



Simulations of Star Formation and the Stellar Initial Mass Function

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Open Questions in ISM Dynamics and Star Formation

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agenda

- Elmegreen, B. G.: Starbursts by gravitational collapse in the inner Lindblad resonance rings of galaxies, *ApJ*, 425, L73 (1994)
- Elmegreen, B. G.: Star Formation in a Crossing Time, *ApJ*, 530, 277 (2000)
- Elmegreen, B. G., Klessen, R. S., Wilson, C. D.: On the Constancy of the Characteristic Mass of Young Stars, *ApJ*, 681, 365, (2008)

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→ **presence of CO-dark H_2 gas**
- Elmegreen, B. G.: Star Formation in a Crossing Time, *ApJ*, 530, 277 (2000)
→ **importance of init. conditions for star formation**
- Elmegreen, B. G., Klessen, R. S., Wilson, C. D.: On the Constancy of the Characteristic Mass of Young Stars, *ApJ*, 681, 365, (2008)
→ **importance of thermodynamics for the IMF**

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→ **importance of thermodynamics for the IMF**

STARBURSTS BY GRAVITATIONAL COLLAPSE IN THE INNER LINDBLAD RESONANCE RINGS OF GALAXIES

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ABSTRACT

Starbursts in inner Lindblad resonance rings are proposed to result from gravitational instabilities that fragment the ring into several bound clouds. Each cloud forms a separate star cluster or hot spot after further energy dissipation and collapse. A linear instability analysis including accretion and an azimuthal magnetic field suggests that the ring instability occurs only after a critical density is reached, which presumably follows a relatively long epoch of gas accretion from bar or spiral torques. The critical density is very high in the inner regions because the Coriolis and tidal forces are high. Typical densities are $>100 \text{ cm}^{-3}$, depending on the inner Lindblad resonance radius, rotation curve, accretion rate, and other parameters. The rapid star formation in the starburst follows from the high density at the expected rate $\epsilon\omega\rho$ for local efficiency per cloud ϵ , instability growth rate ω , and density ρ . Most of the high rate comes from the density dependence of $\omega(\rho)\rho$, but the efficiency ϵ could also increase if the ambient velocity dispersion is high in the ring.

Subject headings: galaxies: starburst — stars: formation — instabilities

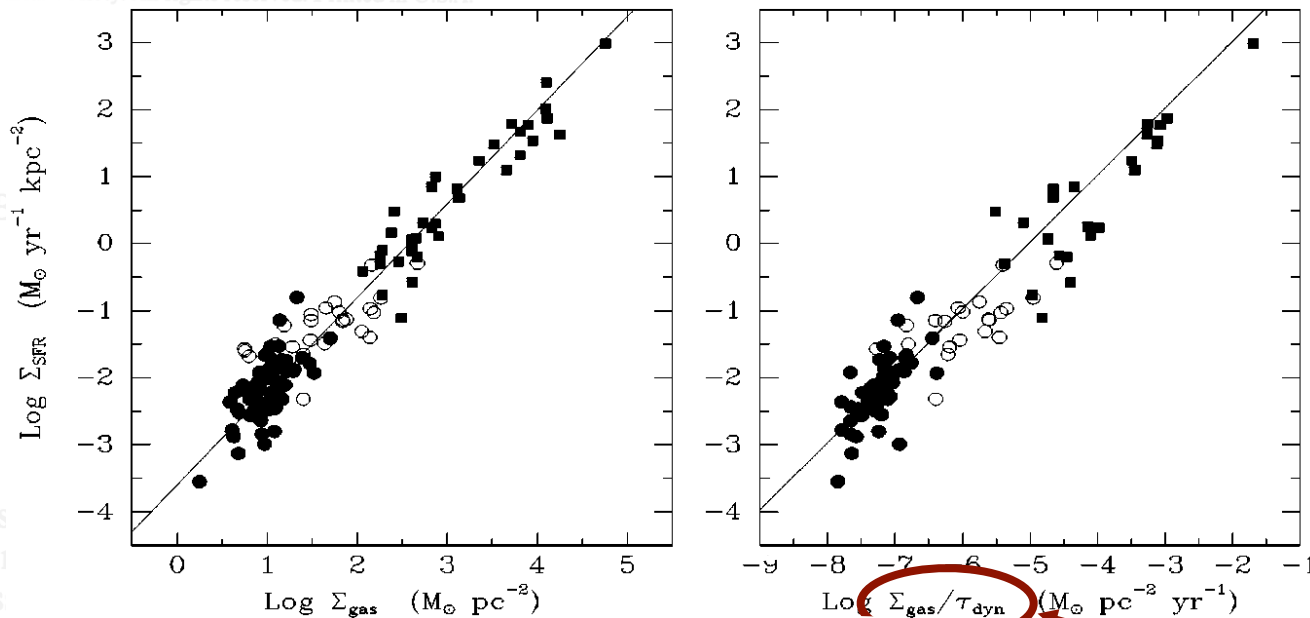
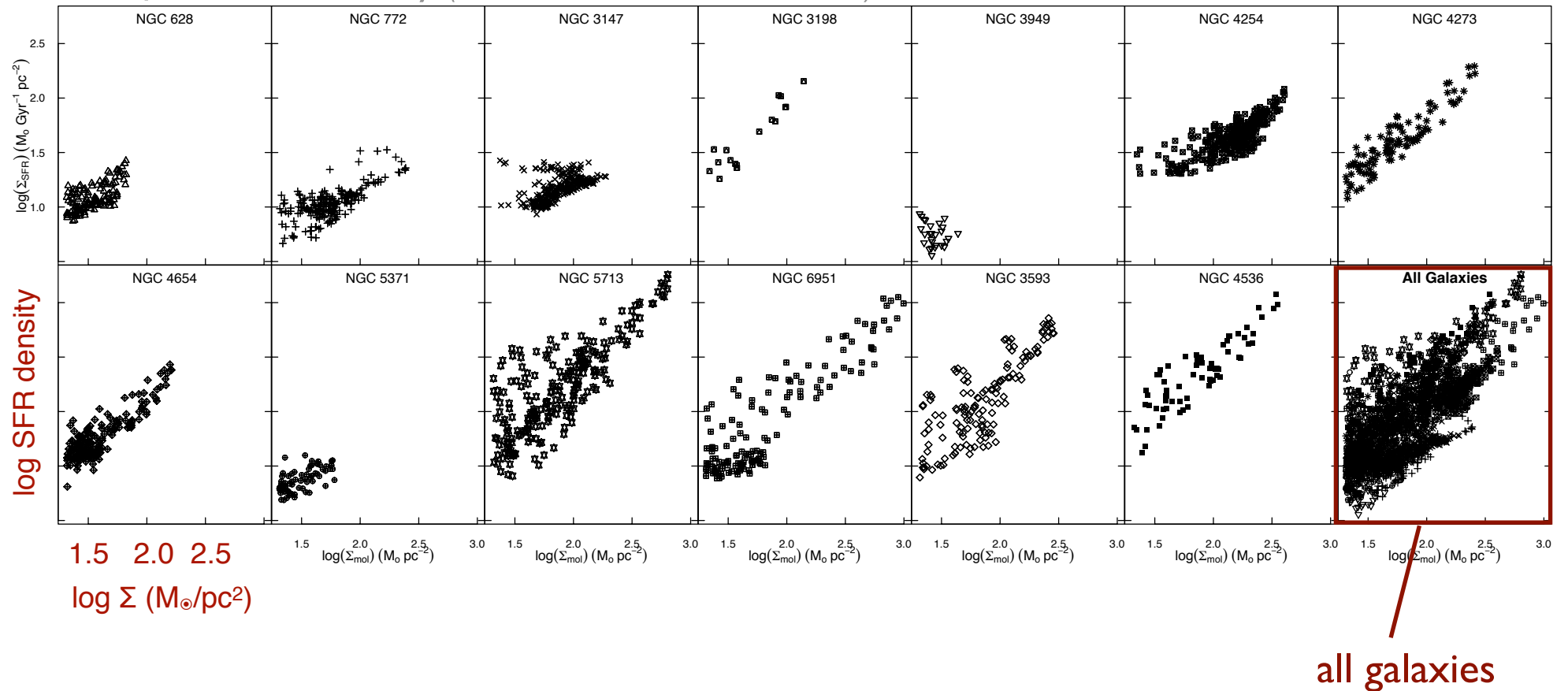


Figure 9. (Left) The global Schmidt law in galaxies. Solid points denote the normal spirals in Figure 5, squares denote the circumnuclear starbursts in Figure 7. The open circles show the SFRs and gas densities of the central regions of the normal disks. (Right) The same SFR data but plotted against the ratio of the gas density to the average orbital time in the disk. Both plots are adapted from Kennicutt (1998).

$$\Sigma_{SFR} = (2.5 \pm 0.7) \times 10^{-4} \left(\frac{\Sigma_{gas}}{1 M_{\odot} \text{ pc}^{-2}} \right)^{1.4 \pm 0.15} M_{\odot} \text{ year}^{-1} \text{ kpc}^{-2},$$

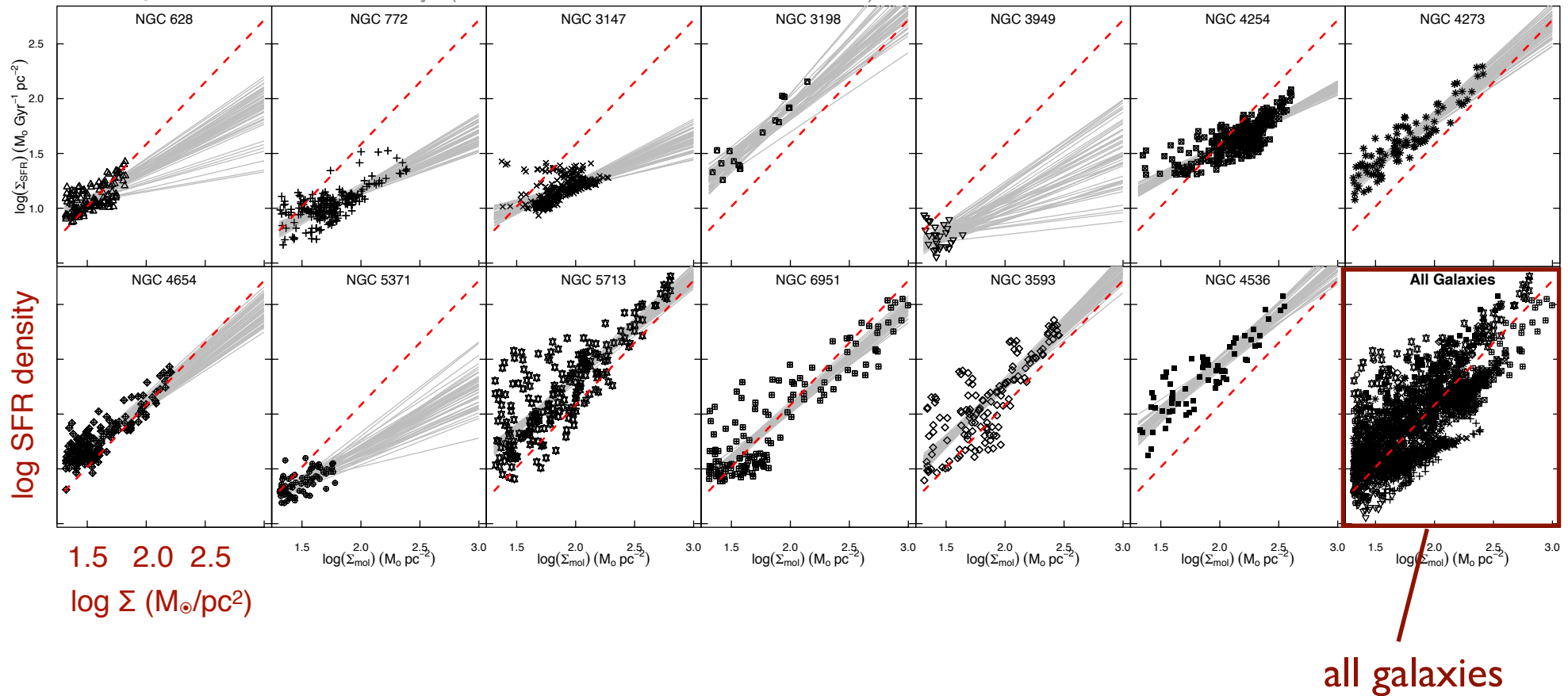
“As discussed by Larson (1992) and Elmegreen (1994), a large-scale Schmidt law with index $N \sim 1.5$ would be expected for self-gravitating disks if the SFR scales as the ratio of the gas density (ρ) to the free-fall time scale ($\propto \rho^{-0.5}$) and the average gas scale height is roughly constant across the sample ($\Sigma \propto \rho$),”

data from STING survey (Rahman et al. 2011, 2012)



- QUIZ: do you see a universal

data from STING survey (Rahman et al. 2011, 2012)



- QUIZ: do you see a universal
- ANSWER: - probably not
- in addition, the relation often is sublinear

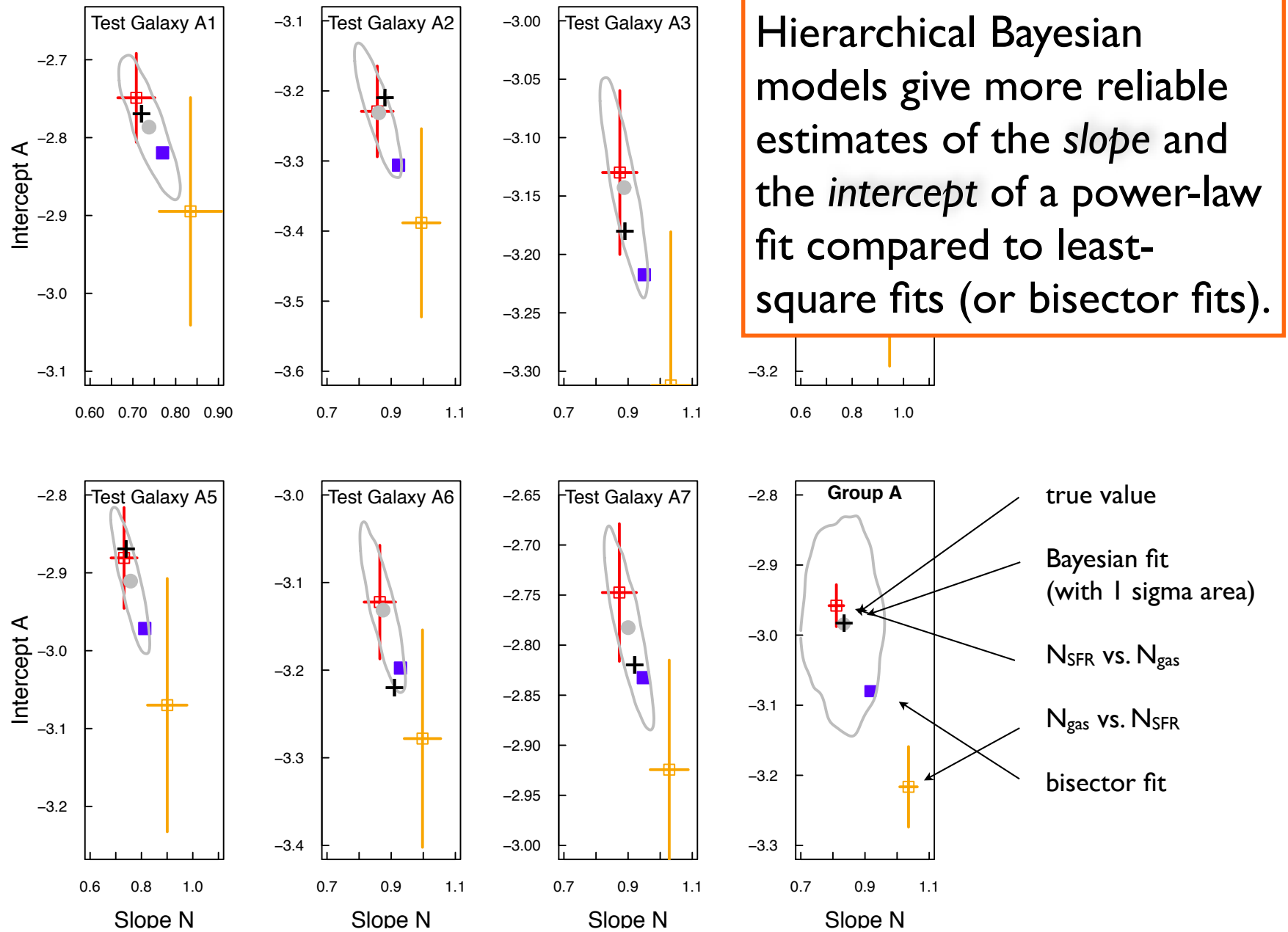
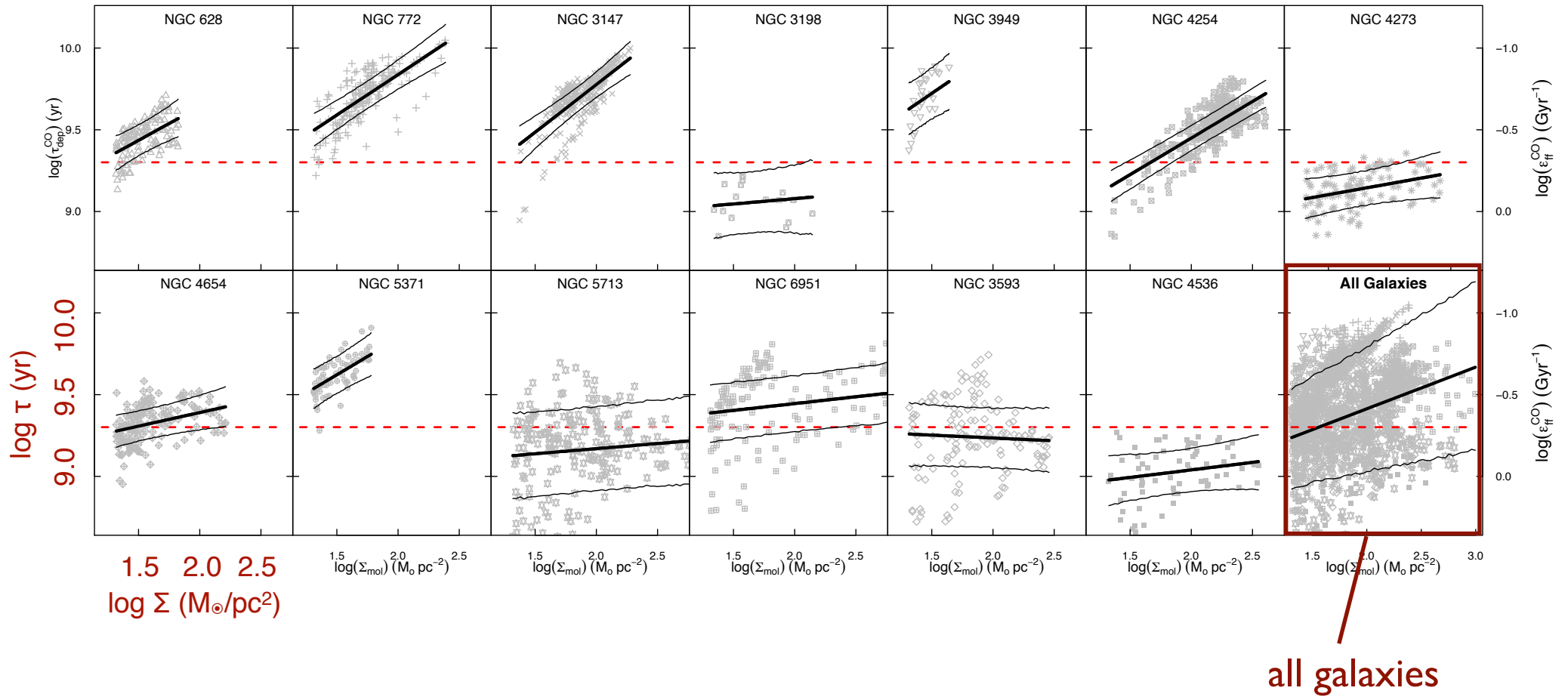


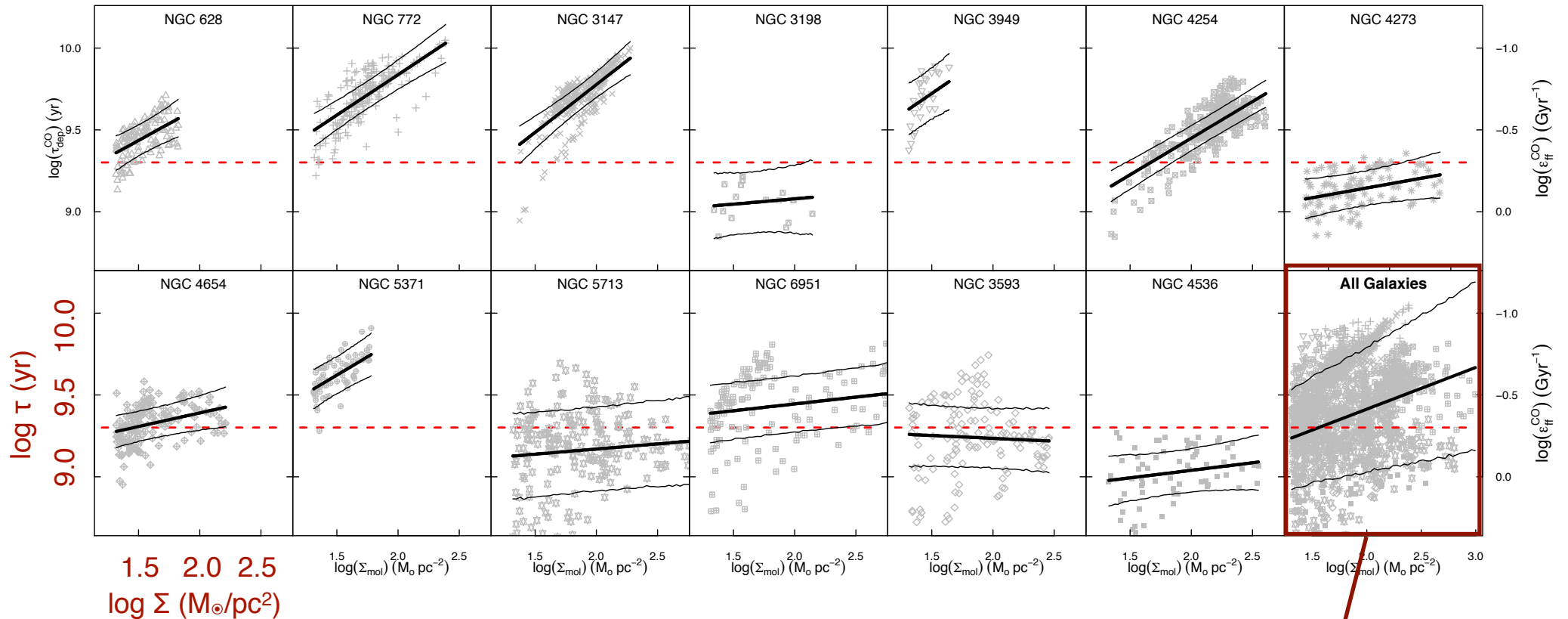
Figure 1. Slope and intercept of test galaxies in Group A. Black cross shows the true values. Red and orange squares show the $OLS(\Sigma_{SFR}|\Sigma_{mol})$ and $OLS(\Sigma_{mol}|\Sigma_{SFR})$ results, with their 1σ uncertainties, respectively. The gray circles indicate the estimate provided by the median of hierarchical Bayesian posterior result, and the contours mark the 1σ deviation. The filled blue squares mark the bisector estimates. The last panel on the bottom row shows the group parameters and fit estimates.

