at density
 $n_{\text{gas}} = 10^{12} - 10^{13} \text{ cm}^{-3}$

(Clark et al. 2007)

cluster build-up

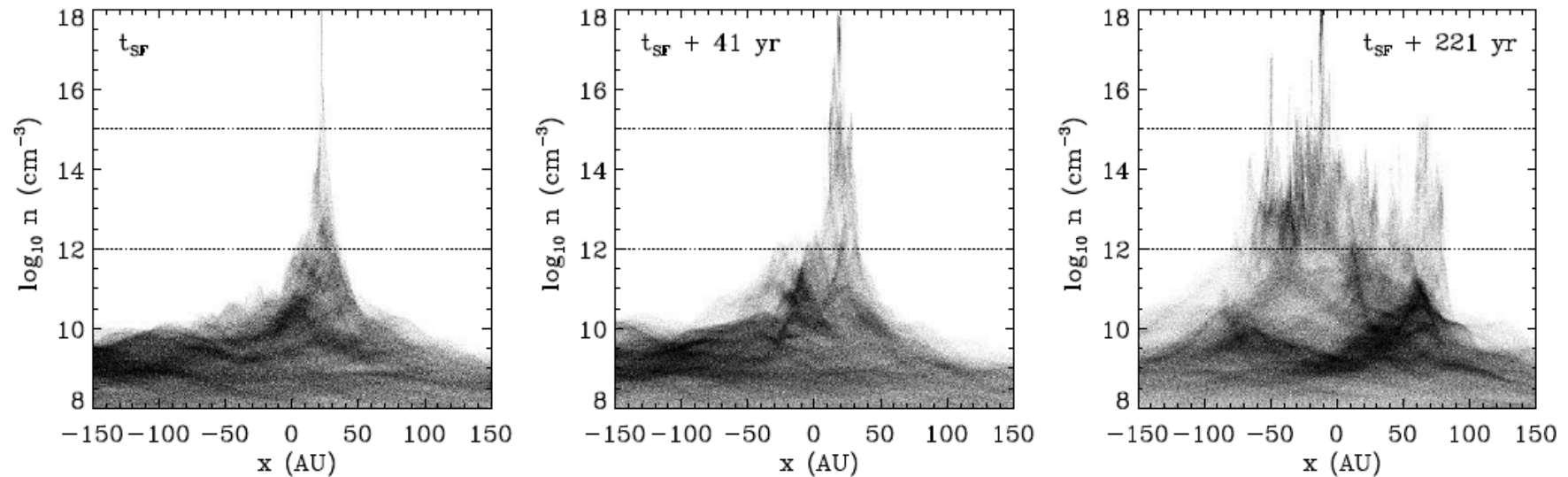
