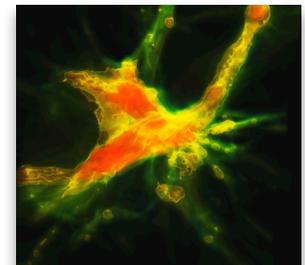
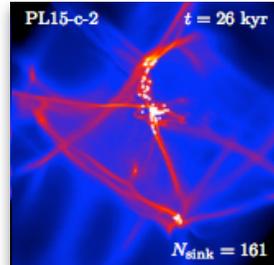
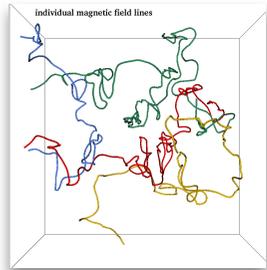


Star Formation



Ralf Klessen



Zentrum für Astronomie der Universität Heidelberg
Institut für Theoretische Astrophysik



thanks to ...



... people in the group in Heidelberg:

Christian Baczynski, Clio Bertelli Mottag, Erik Bertram, Frank Bigiel, Paul Clark, Volker Gaibler, Simon Glover, Dimitrios Gouliermis, Tilman Hartwig, Lukas Konstandin, Camilo Penaloza, Mei Sasaki, Jennifer Schober, Rahul Shetty, Rowan Smith, László Szűcs

... former group members:

Robi Banerjee, Ingo Berentzen, Christoph Federrath, Philipp Girichidis, Thomas Greif, Milica Micic, Thomas Peters, Dominik Schleicher, Stefan Schmeja, Sharanya Sur, ...

... many collaborators abroad!



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STIFTUNG
Wir stiften Zukunft



European
Research
Council

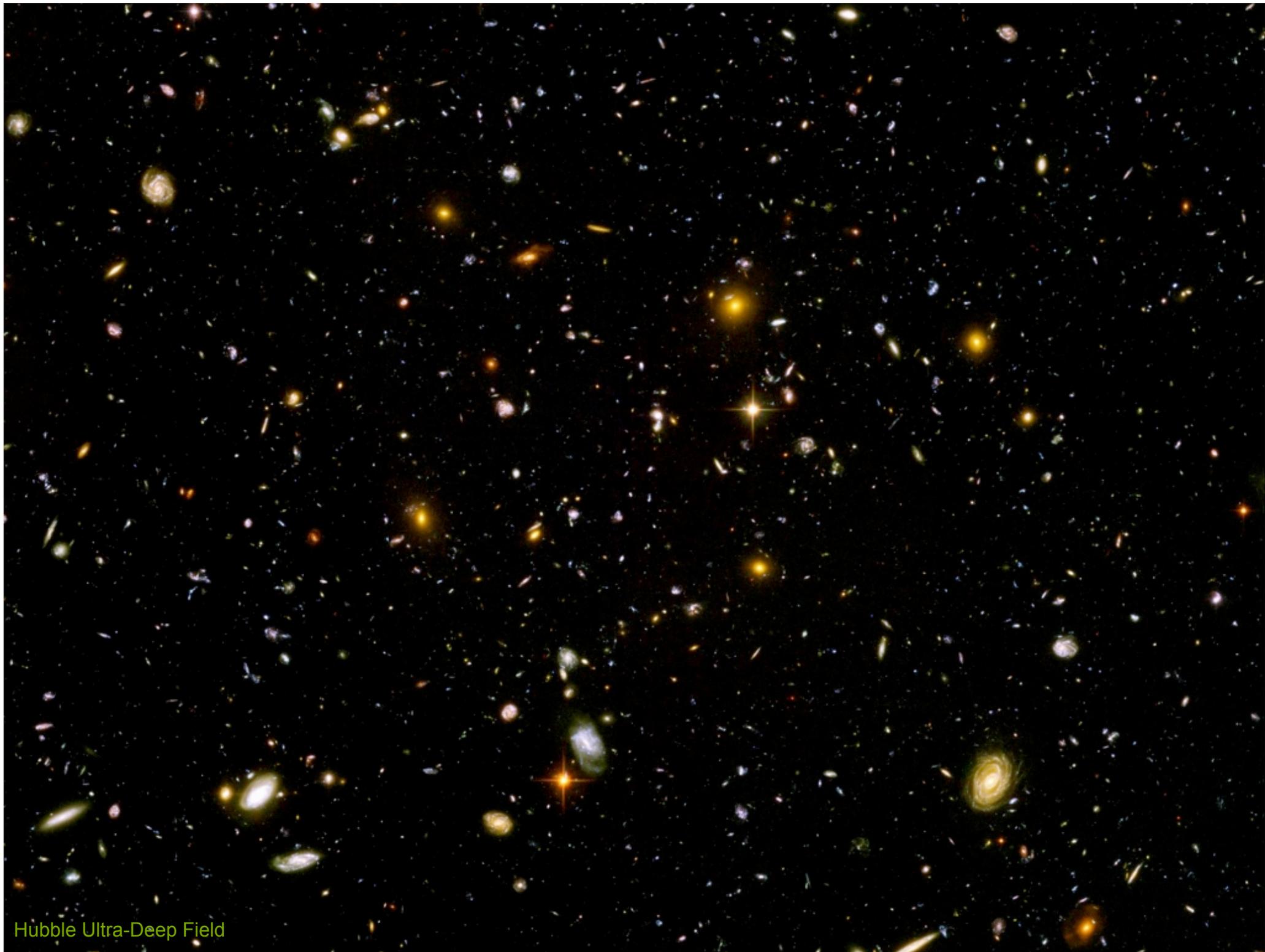
agenda

- star formation theory
 - phenomenology
 - challenges
 - our current understanding and its limitations
- applications
 - the interstellar medium
 - the stellar mass function at birth (IMF)

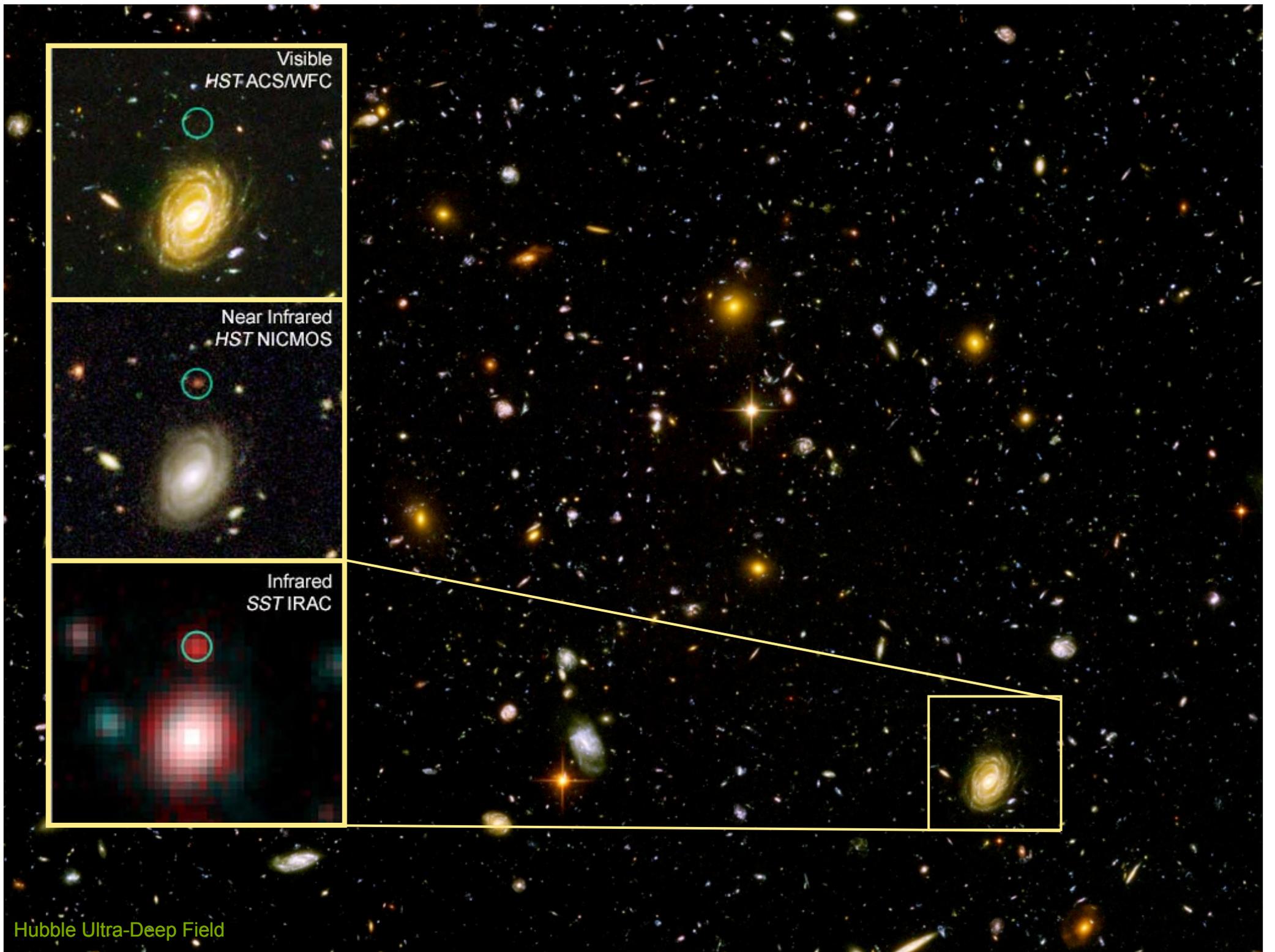


NGC 3324 (Hubble, NASA/ESA)

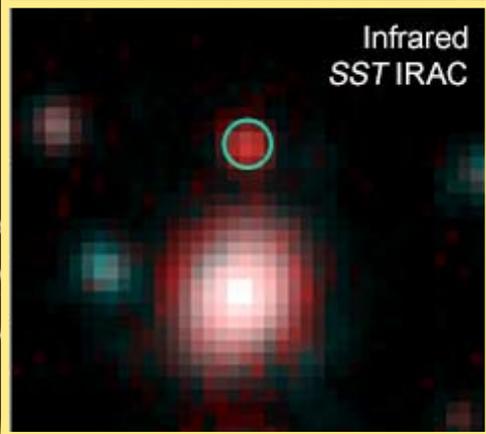
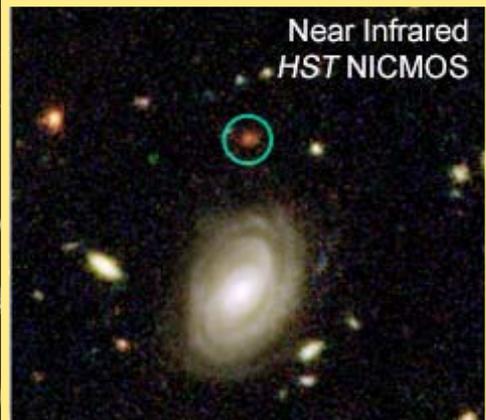
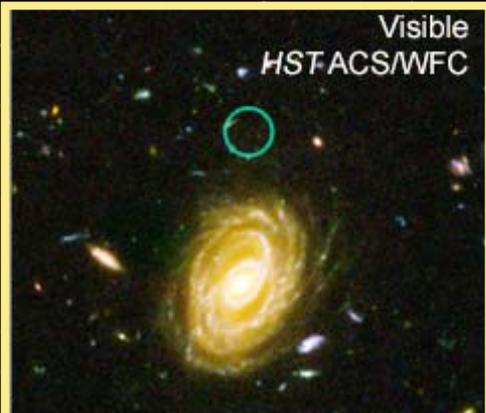
Phenomenology



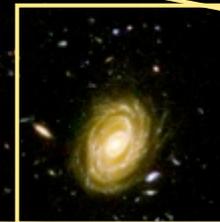
Hubble Ultra-Deep Field

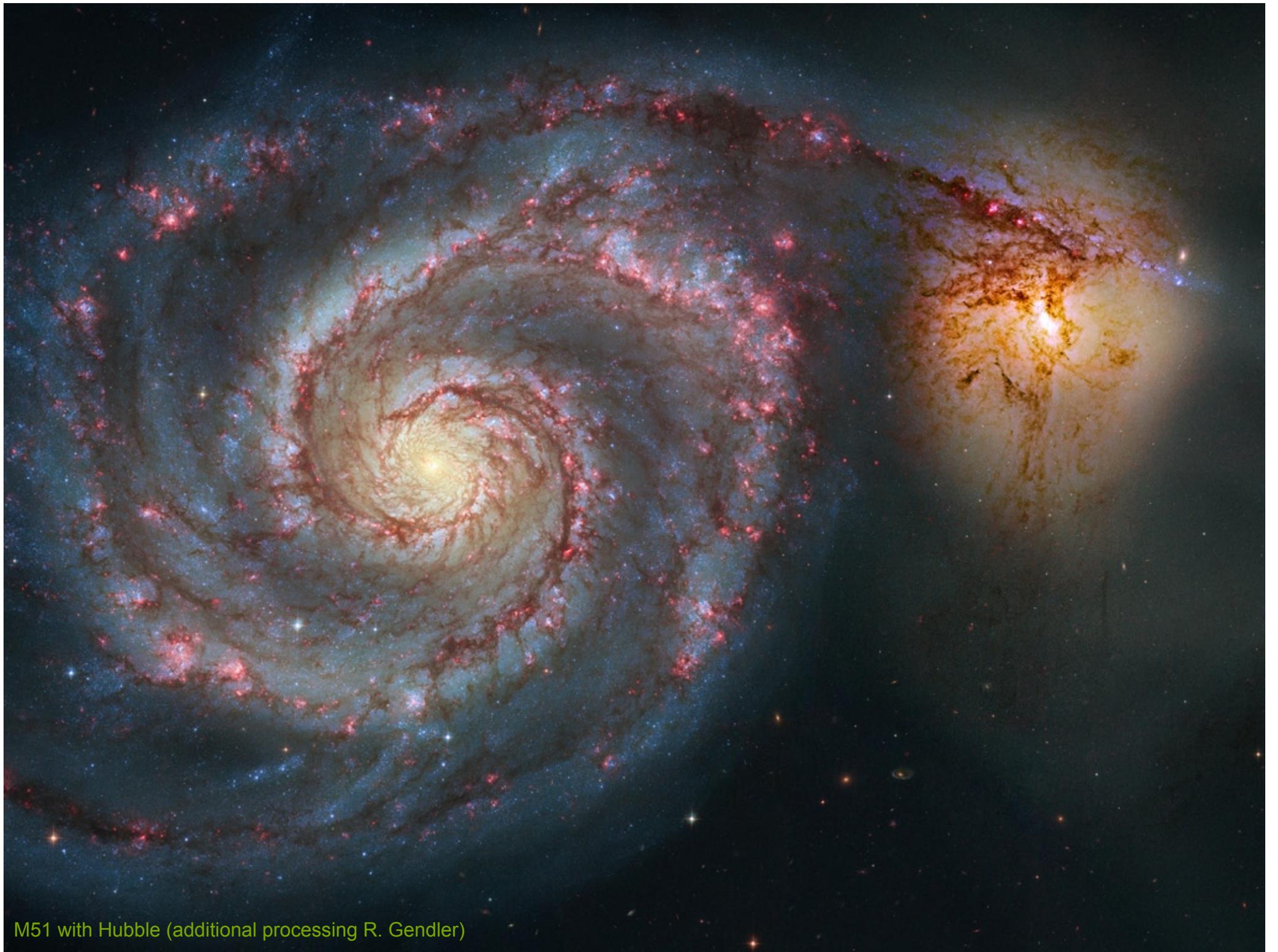


Hubble Ultra-Deep Field

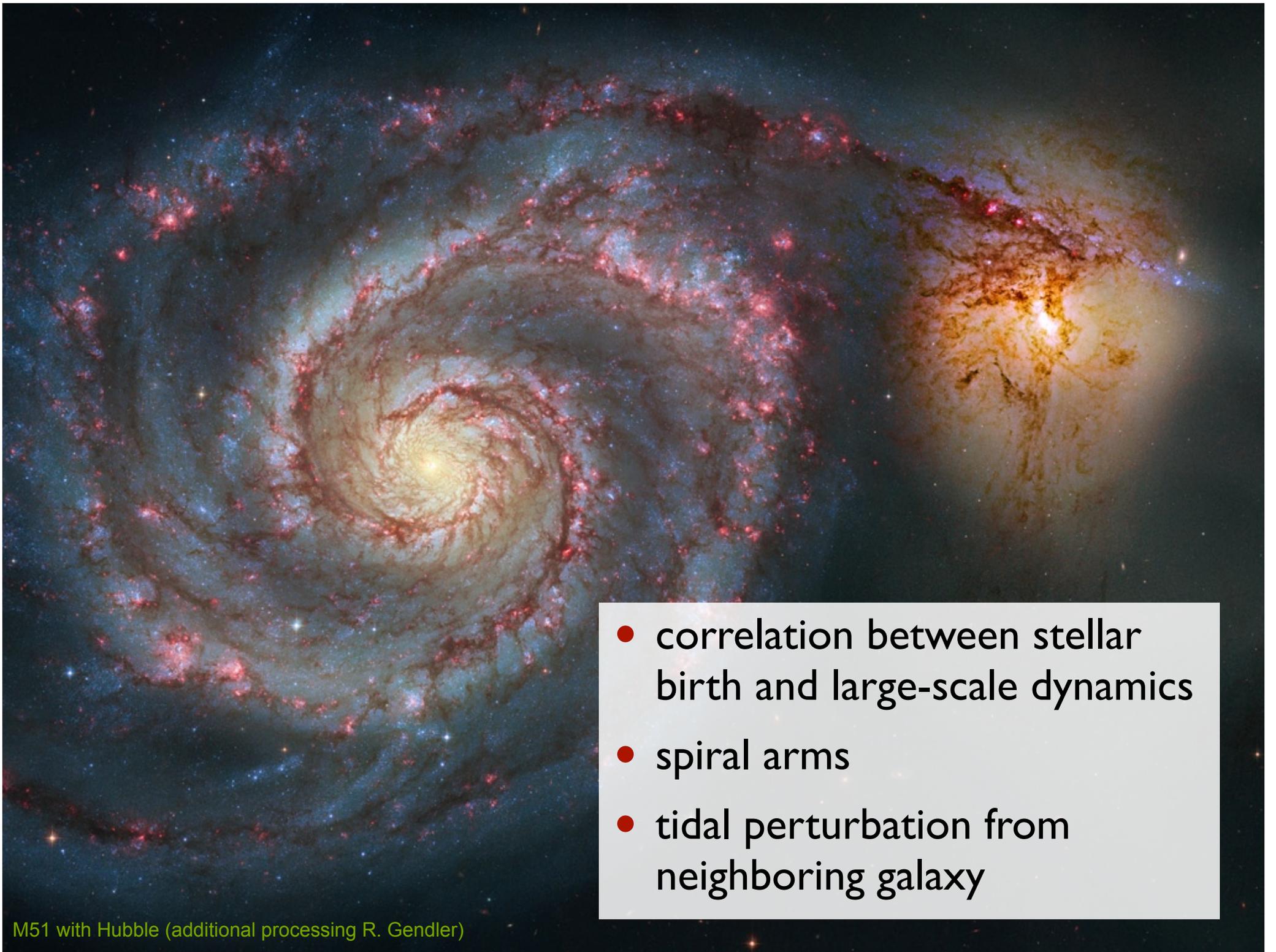


- star formation sets in very early after the big bang
- stars always form in galaxies and protogalaxies
- we cannot see the first generation of stars, but maybe the second one





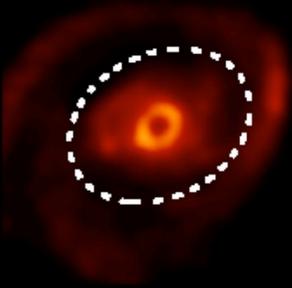
M51 with Hubble (additional processing R. Gendler)



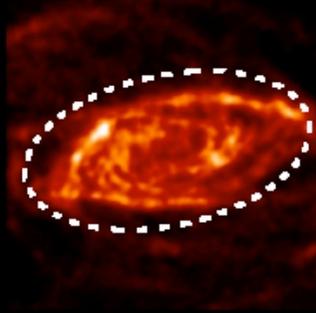
- correlation between stellar birth and large-scale dynamics
- spiral arms
- tidal perturbation from neighboring galaxy

M51 with Hubble (additional processing R. Gendler)

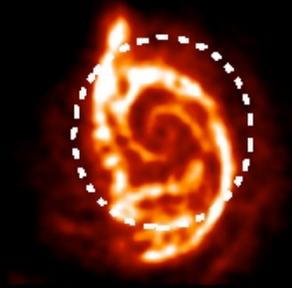
NGC 4736



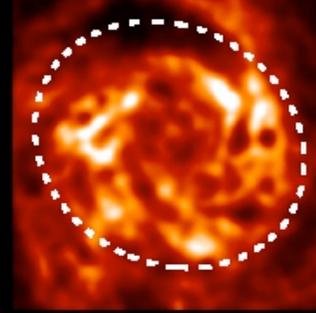
NGC 5055



NGC 5194



NGC 6946

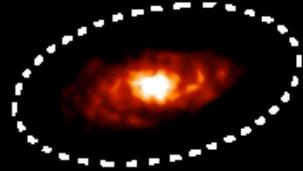


atomic
hydrogen

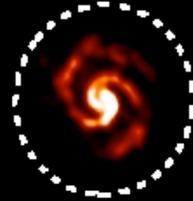
NGC 4736



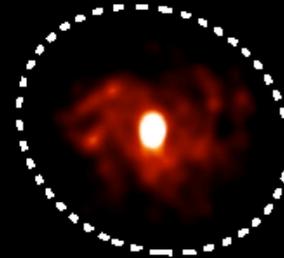
NGC 5055



NGC 5194



NGC 6946

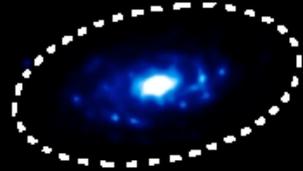


molecular
hydrogen

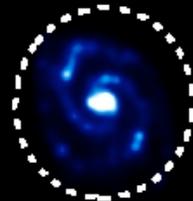
NGC 4736



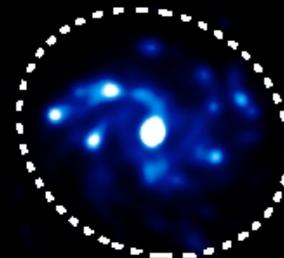
NGC 5055



NGC 5194

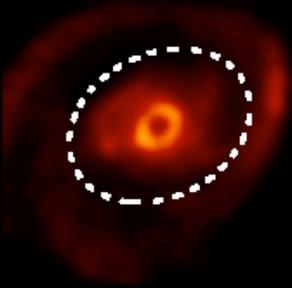


NGC 6946

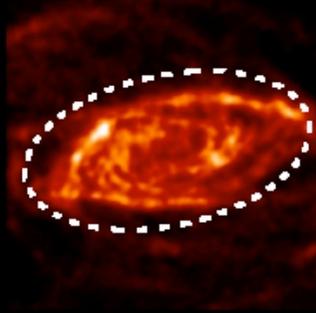


star
formation

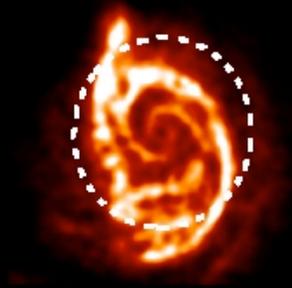
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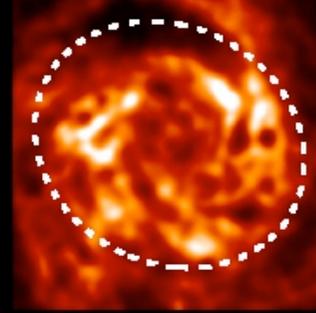
NGC 5055



NGC 5194



NGC 6946

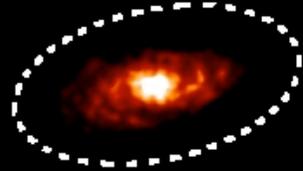


atomic
hydrogen

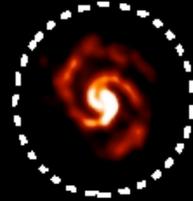
NGC 4736



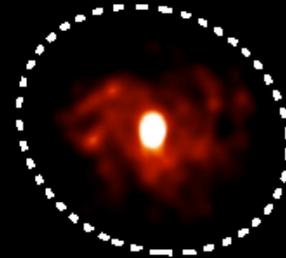
NGC 5055



NGC 5194



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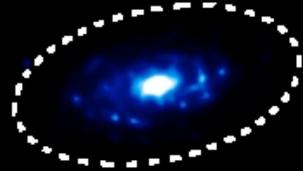


molecular
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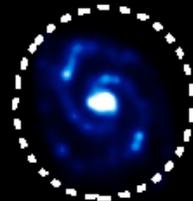
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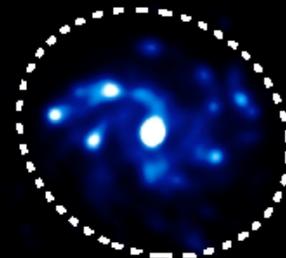
NGC 5055