data from STING survey (Rahman et al. 2011, 2012)



Hierarchical Bayesian model for STING galaxies indicate *varying depleting times.*

data from STING survey (Rahman et al. 2011, 2012)

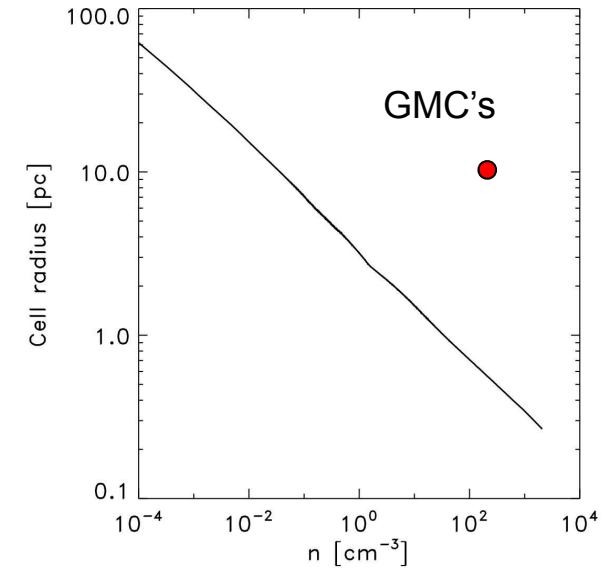
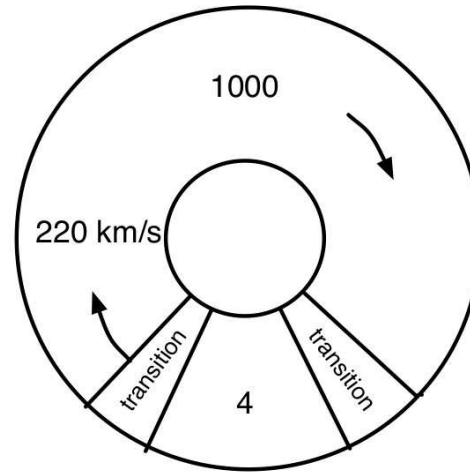
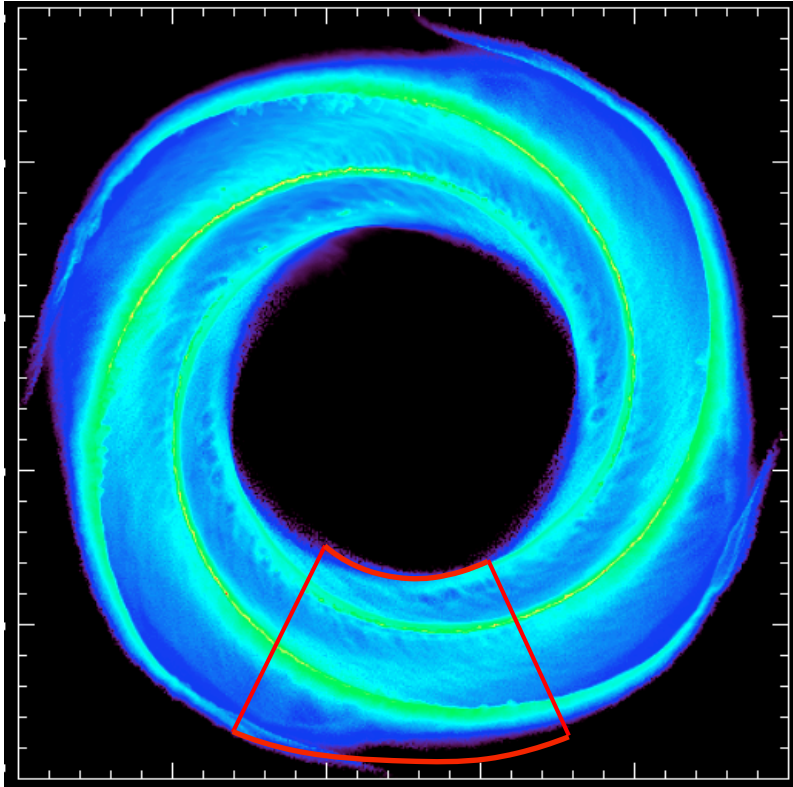


all galaxies

physical origin of this behavior?

- maybe strong shear in dense arms (example M51, Meidt et al. 2013)...
- maybe non-star forming H column densities (recall H

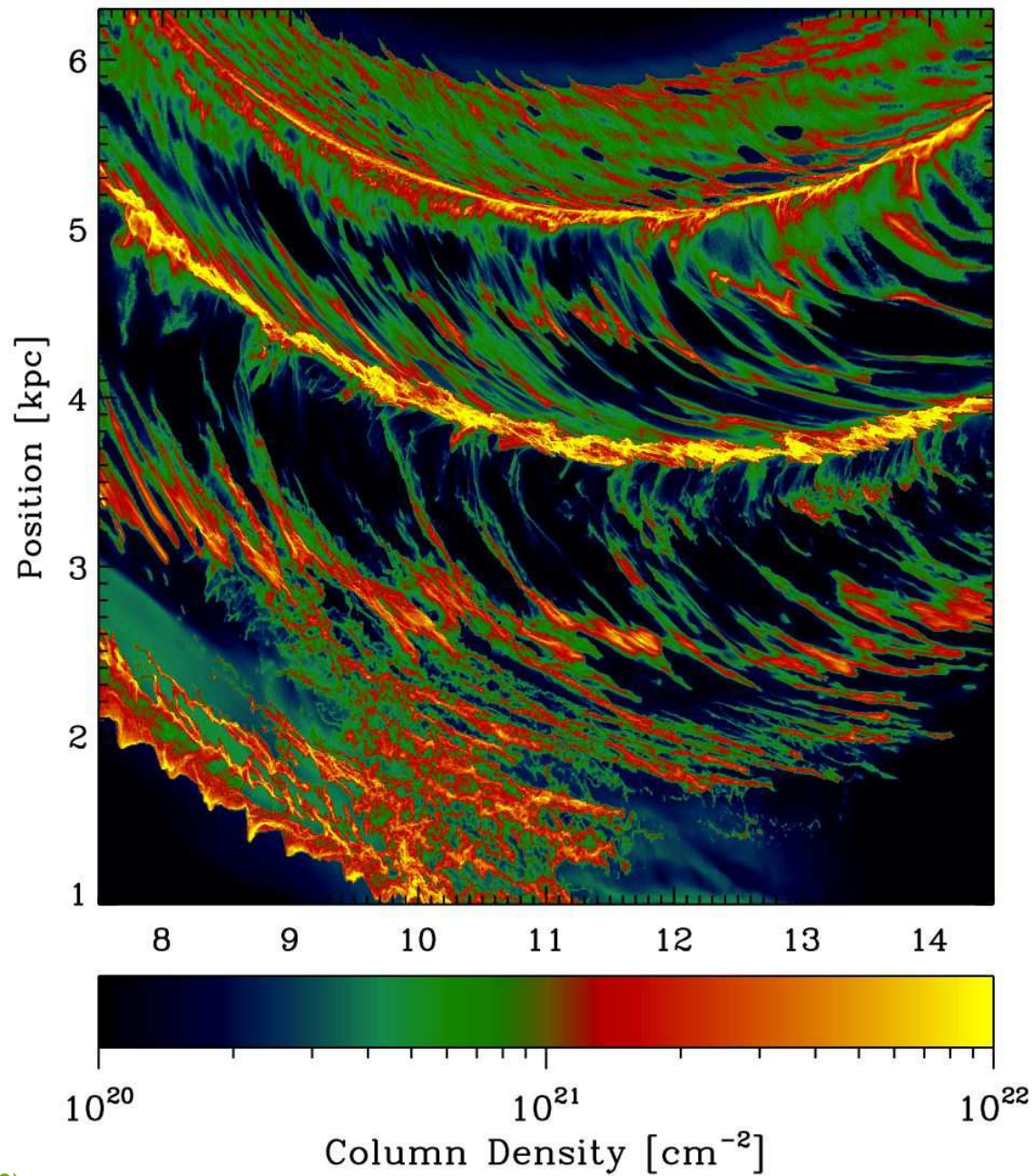
molecular cloud formation

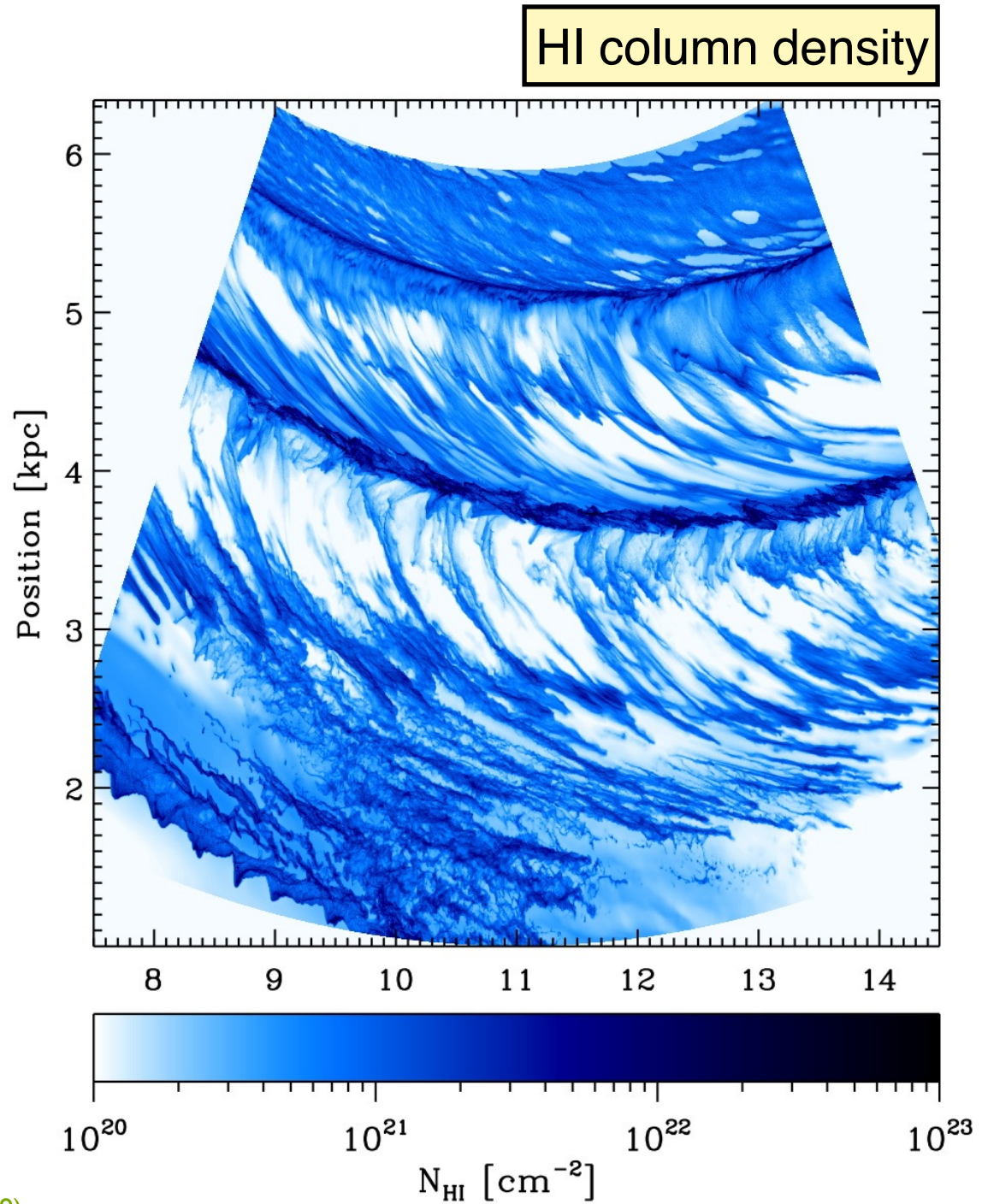
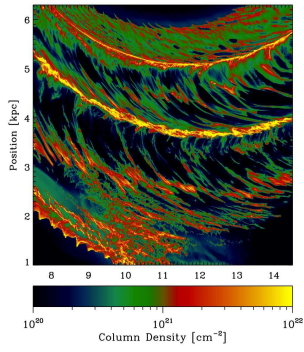


Simulation	Surface Density $M_{\odot} \text{ pc}^{-2}$	Radiation Field G_0
Milky Way	10	1
Low Density	4	1
Strong Field	10	10
Low & Weak	4	0.1

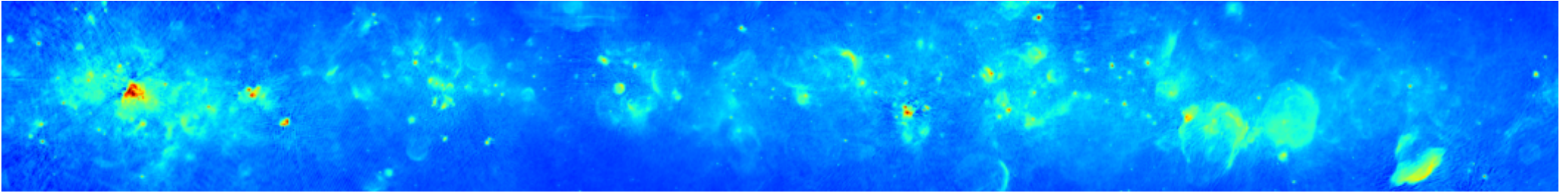
- Arepo moving mesh code (*Springel 2010*)
- time dependent chemistry (*Glover et al. 2007*)
gives heating & cooling in a 2 phase medium
- two layers of refinement with mass resolution down to $4 M_{\odot}$ in full Galaxy simulation
- UV field and cosmic rays
- TreeCol (*Clark et al. 2012*)
- external spiral potential (*Dobbs & Bonnell 2006*)
- no gas self-gravity, SN, or magnetic fields yet

total column density

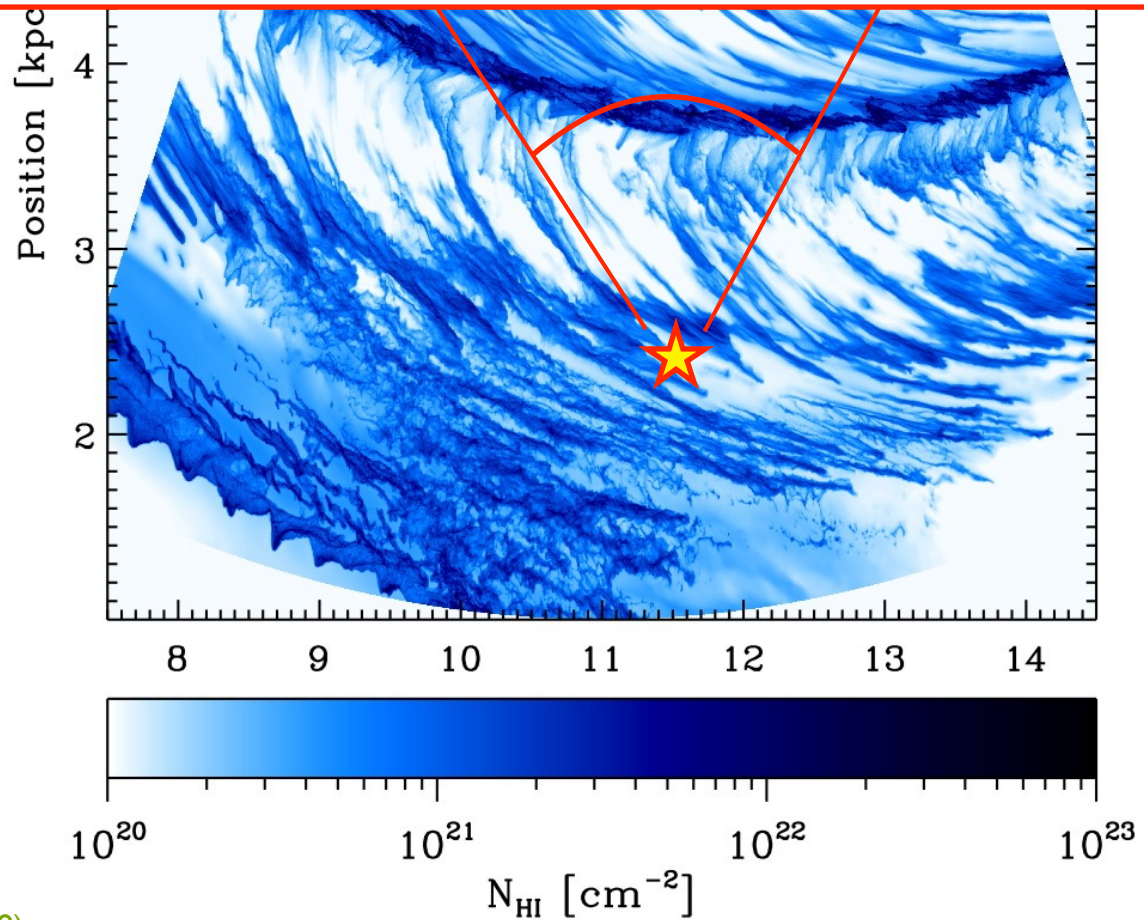


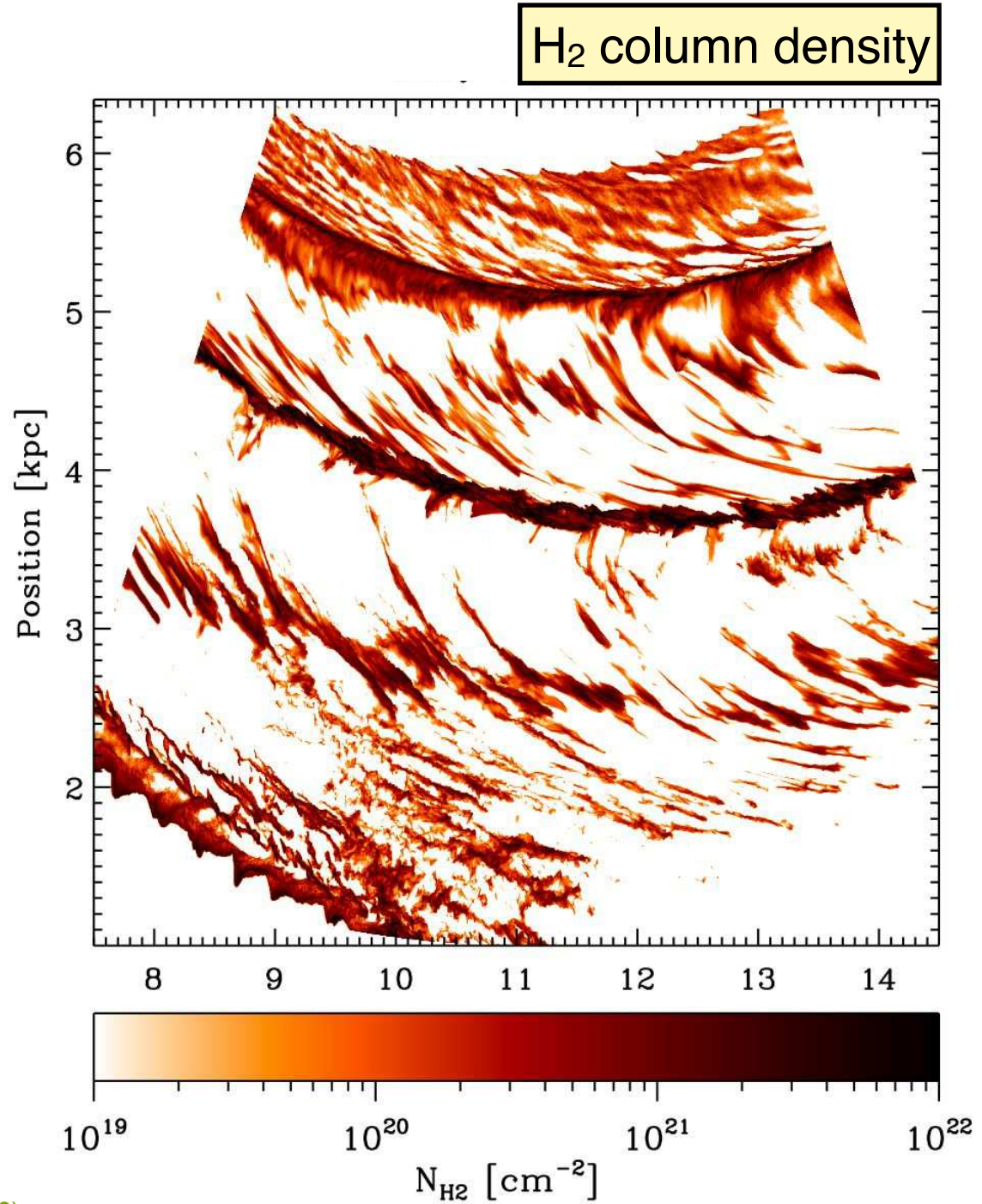
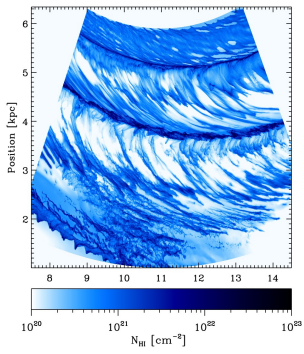
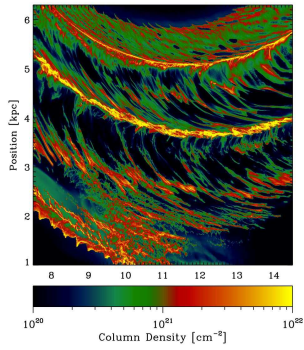