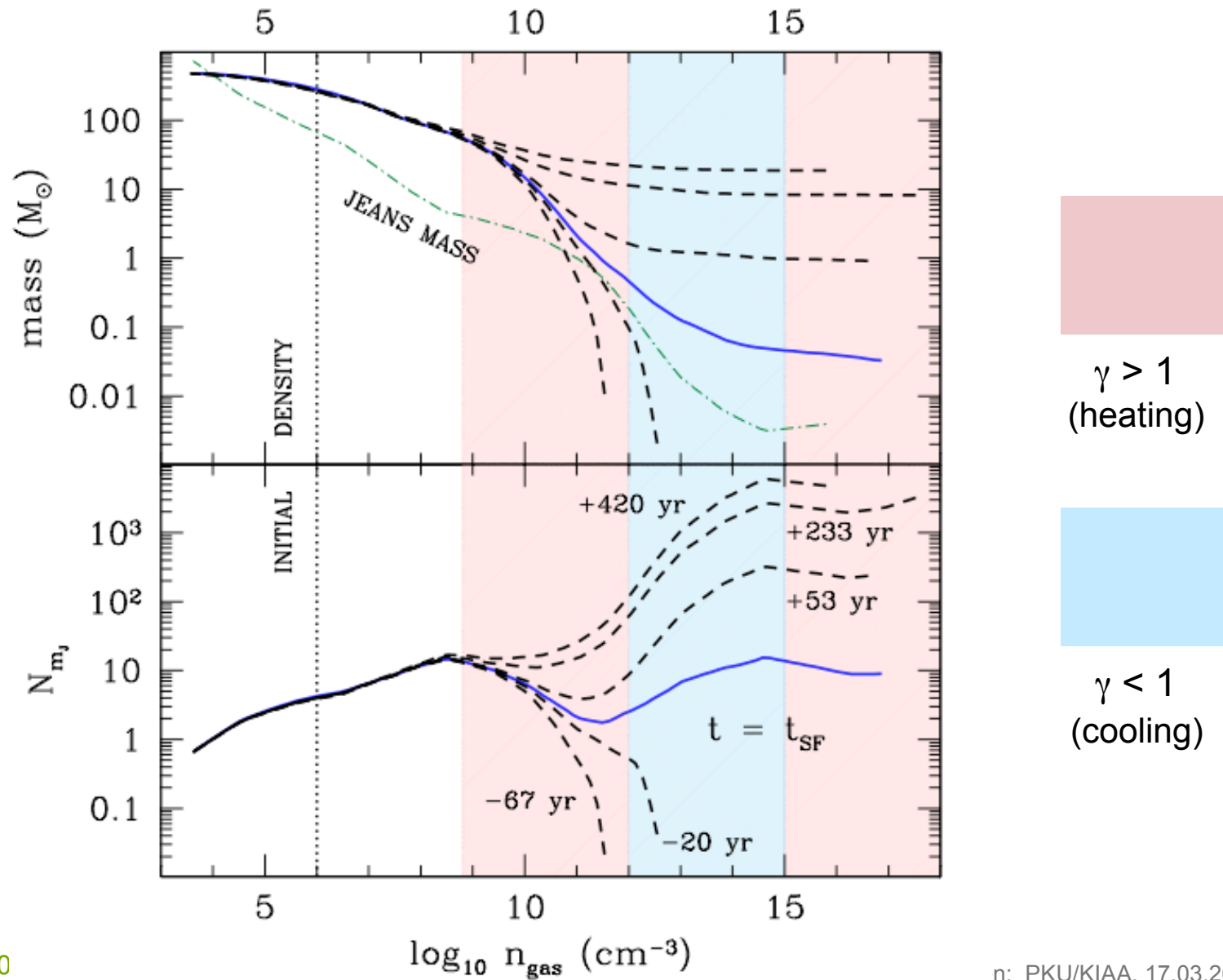
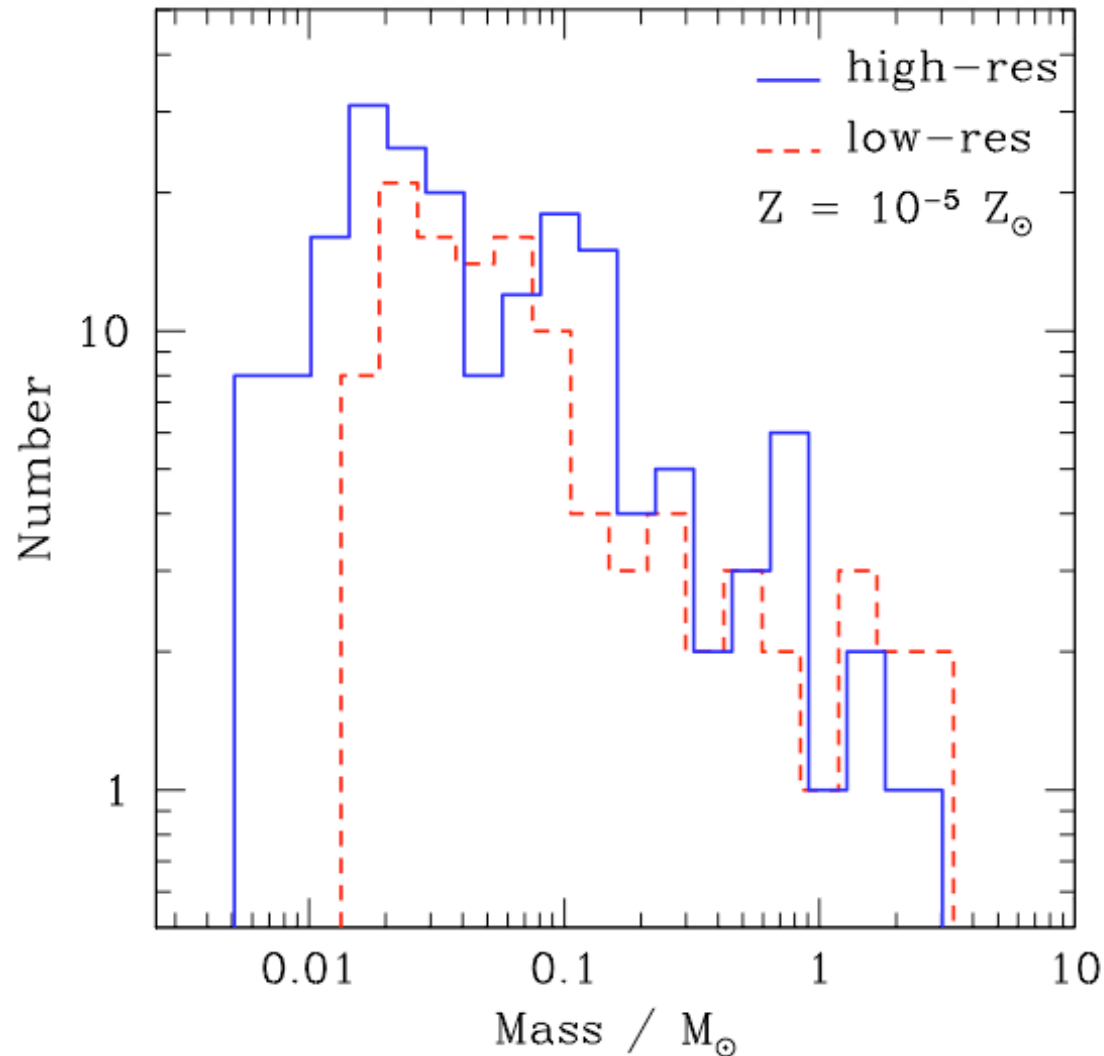


