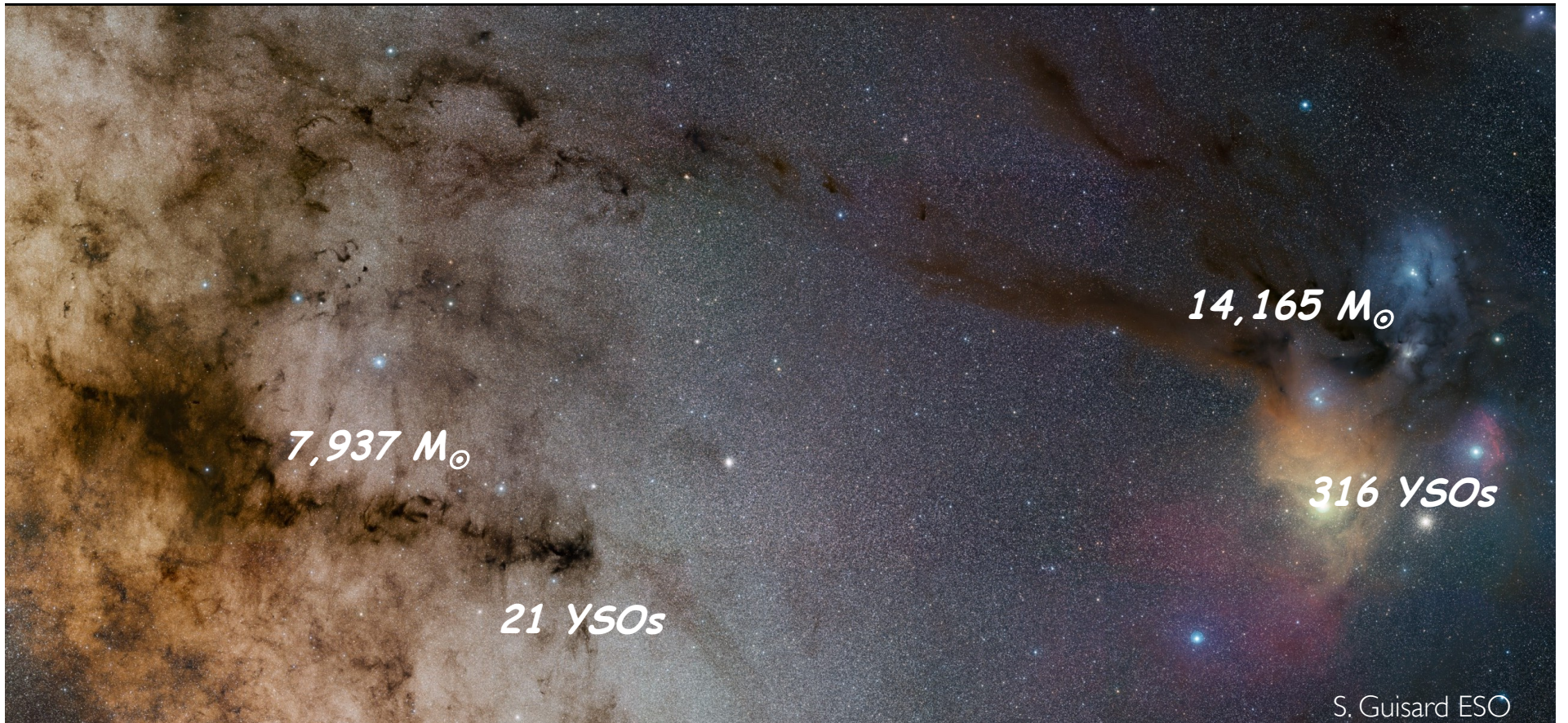


*Star Formation Rates in Molecular Gas and the  
Nature of the Extragalactic Scaling Relations*

With:

Marco Lombardi, University of Milan

Joao Alves & Jan Forbrich, University of Vienna



*Pipe Nebula*

*Rho Ophiuchi Cloud*

$$\text{SFR}_{\text{Oph}} = 15 \times \text{SFR}_{\text{Pipe}}$$

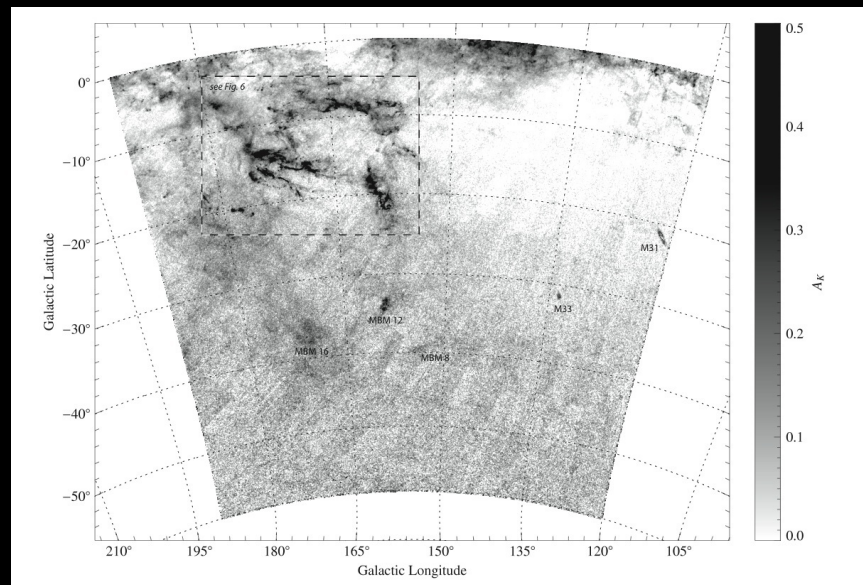
# Inventory of Local Star Formation Activity

*Infrared Extinction & Cloud Masses*

# Inventory of Local Star Formation Activity: Molecular Clouds

Cloud Sample:

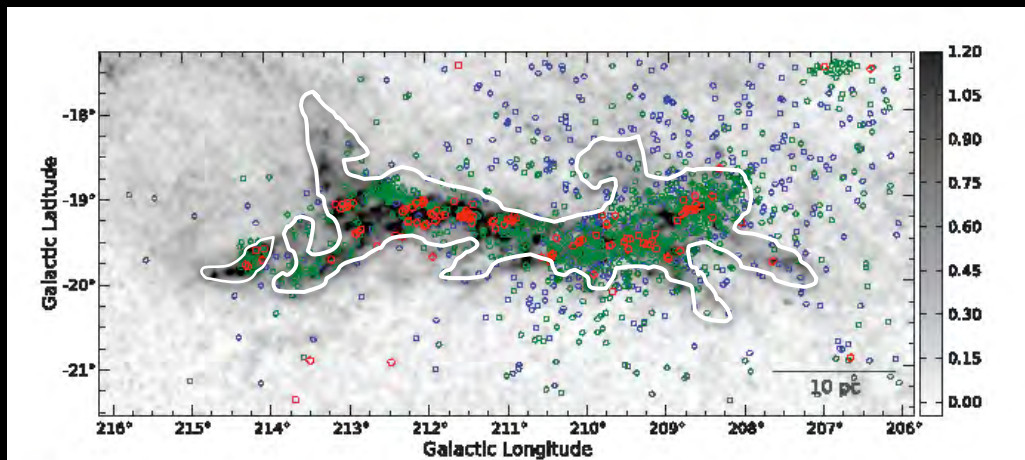
Wide-Field 2MASS Extinction Survey of  
11 Local (<0.5 kpc) Clouds



Cloud:	Mass ( $10^4 M_{\odot}$ )
Orion A	6.77
Orion B	7.18
California	9.99
Perseus	1.84
Taurus	1.49
Ophiuchus	1.41
RCrA	0.11
Pipe	0.79
Lupus 3	0.22
Lupus 3	0.14
Lupus 4	0.08

# Inventory of Local Star Formation Activity: Young Stellar Objects

Mining the Literature; mostly IR (e.g., SPITZER)

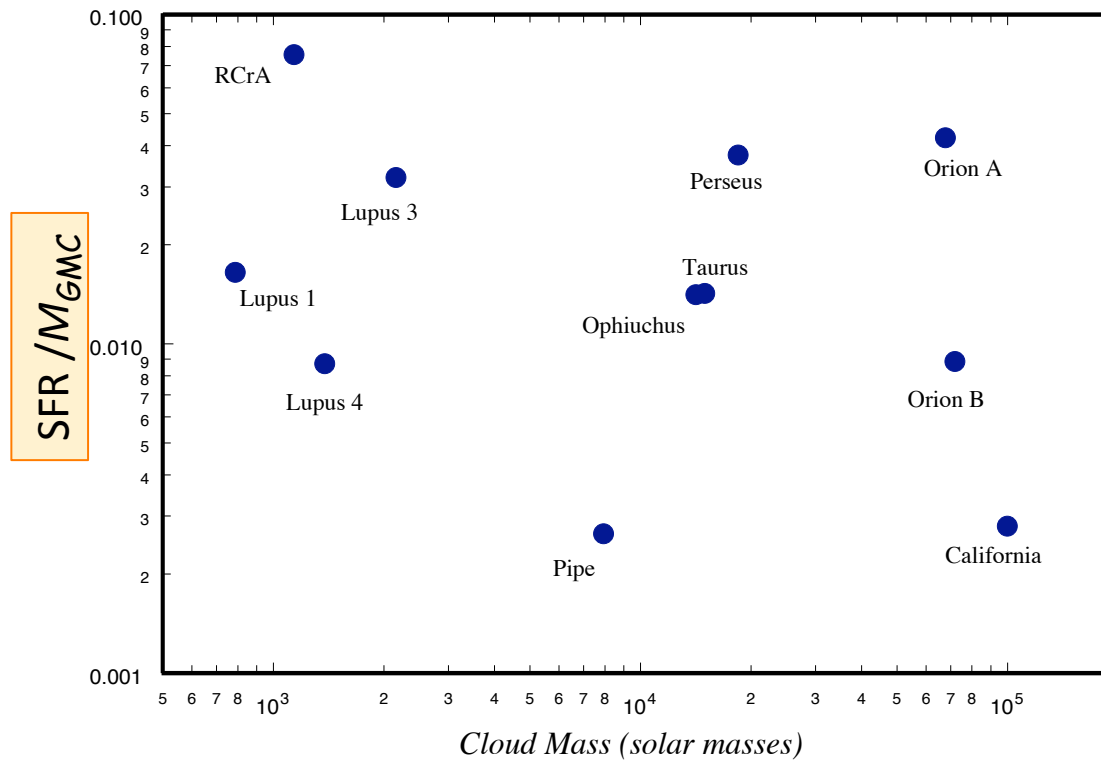


Cloud:	YSOs
Orion A	2862
Orion B	635
California	279
Perseus	598
Taurus	335
Ophiuchus	316
RCrA	100
Pipe	21
Lupus 1	13
Lupus 3	69
Lupus 4	12

Large Variation in Specific Star Formation Rate

## Variations in the Efficiencies & Star Formation Rates of Local GMCs

$$\text{SFR} = (\langle m_* \rangle / t_{\text{sf}}) \times N(\text{YSOs}) = 0.25 \times 10^{-6} N(\text{YSOs}) M_{\odot}/\text{yr}$$



Greater than an order of magnitude variation, *independent* of cloud mass !

