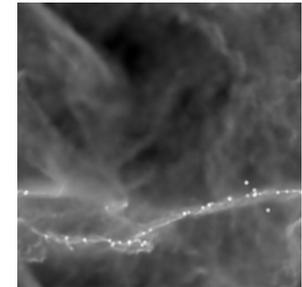
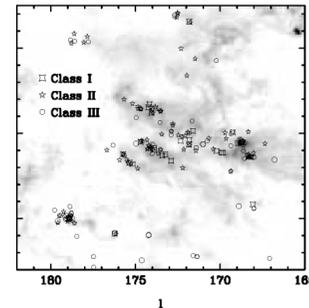
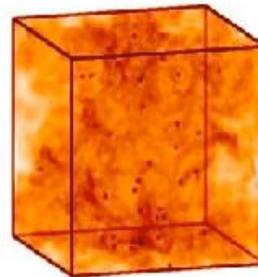
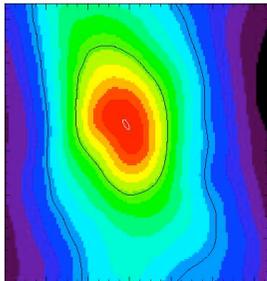
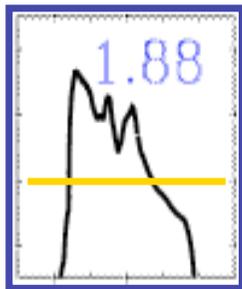


Collaborators

Many thanks to...

- Javier Ballesteros-Paredes
(UNAM, Morelia)
- Peter Bodenheimer (UC Santa Cruz)
- Andreas Burkert (Uni. München)
- Fabian Heitsch (Uni. München)
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(UNAM, Morelia)
- Hans Zinnecker (AIP, Potsdam)

Gravoturbulent Star Formation



Ralf Klessen

Emmy Noether Research Group (DFG)
Astrophysikalisches Institut Potsdam



Würzburg, January 20, 2005

Structure

Motivation and Phenomenology

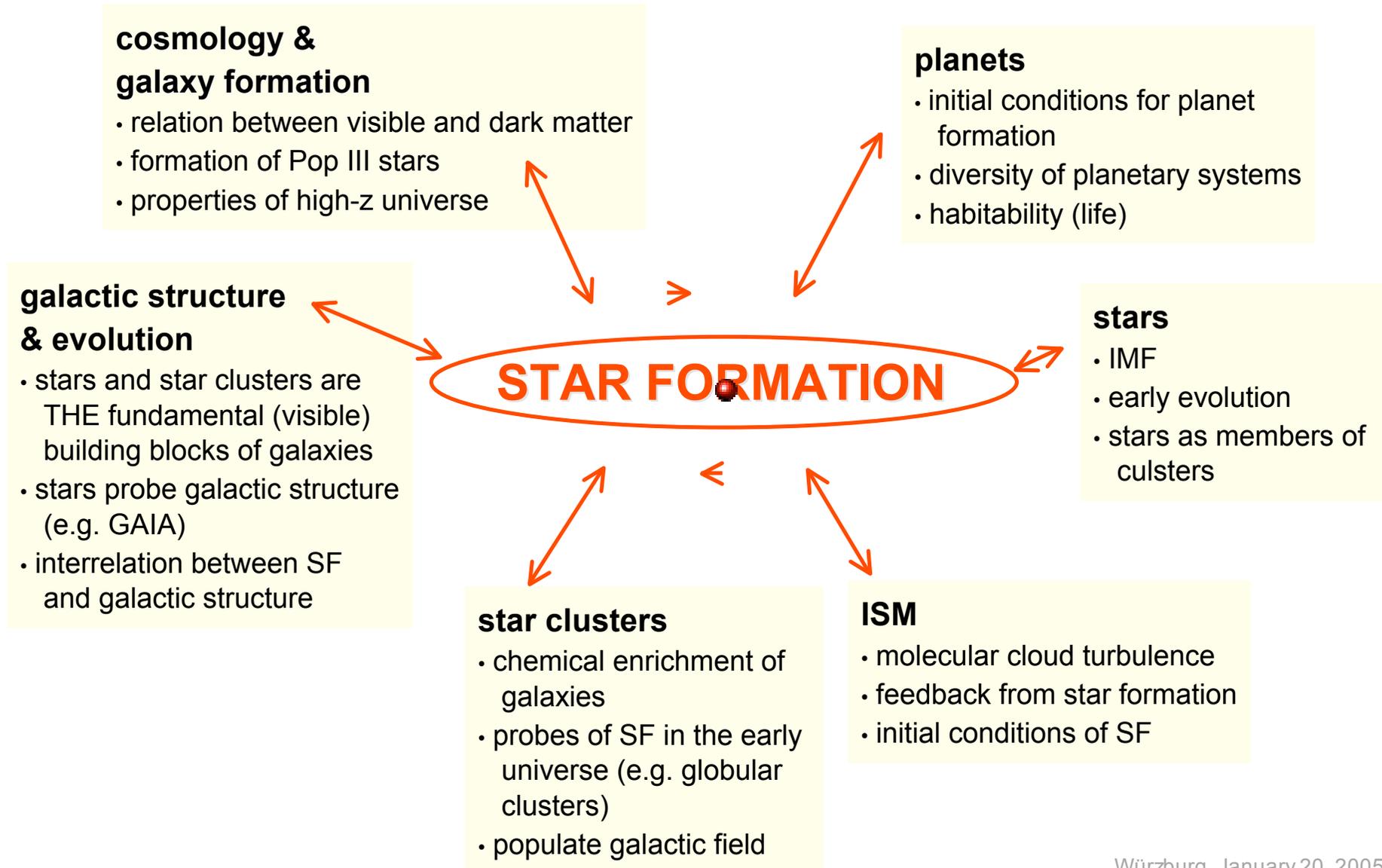
Historic Overview of Star Formation

Star form from *gravoturbulent fragmentation* of molecular cloud material.

