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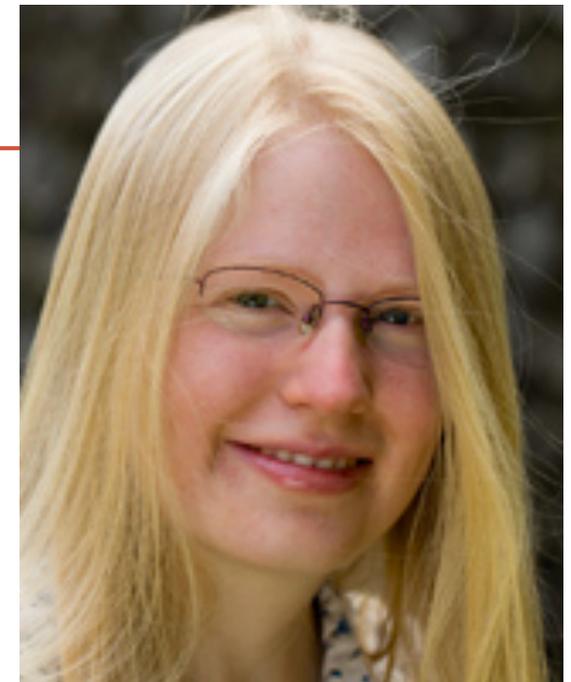


# SIMULATING FILAMENTARY STAR FORMATION

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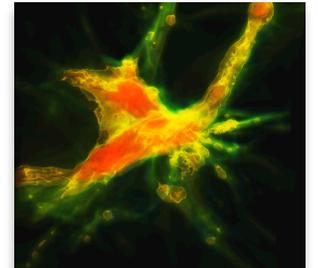
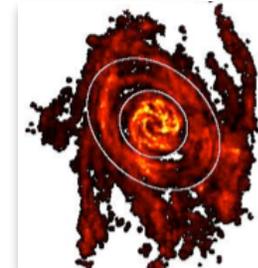
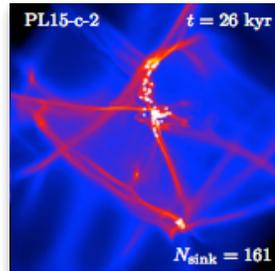
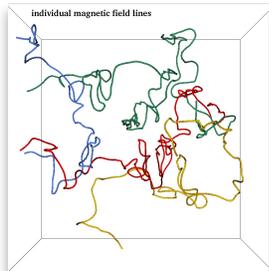
Rowan Smith

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*Simon Glover, Ralf Klessen, Adam Avison, Henrik Beuther, Gary Fuller, Volker Springel*

# High Mass and Clustered Star Formation: Simulations



**Ralf Klessen**



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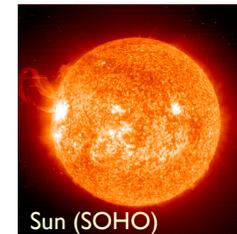
# agenda

- remarks on star formation theory
  - historic remarks
  - current understanding
- controversies / puzzles
  - column density PDFs: *do we really understand them?*
  - molecular gas: *are we sure we see all  $H_2$  gas?*
  - importance of dynamics: *what sets the IMF?*
  - filaments: *are they universal?*



theoretical  
remarks

decrease in spatial scale / increase in density



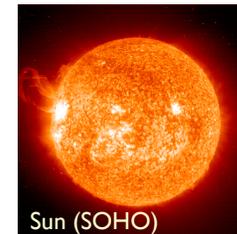
- density

- density of ISM: few particles per  $\text{cm}^3$
- density of molecular cloud: few 100 particles per  $\text{cm}^3$
- density of Sun:  $1.4 \text{ g/cm}^3$

- spatial scale

- size of molecular cloud: few 10s of pc
- size of young cluster:  $\sim 1 \text{ pc}$
- size of Sun:  $1.4 \times 10^{10} \text{ cm}$

decrease in spatial scale / increase in density



- contracting force
  - only force that can do this compression is **GRAVITY**
- opposing forces
  - there are several processes that can oppose gravity
  - **GAS PRESSURE**
  - **TURBULENCE**
  - **MAGNETIC FIELDS**
  - **RADIATION PRESSURE**

Modern star formation theory is based on the complex interplay between *all* these processes.

# early theoretical models

- *Jeans (1902)*: Interplay between self-gravity and thermal pressure
  - stability of homogeneous spherical density enhancements against gravitational collapse
  - dispersion relation:

$$\omega^2 = c_s^2 k^2 - 4\pi G \rho_0$$

- instability when  $\omega^2 < 0$

- minimal mass:  $M_J = \frac{1}{6} \pi^{-5/2} G^{-3/2} \rho_0^{-1/2} c_s^3 \propto \rho_0^{-1/2} T^{+3/2}$



Sir James Jeans, 1877 - 1946

# first approach to turbulence

- *von Weizsäcker (1943, 1951) and Chandrasekhar (1951): concept of **MICROTURBULENCE***

- BASIC ASSUMPTION: separation of scales between dynamics and turbulence

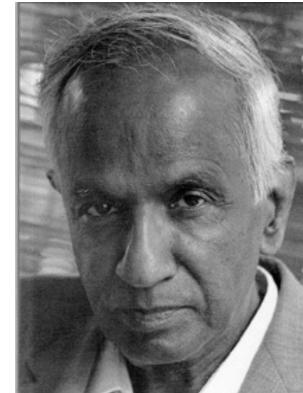
$$\ell_{\text{turb}} \ll \ell_{\text{dyn}}$$

- then turbulent velocity dispersion contributes to effective soundspeed:

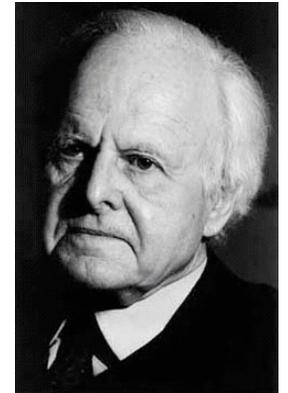
$$c_c^2 \mapsto c_c^2 + \sigma_{rms}^2$$

- $\rightarrow$  Larger effective Jeans masses  $\rightarrow$  more stability
- BUT: (1) turbulence depends on  $k$ :  $\sigma_{rms}^2(k)$

(2) supersonic turbulence  $\rightarrow \sigma_{rms}^2(k) \gg c_s^2$  usually



S. Chandrasekhar,  
1910 - 1995



C.F. von Weizsäcker,  
1912 - 2007

# problems of early dynamical theory

- molecular clouds are *highly Jeans-unstable*, yet, they do *NOT* form stars at high rate and with high efficiency (Zuckerman & Evans 1974 conundrum) (the observed global SFE in molecular clouds is  $\sim 5\%$ )  
→ *something prevents large-scale collapse.*
- all throughout the early 1990's, molecular clouds had been thought to be long-lived quasi-equilibrium entities.
- molecular clouds are *magnetized*

# magnetic star formation

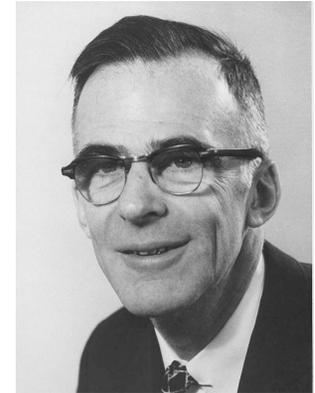
- *Mestel & Spitzer (1956)*: Magnetic fields can prevent collapse!!!
  - Critical mass for gravitational collapse in presence of B-field

$$M_{cr} = \frac{5^{3/2}}{48\pi^2} \frac{B^3}{G^{3/2} \rho^2}$$

- Critical mass-to-flux ratio (Mouschovias & Spitzer 1976)

$$\left[ \frac{M}{\Phi} \right]_{cr} = \frac{\xi}{3\pi} \left[ \frac{5}{G} \right]^{1/2}$$

- Ambipolar diffusion can initiate collapse



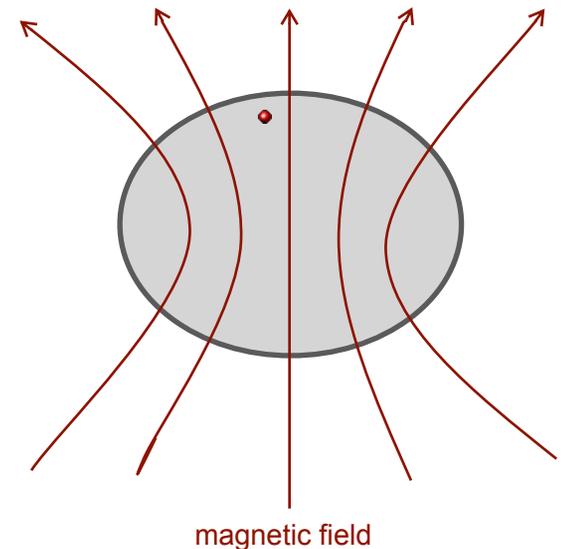
Lyman Spitzer, Jr., 1914 - 1997

# “standard theory” of star formation

- BASIC ASSUMPTION: Stars form from magnetically highly subcritical cores
- Ambipolar diffusion slowly increases  $(M/\Phi)$ :  $\tau_{AD} \approx 10\tau_{ff}$
- Once  $(M/\Phi) > (M/\Phi)_{crit}$  : dynamical collapse of SIS
  - Shu (1977) collapse solution
  - $dM/dt = 0.975 c_s^3/G = \text{const.}$
- Was (in principle) only intended for isolated, low-mass stars



Frank Shu, 1943 -



# problems of “standard theory”

- Observed B-fields are weak, at most marginally critical (Crutcher 1999, Bourke et al. 2001)
- Magnetic fields cannot prevent decay of turbulence (Mac Low et al. 1998, Stone et al. 1998, Padoan & Nordlund 1999)
- Structure of prestellar cores (e.g. Bacman et al. 2000, Alves et al. 2001)
- Strongly time varying  $dM/dt$  (e.g. Hendriksen et al. 1997, André et al. 2000)
- More extended infall motions than predicted by the standard model (Williams & Myers 2000, Myers et al. 2000)
- Most stars form as binaries (e.g. Lada 2006)
- As many prestellar cores as protostellar cores in SF regions (e.g. André et al 2002)
- Molecular cloud clumps are chemically young (Bergin & Langer 1997, Pratap et al 1997, Aikawa et al 2001)
- Stellar age distribution small ( $\tau_{\text{ff}} \ll \tau_{\text{AD}}$ ) (Ballesteros-Paredes et al. 1999, Elmegreen 2000, Hartmann 2001)
- Strong theoretical criticism of the SIS as starting condition for gravitational collapse (e.g. Whitworth et al 1996, Nakano 1998, as summarized in Klessen & Mac Low 2004)
- Standard AD-dominated theory is incompatible with observations (Crutcher et al. 2009, 2010ab, Bertram et al. 2011)

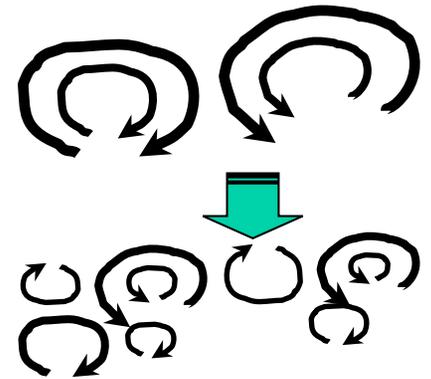
(see e.g. Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125-194, Klessen & Glover 2014, Saas Fee Lecture, arXiv:1412.5182, 1-191)

# properties of turbulence

- laminar flows turn *turbulent* at *high Reynolds numbers*

$$Re = \frac{\text{advection}}{\text{dissipation}} = \frac{VL}{\nu}$$

$V$  = typical velocity on scale  $L$ ,  $\nu = \eta/\rho$  = kinematic viscosity,  
turbulence for  $Re > 1000$  → typical values in ISM  $10^8$ - $10^{10}$



- Navier-Stokes equation (transport of momentum)

$$\rho \frac{d\vec{v}}{dt} = \rho \left( \frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \vec{v} \right) = -\vec{\nabla} P + \eta \vec{\nabla}^2 \vec{v} + \left( \frac{\eta}{3} + \zeta \right) \vec{\nabla} (\vec{\nabla} \cdot \vec{v})$$

shear viscosity

bulk viscosity

$$\sigma_{ij} \equiv \eta \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} - \frac{2}{3} \delta_{ij} \frac{\partial v_k}{\partial x_k} \right) + \zeta \delta_{ij} \frac{\partial v_k}{\partial x_k}$$

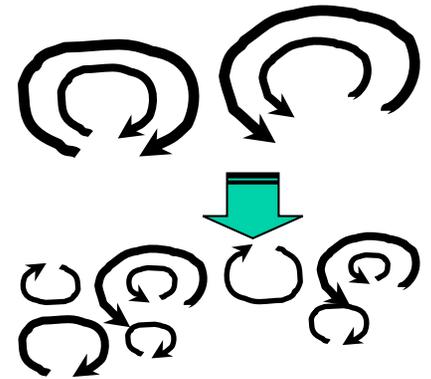
viscous stress tensor

# properties of turbulence

- laminar flows turn *turbulent* at *high Reynolds* numbers

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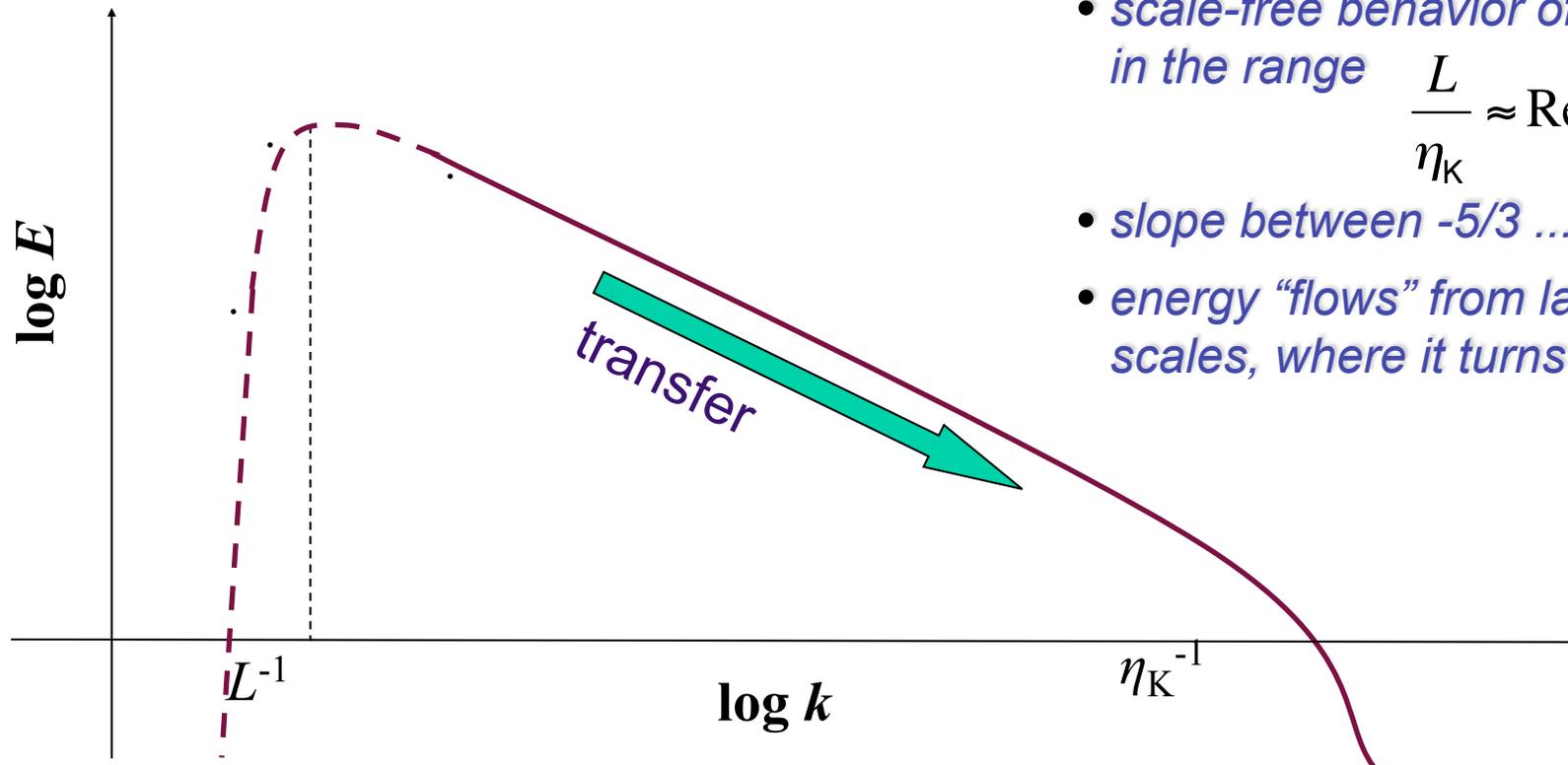


- vortex stretching  $\rightarrow$  turbulence is intrinsically anisotropic  
(only on large scales you may get  
homogeneity & isotropy in a statistical sense;  
see Landau & Lifschitz, Chandrasekhar, Taylor, etc.)