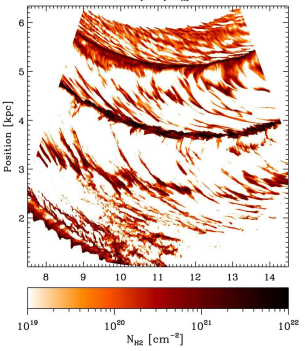
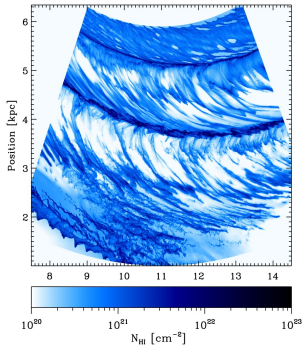
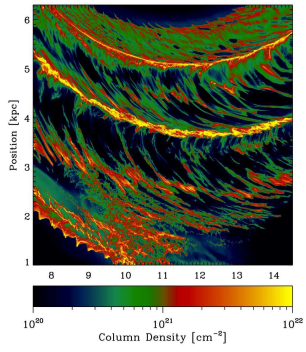
preliminary image from THOR Galactic plane survey (PI H. Beuther)



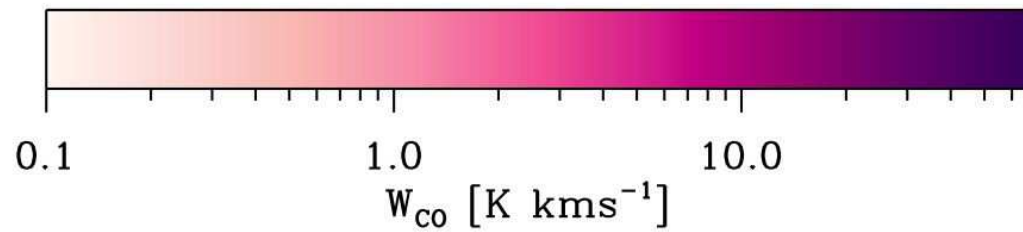
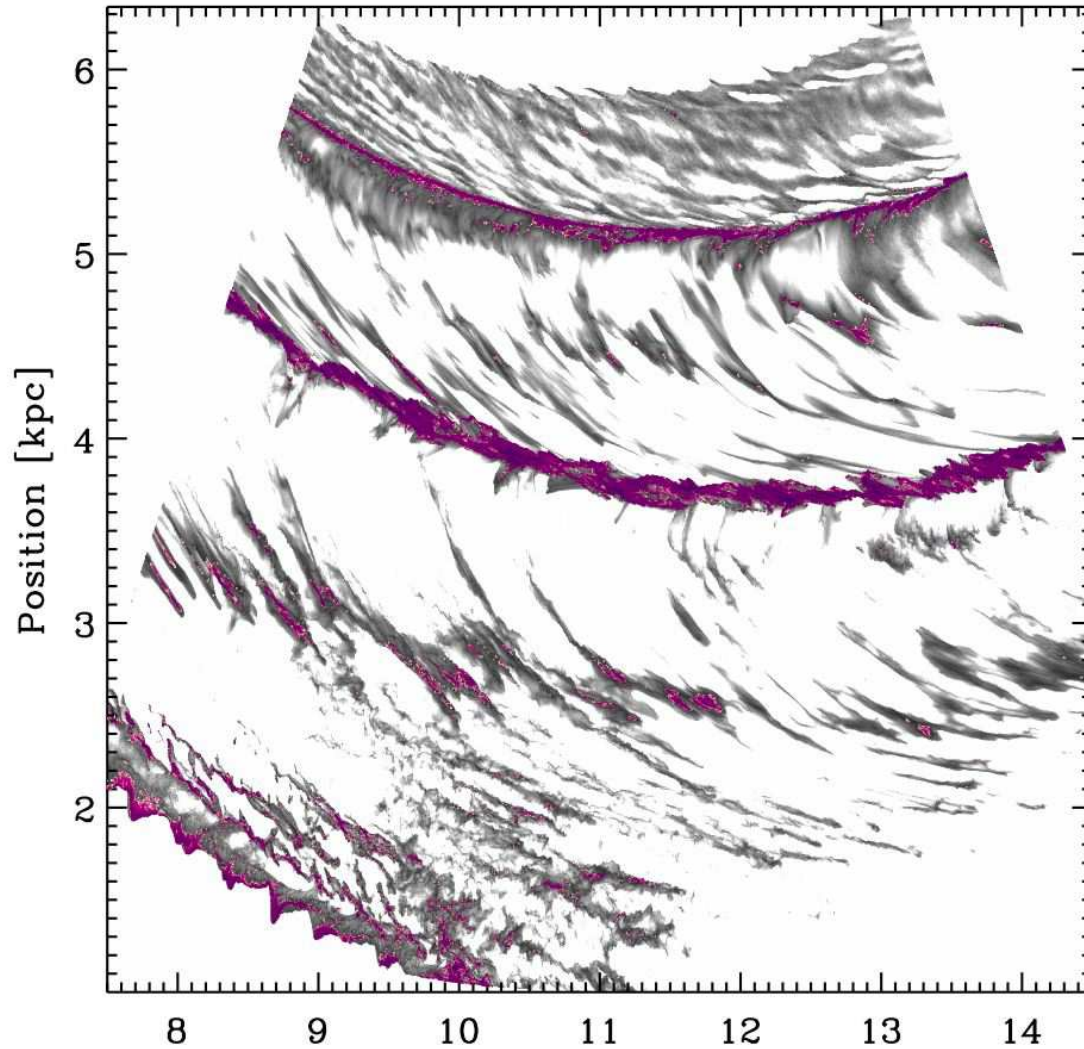
next step: produce all sky maps at various positions in the model galaxy (use RADMC-3D)



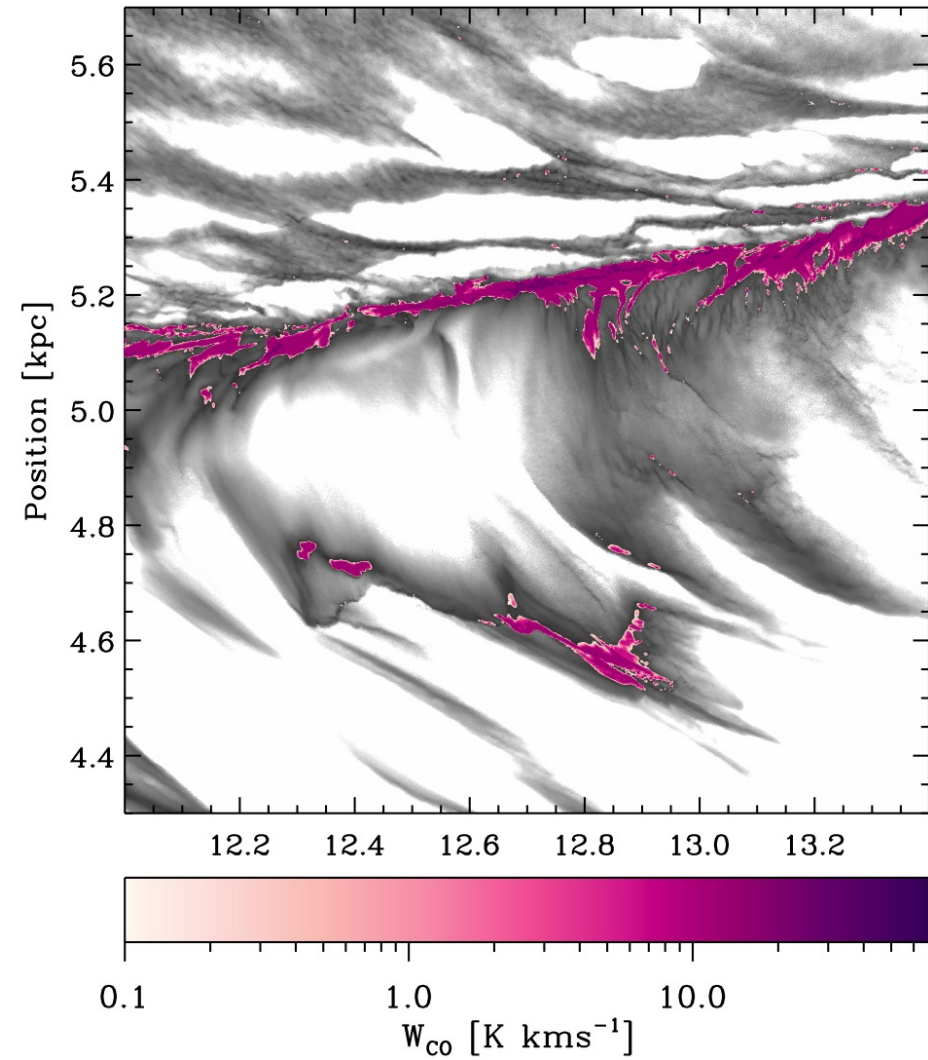
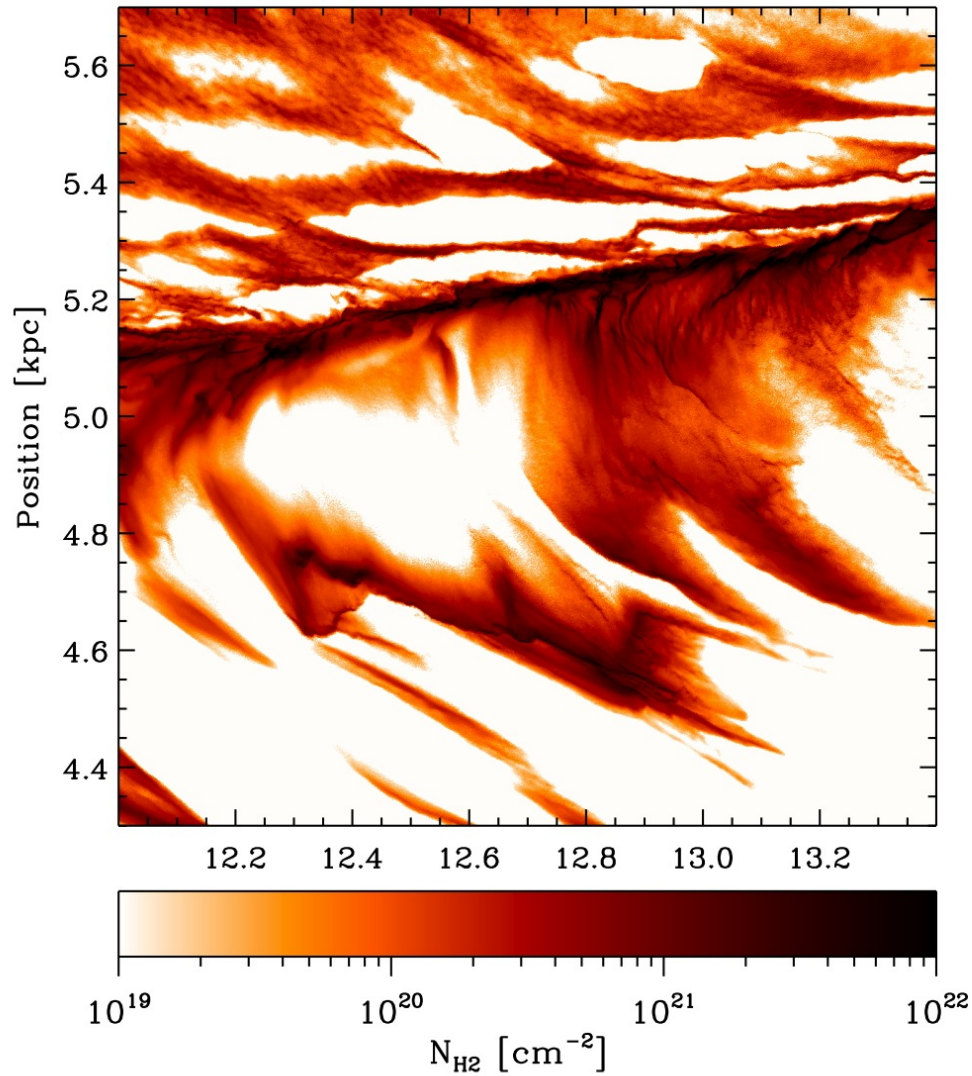




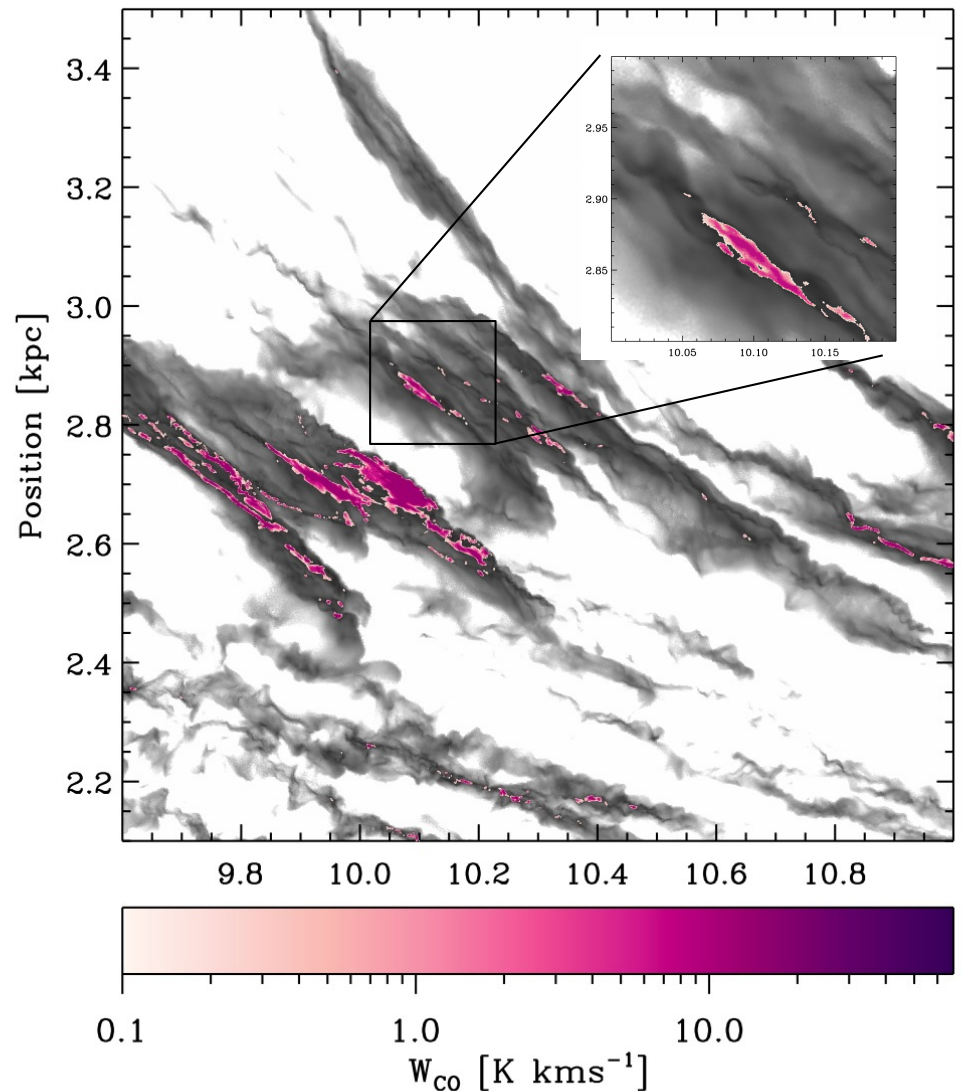
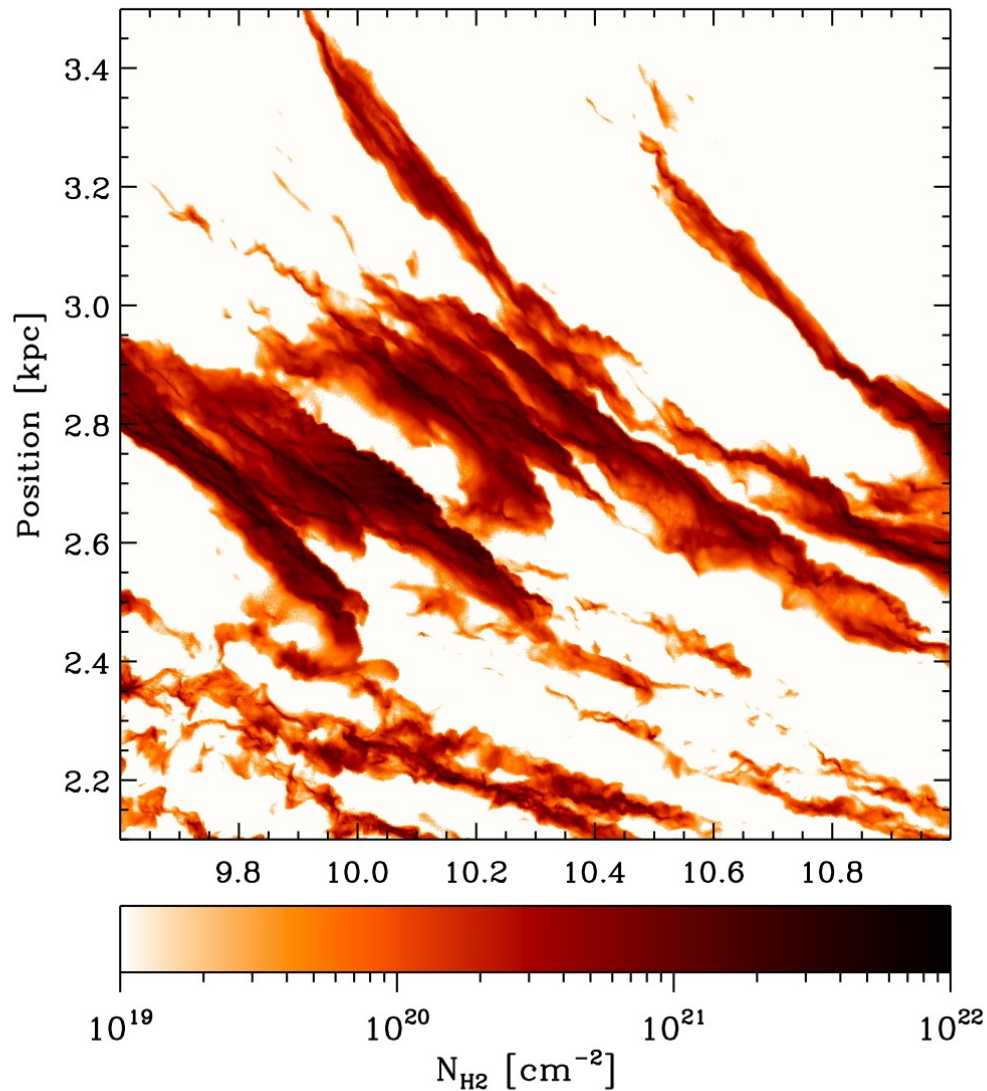
CO column density



relation between CO and H₂

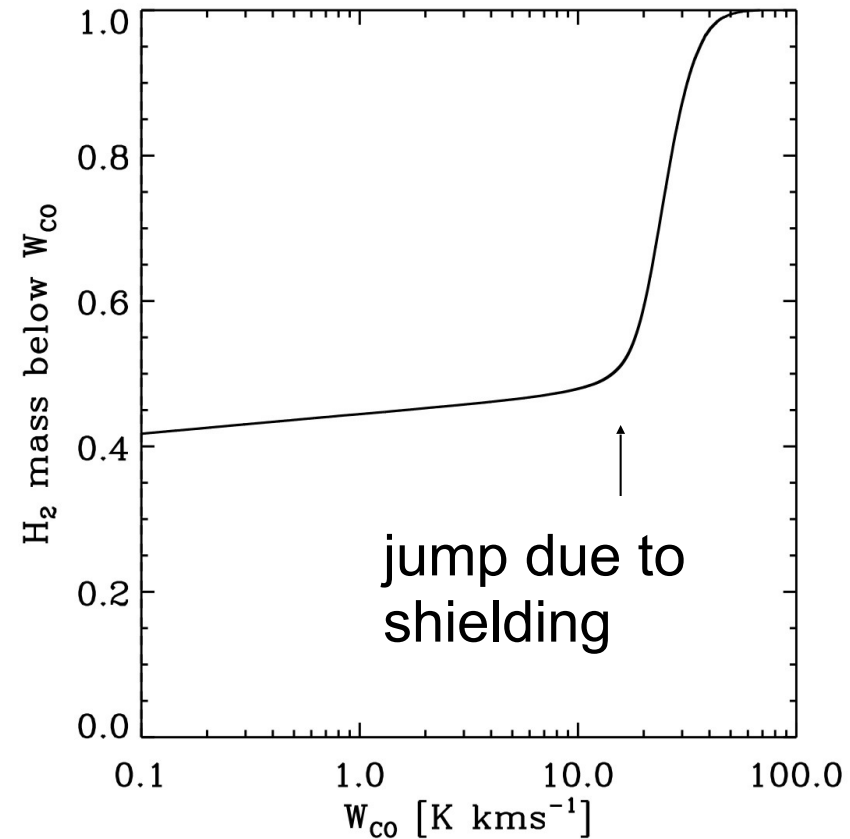
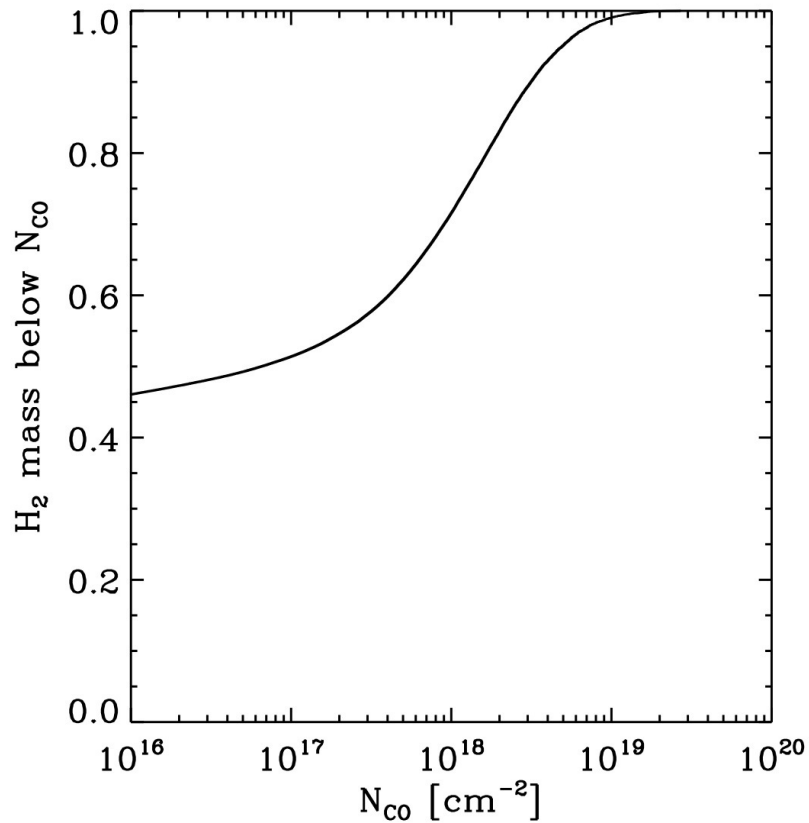


relation between CO and H₂



Filamentary molecular clouds in inter-arm regions are likely only the observable parts of much larger structures.