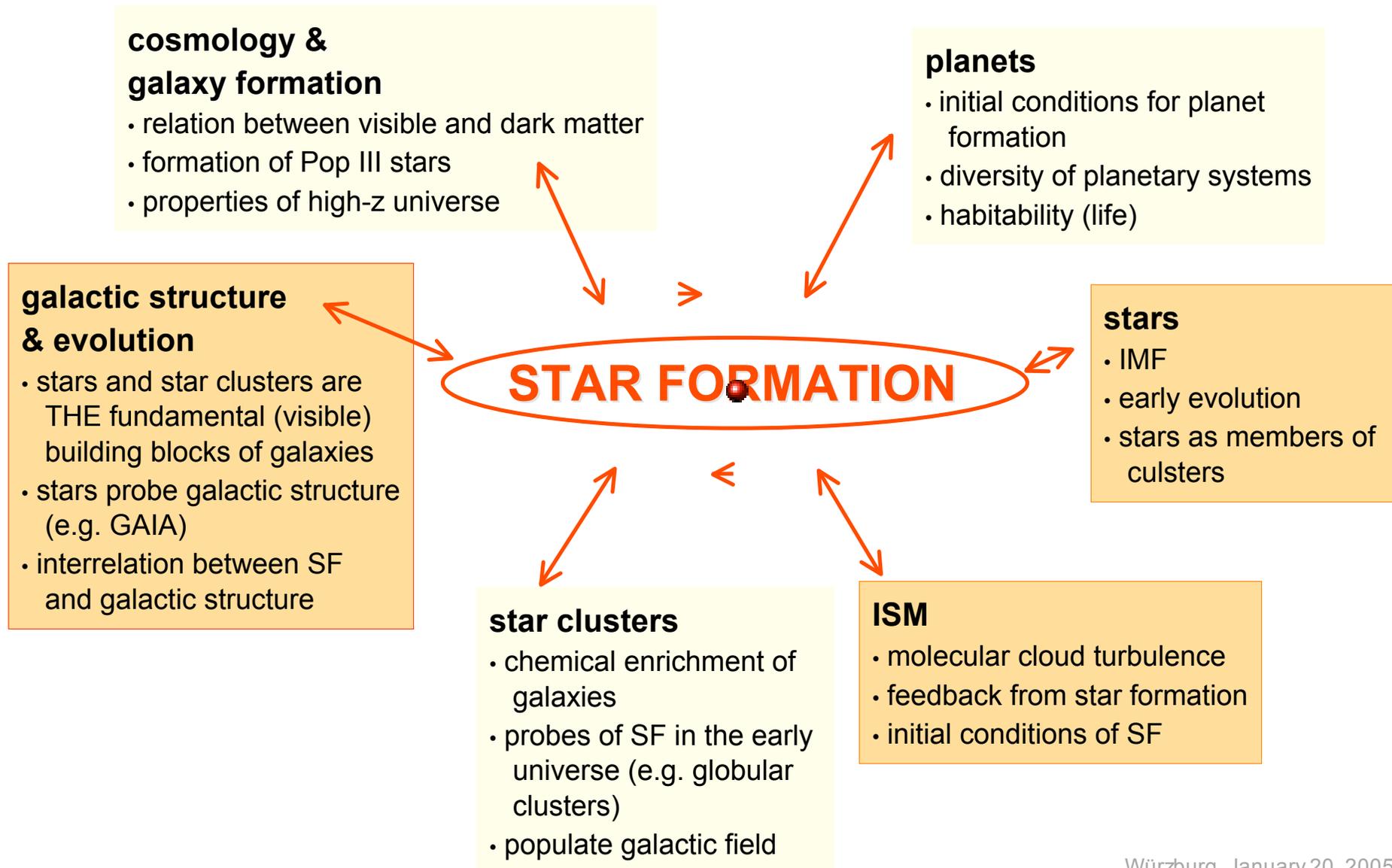
Star formation on galactic scales.

Why SF?