(ISM turbulence: shocks & B-field  
cause additional inhomogeneity)



# turbulent cascade in the ISM

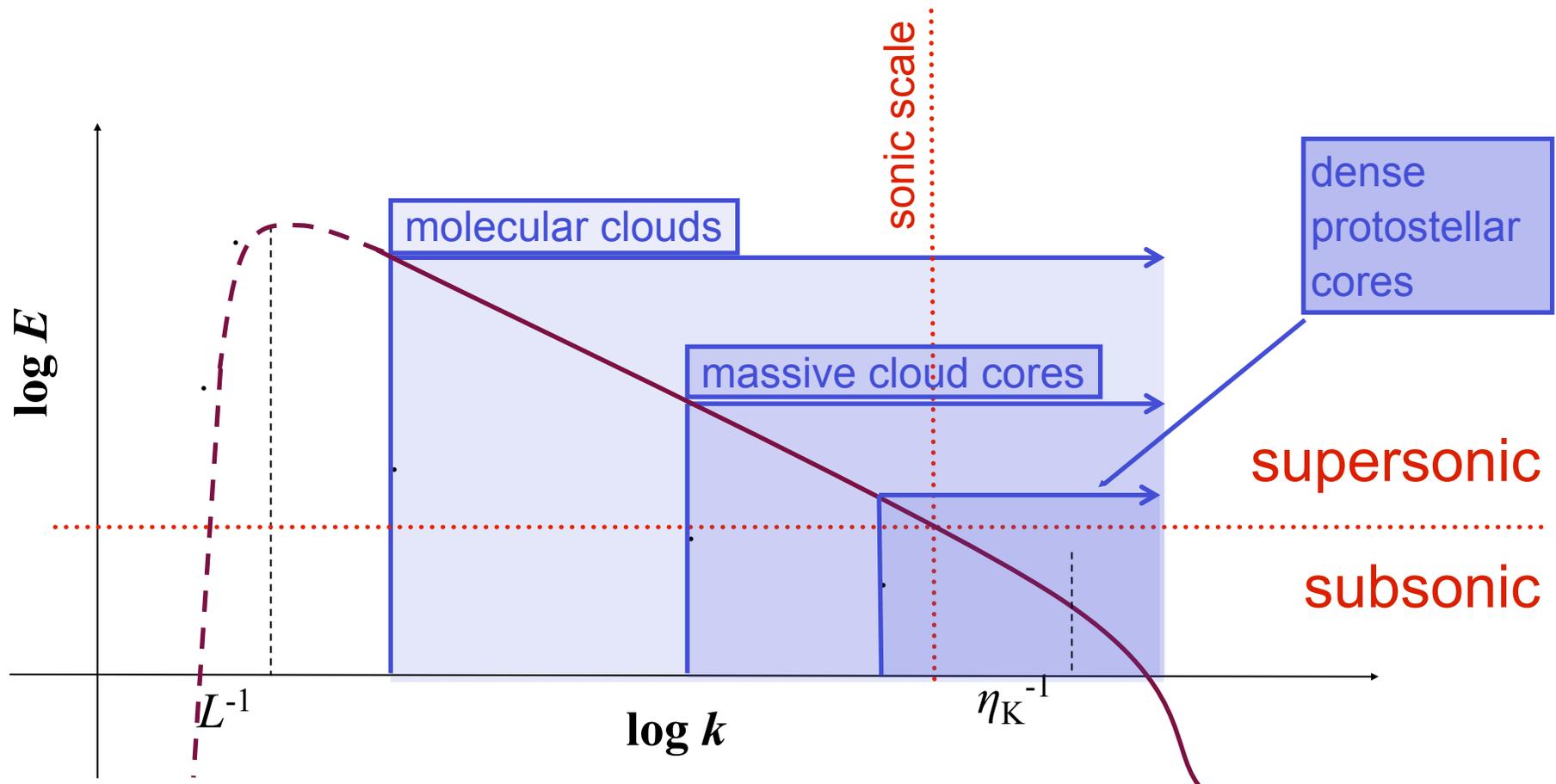


- *scale-free behavior of turbulence in the range  $\frac{L}{\eta_K} \approx \text{Re}^{3/4}$*
- *slope between -5/3 ... -2*
- *energy “flows” from large to small scales, where it turns into heat*

energy source & scale  
*NOT known*  
(supernovae, winds,  
spiral density waves?)

dissipation scale not known  
(ambipolar diffusion,  
molecular diffusion?)

# turbulent cascade in the ISM



energy source & scale  
*NOT known*  
 (supernovae, winds,  
 spiral density waves?)

$$\sigma_{\text{rms}} \ll 1 \text{ km/s}$$

$$M_{\text{rms}} \leq 1$$

$$L \approx 0.1 \text{ pc}$$

dissipation scale not known  
 (ambipolar diffusion,  
 molecular diffusion?)

# gravoturbulent star formation

- BASIC ASSUMPTION:

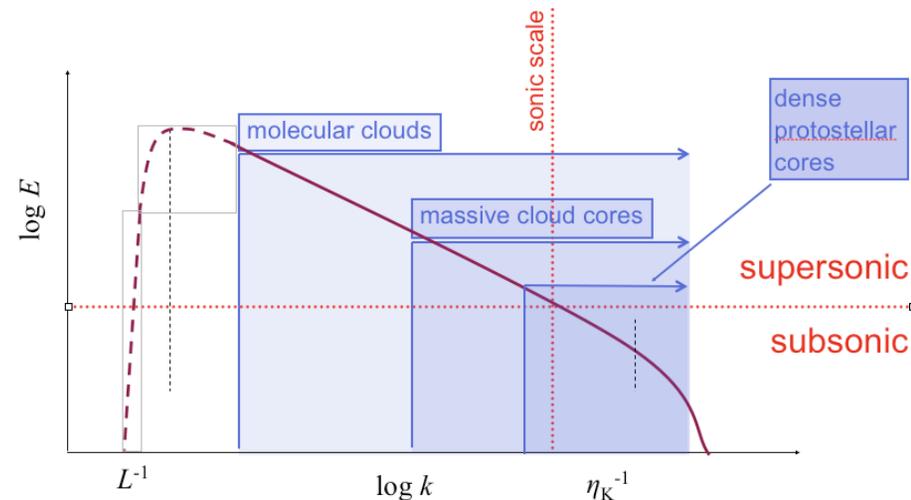
• star formation is controlled by interplay between supersonic turbulence and self-gravity

- turbulence plays a *dual role*:

- on *large scales* it *provides support*
- on *small scales* it can *trigger collapse*

- some predictions:

- dynamical star formation timescale  $\tau_{\text{ff}}$
- high binary fraction
- complex spatial structure of embedded star clusters
- and many more . . .

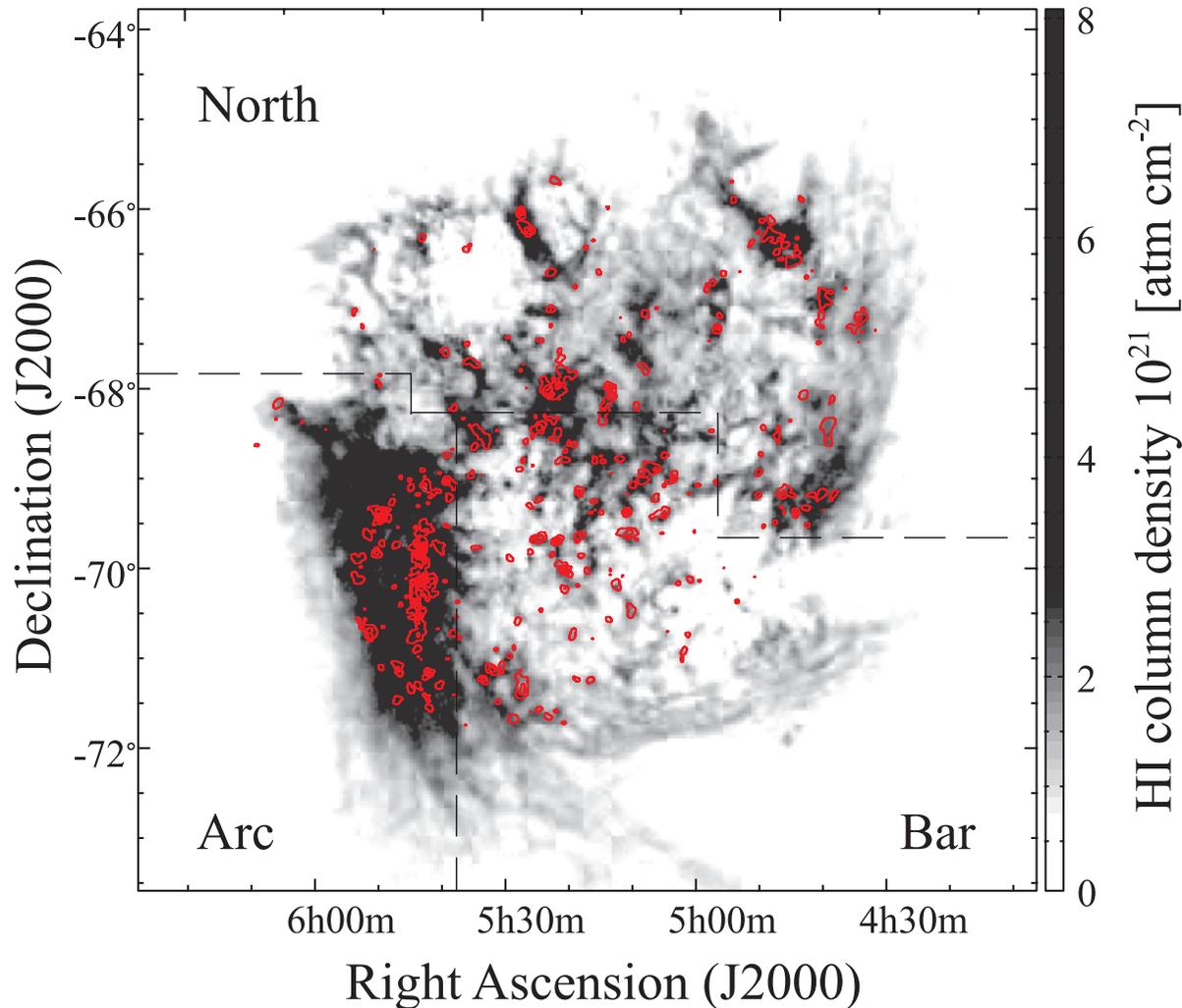


Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125-194

McKee & Ostriker, 2007, ARAA, 45, 565

Klessen & Glover 2014, Saas Fee Lecture, arXiv:1412.5182, 1-191

# molecular cloud formation

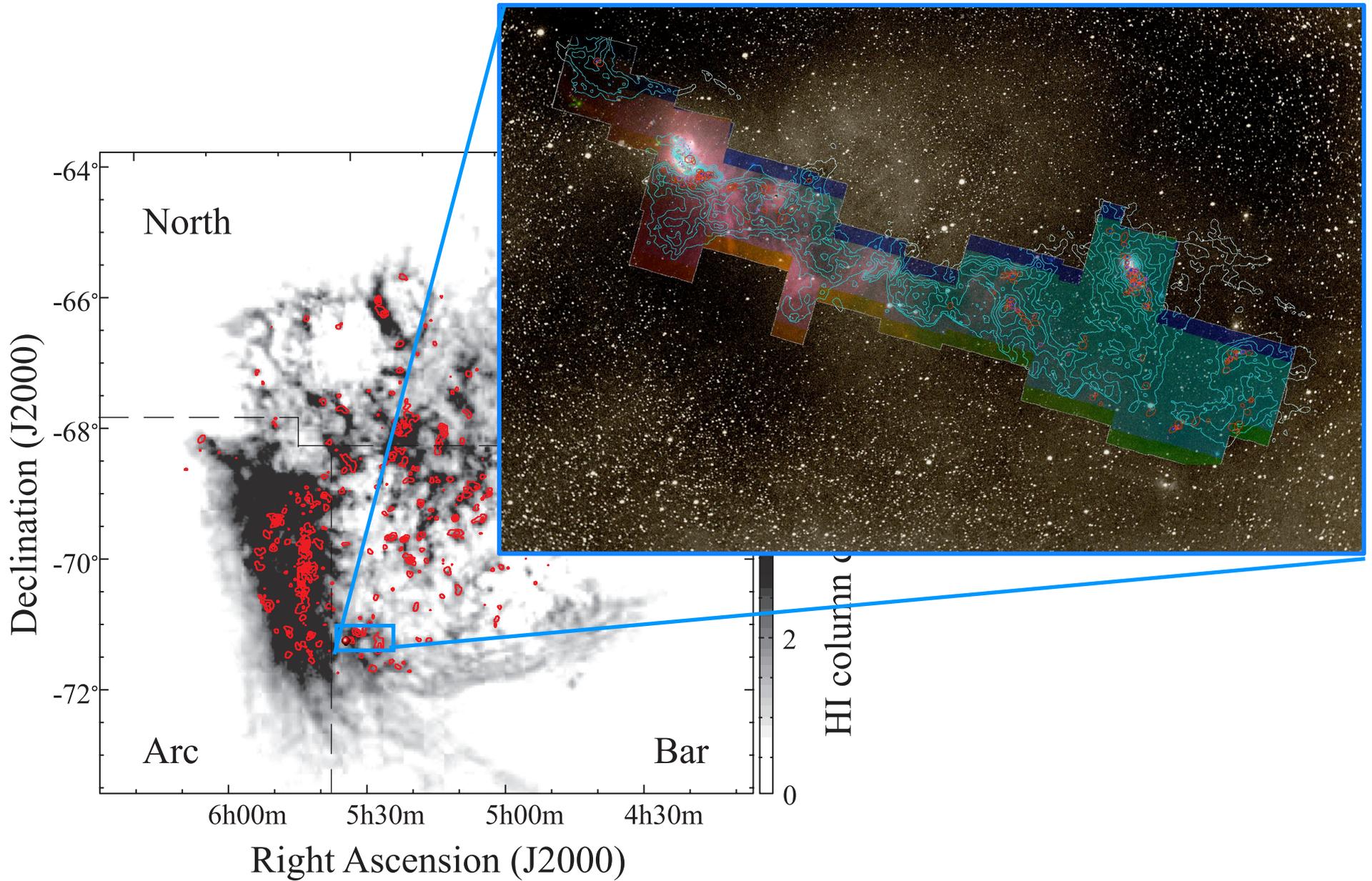


Idea:

Molecular clouds form at *stagnation points* of large-scale convergent flows, mostly triggered by global (or external) perturbations. Their internal turbulence is driven by accretion, i.e. by the process of cloud formation

- molecular clouds grow in mass
- this is inferred by looking at molecular clouds in different evolutionary phases in the LMC (Fukui et al. 2008, 2009)

zooming in ...



# position-position-velocity structure of the Perseus cloud

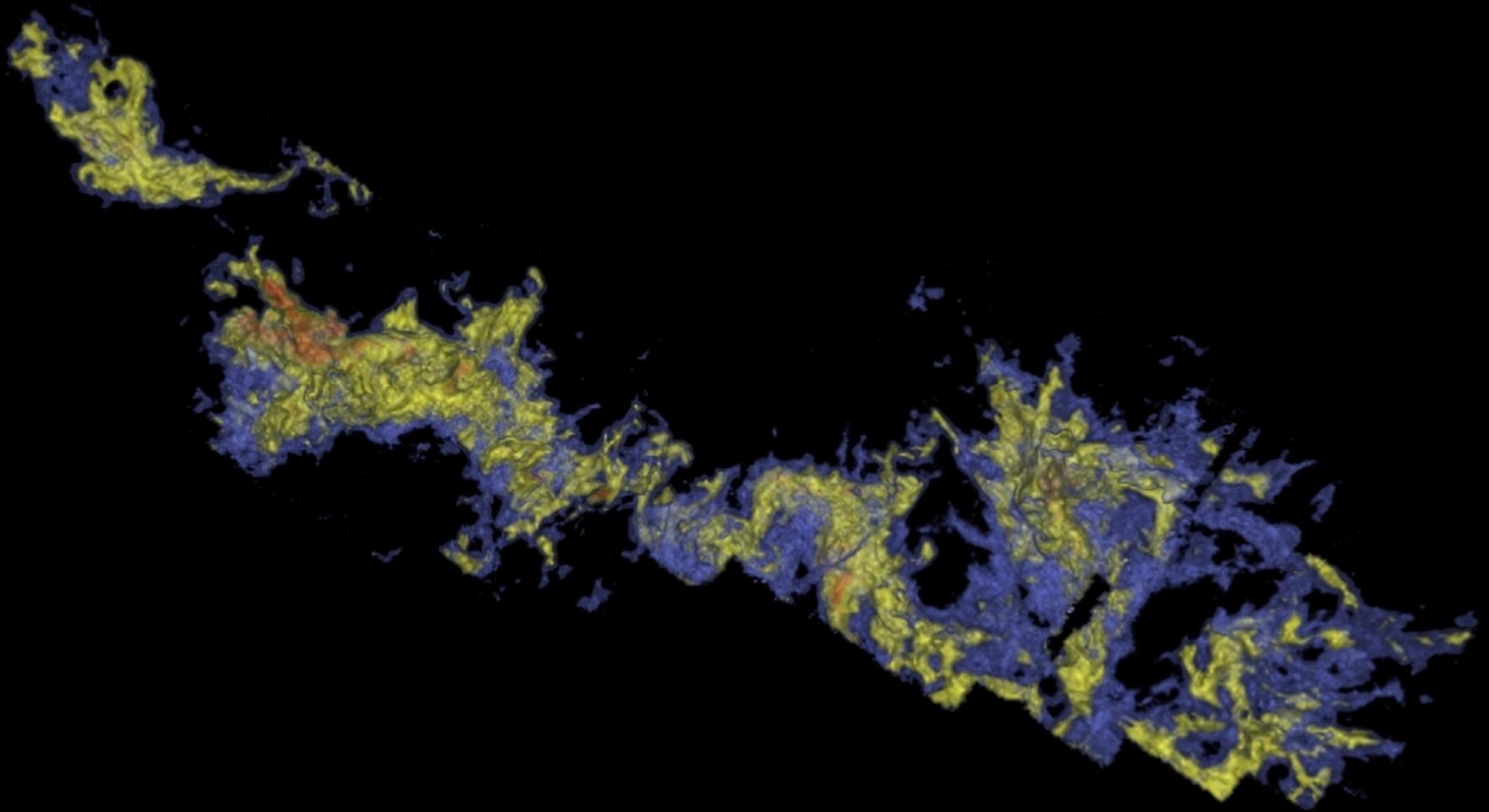
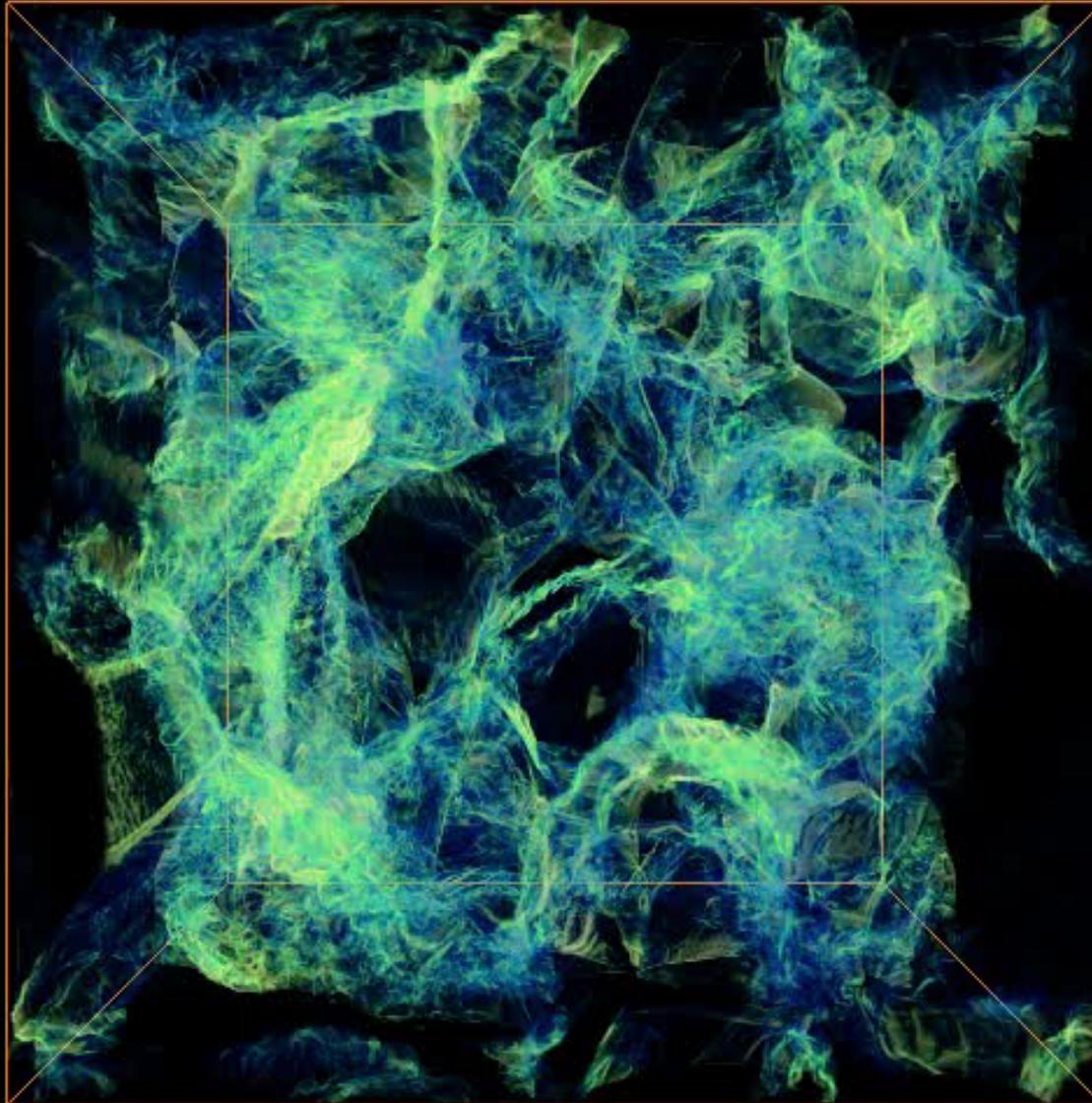