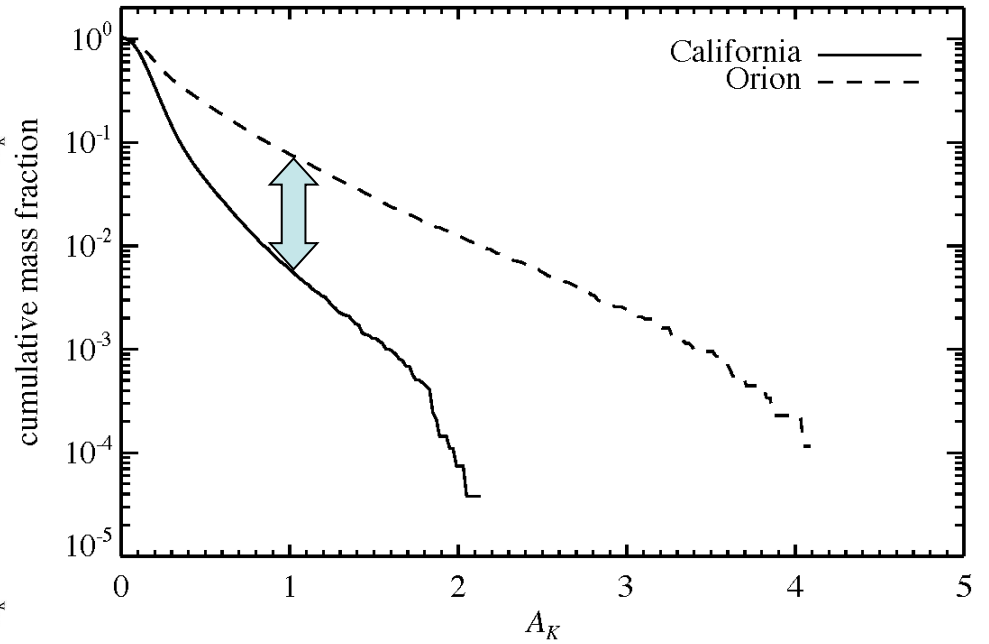
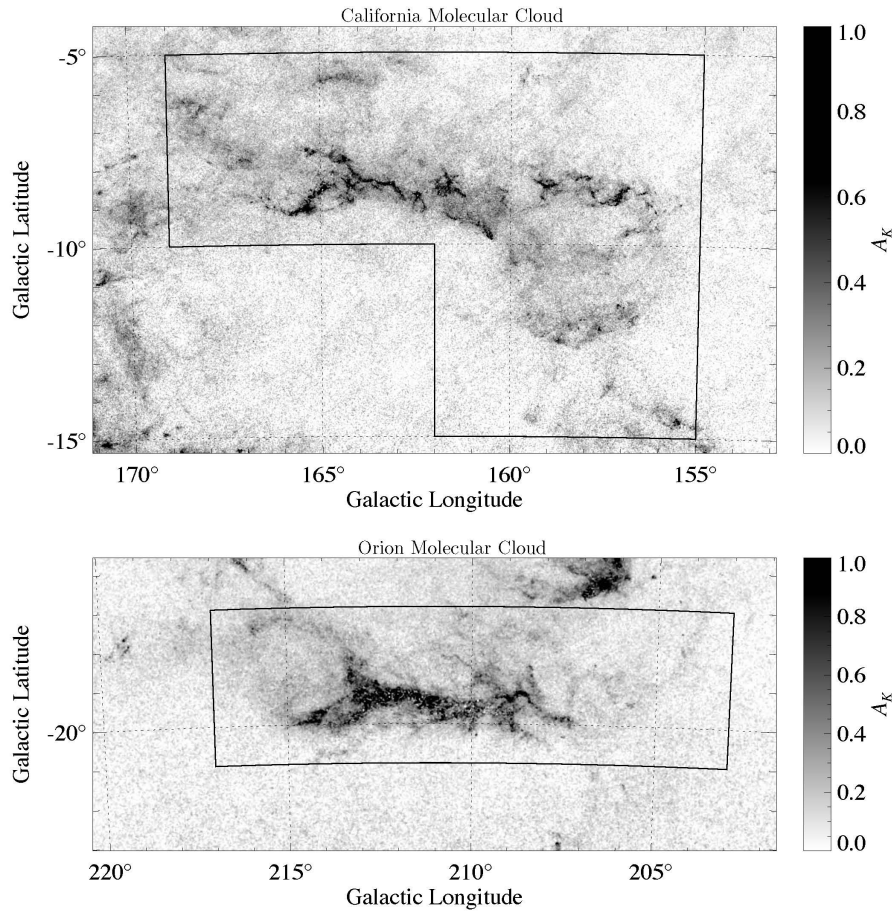
**What Determines the Star  
Formation Rate?**



## Comparing the California and Orion Molecular Clouds

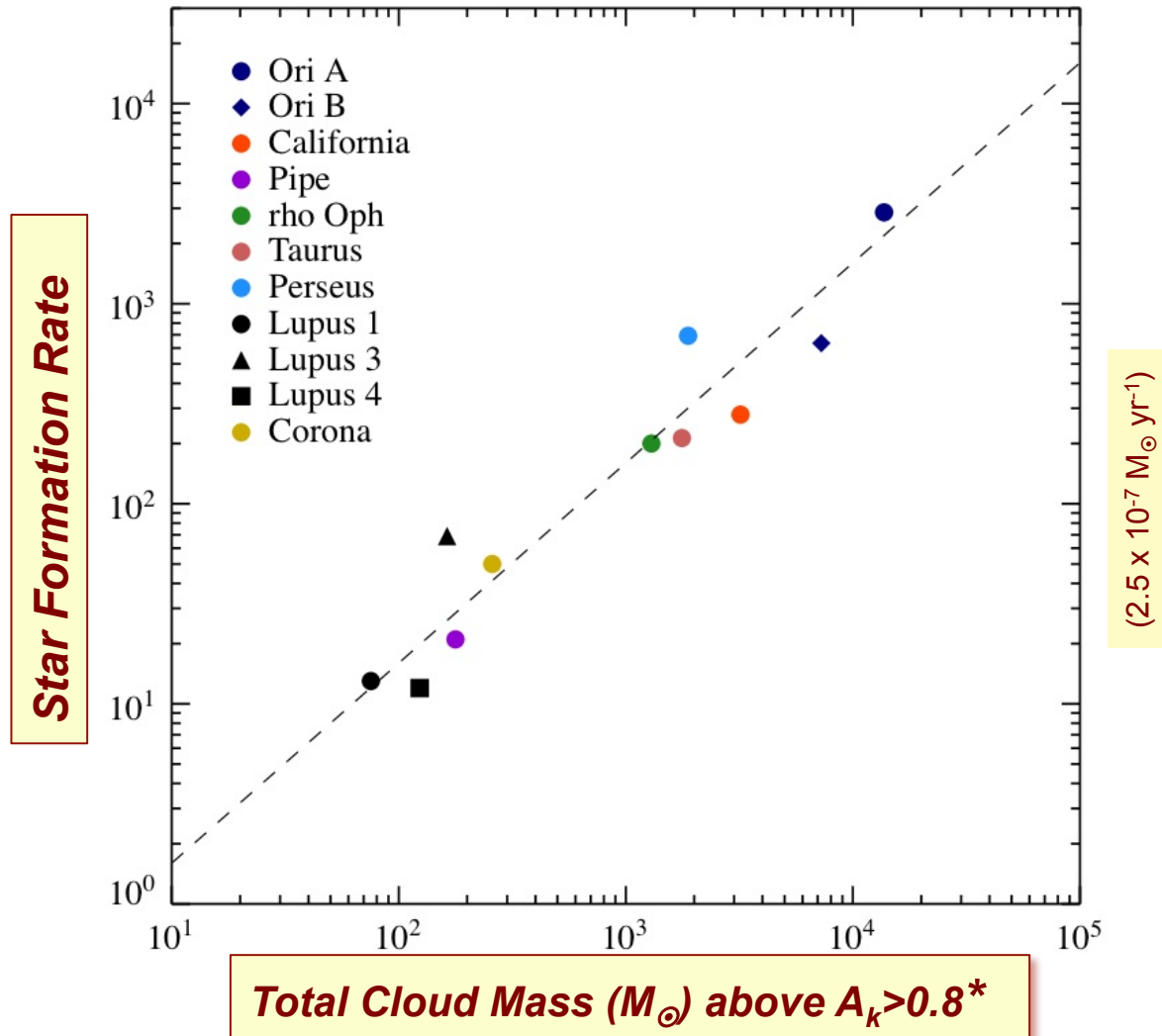
*The two clouds are nearly identical  
in mass & size*

*YSOs(Orion) > 10 x YSOs(California)  
SFR(Orion) > 10 x SFR(California)*



*OMC has 10 x as much material at  $A_K > 1$  mag as the CMC*

***SFR is directly proportional to total gas mass at  $A_k > 0.8^*$***



\* $A_k > 0.8$  corresponds to  $\Sigma_{\text{H}_2} > 116 M_\odot \text{ pc}^{-2}$  &  $\Sigma_{\text{H}_2+\text{He}} > 158 M_\odot \text{ pc}^{-2}$

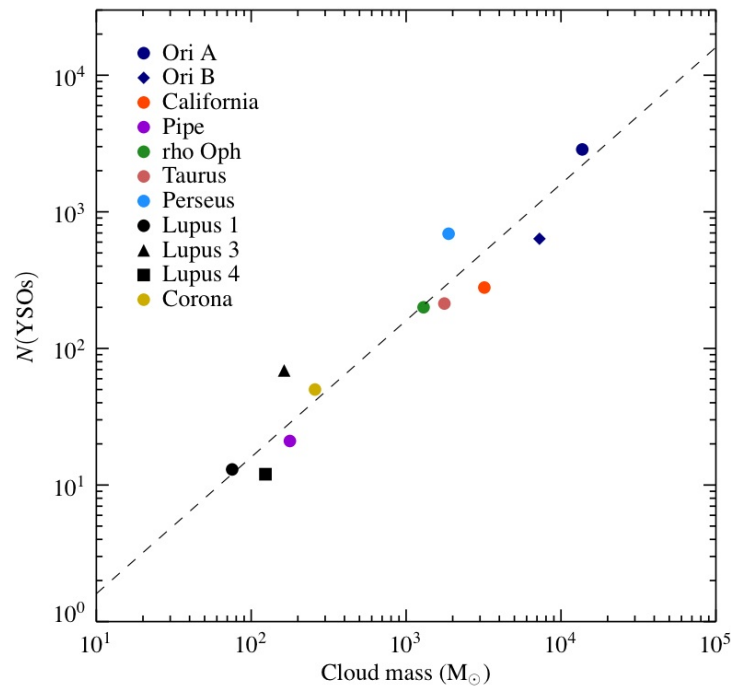
# Star Formation Scaling Laws for Local Clouds

# Star Formation Scaling Law for Local Clouds

$$\text{SFR} = 4.6 \times 10^{-8} M_{0.8} \text{ (M}_\odot \text{ yr}^{-1}\text{)}$$

Where:

$$M_{0.8} = \int_{0.8}^{\infty} M(A_K) dA_K$$



$$\text{SFR} = (t_{\text{gc}})^{-1} M_{0.8}$$

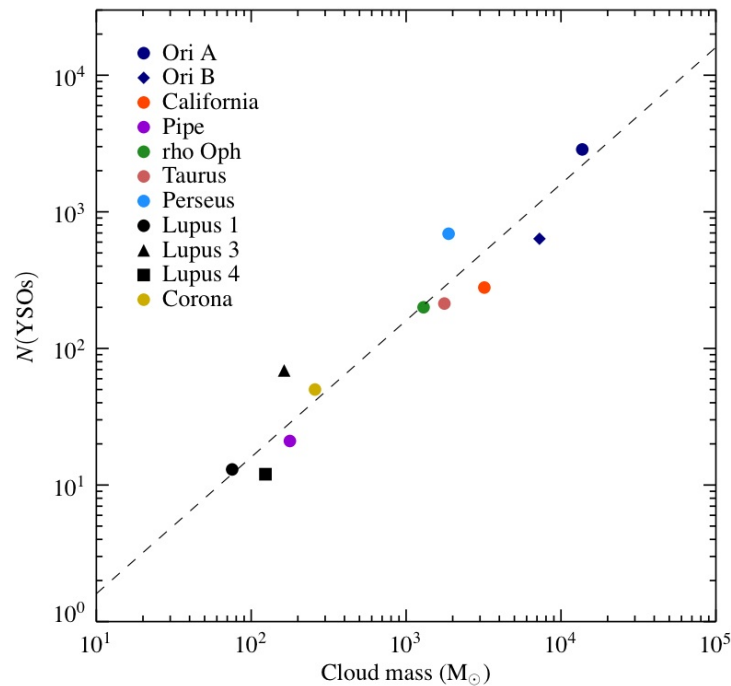
$t_{\text{gc}}$  = gas  
consumption time

$$= 2.2 \times 10^7 \text{ yrs}$$

# Star Formation Scaling Law for Local Clouds

$$\text{SFR} = 4.6 \times 10^{-8} M_{0.8} \text{ (M}_\odot \text{ yr}^{-1}\text{)}$$

$$M_{0.8} = \int_{\text{Volume}} \rho_{0.8}(V) dV = \langle \rho_{0.8} \rangle V_{0.8}$$



$$\text{SFR} = (t_{\text{gc}})^{-1} M_{0.8}$$

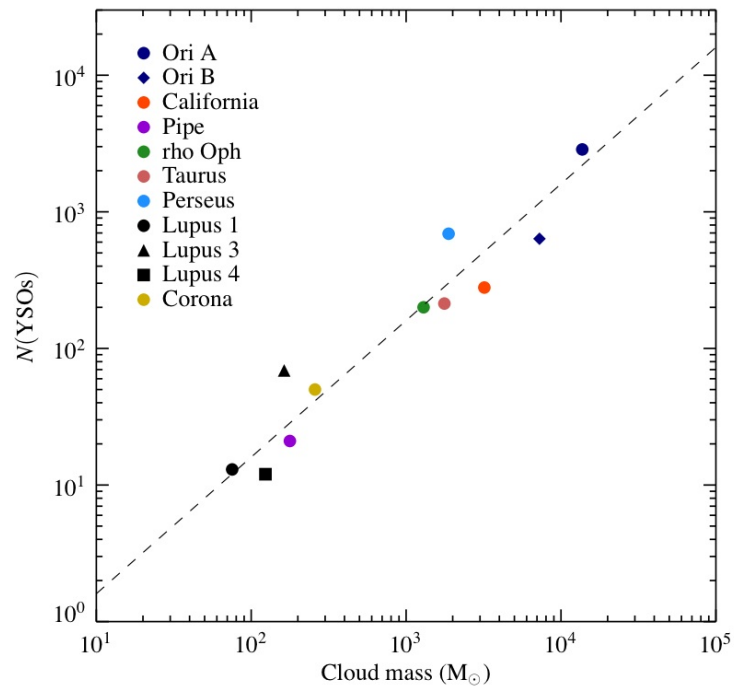
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$$\text{SFR} = 4.6 \times 10^{-8} M_{0.8} \text{ (M}_\odot \text{ yr}^{-1}\text{)}$$