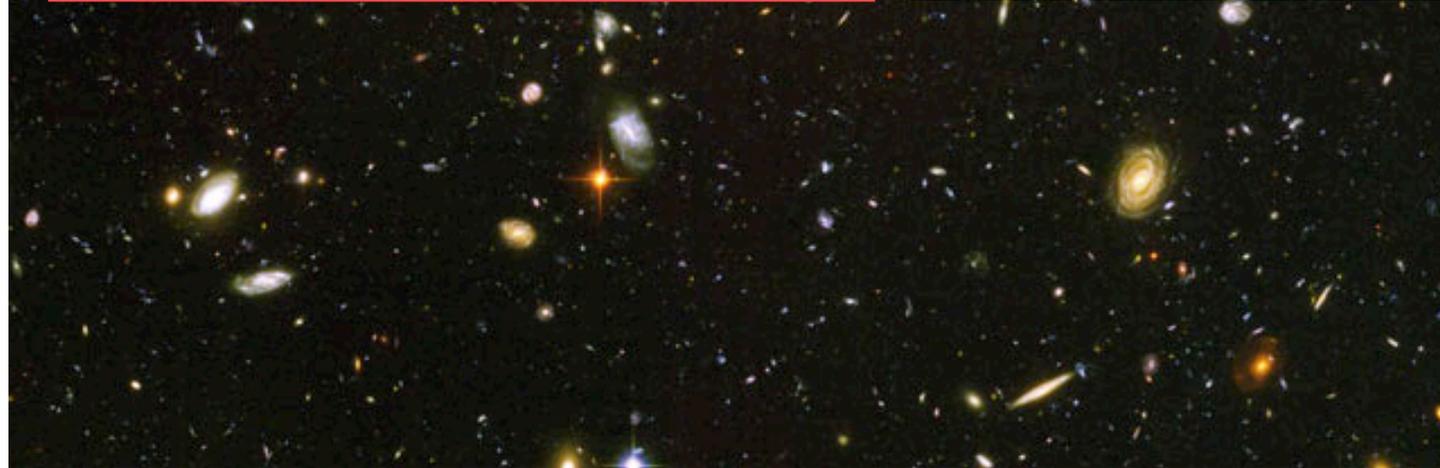
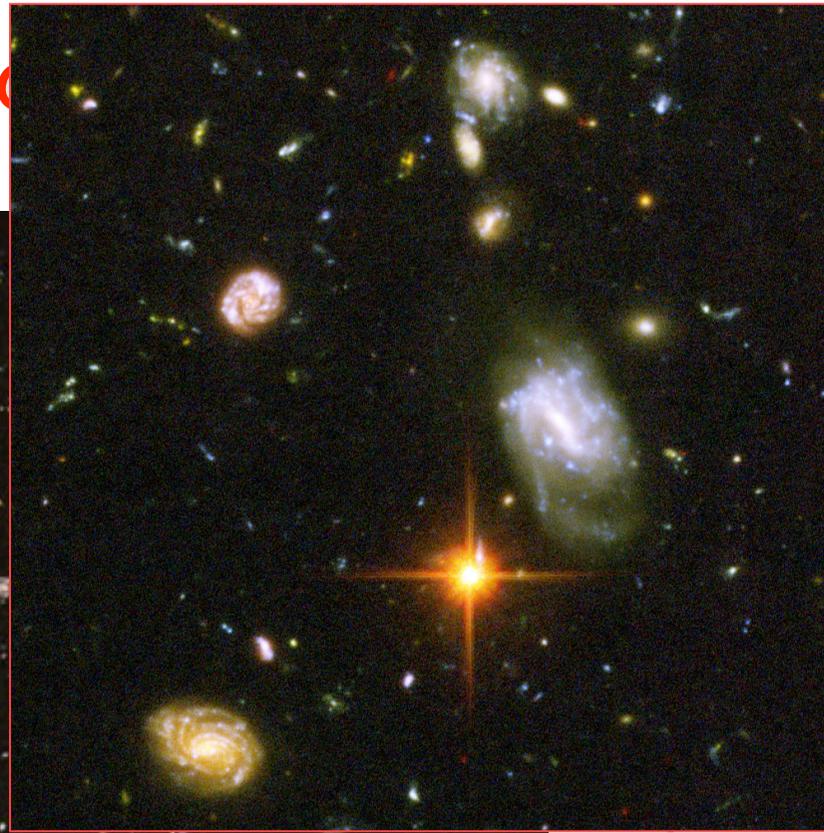
Why study star formation?



Why study star formation?



Star formation



tion
arly

(less than 1Gyr
after big bang!)

Stars form in
galaxies and
protogalaxies

(Hubble Ultra-Deep Field, from HST Web site)

Star formation in "typical" spiral:

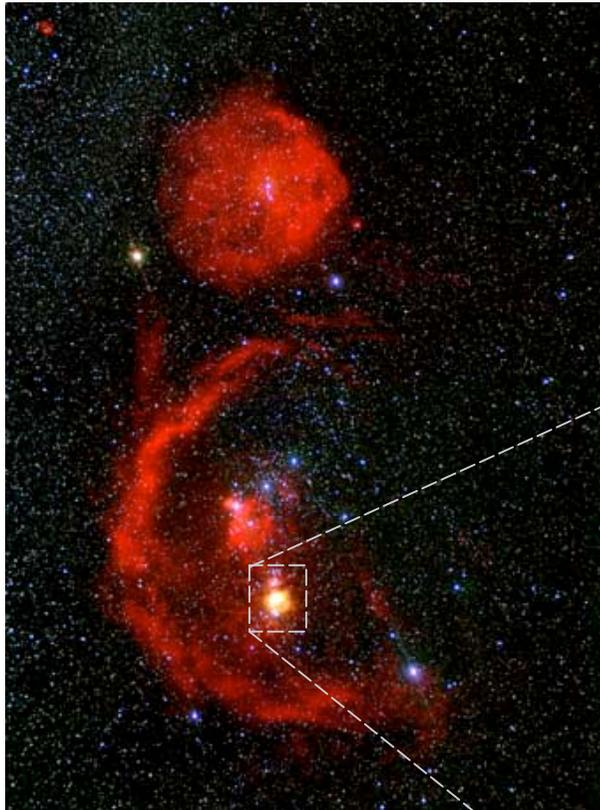


(from the Hubble Heritage Team)

NGC4622

- Star formation *always* is associated with *clouds of gas and dust*.
- Star formation is essentially a *local phenomenon* (on ~pc scale)
- **HOW** is star formation is *influenced* by *global* properties of the galaxy?