NGC 5194

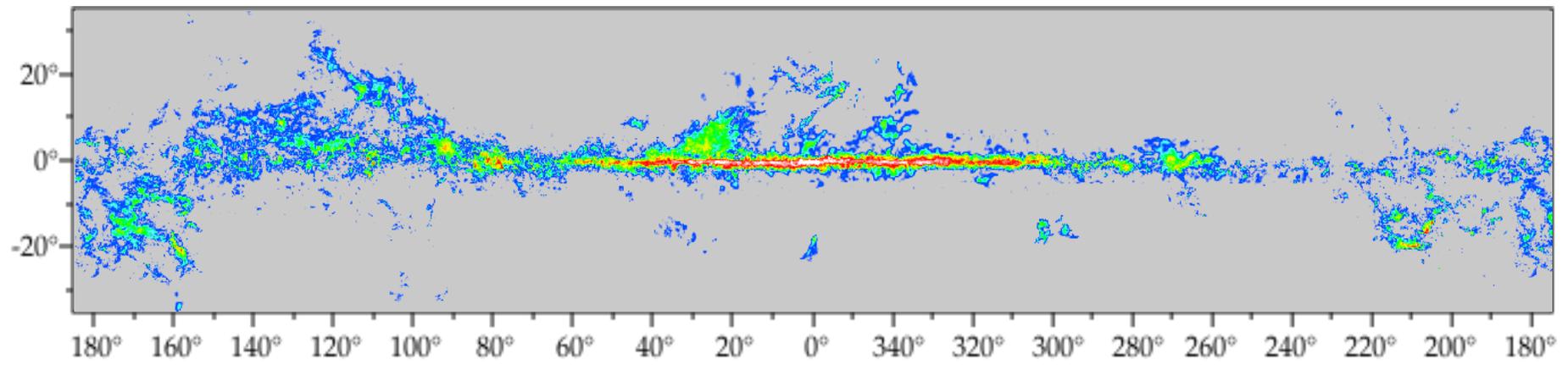


NGC 6946



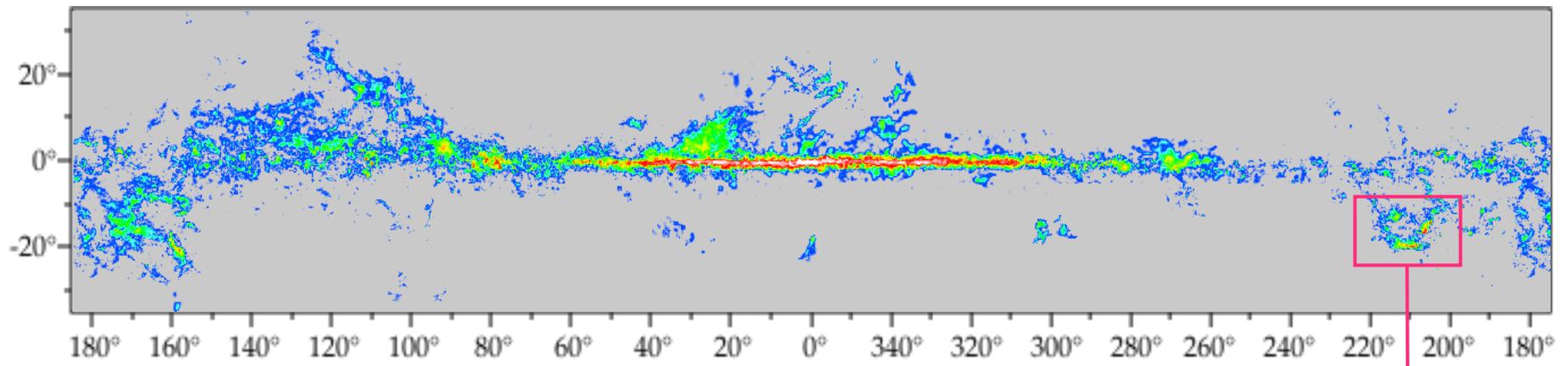
star
formation

- HI gas more extended
- H2 and SF well correlated



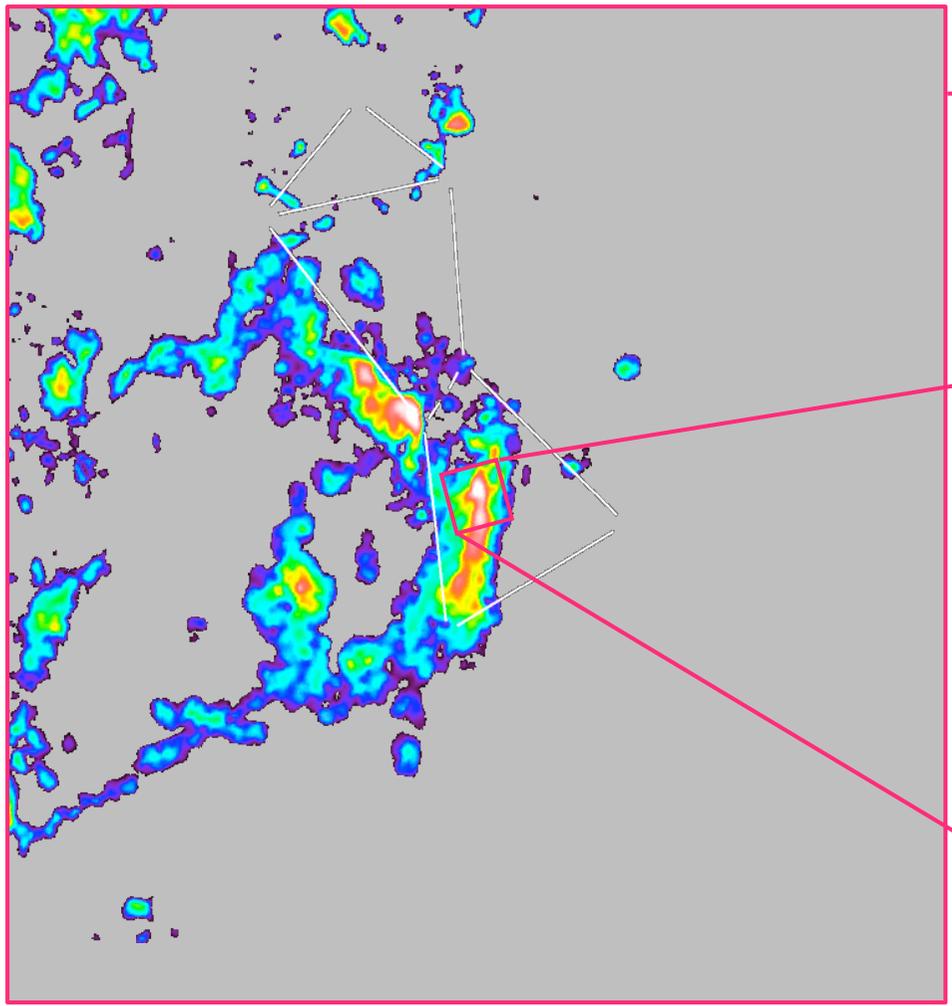
distribution of molecular
gas in the Milky Way as
traced by CO emission

data from T. Dame (CfA Harvard)



Orion

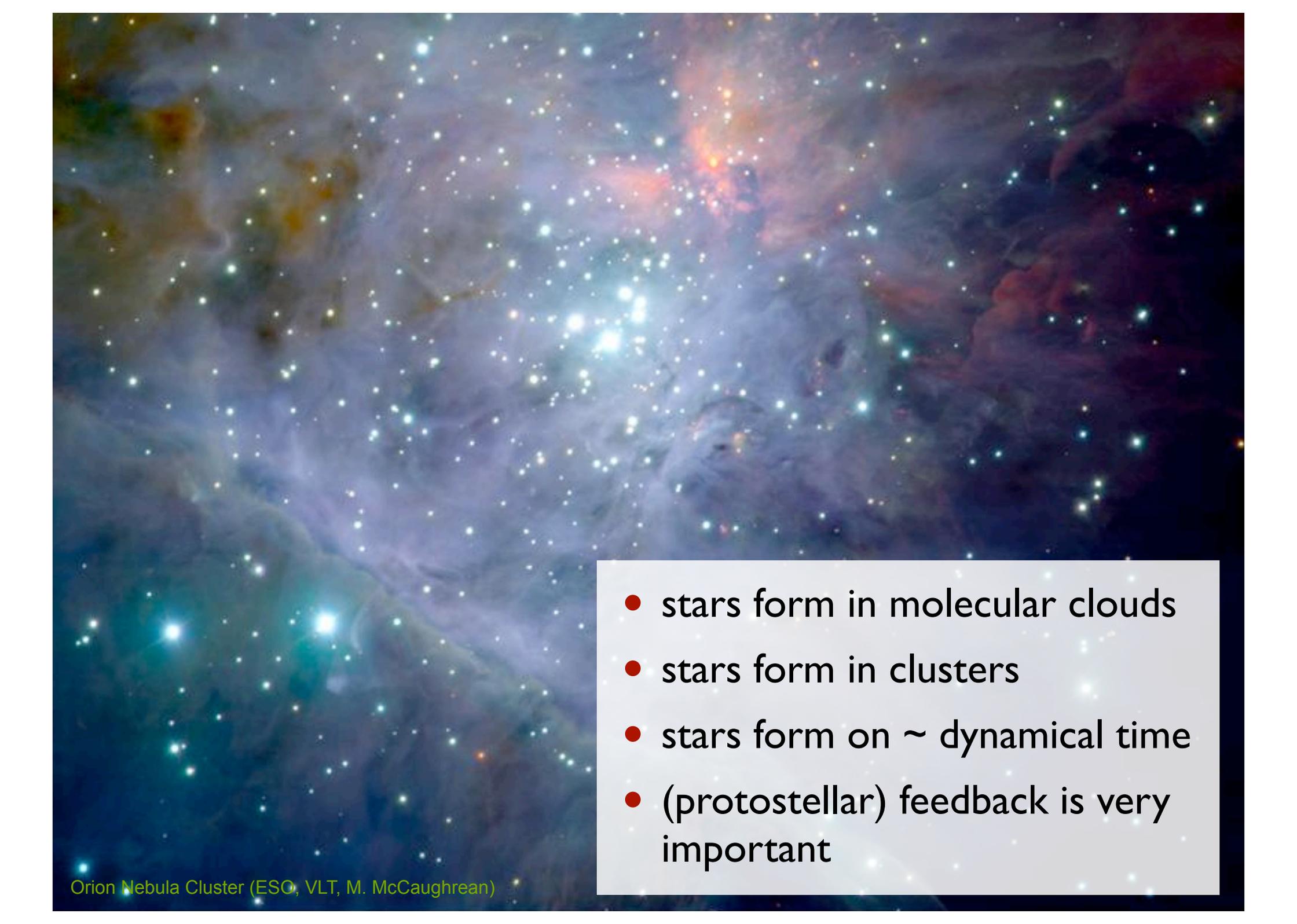
data from T. Dame (CfA Harvard)



Orion Nebula Cluster (ESO, VLT, M. McCaughrean)



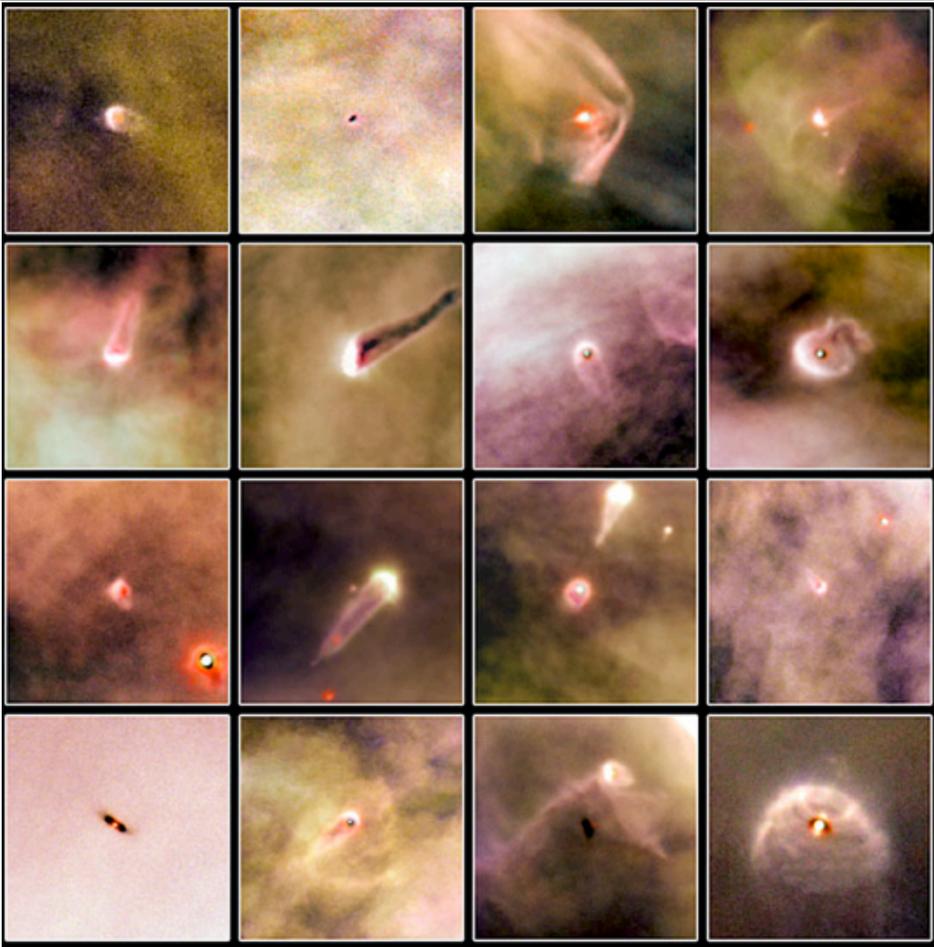
Orion Nebula Cluster (ESO, VLT, M. McCaughrean)

- 
- A wide-field astronomical image of the Orion Nebula Cluster, showing a vast field of stars of various colors (blue, white, yellow, red) and sizes, set against a backdrop of colorful interstellar dust and gas clouds in shades of blue, purple, and red. The stars are densely packed in some areas, particularly in the lower-left and upper-right quadrants.
- stars form in molecular clouds
 - stars form in clusters
 - stars form on \sim dynamical time
 - (protostellar) feedback is very important

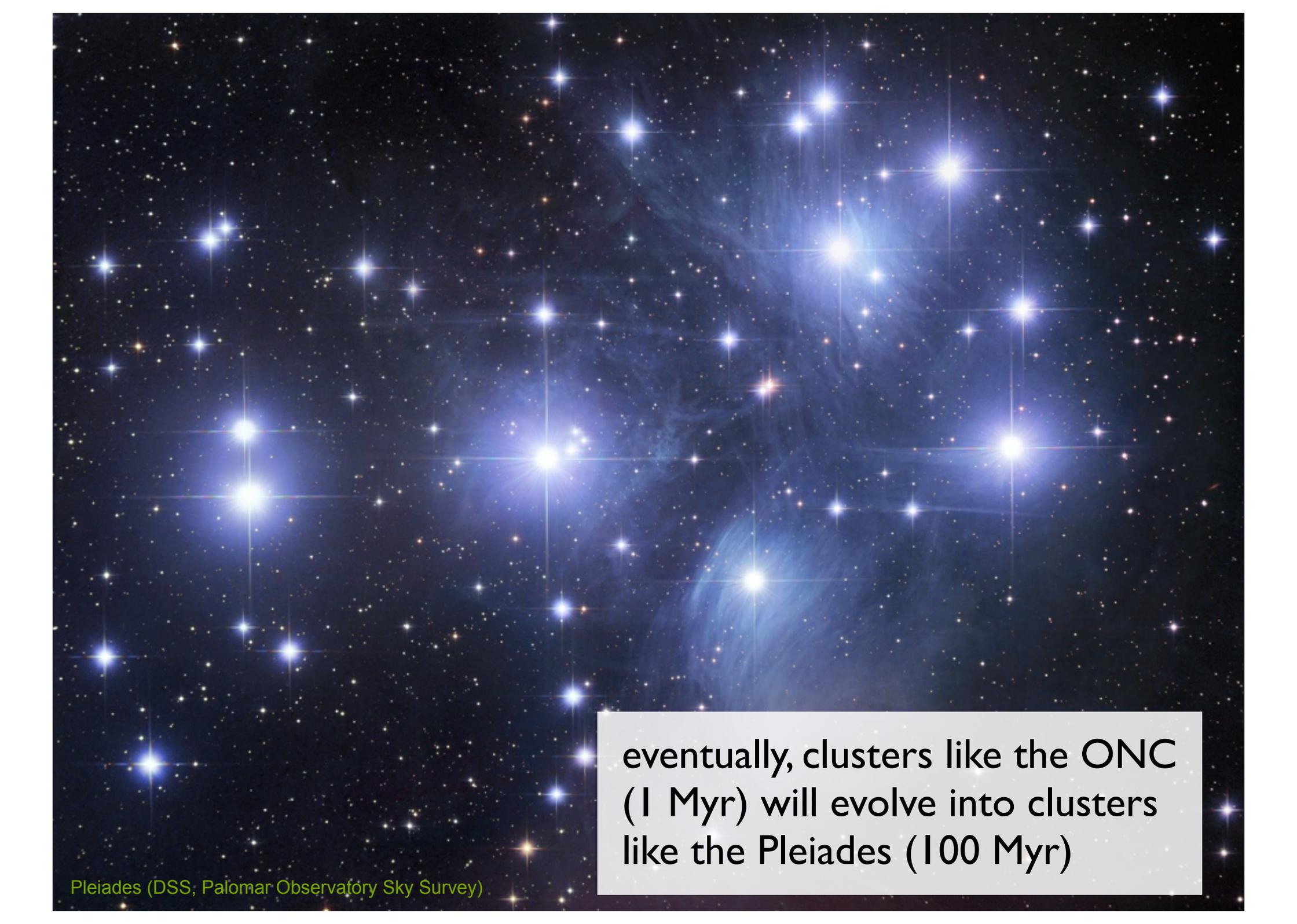


Trapezium stars in the center of the ONC (HST, Johnstone et al. 1998)

- strong feedback: UV radiation from Θ 1C Orionis affects star formation on all cluster scales



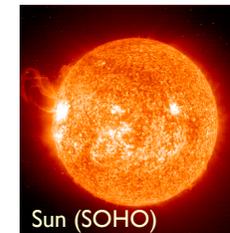
Trapezium stars in the center of the ONC (HST, Johnstone et al. 1998)



eventually, clusters like the ONC
(1 Myr) will evolve into clusters
like the Pleiades (100 Myr)

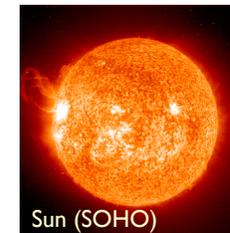
theoretical
approach

decrease in spatial scale / increase in density



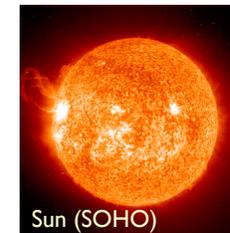
- density
 - density of ISM: few particles per cm^3
 - density of molecular cloud: few 100 particles per cm^3
 - density of Sun: 1.4 g/cm^3
- spatial scale
 - size of molecular cloud: few 10s of pc
 - size of young cluster: $\sim 1 \text{ pc}$
 - size of Sun: $1.4 \times 10^{10} \text{ cm}$

decrease in spatial scale / increase in density



- contracting force
 - only force that can do this compression is **GRAVITY**
- opposing forces
 - there are several processes that can oppose gravity
 - **GAS PRESSURE**
 - **TURBULENCE**
 - **MAGNETIC FIELDS**
 - **RADIATION PRESSURE**

decrease in spatial scale / increase in density



- contracting force
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Modern star formation theory is based on the complex interplay between *all* these processes.



Modern star formation theory is based on the complex interplay between *all* these processes.

early theoretical models

- *Jeans (1902)*: Interplay between self-gravity and thermal pressure
 - stability of homogeneous spherical density enhancements against gravitational collapse
 - dispersion relation:

$$\omega^2 = c_s^2 k^2 - 4\pi G \rho_0$$

- instability when $\omega^2 < 0$

- minimal mass: $M_J = \frac{1}{6} \pi^{-5/2} G^{-3/2} \rho_0^{-1/2} c_s^3 \propto \rho_0^{-1/2} T^{+3/2}$



Sir James Jeans, 1877 - 1946

first approach to turbulence

- *von Weizsäcker (1943, 1951) and Chandrasekhar (1951): concept of **MICROTURBULENCE***

- BASIC ASSUMPTION: separation of scales between dynamics and turbulence

$$\ell_{\text{turb}} \ll \ell_{\text{dyn}}$$

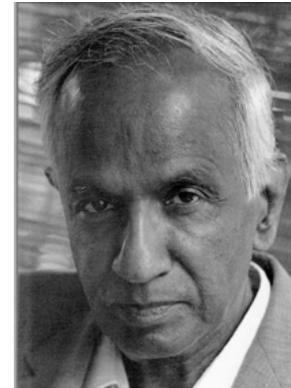
- then turbulent velocity dispersion contributes to effective soundspeed:

$$c_c^2 \mapsto c_c^2 + \sigma_{rms}^2$$

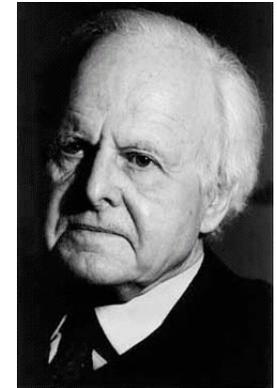
- \rightarrow Larger effective Jeans masses \rightarrow more stability

- BUT: (1) *turbulence depends on k* : $\sigma_{rms}^2(k)$

(2) *supersonic turbulence* $\rightarrow \sigma_{rms}^2(k) \gg c_s^2$ usually



S. Chandrasekhar,
1910 - 1995



C.F. von Weizsäcker,
1912 - 2007

problems of early dynamical theory

- molecular clouds are *highly Jeans-unstable*, yet, they do *NOT* form stars at high rate and with high efficiency (Zuckerman & Evans 1974 conundrum) (the observed global SFE in molecular clouds is $\sim 5\%$)
→ *something prevents large-scale collapse.*
- all throughout the early 1990's, molecular clouds had been thought to be long-lived quasi-equilibrium entities.
- molecular clouds are *magnetized*

magnetic star formation

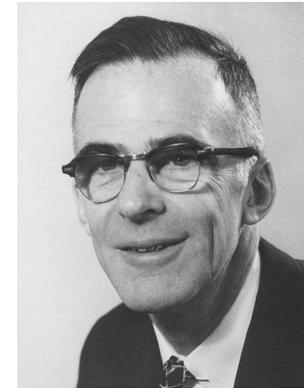
- *Mestel & Spitzer (1956)*: Magnetic fields can prevent collapse!!!
 - Critical mass for gravitational collapse in presence of B-field

$$M_{cr} = \frac{5^{3/2}}{48\pi^2} \frac{B^3}{G^{3/2} \rho^2}$$

- Critical mass-to-flux ratio (Mouschovias & Spitzer 1976)

$$\left[\frac{M}{\Phi} \right]_{cr} = \frac{\xi}{3\pi} \left[\frac{5}{G} \right]^{1/2}$$

- Ambipolar diffusion can initiate collapse



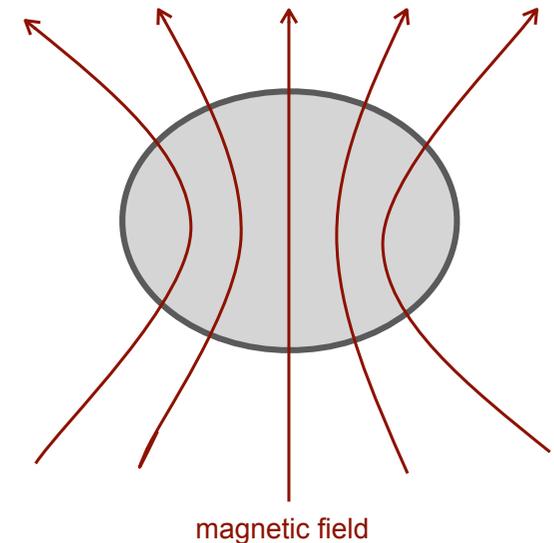
Lyman Spitzer, Jr., 1914 - 1997

“standard theory” of star formation

- BASIC ASSUMPTION: Stars form from magnetically highly subcritical cores
- Ambipolar diffusion slowly increases (M/Φ) : $\tau_{AD} \approx 10\tau_{ff}$
- Once $(M/\Phi) > (M/\Phi)_{crit}$: dynamical collapse of SIS
 - Shu (1977) collapse solution
 - $dM/dt = 0.975 c_s^3/G = \text{const.}$
- Was (in principle) only intended for isolated, low-mass stars



Frank Shu, 1943 -



problems of “standard theory”

- Observed B-fields are weak, at most marginally critical (Crutcher 1999, Bourke et al. 2001)
- Magnetic fields cannot prevent decay of turbulence (Mac Low et al. 1998, Stone et al. 1998, Padoan & Nordlund 1999)
- Structure of prestellar cores (e.g. Bacman et al. 2000, Alves et al. 2001)
- Strongly time varying dM/dt (e.g. Hendriksen et al. 1997, André et al. 2000)
- More extended infall motions than predicted by the standard model (Williams & Myers 2000, Myers et al. 2000)
- Most stars form as binaries (e.g. Lada 2006)
- As many prestellar cores as protostellar cores in SF regions (e.g. André et al 2002)
- Molecular cloud clumps are chemically young (Bergin & Langer 1997, Pratap et al 1997, Aikawa et al 2001)
- Stellar age distribution small ($\tau_{\text{ff}} \ll \tau_{\text{AD}}$) (Ballesteros-Paredes et al. 1999, Elmegreen 2000, Hartmann 2001)
- Strong theoretical criticism of the SIS as starting condition for gravitational collapse (e.g. Whitworth et al 1996, Nakano 1998, as summarized in Klessen & Mac Low 2004)
- Standard AD-dominated theory is incompatible with observations (Crutcher et al. 2009, 2010ab, Bertram et al. 2011)

gravoturbulent star formation

- BASIC ASSUMPTION:

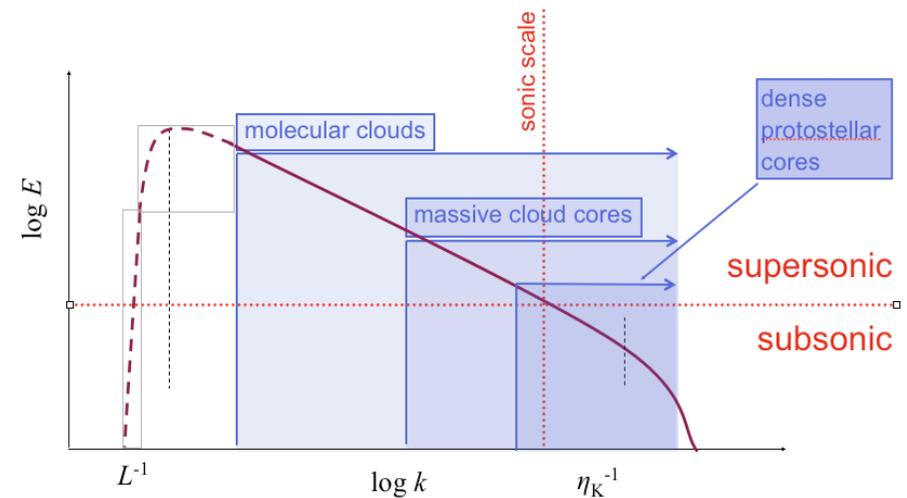
star formation is controlled by interplay between supersonic turbulence and self-gravity

- turbulence plays a *dual role*:

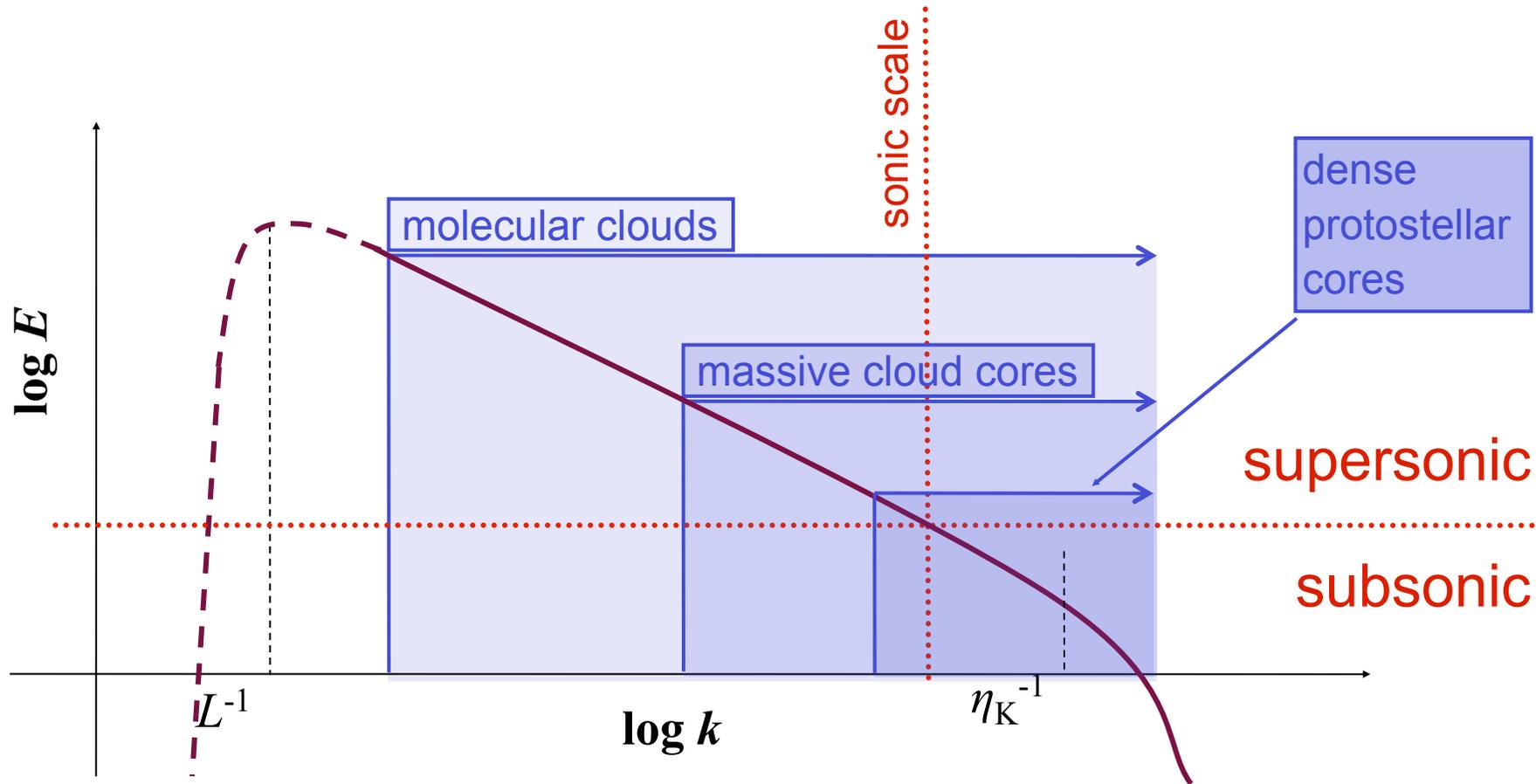
- on *large scales* it *provides support*
- on *small scales* it can *trigger collapse*

- some predictions:

- dynamical star formation timescale τ_{ff}
- high binary fraction
- complex spatial structure of embedded star clusters
- and many more . . .