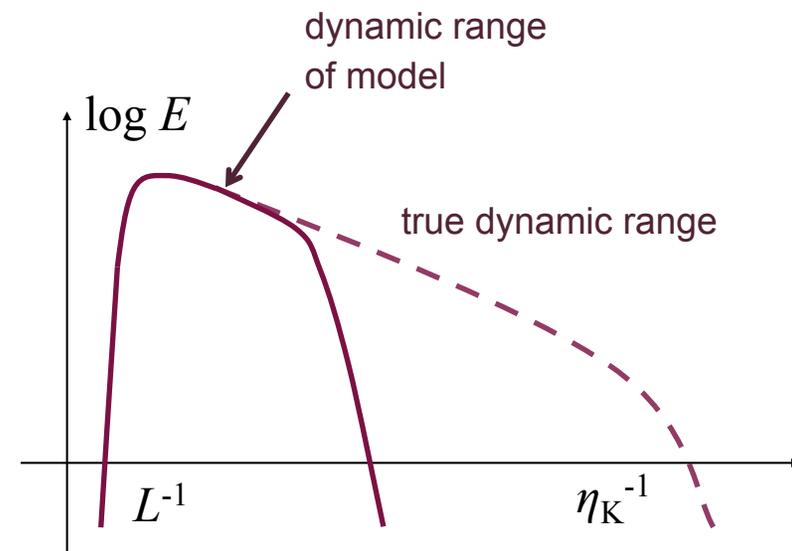
image from Alyssa Goodman: COMPLETE survey



Schmidt et al. (2009, A&A, 494, 127)

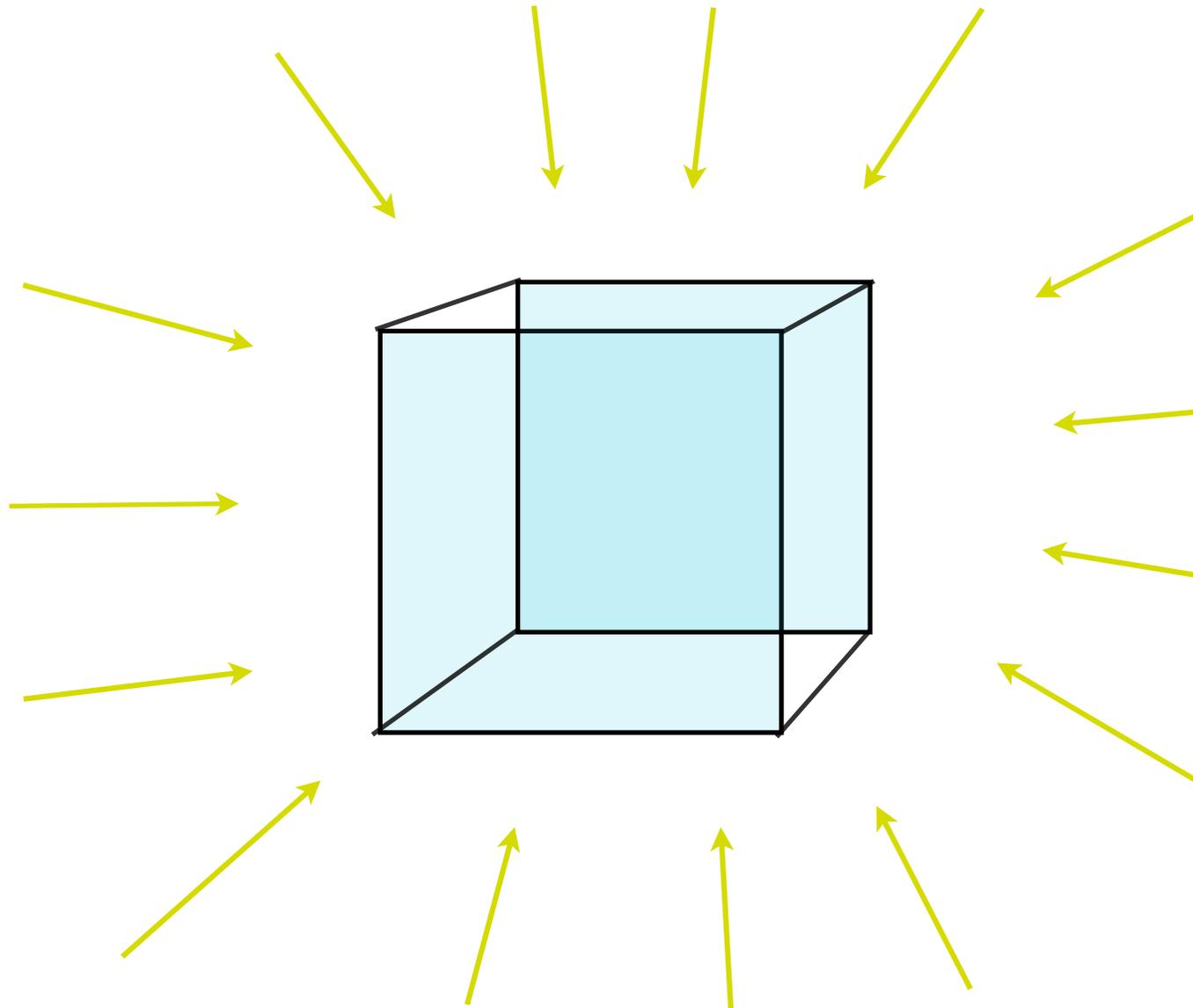
# caveat of numerical simulations

- most astrophysical turbulence simulations use an **LES** approach to model the flow
- principal problem: only large scale flow properties
  - Reynolds number:  $Re = LV/\nu$  ( $Re_{nature} \gg Re_{model}$ )
  - dynamic range much smaller than true physical one
  - need **subgrid model** (often only dissipation)
  - but what to do for more complex when processes on subgrid scale determine large-scale dynamics (chemical reactions, nuclear burning, etc)
  - Turbulence is “space filling” --> difficulty for AMR (don't know what criterion to use for refinement)
- how **large** a Reynolds number do we need to catch basic dynamics right?



including detailed  
chemistry

# experimental set-up



- Arepo and FLASH
- stochastic forcing (Ornstein-Uhlenbeck)
- self-gravity
- time-dependent chemistry (DVODE, standard variable-coefficient ordinary differential equation solver)
- cooling & heating processes
- gives you mathematically well defined boundary conditions
- > good for statistical studies
- gives external radiation with TreeCol (a new approximative scheme to calculate column densities from the gravity solver)

# chemical model 0

- 32 chemical species

- 17 in instantaneous equilibrium:

$H^-$ ,  $H_2^+$ ,  $H_3^+$ ,  $CH^+$ ,  $CH_2^+$ ,  $\dot{O}H^+$ ,  $H_2O^+$ ,  $\check{H}_3O^+$ ,  $CO^+$ ,  $HOC^+$ ,  $O^-$ ,  $C^-$  and  $O_2^+$

- 19 full non-equilibrium evolution

$e^-$ ,  $H^+$ ,  $H$ ,  $H_2$ ,  $He$ ,  $He^+$ ,  $C$ ,  $C^+$ ,  $O$ ,  $O^+$ ,  $OH$ ,  $H_2O$ ,  $CO$ ,

$C_2$ ,  $O_2$ ,  $HCO^+$ ,  $CH$ ,  $CH_2$  and  $CH_3^+$

- 218 reactions

- various heating and cooling processes



# chemical model 1

Process

Reference(s)

## Cooling:

C fine structure lines	Atomic data – Silva & Viegas (2002) Collisional rates (H) – Abrahamsson, Krems & Dalgarno (2007) Collisional rates (H <sub>2</sub> ) – Schroder et al. (1991) Collisional rates (e <sup>-</sup> ) – Johnson et al. (1987) Collisional rates (H <sup>+</sup> ) – Roueff & Le Bourlot (1990)
C <sup>+</sup> fine structure lines	Atomic data – Silva & Viegas (2002) Collisional rates (H <sub>2</sub> ) – Flower & Launay (1977) Collisional rates (H, T < 2000 K) – Hollenbach & McKee (1989) Collisional rates (H, T > 2000 K) – Keenan et al. (1986) Collisional rates (e <sup>-</sup> ) – Wilson & Bell (2002)
O fine structure lines	Atomic data – Silva & Viegas (2002) Collisional rates (H) – Abrahamsson, Krems & Dalgarno (2007) Collisional rates (H <sub>2</sub> ) – see Glover & Jappsen (2007) Collisional rates (e <sup>-</sup> ) – Bell, Berrington & Thomas (1998) Collisional rates (H <sup>+</sup> ) – Pequignot (1990, 1996)
H <sub>2</sub> rovibrational lines	Le Bourlot, Pineau des Forêts & Flower (1999)
CO and H <sub>2</sub> O rovibrational lines	Neufeld & Kaufman (1993); Neufeld, Lepp & Melnick (1995)
OH rotational lines	Pavlovski et al. (2002)
Gas-grain energy transfer	Hollenbach & McKee (1989)
Recombination on grains	Wolfire et al. (2003)
Atomic resonance lines	Sutherland & Dopita (1993)
H collisional ionization	Abel et al. (1997)
H <sub>2</sub> collisional dissociation	See Table B1
Compton cooling	Cen (1992)

## Heating:

Photoelectric effect	Bakes & Tielens (1994); Wolfire et al. (2003)
H <sub>2</sub> photodissociation	Black & Dalgarno (1977)
UV pumping of H <sub>2</sub>	Burton, Hollenbach & Tielens (1990)
H <sub>2</sub> formation on dust grains	Hollenbach & McKee (1989)
Cosmic ray ionization	Goldsmith & Langer (1978)



Table B1. List of collisional gas-phase reactions included in our chemical model 2

# chemical model 2

No.	Reaction	Rate coefficient	Temperature range	Reference
1	$H + e^- \rightarrow H^- + \gamma$	$k_1 = \text{dex}[-17.845 + 0.762 \log T + 0.1523(\log T)^2 - 0.03274(\log T)^3]$ $= \text{dex}[-16.420 + 0.1998(\log T)^2 - 5.447 \times 10^{-3}(\log T)^4 + 4.0415 \times 10^{-5}(\log T)^6]$	$T \leq 6000 \text{ K}$ $T > 6000 \text{ K}$	1
2	$H^- + H \rightarrow H_2 + e^-$	$k_2 = 1.5 \times 10^{-9}$ $= 4.0 \times 10^{-9} T^{-0.17}$	$T \leq 300 \text{ K}$ $T > 300 \text{ K}$	2
3	$H + H^+ \rightarrow H_2^+ + \gamma$	$k_3 = \text{dex}[-19.38 - 1.523 \log T + 1.118(\log T)^2 - 0.1269(\log T)^3]$		3
4	$H + H_2^+ \rightarrow H_2 + H^+$	$k_4 = 6.4 \times 10^{-10}$		4
5	$H^- + H^+ \rightarrow H + H$	$k_5 = 2.4 \times 10^{-9} T^{-1/2} (1.0 + T/20000)$		5
6	$H_2^+ + e^- \rightarrow H + H$	$k_6 = 1.0 \times 10^{-8}$ $= 1.32 \times 10^{-6} T^{-0.76}$	$T \leq 617 \text{ K}$ $T > 617 \text{ K}$	6
7	$H_2 + H^+ \rightarrow H_2^+ + H$	$k_7 = [-3.3232183 \times 10^{-7} + 3.3735382 \times 10^{-7} \ln T - 1.4491368 \times 10^{-7} (\ln T)^2 + 3.4172805 \times 10^{-8} (\ln T)^3 - 4.7813720 \times 10^{-9} (\ln T)^4 + 3.9731542 \times 10^{-10} (\ln T)^5 - 1.8171411 \times 10^{-11} (\ln T)^6 + 3.5311932 \times 10^{-13} (\ln T)^7] \times \exp\left(\frac{-21237.15}{T}\right)$		7
8	$H_2 + e^- \rightarrow H + H + e^-$	$k_8 = 3.73 \times 10^{-9} T^{0.1121} \exp\left(\frac{-99430}{T}\right)$		8
9	$H_2 + H \rightarrow H + H + H$	$k_{9,l} = 6.67 \times 10^{-12} T^{1/2} \exp\left[-\left(1 + \frac{63590}{T}\right)\right]$ $k_{9,h} = 3.52 \times 10^{-9} \exp\left(\frac{-43900}{T}\right)$		9 10
		$n_{cr,H} = \text{dex}\left[3.0 - 0.416 \log\left(\frac{T}{10000}\right) - 0.327 \left\{\log\left(\frac{T}{10000}\right)\right\}^2\right]$		10
10	$H_2 + H_2 \rightarrow H_2 + H + H$	$k_{10,l} = \frac{5.996 \times 10^{-30} T^{4.1881}}{(1.0 + 6.761 \times 10^{-6} T)^{5.6881}} \exp\left(\frac{-54657.4}{T}\right)$ $k_{10,h} = 1.3 \times 10^{-9} \exp\left(\frac{-53300}{T}\right)$		11 12
		$n_{cr,H_2} = \text{dex}\left[4.845 - 1.3 \log\left(\frac{T}{10000}\right) + 1.62 \left\{\log\left(\frac{T}{10000}\right)\right\}^2\right]$		12
11	$H + e^- \rightarrow H^+ + e^- + e^-$	$k_{11} = \exp[-3.271396786 \times 10^1 + 1.35365560 \times 10^1 \ln T_e - 5.73932875 \times 10^0 (\ln T_e)^2 + 1.56315498 \times 10^0 (\ln T_e)^3 - 2.87705600 \times 10^{-1} (\ln T_e)^4 + 3.48255977 \times 10^{-2} (\ln T_e)^5 - 2.63197617 \times 10^{-3} (\ln T_e)^6 + 1.11954395 \times 10^{-4} (\ln T_e)^7 - 2.03914985 \times 10^{-6} (\ln T_e)^8]$		13
12	$H^+ + e^- \rightarrow H + \gamma$	$k_{12,A} = 1.269 \times 10^{-13} \left(\frac{315614}{T}\right)^{1.503} \times \left[1.0 + \left(\frac{604625}{T}\right)^{0.470}\right]^{-1.923}$ $k_{12,B} = 2.753 \times 10^{-14} \left(\frac{315614}{T}\right)^{1.500} \times \left[1.0 + \left(\frac{115188}{T}\right)^{0.407}\right]^{-2.242}$	Case A Case B	14 14
13	$H^- + e^- \rightarrow H + e^- + e^-$	$k_{13} = \exp[-1.801849334 \times 10^1 + 2.36085220 \times 10^0 \ln T_e - 2.82744300 \times 10^{-1} (\ln T_e)^2 + 1.62331664 \times 10^{-2} (\ln T_e)^3 - 3.36501203 \times 10^{-2} (\ln T_e)^4 + 1.17832978 \times 10^{-2} (\ln T_e)^5 - 1.65619470 \times 10^{-3} (\ln T_e)^6 + 1.06827520 \times 10^{-4} (\ln T_e)^7 - 2.63128581 \times 10^{-6} (\ln T_e)^8]$		13



# chemical model 2

Table B1.