Local star forming region: The Trapezium Cluster in Orion



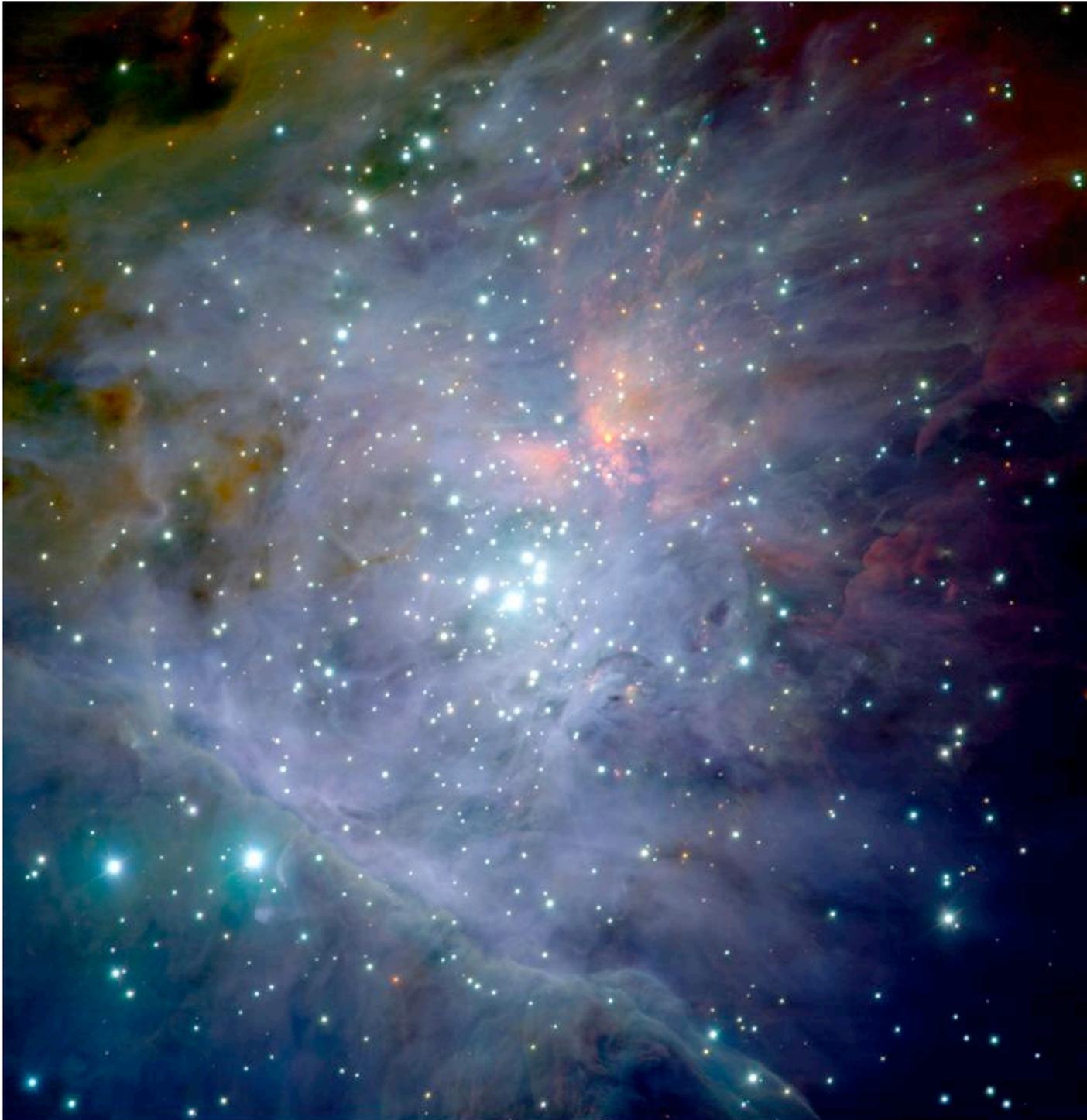
Orion molecular cloud

The Orion molecular cloud is the birth- place of several young embedded star clusters.

The Trapezium cluster is only visible in the IR and contains about 2000 newly born stars.