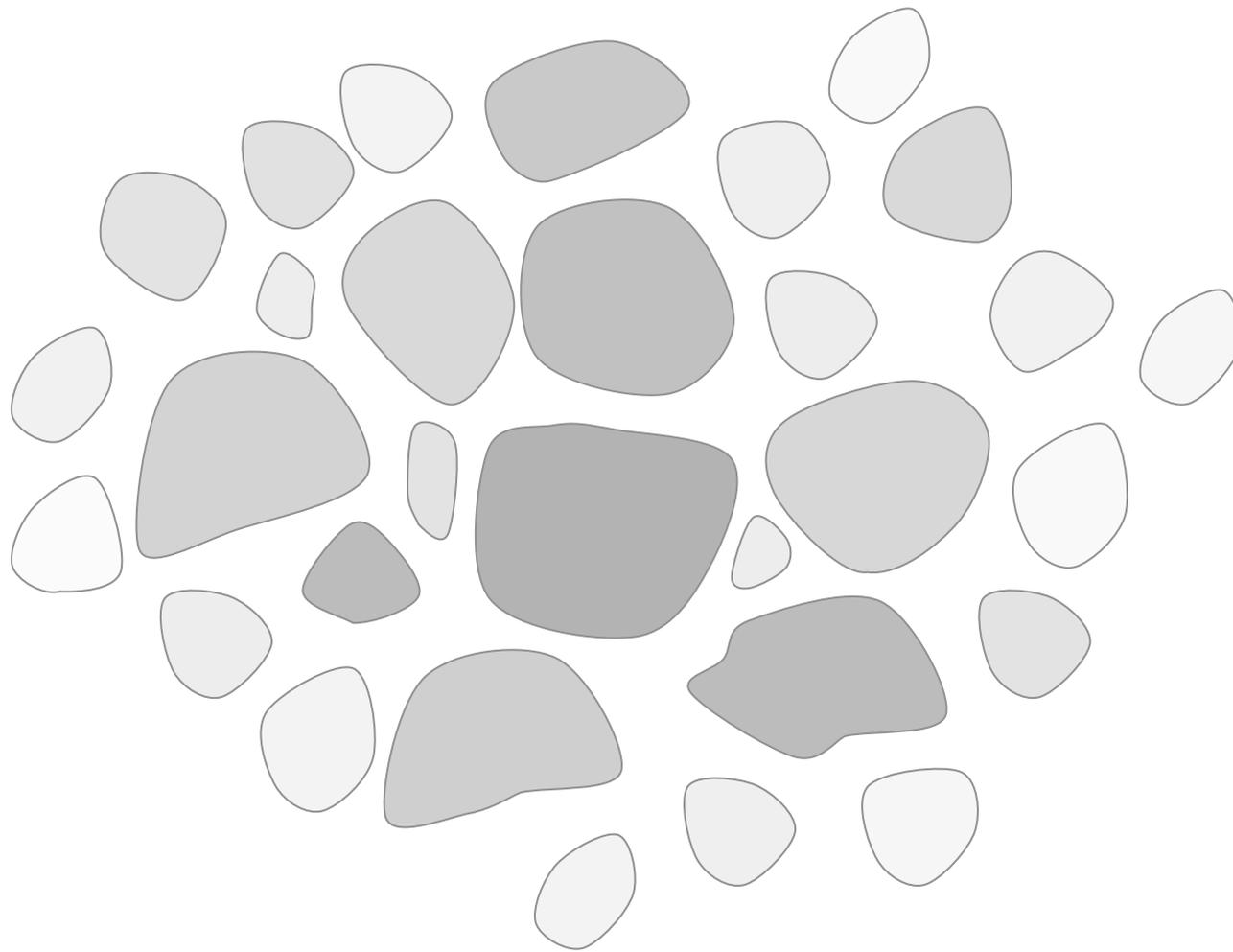
turbulent cascade in the ISM



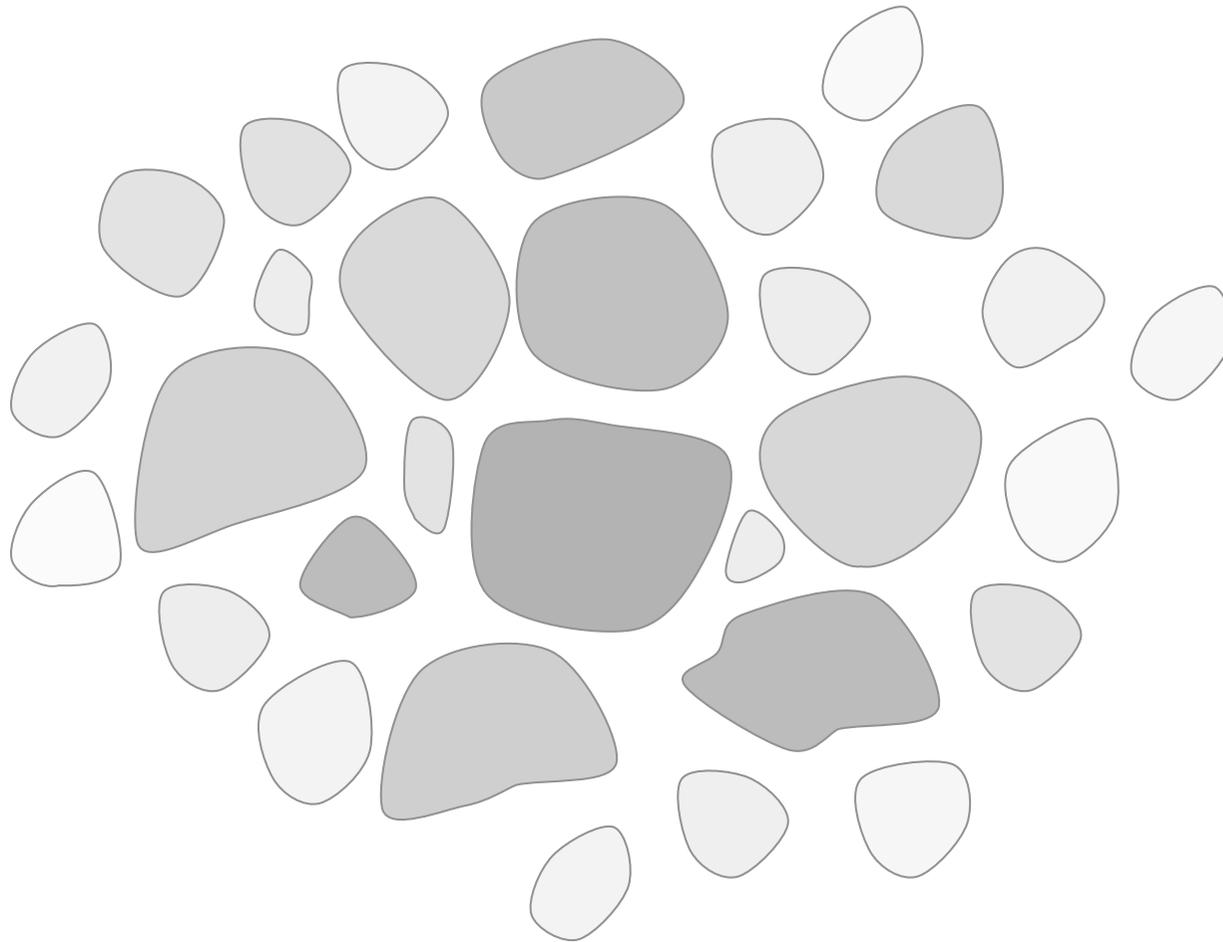
energy source & scale
NOT known
 (supernovae, winds,
 spiral density waves?)

$\sigma_{\text{rms}} \ll 1 \text{ km/s}$
 $M_{\text{rms}} \leq 1$
 $L \approx 0.1 \text{ pc}$

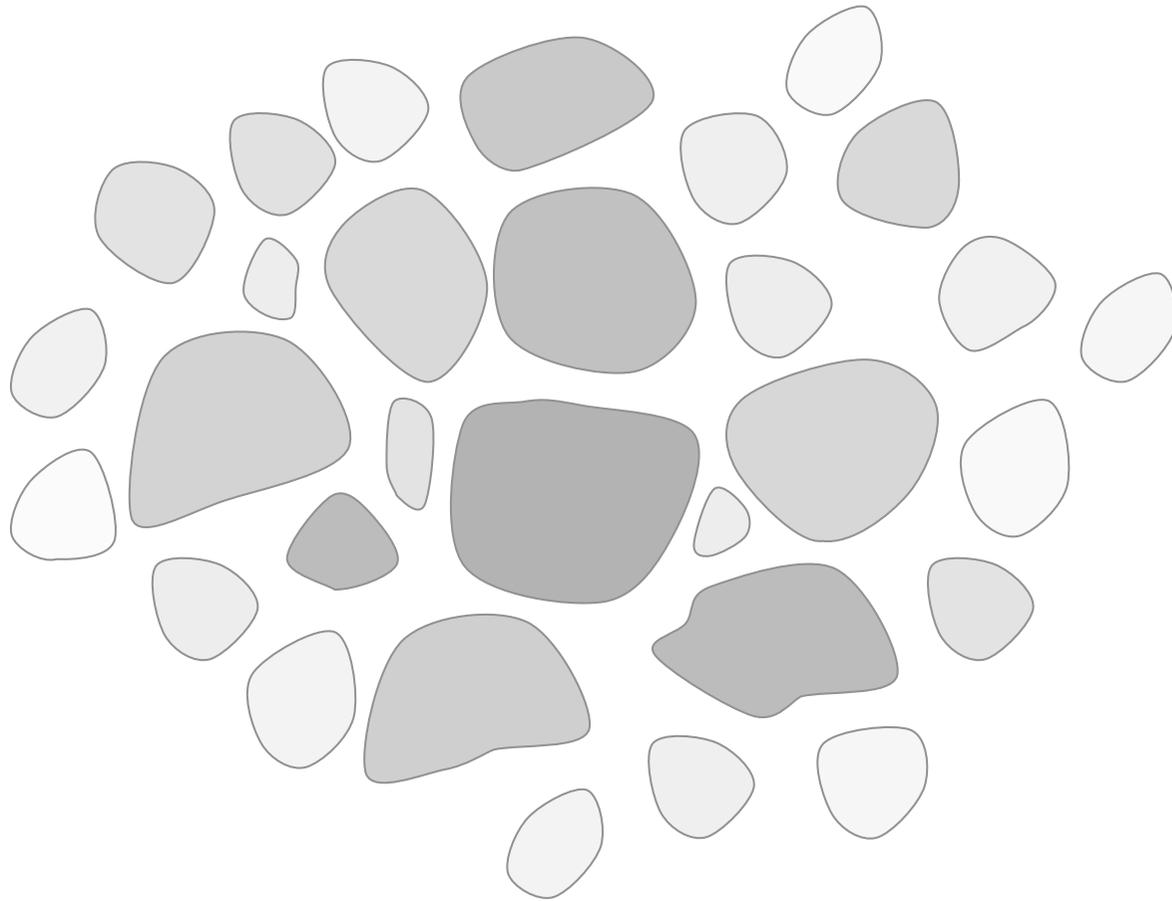
dissipation scale not known
 (ambipolar diffusion,
 molecular diffusion?)



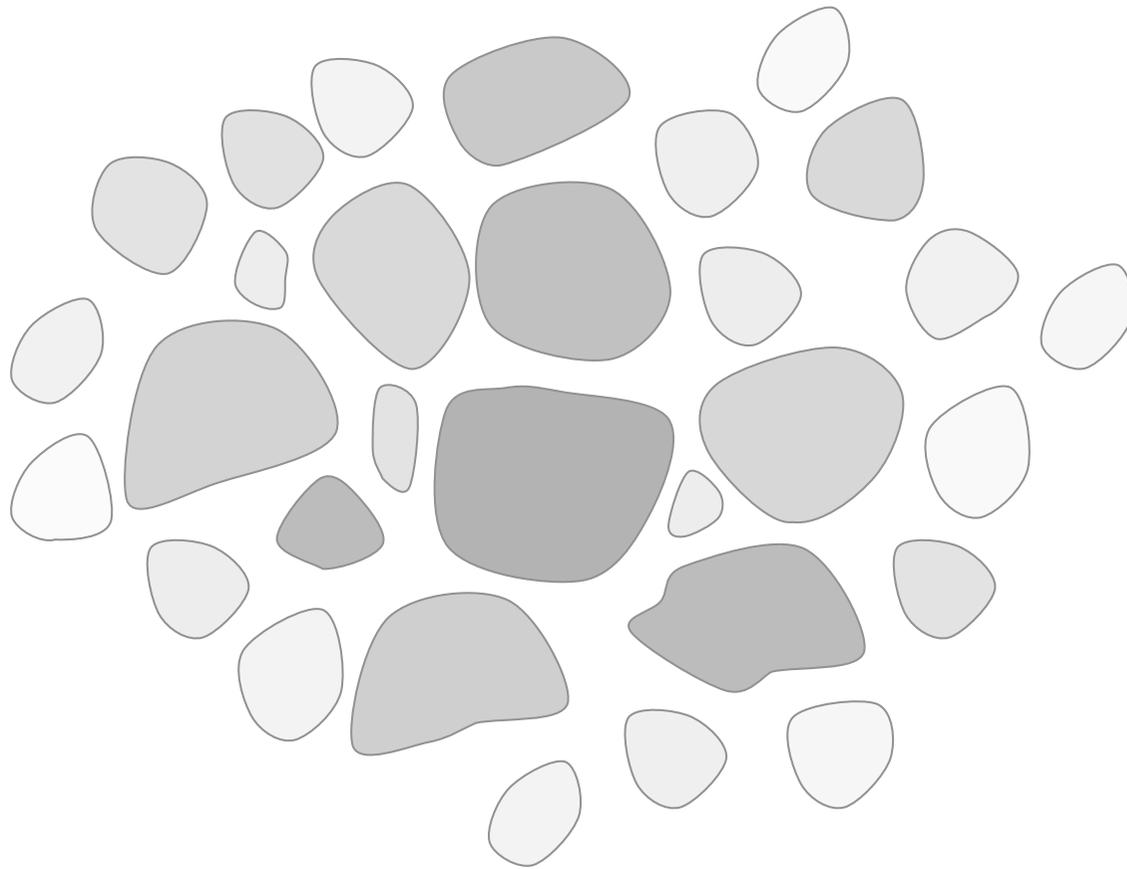
turbulence creates a hierarchy of clumps



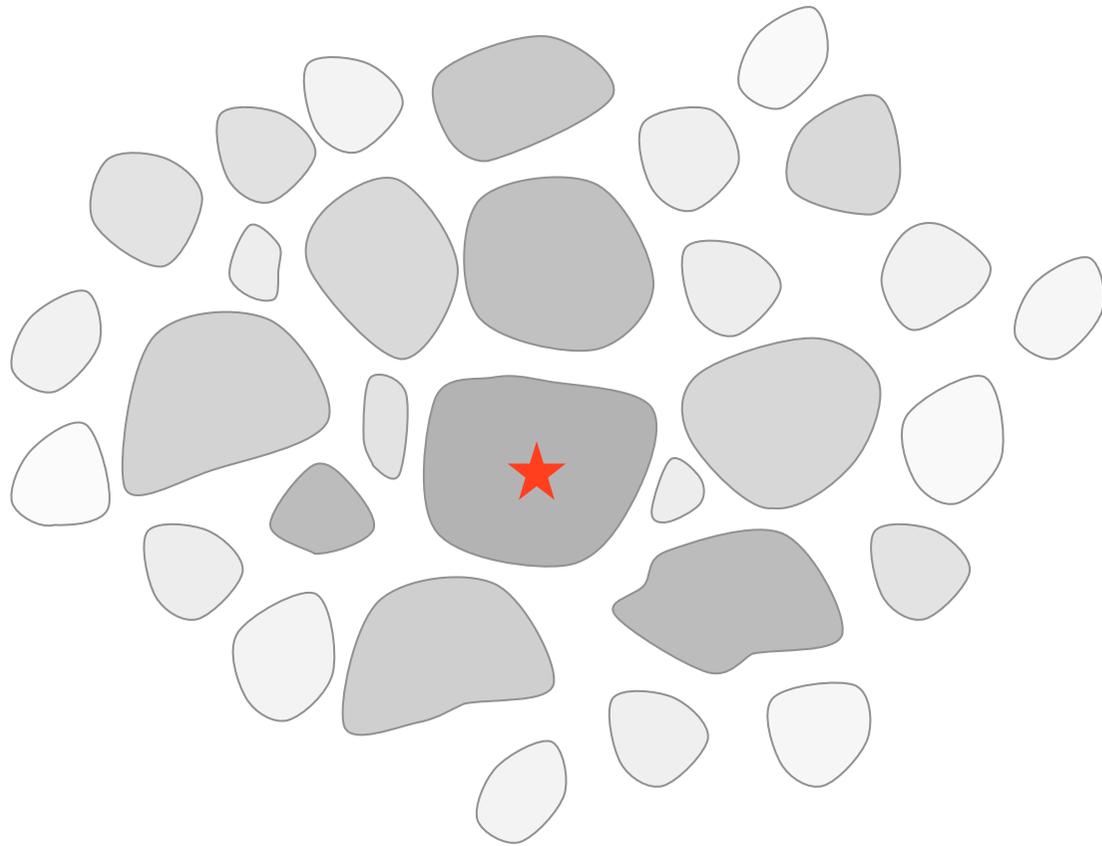
as turbulence decays locally, contraction sets in



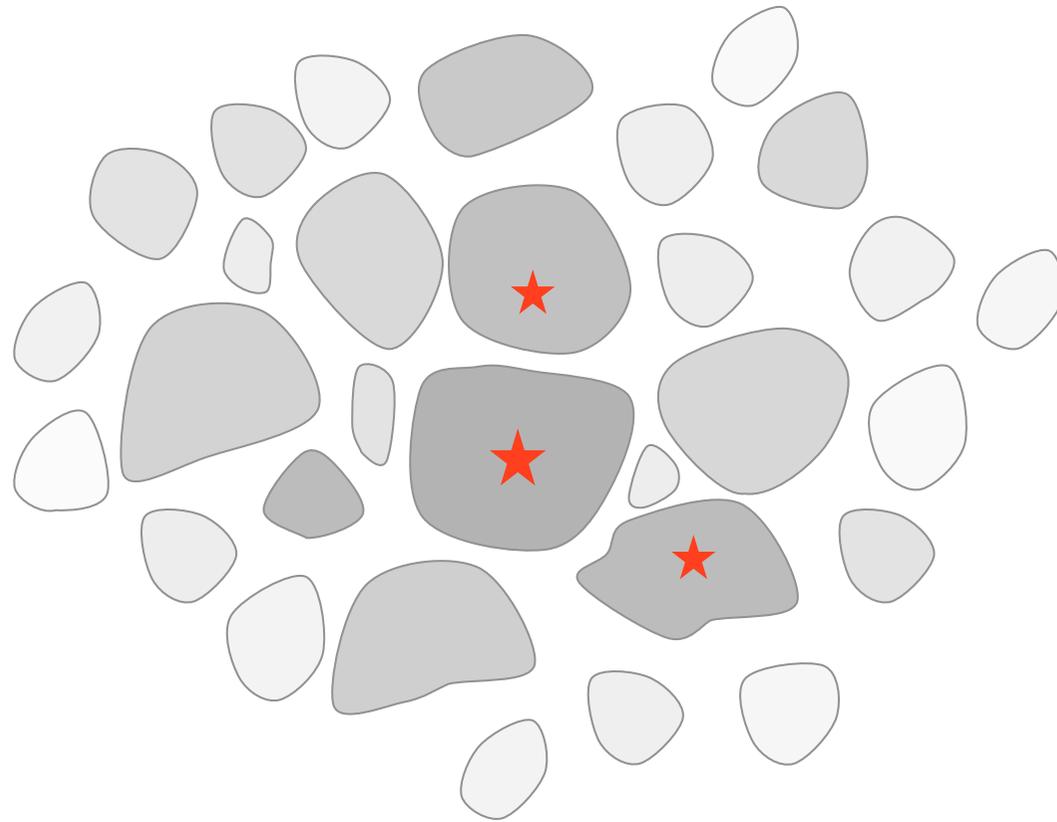
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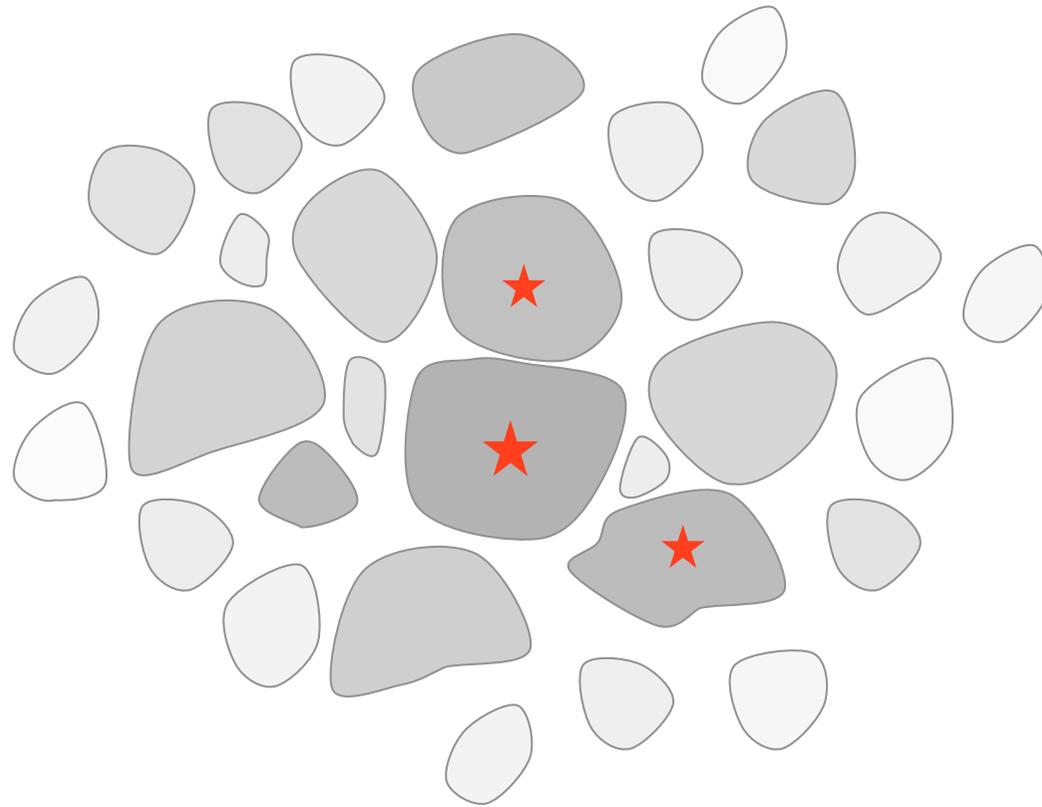
while region contracts, individual clumps collapse to form stars