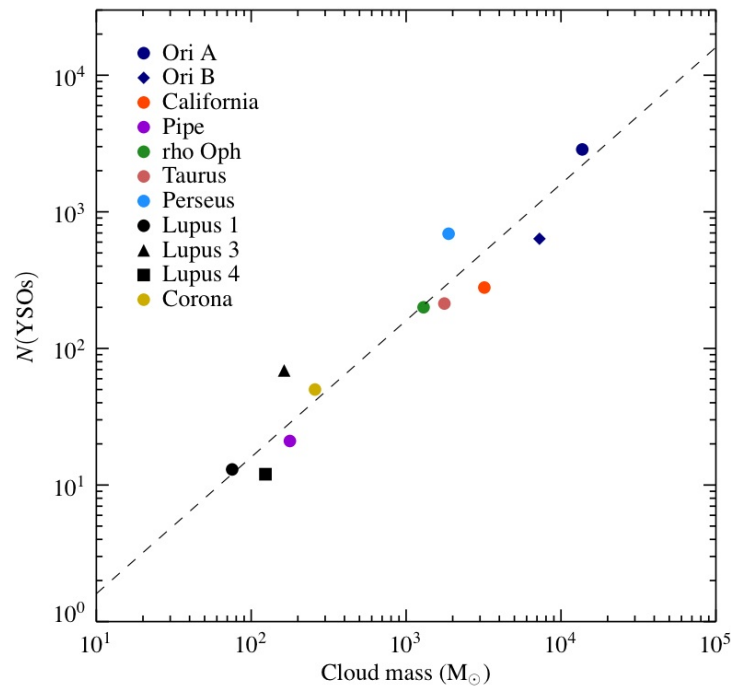
$$\text{SFR} = 4.6 \times 10^{-8} \langle \rho_{0.8} \rangle V_{0.8}$$



# Star Formation Scaling Law for Local Clouds

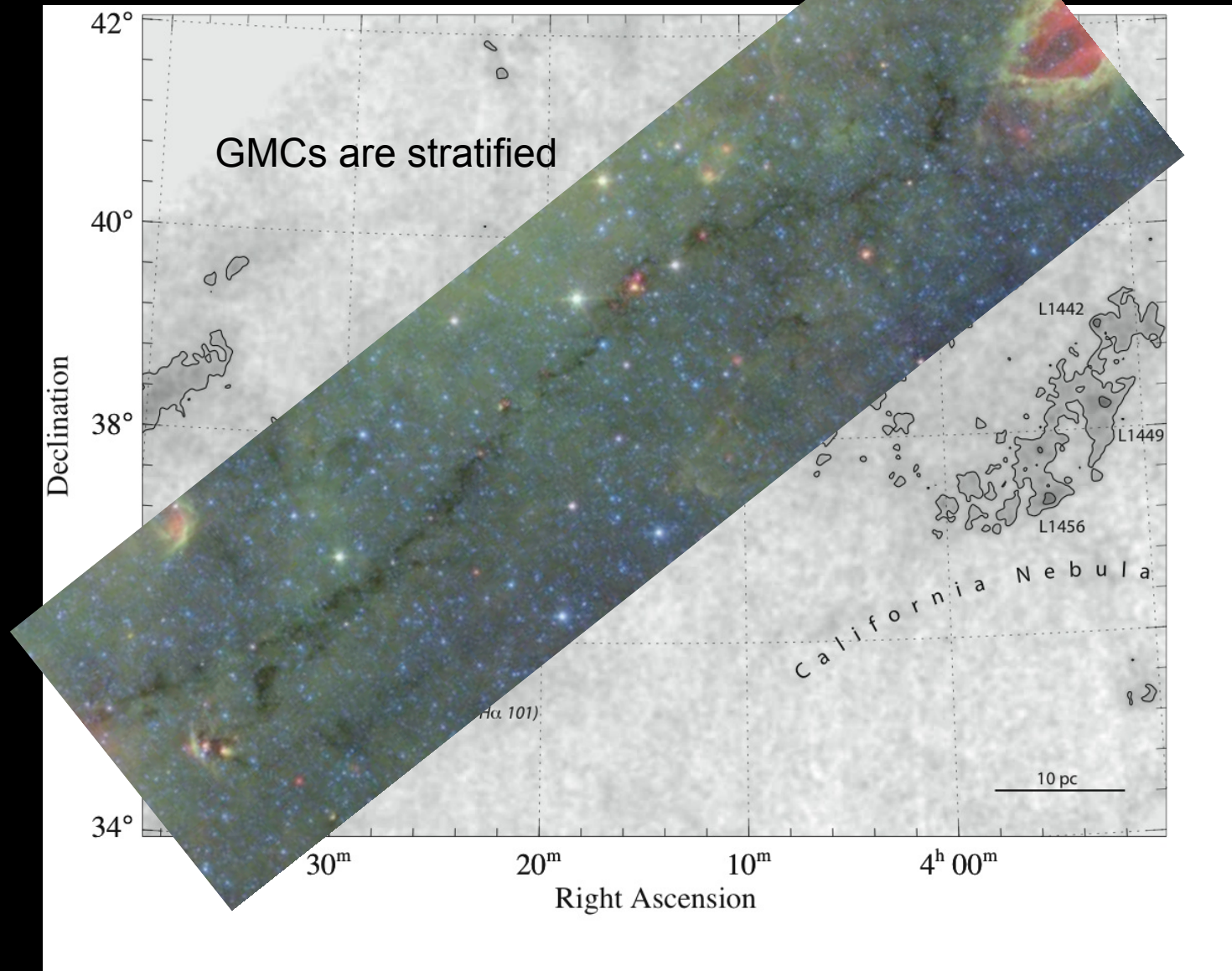
$$\text{SFR} = 4.6 \times 10^{-8} M_{0.8} \text{ (M}_\odot \text{ yr}^{-1}\text{)}$$

**A Linear Volumetric Scaling Law for Star Formation**



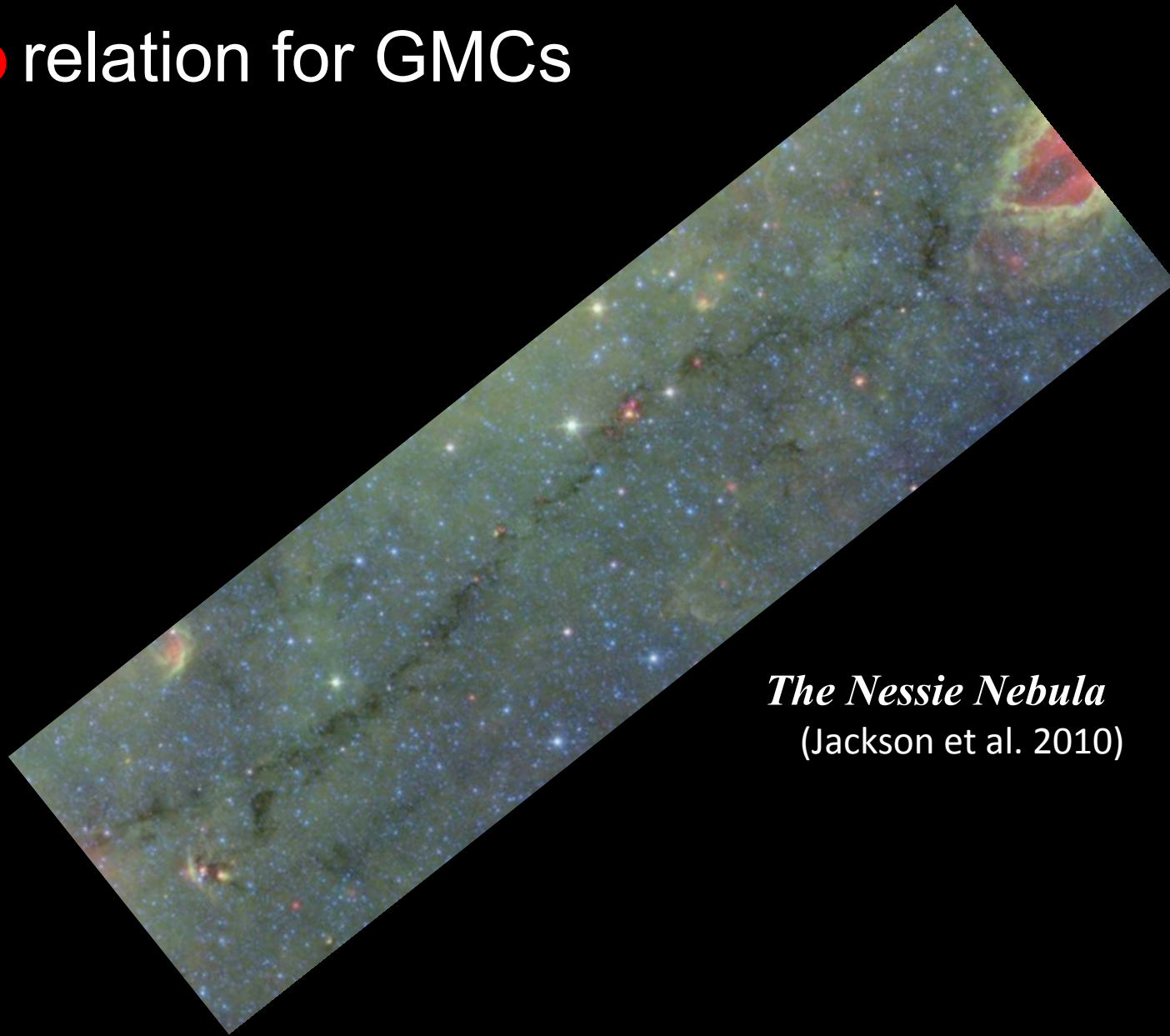
$$\rho_{\text{SFR}} = 4.6 \times 10^{-8} \langle \rho_{0.8} \rangle$$

# A $\Sigma$ - $\rho$ relation for GMCs





# A $\Sigma$ - $\rho$ relation for GMCs



*The Nessie Nebula*  
(Jackson et al. 2010)

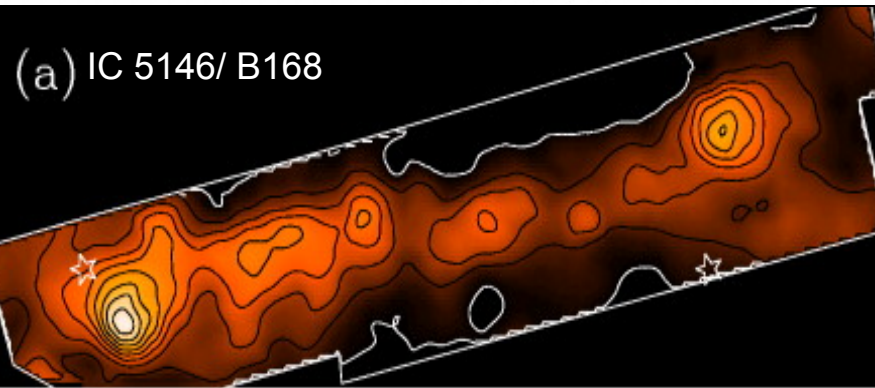
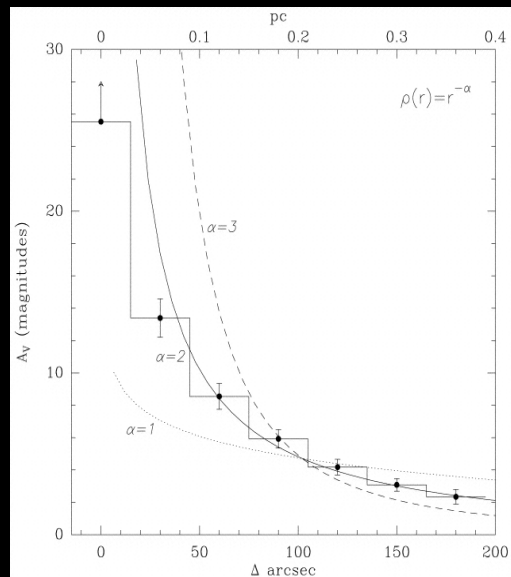
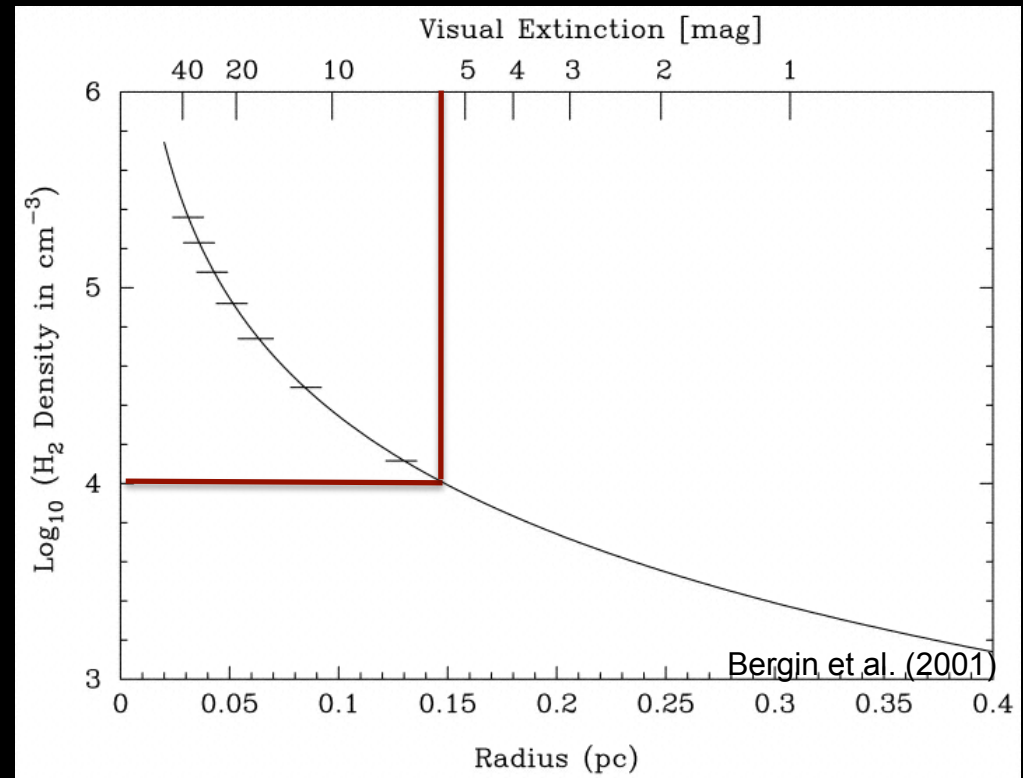
Infrared Dark Clouds