dark gas fraction



46% molecular gas below CO column densities of 10^{16} cm⁻²

42% has an integrated CO emission of less than 0.1 K kms⁻¹

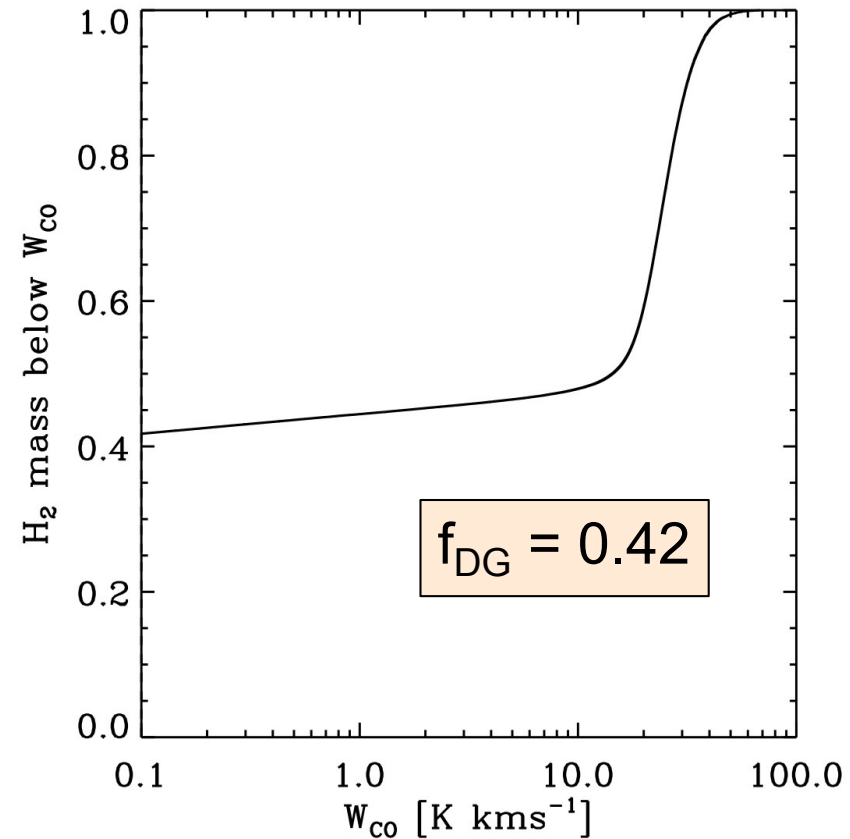
$$f_{\text{DG}} = 0.42$$

$$X_{\text{CO}} = 2.2 \times 10^{20} \text{ cm}^{-2} \text{K}^{-1} \text{km}^{-1} \text{s}$$

dark gas fraction

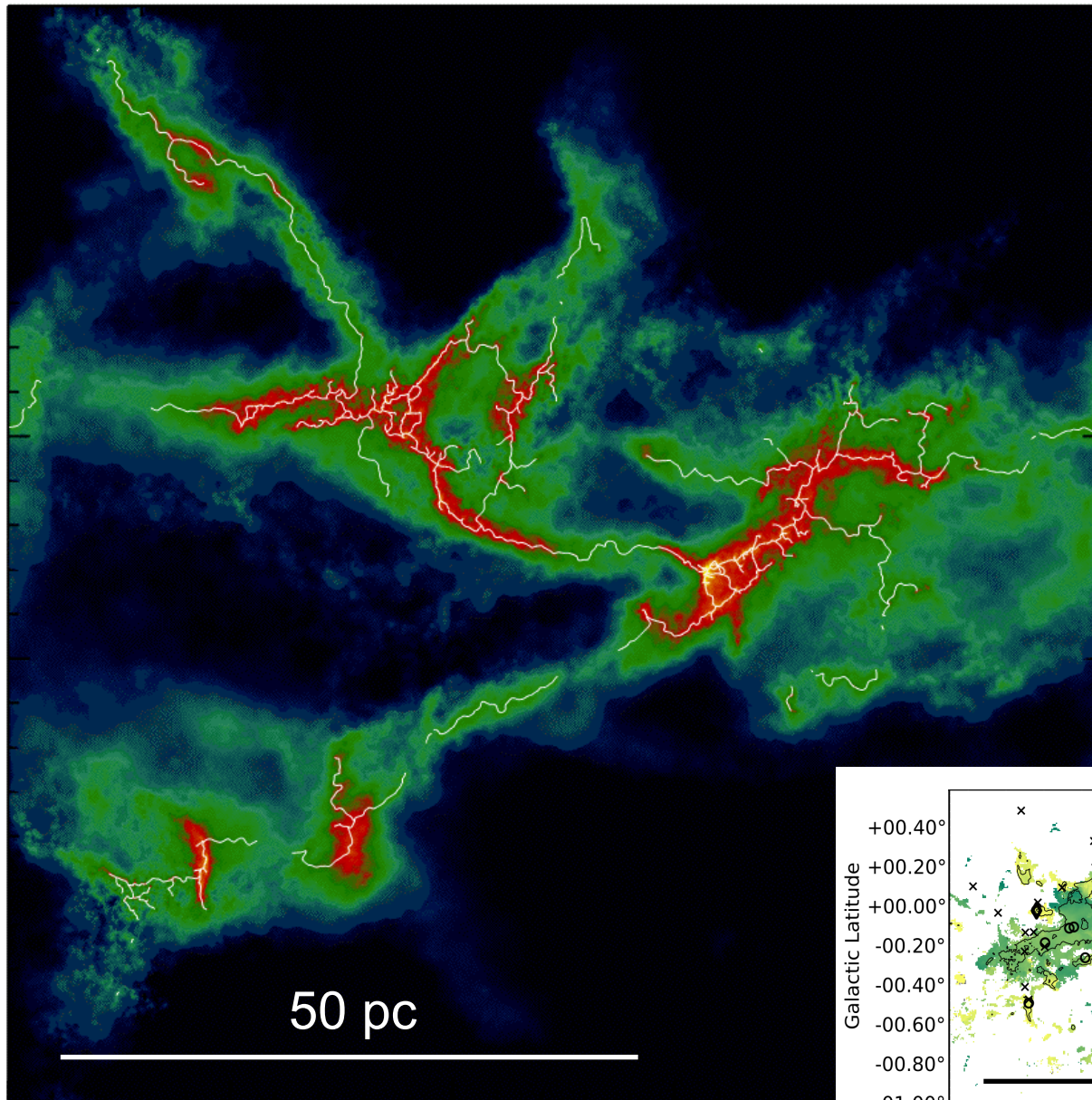
Observational estimates:

- Wolfire et al. 2010 $f_{\text{DG}} \approx 0.30$
- Grenier et al. 2005 $f_{\text{DG}} = 0.33\text{-}0.5$
- Planck collaboration 2011* $f_{\text{DG}} = 0.54$
- Paradis et al. 2012* $f_{\text{DG}} = 0.62$
 inner $f_{\text{DG}} = 0.71$, outer $f_{\text{DG}} = 0.43$
- Pineda et al. 2013 $f_{\text{D}} = 0.3$



* dust methods have large uncertainties.

large-scale filaments



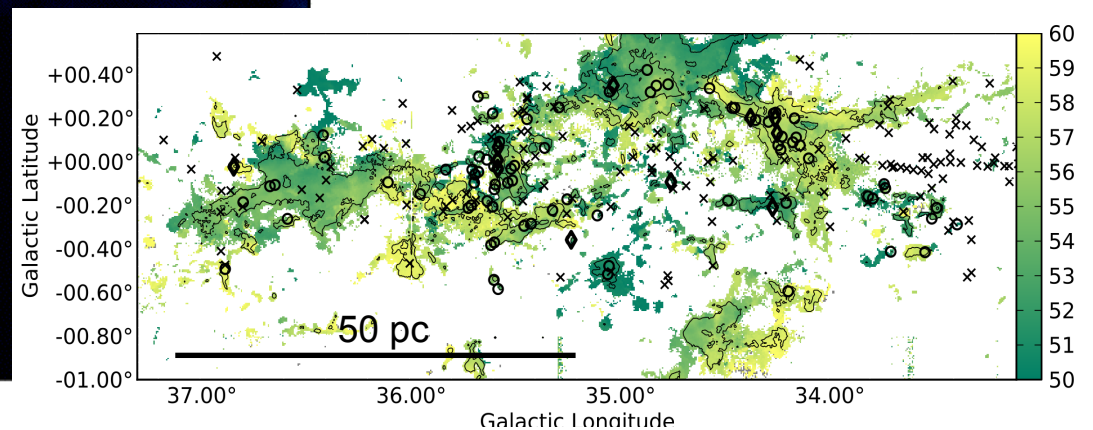
Smith et al. (2014, in preparation)

next steps:

studying details of ISM morphology and star formation in dedicated zoom-in simulation

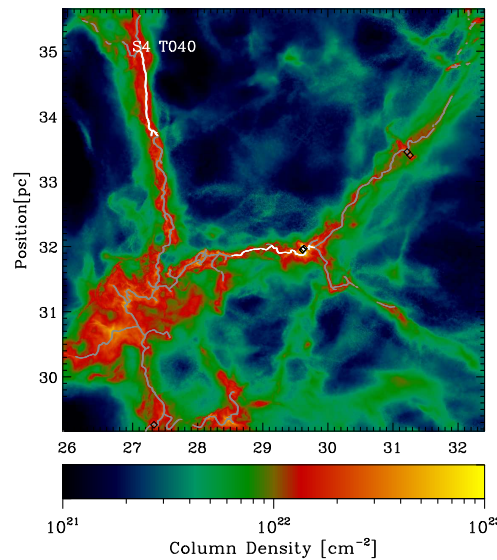
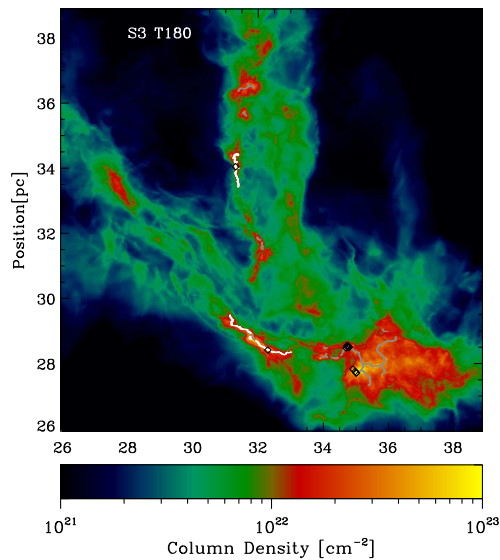
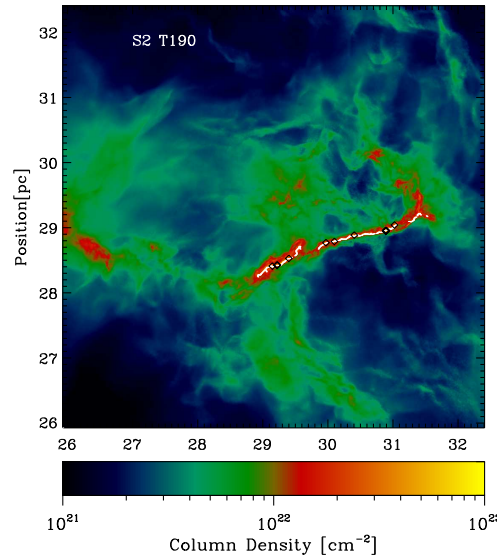
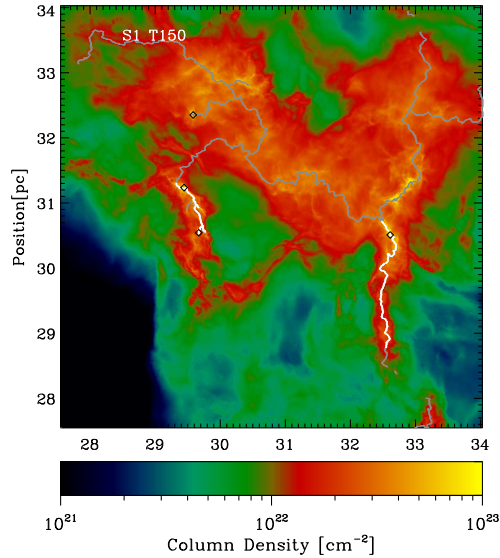
example:

giant molecular cloud complex ($\sim 10^6 M_{\odot}$) viewed in the plane of the disk.



Ragan et al., 2014, A&A submitted, arXiv:1403.1450)

zoom-in on filaments



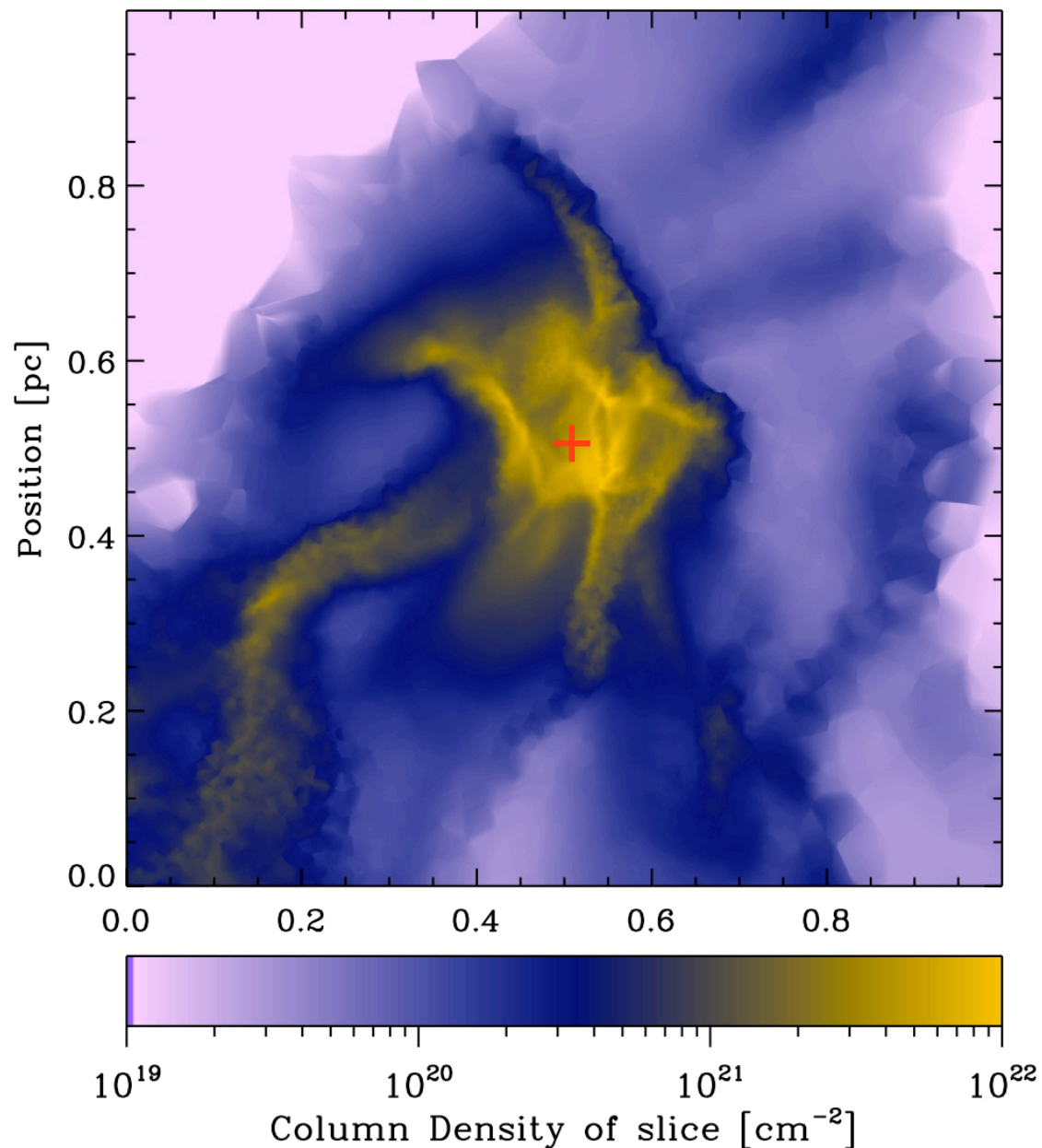
next steps:

studying details of ISM morphology and star formation in dedicated zoom-in simulation
(resolution ≈ 2000 AU, with full chemistry)

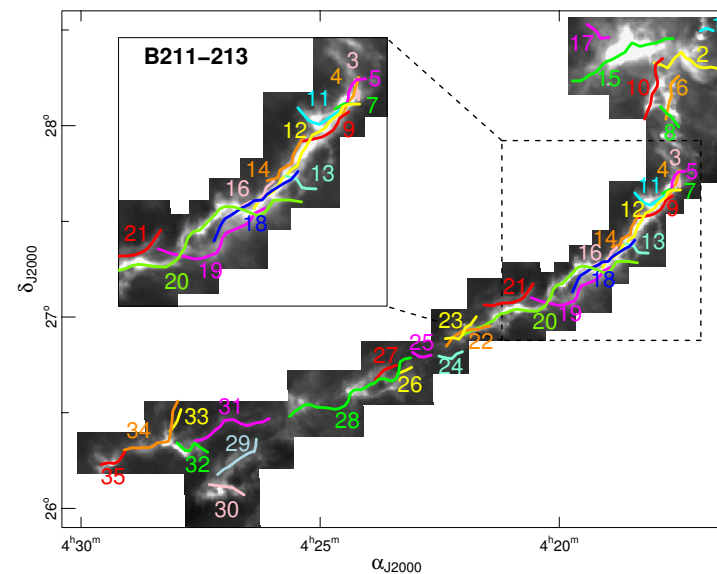
analysis:

- morphology
- velocity
- chemistry
- observations (dust maps for Herschel, CO, N₂H⁺, HCN, etc. for line obs.)

walk along the filament



- walking along the filament exhibits complex 3D structure that is now (fully) seen in projected density
- is this similar to the filament fibers proposed by Hacar et al. (2013, A&A, 554, 55)





ON THE CONSTANCY OF THE CHARACTERISTIC MASS OF YOUNG STARS

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ABSTRACT

The characteristic mass M_c in the stellar initial mass function (IMF) is about constant for most star-forming regions. Numerical simulations consistently show a proportionality between M_c and the thermal Jeans mass M_J at the time of cloud fragmentation, but no models have explained how it can be the same in diverse conditions. Here we show that M_J depends weakly on density, temperature, metallicity, and radiation field in three environments: the dense cores where stars form, larger star-forming regions ranging from GMCs to galactic disks, and the interiors of H II regions and super star clusters. In dense cores, the quantity $T^{3/2}n^{-1/2}$ that appears in M_J scales with core density as $n^{0.25}$ or with radiation density as $U^{0.1}$ at the density where dust and gas come into thermal equilibrium. On larger scales, this quantity varies with ambient density as $n^{-0.05}$ and ambient radiation field as $U^{-0.033}$ when the Kennicutt-Schmidt law of star formation determines $U(n)$. In super star clusters with ionization and compression of prestellar globules, M_J varies as the 0.13 power of the cluster column density. These weak dependencies on n , U , and column density imply that most environmental variations affect the thermal Jeans mass by at most a factor of ~ 2 . Cosmological increases in M_J , which have been suggested by observations, may be explained if the star formation efficiency is systematically higher at high redshift for a given density and pressure, if dust grains are smaller at lower metallicity, and so hotter for a given radiation field, or if small prestellar cores are more severely ionized in extreme starburst conditions.