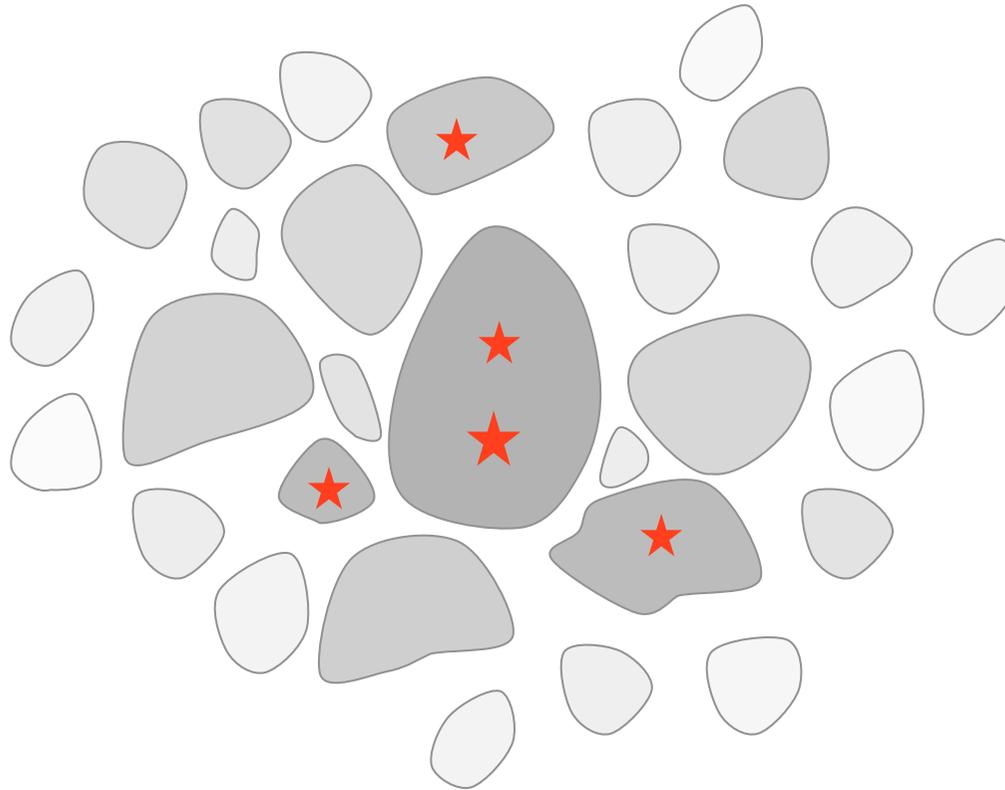
while region contracts, individual clumps collapse to form stars



individual clumps collapse to form stars

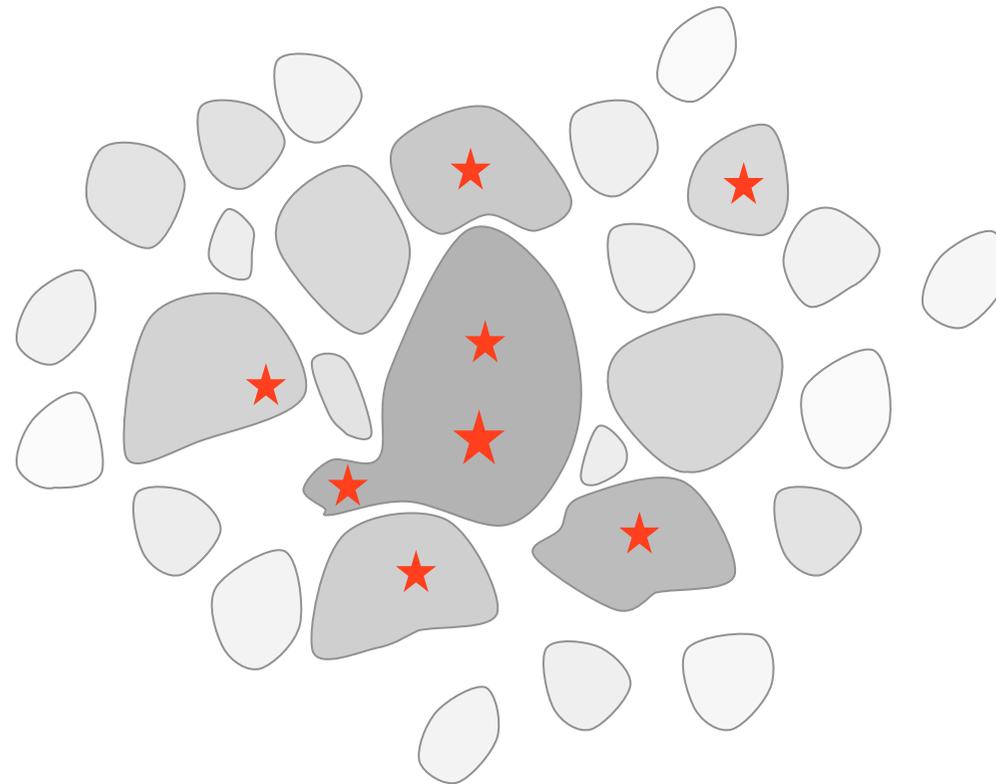


individual clumps collapse to form stars

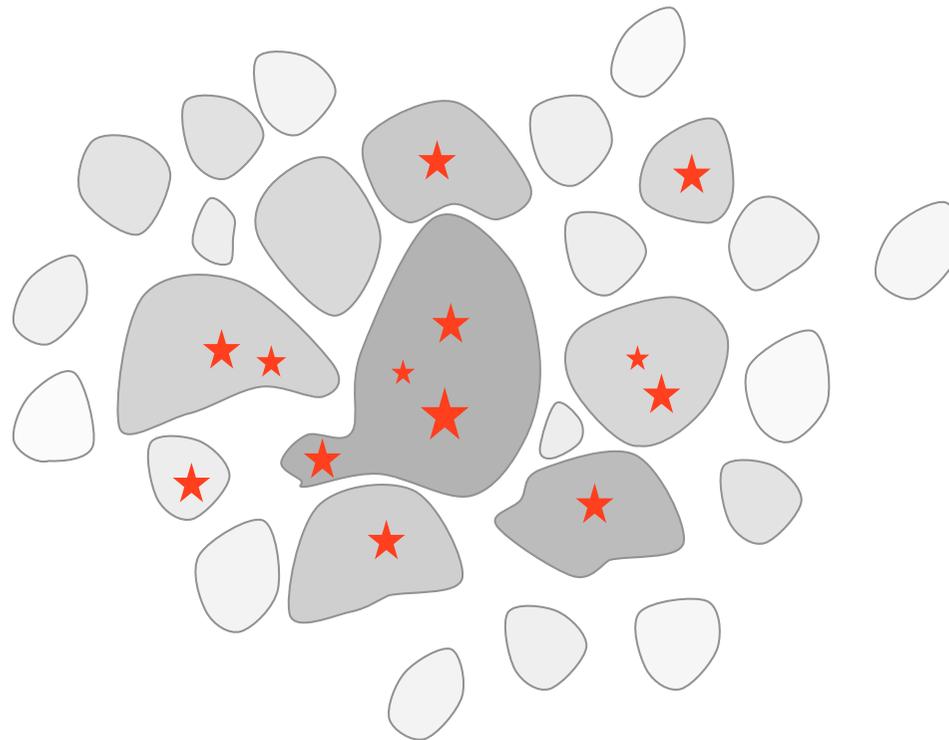


$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

in *dense clusters*, clumps may merge while collapsing
--> then contain multiple protostars



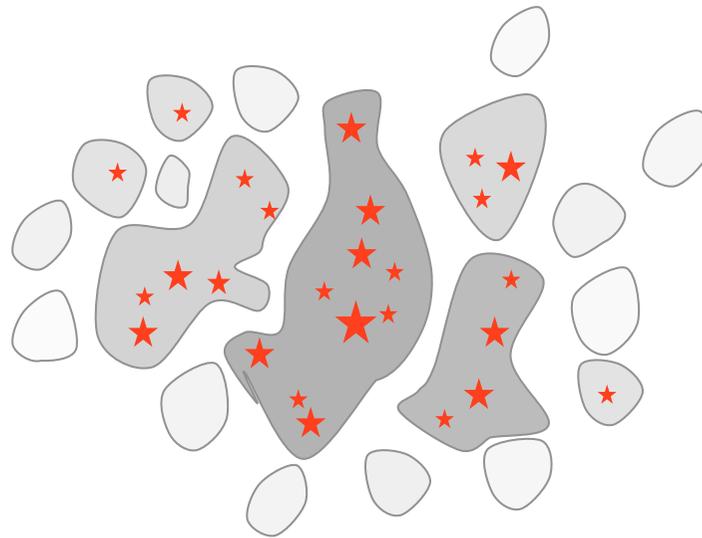
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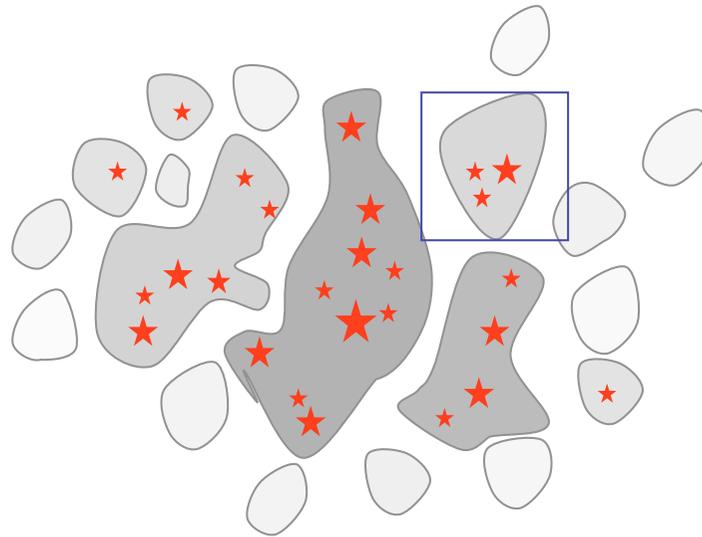
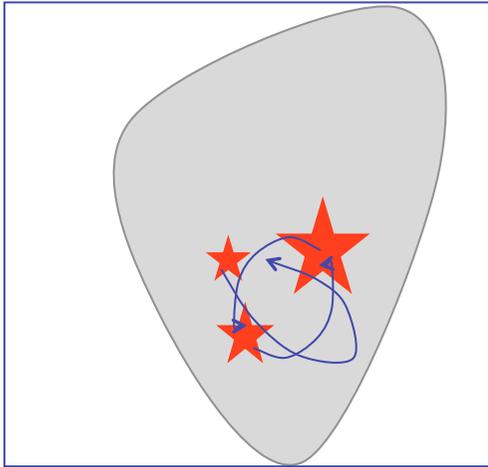
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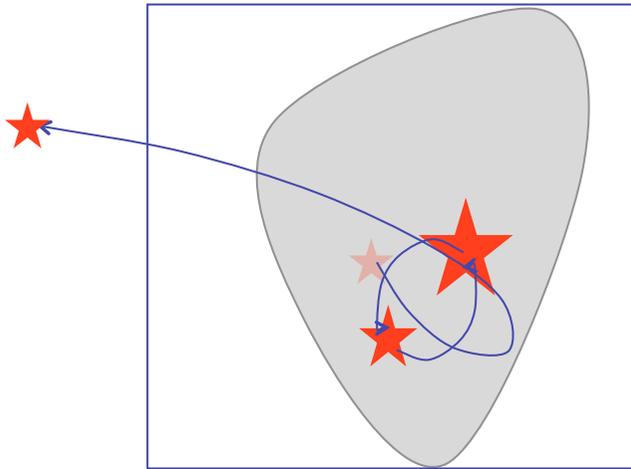
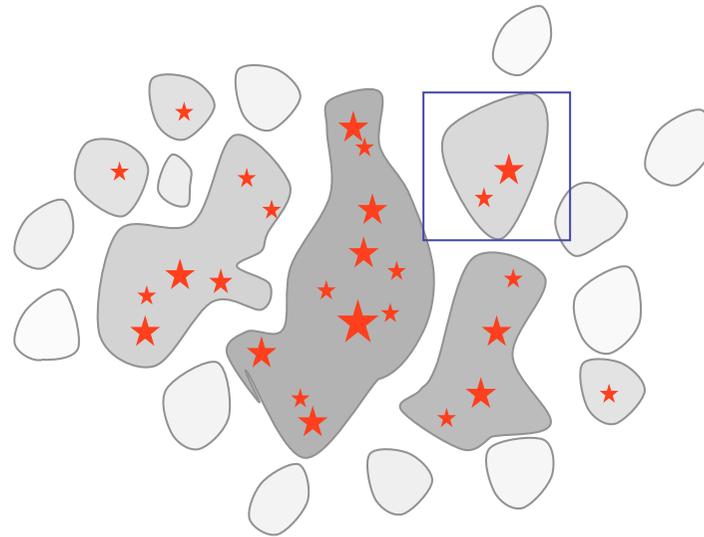
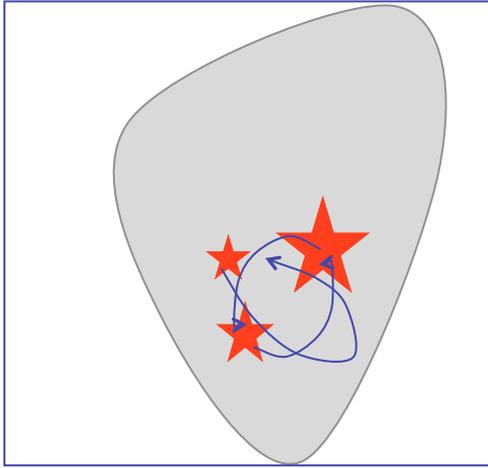
in *dense clusters*, competitive mass growth becomes important



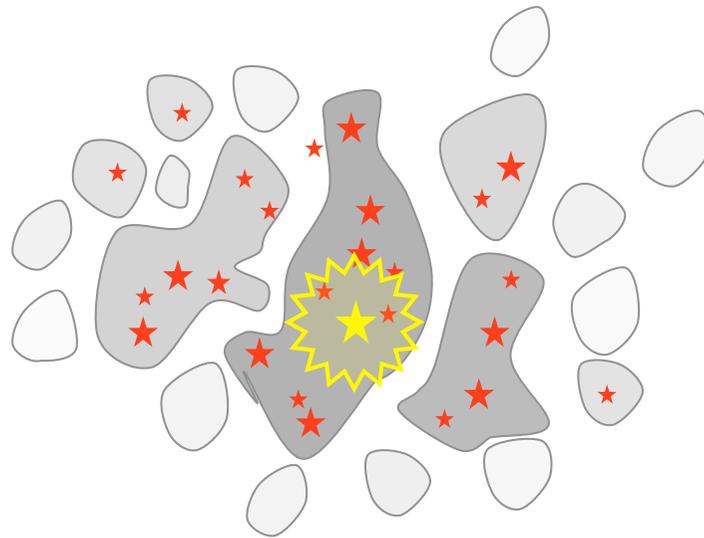
in *dense clusters*, competitive mass growth becomes important



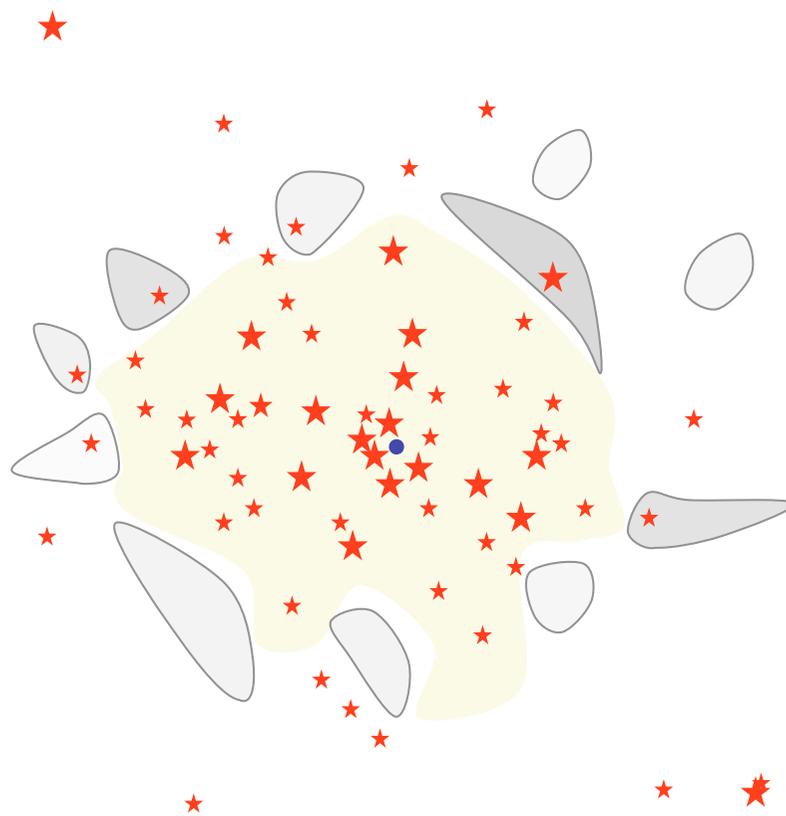
in *dense clusters*, *N*-body effects influence mass growth



low-mass objects may
become ejected --> accretion stops



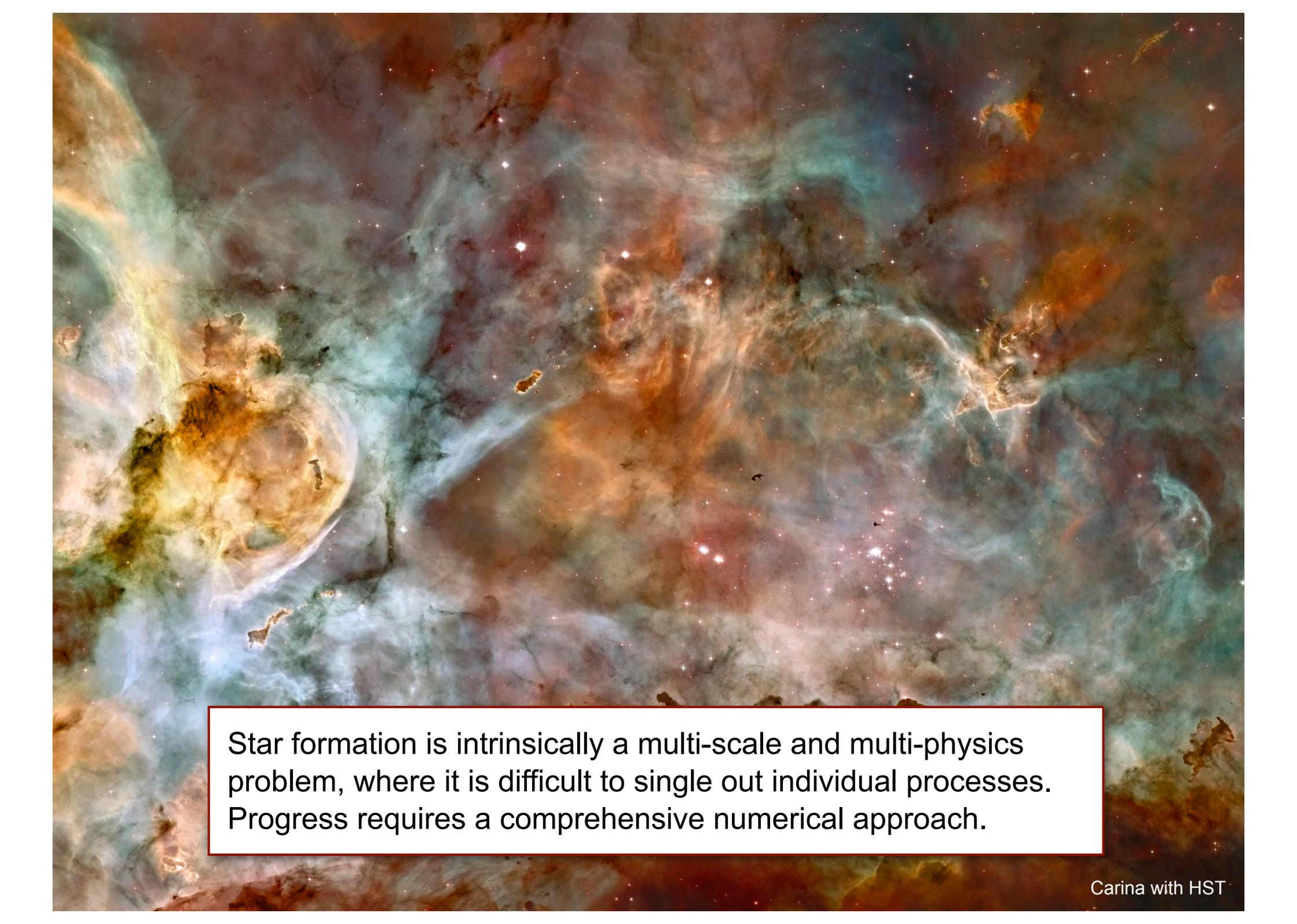
feedback terminates star formation



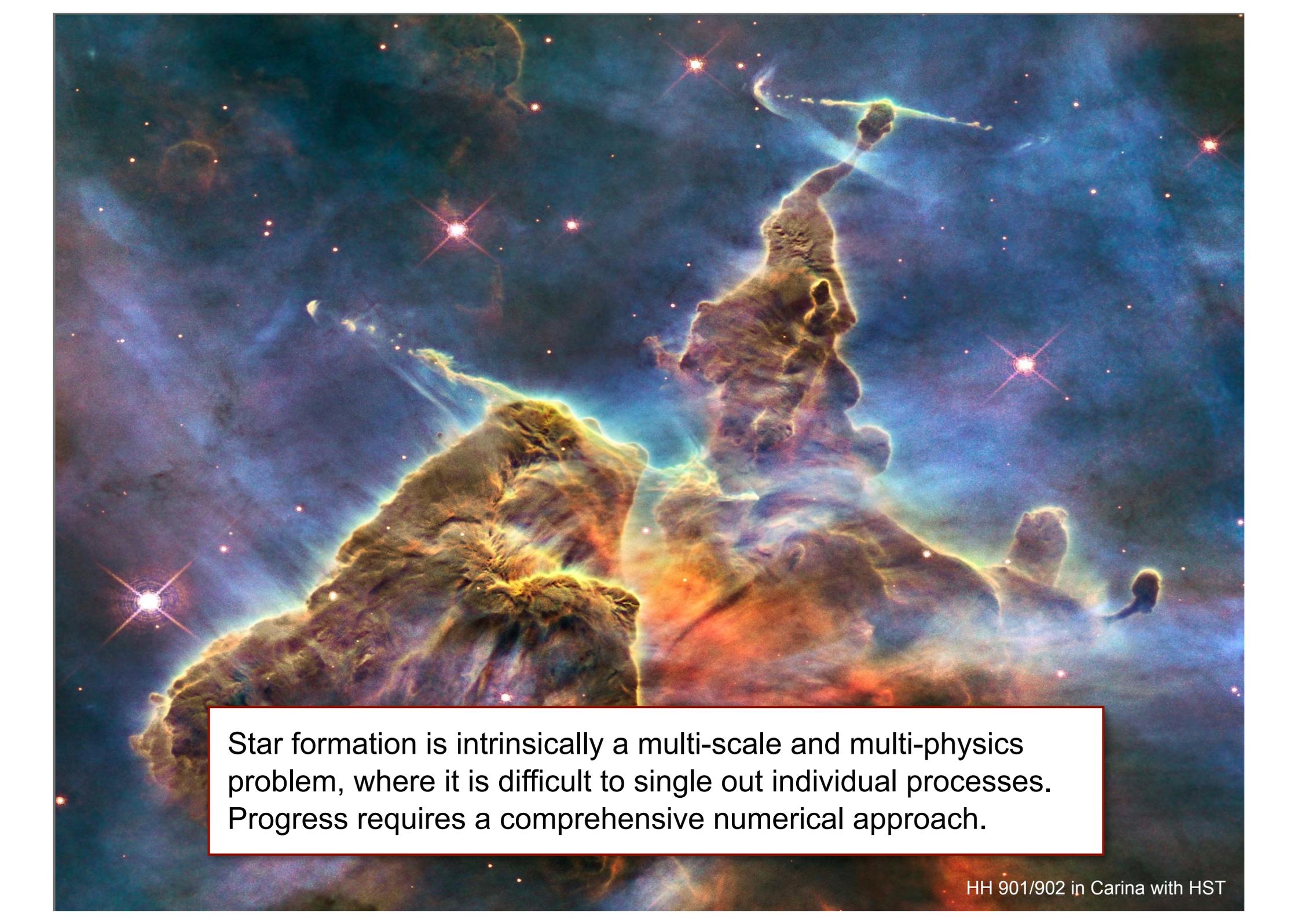
result: *star cluster*, possibly with H_{II} region



Carina with HST



Star formation is intrinsically a multi-scale and multi-physics problem, where it is difficult to single out individual processes. Progress requires a comprehensive numerical approach.



Star formation is intrinsically a multi-scale and multi-physics problem, where it is difficult to single out individual processes. Progress requires a comprehensive numerical approach.

two selected examples

- formation and evolution of molecular clouds
 - combine MHD with self-gravity and time-dependent chemistry
 - model the turbulent multi-phase interstellar medium
- stellar mass function
 - distribution of stellar masses today and in the early univers

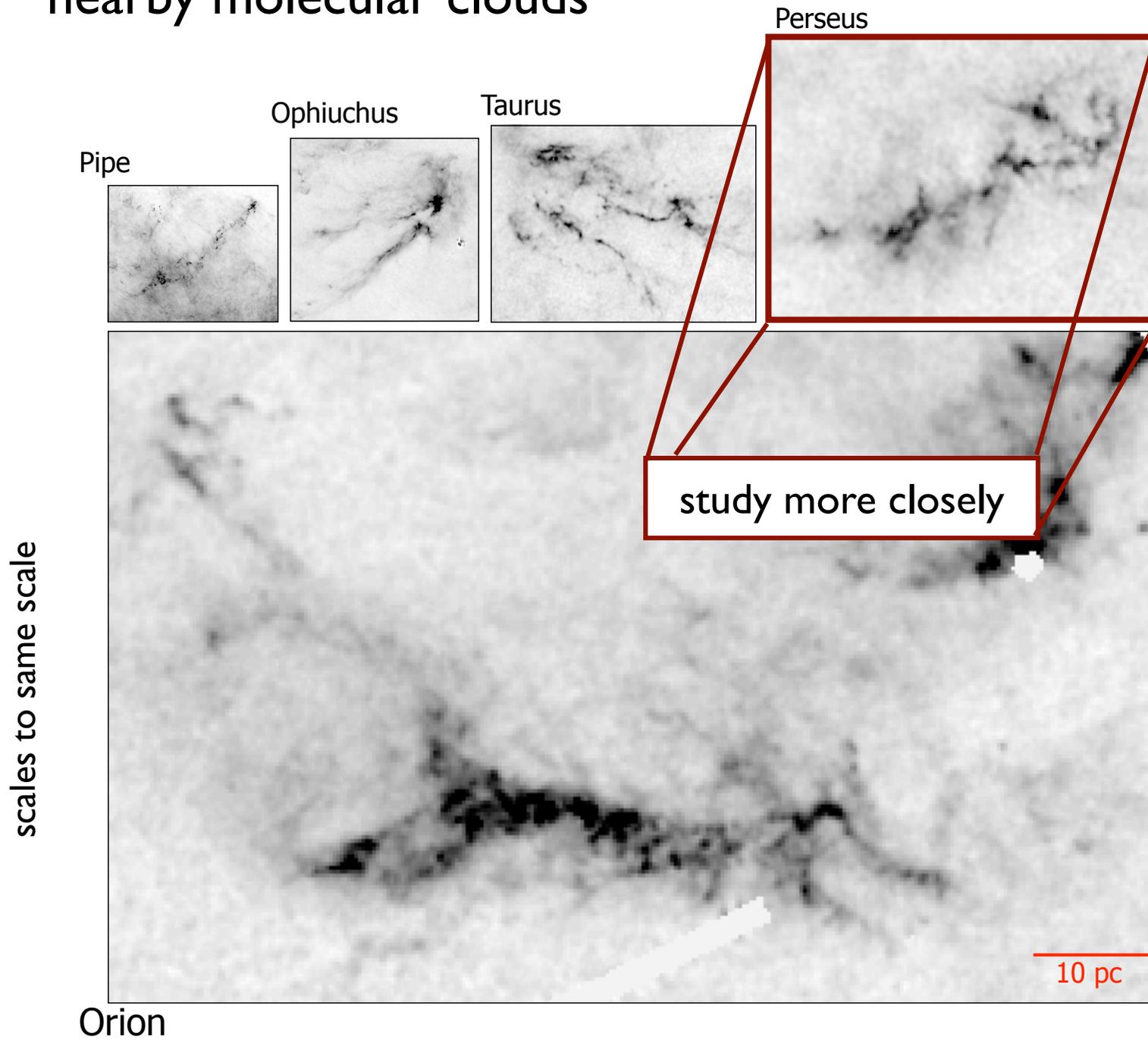


two selected examples

- formation and evolution of molecular clouds
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- stellar mass function
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nearby molecular clouds

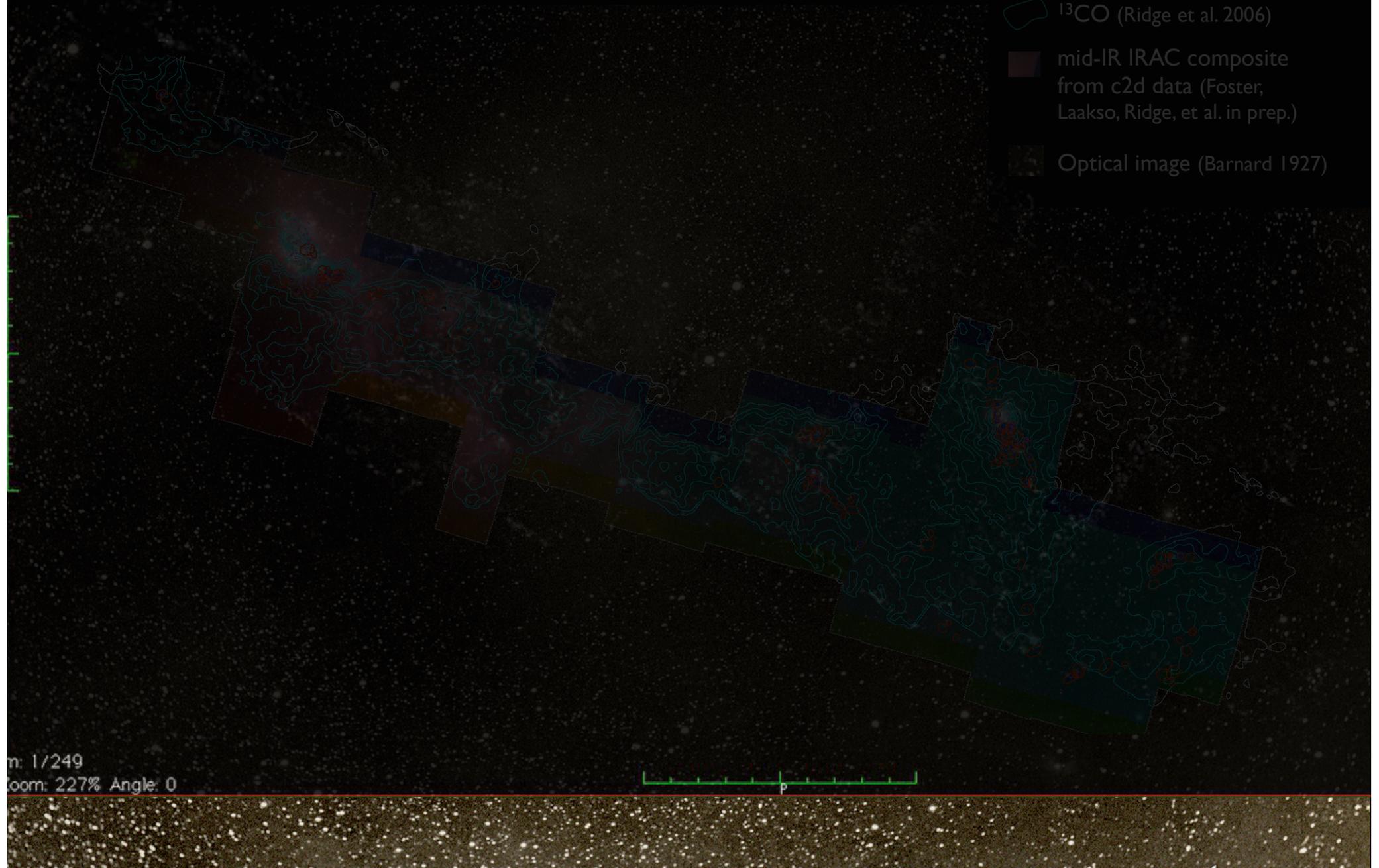


(from A. Goodman)