FIG. 3.— We illustrate the onset of the fragmentation process in the high resolution $Z = 10^{-5} Z_{\odot}$ simulation. The graphs show the densities of the particles, plotted as a function of their x -position. Note that for each plot, the particle data has been centered on the region of interest. We show here results at three different output times, ranging from the time that the first star forms (t_{SF}) to 221 years afterwards. The densities lying between the two horizontal dashed lines denote the range over which dust cooling lowers the gas temperature.

cluster build-up



dust induced fragmentation at $Z=10^{-5}$



dense cluster of low-mass protostars builds up:

- mass spectrum peaks below $1 M_{\text{sun}}$
- cluster VERY dense
 $n_{\text{stars}} = 2.5 \times 10^9 \text{ pc}^{-3}$
- fragmentation at density
 $n_{\text{gas}} = 10^{12} - 10^{13} \text{ cm}^{-3}$

(Clark et al. 2007)

comparison for different Z

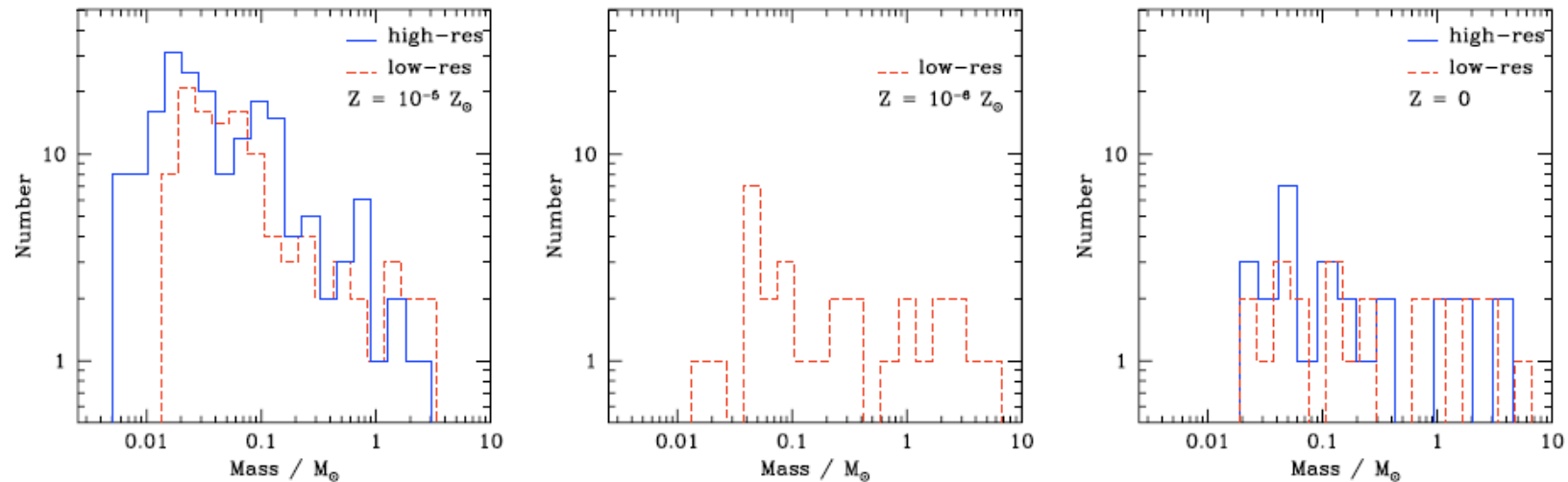


FIG. 4.— Mass functions resulting from simulations with metallicities $Z = 10^{-5} Z_{\odot}$ (left-hand panel), $Z = 10^{-6} Z_{\odot}$ (center panel), and $Z = 0$ (right-hand panel). The plots refer to the point in each simulation at which $19 M_{\odot}$ of material has been accreted (which occurs at a slightly different time in each simulation). The mass resolutions are $0.002 M_{\odot}$ and $0.025 M_{\odot}$ for the high and low resolution simulations, respectively. Note the similarity between the results of the low-resolution and high-resolution simulations. The onset of dust-cooling in the $Z = 10^{-5} Z_{\odot}$ cloud results in a stellar cluster which has a mass function similar to that for present day stars, in that the majority of the mass resides in the lower-mass objects. This contrasts with the $Z = 10^{-6} Z_{\odot}$ and primordial clouds, in which the bulk of the cluster mass is in high-mass stars.

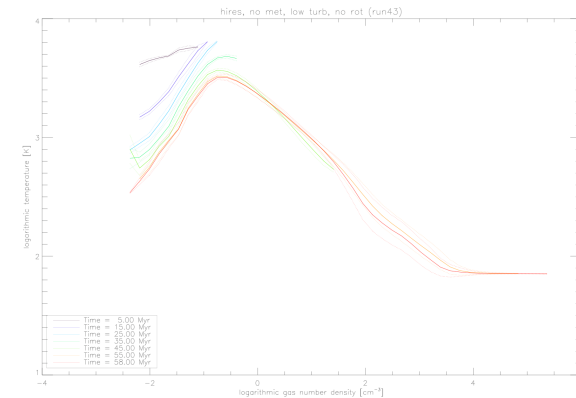
even zero-metallicity case fragments
(although much more weakly)

(Clark et al. 2007)

Simple EOS vs. radiation transfer

● how good is EOS approach?

- time to reach chemical and thermal equilibrium shorter than dynamical time?
- how does EOS depend on dynamics? (e.g. 1D collapse with large-gradient approx. versus complex 3D turbulent flows)



● how important is heating from stars?