# A $\Sigma$ - $\rho$ relation for GMCs

Assume:  $M_{0.8} = M(\rho > \rho_t)$

$$n_t \approx 10^4 \text{ cm}^{-3}$$

$$\rho_t = 400 M_\odot/\text{pc}^3$$



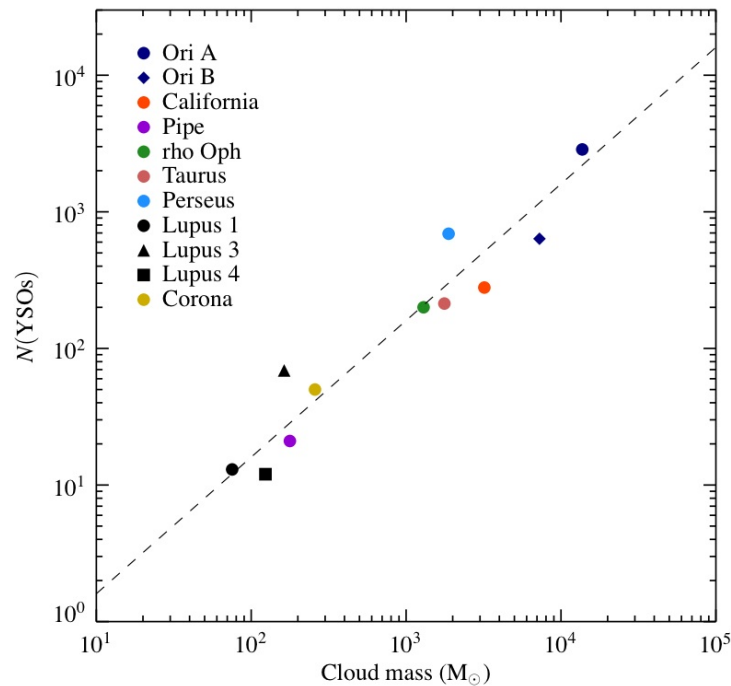
Lada, Alves, Lada (1999)

# Star Formation Scaling Law for Local Clouds

$$\text{SFR} = 4.6 \times 10^{-8} M(\rho > \rho_t) \quad \text{for } \rho \geq \rho_t$$

Where:

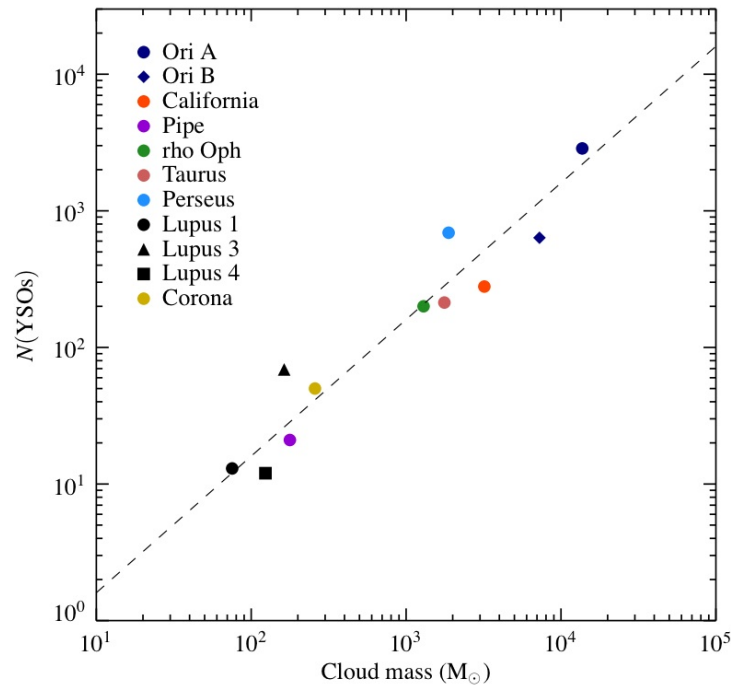
$$M(\rho > \rho_t) = \int_{\rho_t}^{\infty} M(\rho) d\rho$$



$$\rho_{\text{SFR}} = 4.6 \times 10^{-8} \langle \rho_{0.8} \rangle$$

# Star Formation Scaling Law for Local Clouds

$$\text{SFR} = 4.6 \times 10^{-8} M(\rho > \rho_t) \quad \text{for } \rho \geq \rho_t$$

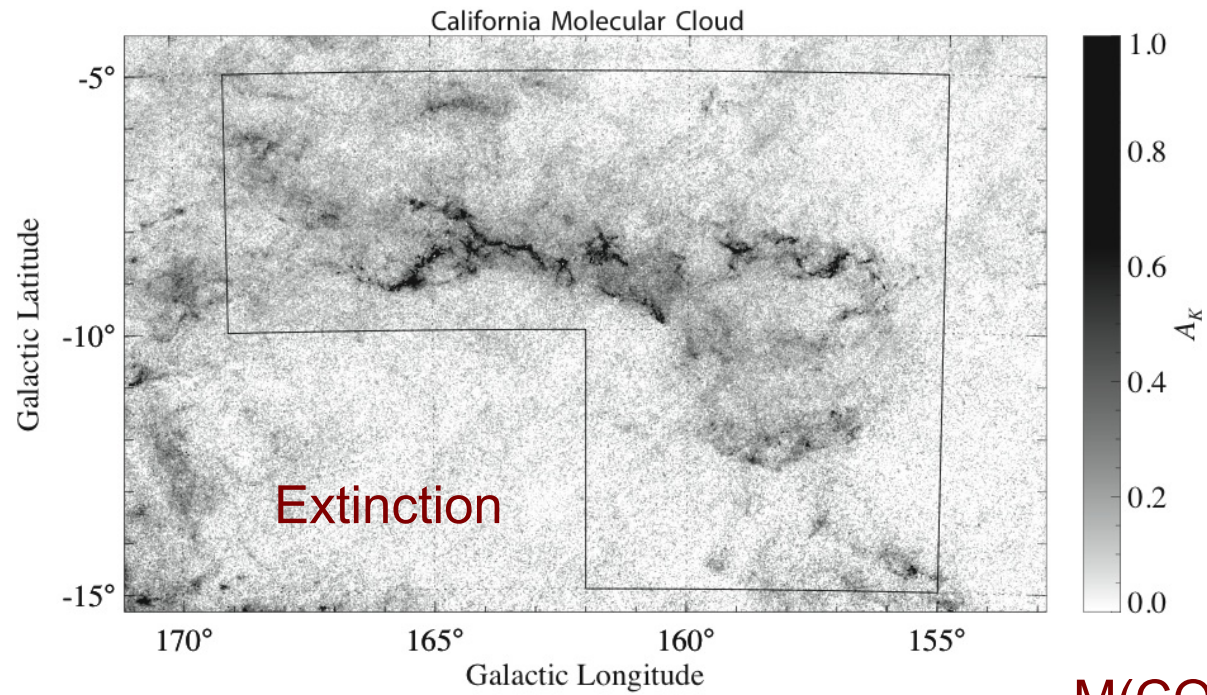


$$\rho_{\text{SFR}} = 4.6 \times 10^{-8} \langle \rho_{0.8} \rangle$$

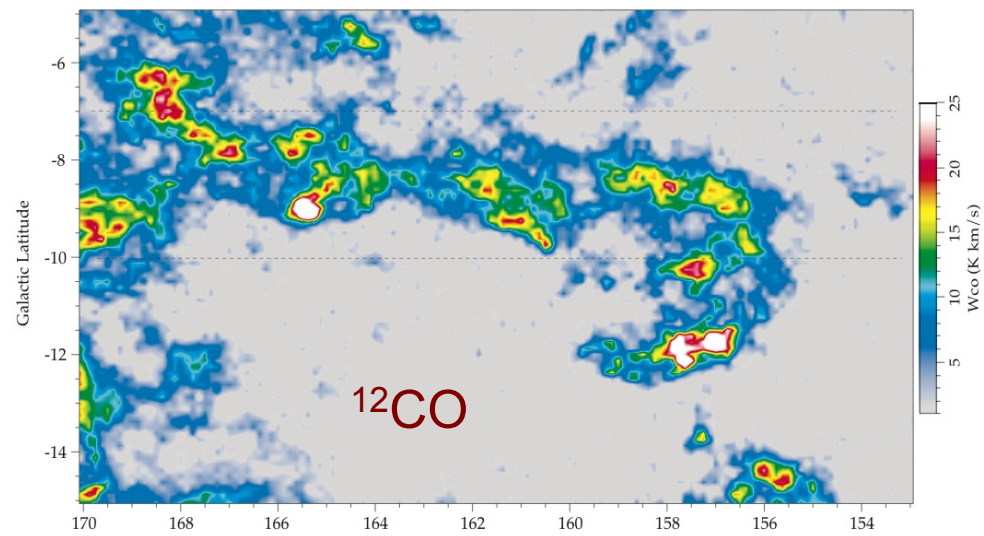
$$\langle \rho_{0.8} \rangle = \langle \rho \rangle \quad \text{for } \rho > \rho_t$$

$$n_t \approx 10^4 \text{ cm}^{-3}$$

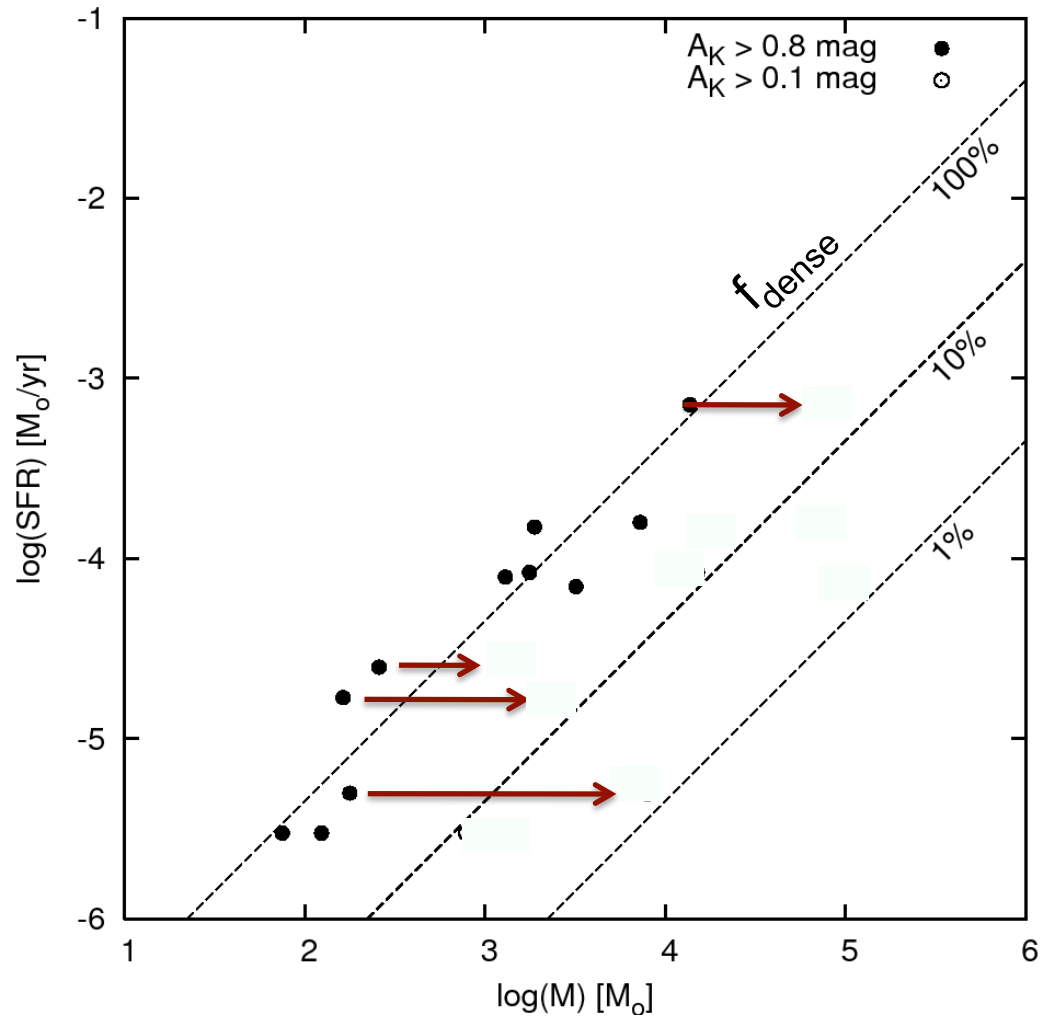
# SF Scaling Law for Low Density Gas



$$M(\text{CO}) \approx M(A_K > 0.1)$$



## Star Formation Scaling Laws for Local Molecular Clouds



$$\text{SFR} = 4.6 \times 10^{-8} M_{\text{dense}} = 4.6 \times 10^{-8} f_{\text{dense}} M_{\text{gas}}$$