No.	Rea
1	H +

14	$H^- + H \rightarrow H + H + e^-$	88	$H_2 + He^+ \rightarrow He + H_2^+$	$k_{88} = 7.2 \times 10^{-15}$	63
36	$CH + H_2$	89	$H_2 + He^+ \rightarrow He + H + H^+$	$k_{89} = 3.7 \times 10^{-14} \exp\left(\frac{35}{T}\right)$	63
37	$CH + C$	90	$CH + H^+ \rightarrow CH^+ + H$	$k_{90} = 1.9 \times 10^{-9}$	28
38	$CH + O$	91	$CH_2 + H^+ \rightarrow CH_2^+ + H$	$k_{91} = 1.4 \times 10^{-9}$	28
39	$C + O$	92	$Cl_2 + H^+ \rightarrow Cl_2^+ + H$	$k_{92} = 5 \times 10^{-10}$	28
40	$CH_2 + O$	93	$C_2 + e^- \rightarrow C + C$	$k_{93} = 6 \times 10^{-9}$	28
41	$CH_2 + O$	94	$OH + H^+ \rightarrow OH^+ + H$	$k_{94} = 2.1 \times 10^{-9}$	28
42	$C_2 + O \rightarrow$	95	$OH + He^+ \rightarrow O^+ + He + H$	$k_{95} = 1.1 \times 10^{-9}$	28
		96	$H_2O + H^+ \rightarrow H_2O^+ + H$	$k_{96} = 6.9 \times 10^{-9}$	64
		97	$H_2O + He^+ \rightarrow OH + He + H^+$	$k_{97} = 2.04 \times 10^{-10}$	65
		98	$H_2O + He^+ \rightarrow OH^+ + He + H$	$k_{98} = 2.04 \times 10^{-10}$	65

Table B2. List of photochemical reactions included in our chemical model

No.	Reaction	Optically thin rate ( $s^{-1}$ )	$\gamma$	Ref.		
166	$H^- + \gamma \rightarrow H + e^-$	$R_{166} = 7.1 \times 10^{-7}$	0.5	1		
167	$H_2^+ + \gamma \rightarrow H + H^+$	$R_{167} = 1.1 \times 10^{-9}$	1.9	2		
168	$H_2 + \gamma \rightarrow H + H$	$R_{168} = 5.6 \times 10^{-11}$	See §2.2	3		
169	$H_3^+ + \gamma \rightarrow H_2 + H^+$	$R_{169} = 4.9 \times 10^{-13}$	1.8	4		
170	$H_3^+ + \gamma \rightarrow H_2^+ + H$	$R_{170} = 4.9 \times 10^{-13}$	2.3	4		
171	$C + \gamma \rightarrow C^+ + e^-$	$R_{171} = 2.1 \times 10^{-10}$	2.0	5	$25 \times 10^{-15}$	81
172	$C^- + \gamma \rightarrow$				$0 \times 10^{-17}$	82
173	$CH + \gamma \rightarrow$				$0 \times 10^{-17}$	82
174	$CH + \gamma \rightarrow$				$36 \times 10^{-18} \left(\frac{T}{300}\right)^{0.35} \exp\left(-\frac{161.3}{T}\right)$	83
175	$CH^+ + \gamma \rightarrow$				$1 \times 10^{-19}$	84
176	$CH_2 + \gamma \rightarrow$				$0.9 \times 10^{-17} \left(\frac{T}{300}\right)^{0.33} \exp\left(-\frac{1629}{T}\right)$	$T \leq 300$ K
177	$CH_2 + \gamma \rightarrow$				$46 \times 10^{-16} T^{-0.5} \exp\left(-\frac{4.93}{T^{2/3}}\right)$	$T > 300$ K
178	$CH_3^+ + \gamma \rightarrow$				$0 \times 10^{-16} \left(\frac{T}{300}\right)^{-0.2}$	
179	$CH_3^+ + \gamma \rightarrow$				$5 \times 10^{-18}$	$T \leq 300$ K
180	$CH_3^+ + \gamma \rightarrow$				$14 \times 10^{-18} \left(\frac{T}{300}\right)^{-0.15} \exp\left(\frac{68}{T}\right)$	$T > 300$ K

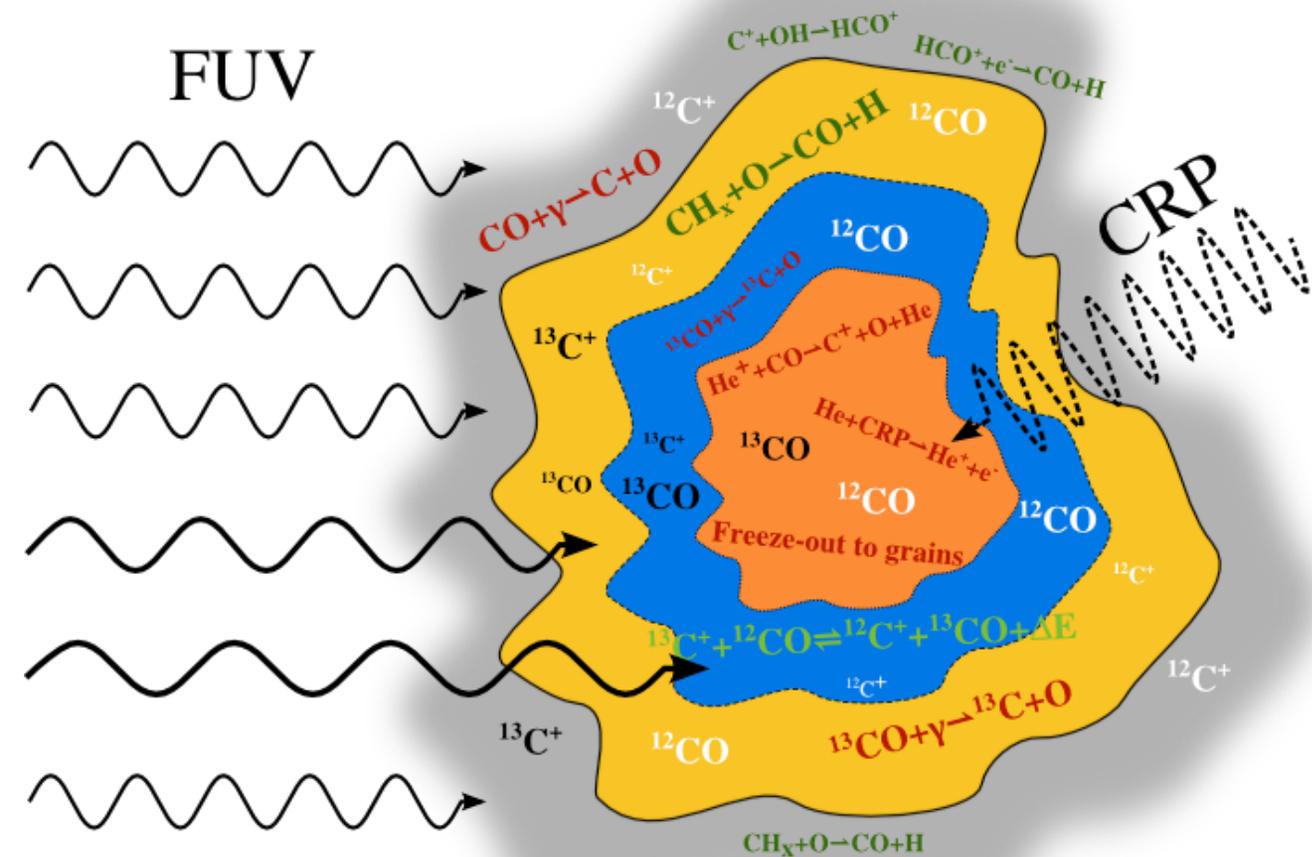
Table B3. List of reactions included in our chemical model that involve cosmic rays or cosmic-ray induced UV emission

No.	Reaction	Rate ( $s^{-1} \zeta_H^{-1}$ )	Ref.
199	$H + c.r. \rightarrow H^+ + e^-$	$R_{199} = 1.0$	—
200	$He + c.r. \rightarrow He^+ + e^-$	$R_{200} = 1.1$	1
201	$H_2 + c.r. \rightarrow H^+ + H + e^-$	$R_{201} = 0.037$	1
202	$H_2 + c.r. \rightarrow H + H$	$R_{202} = 0.22$	1
203	$H_2 + c.r. \rightarrow H^+ + H^-$	$R_{203} = 6.5 \times 10^{-4}$	1
204	$H_2 + c.r. \rightarrow H_2^+ + e^-$	$R_{204} = 2.0$	1
205	$C + c.r. \rightarrow C^+ + e^-$	$R_{205} = 3.8$	1
206	$O + c.r. \rightarrow O^+ + e^-$	$R_{206} = 5.7$	1
207	$CO + c.r. \rightarrow CO^+ + e^-$	$R_{207} = 6.5$	1
208	$C + \gamma_{c.r.} \rightarrow C^+ + e^-$	$R_{208} = 2800$	2
209	$CH + \gamma_{c.r.} \rightarrow C + H$	$R_{209} = 4000$	3
210	$CH^+ + \gamma_{c.r.} \rightarrow C^+ + H$	$R_{210} = 960$	3
211	$CH_2 + \gamma_{c.r.} \rightarrow CH_2^+ + e^-$	$R_{211} = 2700$	1
212	$CH_2 + \gamma_{c.r.} \rightarrow CH + H$	$R_{212} = 2700$	1
213	$C_2 + \gamma_{c.r.} \rightarrow C + C$	$R_{213} = 1300$	3
214	$OH + \gamma_{c.r.} \rightarrow O + H$	$R_{214} = 2800$	3
215	$H_2O + \gamma_{c.r.} \rightarrow OH + H$	$R_{215} = 5300$	3
216	$O_2 + \gamma_{c.r.} \rightarrow O + O$	$R_{216} = 4100$	3
217	$O_2 + \gamma_{c.r.} \rightarrow O_2^+ + e^-$	$R_{217} = 640$	3
218	$CO + \gamma_{c.r.} \rightarrow C + O$	$R_{218} = 0.21 T^{1/2} x_{H_2} x_{CO}^{-1/2}$	4
197	$O_2 + \gamma \rightarrow O + O$	$R_{197} = 7.0 \times 10^{-10}$	7
198	$CO + \gamma \rightarrow C + O$	$R_{198} = 2.0 \times 10^{-10}$	See §2.2

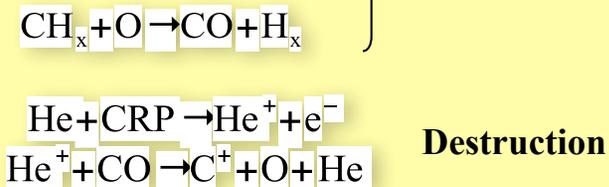
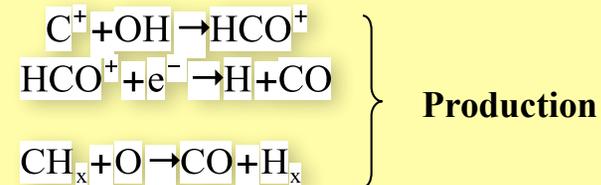
86	$HCO^+ + C$	140	$O^- + C \rightarrow CO + e^-$	$k_{140} = 5.0 \times 10^{-10}$	28
87	$HCO^+ + H_2O$		$\rightarrow CO + H_3O^+$	$k_{87} = 2.5 \times 10^{-9}$	28

$^{12}\text{CO} / ^{13}\text{CO}$  ratio

# CO chemistry in GMCs



## Non-isotope selective reactions



Accretion to grains **Depletion**

I. Diffuse region ( $A_v < 0.5^m$ )



II. Translucent region ( $1^m < A < 2^m$ )

a) **preferential  $^{13}\text{CO}$  photo-dissociation**

b) **Fractionation reaction**



III. Dense core ( $A_v \approx 5^m$ )

$\text{C}^+$  depletes

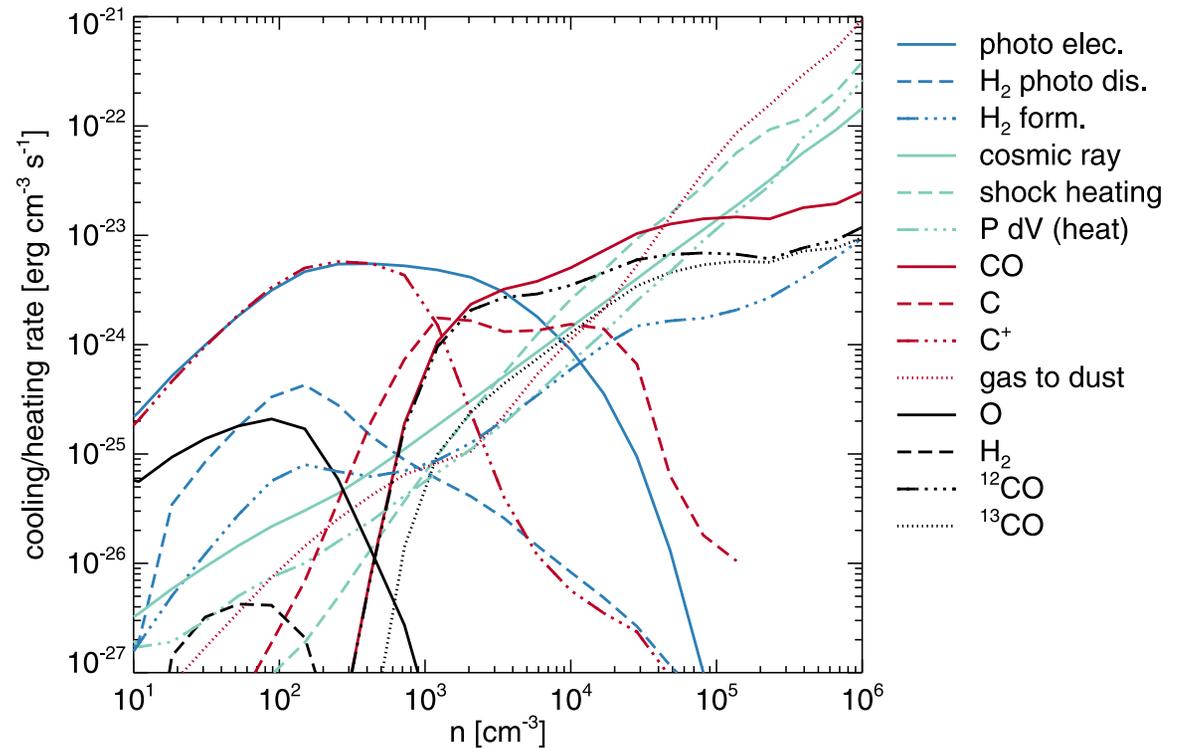
Freeze-out & CRP destruction

# Detailed thermodynamic analysis

## 6 different models:

Model	$n_0$ [cm <sup>-3</sup> ]	Metallicity [ $Z_{\odot}$ ]	ISRF [ $G_0$ ]	Time [Myr]
a	300	0.3	1	2.046
b	300	0.6	1	1.930
c	300	1	0.1	2.124
d	300	1	1	2.150
e	300	1	10	2.022
f	1000	1	1	0.973