- accretion luminosity may heat gas and reduce degree of cloud fragmentation (cluster formation vs. high-mass SF)

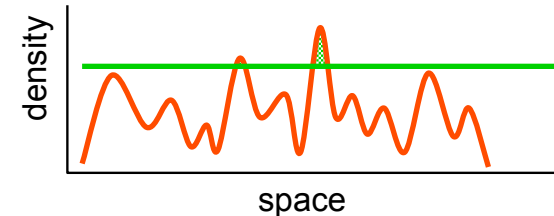
● how can we model that best?

- full radiation transfer vs. approximate schemes

Summary

Summary I

- interstellar gas is highly *inhomogeneous*
 - *thermal instability*
 - *gravitational instability*
 - *turbulent compression* (in shocks $\delta\rho/\rho \propto M^2$; in atomic gas: $M \approx 1...3$)
- cold *molecular clouds* can form rapidly in high-density regions at *stagnation points of convergent large-scale flows*
 - chemical *phase transition*: atomic \rightarrow molecular
 - process is *modulated* by large-scale *dynamics* in the galaxy
- inside *cold clouds*: turbulence is highly supersonic ($M \approx 1...20$)
 \rightarrow *turbulence* creates density contrast, *gravity* selects for collapse
 \longrightarrow **GRAVOTUBULENT FRAGMENTATION**
- *turbulent cascade*: local compression *within* a cloud provokes collapse \rightarrow formation of individual *stars* and *star clusters*
- *star cluster*: gravity dominates in large region (\rightarrow competitive accretion)



Summary II

- *thermodynamic response* (EOS) determines fragmentation behavior

- characteristic stellar mass from fundamental atomic and molecular parameters
--> explanation for quasi-universal IMF?



- *stellar feedback* is important

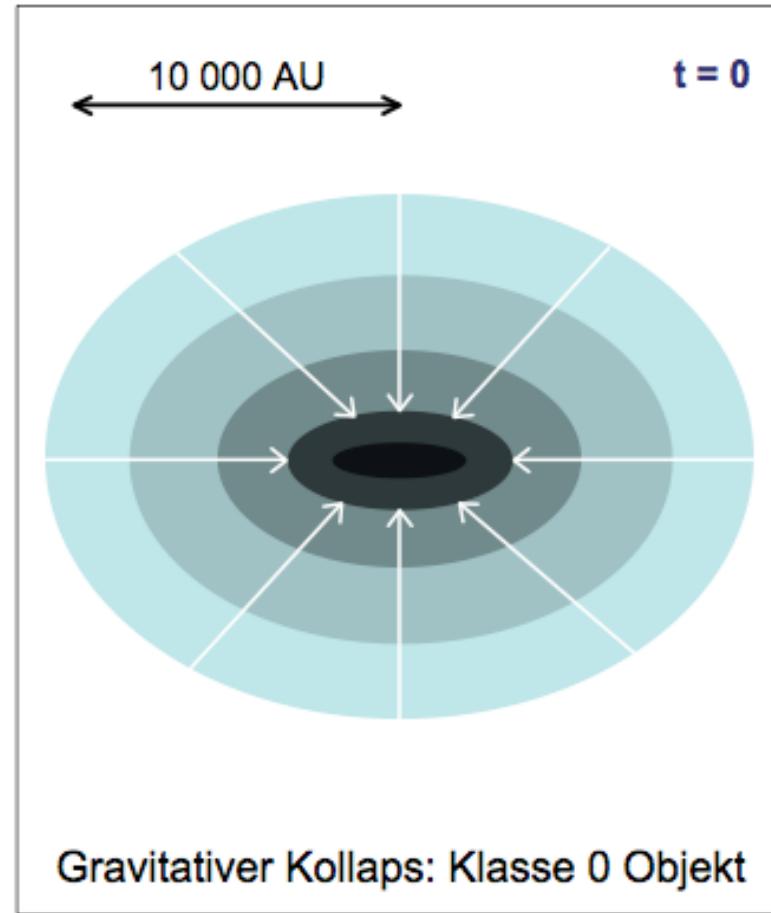
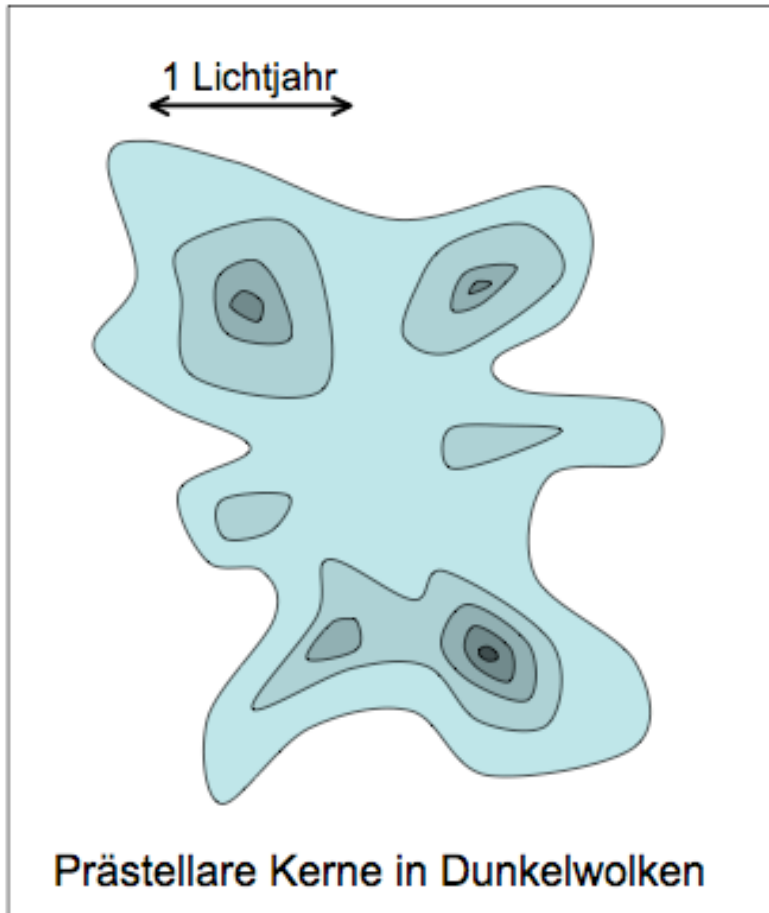
- accretion heating may reduce degree of fragmentation
- ionizing radiation will set efficiency of star formation