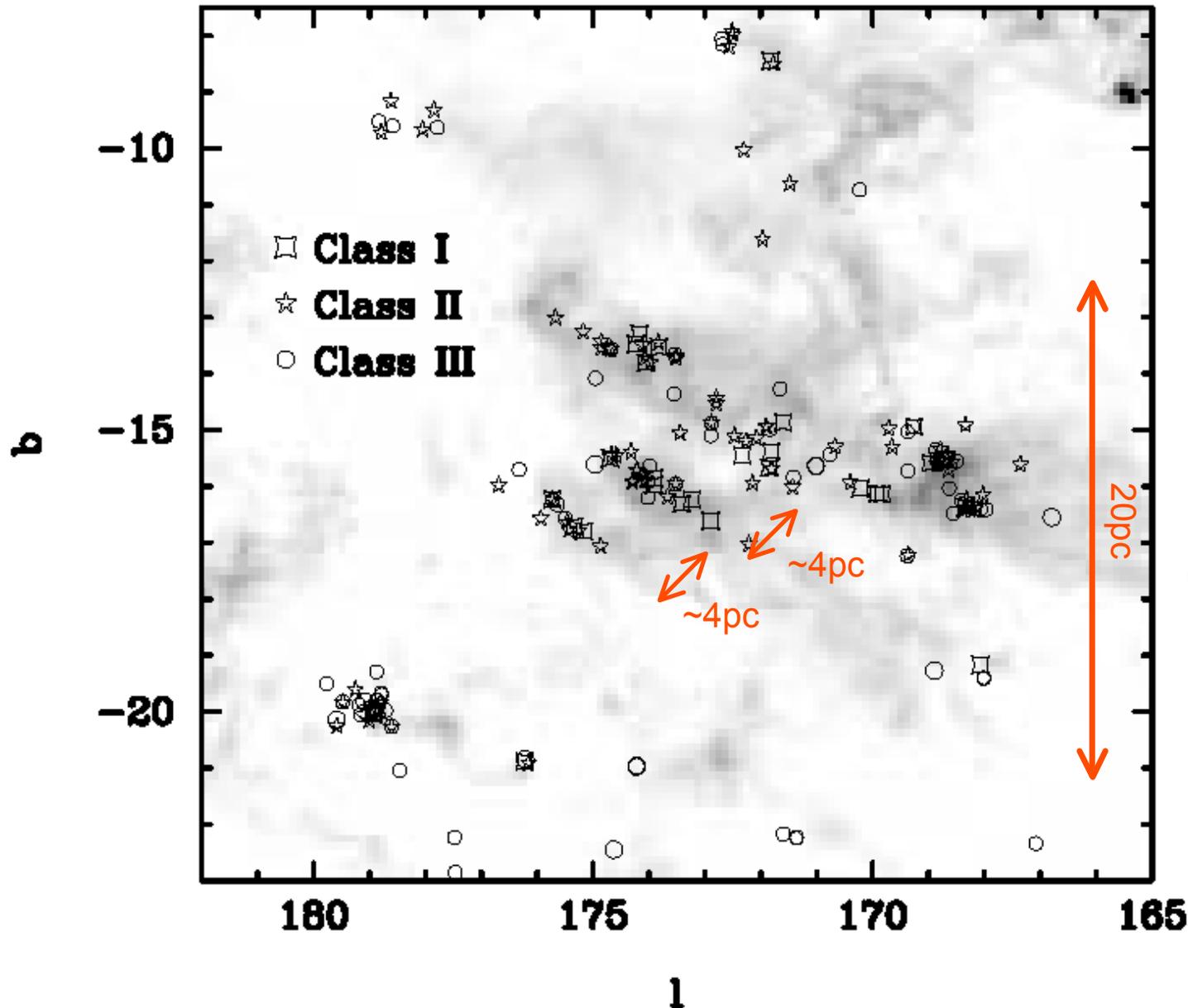
Trapezium cluster



Trapezium Cluster (detail)

- stars form in **clusters**
- stars form in **molecular clouds**
- (proto)stellar **feedback** is important

(color composite J,H,K
by M. McCaughrean,
VLT, Paranal, Chile)



Taurus molecular cloud

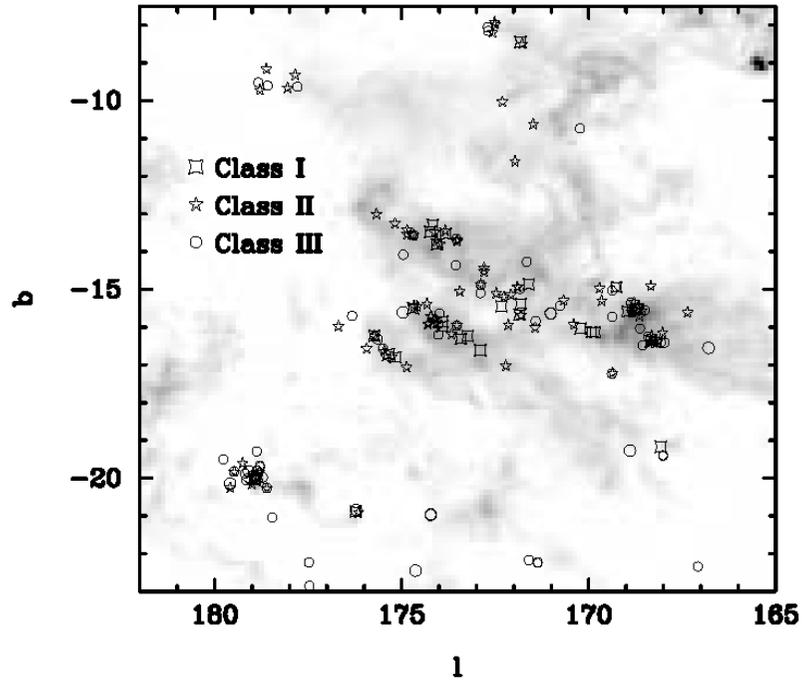
star-forming
filaments in the
Taurus cloud

- Structure and dynamics of young star clusters is coupled to *structure of mol. cloud*