## all relevant heating and cooling processes:



# Results – $N(^{12}\text{CO})/N(^{13}\text{CO})$ column densities ratio

$N_0 = 300 \text{ cm}^{-3}$

$\text{ISRF} = 1 G_0$

$Z = 1 Z_\odot$

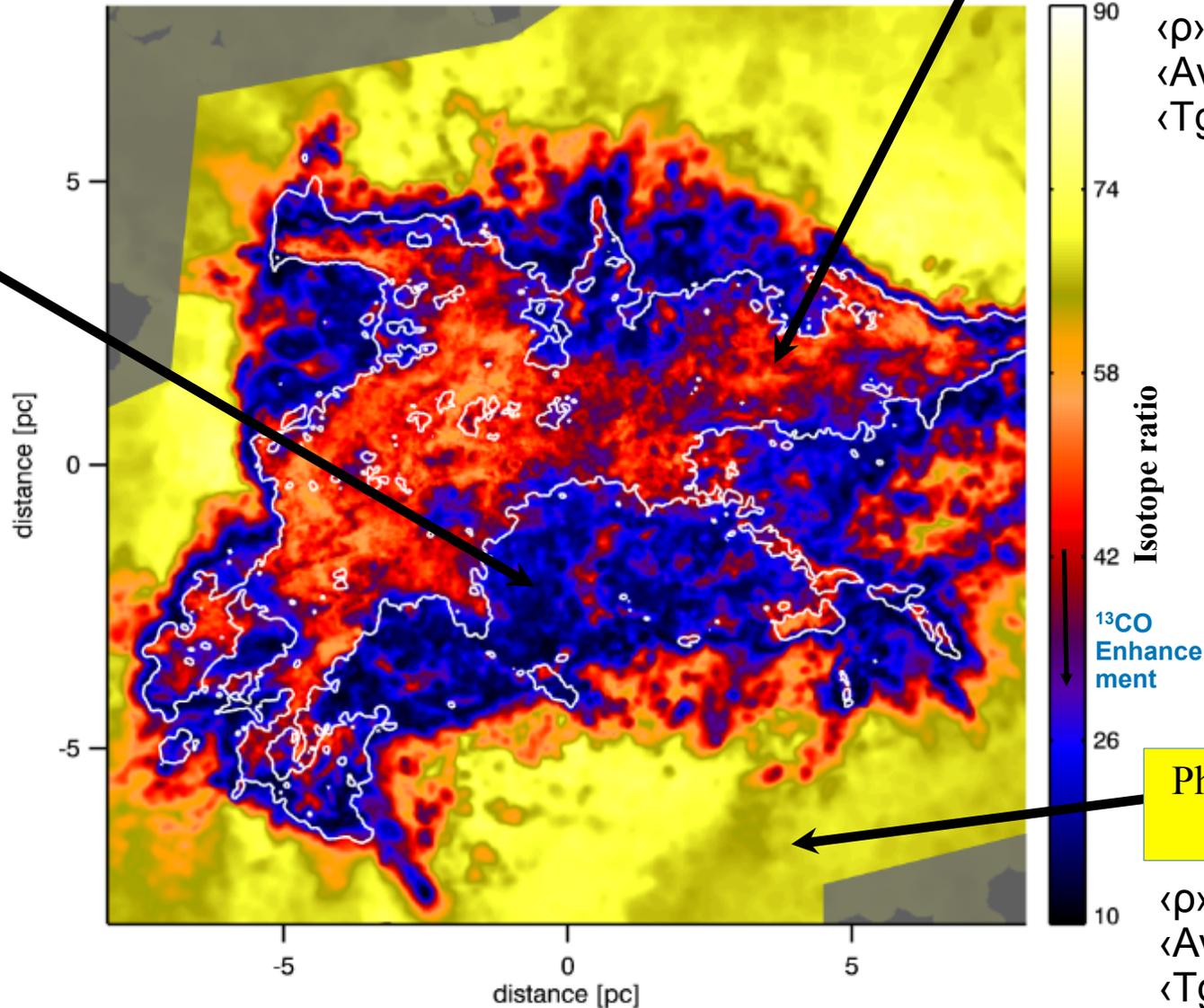
Before first sink  
particle forms

White contour shows  $5 \times 10^{21} \text{ cm}^{-2}$

Around the  $^{12}\text{C}/^{13}\text{C}$   
ratio

Chemical  
fractionation

$\langle \rho \rangle \approx 10^{-21} \text{ g cm}^{-3}$   
 $\langle A_V \rangle \approx 1^m$   
 $\langle T_{\text{gas}} \rangle \approx 20 \text{ K}$

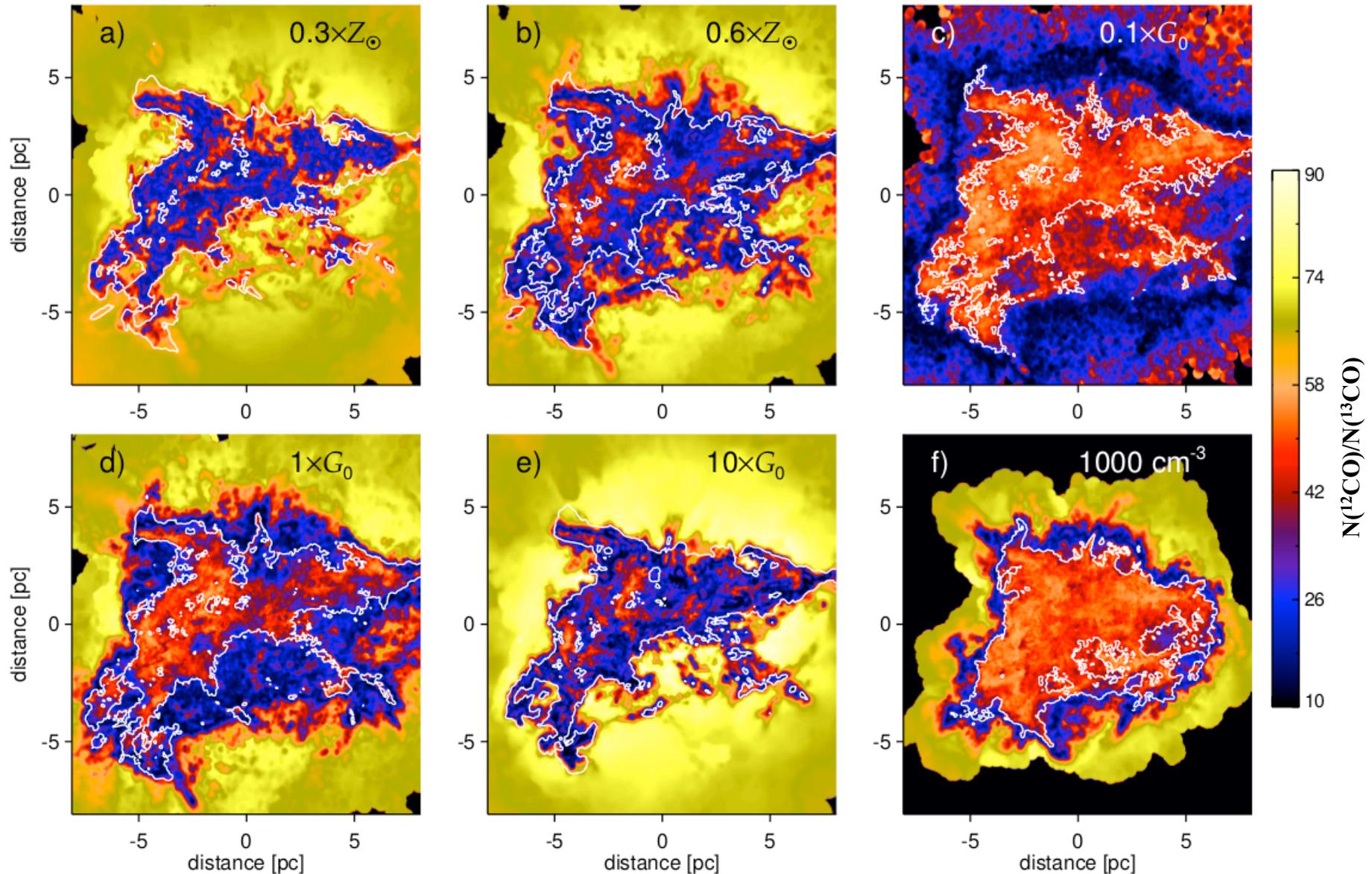


$\langle \rho \rangle \approx 10^{-20} \text{ g cm}^{-3}$   
 $\langle A_V \rangle > 1.5^m$   
 $\langle T_{\text{gas}} \rangle \approx 15 \text{ K}$

Photo-dissociation  
dominates

$\langle \rho \rangle \approx 10^{-22} \text{ g cm}^{-3}$   
 $\langle A_V \rangle \ll 1^m$   
 $\langle T_{\text{gas}} \rangle \approx 40 \text{ K}$

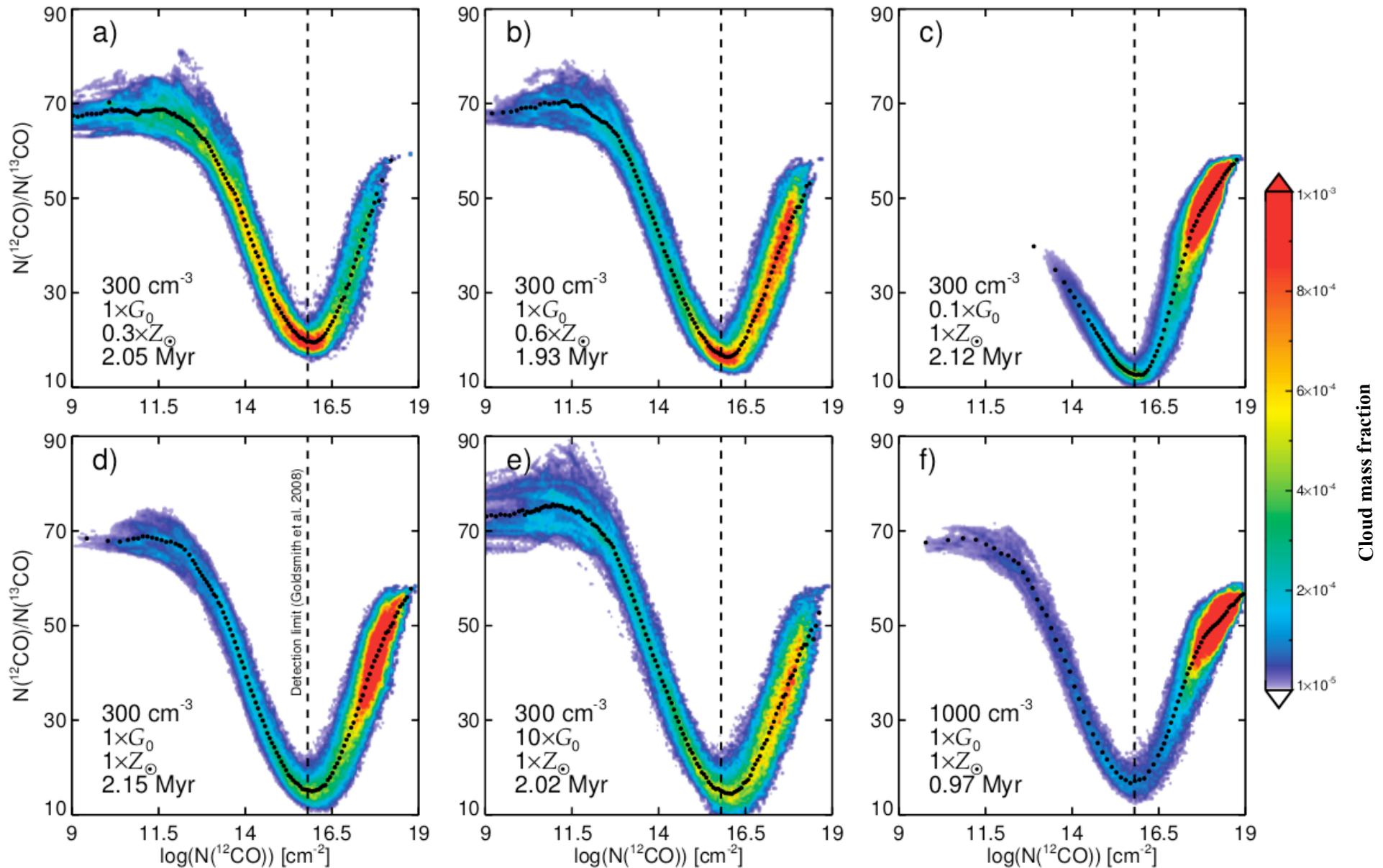
# Results – $N(^{12}\text{CO})/N(^{13}\text{CO})$ column densities ratio



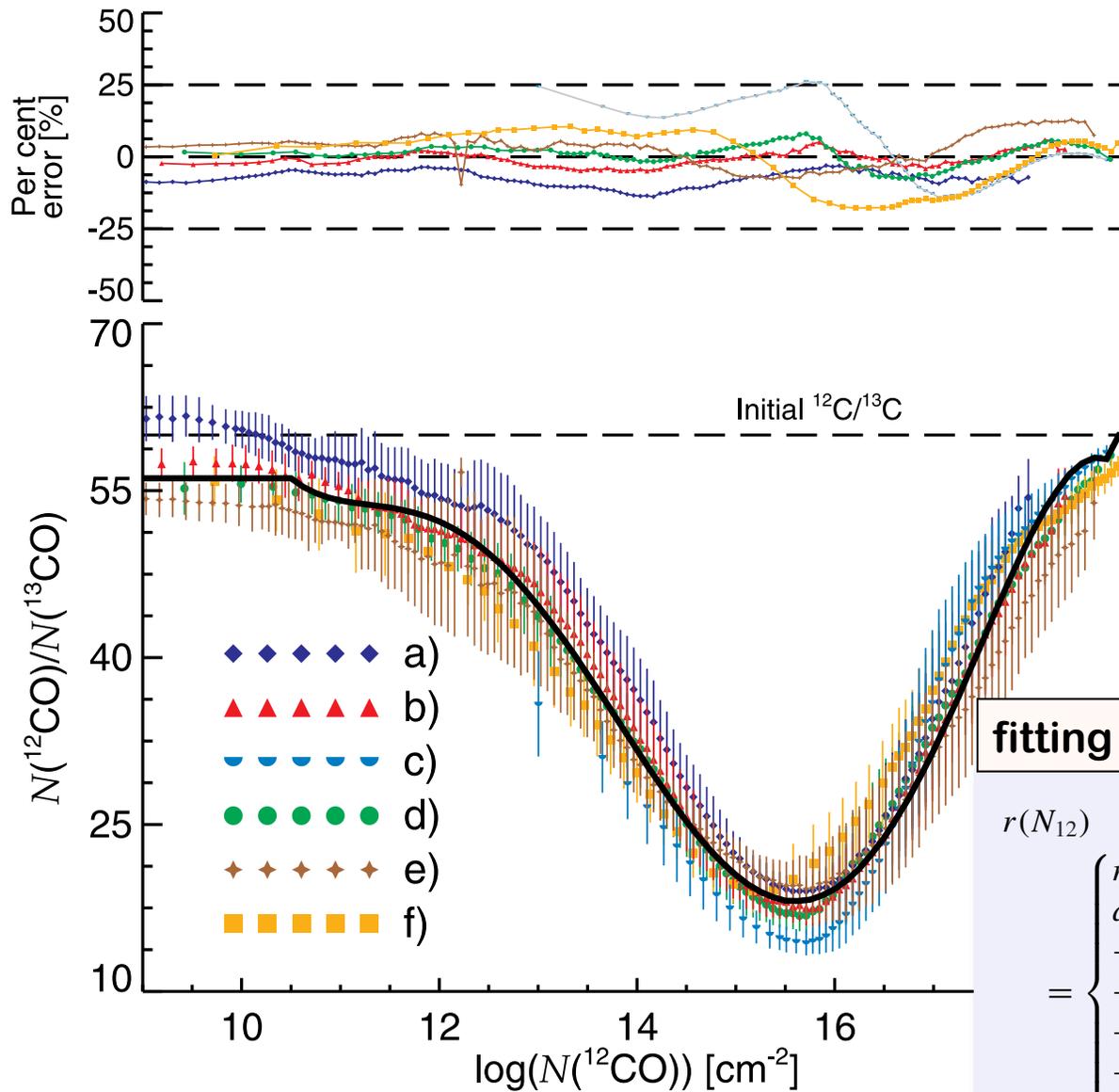
(Szücs et al. 2014, MNRAS 445, 4055-4072)

White contour shows  $5 \times 10^{21} \text{ cm}^{-2}$   
→ overall density is not changing significantly

# Results – $N(^{12}\text{CO})/N(^{13}\text{CO})$ column densities ratio



# Fitting formula

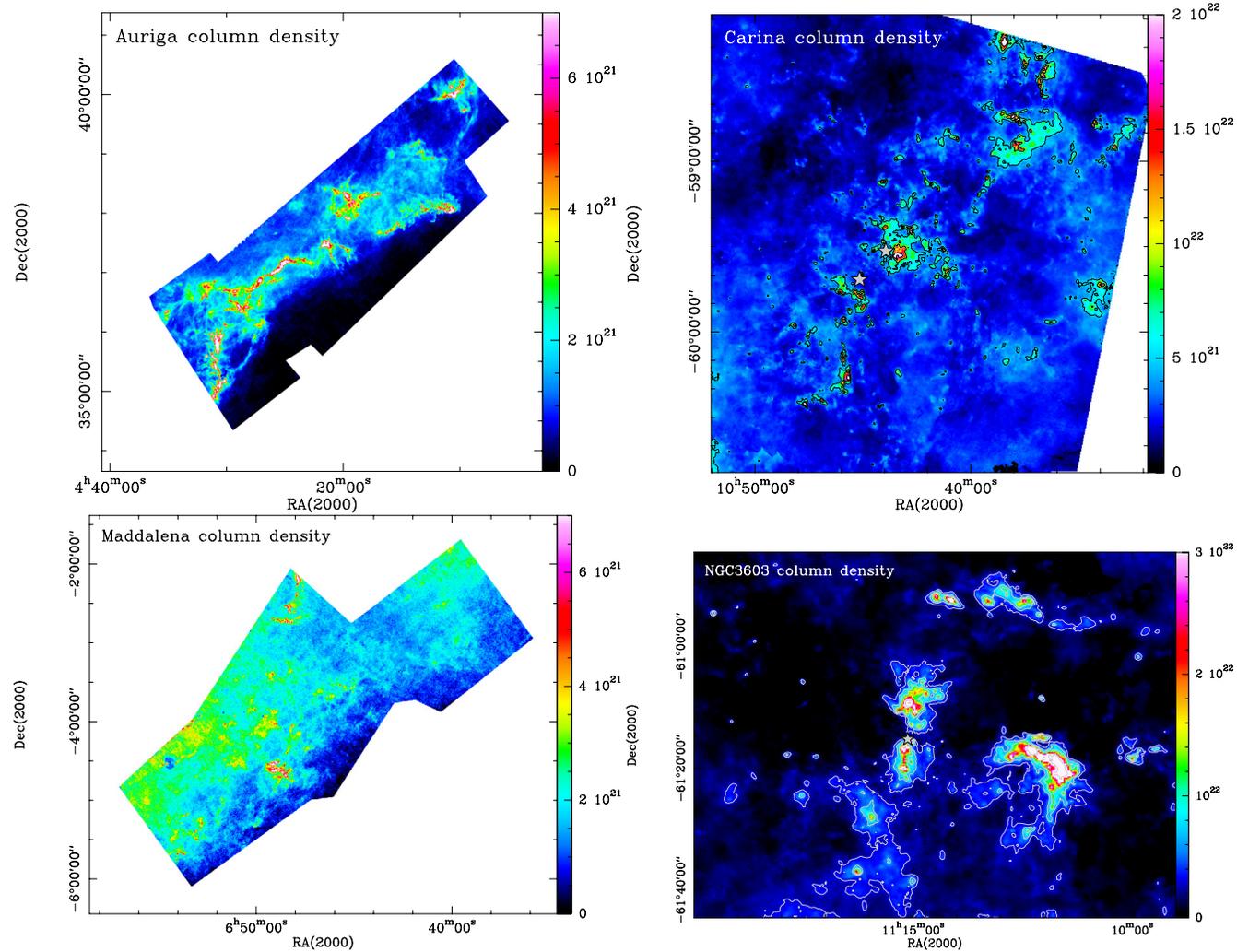


fitting formula:

$$r(N_{12}) = \begin{cases} r(N_{12} = 3.2 \times 10^{10}) & \text{if } N_{12} < 3.2 \times 10^{10} \\ a_{0,12} + a_{1,12} \log_{10}(N_{12}) \\ \quad + a_{2,12} \log_{10}(N_{12})^2 \\ \quad + a_{3,12} \log_{10}(N_{12})^3 \\ \quad + a_{4,12} \log_{10}(N_{12})^4 \\ \quad + a_{5,12} \log_{10}(N_{12})^5 & \text{if } 3.2 \times 10^{10} \leq N_{12} \leq 6 \times 10^{18} \\ 60 & \text{if } N_{12} > 6 \times 10^{18} \end{cases}$$