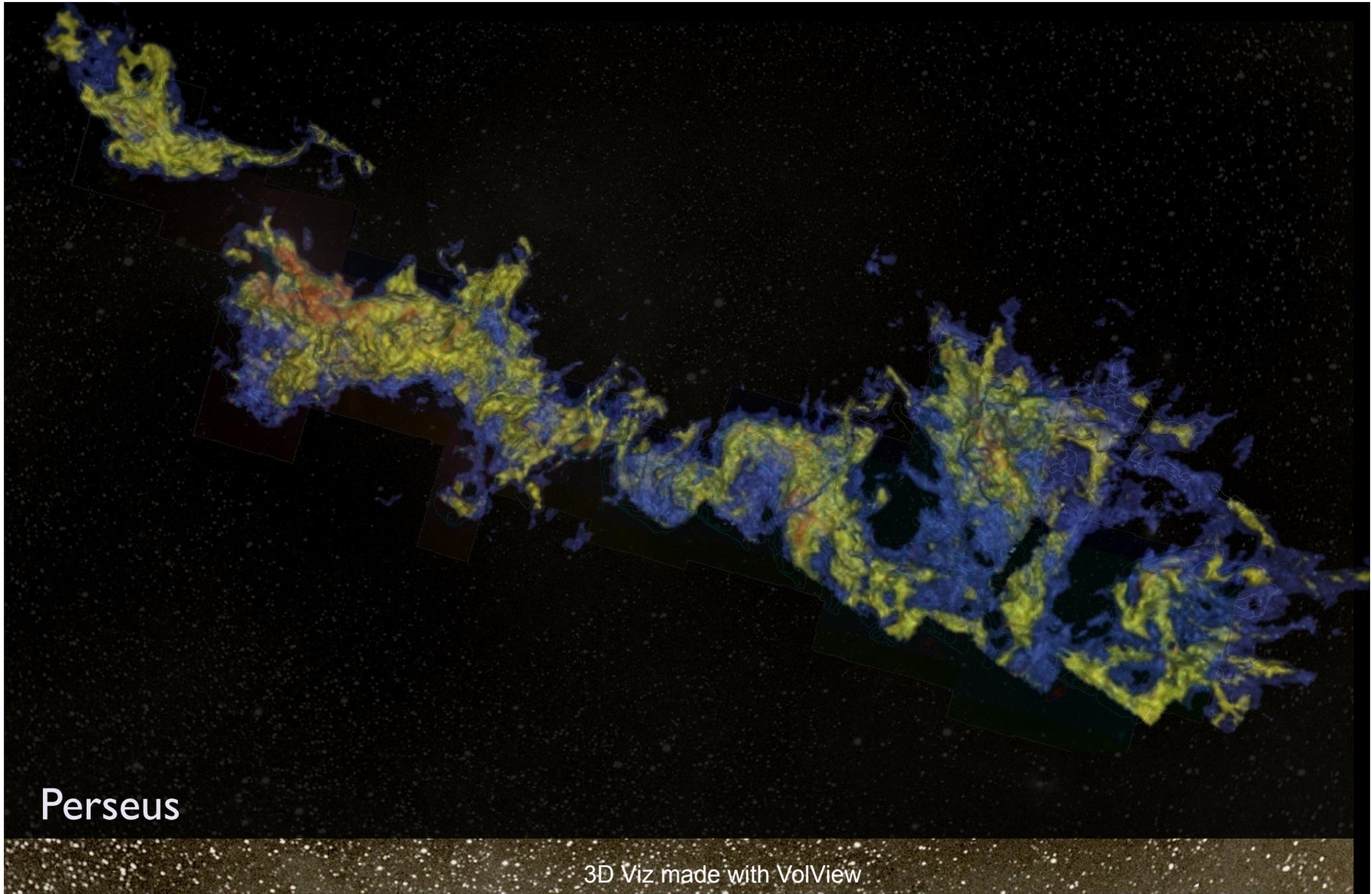
COMPLETE Perseus

Image size: 1305 x 733
H: 63 W: 127

-  mm peak (Enoch et al. 2006)
-  sub-mm peak (Hatchell et al. 2005, Kirk et al. 2006)
-  ^{13}CO (Ridge et al. 2006)
-  mid-IR IRAC composite from c2d data (Foster, Laakso, Ridge, et al. in prep.)
-  Optical image (Barnard 1927)

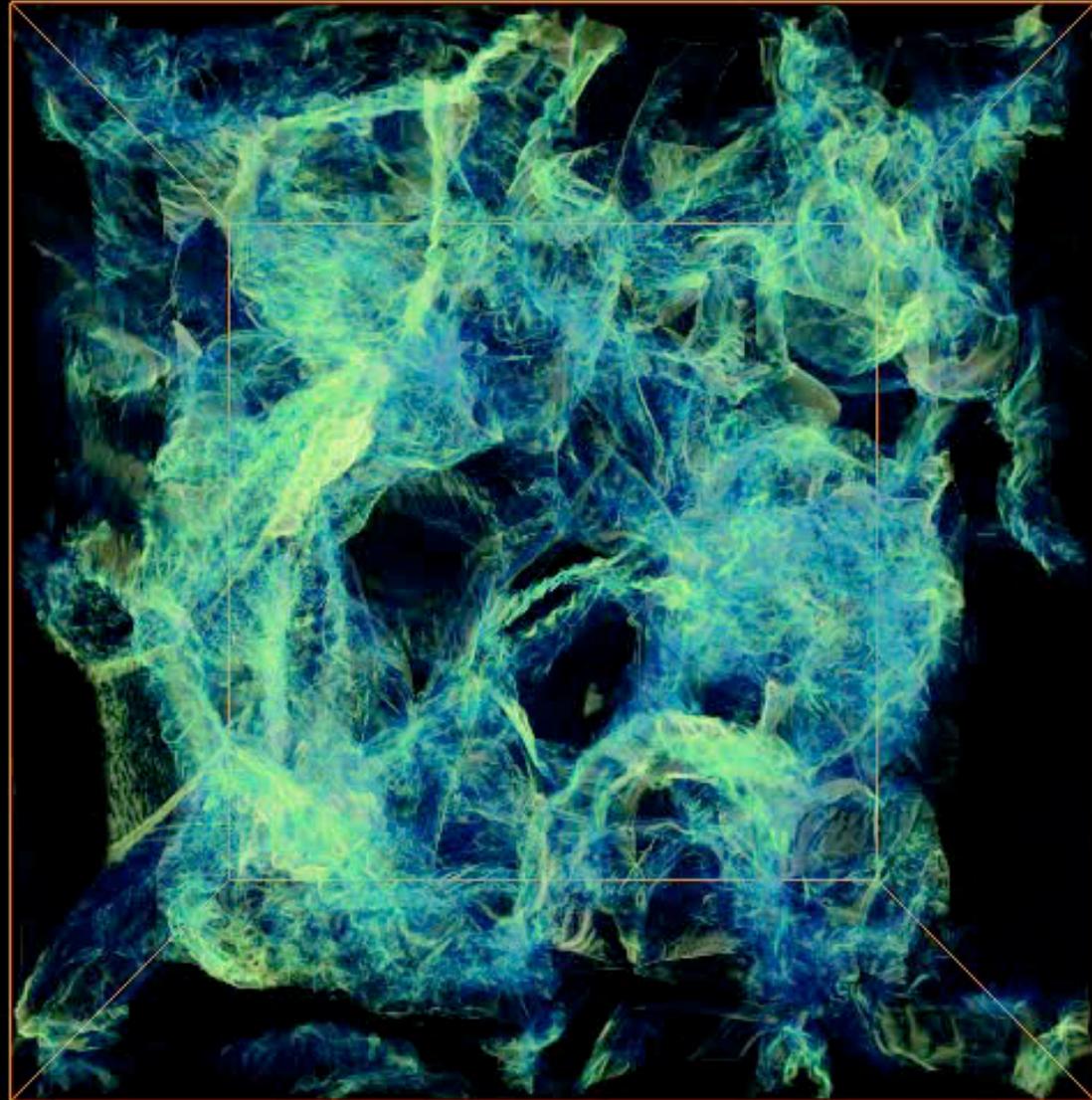


m: 1/249
Zoom: 227% Angle: 0



Perseus

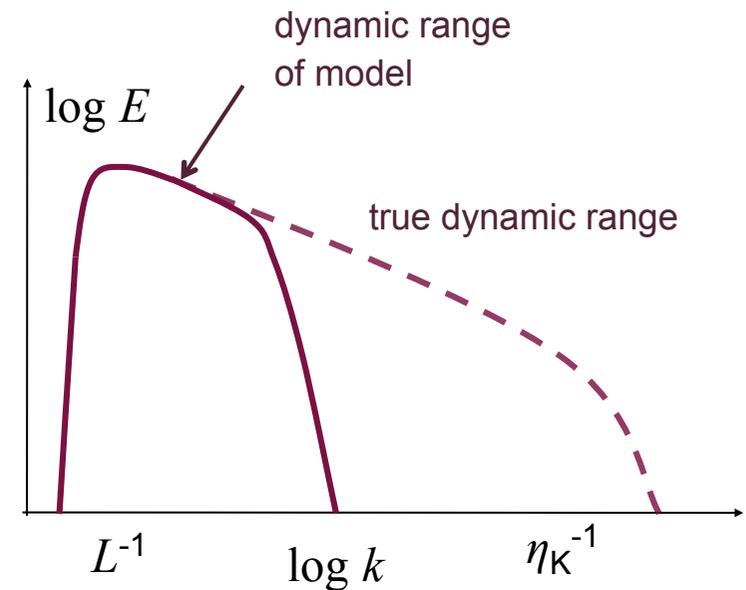
3D Viz made with VolView



Schmidt et al. (2009, A&A, 494, 127)

large eddy simulations

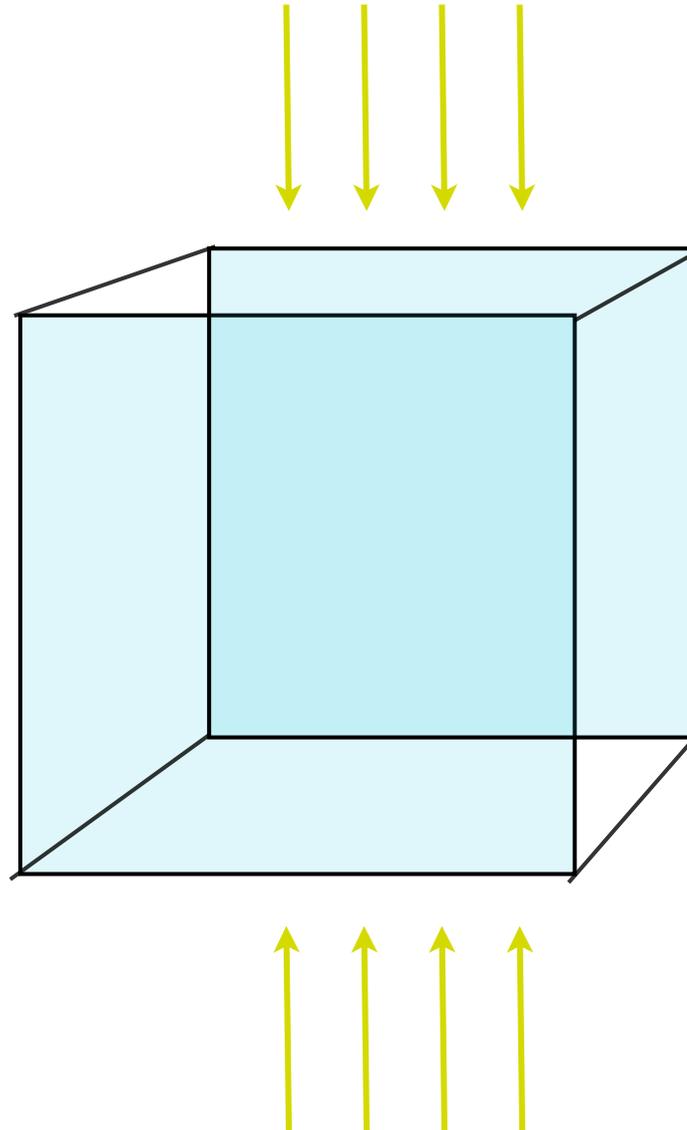
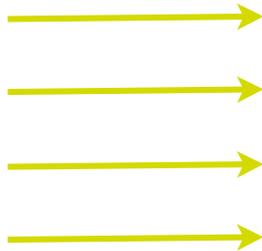
- We use **LES** to model the large-scale dynamics
- Principal problem: only large scale flow properties
 - Reynolds number: $Re = LV/\nu$ ($Re_{nature} \gg Re_{model}$)
 - dynamic range much smaller than true physical one
 - need **subgrid model** (in our case simple: only dissipation)
 - but what to do for more complex when processes on subgrid scale determine large-scale dynamics (chemical reactions, nuclear burning, etc)
 - Turbulence is “space filling” --> difficulty for AMR (don't know what criterion to use for refinement)
- How **large** a Reynolds number do we need to catch basic dynamics right?



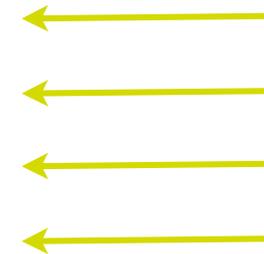


experimental set-up

external radiation either with 6-ray approximation, or with TreeCol (a new approximative scheme to calculate column densities from the gravity solver)



- AMR MHD ($B = 2 \mu\text{G}$)
- stochastic forcing (Ornstein-Uhlenbeck)
- self-gravity
- time-dependent chemistry (DVODE, standard variable-coefficient ordinary differential equation solver)
- cooling & heating processes



- gives you mathematically well defined boundary conditions
- > good for statistical studies



chemical model 0

- 32 chemical species

- 17 in instantaneous equilibrium:

H^- , H_2^+ , H_3^+ , CH^+ , CH_2^+ , OH^+ , H_2O^+ , H_3O^+ , CO^+ , HOC^+ , O^- , C^- and O_2^+

- 19 full non-equilibrium evolution

e^- , H^+ , H , H_2 , He , He^+ , C , C^+ , O , O^+ , OH , H_2O , CO ,

C_2 , O_2 , HCO^+ , CH , CH_2 and CH_3^+

- 218 reactions

- various heating and cooling processes



chemical model 1

Process

Cooling:

C fine structure lines

Atomic data – Silva & Viegas (2002)

Collisional rates (H) – Abrahamsson, Krems & Dalgarno (2007)

Collisional rates (H₂) – Schroder et al. (1991)

Collisional rates (e⁻) – Johnson et al. (1987)

Collisional rates (H⁺) – Roueff & Le Bourlot (1990)

C⁺ fine structure lines

Atomic data – Silva & Viegas (2002)

Collisional rates (H₂) – Flower & Launay (1977)

Collisional rates (H, *T* < 2000 K) – Hollenbach & McKee (1989)

Collisional rates (H, *T* > 2000 K) – Keenan et al. (1986)

Collisional rates (e⁻) – Wilson & Bell (2002)

O fine structure lines

Atomic data – Silva & Viegas (2002)

Collisional rates (H) – Abrahamsson, Krems & Dalgarno (2007)

Collisional rates (H₂) – see Glover & Jappsen (2007)

Collisional rates (e⁻) – Bell, Berrington & Thomas (1998)

Collisional rates (H⁺) – Pequignot (1990, 1996)

H₂ rovibrational lines

Le Bourlot, Pineau des Forêts & Flower (1999)

CO and H₂O rovibrational lines

Neufeld & Kaufman (1993); Neufeld, Lepp & Melnick (1995)

OH rotational lines

Pavlovski et al. (2002)

Gas-grain energy transfer

Hollenbach & McKee (1989)

Recombination on grains

Wolfire et al. (2003)

Atomic resonance lines

Sutherland & Dopita (1993)

H collisional ionization

Abel et al. (1997)

H₂ collisional dissociation

See Table B1

Compton cooling

Cen (1992)

Heating:

Photoelectric effect

Bakes & Tielens (1994); Wolfire et al. (2003)

H₂ photodissociation

Black & Dalgarno (1977)

UV pumping of H₂

Burton, Hollenbach & Tielens (1990)

H₂ formation on dust grains

Hollenbach & McKee (1989)

Cosmic ray ionization

Goldsmith & Langer (1978)



chemical model 2

Table B1. List of collisional gas-phase reactions included in our chemical model

No.	Reaction	Rate coefficient	Temperature range	
1	$H + e^- \rightarrow H^- + \gamma$	$k_1 = \text{dex}[-17.843 + 0.762 \log T + 0.1923(\log T)^2 - 0.05274(\log T)^3]$ $= \text{dex}[-16.420 + 0.1998(\log T)^2 - 5.447 \times 10^{-3}(\log T)^4 + 4.0415 \times 10^{-5}(\log T)^6]$	$T \approx 6000 \text{ K}$	
2	$H^- + H \rightarrow H_2 + e^-$	$k_2 = 1.5 \times 10^{-9}$ $= 4.0 \times 10^{-9} T^{-0.17}$	$T > 6000 \text{ K}$ $T \leq 300 \text{ K}$ $T > 300 \text{ K}$	2
3	$H + H^+ \rightarrow H_2^+ + \gamma$	$k_3 = \text{dex}[-19.38 - 1.523 \log T + 1.118(\log T)^2 - 0.1269(\log T)^3]$		3
4	$H + H_2^+ \rightarrow H_2 + H^+$	$k_4 = 6.4 \times 10^{-10}$		4
5	$H^- + H^+ \rightarrow H + H$	$k_5 = 2.4 \times 10^{-6} T^{-1/2} (1.0 + T/20000)$		5
6	$H_2^+ + e^- \rightarrow H + H$	$k_6 = 1.0 \times 10^{-8}$ $= 1.32 \times 10^{-6} T^{-0.76}$	$T \leq 617 \text{ K}$ $T > 617 \text{ K}$	6
7	$H_2 + H^+ \rightarrow H_2^+ + H$	$k_7 = [-3.3232183 \times 10^{-7} + 3.3735382 \times 10^{-7} \ln T - 1.4491368 \times 10^{-7} (\ln T)^2 + 3.4172805 \times 10^{-8} (\ln T)^3 - 4.7813720 \times 10^{-9} (\ln T)^4 + 3.9731542 \times 10^{-10} (\ln T)^5 - 1.8171411 \times 10^{-11} (\ln T)^6 + 3.5311932 \times 10^{-13} (\ln T)^7] \times \exp\left(\frac{-21237.15}{T}\right)$		7
8	$H_2 + e^- \rightarrow H + H + e^-$	$k_8 = 3.73 \times 10^{-9} T^{0.1121} \exp\left(\frac{-99430}{T}\right)$		8
9	$H_2 + H \rightarrow H + H + H$	$k_{9,l} = 6.67 \times 10^{-12} T^{1/2} \exp\left[-\left(1 + \frac{63590}{T}\right)\right]$ $k_{9,h} = 3.52 \times 10^{-9} \exp\left(-\frac{43900}{T}\right)$		9 10
		$n_{cr,H} = \text{dex}\left[3.0 - 0.416 \log\left(\frac{T}{10000}\right) - 0.327 \left\{\log\left(\frac{T}{10000}\right)\right\}^2\right]$		10
10	$H_2 + H_2 \rightarrow H_2 + H + H$	$k_{10,l} = \frac{5.996 \times 10^{-30} T^{4.1881}}{(1.0 + 6.761 \times 10^{-9} T)^{5.6881}} \exp\left(-\frac{54637.4}{T}\right)$ $k_{10,h} = 1.3 \times 10^{-9} \exp\left(-\frac{53300}{T}\right)$		11 12
		$n_{cr,H_2} = \text{dex}\left[4.845 - 1.3 \log\left(\frac{T}{10000}\right) + 1.62 \left\{\log\left(\frac{T}{10000}\right)\right\}^2\right]$		12
11	$H + e^- \rightarrow H^+ + e^- + e^-$	$k_{11} = \exp[-3.271396786 \times 10^1 + 1.35365560 \times 10^1 \ln T_0 - 5.73932875 \times 10^0 (\ln T_0)^2 + 1.56315498 \times 10^0 (\ln T_0)^3 - 2.87705600 \times 10^{-1} (\ln T_0)^4 + 3.48255977 \times 10^{-2} (\ln T_0)^5 - 2.63197617 \times 10^{-3} (\ln T_0)^6 + 1.11954395 \times 10^{-4} (\ln T_0)^7 - 2.03914985 \times 10^{-6} (\ln T_0)^8]$		13
12	$H^+ + e^- \rightarrow H + \gamma$	$k_{12,A} = 1.269 \times 10^{-13} \left(\frac{315614}{T}\right)^{1.503} \times [1.0 + \left(\frac{604625}{T}\right)^{0.470}]^{-1.923}$ $k_{12,B} = 2.753 \times 10^{-14} \left(\frac{315614}{T}\right)^{1.500} \times [1.0 + \left(\frac{115188}{T}\right)^{0.407}]^{-2.242}$	Case A Case B	14 14
13	$H^- + e^- \rightarrow H + e^- + e^-$	$k_{13} = \exp[-1.801849334 \times 10^1 + 2.36085220 \times 10^0 \ln T_0 - 2.82744300 \times 10^{-1} (\ln T_0)^2 + 1.62331664 \times 10^{-2} (\ln T_0)^3 - 3.36501203 \times 10^{-3} (\ln T_0)^4 + 1.17832978 \times 10^{-2} (\ln T_0)^5 - 1.65619470 \times 10^{-3} (\ln T_0)^6 + 1.06827520 \times 10^{-4} (\ln T_0)^7 - 2.63128581 \times 10^{-6} (\ln T_0)^8]$		13



chemical model 2

Table B1.

No. Rea

1 H +

2 H⁻

3 H +

4 H +

5 H⁻

6 H₂⁺

7 H₂

8 H₂

9 H₂

10 H₂

11 H +

12 H⁺

13 H⁻

14	$H^- + H \rightarrow H + H + e^-$	$k_{14} = 2.5634 \times 10^{-9} T_e^{-1.78186}$ $= \exp[-2.0372609 \times 10^1$ $+ 1.13944933 \times 10^0 \ln T_e$ $- 1.4210135 \times 10^{-1} (\ln T_e)^2$ $+ 8.9644554 \times 10^{-3} (\ln T_e)^3$ $- 1.377641 \times 10^{-3} (\ln T_e)^4$ $+ 2.11250 \times 10^{-4} (\ln T_e)^5$ $+ 8.6639632 \times 10^{-5} (\ln T_e)^6$ $- 2.5850097 \times 10^{-5} (\ln T_e)^7$ $+ 2.4555012 \times 10^{-6} (\ln T_e)^8$ $- 8.0683825 \times 10^{-8} (\ln T_e)^9]$	$T_e \leq 0.1 \text{ eV}$	13
15	$H^- + H^+ \rightarrow H_2^+ + e^-$	$k_{15} = 6.9 \times 10^{-9} T^{-0.35}$ $= 9.6 \times 10^{-7} T^{-0.90}$	$T_e > 0.1 \text{ eV}$ $T \leq 8000 \text{ K}$ $T > 8000 \text{ K}$	15
16	$He + e^- \rightarrow He^+ + e^- + e^-$	$k_{16} = \exp[-4.409864886 \times 10^1$ $+ 2.391596563 \times 10^1 \ln T_e$ $- 1.07532302 \times 10^1 (\ln T_e)^2$ $+ 3.05803875 \times 10^0 (\ln T_e)^3$ $- 5.6851189 \times 10^{-1} (\ln T_e)^4$ $+ 6.79539123 \times 10^{-2} (\ln T_e)^5$ $- 5.0090561 \times 10^{-3} (\ln T_e)^6$ $+ 2.06723616 \times 10^{-4} (\ln T_e)^7$ $- 3.64916141 \times 10^{-6} (\ln T_e)^8]$		13
17	$He^+ + e^- \rightarrow He + \gamma$	$k_{17,rr,A} = 10^{-11} T^{-0.5} [12.72 - 1.615 \log T$ $- 0.3162 (\log T)^2 + 0.0493 (\log T)^3]$ $k_{17,rr,B} = 10^{-11} T^{-0.5} [11.19 - 1.676 \log T$ $- 0.2852 (\log T)^2 + 0.04433 (\log T)^3]$ $k_{17,di} = 1.9 \times 10^{-3} T^{-1.5} \exp\left(-\frac{473421}{T}\right)$ $\times [1.0 + 0.3 \exp\left(-\frac{94684}{T}\right)]$	Case A Case B	16 16
18	$He^+ + H \rightarrow He + H^+$	$k_{18} = 1.25 \times 10^{-15} \left(\frac{T}{300}\right)^{0.25}$		18
19	$He + H^+ \rightarrow He^+ + H$	$k_{19} = 1.26 \times 10^{-9} T^{-0.75} \exp\left(-\frac{127500}{T}\right)$ $= 4.0 \times 10^{-37} T^{4.74}$	$T \leq 10000 \text{ K}$ $T > 10000 \text{ K}$	19
20	$C^+ + e^- \rightarrow C + \gamma$	$k_{20} = 4.67 \times 10^{-12} \left(\frac{T}{300}\right)^{-0.6}$ $= 1.23 \times 10^{-17} \left(\frac{T}{300}\right)^{2.49} \exp\left(\frac{21845.6}{T}\right)$ $= 9.62 \times 10^{-8} \left(\frac{T}{300}\right)^{-1.37} \exp\left(\frac{-115786.2}{T}\right)$	$T \leq 7950 \text{ K}$ $7950 \text{ K} < T \leq 21140 \text{ K}$ $T > 21140 \text{ K}$	20
21	$O^+ + e^- \rightarrow O + \gamma$	$k_{21} = 1.30 \times 10^{-10} T^{-0.64}$ $= 1.41 \times 10^{-10} T^{-0.66} + 7.4 \times 10^{-4} T^{-1.5}$ $\times \exp\left(-\frac{175000}{T}\right) [1.0 + 0.062 \times \exp\left(-\frac{145000}{T}\right)]$	$T \leq 400 \text{ K}$ $T > 400 \text{ K}$	21
22	$C + e^- \rightarrow C^+ + e^- + e^-$	$k_{22} = 6.85 \times 10^{-8} (0.193 + u)^{-1} u^{0.25} e^{-u}$	$u = 11.26/T_e$	22
23	$O + e^- \rightarrow O^+ + e^- + e^-$	$k_{23} = 3.59 \times 10^{-8} (0.073 + u)^{-1} u^{0.34} e^{-u}$	$u = 13.6/T_e$	22
24	$O^+ + H \rightarrow O + H^+$	$k_{24} = 4.99 \times 10^{-12} T^{0.405} + 7.54 \times 10^{-10} T^{-0.458}$		23
25	$O + H^+ \rightarrow O^+ + H$	$k_{25} = [1.08 \times 10^{-11} T^{-0.517}$ $+ 4.00 \times 10^{-10} T^{0.00669}] \exp\left(-\frac{227}{T}\right)$		24
26	$O + He^+ \rightarrow O^+ + He$	$k_{26} = 4.991 \times 10^{-15} \left(\frac{T}{10000}\right)^{0.3794} \exp\left(-\frac{T}{1121000}\right)$ $+ 2.780 \times 10^{-15} \left(\frac{T}{10000}\right)^{-0.2163} \exp\left(\frac{T}{815800}\right)$		25
27	$C + H^+ \rightarrow C^+ + H$	$k_{27} = 3.9 \times 10^{-16} T^{0.213}$		24
28	$C^+ + H \rightarrow C + H^+$	$k_{28} = 6.08 \times 10^{-14} \left(\frac{T}{10000}\right)^{1.96} \exp\left(-\frac{170000}{T}\right)$		24
29	$C + He^+ \rightarrow C^+ + He$	$k_{29} = 8.58 \times 10^{-17} T^{0.757}$ $= 3.25 \times 10^{-17} T^{0.968}$ $= 2.77 \times 10^{-19} T^{1.597}$	$T \leq 200 \text{ K}$ $200 < T \leq 2000 \text{ K}$ $T > 2000 \text{ K}$	26
30	$H_2 + He \rightarrow H + H + He$	$k_{30,l} = \text{dex}[-27.029 + 3.801 \log(T) - 29487/T]$ $k_{30,h} = \text{dex}[-2.729 - 1.75 \log(T) - 23474/T]$ $n_{cr,He} = \text{dex}[5.0792(1.0 - 1.23 \times 10^{-5}(T - 2000))]$		27 27 27
31	$OH + H \rightarrow O + H + H$	$k_{31} = 6.0 \times 10^{-9} \exp\left(-\frac{50900}{T}\right)$		28
32	$HOC^+ + H_2 \rightarrow HCO^+ + H_2$	$k_{32} = 3.8 \times 10^{-10}$		29
33	$HOC^+ + CO \rightarrow HCO^+ + CO$	$k_{33} = 4.0 \times 10^{-10}$		30
34	$C + H_2 \rightarrow CH + H$	$k_{34} = 6.64 \times 10^{-10} \exp\left(-\frac{11700}{T}\right)$		31
35	$CH + H \rightarrow C + H_2$	$k_{35} = 1.31 \times 10^{-10} \exp\left(-\frac{80}{T}\right)$		32



(Glover, Federrath, Mac Low, Klessen, 2010, MNRS, 404, 2)

Table B1.