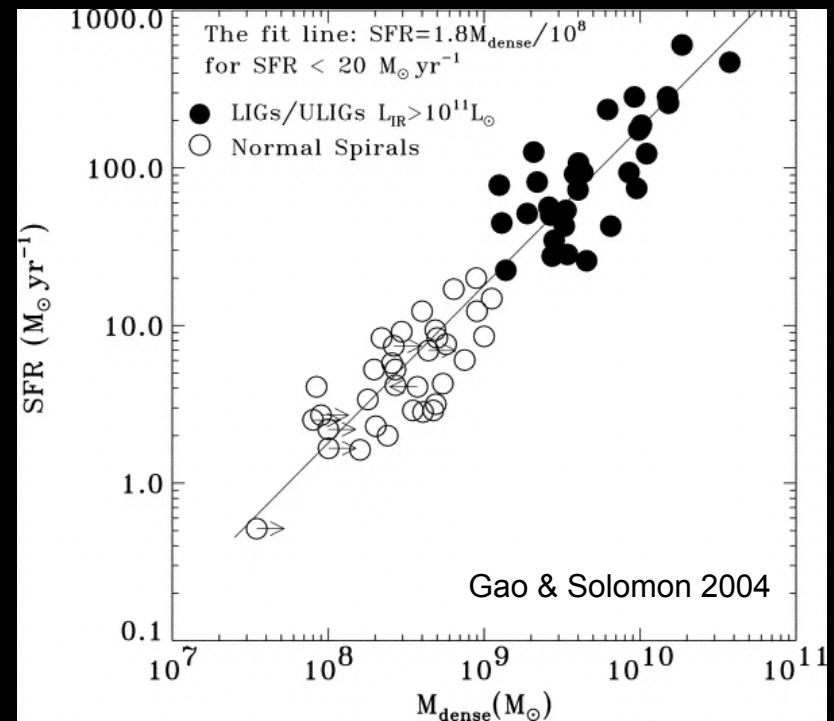
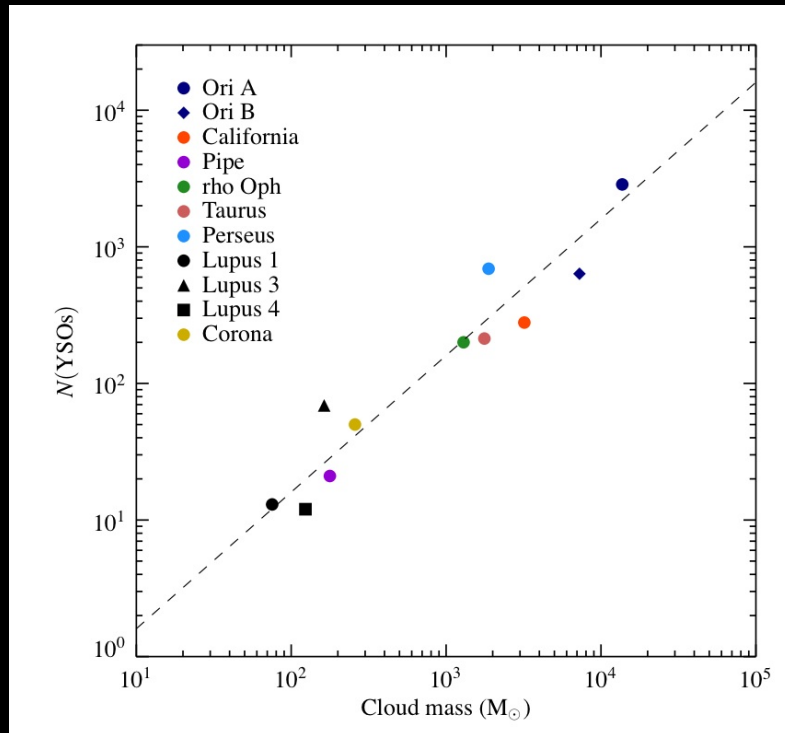
# From Clouds to Galaxies



# SF Scaling Laws for Dense Gas

Local GMC SF Scaling Law:  $\text{SFR}_{\text{gmc}} = 4.6 \times 10^{-8} M_{0.8} \text{ (M}_{\odot} \text{ yr}^{-1})$

Extragalactic SF Scaling Law:  $\text{SFR}_{\text{xgal}} = 1.8 \times 10^{-8} M_{\text{HCN}} \text{ (M}_{\odot} \text{ yr}^{-1})$

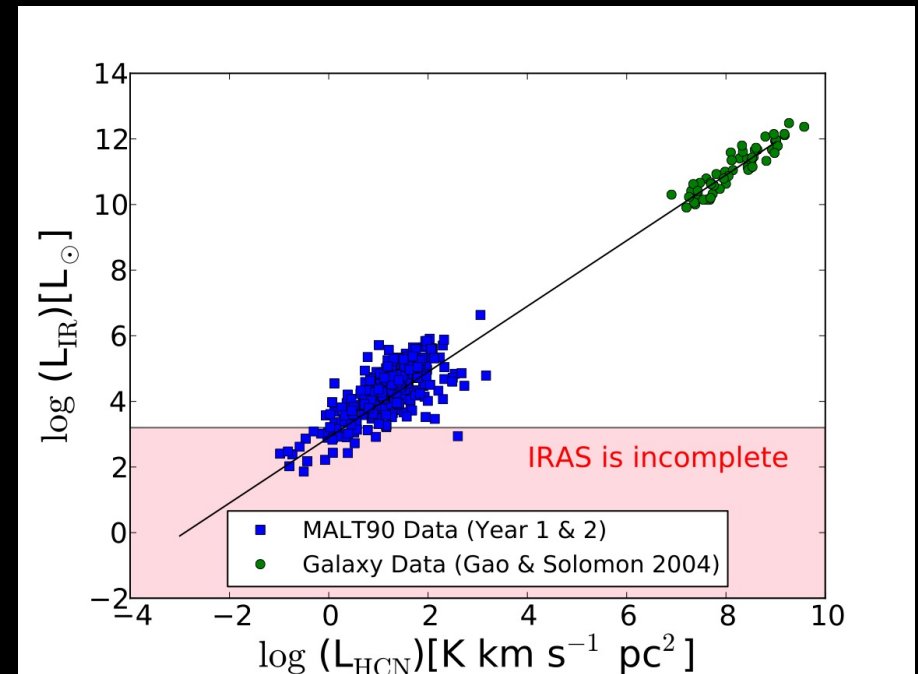
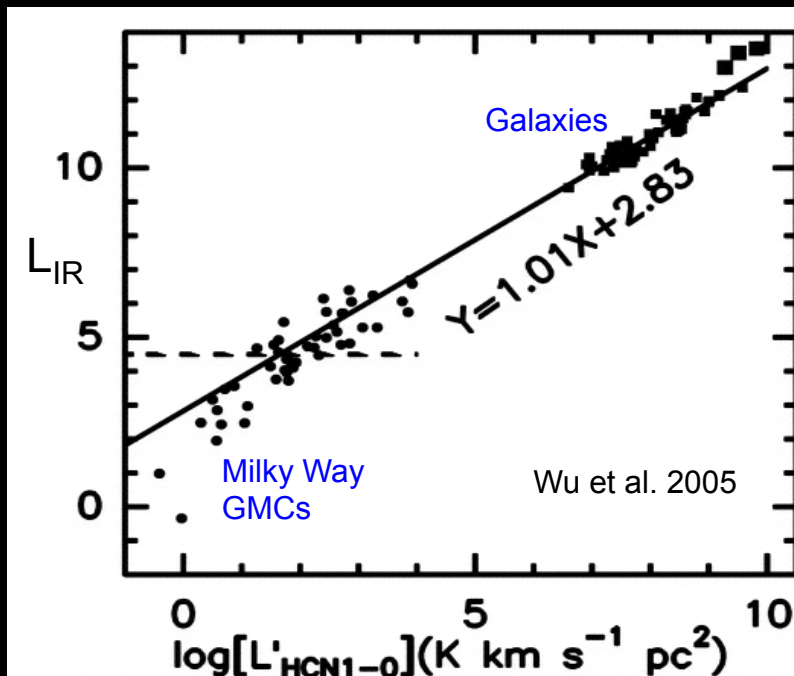


HCN: critical density  $\sim 2\text{-}3 \times 10^4 \text{ cm}^{-3}$

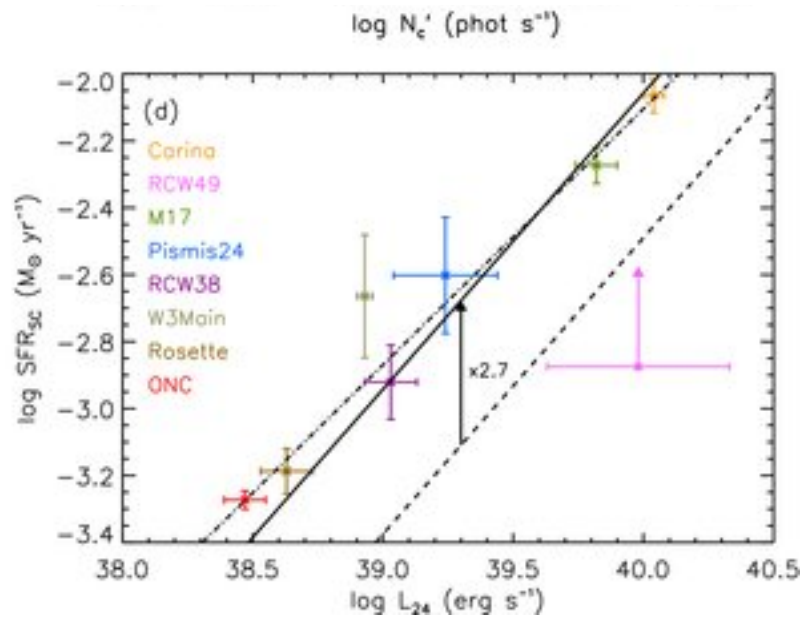
# SF Scaling Laws for Dense Gas

Local GMC SF Scaling Law:  $\text{SFR}_{\text{gmc}} = 4.6 \times 10^{-8} M_{0.8} \text{ (M}_{\odot} \text{ yr}^{-1})$

Extragalactic SF Scaling Law:  $\text{SFR}_{\text{xgal}} = 1.8 \times 10^{-8} M_{\text{HCN}} \text{ (M}_{\odot} \text{ yr}^{-1})$



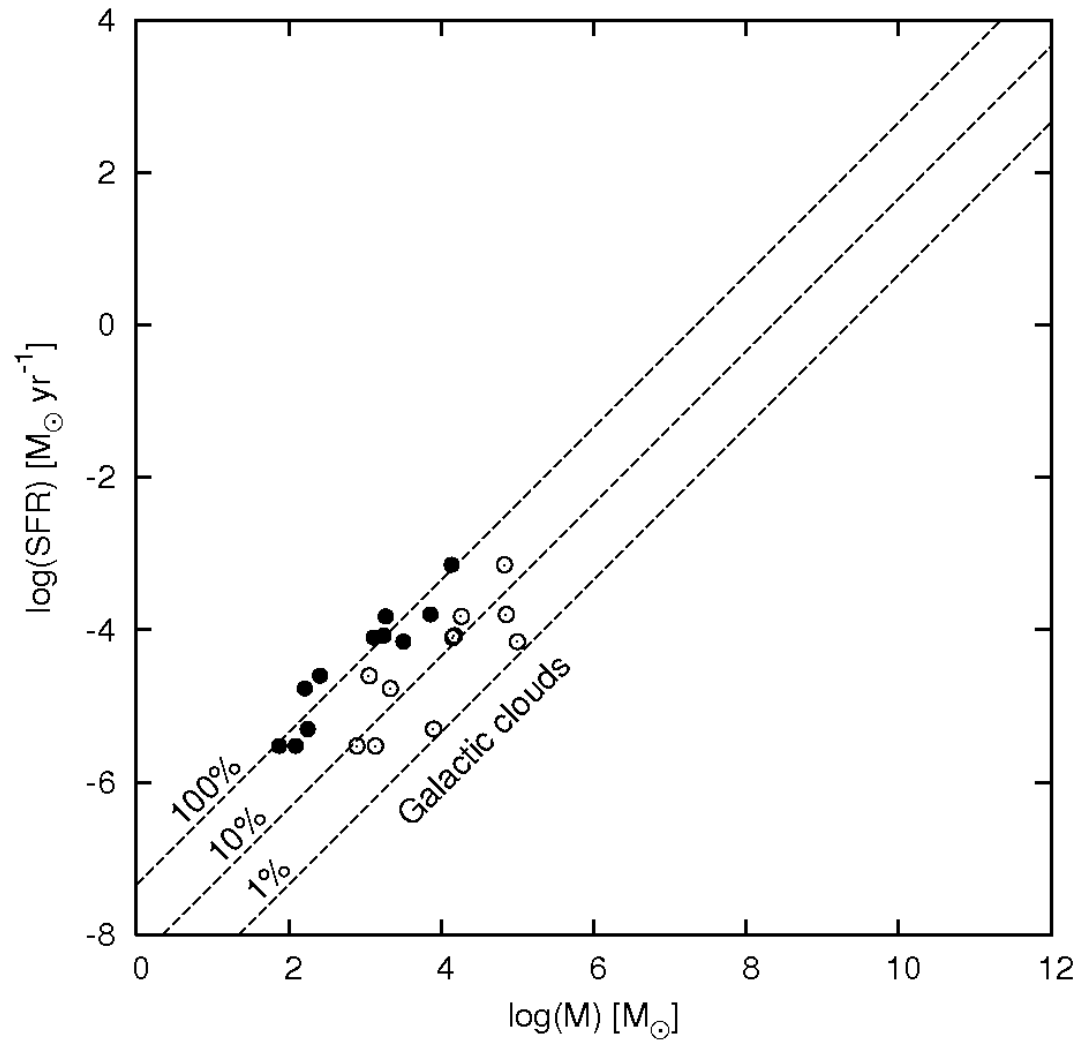
## Comparison of SFRs for Galactic clouds