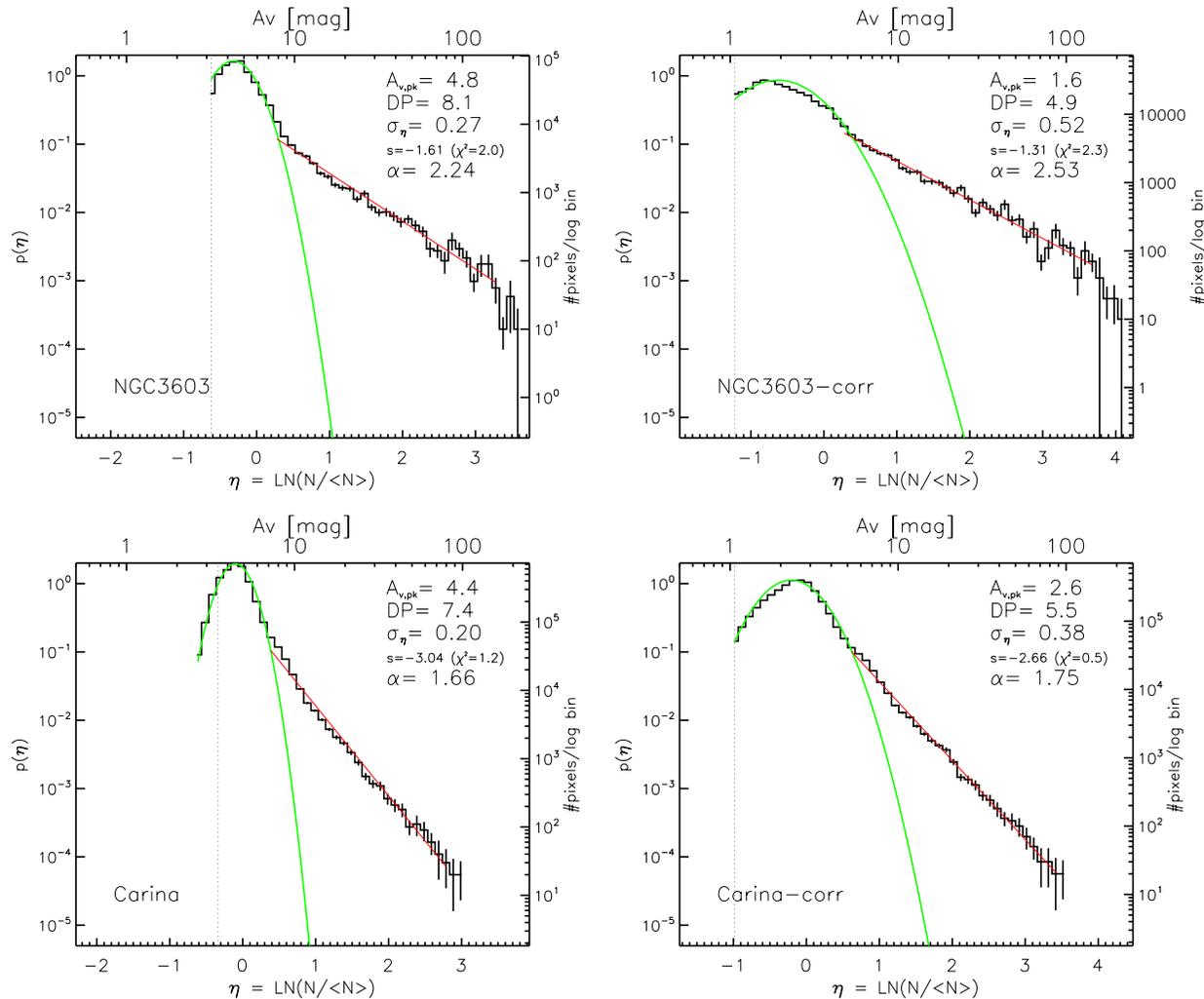
column density  
PDFs

# dust emission PDFs



**Fig. 1.** *Herschel* column density maps (in  $\text{cm}^{-2}$ ), all starting at zero) of Auriga, Maddalena, NGC 3603, and Carina after correcting for line-of-sight contamination and removing noisy edges and areas where there was no overlap between PACS and SPIRE. The contour levels are 3, 6, 10, and  $50 \times 10^{21} \text{ cm}^{-2}$  for NGC 3606 and 5, 10, and  $20 \times 10^{21} \text{ cm}^{-2}$  for Carina.

# influence of fore/background

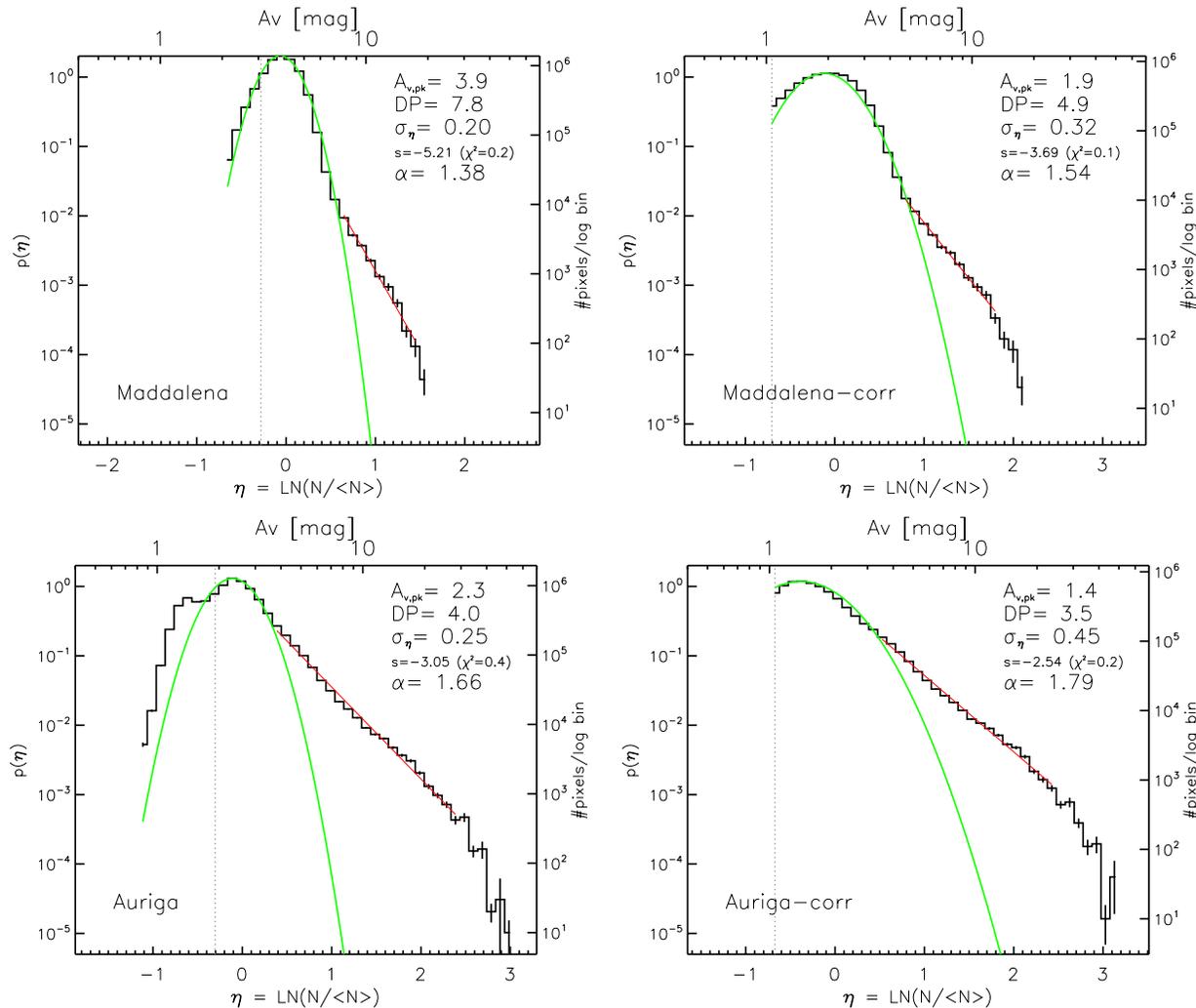


high-mass  
SF region

results of fore/background  
correction:

- peak of 'log-normal' shifts to lower  $A_v$
- transition from 'log-normal' to power-law shifts to lower  $A_v$
- power-law tail remains

# influence of fore/background

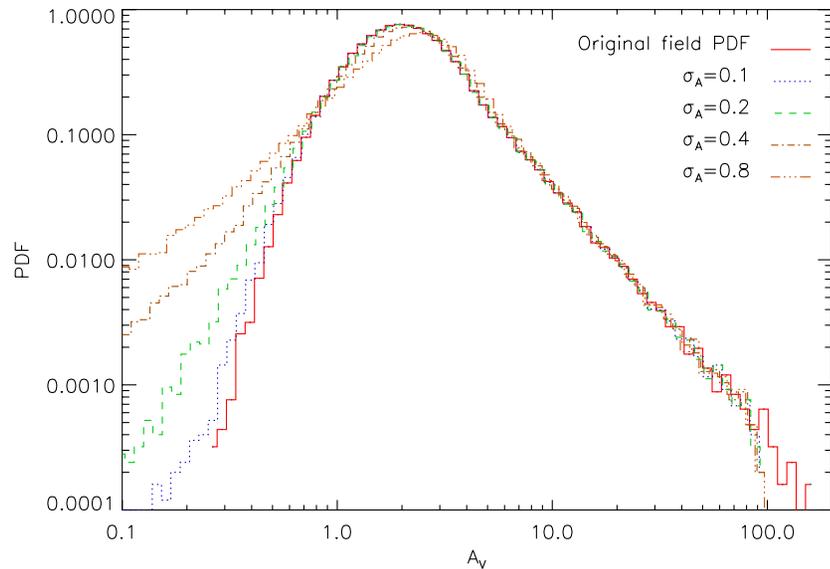


**low-mass  
SF region**

results of fore/background correction:

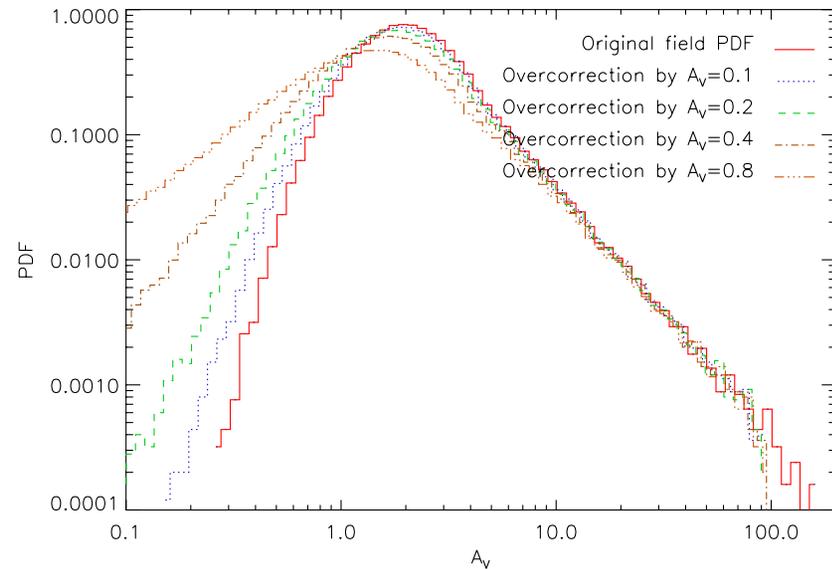
- peak of 'log-normal' shifts to lower  $A_v$
- transition from 'log-normal' to power-law shifts to lower  $A_v$
- power-law tail remains

# detailed analysis on synthetic data



**Fig. 8.** Simulations of reconstructed PDFs observed with different amplitudes of noise  $\sigma_A$ , expressed in terms of visual extinction. The reconstruction does not depend on the absolute value of the foreground/background contamination.

different noise levels

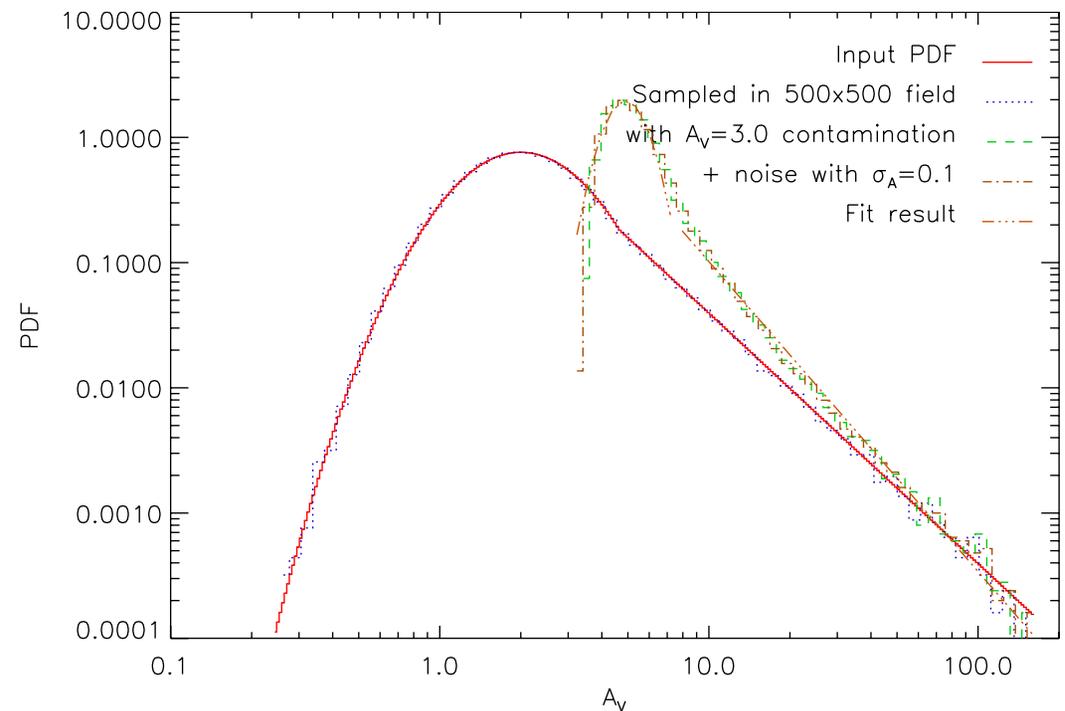
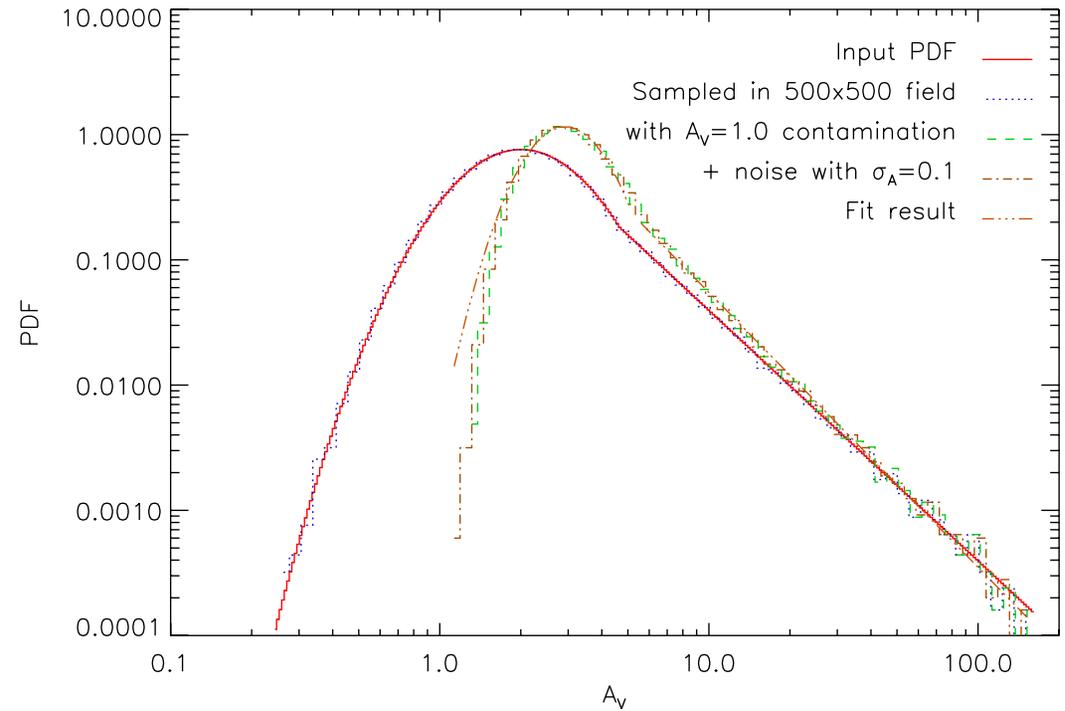