No.	Rea
1	H+
2	H ⁻
3	H+
4	H+
5	H ⁻
6	H ₂ ⁺
7	H ₂
8	H ₂
9	H ₂
10	H ₂
11	H+
12	H ⁺
13	H ⁻

14		$H^- + H \rightarrow H + H + e^-$	$k_{14} = 2.5634 \times 10^{-9} T_e^{1.78186}$	$T_e \leq 0.1 \text{ eV}$	13
36		$CH + H_2 \rightarrow CH_2 + H$	$k_{36} = 5.46 \times 10^{-10} \exp\left(-\frac{1843}{T}\right)$		33
37		$CH + C \rightarrow C_2 + H$	$k_{37} = 6.59 \times 10^{-11}$		34
38		$CH + CO \rightarrow C_2 + H$	$k_{38} = 6.6 \times 10^{-11}$		35
39		$CH + H \rightarrow C + H_2$	$k_{39} = 7.0 \times 10^{-10} \exp\left(-\frac{11}{T}\right)$	$T \leq 2000 \text{ K}$	36
40		$CH_2 + O \rightarrow CO + H + H$	$k_{40} = 1.33 \times 10^{-10}$		38
41		$CH_2 + O \rightarrow CO + H_2$	$k_{41} = 8.0 \times 10^{-11}$		39
42		$C_2 + O \rightarrow CO + C$	$k_{42} = 5.0 \times 10^{-11} \left(\frac{T}{300}\right)^{0.5}$ $= 5.0 \times 10^{-11} \left(\frac{T}{300}\right)^{0.757}$	$T \leq 300 \text{ K}$ $T > 300 \text{ K}$	40 41
43		$O + H_2 \rightarrow OH + H$	$k_{43} = 3.14 \times 10^{-13} \left(\frac{T}{300}\right)^{2.7} \exp\left(-\frac{3150}{T}\right)$		42
44		$OH + H \rightarrow O + H_2$	$k_{44} = 6.99 \times 10^{-14} \left(\frac{T}{300}\right)^{2.8} \exp\left(-\frac{1950}{T}\right)$		43
45		$OH + H_2 \rightarrow H_2O + H$	$k_{45} = 2.05 \times 10^{-12} \left(\frac{T}{300}\right)^{1.52} \exp\left(-\frac{1736}{T}\right)$		44
46		$OH + C \rightarrow CO + H$	$k_{46} = 1.0 \times 10^{-10}$		34
47		$OH + O \rightarrow O_2 + H$	$k_{47} = 3.50 \times 10^{-11}$ $= 1.77 \times 10^{-11} \exp\left(\frac{178}{T}\right)$	$T \leq 261 \text{ K}$ $T > 261 \text{ K}$	45 33
48		$OH + OH \rightarrow H_2O + H$	$k_{48} = 1.65 \times 10^{-12} \left(\frac{T}{300}\right)^{1.14} \exp\left(-\frac{50}{T}\right)$		34
49		$H_2O + H \rightarrow H_2 + OH$	$k_{49} = 1.59 \times 10^{-11} \left(\frac{T}{300}\right)^{1.2} \exp\left(-\frac{9610}{T}\right)$		46
50		$O_2 + H \rightarrow OH + O$	$k_{50} = 2.61 \times 10^{-10} \exp\left(-\frac{8156}{T}\right)$		33
51		$O_2 + H_2 \rightarrow OH + OH$	$k_{51} = 3.16 \times 10^{-10} \exp\left(-\frac{21890}{T}\right)$		47
52		$O_2 + C \rightarrow CO + O$	$k_{52} = 4.7 \times 10^{-11} \left(\frac{T}{300}\right)^{-0.34}$ $= 2.48 \times 10^{-12} \left(\frac{T}{300}\right)^{1.54} \exp\left(\frac{613}{T}\right)$	$T \leq 295 \text{ K}$ $T > 295 \text{ K}$	34 33
53		$CO + H \rightarrow C + OH$	$k_{53} = 1.1 \times 10^{-10} \left(\frac{T}{300}\right)^{0.5} \exp\left(-\frac{77700}{T}\right)$		28
54		$H_2^+ + H_2 \rightarrow H_3^+ + H$	$k_{54} = 2.24 \times 10^{-9} \left(\frac{T}{300}\right)^{0.042} \exp\left(-\frac{46600}{T}\right)$		48
55		$H_3^+ + H \rightarrow H_2^+ + H_2$	$k_{55} = 7.7 \times 10^{-9} \exp\left(-\frac{17590}{T}\right)$		49
56		$C + H_2^+ \rightarrow CH^+ + H$	$k_{56} = 2.4 \times 10^{-9}$		28
57		$C + H_3^+ \rightarrow CH^+ + H_2$	$k_{57} = 2.0 \times 10^{-9}$		28
58		$C^+ + H_2 \rightarrow CH^+ + H$	$k_{58} = 1.0 \times 10^{-10} \exp\left(-\frac{4640}{T}\right)$		50
59		$CH^+ + H \rightarrow C^+ + H_2$	$k_{59} = 7.5 \times 10^{-10}$		51
60		$CH^+ + H_2 \rightarrow CH_2^+ + H$	$k_{60} = 1.2 \times 10^{-9}$		51
61		$CH^+ + O \rightarrow CO^+ + H$	$k_{61} = 3.5 \times 10^{-10}$		52
62		$CH_2^+ + H \rightarrow CH^+ + H_2$	$k_{62} = 1.4 \times 10^{-9}$		28
63		$CH_2^+ + H_2 \rightarrow CH_3^+ + H$	$k_{63} = 1.0 \times 10^{-9} \exp\left(-\frac{7080}{T}\right)$		28
64		$CH_2^+ + O \rightarrow HCO^+ + H$	$k_{64} = 1.6 \times 10^{-9}$		53
65		$CH_2^+ + O \rightarrow HCO^+ + H$	$k_{65} = 7.5 \times 10^{-10}$		28
66		$CH_3^+ + H \rightarrow CH_2^+ + H_2$	$k_{66} = 7.0 \times 10^{-10} \exp\left(-\frac{10560}{T}\right)$		28
67		$CH_3^+ + O \rightarrow HCO^+ + H_2$	$k_{67} = 4.0 \times 10^{-10}$		54
68		$C_2 + O^+ \rightarrow CO^+ + C$	$k_{68} = 4.8 \times 10^{-10}$		28
69		$O^+ + H_2 \rightarrow OH^+ + H$	$k_{69} = 1.7 \times 10^{-9}$		55
70		$O + H_2^+ \rightarrow OH^+ + H$	$k_{70} = 1.5 \times 10^{-9}$		28
71		$O + H_3^+ \rightarrow OH^+ + H_2$	$k_{71} = 8.4 \times 10^{-10}$		56
72		$OH + H_3^+ \rightarrow H_2O^+ + H_2$	$k_{72} = 1.3 \times 10^{-9}$		28
73		$OH + C^+ \rightarrow CO^+ + H$	$k_{73} = 7.7 \times 10^{-10}$		28
74		$OH^+ + H_2 \rightarrow H_2O^+ + H$	$k_{74} = 1.01 \times 10^{-9}$		57
75		$H_2O^+ + H_2 \rightarrow H_3O^+ + H$	$k_{75} = 6.4 \times 10^{-10}$		58
76		$H_2O + H_3^+ \rightarrow H_3O^+ + H_2$	$k_{76} = 5.9 \times 10^{-9}$		59
77		$H_2O + C^+ \rightarrow HCO^+ + H$	$k_{77} = 9.0 \times 10^{-10}$		60
78		$H_2O + C^+ \rightarrow HOC^+ + H$	$k_{78} = 1.8 \times 10^{-9}$		60
79		$H_3O^+ + C \rightarrow HCO^+ + H_2$	$k_{79} = 1.0 \times 10^{-11}$		28
80		$O_2 + C^+ \rightarrow CO^+ + O$	$k_{80} = 3.8 \times 10^{-10}$		53
81		$O_2 + C^+ \rightarrow CO + O^+$	$k_{81} = 6.2 \times 10^{-10}$		53
82		$O_2 + CH_2^+ \rightarrow HCO^+ + OH$	$k_{82} = 9.1 \times 10^{-10}$		53
83		$O_2^+ + C \rightarrow CO^+ + O$	$k_{83} = 5.2 \times 10^{-11}$		28
84		$CO + H_3^+ \rightarrow HOC^+ + H_2$	$k_{84} = 2.7 \times 10^{-11}$		61
85		$CO + H_3^+ \rightarrow HCO^+ + H_2$	$k_{85} = 1.7 \times 10^{-9}$		61
86		$HCO^+ + C \rightarrow CO + CH^+$	$k_{86} = 1.1 \times 10^{-9}$		28
87		$HCO^+ + H_2O \rightarrow CO + H_3O^+$	$k_{87} = 2.5 \times 10^{-9}$		62

chemical model 2





(Glover, Federrath, Mac Low, Klessen, 2010, MNRS, 404, 2)

Table B1.

No.	Rea				
1	H ⁺	36	CH + H ₂	88	H ₂ + He ⁺ → H + H + e ⁻
2	H ⁻	37	CH + C	89	H ₂ + He ⁺ → He + H + H ⁺
3	H ⁺	38	CH + C ⁺	90	CH + H ⁺ → CH ⁺ + H
4	H ⁺	39	CH + C ⁺	91	CH ₂ + H ⁺ → CH ₂ ⁺ + H
5	H ⁻	40	CH ₂ + O	92	CH ₂ + H ⁺ → CH ₂ ⁺ + H
6	H ₂ ⁺	41	CH ₂ + O	93	C ₂ + e ⁻ → C + C ⁻
7	H ₂	42	C ₂ + O →	94	OH + H ⁺ → OH ⁺ + H
8	H ₂	15	H ⁻	95	OH + He ⁺ → O ⁺ + He + H
9	H ₂	16	He ⁻	96	H ₂ O + H ⁺ → H ₂ O ⁺ + H
10	H ₂	43	O + H ₂ →	97	H ₂ O + He ⁺ → OH + He + H ⁺
11	H ⁺	44	OH + H →	98	H ₂ O + He ⁺ → OH ⁺ + He + H
12	H ⁺	45	OH + H ₂	99	H ₂ O + He ⁺ → H ₂ O ⁺ + He
13	H ⁻	46	OH + C →	100	O ₂ + H ⁺ → O ₂ ⁺ + H
		47	OH + O →	101	O ₂ + He ⁺ → O ₂ ⁺ + He
		48	OH + OH	102	O ₂ + He ⁺ → O ⁺ + O + He
		49	H ₂ O + H →	103	O ₂ ⁺ + C → O ₂ + C ⁺
		50	O ₂ + H →	104	CO + He ⁺ → C ⁺ + O + He
		51	O ₂ + H ₂ →	105	CO + He ⁺ → C + O ⁺ + He
		52	O ₂ + C →	106	CO ⁺ + H → CO + H ⁺
		53	CO + H →	107	C ⁻ + H ⁺ → C + H
		54	H ₂ ⁺ + H ₂	108	O ⁻ + H ⁺ → O + H
		55	H ₃ ⁺ + H →	109	He ⁺ + H ⁻ → He + H
		56	C + H ₂ ⁺ →	110	H ₃ ⁺ + e ⁻ → H ₂ + H
		57	C + H ₃ ⁺ →	111	H ₃ ⁺ + e ⁻ → H + H + H
		58	C ⁺ + H ₂	112	CH ⁺ + e ⁻ → C + H
		59	CH ⁺ + H	113	CH ₂ ⁺ + e ⁻ → CH + H
		60	CH ⁺ + H ₂	114	CH ₂ ⁺ + e ⁻ → C + H + H
		61	CH ⁺ + O	115	CH ₂ ⁺ + e ⁻ → C + H ₂
		62	CH ₂ + H ⁺	116	CH ₃ ⁺ + e ⁻ → CH ₂ + H
		63	CH ₂ ⁺ + H	117	CH ₃ ⁺ + e ⁻ → CH + H ₂
		64	CH ₂ ⁺ + H ₂	118	CH ₃ ⁺ + e ⁻ → CH + H + H
		65	CH ₂ ⁺ + O	119	OH ⁺ + e ⁻ → O + H
		66	CH ₃ ⁺ + H	120	H ₂ O ⁺ + e ⁻ → O + H + H
		67	CH ₃ ⁺ + O	121	H ₂ O ⁺ + e ⁻ → O + H ₂
		68	C ₂ + O ⁺	122	H ₂ O ⁺ + e ⁻ → OH + H
		69	O ⁺ + H ₂	123	H ₃ O ⁺ + e ⁻ → H + H ₂ O
		70	O + H ₂ ⁺	124	H ₃ O ⁺ + e ⁻ → OH + H ₂
		71	O + H ₃ ⁺	125	H ₃ O ⁺ + e ⁻ → OH + H + H
		72	OH + H ₃ ⁺	126	H ₃ O ⁺ + e ⁻ → O + H + H ₂
		73	OH + C ⁺	127	O ₂ ⁺ + e ⁻ → O + O
		74	OH ⁺ + H ₂	128	CO ⁺ + e ⁻ → C + O
		75	H ₂ O ⁺ + H	129	HCO ⁺ + e ⁻ → CO + H
		76	H ₂ O + H ₃ ⁺	130	HCO ⁺ + e ⁻ → OH + C
		77	H ₂ O + C ⁺	131	HOC ⁺ + e ⁻ → CO + H
		78	H ₂ O + C ⁺	132	H ⁻ + C → CH + e ⁻
		79	H ₃ O ⁺ + C	133	H ⁻ + O → OH + e ⁻
		80	O ₂ + C ⁺	134	H ⁻ + OH → H ₂ O + e ⁻
		81	O ₂ + C ⁺	135	C ⁻ + H → CH + e ⁻
		82	O ₂ + CH ₂	136	C ⁻ + H ₂ → CH ₂ + e ⁻
		83	O ₂ ⁺ + C →	137	C ⁻ + O → CO + e ⁻
		84	CO + H ₃ ⁺	138	O ⁻ + H → OH + e ⁻
		85	CO + H ₃ ⁺	139	O ⁻ + H ₂ → H ₂ O + e ⁻
		86	HCO ⁺ + C	140	O ⁻ + C → CO + e ⁻
		87	HCO ⁺ + H ₂ O → CO + H ₃ O ⁺		
				88	k ₈₈ = 7.2 × 10 ⁻¹⁵
				89	k ₈₉ = 3.7 × 10 ⁻¹⁴ exp(35/T)
				90	k ₉₀ = 1.9 × 10 ⁻⁹
				91	k ₉₁ = 1.4 × 10 ⁻⁹
				92	k ₉₂ = 1.5 × 10 ⁻⁹
				93	k ₉₃ = 6.1 × 10 ⁻⁹
				94	k ₉₄ = 2.1 × 10 ⁻⁹
				95	k ₉₅ = 1.1 × 10 ⁻⁹
				96	k ₉₆ = 6.9 × 10 ⁻⁹
				97	k ₉₇ = 2.04 × 10 ⁻¹⁰
				98	k ₉₈ = 2.86 × 10 ⁻¹⁰
				99	k ₉₉ = 6.05 × 10 ⁻¹¹
				100	k ₁₀₀ = 2.0 × 10 ⁻⁹
				101	k ₁₀₁ = 3.3 × 10 ⁻¹¹
				102	k ₁₀₂ = 1.1 × 10 ⁻⁹
				103	k ₁₀₃ = 5.2 × 10 ⁻¹¹
				104	k ₁₀₄ = 1.4 × 10 ⁻⁹ (T/300) ^{-0.5}
				105	k ₁₀₅ = 1.4 × 10 ⁻¹⁶ (T/300) ^{-0.5}
				106	k ₁₀₆ = 7.5 × 10 ⁻¹⁰
				107	k ₁₀₇ = 2.3 × 10 ⁻⁷ (T/300) ^{-0.5}
				108	k ₁₀₈ = 2.3 × 10 ⁻⁷ (T/300) ^{-0.5}
				109	k ₁₀₉ = 2.32 × 10 ⁻⁷ (T/300) ^{-0.52} exp(T/22400)
				110	k ₁₁₀ = 2.34 × 10 ⁻⁸ (T/300) ^{-0.52}
				111	k ₁₁₁ = 4.36 × 10 ⁻⁸ (T/300) ^{-0.52}
				112	k ₁₁₂ = 7.0 × 10 ⁻⁸ (T/300) ^{-0.5}
				113	k ₁₁₃ = 1.6 × 10 ⁻⁷ (T/300) ^{-0.6}
				114	k ₁₁₄ = 4.03 × 10 ⁻⁷ (T/300) ^{-0.6}
				115	k ₁₁₅ = 7.68 × 10 ⁻⁸ (T/300) ^{-0.6}
				116	k ₁₁₆ = 7.75 × 10 ⁻⁸ (T/300) ^{-0.5}
				117	k ₁₁₇ = 1.95 × 10 ⁻⁷ (T/300) ^{-0.5}
				118	k ₁₁₈ = 2.0 × 10 ⁻⁷ (T/300) ^{-0.4}
				119	k ₁₁₉ = 6.3 × 10 ⁻⁹ (T/300) ^{-0.48}
				120	k ₁₂₀ = 3.05 × 10 ⁻⁷ (T/300) ^{-0.5}
				121	k ₁₂₁ = 3.9 × 10 ⁻⁸ (T/300) ^{-0.5}
				122	k ₁₂₂ = 8.6 × 10 ⁻⁸ (T/300) ^{-0.5}
				123	k ₁₂₃ = 1.08 × 10 ⁻⁷ (T/300) ^{-0.5}
				124	k ₁₂₄ = 6.02 × 10 ⁻⁸ (T/300) ^{-0.5}
				125	k ₁₂₅ = 2.58 × 10 ⁻⁷ (T/300) ^{-0.5}
				126	k ₁₂₆ = 5.6 × 10 ⁻⁹ (T/300) ^{-0.5}
				127	k ₁₂₇ = 1.95 × 10 ⁻⁷ (T/300) ^{-0.7}
				128	k ₁₂₈ = 2.75 × 10 ⁻⁷ (T/300) ^{-0.55}
				129	k ₁₂₉ = 2.76 × 10 ⁻⁷ (T/300) ^{-0.64}
				130	k ₁₃₀ = 2.4 × 10 ⁻⁸ (T/300) ^{-0.64}
				131	k ₁₃₁ = 1.1 × 10 ⁻⁷ (T/300) ^{-1.0}
				132	k ₁₃₂ = 1.0 × 10 ⁻⁹
				133	k ₁₃₃ = 1.0 × 10 ⁻⁹
				134	k ₁₃₄ = 1.0 × 10 ⁻¹⁰
				135	k ₁₃₅ = 5.0 × 10 ⁻¹⁰
				136	k ₁₃₆ = 1.0 × 10 ⁻¹³
				137	k ₁₃₇ = 5.0 × 10 ⁻¹⁰
				138	k ₁₃₈ = 5.0 × 10 ⁻¹⁰
				139	k ₁₃₉ = 7.0 × 10 ⁻¹⁰
				140	k ₁₄₀ = 5.0 × 10 ⁻¹⁰
				87	k ₈₇ = 2.5 × 10 ⁻⁹

chemical model 2



(Glover, Federrath, Mac Low, Klessen, 2010, MNRS, 404, 2)

Table B1.

No.	Rea					
1	H ⁺	36	CH + H ₂	88	H ₂ + He ⁺ → He + H ₂ ⁺	63
		37	CH + C	89	H ₂ + He ⁺ → He + H + H ⁺	63
		38	CH + C ⁺	90	CH + H ⁺ → CH ⁺ + H	28
				91	CH ₂ + H ⁺ → CH ₂ ⁺ + H	28
				92	CH ₂ + H ⁺ → CH ₂ ⁺ + H	28
				93	C + e ⁻ → C ⁻ + γ	28
		39	C + H	94	OH + H ⁺ → OH ⁺ + H	28
		40	CH ₂ + O	95	OH + He ⁺ → O ⁺ + He + H	28
		41	CH ₂ + O ⁺	96	H ₂ O + H ⁺ → H ₂ O ⁺ + H	64
		42	C ₂ + O →	97	H ₂ O + He ⁺ → OH + He + H ⁺	65
				98		65
2	H ⁻	15	H ⁻	99	142 C + e ⁻ → C ⁻ + γ	81
		16	He ⁻	100	143 C + H → CH + γ	82
3	H ⁺			101	144 C + H ₂ → CH ₂ + γ	82
				102	145 C + C → C ₂ + γ	83
4	H ⁺			103	146 C + O → CO + γ	84
5	H ⁺				$k_{145} = 4.36 \times 10^{-18} \left(\frac{T}{300}\right)^{0.35} \exp\left(-\frac{161.3}{T}\right)$	$T \leq 300 \text{ K}$
6	H ₂ ⁺				$k_{146} = 2.1 \times 10^{-19}$	$T > 300 \text{ K}$
					$= 3.09 \times 10^{-17} \left(\frac{T}{300}\right)^{0.33} \exp\left(-\frac{1629}{T}\right)$	85
7	H ₂			104	147 C ⁺ + H → CH ⁺ + γ	86
				105	148 C ⁺ + H ₂ → CH ₂ ⁺ + γ	87
				106	149 C ⁺ + O → CO ⁺ + γ	84
					$k_{147} = 4.46 \times 10^{-16} T^{-0.5} \exp\left(-\frac{4.93}{T^{2/3}}\right)$	86
					$k_{148} = 4.0 \times 10^{-16} \left(\frac{T}{300}\right)^{-0.2}$	87
					$k_{149} = 2.5 \times 10^{-18}$	$T \leq 300 \text{ K}$
					$= 3.14 \times 10^{-18} \left(\frac{T}{300}\right)^{-0.15} \exp\left(\frac{68}{T}\right)$	$T > 300 \text{ K}$
				107	150 O + e ⁻ → O ⁻ + γ	28
				108	151 O + H → OH + γ	28
				109	152 O + O → O ₂ + γ	82
					$k_{150} = 1.5 \times 10^{-15}$	28
					$k_{151} = 9.9 \times 10^{-19} \left(\frac{T}{300}\right)^{-0.38}$	28
					$k_{152} = 4.9 \times 10^{-20} \left(\frac{T}{300}\right)^{1.58}$	82
					$k_{153} = 5.26 \times 10^{-18} \left(\frac{T}{300}\right)^{-5.22} \exp\left(-\frac{90}{T}\right)$	88
8	H ₂	18	He ⁺	110	153 OH + H → H ₂ O + γ	89
9	H ₂	19	He ⁺	111	154 H + H + H → H ₂ + H	90
					$k_{154} = 1.32 \times 10^{-32} \left(\frac{T}{300}\right)^{-0.38}$	$T \leq 300 \text{ K}$
					$= 1.32 \times 10^{-32} \left(\frac{T}{300}\right)^{-1.0}$	$T > 300 \text{ K}$
				112	155 H + H + H ₂ → H ₂ + H ₂	91
				113	156 H + H + He → H ₂ + He	92
					$k_{155} = 2.8 \times 10^{-31} T^{-0.6}$	91
					$k_{156} = 6.9 \times 10^{-32} T^{-0.4}$	92
				114	157 C + C + M → C ₂ + M	93
					$k_{157} = 5.99 \times 10^{-33} \left(\frac{T}{5000}\right)^{-1.6}$	$T \leq 5000 \text{ K}$
					$= 5.99 \times 10^{-33} \left(\frac{T}{5000}\right)^{-0.64} \exp\left(\frac{5255}{T}\right)$	$T > 5000 \text{ K}$
10	H ₂	20	C ⁺	115	158 C + O + M → CO + M	35
					$k_{158} = 6.16 \times 10^{-29} \left(\frac{T}{300}\right)^{-3.08}$	$T \leq 2000 \text{ K}$
					$= 2.14 \times 10^{-29} \left(\frac{T}{300}\right)^{-3.08} \exp\left(\frac{2114}{T}\right)$	$T > 2000 \text{ K}$
				116	159 C ⁺ + O + M → CO ⁺ + M	67
				117	160 C + O ⁺ + M → CO ⁺ + M	67
				118	161 O + H + M → OH + M	43
				119	162 OH + H + M → H ₂ O + M	35
				120	163 O + O + M → O ₂ + M	37
				121	164 O + CH → HCO ⁺ + e ⁻	95
				122	165 H + H(s) → H ₂	95
					$k_{159} = 100 \times k_{210}$	67
					$k_{160} = 100 \times k_{210}$	67
					$k_{161} = 4.33 \times 10^{-32} \left(\frac{T}{300}\right)^{-1.0}$	43
					$k_{162} = 2.56 \times 10^{-31} \left(\frac{T}{300}\right)^{-2.0}$	35
					$k_{163} = 9.2 \times 10^{-34} \left(\frac{T}{300}\right)^{-1.0}$	37
					$k_{164} = 2.0 \times 10^{-11} \left(\frac{T}{300}\right)^{0.44}$	95
					$k_{165} = 3.0 \times 10^{-18} T^{0.5} f_A [1.0 + 0.04(T + T_d)^{0.5}]^{-1}$	96
					$+ 0.002 T + 8 \times 10^{-6} T^2]^{-1}$	96
				123	129 HCO ⁺ + e ⁻ → CO + H	79
				124	130 HCO ⁺ + e ⁻ → OH + C	79
				125	131 HOC ⁺ + e ⁻ → CO + H	28
				126	132 H ⁻ + C → CH + e ⁻	28
				127	133 H ⁻ + O → OH + e ⁻	28
				128	134 H ⁻ + OH → H ₂ O + e ⁻	28
				129	135 C ⁻ + H → CH + e ⁻	28
				130	136 C ⁻ + H ₂ → CH ₂ + e ⁻	28
				131	137 C ⁻ + O → CO + e ⁻	28
				132	138 O ⁻ + H → OH + e ⁻	28
				133	139 O ⁻ + H ₂ → H ₂ O + e ⁻	28
				134	140 O ⁻ + C → CO + e ⁻	28
				135	141 HCO ⁺ + H ₂ O → CO + H ₃ O ⁺	62
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				258		62



chemical model 2

Table B1.