Subject headings: dust, extinction — stars: formation — stars: luminosity function, mass function

thermodynamics & fragmentation

degree of fragmentation depends on *EOS!*

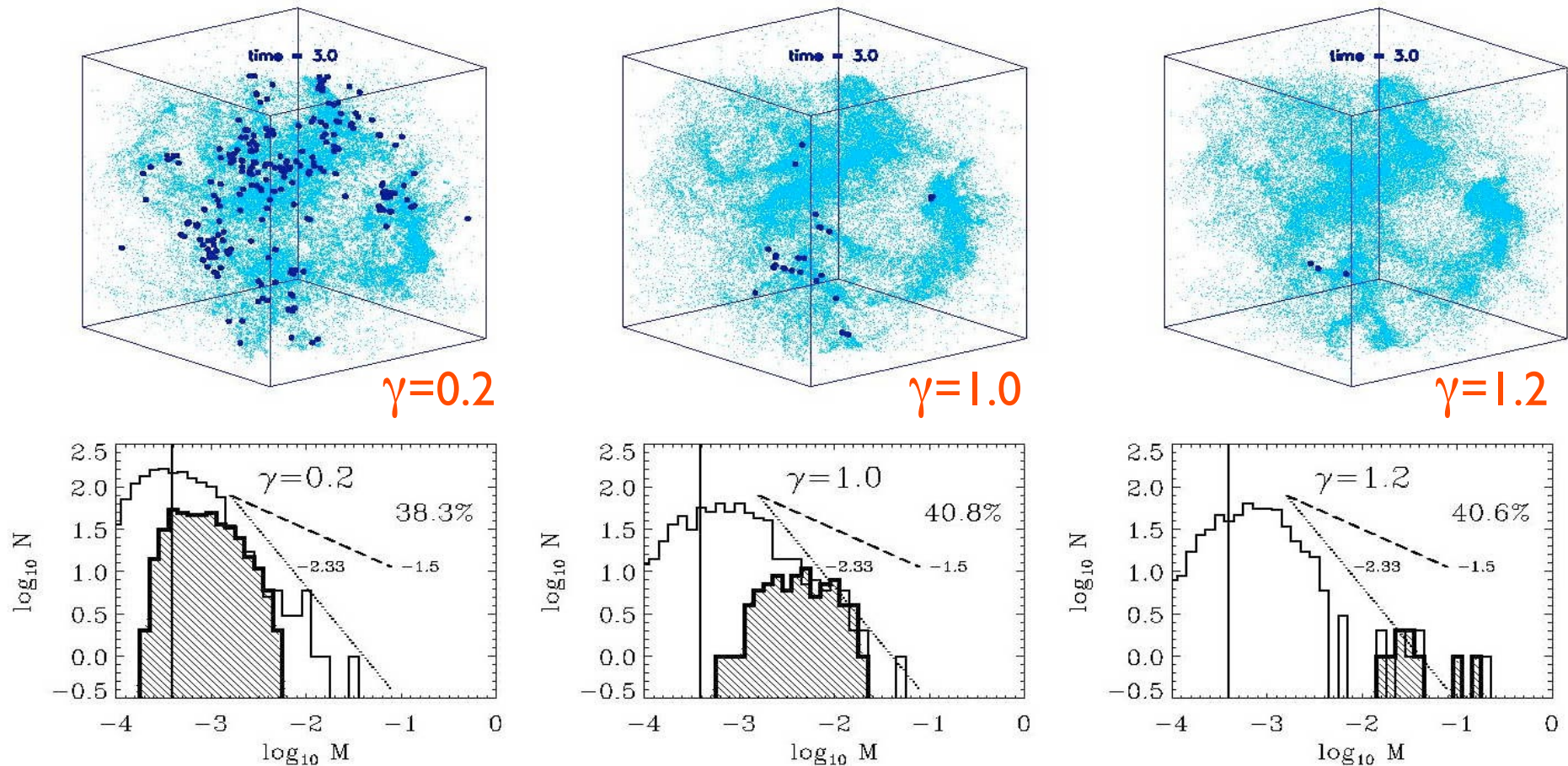
polytropic EOS: $p \propto \rho^\gamma$

$\gamma < 1$: dense cluster of low-mass stars

$\gamma > 1$: isolated high-mass stars

(see Li et al. 2003; also Kawachi & Hanawa 1998, Larson 2003)

dependency on EOS

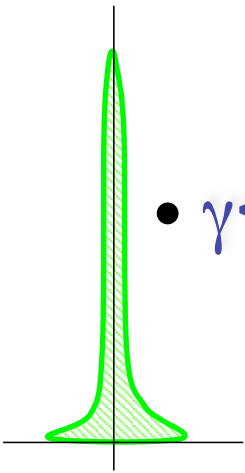


for $\gamma < 1$ fragmentation is enhanced \rightarrow *cluster of low-mass stars*
for $\gamma > 1$ it is suppressed \rightarrow *isolated massive stars*

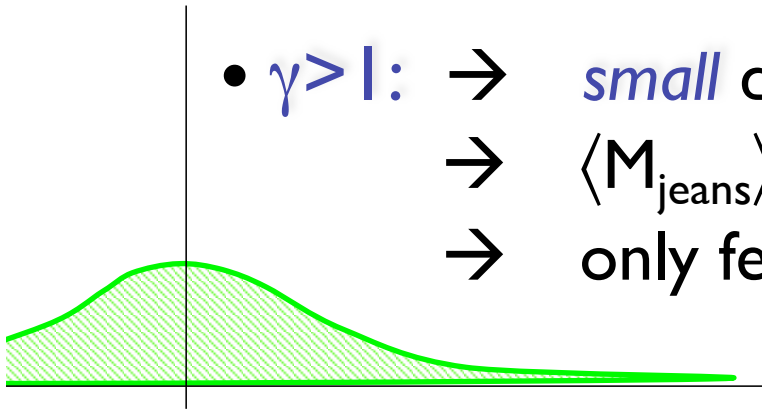
how does that work?

$$(1) \quad p \propto \rho^\gamma \quad \rightarrow \quad \rho \propto p^{1/\gamma}$$

$$(2) \quad M_{\text{jeans}} \propto \gamma^{3/2} \rho^{(3\gamma-4)/2}$$

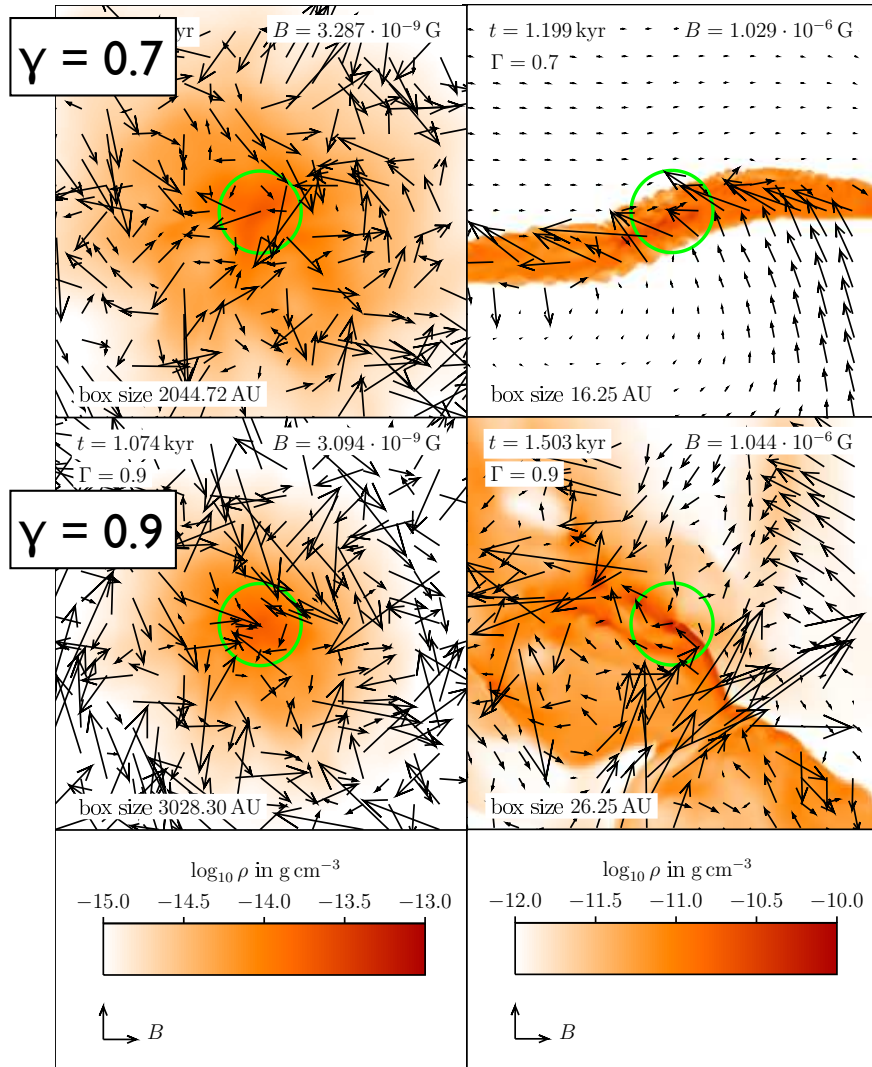


- $\gamma < 1$: \rightarrow *large* density excursion for given pressure
 - \rightarrow $\langle M_{\text{jeans}} \rangle$ becomes small
 - \rightarrow number of fluctuations with $M > M_{\text{jeans}}$ is large

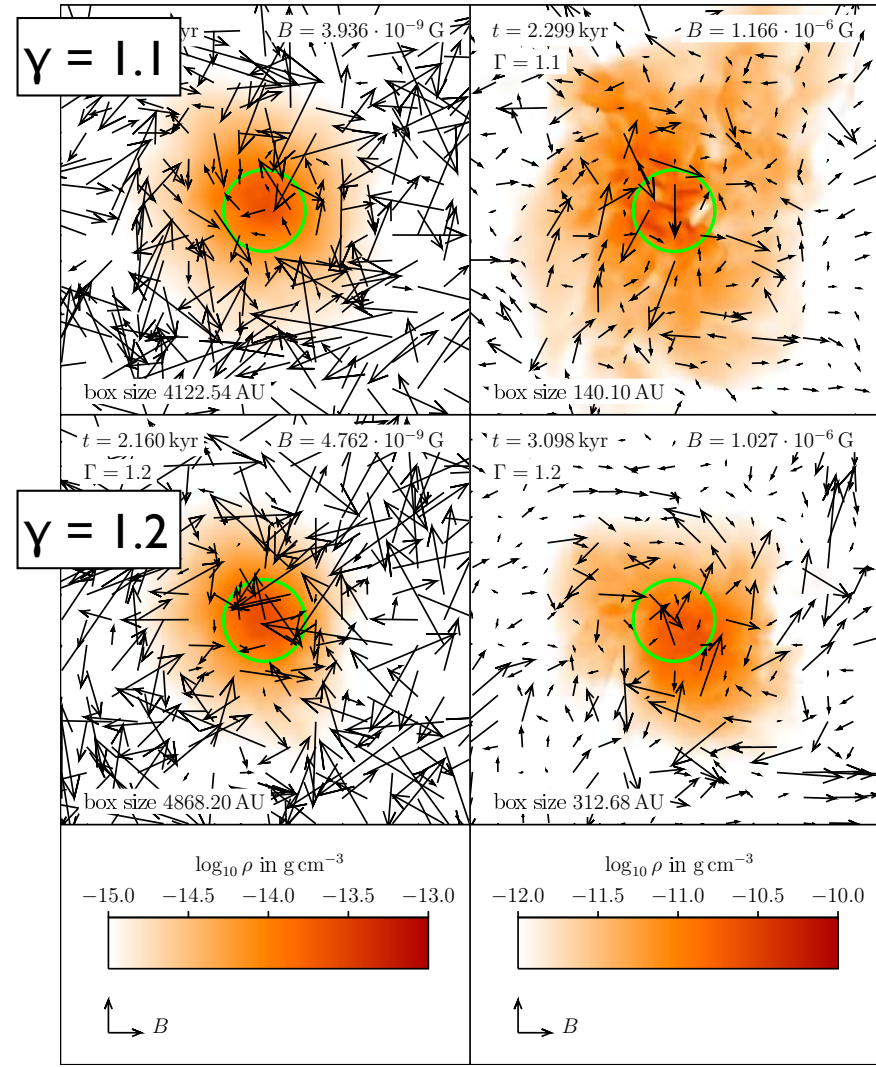


- $\gamma > 1$: \rightarrow *small* density excursion for given pressure
 - \rightarrow $\langle M_{\text{jeans}} \rangle$ is large
 - \rightarrow only few and massive clumps exceed M_{jeans}

gas cools when compressed

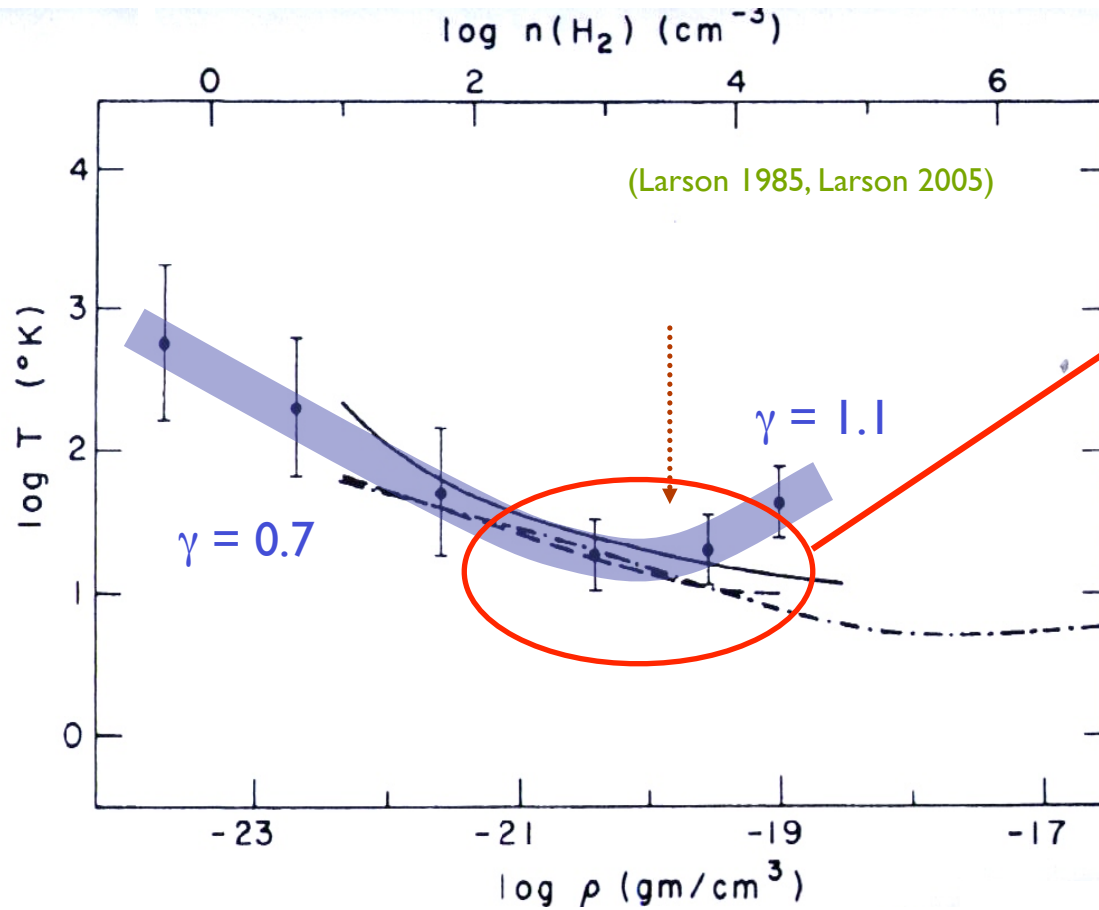


gas heats up when compressed



— filaments form easier in a cooling regime ($\gamma < 1$)
 as the pressure drops when the density increases
 — relevance for Herschel filaments?

SF in present-day IMF



ON THE CONSTANCY OF THE CHARACTERISTIC MASS OF YOUNG STARS

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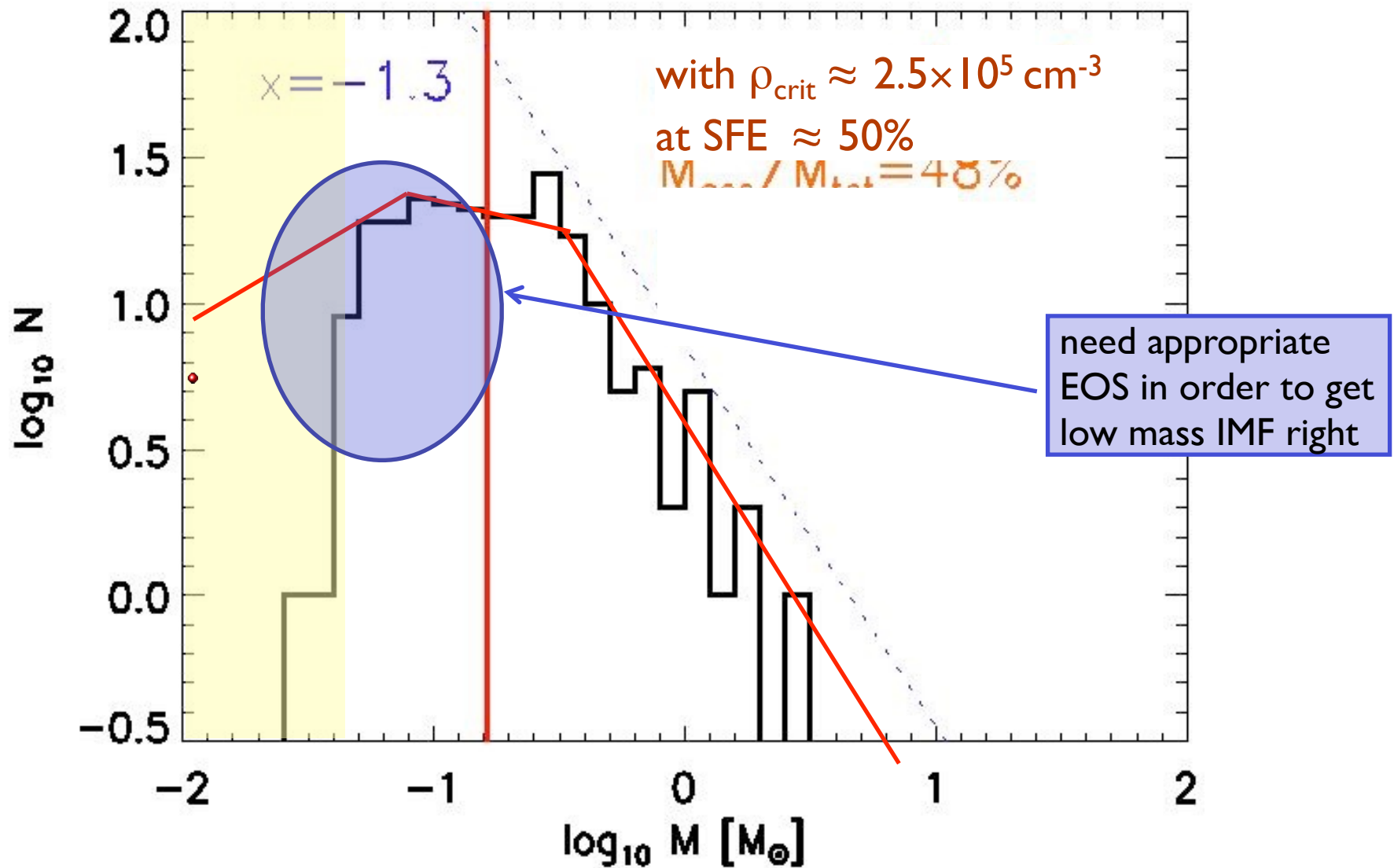
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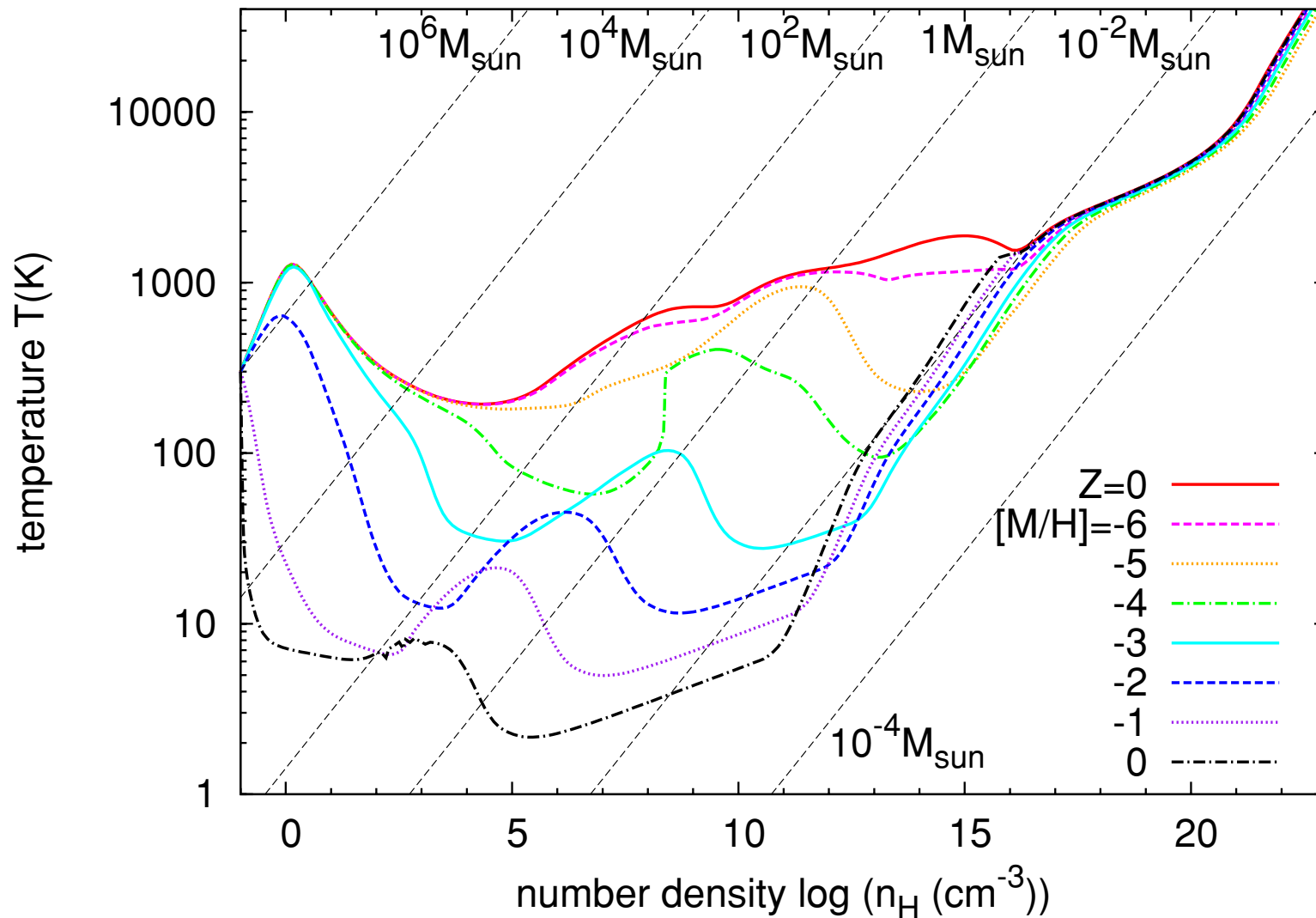
Subject headings: dust, extinction — stars: formation — stars: luminosity function, mass function

(Elmegreen et al. 2008)