**Fig. 9.** Simulations of a PDF with negligible noise ( $\sigma_A = 0.01$ ) when applying values that are too high for the contamination correction  $\Delta A_v$ . The reconstruction does not depend on the absolute value of the foreground/background contamination but only on the difference between actual contamination and subtracted contamination.

influence of 'over correction'

# 2 examples

fore/background correction  
leads to  
— flatter power laws  
— wider ‘log-normal’ part  
in the standard fitting  
approach



turbulence  
and the IMF



# different statistical approaches

- there are different quantitative IMF based on turbulence
  - Padoan & Nordlund (2002, 2007)
  - Hennebelle & Chabrier (2008, 2009)
  - Hopkins (2012)
  - all relate the mass spectrum to statistical characteristics of the turbulent velocity fields

THE ASTROPHYSICAL JOURNAL, 684:395–410, 2008 September 1

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## ANALYTICAL THEORY FOR THE INITIAL MASS FUNCTION: CO CLUMPS AND PRESTELLAR CORES

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*Received 2008 February 12; accepted 2008 May 4*



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doi:[10.1088/0004-637X/702/2/1428](https://doi.org/10.1088/0004-637X/702/2/1428)

## ANALYTICAL THEORY FOR THE INITIAL MASS FUNCTION. II. PROPERTIES OF THE FLOW

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*Received 2009 April 1; accepted 2009 July 17; published 2009 August 21*



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ANA Monthly Notices of the ROYAL ASTRONOMICAL SOCIETY  
Mon. Not. R. Astron. Soc. **423**, 2037–2044 (2012) doi:[10.1111/j.1365-2966.2012.20731.x](https://doi.org/10.1111/j.1365-2966.2012.20731.x)

<sup>1</sup> Laboratoire

**The stellar initial mass function, core mass function and the last-crossing distribution**

Philip F. Hopkins<sup>★</sup>

*Department of Astronomy, University of California Berkeley, Berkeley, CA 94720, USA*

OW

05, France

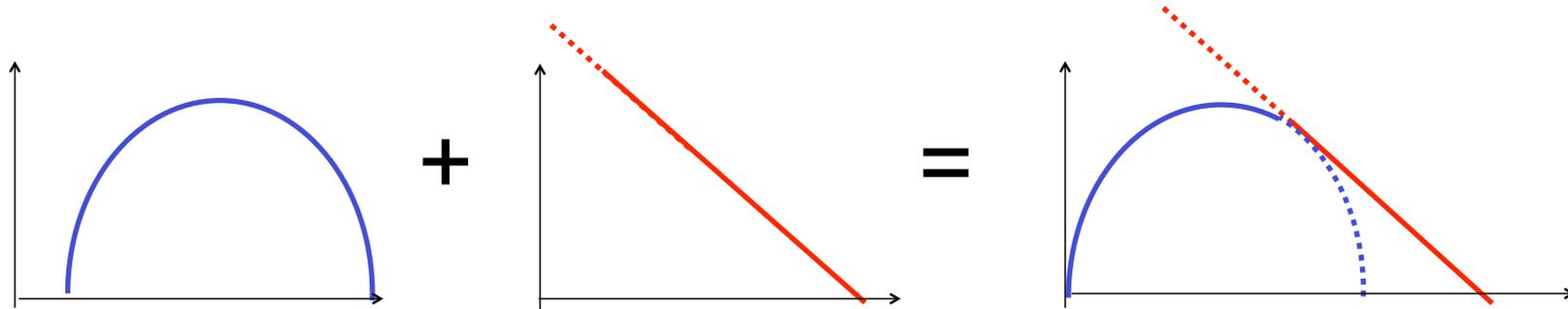


# different statistical approaches

- there are different quantitative IMF based on turbulence
  - Padoan & Nordlund (2002, 2007)
  - Hennebelle & Chabrier (2008, 2009)
  - Hopkins (2012)
  - all relate the mass spectrum to statistical characteristics of the turbulent velocity fields
- there are alternative approaches
  - IMF as closest packing problem / *sampling* problem in *fractal* clouds (Larson 1992, 1995, Elmegreen 1997ab, 2000ab, 2002)
  - IMF as purely *statistical* problem (Larson 1973, Zinnecker 1984, 1990, Adams & Fatuzzo 1996)
  - IMF from (proto)stellar *feedback* (Silk 1995, Adams & Fatuzzo 1996)
  - IMF from competitive *coagulation* (Murray & Lin 1995, Bonnell et al. 2001ab, etc.)



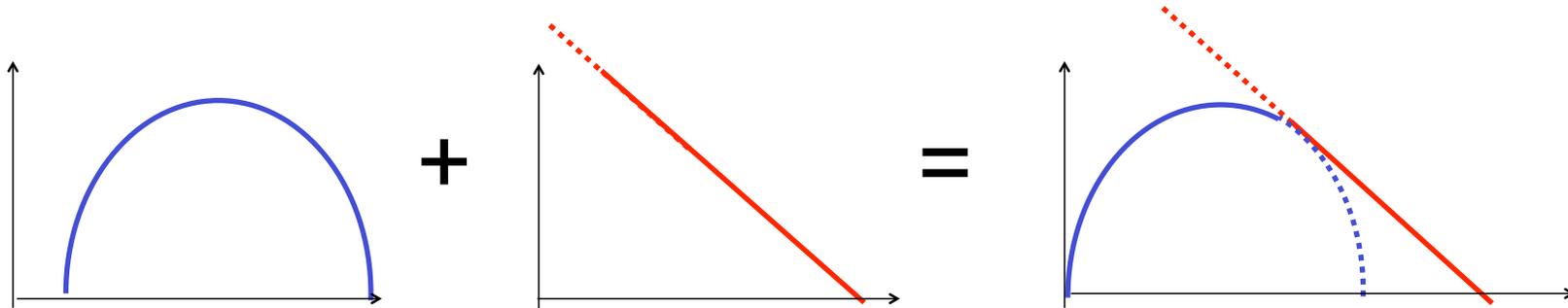
# caveat: everybody gets the IMF!



- combine scale free process → *POWER LAW BEHAVIOR*
  - turbulence (Padoan & Nordlund 2002, Hennebelle & Chabrier 2008, Hopkins 2008)
  - gravity in dense clusters (Bonnell & Bate 2006, Klessen 2001)
- with highly stochastic processes → central limit theorem  
→ *GAUSSIAN DISTRIBUTION*
  - basically mean thermal Jeans length (or feedback)
  - universality due to dust physics: coupling between dust and gas insensitive to radiation field and metallicity  
(Elmegreen et al. 2008, Omukai et al. 2005)



# caveat: everybody gets the IMF!



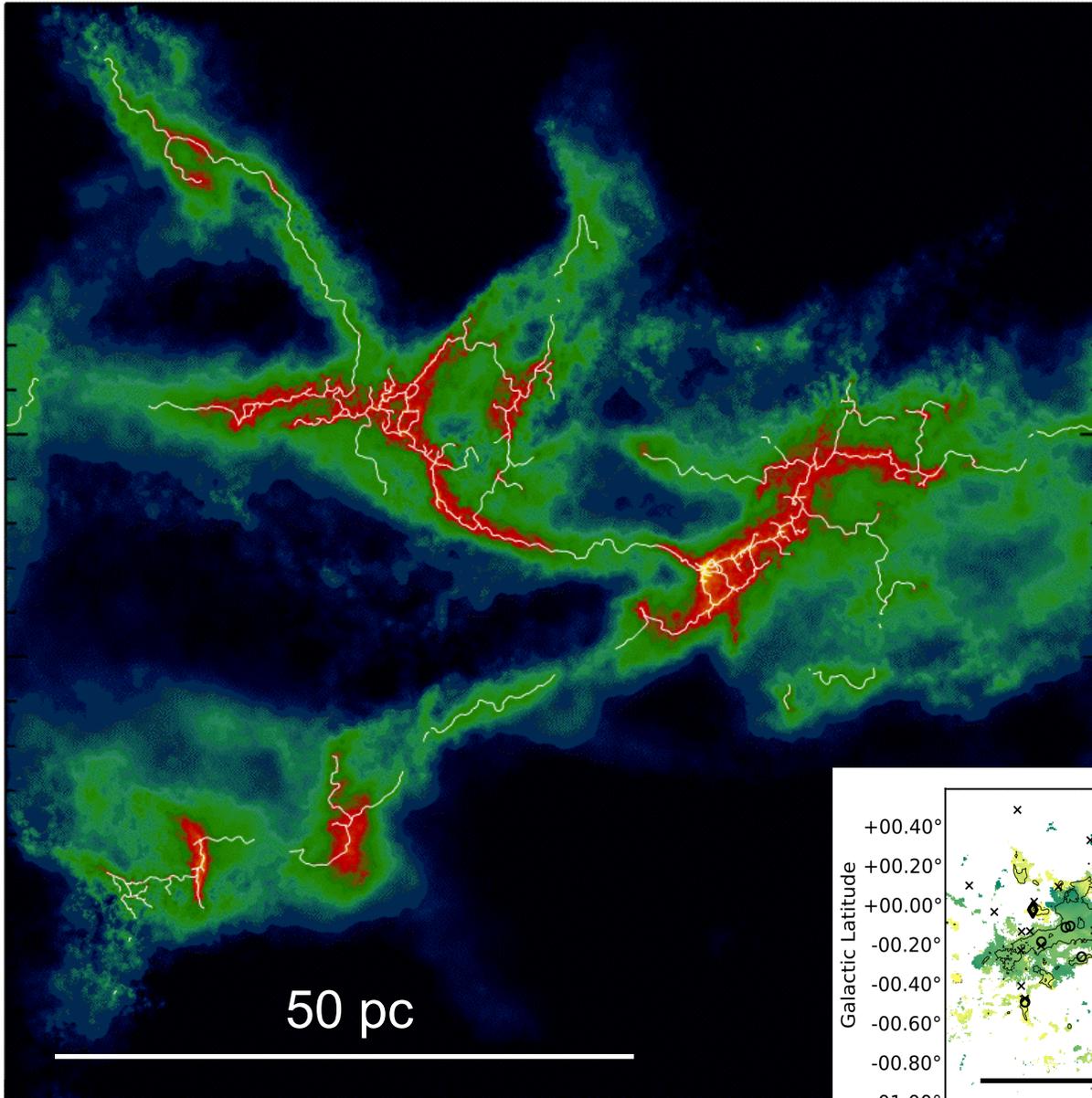
“everyone” gets the right IMF  
→ better look for secondary indicators

- *stellar multiplicity*
- protostellar *spin* (including disk)
- *spatial distribution + kinematics* in young clusters
- *magnetic field strength and orientation*



Properties of star  
forming filaments

# large-scale filaments



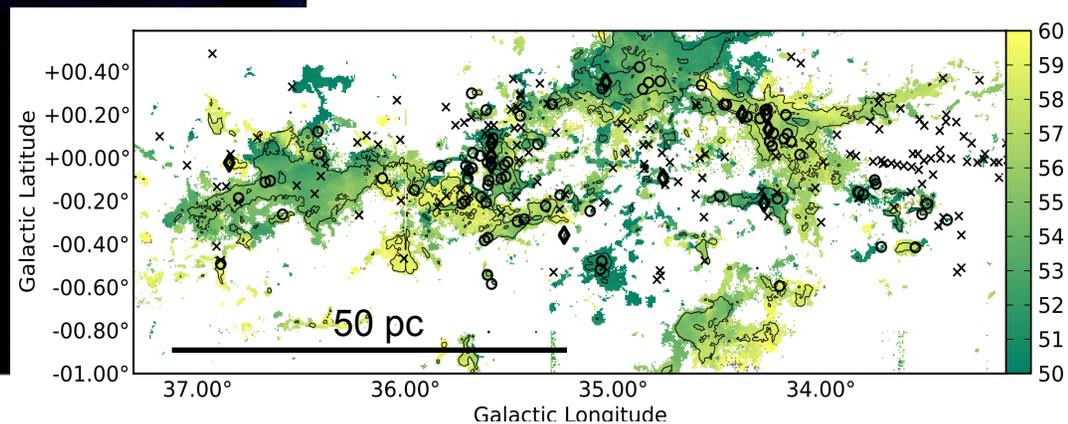
Smith et al. (2014, MNRAS, 445, 2900)

## *next steps:*

studying details of ISM morphology and star formation in dedicated zoom-in simulation

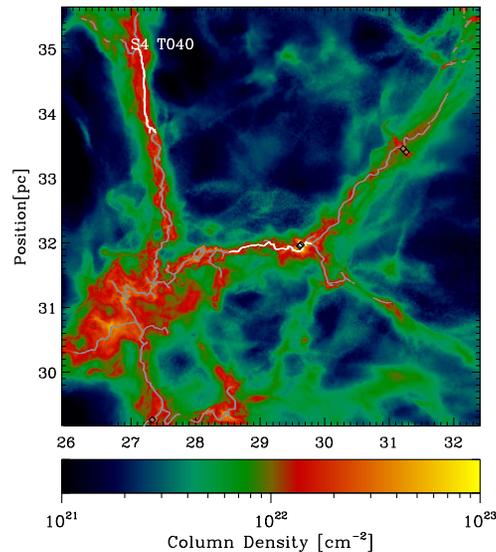
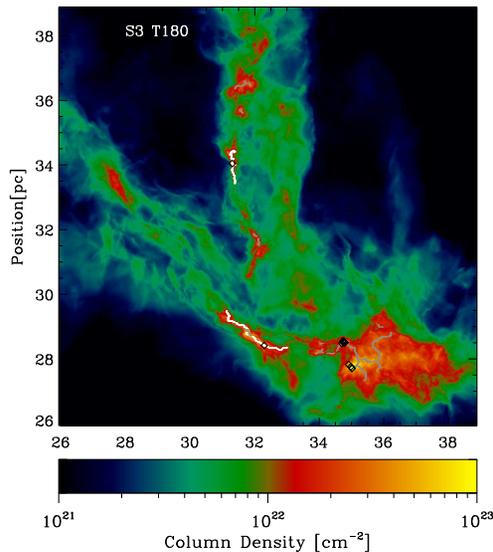
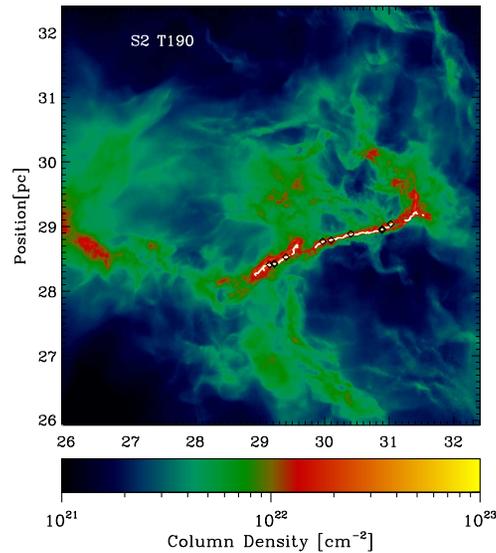
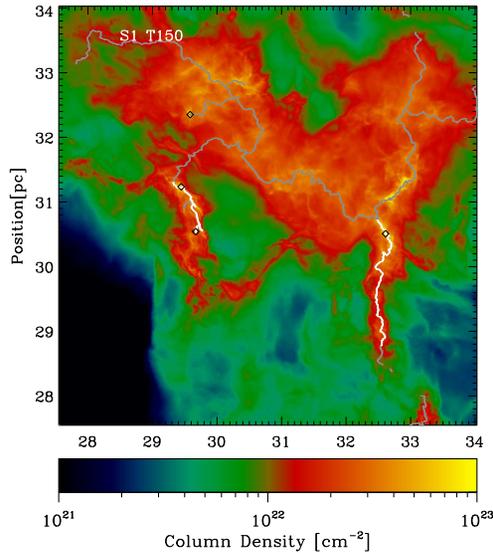
## *example:*

giant molecular cloud complex ( $\sim 10^6 M_{\odot}$ ) viewed in the plane of the disk.