Chomiuk & Povich 2011 AJ, 142, 197

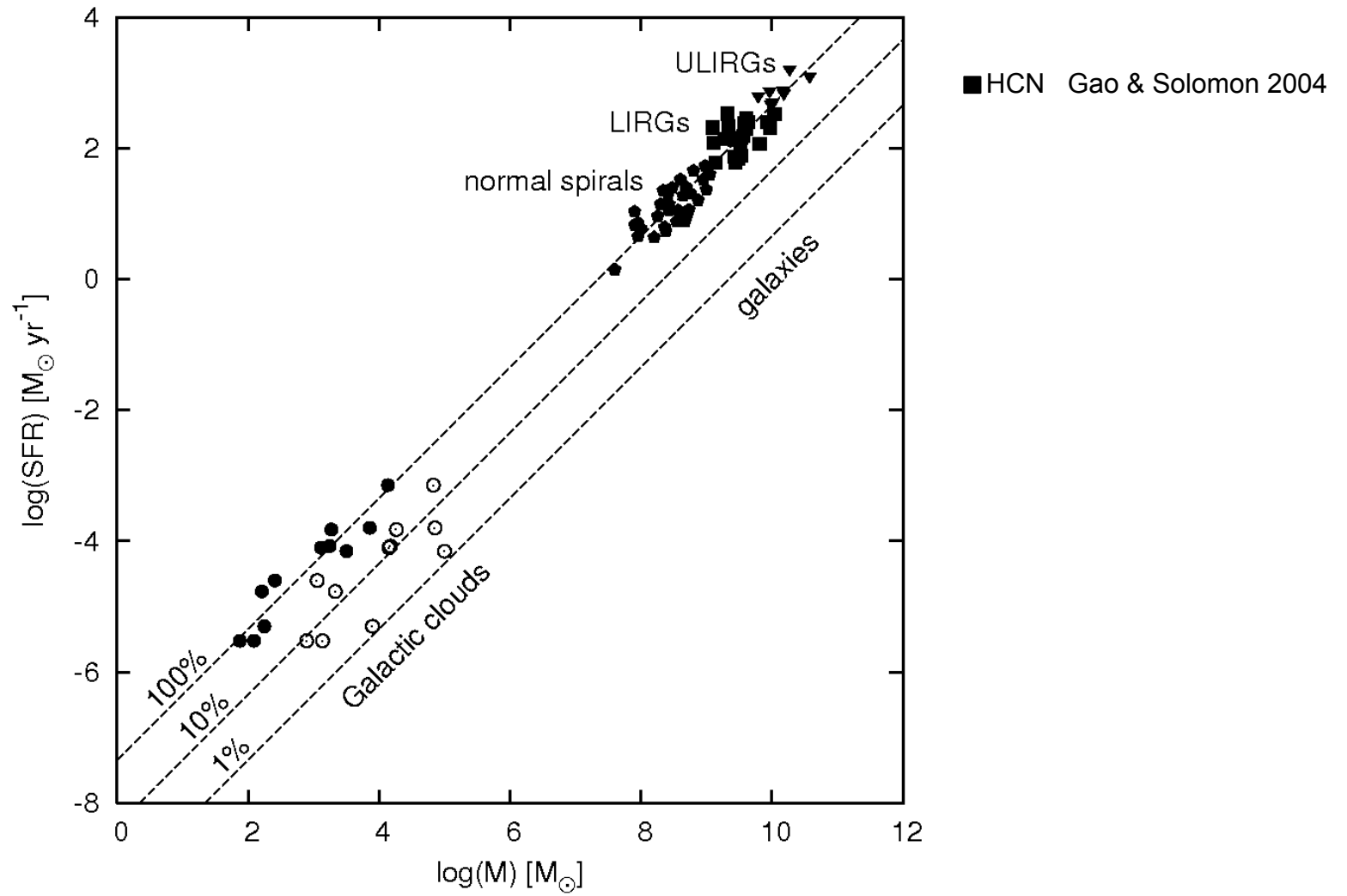
$$\text{SFR}_{\text{GMC}} = 2.7 \times \text{SFR}_{\text{SB99}}$$

# Star Formation Scaling Laws from Local Clouds to Galaxies

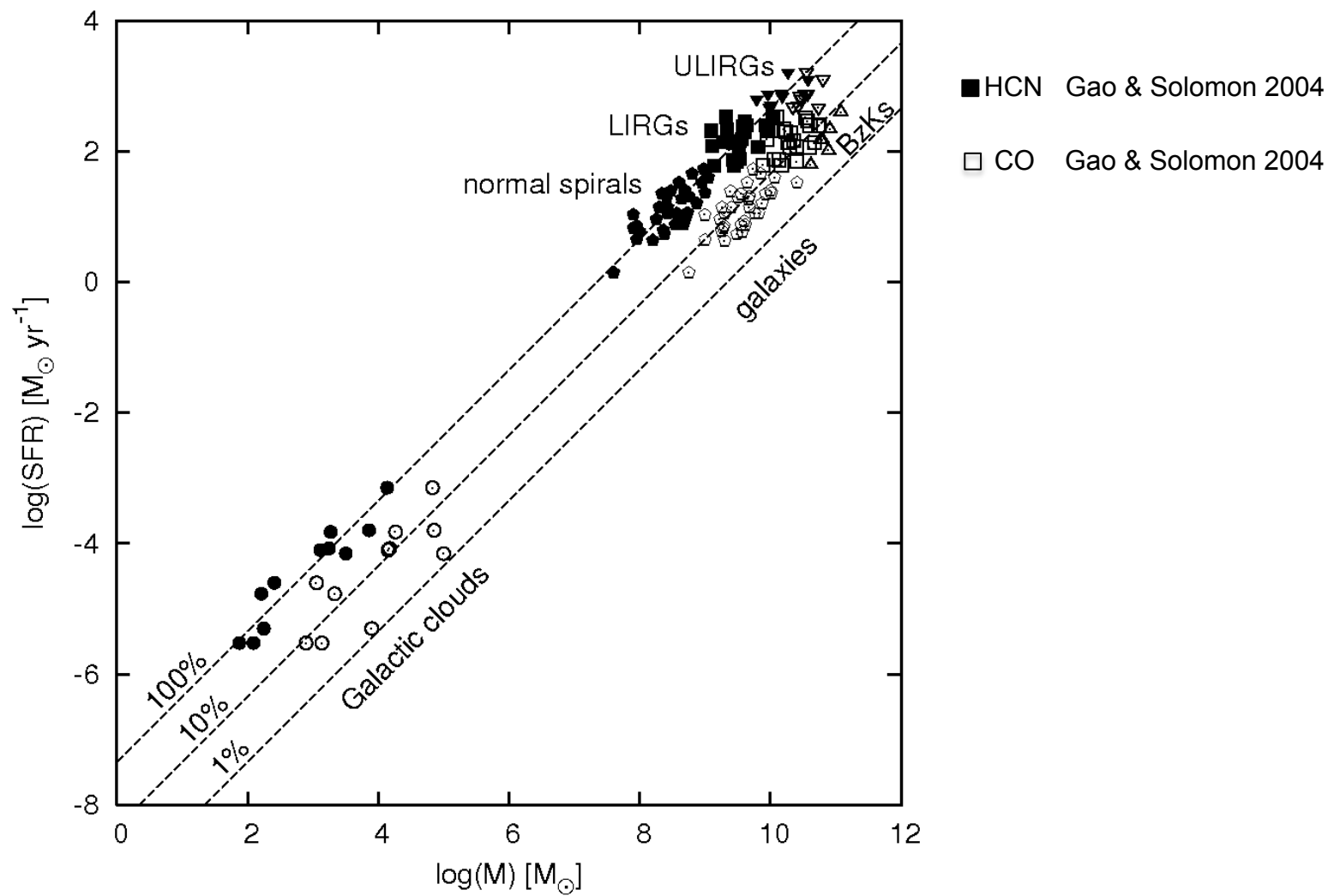


$$\text{SFR} = 4.6 \times 10^{-8} M_{\text{dense}}$$

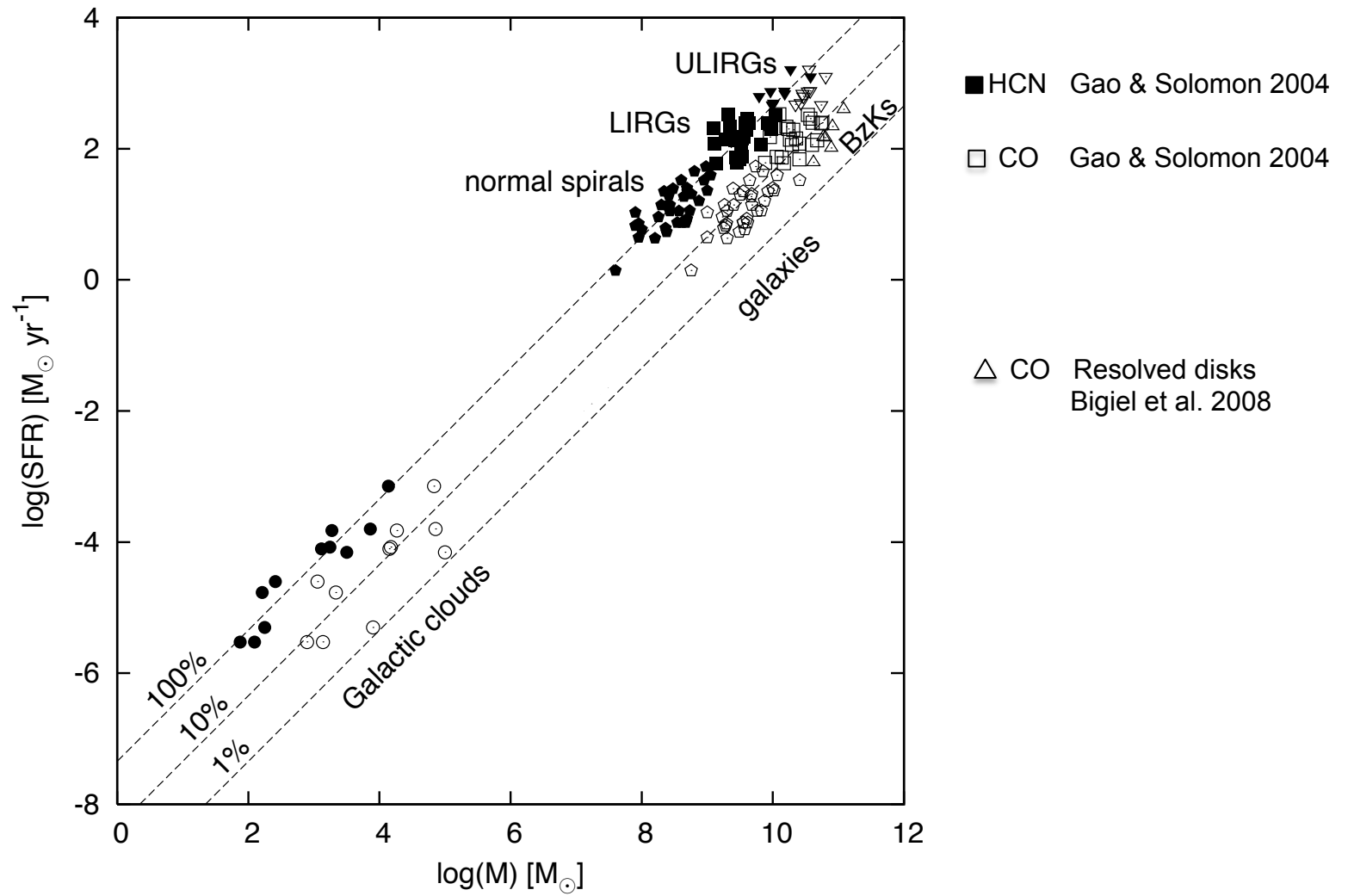
# Star Formation Scaling Laws from Local Clouds to Galaxies