SF in present-day IMF

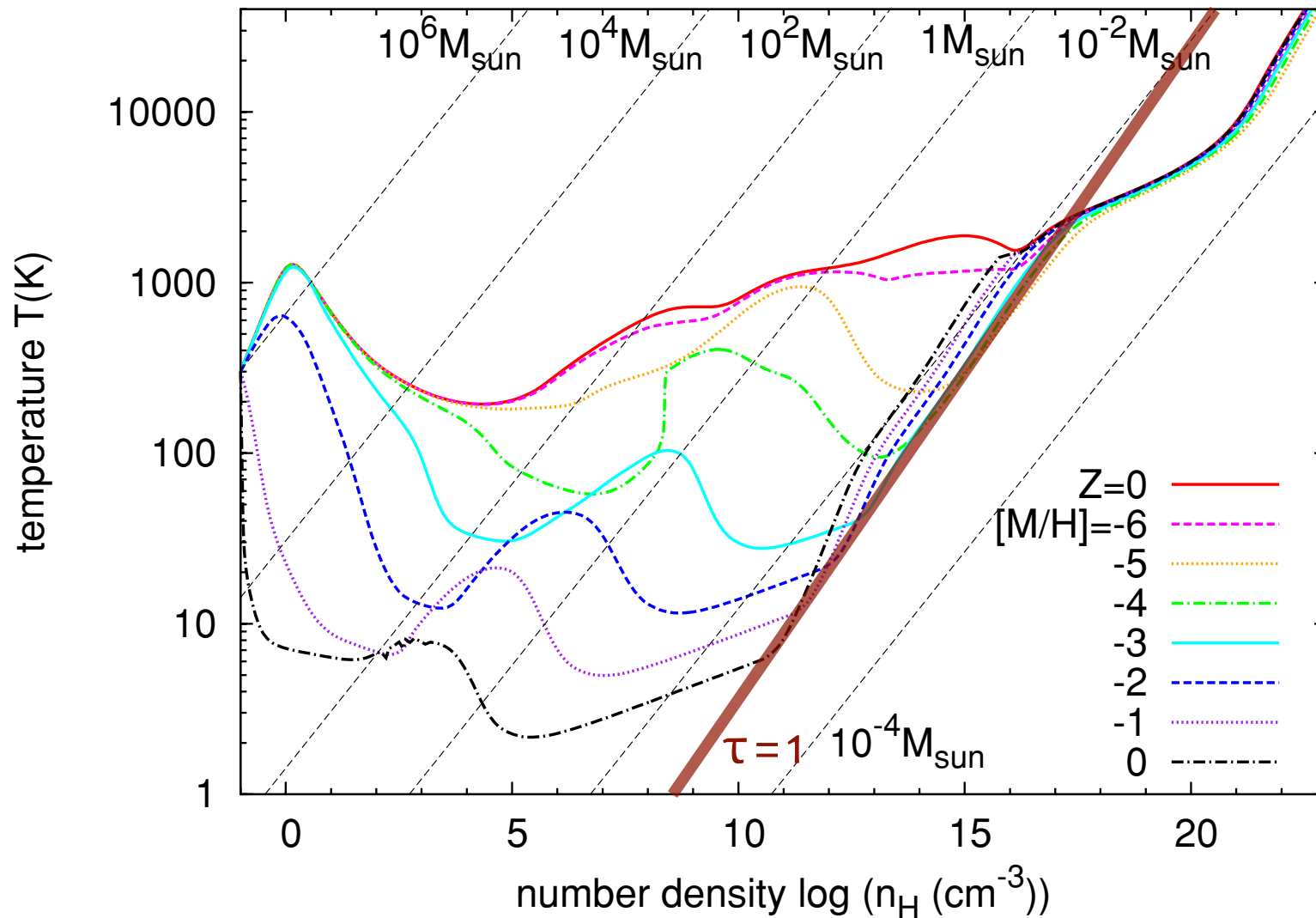


EOS as function of metallicity



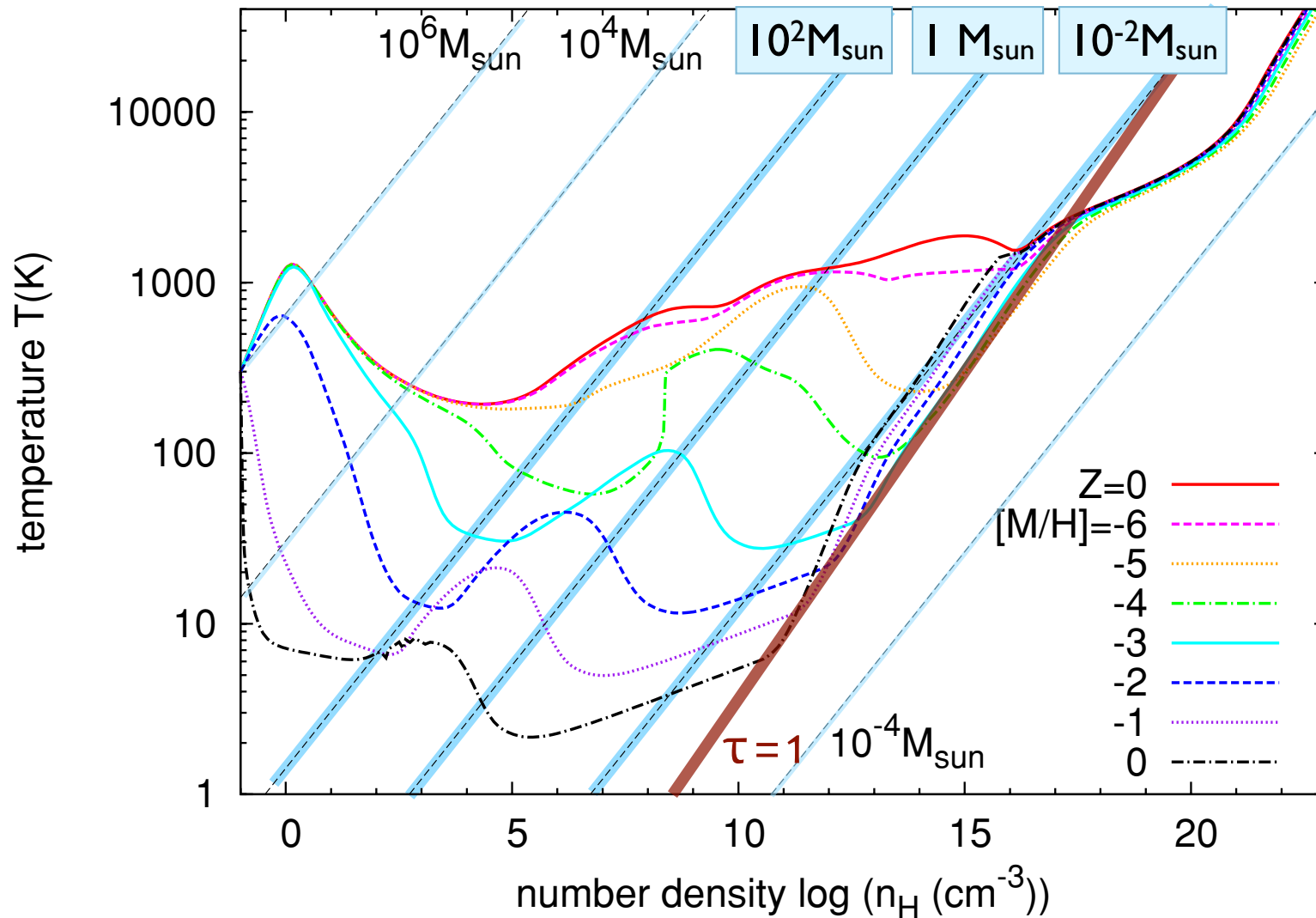
(Omukai et al. 2005, 2010)

EOS as function of metallicity



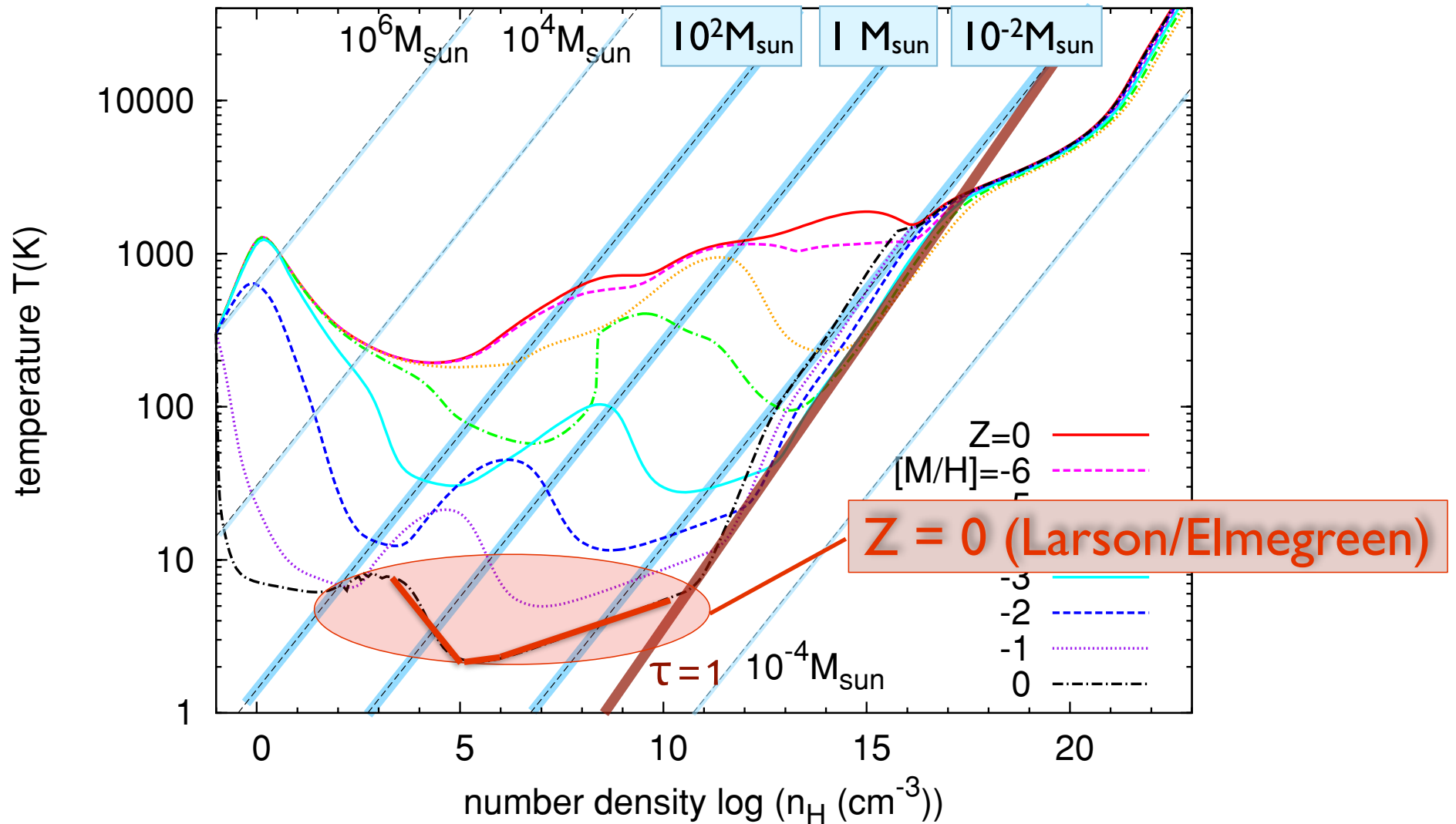
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EOS as function of metallicity



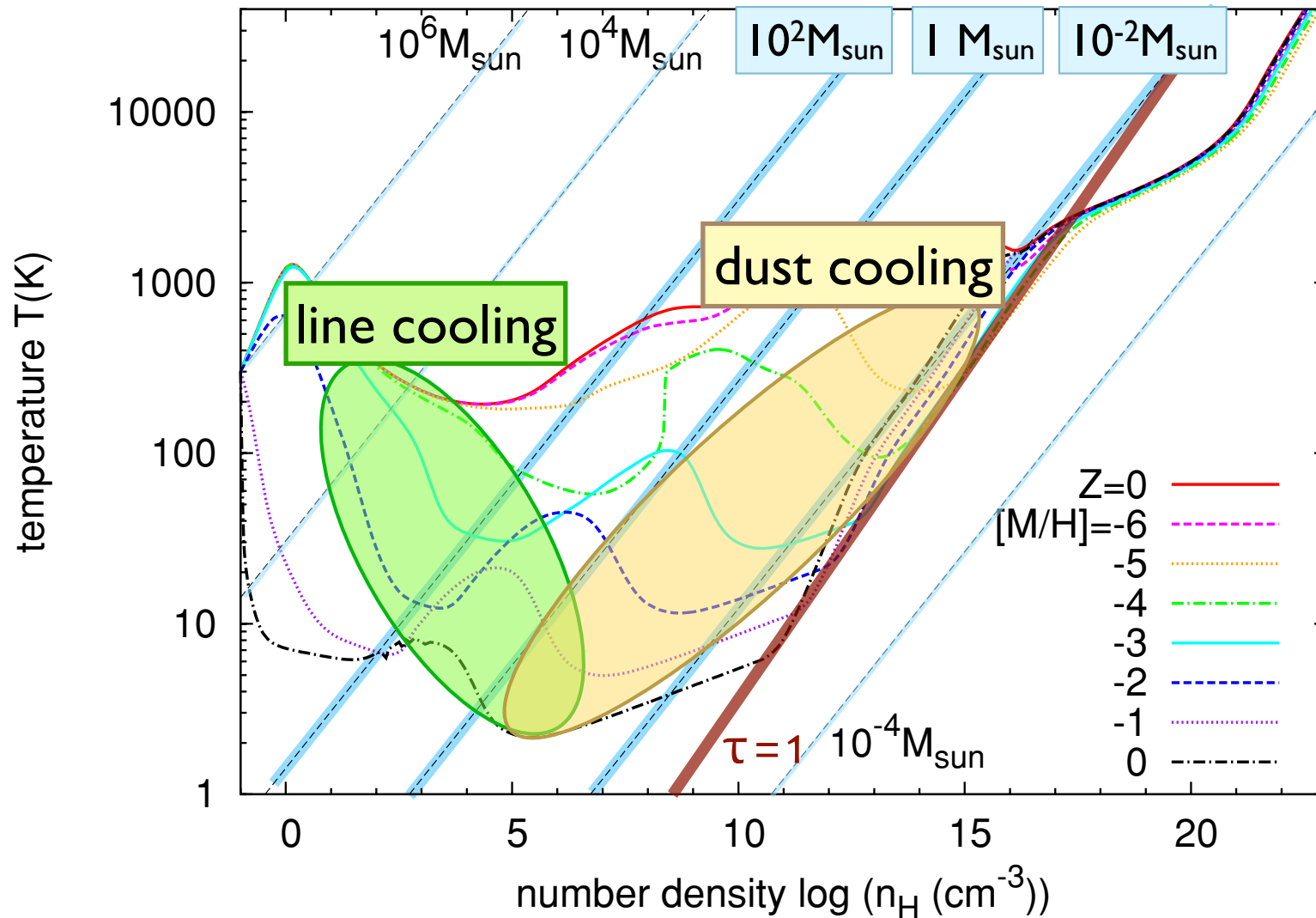
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EOS as function of metallicity



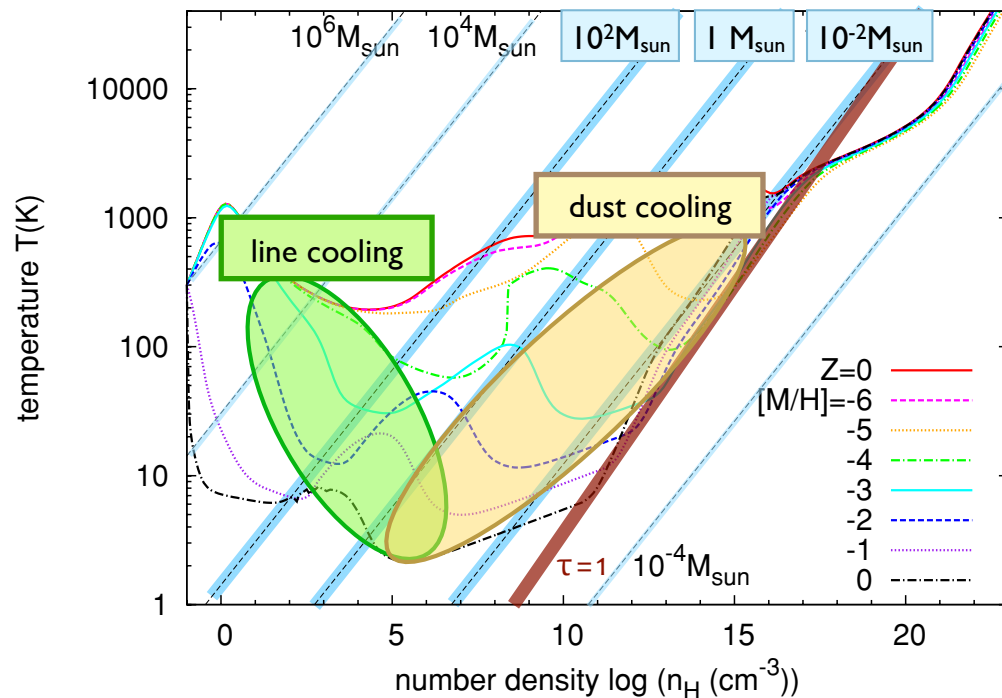
(Omukai et al. 2005, 2010)

EOS as function of metallicity



(Omukai et al. 2005, 2010)

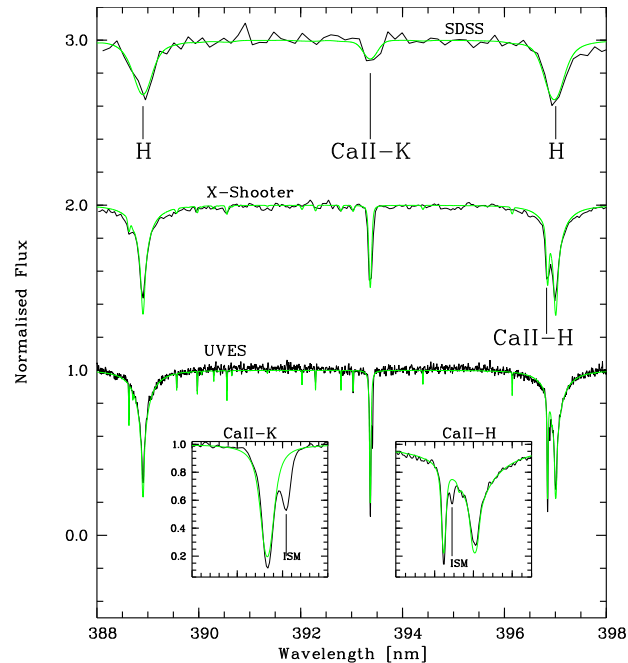
transition: Pop III to Pop II.5



two competing models:

- cooling due to atomic fine-structure lines ($Z > 10^{-3.5} Z_{\text{sun}}$)
- cooling due to coupling between gas and dust ($Z > 10^{-5 \dots -6} Z_{\text{sun}}$)
- which one explains origin of extremely metal-poor stars?
NB: lines would only make very massive stars, with $M > \text{few} \times 10 M_{\text{sun}}$.

transition: Pop III to Pop II.5



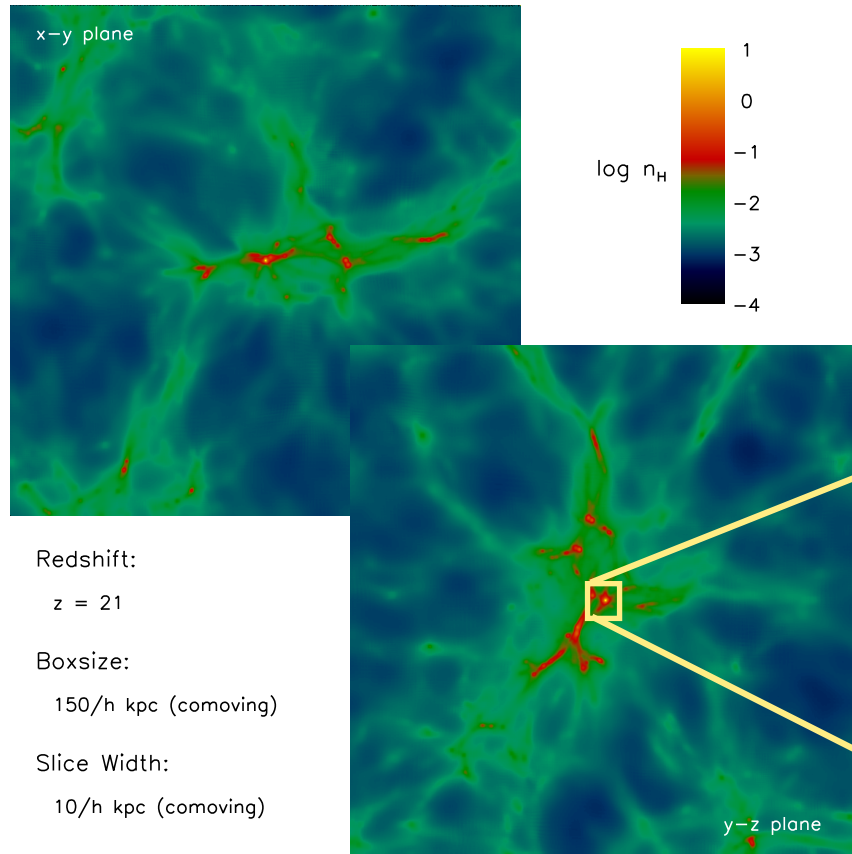
SDSS J1029151+172927

- is first ultra metal-poor star with $Z \sim 10^{-4.5} Z_{\text{sun}}$ for all metals seen (Fe, C, N, etc.)
[see Caffau et al. 2011]
- this is in regime, where metal-lines cannot provide cooling
[e.g. Schneider et al. 2011, 2012, Klessen et al. 2012]

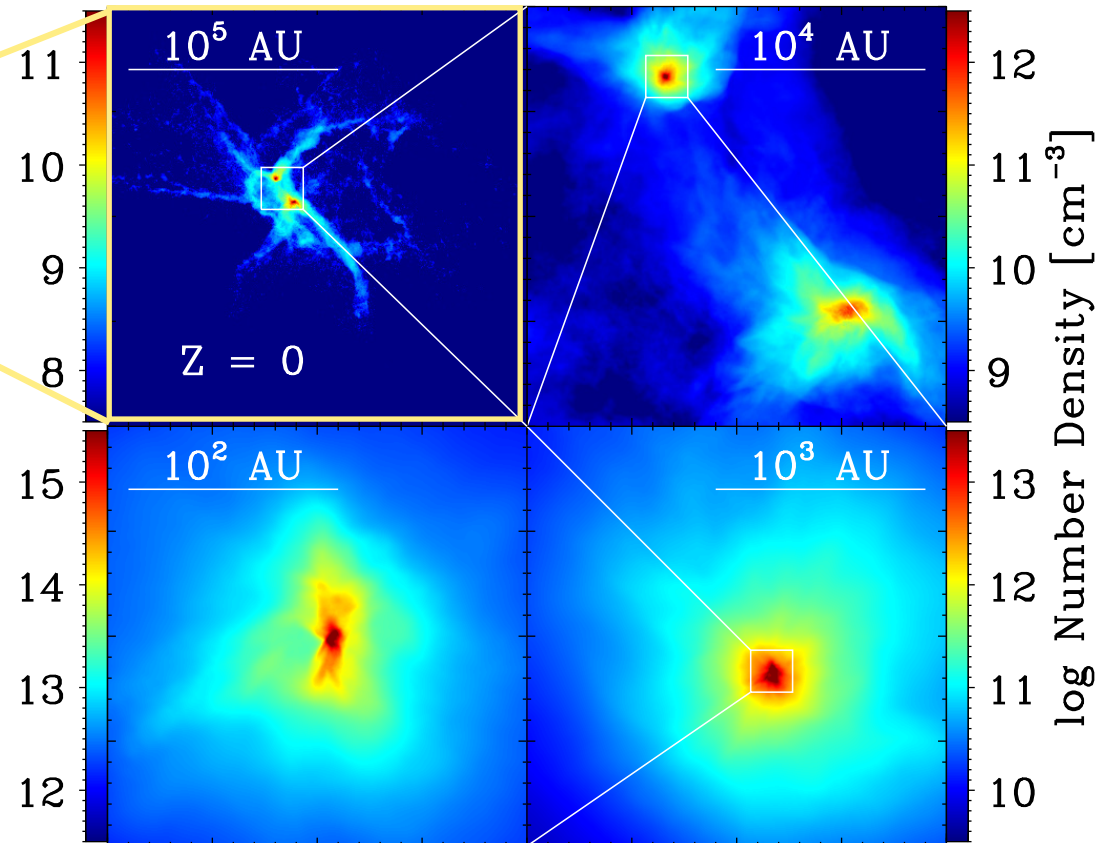
Element		[X/H] _{1D}		N lines	S _H	A(X) _⊙
	+3Dcor.	+NLTE cor.	+ 3D cor + NLTE cor			
C	≤ -3.8	≤ -4.5		G-band		8.50
N	≤ -4.1	≤ -5.0		NH-band		7.86
Mg I	-4.71 ± 0.11	-4.68 ± 0.11	-4.52 ± 0.11	5	0.1	7.54
Si I	-4.27	-4.30	-3.93	1	0.1	7.52
Ca I	-4.72	-4.82	-4.44	1	0.1	6.33
Ca II	-4.81 ± 0.11	-4.93 ± 0.03	-5.02 ± 0.02	3	0.1	6.33
Ti II	-4.75 ± 0.18	-4.83 ± 0.16	-4.76 ± 0.18	6	1.0	4.90
Fe I	-4.73 ± 0.13	-5.02 ± 0.10	-4.60 ± 0.13	43	1.0	7.52
Ni I	-4.55 ± 0.14	-4.90 ± 0.11		10		6.23
Sr II	≤ -5.10	≤ -5.25	≤ -4.94	1	0.01	2.92