- *CAVEATS:*

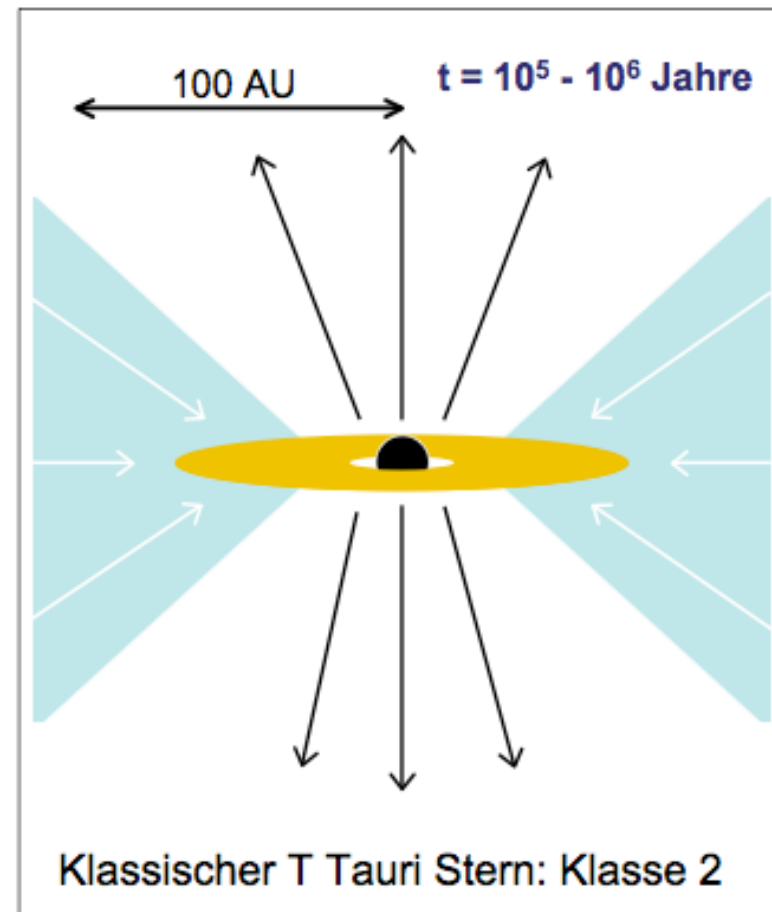
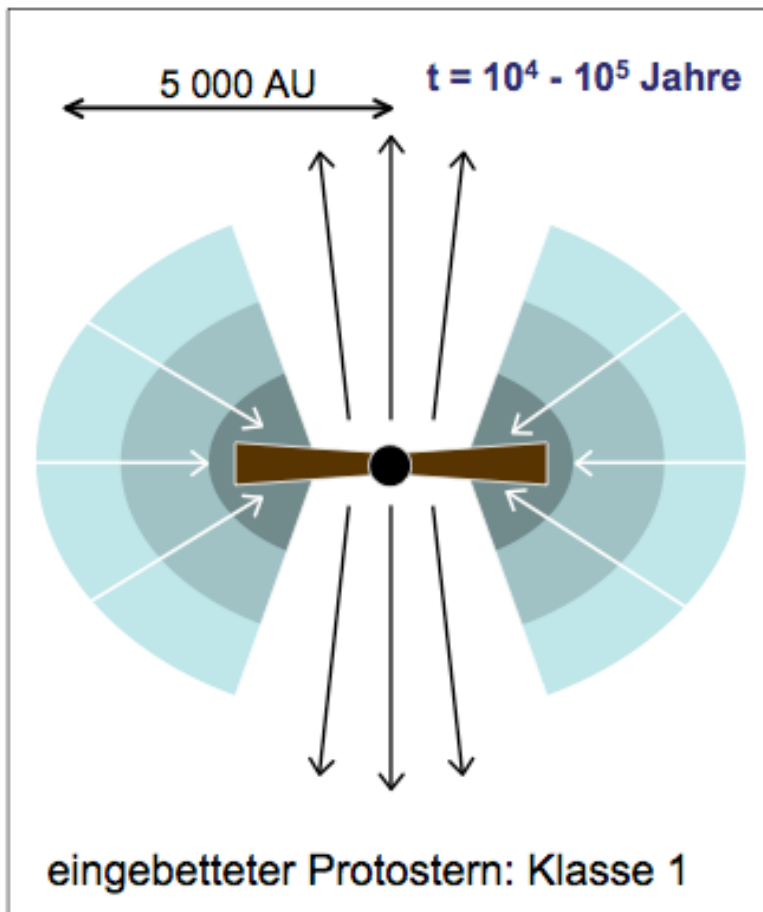
- star formation is *multi-scale, multi-physics* problem --> VERY difficult to model
- in simulations: very small turbulent inertial range ($Re < 1000$)
- can we use EOS to describe thermodynamics of gas, or do we need time-dependent chemical network and radiative transport?
- stellar feedback requires (at least approximative) radiative transport, most numerical calculations so far have neglected that aspect

Thanks!