# Star Formation Scaling Laws from Local Clouds to Galaxies

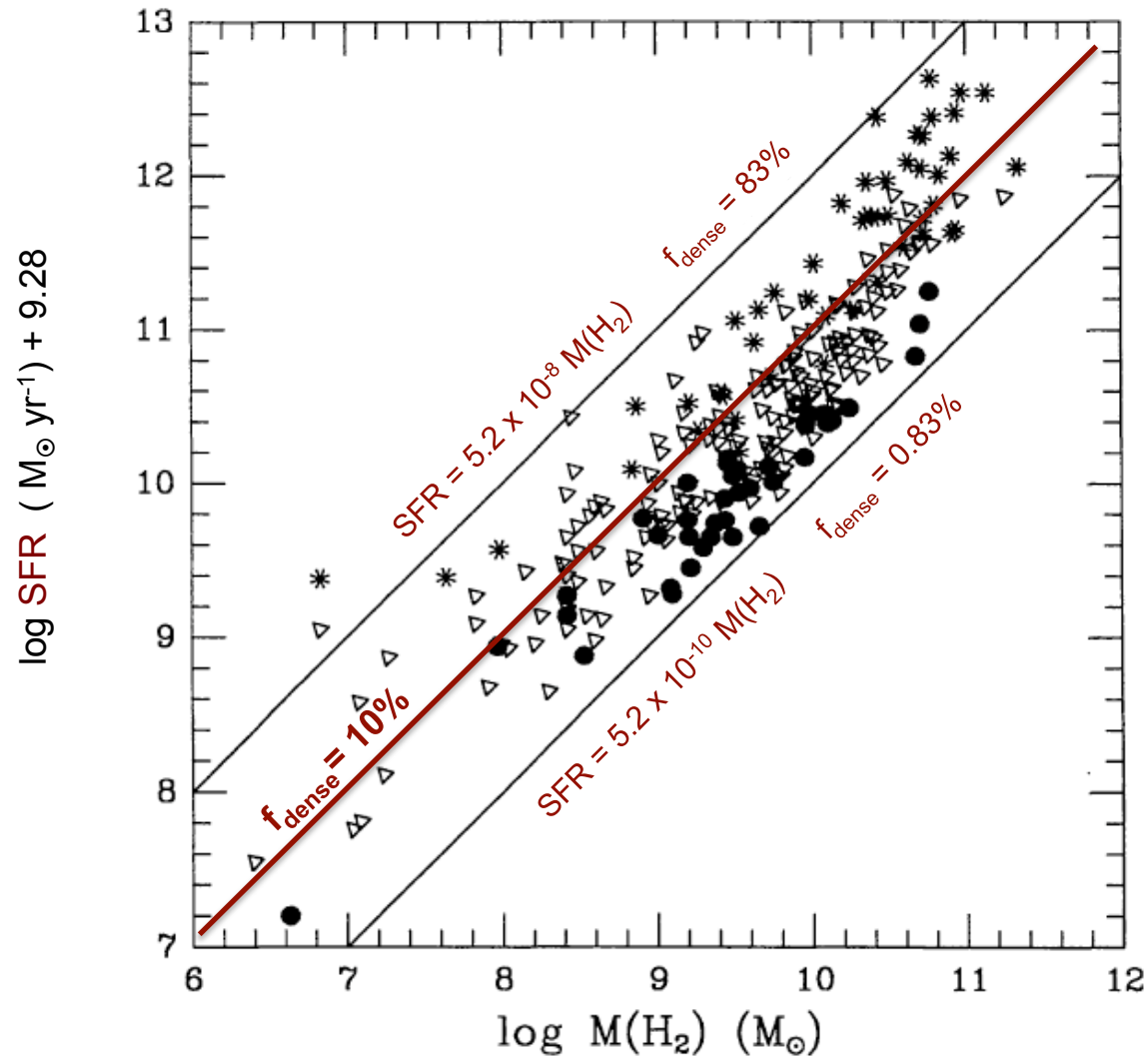


# Star Formation Scaling Laws from Local Clouds to Galaxies



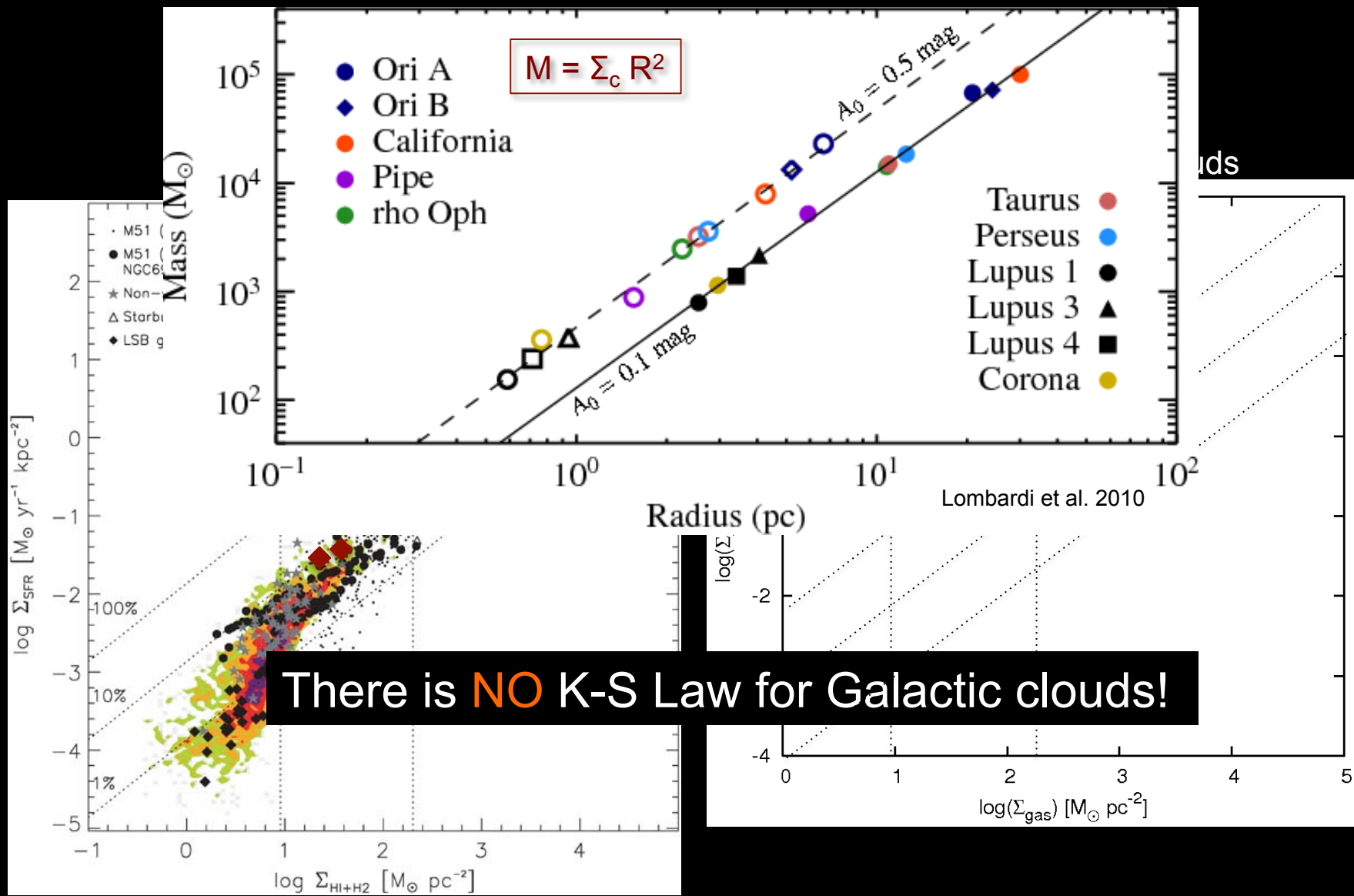
# A Linear Scaling Law for Galaxies

Young & Scoville 1991, ARAA 32, 581





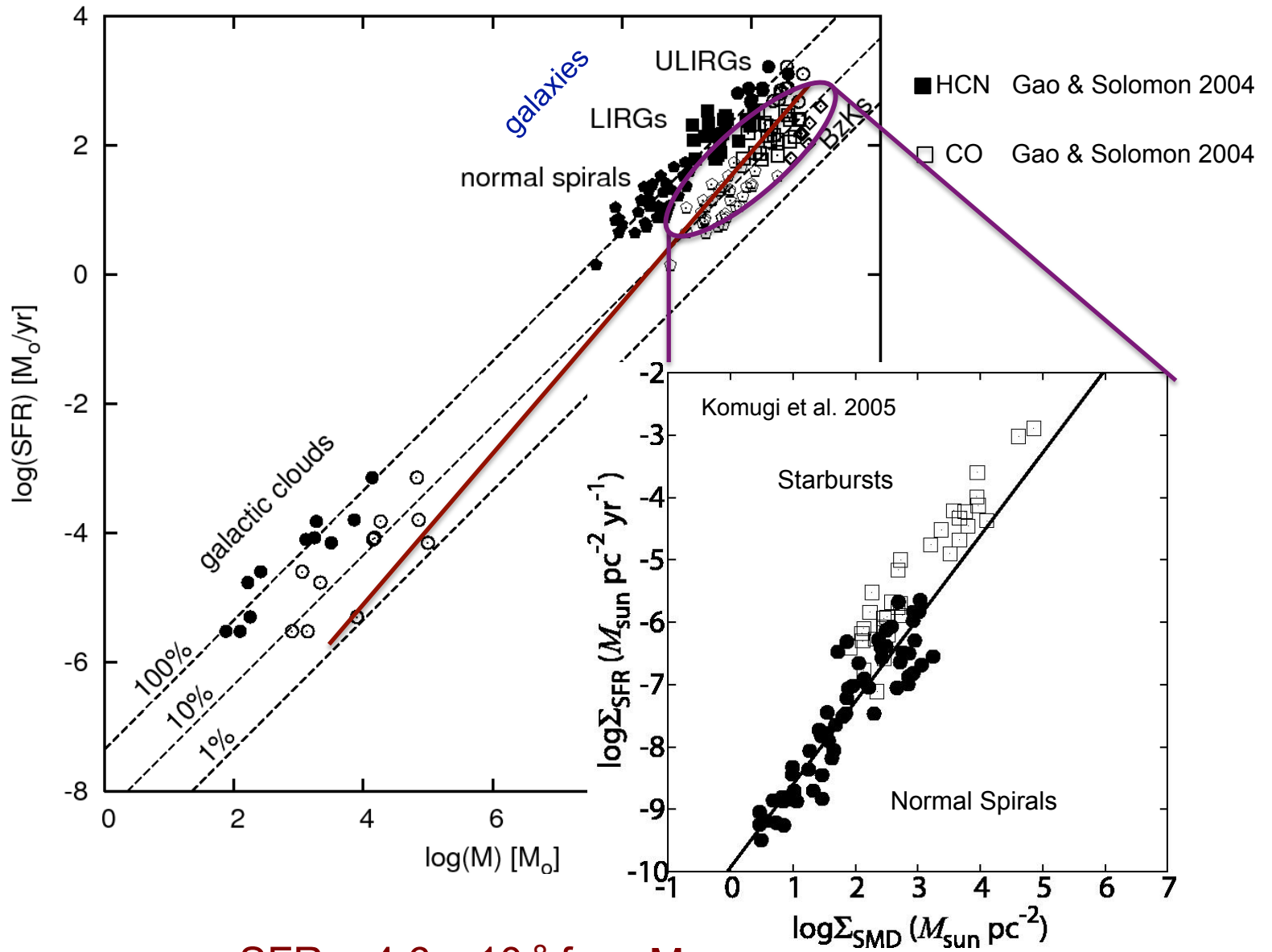
# The Nature of the Schmidt-Kennicutt Scaling Relation



There is **NO** K-S Law for Galactic clouds!