- TOPoS: ESO large program to find more of these stars (120h x-shooter, 30h UVES) [PI E. Caffau]
- first paper out, more come soon ...

modeling the formation of the first/second stars



successive zoom-in calculation from cosmological initial conditions (using SPH and new grid-code AREPO)

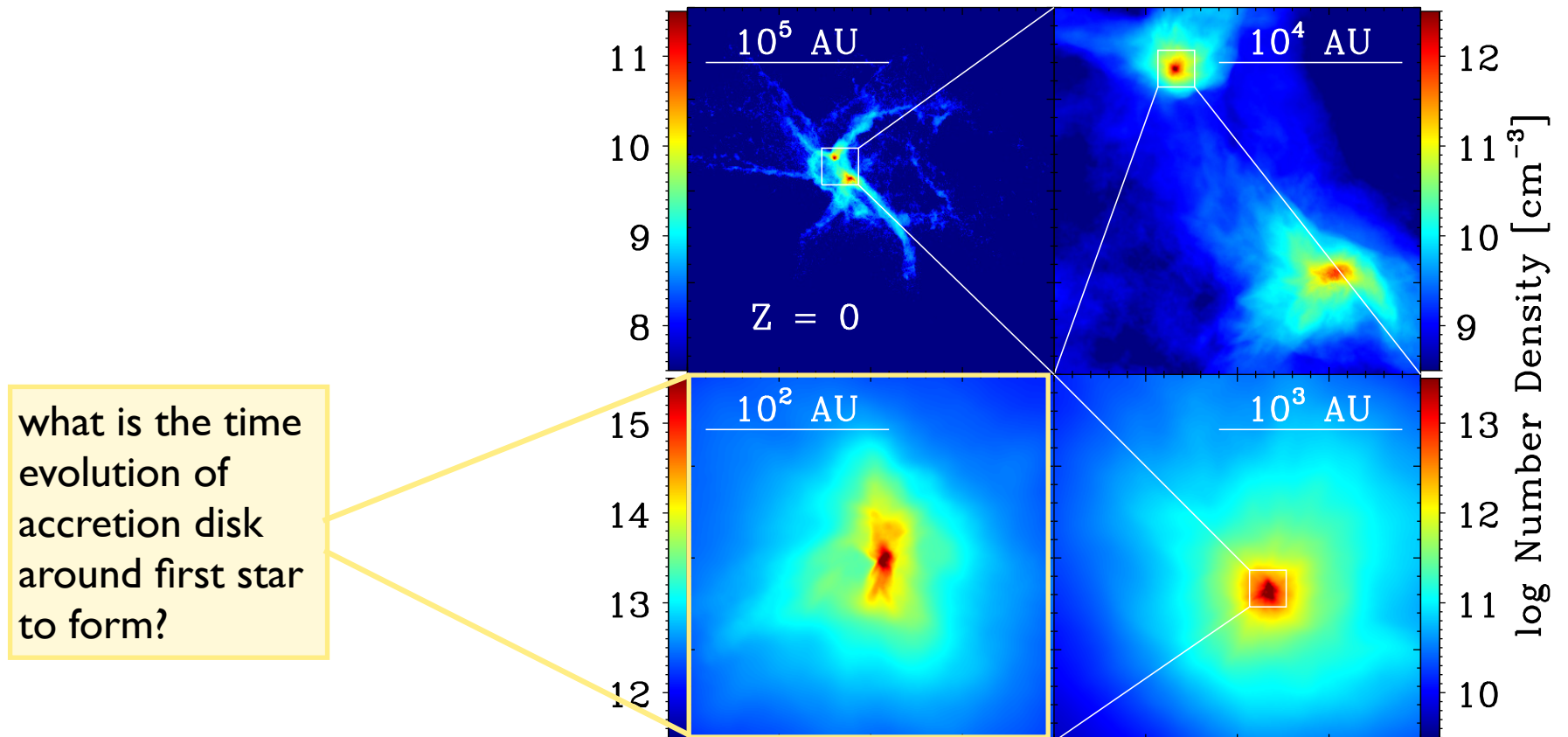


(Greif et al., 2007, ApJ, 670, 1)

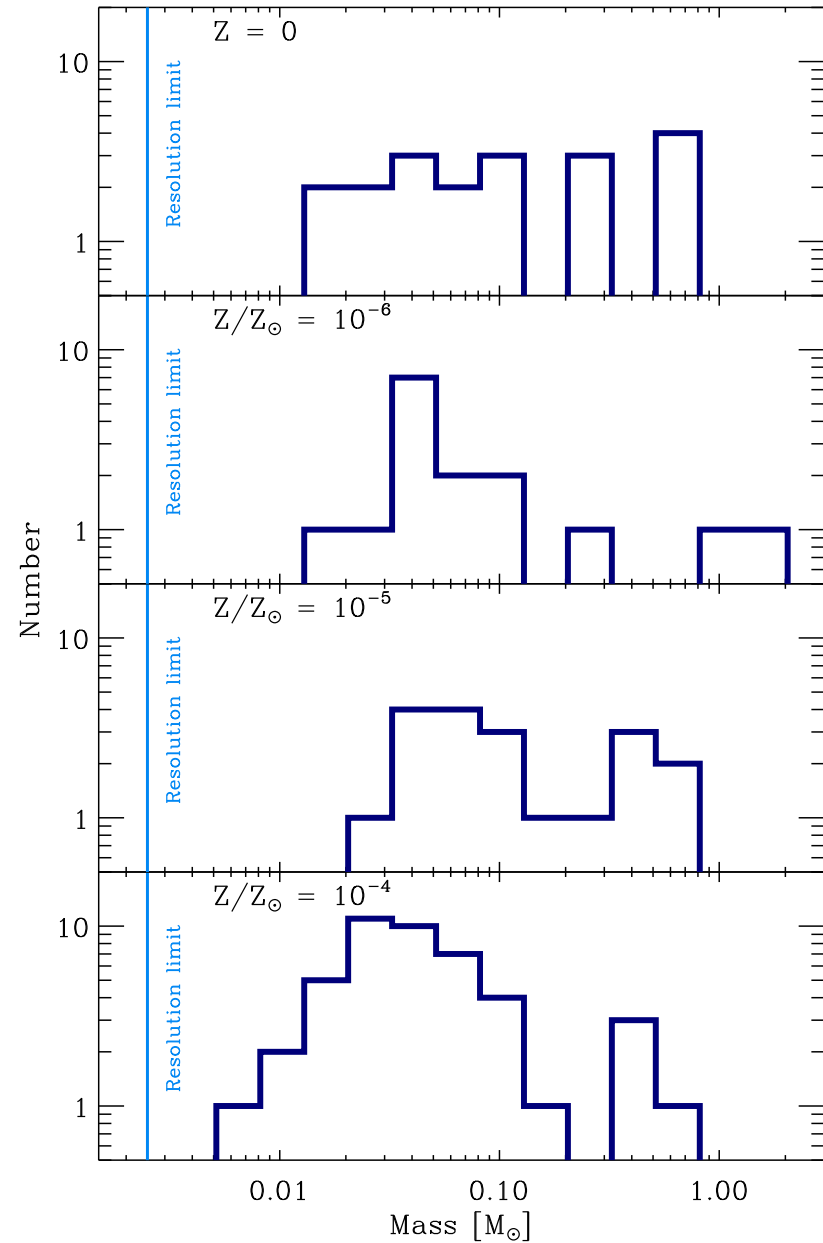
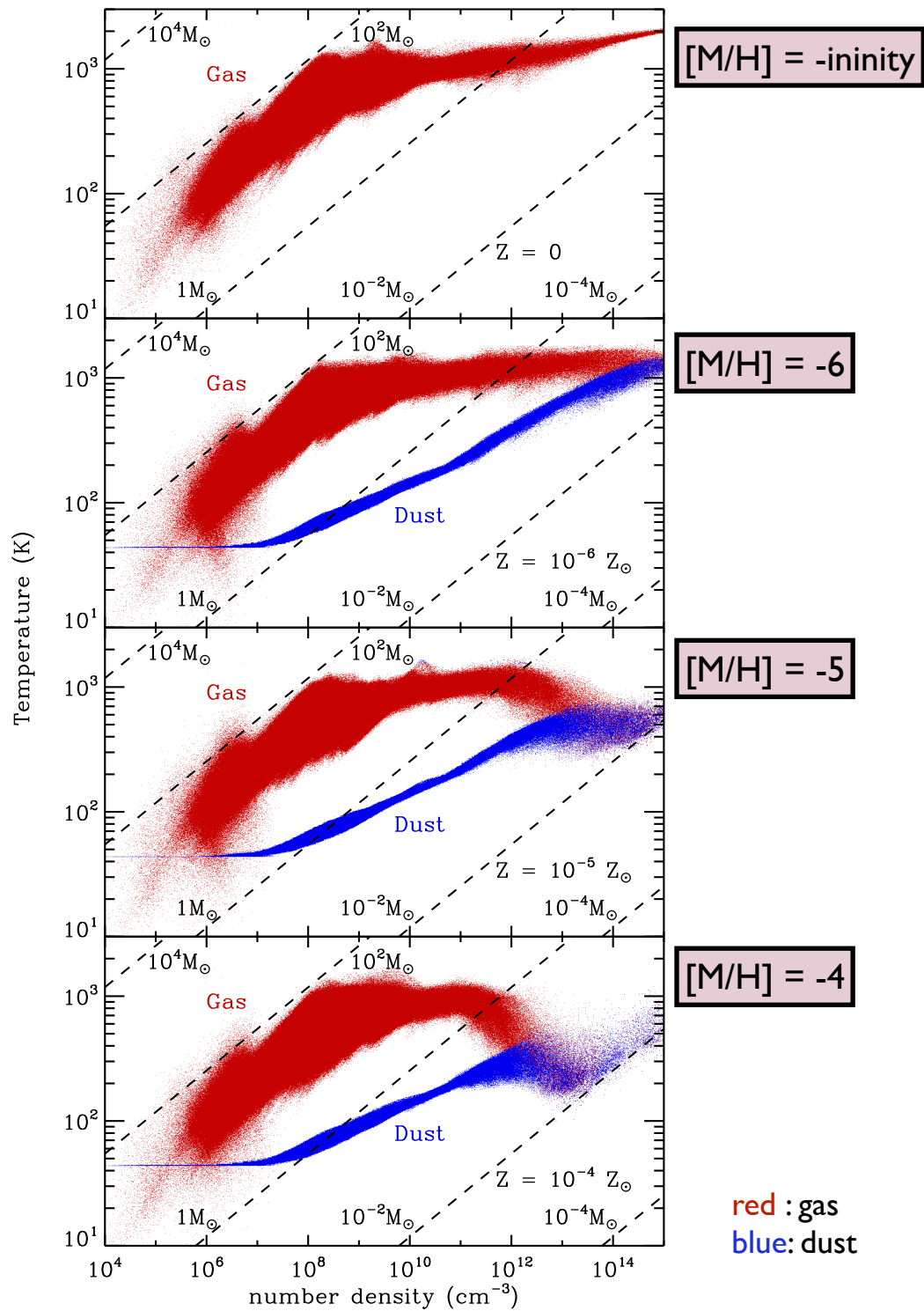
(Greif et al. 2011, ApJ, 737, 75, Greif et al. 2012, MNRAS, 424, 399, Dopcke et al. 2013, ApJ, 776, 103)

modeling the formation of the first/second stars

successive zoom-in calculation from cosmological initial conditions (using SPH and new grid-code AREPO)



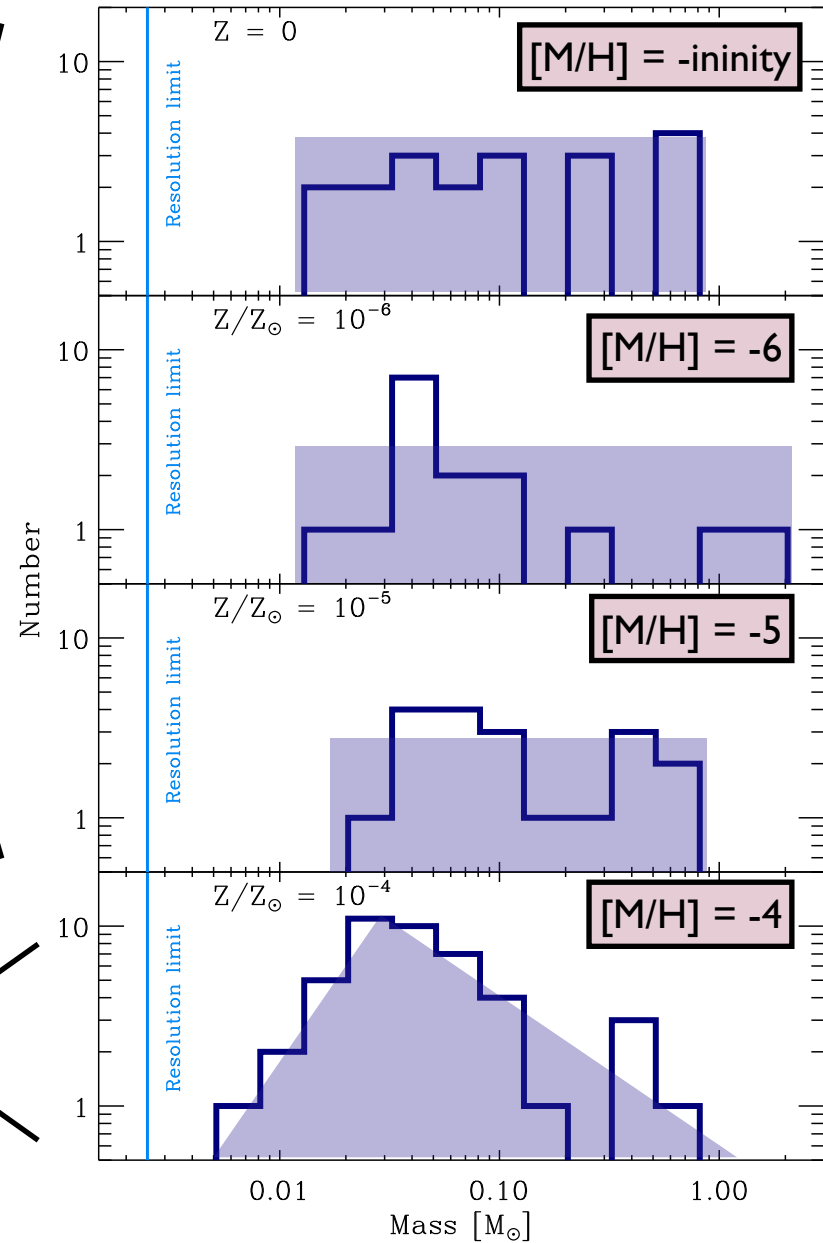
(Greif et al. 2011, ApJ, 737, 75, Greif et al. 2012, MNRAS, 424, 399, Dopcke et al. 2013, ApJ, 776, 103)

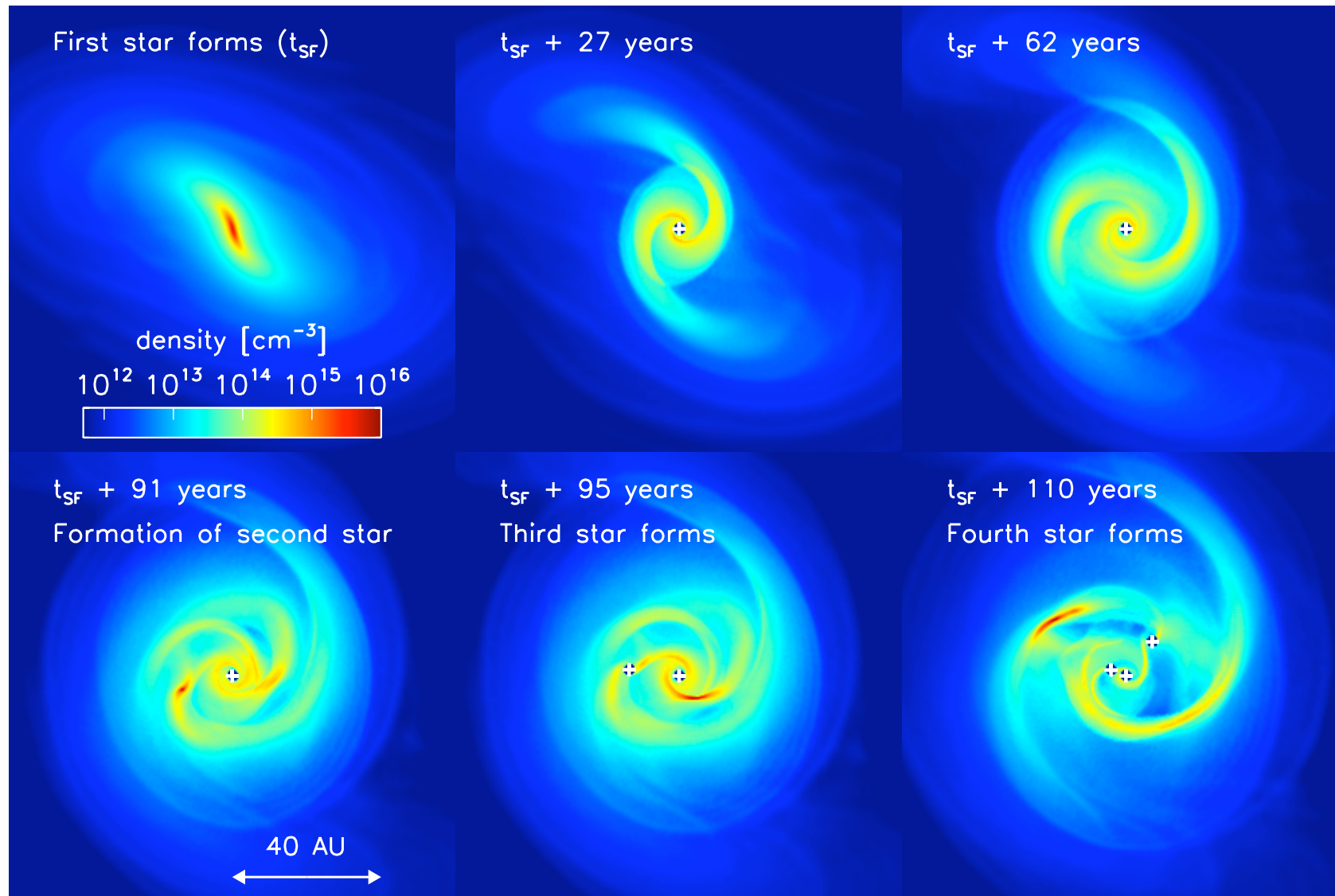


hints for differences
in mass spectrum

disk fragmentation mode

gravoturbulent fragmentation mode

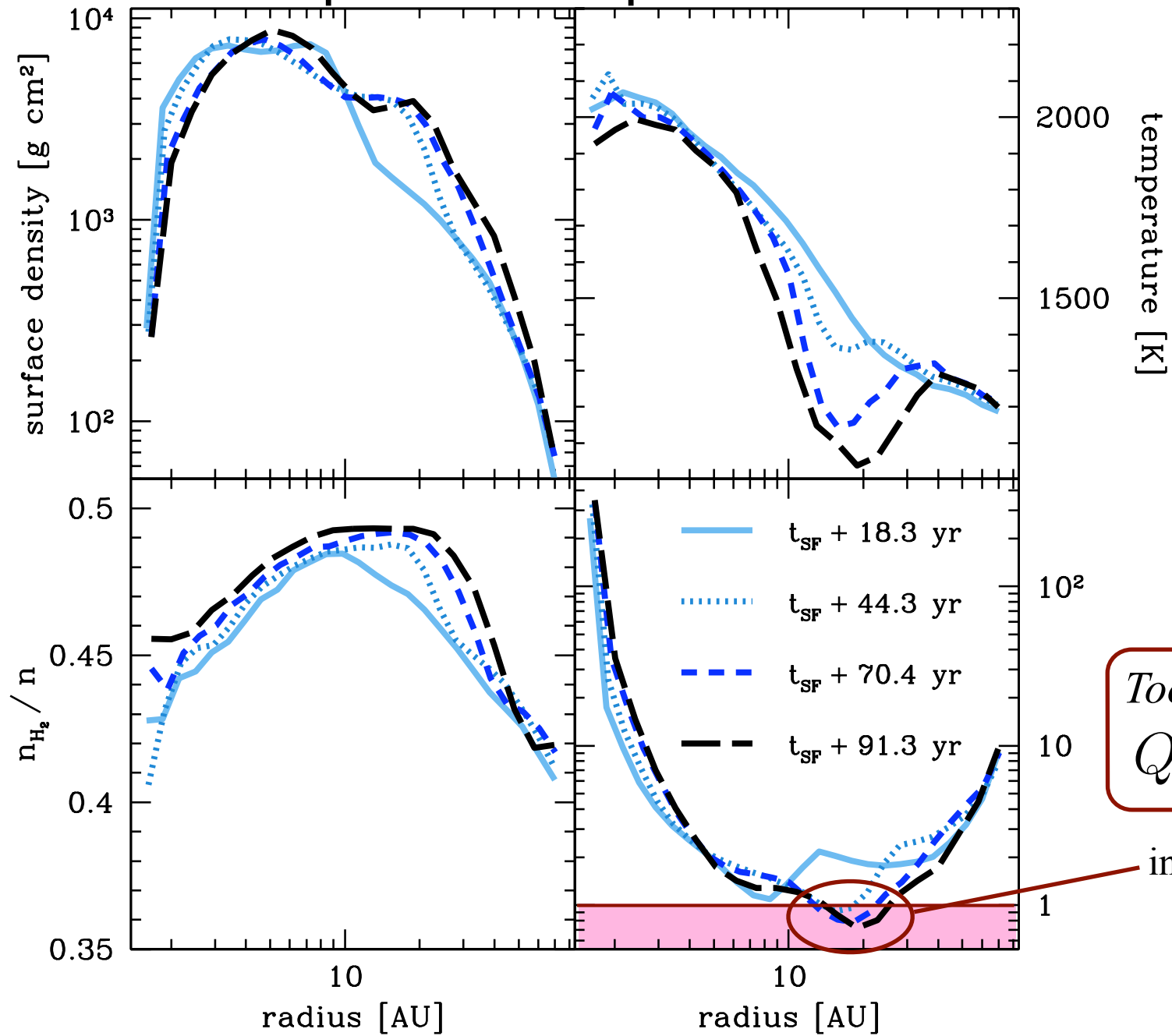




detailed look at accretion disk

Figure 1: Density evolution in a 120 AU region around the first protostar, showing the build-up of the protostellar disk and its eventual fragmentation. We also see ‘wakes’ in the low-density regions, produced by the previous passage of the spiral arms.