Taurus molecular cloud

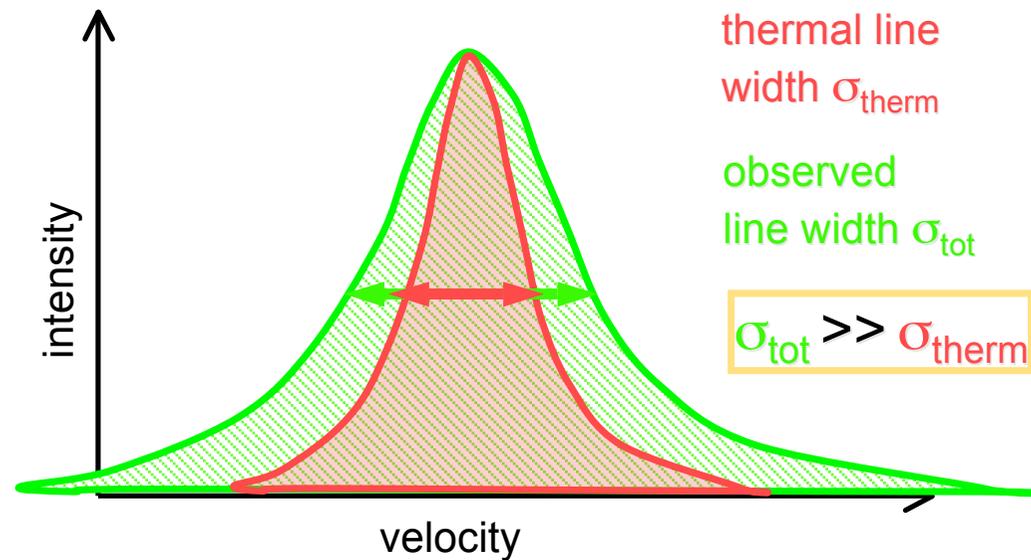
Star-forming filaments in *Taurus* cloud

(from Hartmann 2002)



- Structure and dynamics of young star clusters is coupled to *structure of molecular cloud*

- Structure and dynamics of *molecular cloud* is determined by *supersonic turbulence*



HISTORY

Early dynamical theory

- *Jeans (1902)*: Interplay between self-gravity and thermal pressure

- stability of homogeneous spherical density enhancements against gravitational collapse
- dispersion relation:

$$\omega^2 = c_s^2 k^2 - 4\pi G \rho_0$$

- instability when $\omega^2 < 0$

- minimal mass: $M_J = \frac{1}{6} \pi^{-5/2} G^{-3/2} \rho_0^{-1/2} c_s^3 \propto \rho_0^{-1/2} T^{3/2}$



Sir James Jeans, 1877 - 1946

First approach to turbulence

- *von Weizsäcker (1943, 1951) and Chandrasekhar (1951):* concept of **MICROTURBULENCE**

- BASIC ASSUMPTION: separation of scales between dynamics and turbulence

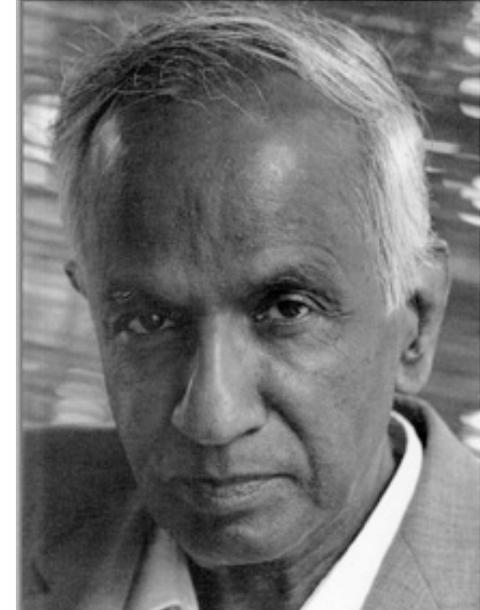
$$l_{\text{turb}} \ll l_{\text{dyn}}$$

- then turbulent velocity dispersion contributes to effective soundspeed:

$$c_c^2 \mapsto c_c^2 + \sigma_{rms}^2$$

- → Larger effective Jeans masses → more stability
- BUT: (1) turbulence depends on k : $\sigma_{rms}^2(k)$

$$(2) \text{ supersonic turbulence } \rightarrow \text{ usually } \sigma_{rms}^2(k) \gg c_s^2$$



S. Chandrasekhar, 1910 - 1995

Problems of early dynamical theory

- Molecular clouds are *highly Jeans-unstable*
Yet, they do *NOT* form stars at high rate
and with high efficiency.
(the observed global SFE in molecular clouds is $\sim 5\%$)
→ *something prevents large-scale collapse.*
- All throughout the early 1990's, molecular clouds
had been thought to be long-lived quasi-equilibrium
entities.
- Molecular clouds are *magnetized*.

Magnetic star formation

- *Mestel & Spitzer (1956)*: Magnetic fields can prevent collapse!!!

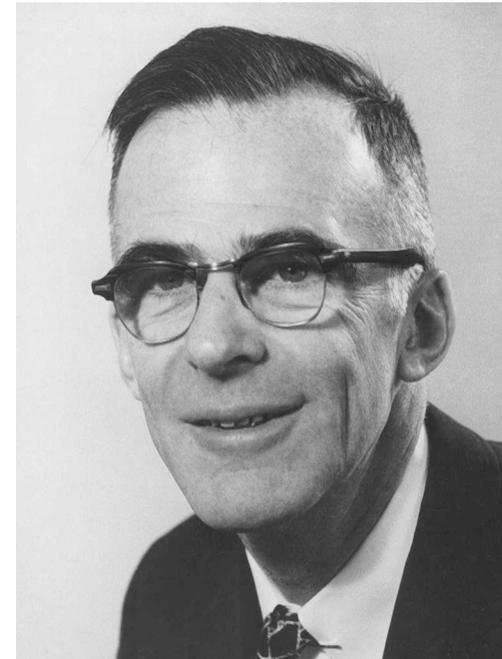
- Critical mass for gravitational collapse in presence of B-field

$$M_{cr} = \frac{5^{3/2}}{48\pi^2} \frac{B^3}{G^{3/2} \rho^2}$$

- Critical mass-to-flux ratio (Mouschovias & Spitzer 1976)

$$\left[\frac{M}{\Phi} \right]_{cr} = \frac{\xi}{3\pi} \left[\frac{5}{G} \right]^{1/2}$$