$$\Sigma_{\text{SFR}} \neq f(\Sigma_{\text{gas}})$$

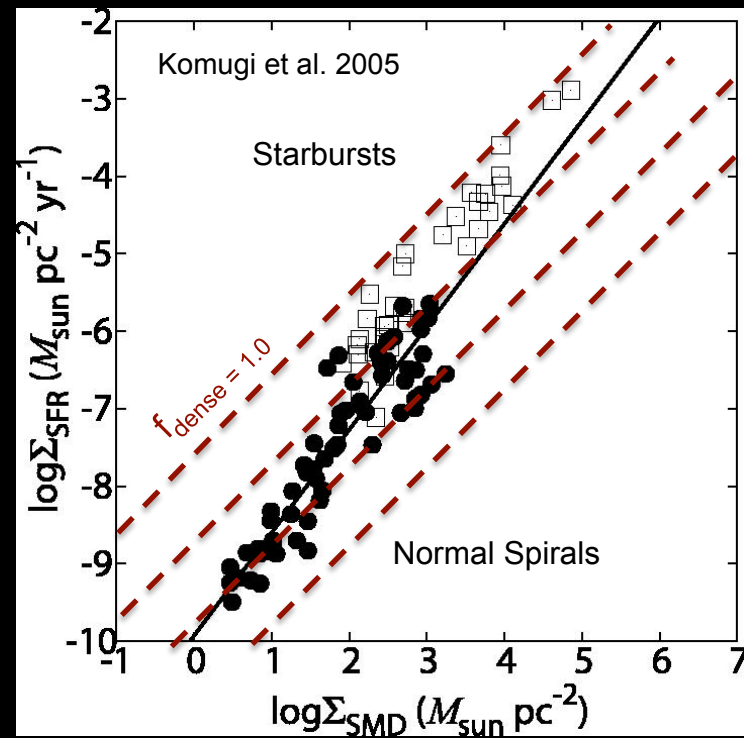
# Star Formation Scaling Laws from Local Clouds to Galaxies



$$\text{SFR} = 4.6 \times 10^{-8} f_{\text{dense}} M_{\text{gas}}$$

$$\Sigma_{\text{SFR}} = 4.6 \times 10^{-8} f_{\text{dense}} \Sigma_{\text{gas}}$$

$$f_{\text{dense}} \sim (\Sigma_{\text{gas}})^{0.5}$$



# Implications for Modelling Star Forming Galaxies

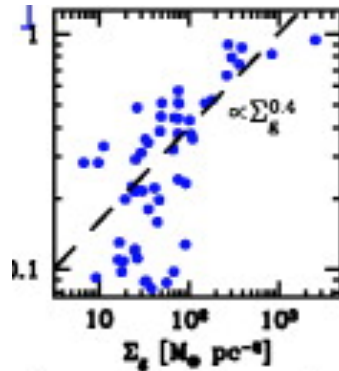
SF threshold density:  $n_{\text{gas}} > 50 \text{ cm}^{-3}$

$t_{\text{sf}} = \text{Constant}$

Input  $\neq$  Output

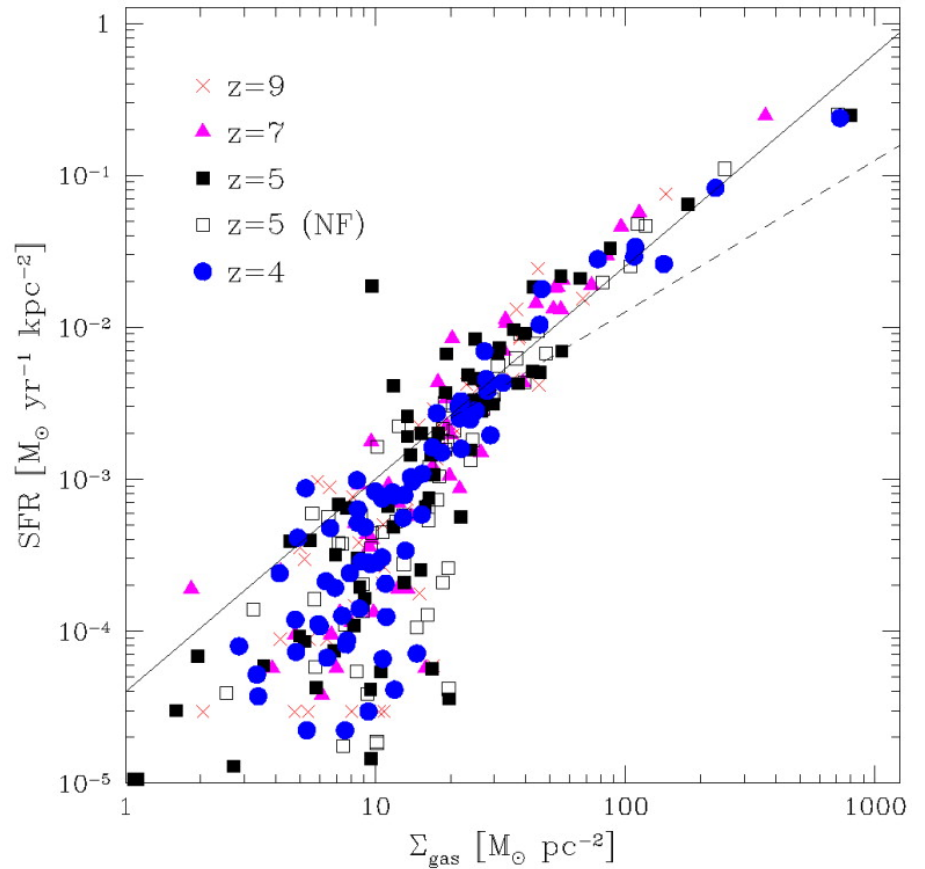
$$\rho_{\text{SFR}} = A(\rho_{\text{gas}})^{1.0}$$

$$\Sigma_{\text{SFR}} = B(\Sigma_{\text{gas}})^{1.4}$$



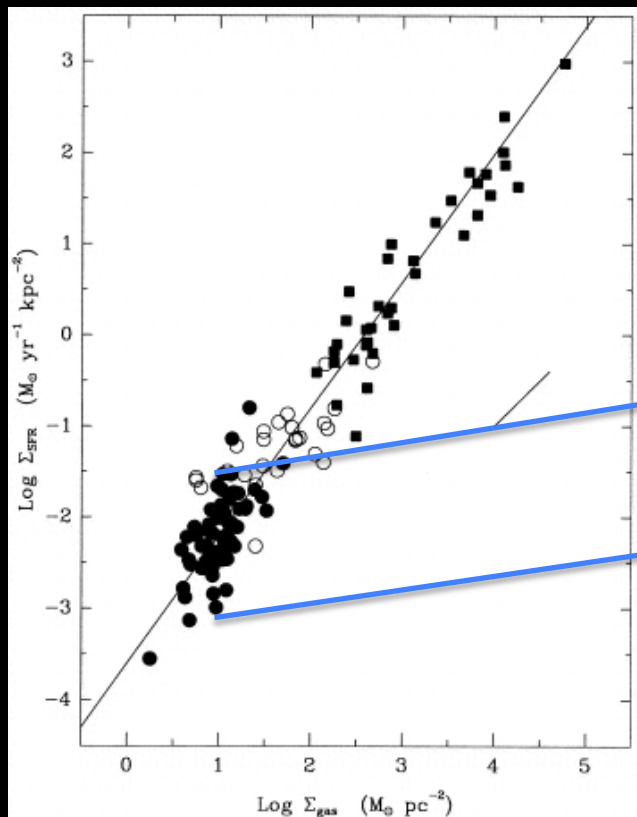
$$f_{\text{dense}} \sim (\Sigma_{\text{gas}})^{0.4}$$

Kravtsov (2003)

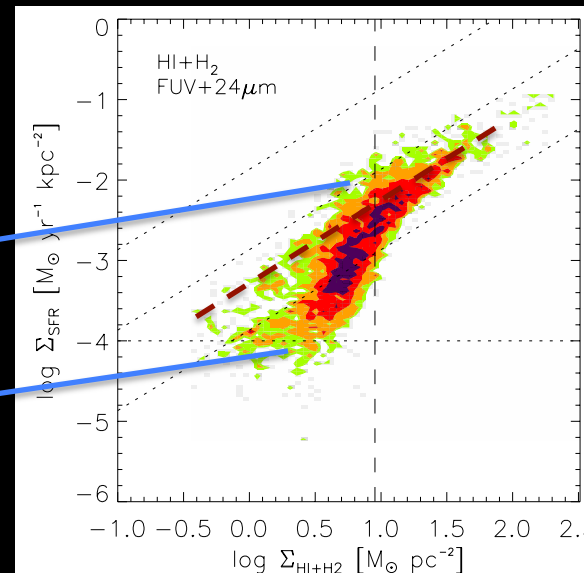


# Schmidt-Kennicutt Law for Star Formation

$$\Sigma_{\text{SFR}} = A (\Sigma_{\text{g}})^{1.6}$$



HI gas dilutes specific SFR signal!

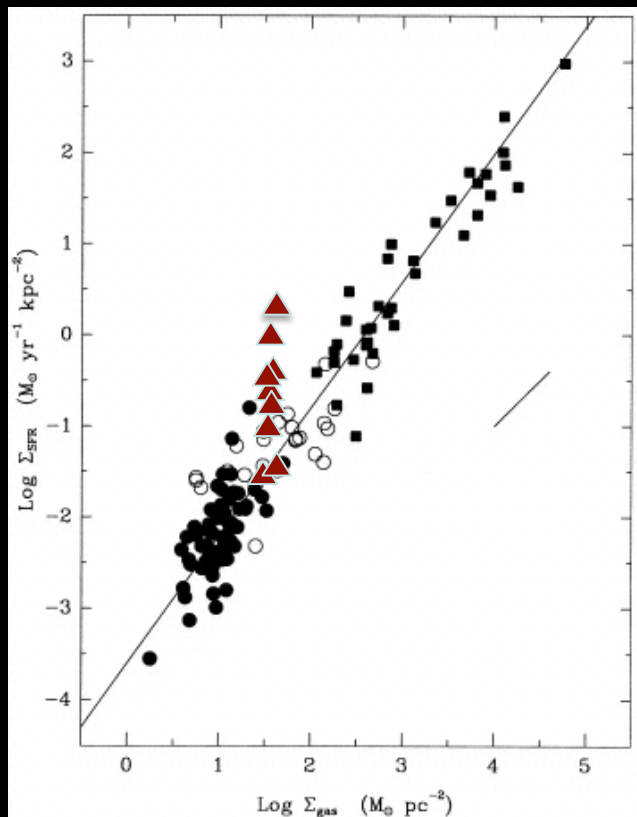


$$\Sigma_{\text{gas}} = \Sigma(\text{HI} + \text{H}_2)$$

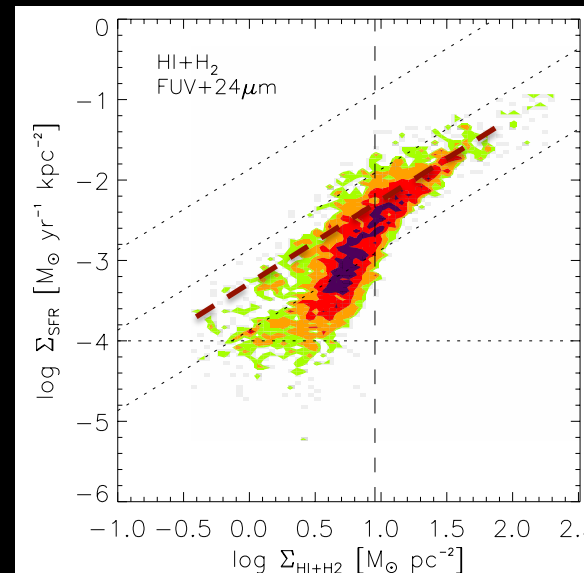
Bigiel et al 2008

# Schmidt-Kennicutt Law for Star Formation

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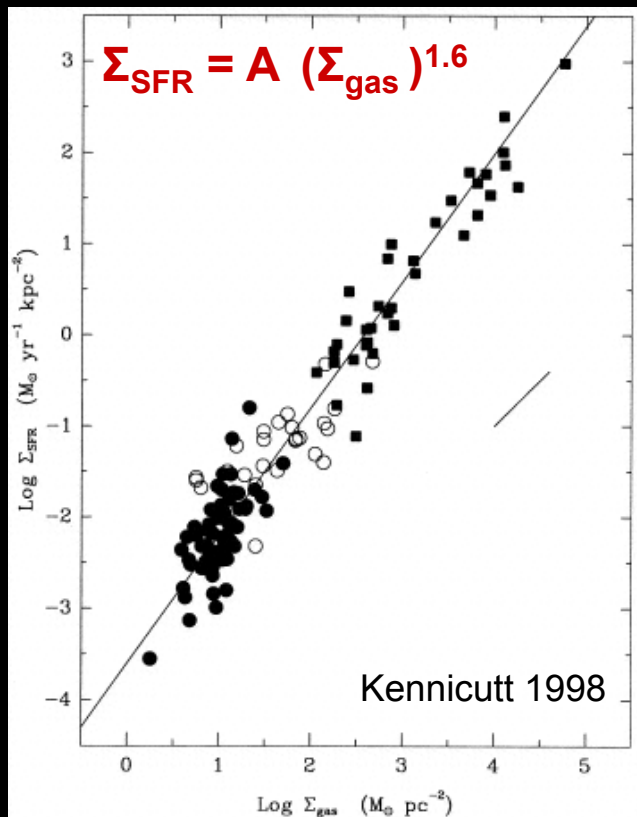
$$\Sigma_{\text{gas}} = \Sigma(\text{HI} + \text{H}_2)$$

Bigiel et al 2008

# Schmidt - Kennicutt Law for Star Formation

Unlike Individual GMCs, for galaxies there is no underlying relation between  $\Sigma$  and  $\rho$ , i.e.,  $\Sigma \neq f(\rho)$

Theoretical Explanation:



Consider that:

$$\text{SFR} \sim M_{\text{gas}} / t_{\text{SF}}$$

$$\text{And since } M_{\text{gas}} \sim \rho$$

$$\text{If } t_{\text{SF}} \sim (G\rho)^{-1/2} \text{ then } \text{SFR} \sim \rho^{3/2}$$



A deep-field astronomical image showing a vast field of galaxies in various colors (blue, yellow, red, purple) and shapes (spiral, elliptical, irregular) against a dark background. The text "The End" is overlaid in the center in a white, italicized font.

*The End*