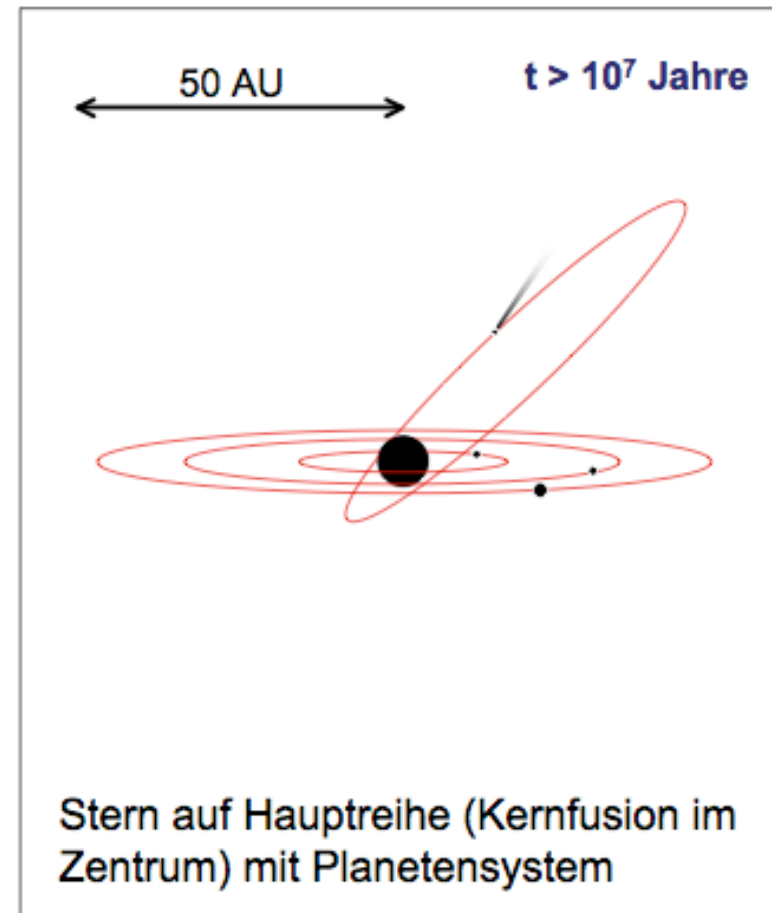
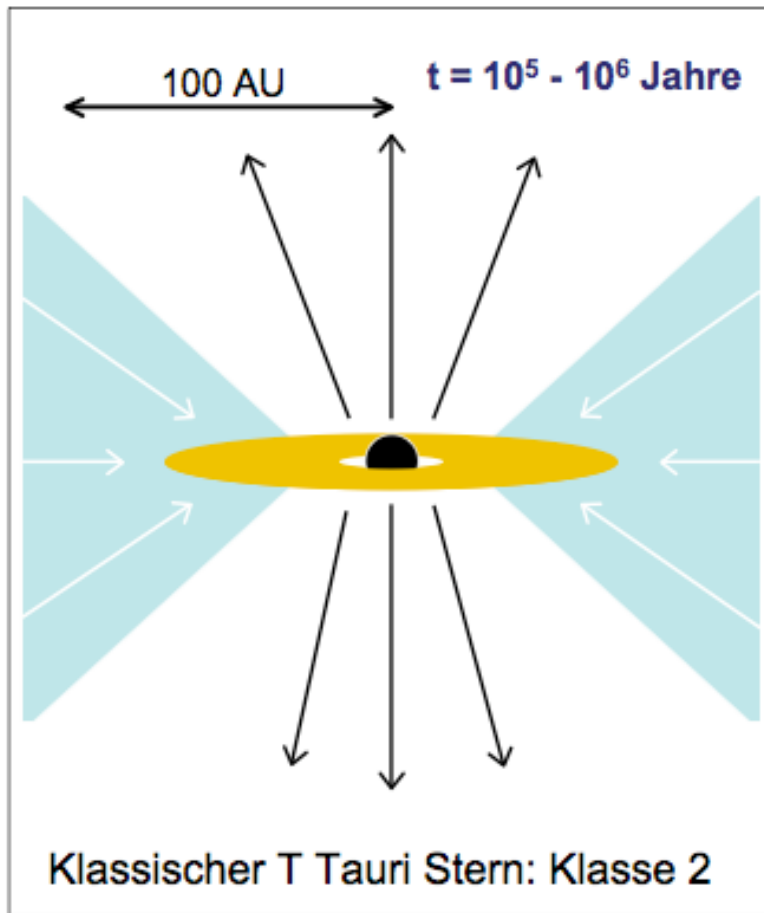
Stadien der Sternbildung 1



Stadien der Sternbildung 2



Stadien der Sternbildung 3



hires, no met, low turb, no rot (run43)