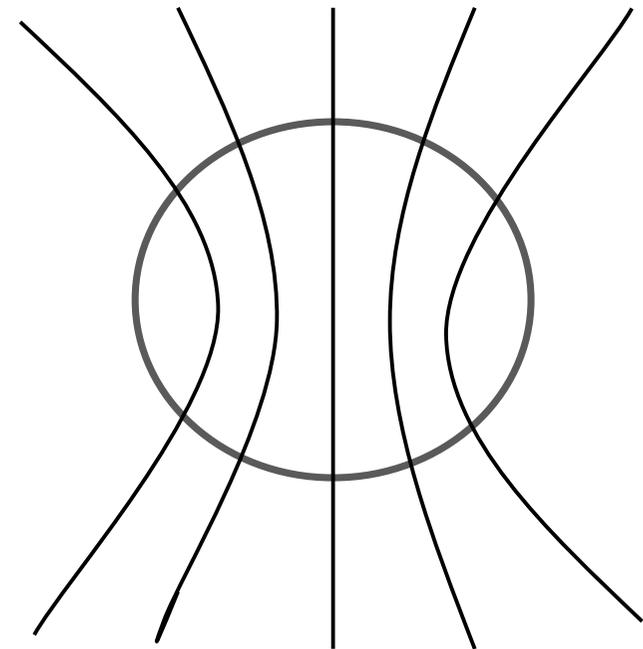
- Ambipolar diffusion can initiate collapse



Lyman Spitzer, Jr., 1914 - 1997

The "standard theory" of star formation:

- BASIC ASSUMPTION: Stars form from magnetically highly subcritical cores
- Ambipolar diffusion slowly increases (M/Φ) : $\tau_{AD} \approx 10\tau_{ff}$
- Once $(M/\Phi) > (M/\Phi)_{crit}$: dynamical collapse of SIS
 - Shu (1977) collapse solution
 - $dM/dt = 0.975 c_s^3/G = \text{const.}$
- Was (in principle) only intended for isolated, low-mass stars



Problems of magnetic SF

- Observed B-fields are weak, at most marginally critical (Crutcher 1999, Bourke et al. 2001)
- Magnetic fields cannot prevent decay of turbulence (Mac Low et al. 1998, Stone et al. 1998, Padoan & Nordlund 1999)
- Structure of prestellar cores (Bacman et al. 2000, e.g. Barnard 68 from Alves et al. 2001)
- Strongly time varying dM/dt (e.g. Hendriksen et al. 1997, André et al. 2000)
- More extended infall motions than predicted by the standard model (Williams & Myers 2000, Myers et al. 2000)

Problems of magnetic SF

- As many prestellar cores as protostellar cores in SF regions (e.g. André et al 2002)
- Molecular cloud clumps seem to be chemically young
(Bergin & Langer 1997, Pratap et al 1997, Aikawa et al 2001)
- Stellar age distribution small ($\tau_{\text{ff}} \ll \tau_{\text{AD}}$)
(Ballesteros-Paredes et al. 1999, Elmegreen 2000, Hartmann 2001)
- Strong theoretical criticism of the SIS as starting condition for gravitational collapse
(e.g. Whitworth et al 1996, Nakano 1998, as summarized in Klessen & Mac Low 2004)
- Most stars form as binaries

NEW THEORY

Gravoturbulent star formation

- New theory of star formation:

*Star formation is controlled
by interplay between
gravity and
supersonic turbulence!*

- Dual role of turbulence:
 - *stability on large scales*
 - *initiating collapse on small scales*

Gravoturbulent star formation

- New theory of star formation:

*Star formation is controlled
by interplay between
gravity and
supersonic turbulence!*

- Validity:

This hold on *all* scales and applies to build-up of stars and star clusters within molecular clouds as well as to the formation of molecular clouds in galactic disk.

Gravoturbulent Star Formation

- *Supersonic turbulence* in the galactic disk creates strong **density fluctuations** (in shocks: $\delta\rho/\rho \propto M^2$)
 - chemical phase transition: atomic \rightarrow molecular
 - cooling instability
 - gravitational instability
- Cold *molecular clouds* form at the high-density peaks.
- *Turbulence* creates density structure, *gravity* selects for collapse
—————→ **GRAVOTUBULENT FRAGMENTATION**
- *Turbulent cascade*: Local compression *within* a cloud provokes collapse \rightarrow individual *stars* and *star clusters*

In detail...