important disk parameters



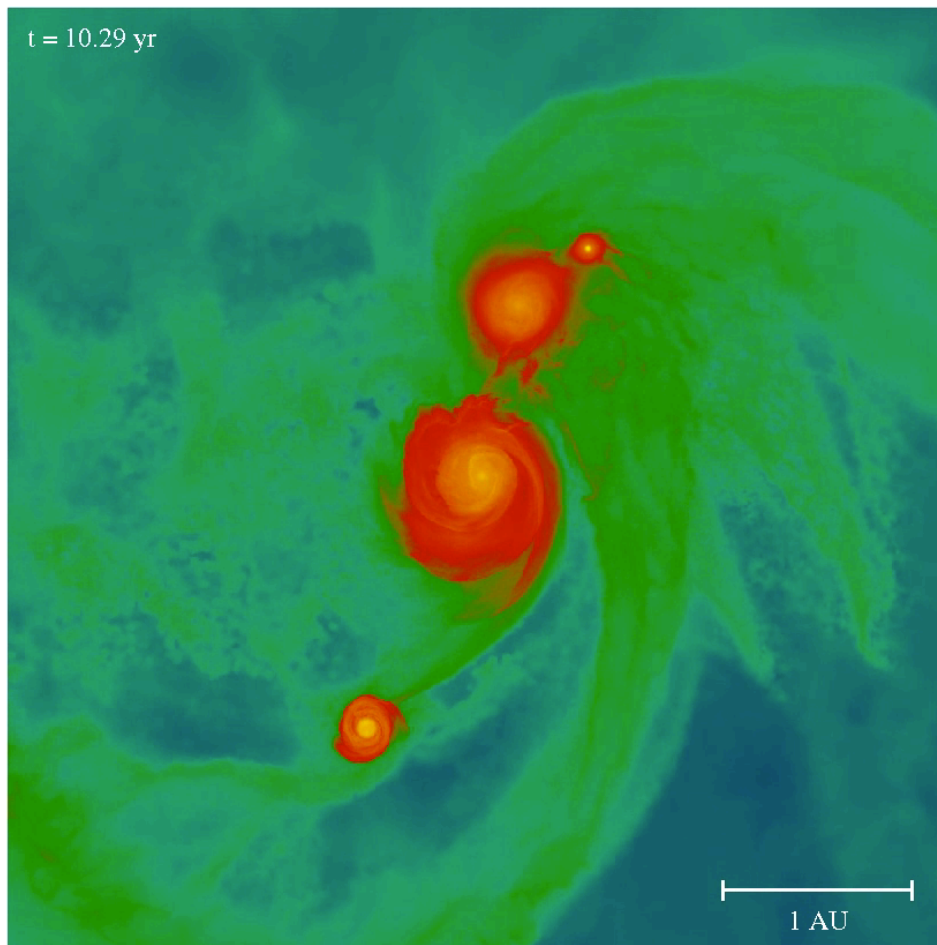
Toomre Q:

$$Q = c_s \kappa / \pi G \Sigma$$

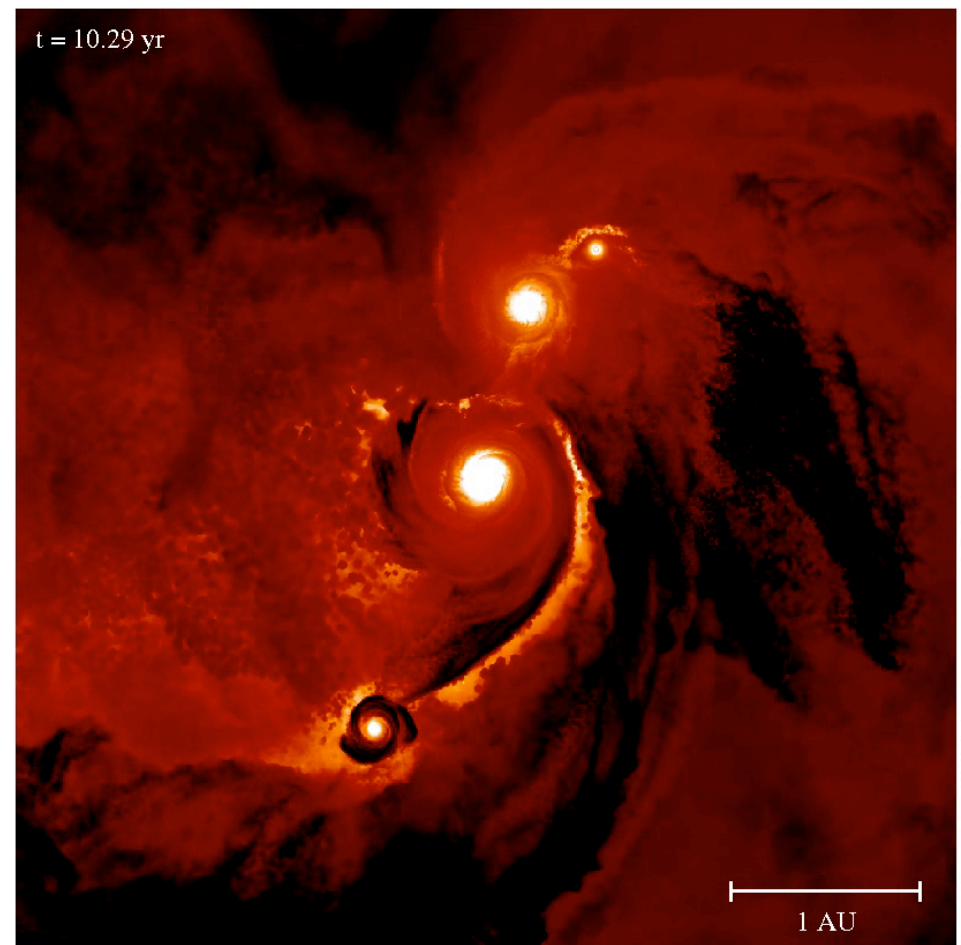
instability for $Q < 1$

Most recent calculations:

*fully sink-less simulations, following the disk build-up over ~ 10 years
(resolving the protostars - first cores - down to 10^5 km $\sim 0.01 R_{\odot}$)*



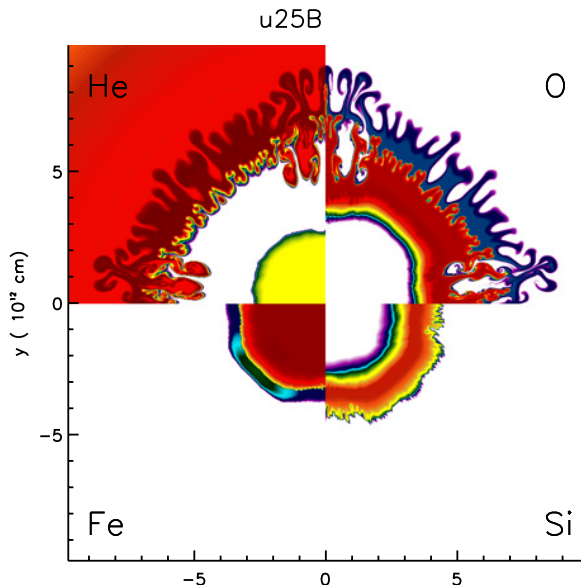
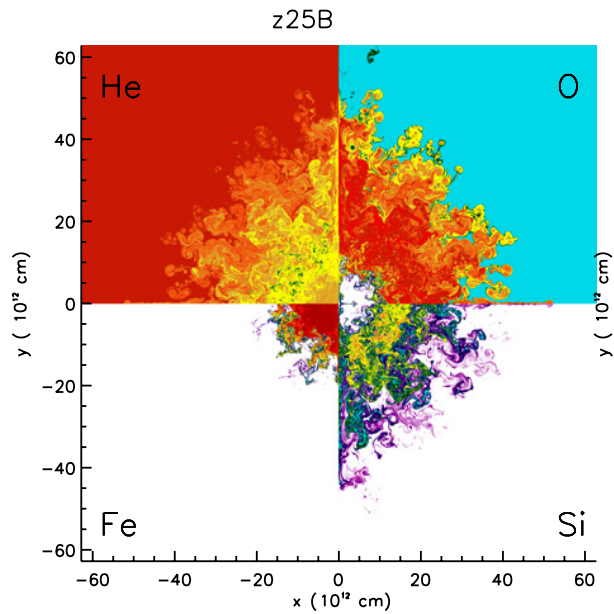
density



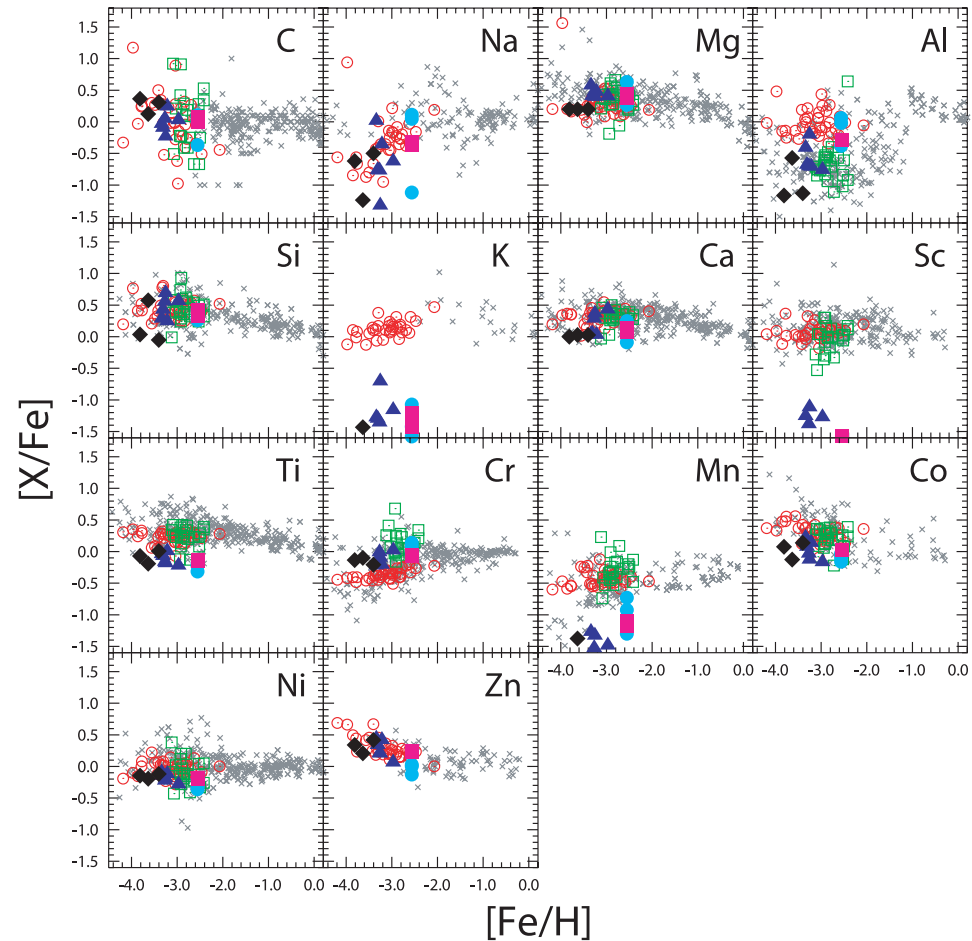
temperature

expected mass spectrum

- *expected IMF is flat* and covers a wide range of masses
- implications
 - because slope > -2 , most *mass is in massive objects* as predicted by most previous calculations
 - most high-mass Pop III stars should be in *binary systems* --> source of *high-redshift gamma-ray bursts*
 - because of ejection, some *low-mass objects* ($< 0.8 M_{\odot}$) might have *survived* until today and could potentially be found in the Milky Way
- consistent with abundance patterns found in second generation stars



(Joggerst et al. 2009, 2010)



(Tominaga et al. 2007)

The metallicities of extremely metal-poor stars in the halo are consistent with the yields of core-collapse supernovae, i.e. progenitor stars with 20 - 40 M_{\odot}

(e.g. Tominaga et al. 2007, Izutani et al. 2009, Joggerst et al. 2009, 2010)

predicting number of Pop III stars

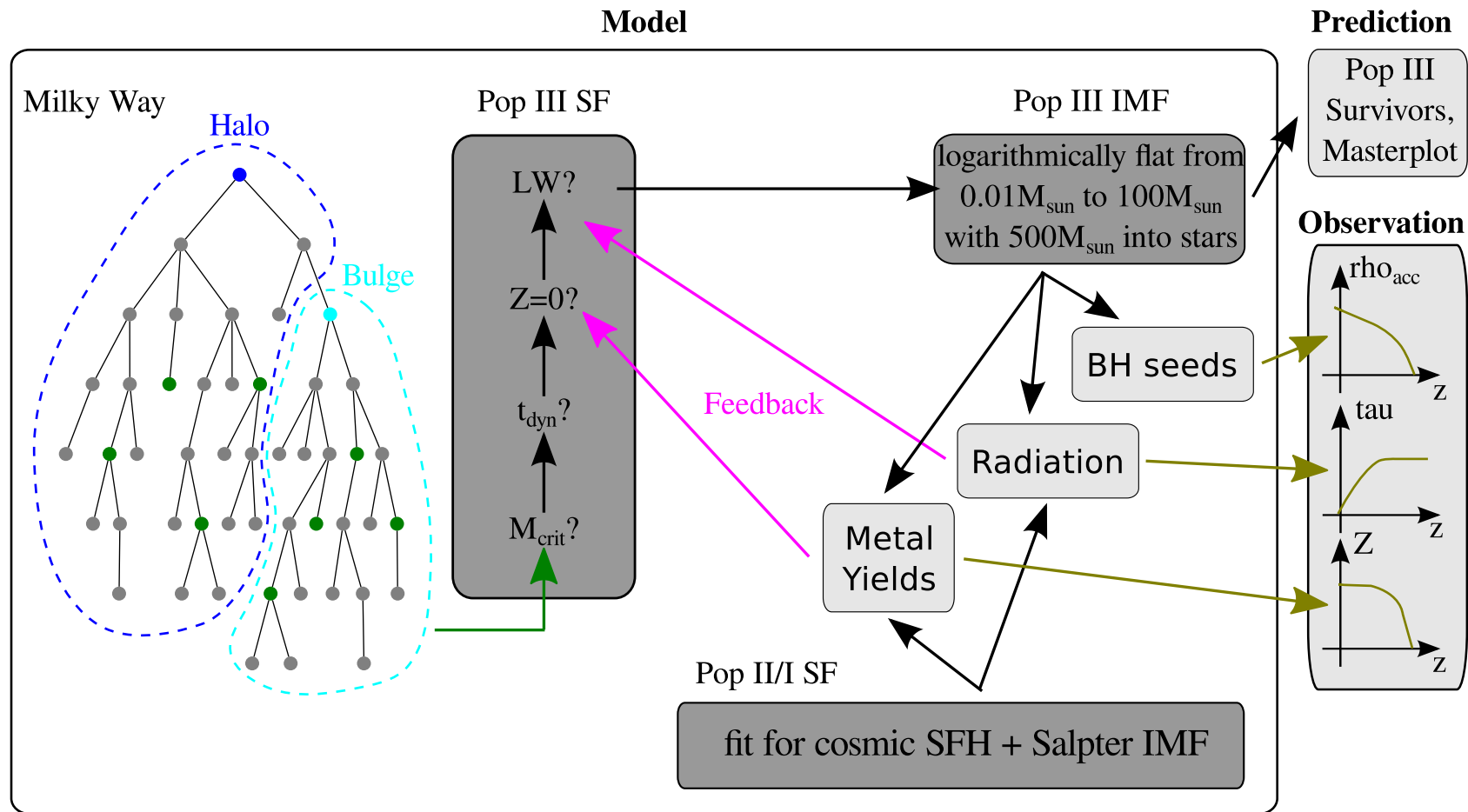


Figure 1. Illustration of the model we use. Based on the merger tree, we check which halos are able to form Pop III stars based on their critical mass, the absence of dynamical heating due to mergers, no pollution by metals and the strength of the LW background. We assign an individual number of Pop III stars to each successful halo and determine the influence on their environment. The influence of Pop I/II star formation is modelled based on the cosmic star formation history. By comparing these influences to existing observations, we can gauge our model assumptions. Finally, we derive a prediction for the number of Pop III survivors in the Milky Way and determine constraints to the primordial IMF. Tilman: too many arrows - probably combine BH seeds, Radiation and Metal Yields?

predicting number of Pop III stars

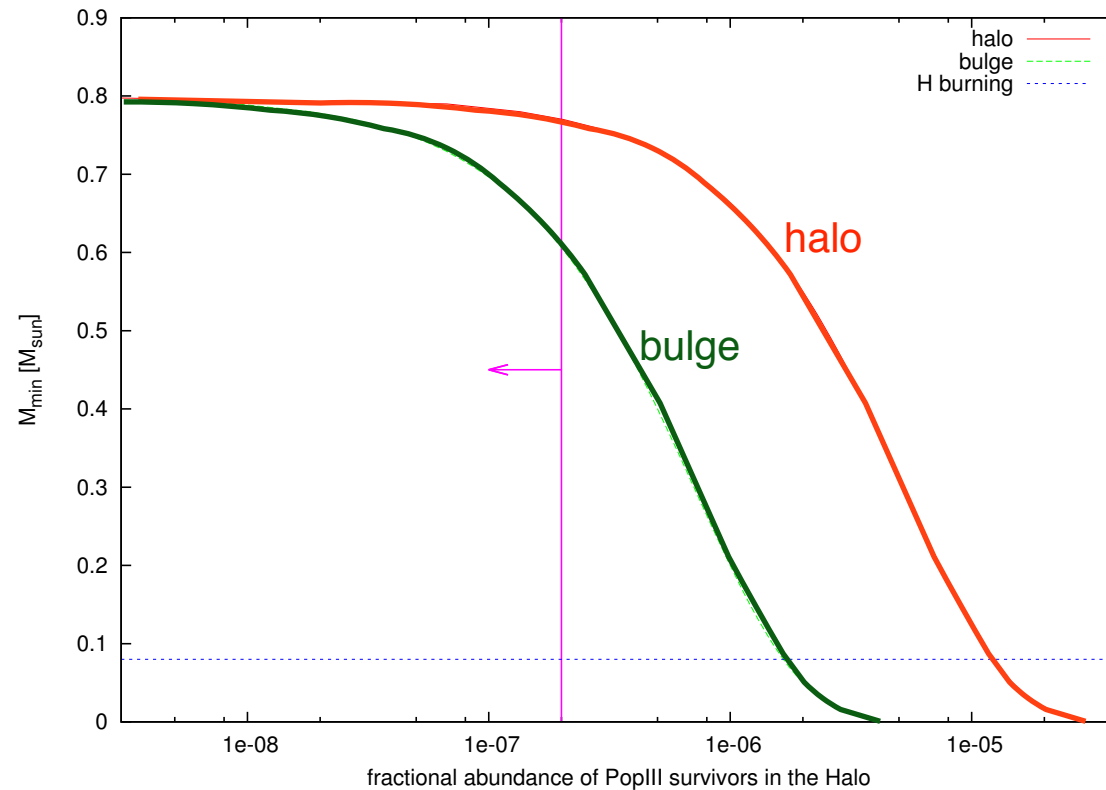


Figure 9: Expected lower mass of the primordial IMF as a function of the fractional abundance of Pop III survivors. The purple line indicates an upper limit for the fractional abundance based on current observational sample sizes. Whereas this sample only covers the halo and is therefore not valid for the bulge. Bulge values are wrong (see above)!

reducing fragmentation

- from present-day star formation theory we know, that
 - magnetic fields: Peters et al. 2011, Seifried et al. 2012, Hennebelle et al. 2011
 - accretion heating: Peters et al. 2010, Krumholz et al. 2009, Kuipers et al. 2011can influence the fragmentation behavior.
- in the context of Pop III
 - radiation: Hosokawa et al. 2012, Stacy et al. 2012a
 - magnetic fields: Turk et al. 2012, but see also Bovino et al. 2013
Schleicher et al. 2010, Sur et al. 2010, Federrath et al. 2011, Schober et al. 2012ab, 2013
- all these will reduce degree of fragmentation
(but not by much, see Rowan Smith et al. 2011, 2012, at least for accretion heating)
- DM annihilation might become important for disk dynamics and fragmentation (Ripamonti et al. 2011, Stacy et al. 2012b, Rowan Smith et al. 2012)

summary

- stars form in the ISM from the **complex interplay** of **self-gravity** and a large number of competing processes (such as **turbulence, B-field, feedback, thermal pressure**)
- **thermodynamic properties** of the gas (heating vs cooling) play a key role in the star formation process
- detailed studies require the **consistent treatment** of many **different physical processes** (this is a theoretical and computational challenge)
- **primordial star formation** shares the **same complexities** as present-day star formation

thanks to ...



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... many collaborators abroad!



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