No.	Reaction
1	H + ...

14	H ⁻ + H → H + H + e ⁻	88	H ₂ + He ⁺ → He + H ₂ ⁺	$k_{88} = 7.2 \times 10^{-15}$	63
36	CH + H ₂	89	H ₂ + He ⁺ → He + H + H ⁺	$k_{89} = 3.7 \times 10^{-14} \exp\left(\frac{35}{T}\right)$	63
37	CH + C	90	CH + H ⁺ → CH ⁺ + H	$k_{90} = 1.9 \times 10^{-9}$	28
38	CH + C ⁺	91	CH ₂ + H ⁺ → CH ₂ ⁺ + H	$k_{91} = 1.4 \times 10^{-9}$	28
		92	CH ₂ + H ⁺ → CH + H ₂	$k_{92} = 1.5 \times 10^{-9}$	28
39	C + ...	93	C ₂ + e ⁻ → C + C ⁻	$k_{93} = 1.6 \times 10^{-15}$	28
40	CH ₂ + O	94	OH + H ⁺ → OH ⁺ + H	$k_{94} = 2.1 \times 10^{-9}$	28
41	CH ₂ + O ⁻	95	OH + He ⁺ → O ⁺ + He + H	$k_{95} = 1.1 \times 10^{-9}$	28
42	C ₂ + O →	96	H ₂ O + H ⁺ → H ₂ O ⁺ + H	$k_{96} = 6.9 \times 10^{-9}$	64
		97	H ₂ O + He ⁺ → OH + He + H ⁺	$k_{97} = 2.04 \times 10^{-10}$	65
		98	H ₂ O + H ⁺ → OH + H ₂	$k_{98} = 1.0 \times 10^{-10}$	65

Table B2. List of photochemical reactions included in our chemical model

No.	Reaction	Optically thin rate (s ⁻¹)	γ	Ref.	Rate	Temp. Range
166	H ⁻ + γ → H + e ⁻	$R_{166} = 7.1 \times 10^{-7}$	0.5	1	25×10^{-15}	
167	H ₂ ⁺ + γ → H + H ⁺	$R_{167} = 1.1 \times 10^{-9}$	1.9	2	0×10^{-17}	
168	H ₂ + γ → H + H	$R_{168} = 5.6 \times 10^{-11}$	See §2.2	3	0×10^{-17}	
169	H ₃ ⁺ + γ → H ₂ + H ⁺	$R_{169} = 4.9 \times 10^{-13}$	1.8	4	$36 \times 10^{-18} \left(\frac{T}{300}\right)^{0.35} \exp\left(-\frac{161.3}{T}\right)$	$T \leq 300$ K
170	H ₃ ⁺ + γ → H ₂ ⁺ + H	$R_{170} = 4.9 \times 10^{-13}$	2.3	4	$0.9 \times 10^{-17} \left(\frac{T}{300}\right)^{0.33} \exp\left(-\frac{1629}{T}\right)$	$T > 300$ K
171	C + γ → C ⁺ + e ⁻	$R_{171} = 2.1 \times 10^{-10}$	2.0	5	$46 \times 10^{-16} T^{-0.5} \exp\left(-\frac{4.93}{T^{2/3}}\right)$	
172	C ⁻ + γ →				$0 \times 10^{-16} \left(\frac{T}{300}\right)^{-0.2}$	$T \leq 300$ K
173	CH + γ →				5×10^{-18}	
174	CH + γ →				$14 \times 10^{-18} \left(\frac{T}{300}\right)^{-0.15} \exp\left(\frac{68}{T}\right)$	$T > 300$ K
175	CH ⁺ + γ →				1×10^{-19}	
176	CH ₂ + γ →					
177	CH ₂ + γ →					
178	CH ₂ ⁺ + γ →					
179	CH ₃ ⁺ + γ →					
180	CH ₃ ⁺ + γ →					
181	C ₂ + γ →					
182	O ⁻ + γ →					
183	OH + γ →					
184	OH + γ →					
185	OH ⁺ + γ →					
186	H ₂ O + γ →					
187	H ₂ O + γ →					
188	H ₂ O ⁺ + γ →					
189	H ₂ O ⁺ + γ →					
190	H ₂ O ⁺ + γ →					
191	H ₂ O ⁺ + γ →					
192	H ₃ O ⁺ + γ →					
193	H ₃ O ⁺ + γ →					
194	H ₃ O ⁺ + γ →					
195	H ₃ O ⁺ + γ →					
196	O ₂ + γ →					
197	O ₂ + γ → O + O	$R_{197} = 7.0 \times 10^{-10}$	1.8	7	$\times 10^{-10}$	
198	CO + γ → C + O	$R_{198} = 2.0 \times 10^{-10}$	See §2.2	13	$\times 10^{-10}$	

Table B3. List of reactions included in our chemical model that involve cosmic rays or cosmic-ray induced UV emission

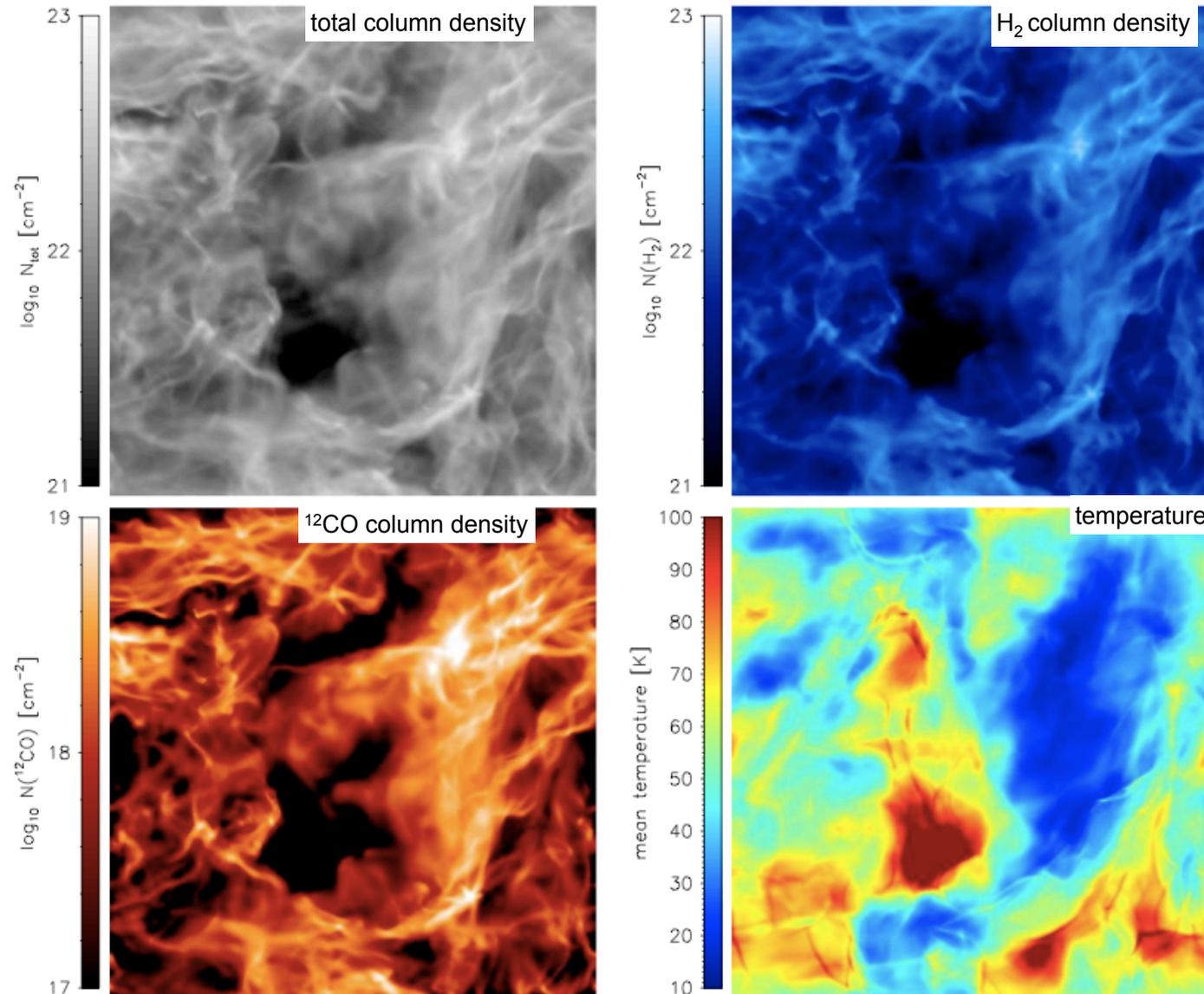
No.	Reaction	Rate (s ⁻¹ ζ_{H}^{-1})	Ref.
199	H + c.r. → H ⁺ + e ⁻	$R_{199} = 1.0$	—
200	He + c.r. → He ⁺ + e ⁻	$R_{200} = 1.1$	1
201	H ₂ + c.r. → H ⁺ + H + e ⁻	$R_{201} = 0.037$	1
202	H ₂ + c.r. → H + H	$R_{202} = 0.22$	1
203	H ₂ + c.r. → H ⁺ + H ⁻	$R_{203} = 6.5 \times 10^{-4}$	1
204	H ₂ + c.r. → H ₂ ⁺ + e ⁻	$R_{204} = 2.0$	1
205	C + c.r. → C ⁺ + e ⁻	$R_{205} = 3.8$	1
206	O + c.r. → O ⁺ + e ⁻	$R_{206} = 5.7$	1
207	CO + c.r. → CO ⁺ + e ⁻	$R_{207} = 6.5$	1
208	C + $\gamma_{\text{c.r.}}$ → C ⁺ + e ⁻	$R_{208} = 2800$	2
209	CH + $\gamma_{\text{c.r.}}$ → C + H	$R_{209} = 4000$	3
210	CH ⁺ + $\gamma_{\text{c.r.}}$ → C ⁺ + H	$R_{210} = 960$	3
211	CH ₂ + $\gamma_{\text{c.r.}}$ → CH ₂ ⁺ + e ⁻	$R_{211} = 2700$	1
212	CH ₂ + $\gamma_{\text{c.r.}}$ → CH + H	$R_{212} = 2700$	1
213	C ₂ + $\gamma_{\text{c.r.}}$ → C + C	$R_{213} = 1300$	3
214	OH + $\gamma_{\text{c.r.}}$ → O + H	$R_{214} = 2800$	3
215	H ₂ O + $\gamma_{\text{c.r.}}$ → OH + H	$R_{215} = 5300$	3
216	O ₂ + $\gamma_{\text{c.r.}}$ → O + O	$R_{216} = 4100$	3
217	O ₂ + $\gamma_{\text{c.r.}}$ → O ₂ ⁺ + e ⁻	$R_{217} = 640$	3
218	CO + $\gamma_{\text{c.r.}}$ → C + O	$R_{218} = 0.21T^{1/2} x_{\text{H}_2} x_{\text{CO}}^{-1/2}$	4

86	HCO ⁺ + C	140	O ⁻ + C → CO + e ⁻	$k_{140} = 5.0 \times 10^{-10}$	28
87	HCO ⁺ + H ₂ O → CO + H ₃ O ⁺	$k_{87} = 2.5 \times 10^{-9}$			28

(Glover, Federrath, Mac Low, Klessen, 2010, MNRAS, 404, 2)



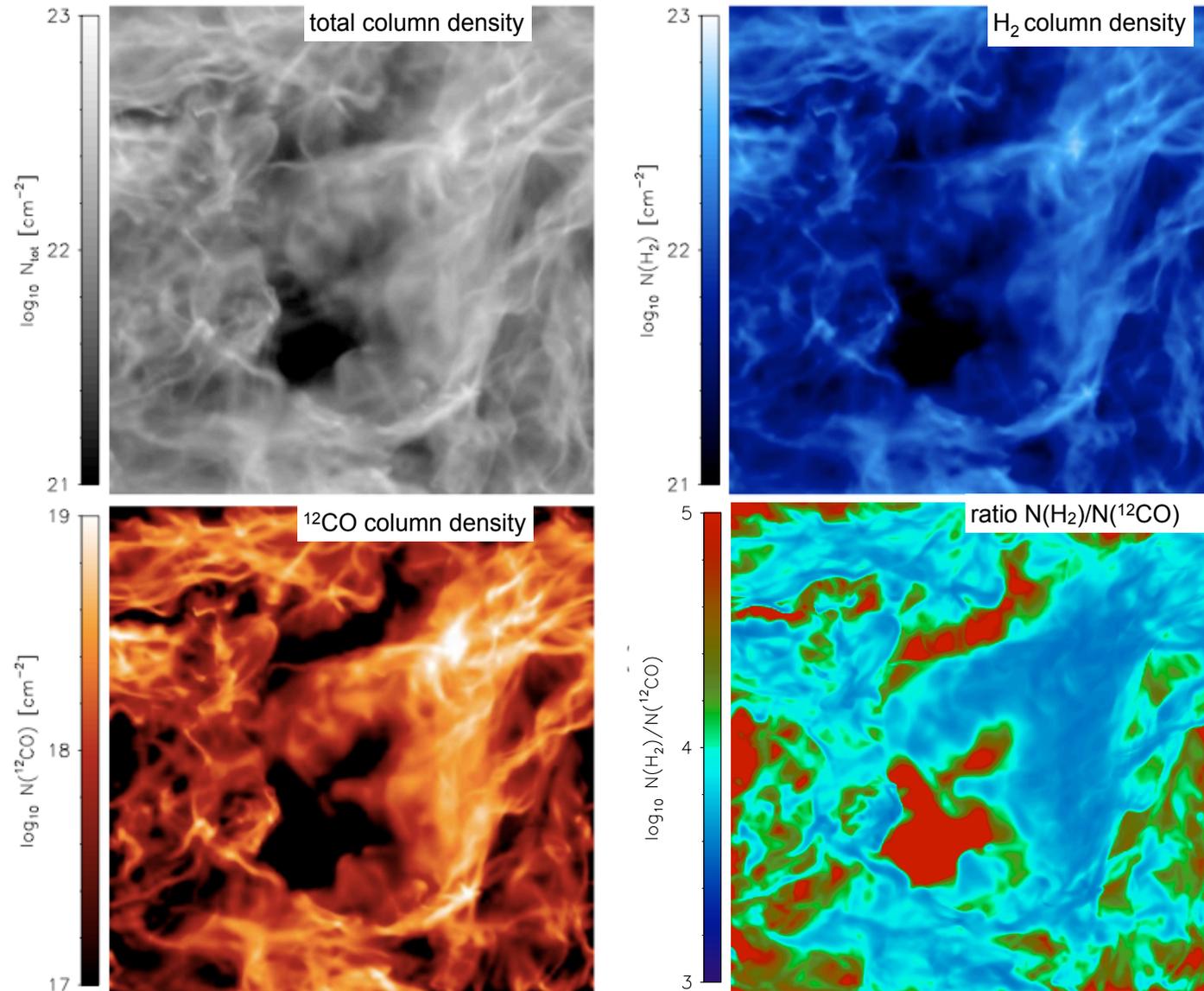
effects of chemistry 1



(Glover, Federrath, Mac Low, Klessen, 2010)



effects of chemistry 2



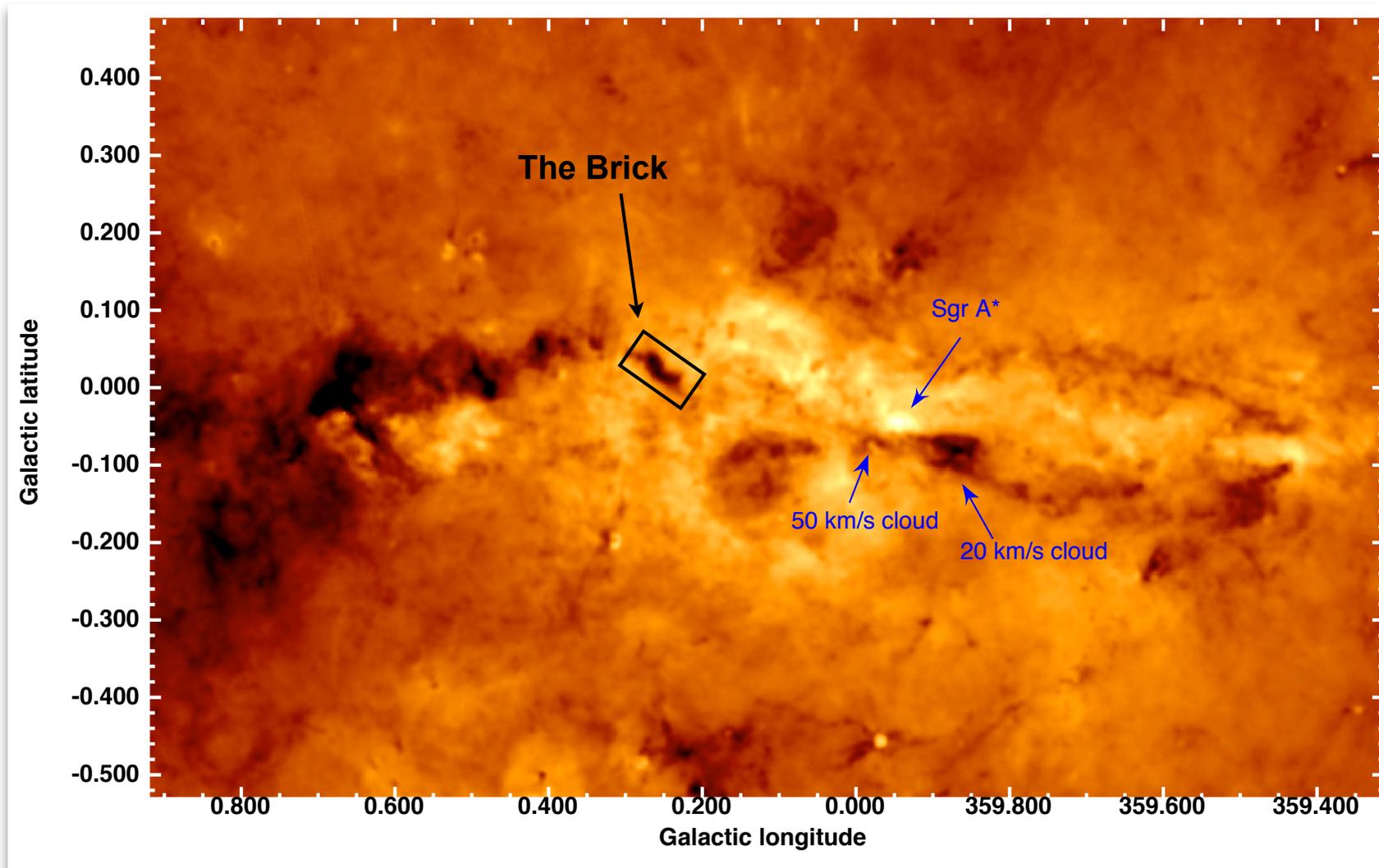
(Glover, Federrath, Mac Low, Klessen, 2010)

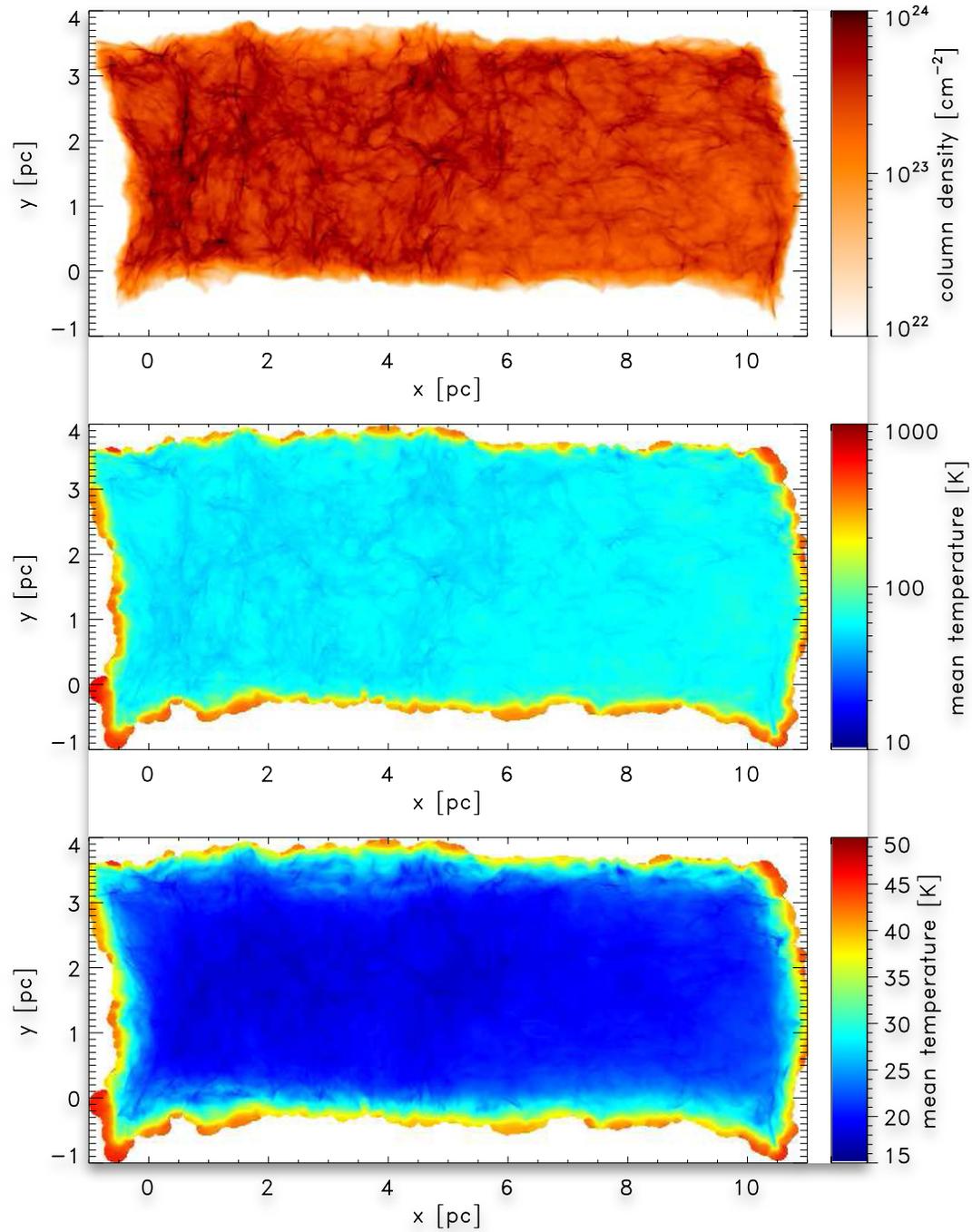


Molinari et al. (2012), image HERSCHEL: ESA/NASA/JPL-Caltech



Molinari et al. (2012), image HERSCHEL: ESA/NASA/JPL-Caltech





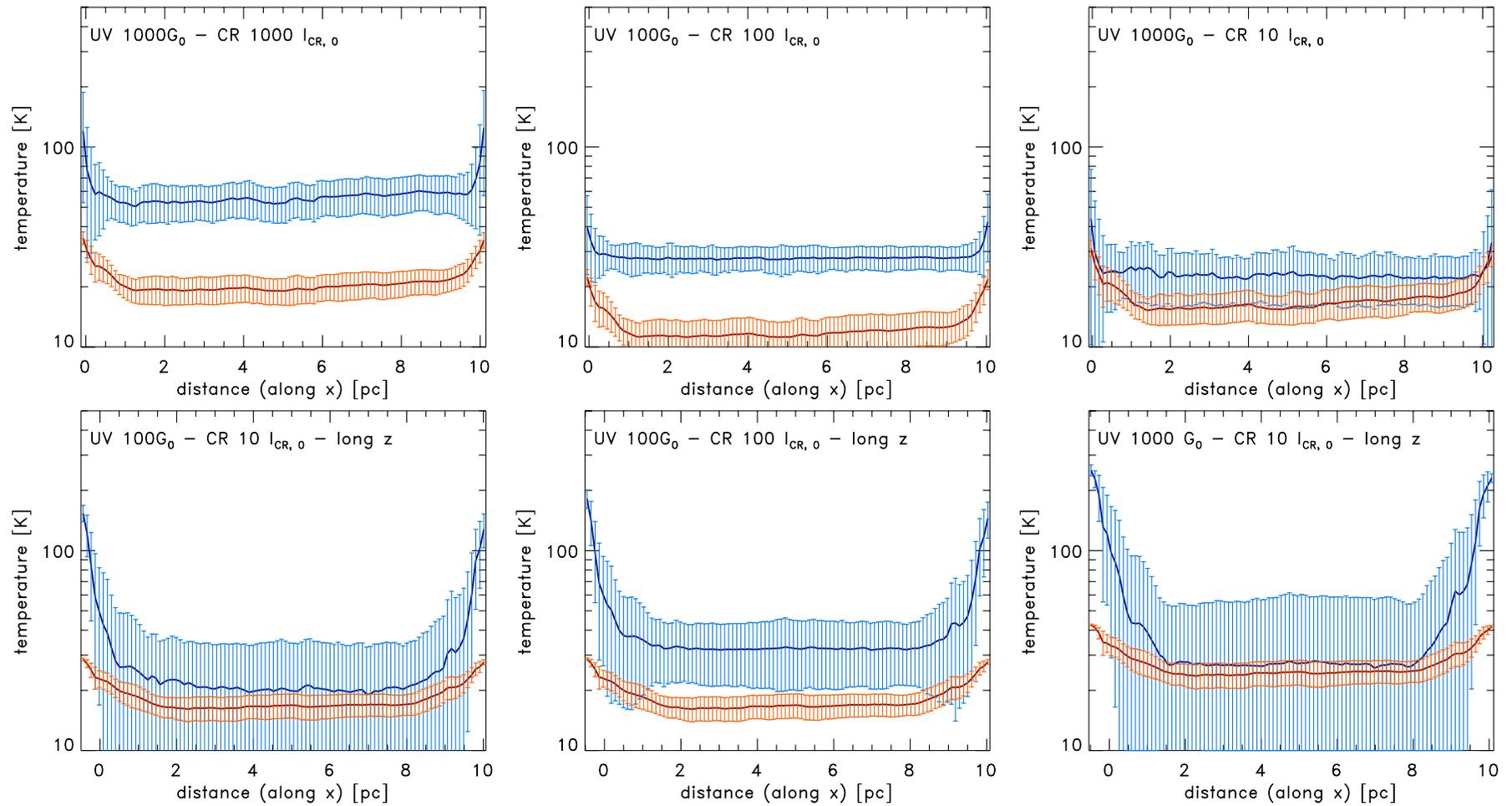


Figure 2. Gas (blue) and dust (red) temperatures as a function of x . The top row contains the clouds that have the fiducial setup (x is the longest axis), while the bottom row contains the low-density clouds (those with z as the longest axis). The lines denote the mass-averaged temperature along the line of sight. The vertical bars denote the 1σ spread.