Ragan et al., 2014, A&A submitted, arXiv:1403.1450

# zoom-in on filaments



## ***next steps:***

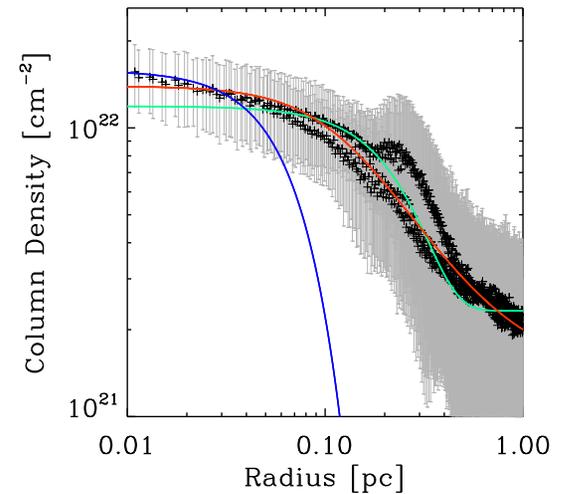
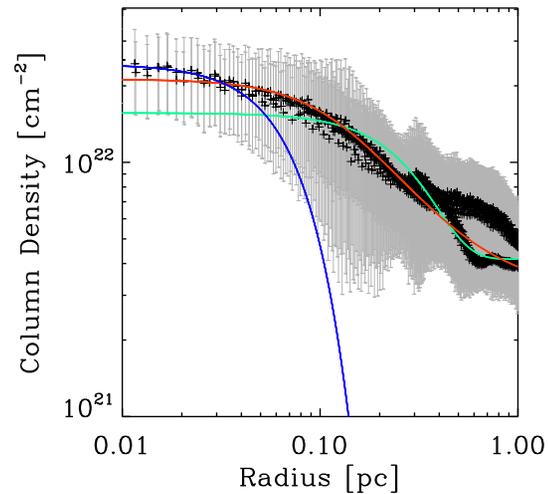
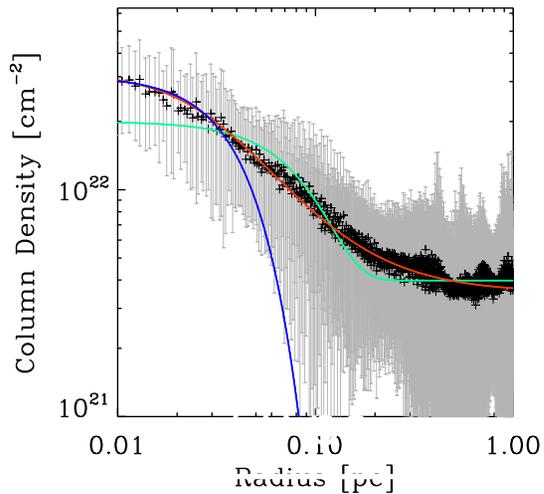
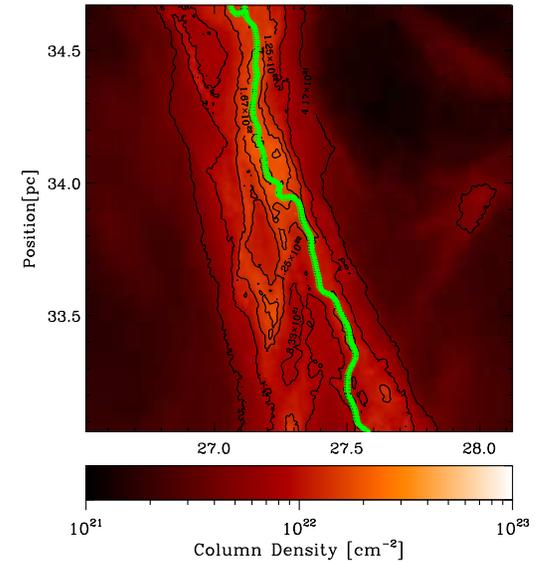
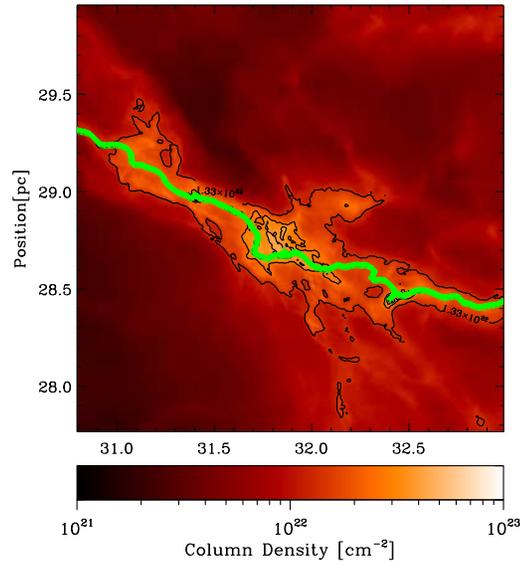
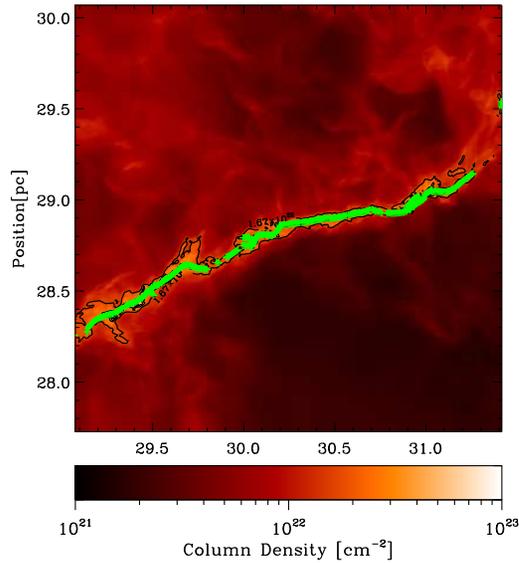
studying details of ISM morphology and star formation in dedicated zoom-in simulation

*(resolution  $\approx 2000$  AU, with full chemistry)*

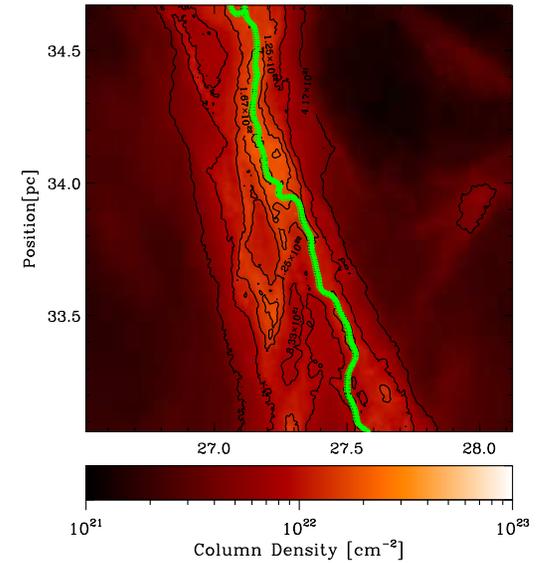
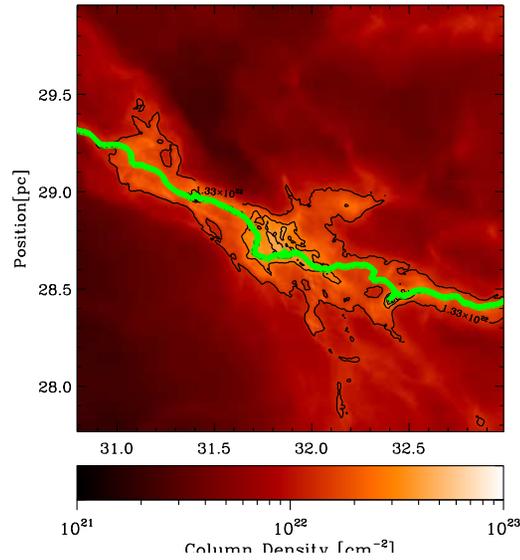
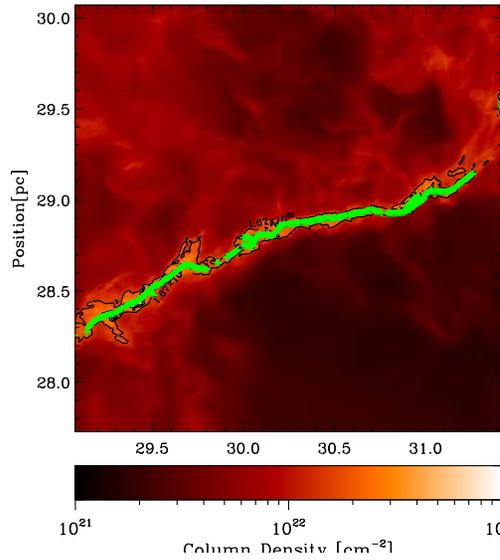
## ***analysis:***

- morphology
- velocity
- chemistry
- observations (dust maps for Herschel, CO, N<sub>2</sub>H<sup>+</sup>, HCN, etc. for line obs.)

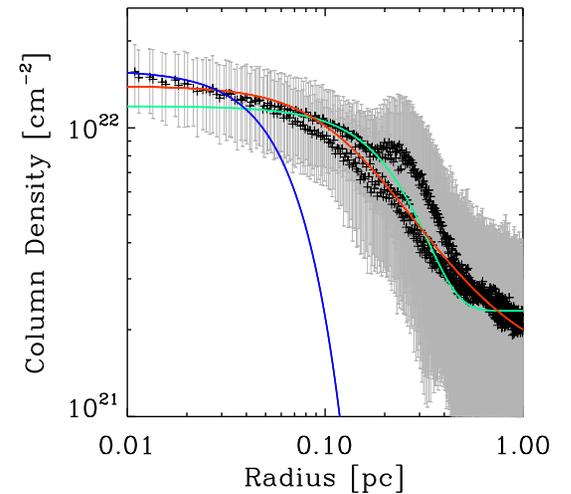
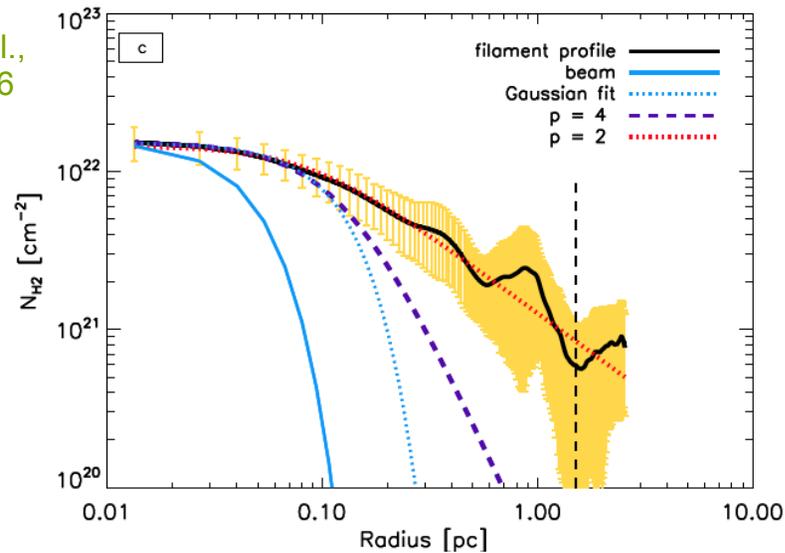
# filaments do not have universal width



# filaments do not have universal width

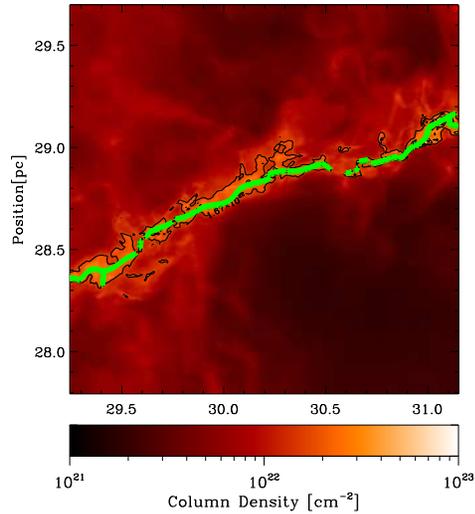


Arzoumanian, et al.,  
2011, A&A, 529, L6

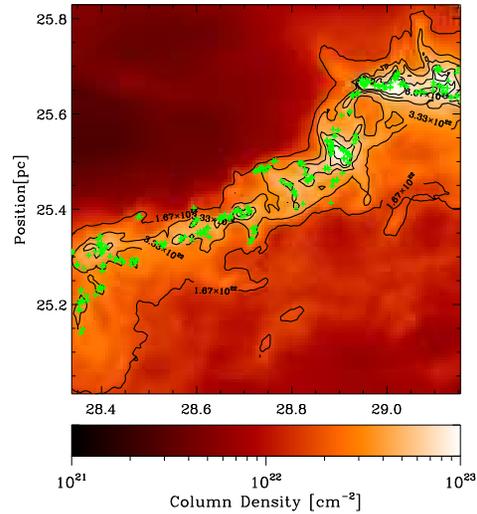


Smith et al. (2014, MNRAS, 445, 2900)

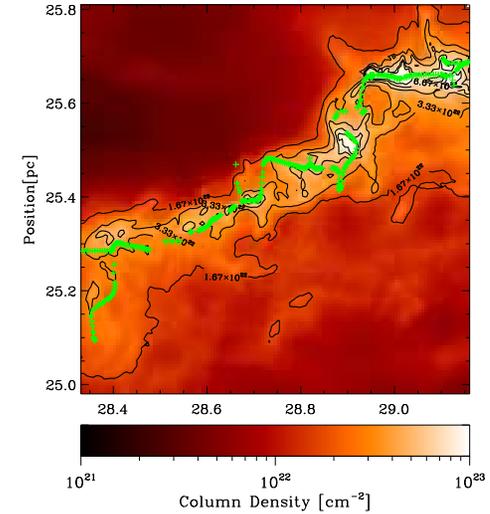
# 3D filaments have complex structure



2D filament detection shows nice coherent filament

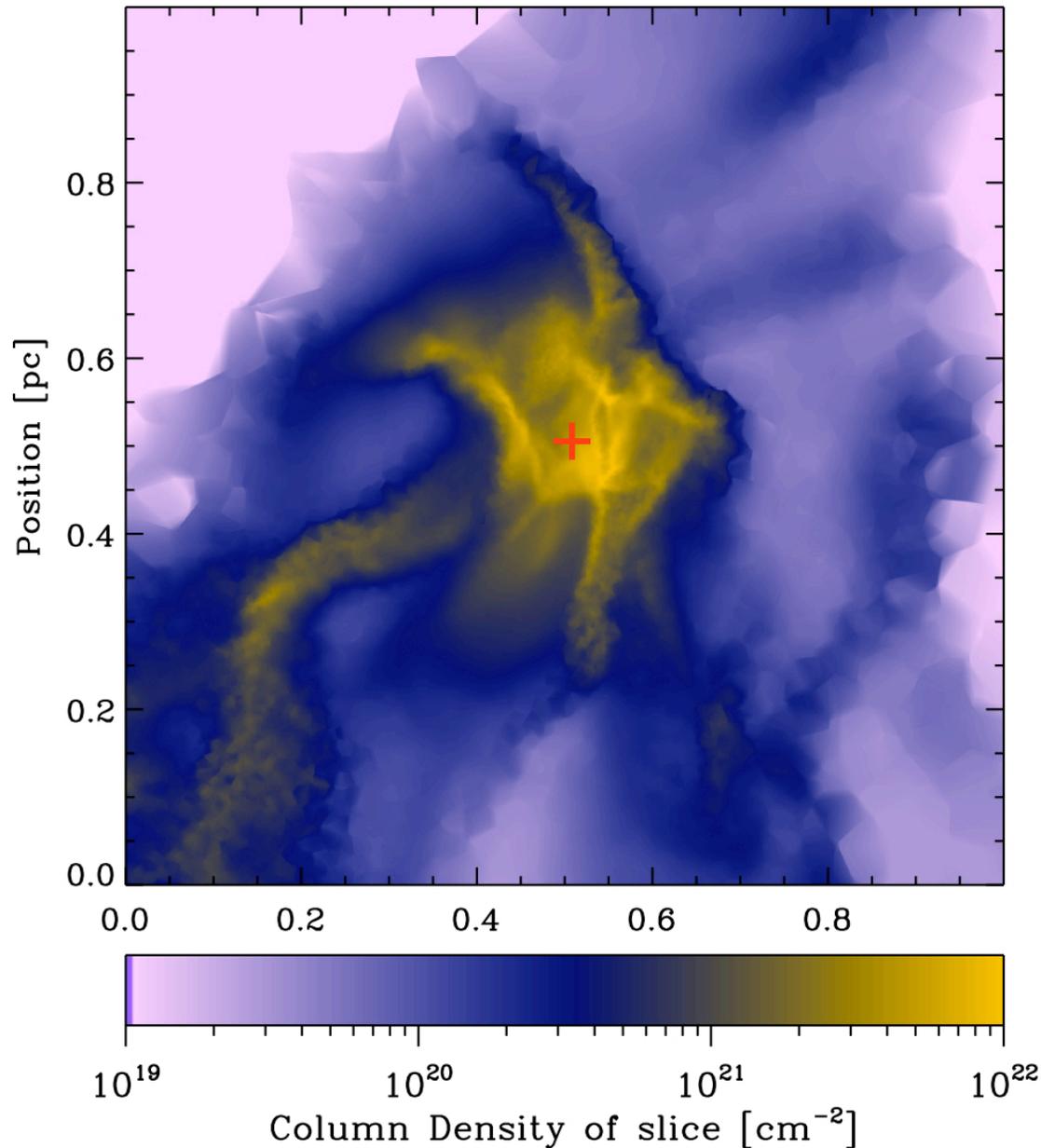


2D + LOS peak detection shows complex structure

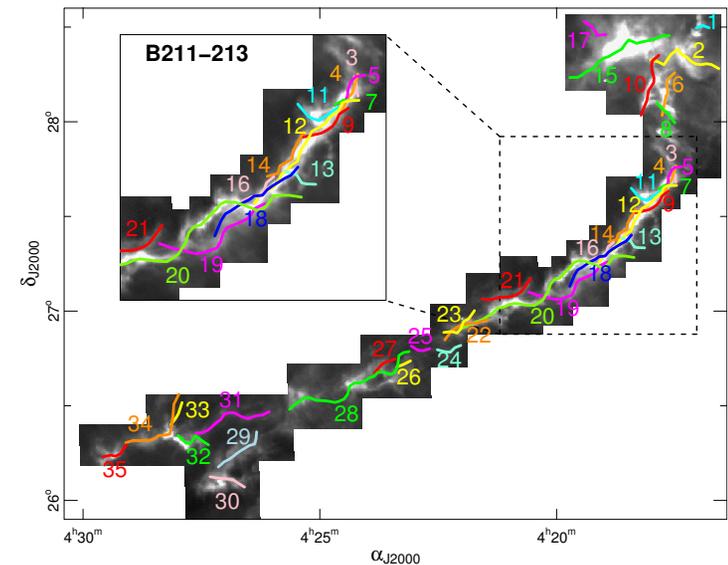


full 3D filament analysis confirms this picture

# walk along the filament



- walking along the filament exhibits complex 3D structure that is now (fully) seen in projected density
- is this similar to the filament fibers proposed by Hacar et al. (2013, A&A, 554, 55)



summary

# summary

- controversies / puzzles
  - column density PDFs: *do we really understand them?*  
—> *more work needed, also on line PDFs*
  - molecular gas: *are we sure we see all H<sub>2</sub> gas?*  
—> *we may be missing lots of H<sub>2</sub> gas in clouds*
  - importance of dynamics: *what sets the IMF?*  
—> *the IMF is easy to get, better look for other tracers*
  - filaments: *are they universal?*  
—> *much more work needed including kinematic tracers*



thanks