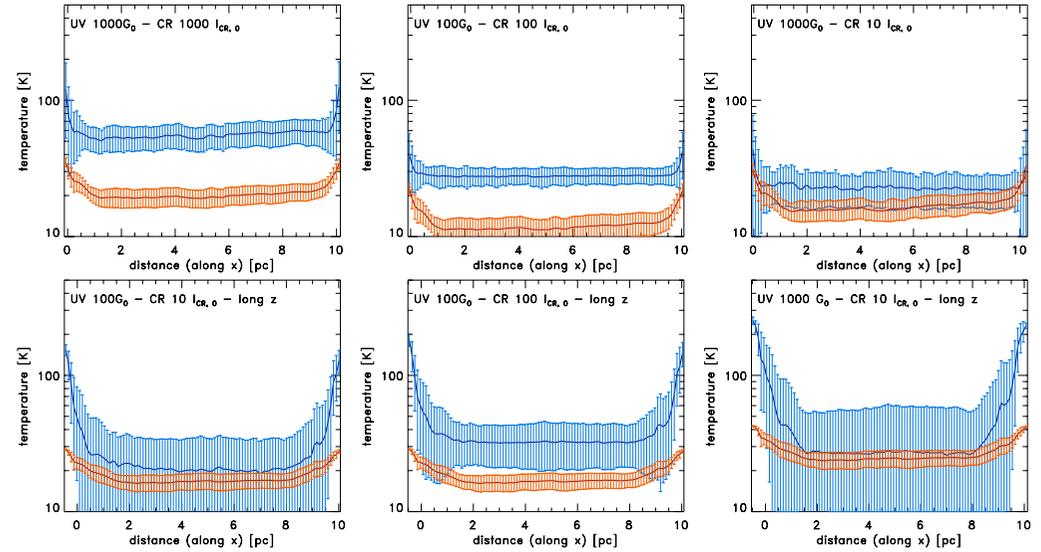
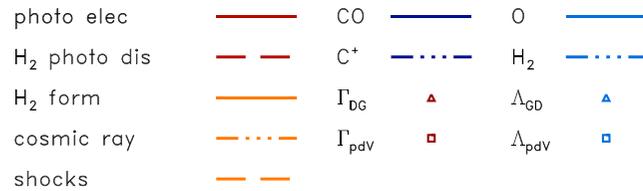
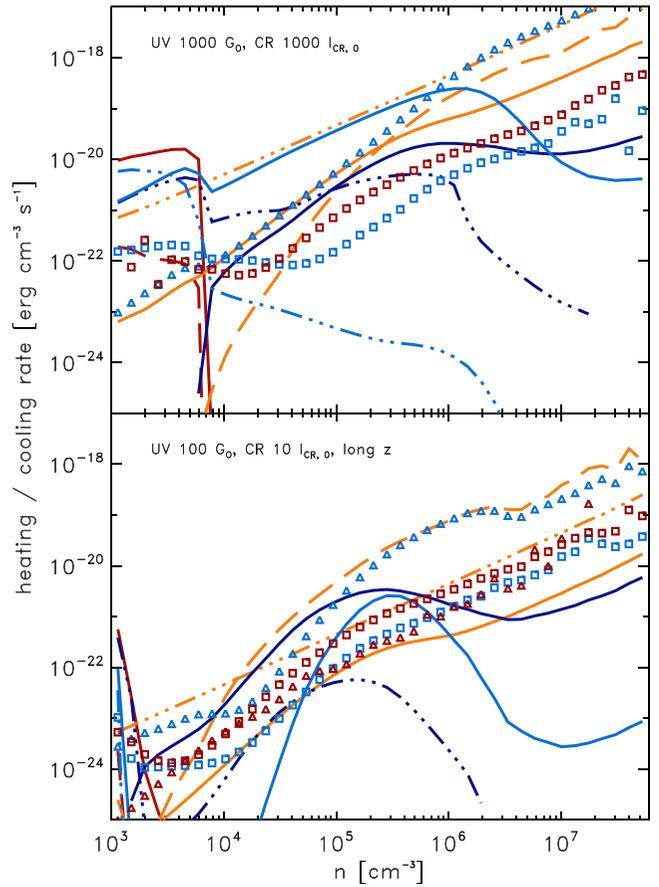
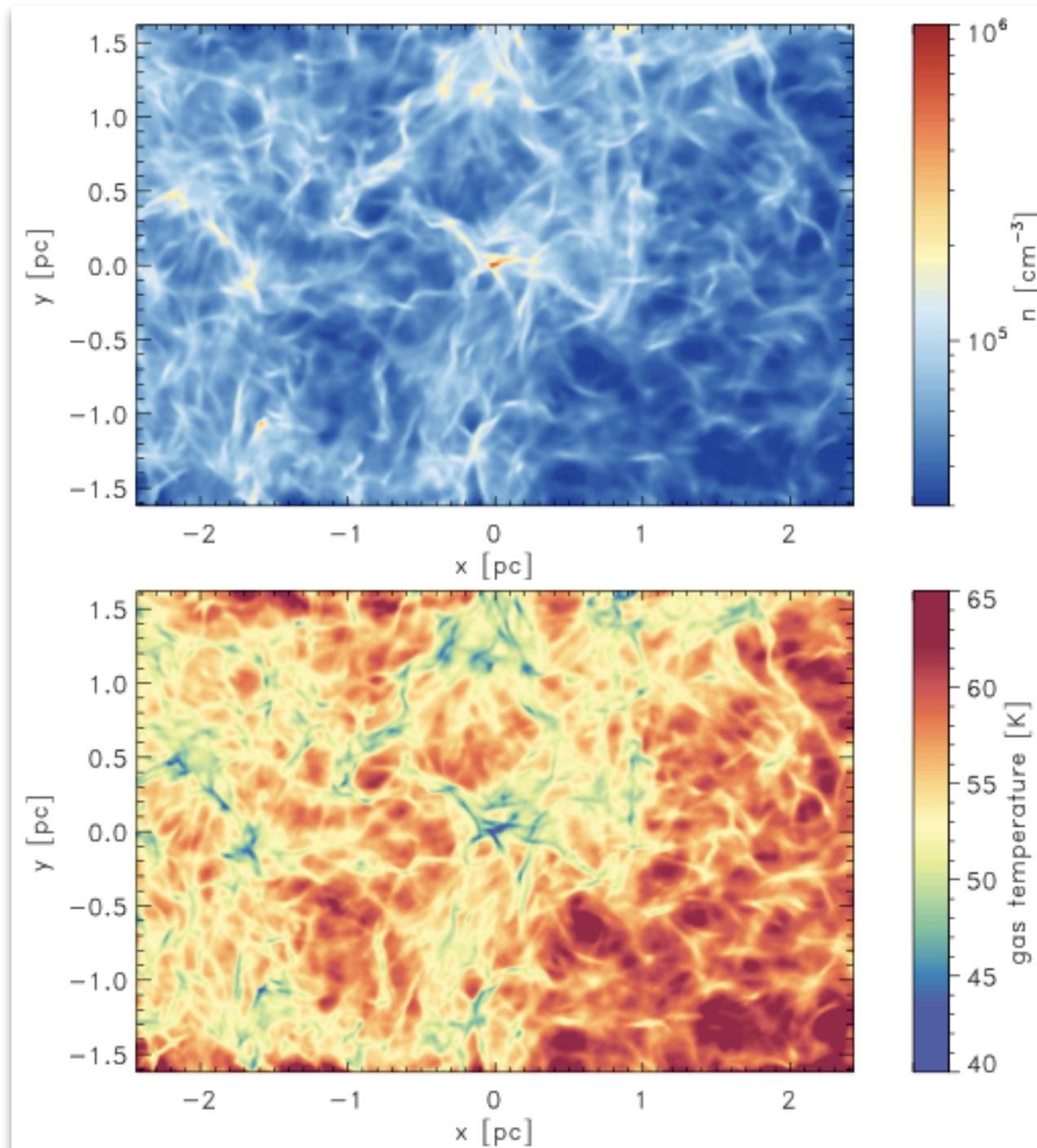


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Comparison of all relevant heating and cooling processes.



two selected examples

- formation and evolution of molecular clouds
 - combine MHD with self-gravity and time-dependent chemistry
 - model the turbulent multi-phase interstellar medium
- stellar mass function
 - distribution of stellar masses today and in the early univers

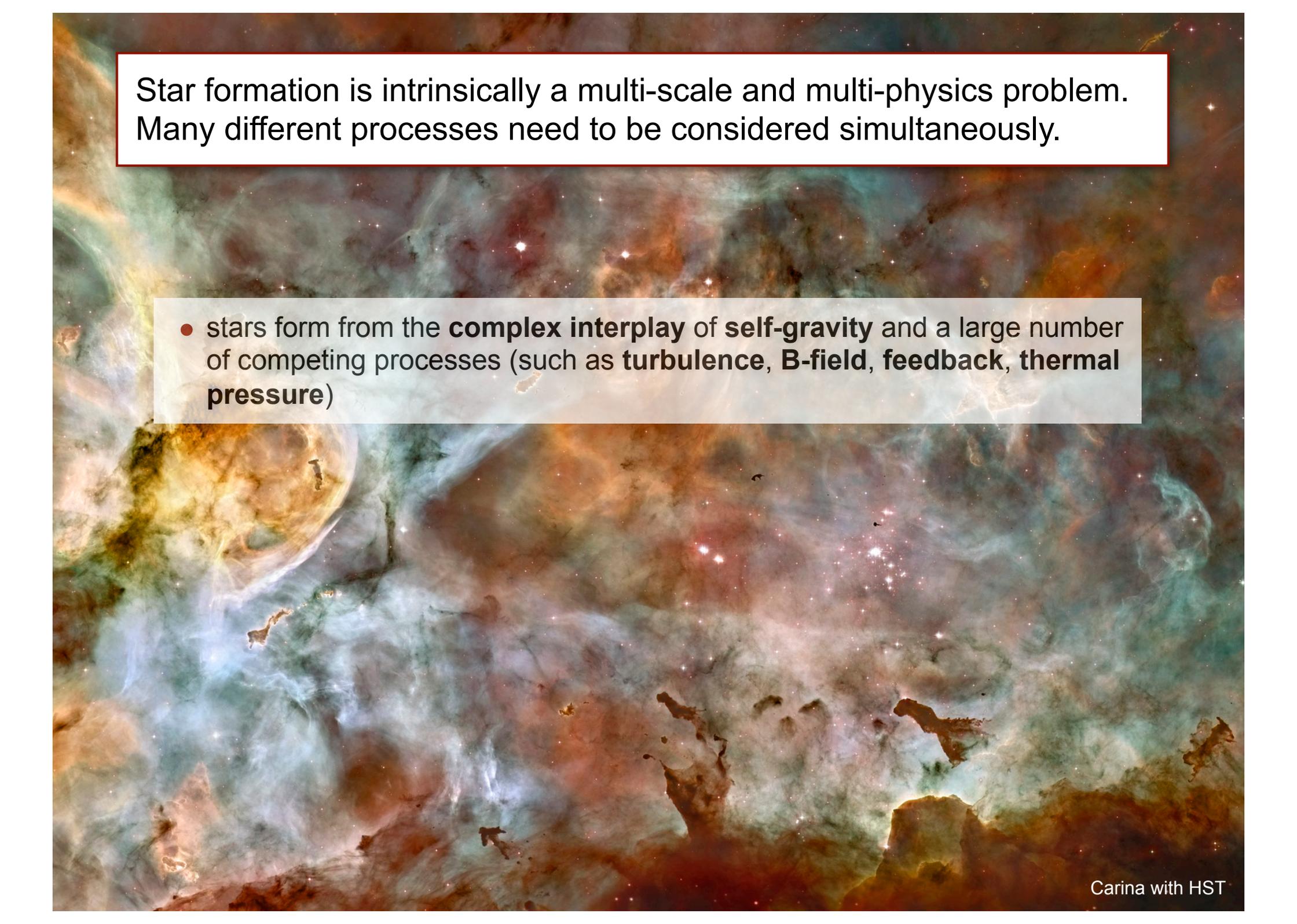




Carina with HST

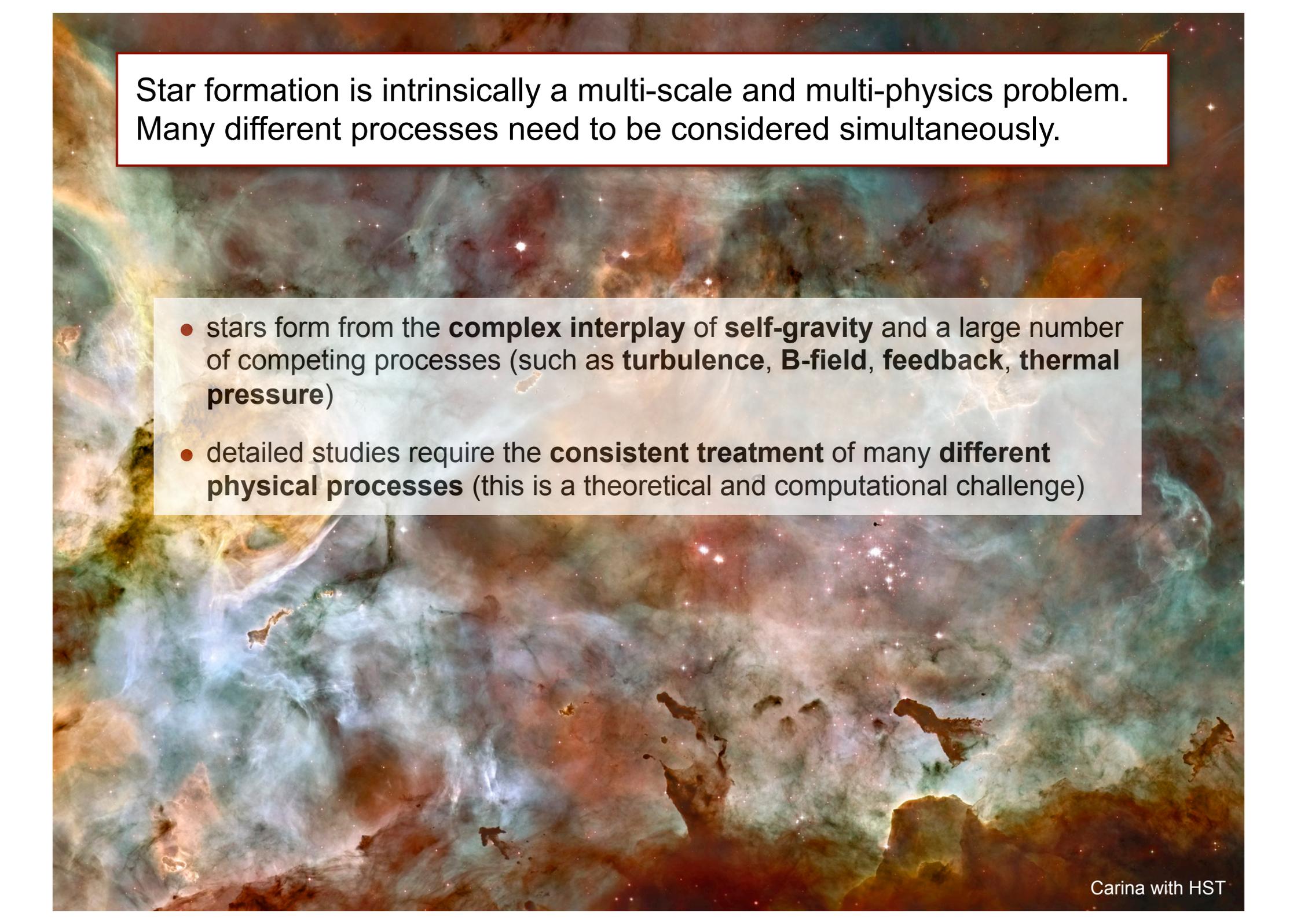
Star formation is intrinsically a multi-scale and multi-physics problem. Many different processes need to be considered simultaneously.





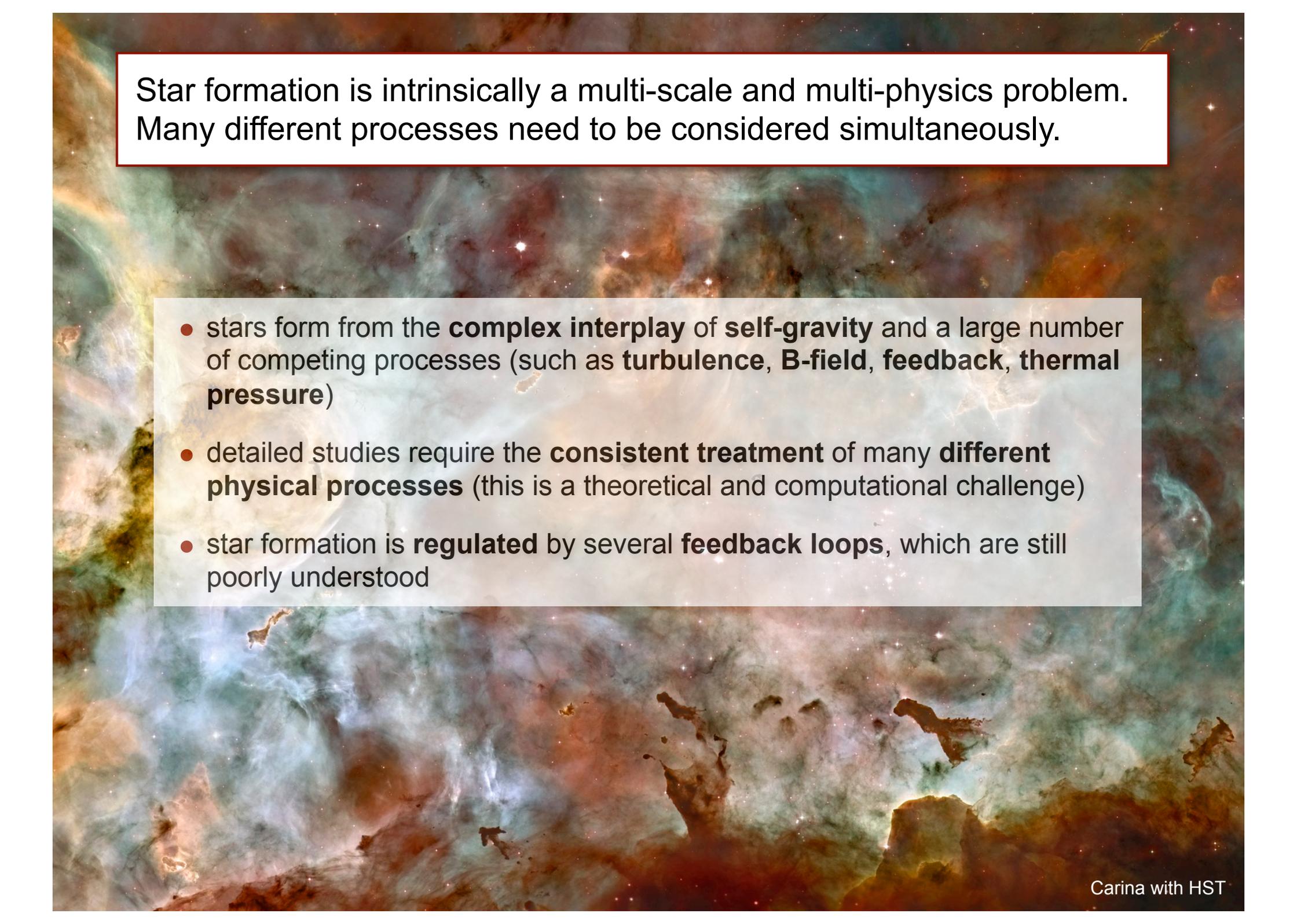
Star formation is intrinsically a multi-scale and multi-physics problem. Many different processes need to be considered simultaneously.

- stars form from the **complex interplay** of **self-gravity** and a large number of competing processes (such as **turbulence**, **B-field**, **feedback**, **thermal pressure**)



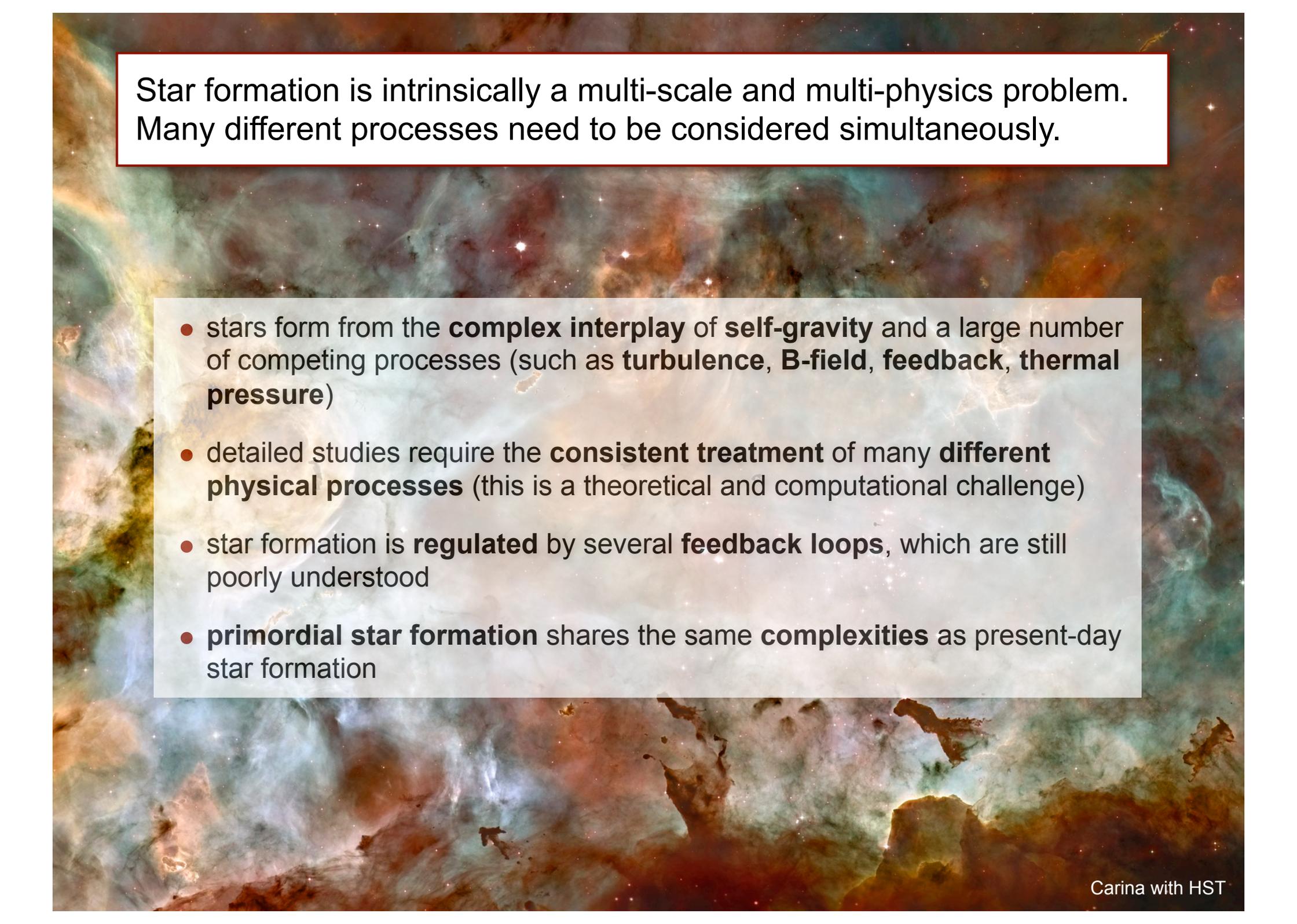
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- detailed studies require the **consistent treatment** of many **different physical processes** (this is a theoretical and computational challenge)



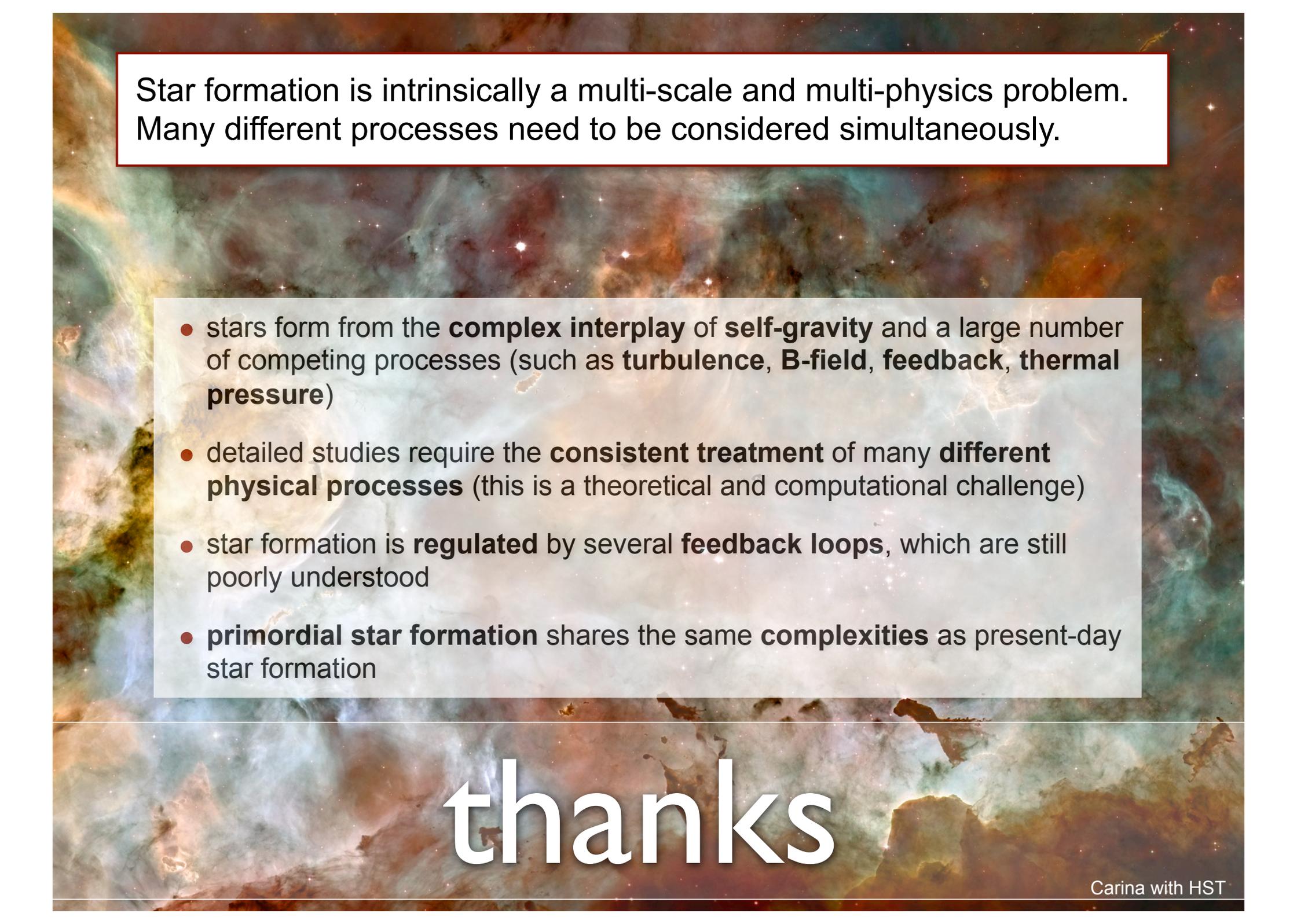
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- **primordial star formation** shares the same **complexities** as present-day star formation



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thanks