Molecular clouds

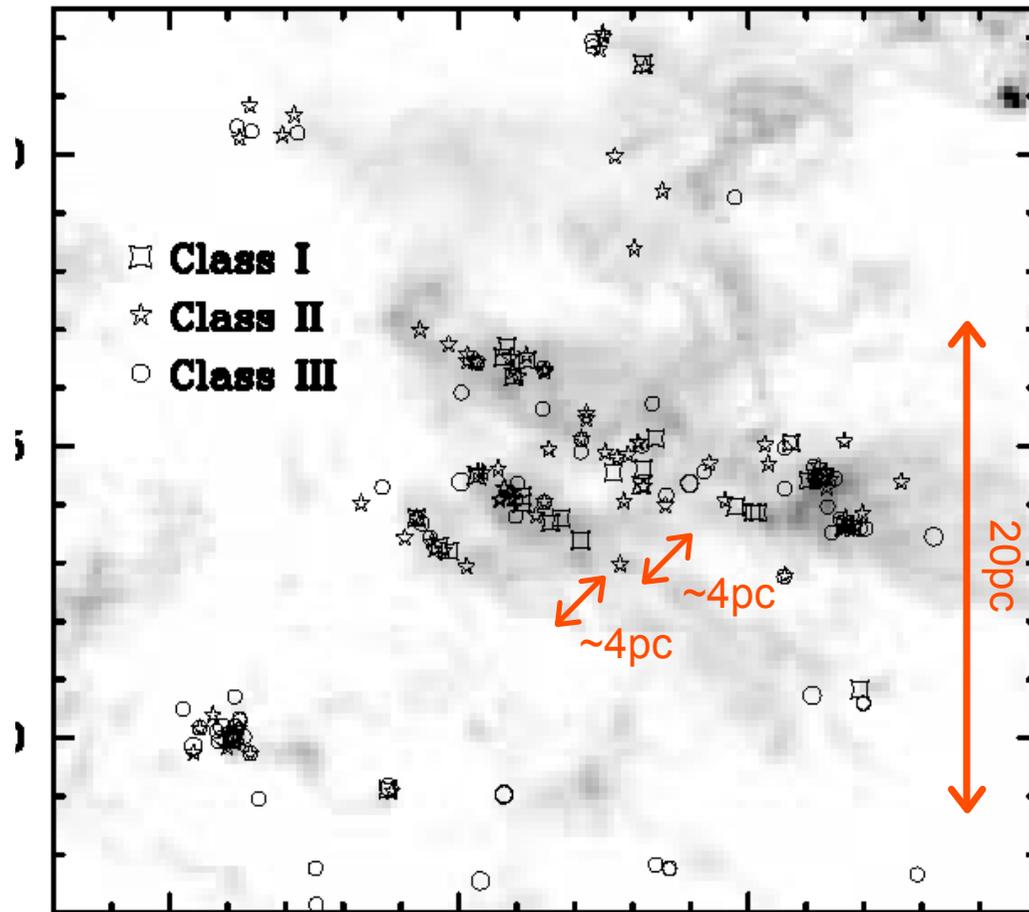
- MC's are *massive* ($M_{\text{cloud}} = 10^3 \dots 10^6 M_{\odot} \leftrightarrow M_{\text{Jeans}} = 1 \dots 100 M_{\odot}$)
- MC's are *cold* ($T_{\text{cloud}} = 10 \dots 20 \text{ K}$)
- MC's are *transient* (life time \approx few $\tau_{\text{cross}} \approx$ few $\tau_{\text{ff}} \approx$ few 10^6 yr)
- MC structure is determined by *supersonic turbulence*
(density and velocity structure dominated by large-scale modes)
- Energy budget: *Turbulent energy*
 \approx gravitational energy $>$ magnetic energy
- *BUT*: Turbulence *decays* rapidly ($\tau_{\text{decay}} \leq \tau_{\text{ff}} \approx 10^6 \text{ yr}$)
→ need for certain degree of energy input
- Typical *SF efficiency* $\sim 5\%$

Turbulent Jeans analysis

How do perturbations in self-gravitating supersonically turbulent gas evolve?

- Classical approach: **dispersion relations**
 $\omega^2 - c_s^2 k^2 + 4\pi G \rho_0 = 0$ (Jeans 1921)
to include turbulence: $c_s^2 \rightarrow c_s^2 + 1/3 \langle v^2 \rangle$ (Chandrasekhar 1951)
- Consider wavelength dependence: $c_s^2 \rightarrow c_s^2 + 1/3 v^2(k)$
- For **incompressible turbulence**: support needs to act on wavelengths *below* the *thermal Jeans scale*. (Bonazzola et al. 1992)
- For **compressible turbulence**: 1D simulations show high-Mach number turbulence induces (local) collapse. (Gammie & Ostriker 1996)
- **Our group**: Since 2000/1, systematic 3D large-eddy simulations of (M)HD turbulence with SPH and ZEUS
(Klessen, Heitsch, & Mac Low 2000 + Heitsch, Mac Low, & Klessen 2001)
- In the past 5-6 years: many studies with SPH, different finite difference schemes, spectral codes, BGK, etc....

Gravoturbulent fragmentation



Map of Taurus: Hartmann 2002

Movie: a model for star formation in the Taurus cloud
from Klessen & Ballesteros Paredes, in preparation

Gravoturbulent fragmentation in molecular clouds:

- SPH model with 1.6×10^6 particles
- large-scale driven turbulence
- Mach number $\mathcal{M} = 6$
- periodic boundaries
- isothermal EOS
- total mass $M_{\text{tot}} = 120 \times M_J$
(M_J = thermal Jeans mass)
- physical scaling:

“Taurus”:

→ density $n(\text{H}_2) \approx 10^2 \text{ cm}^{-3}$:

→ $L = 6 \text{ pc}, M = 5000 M_J$

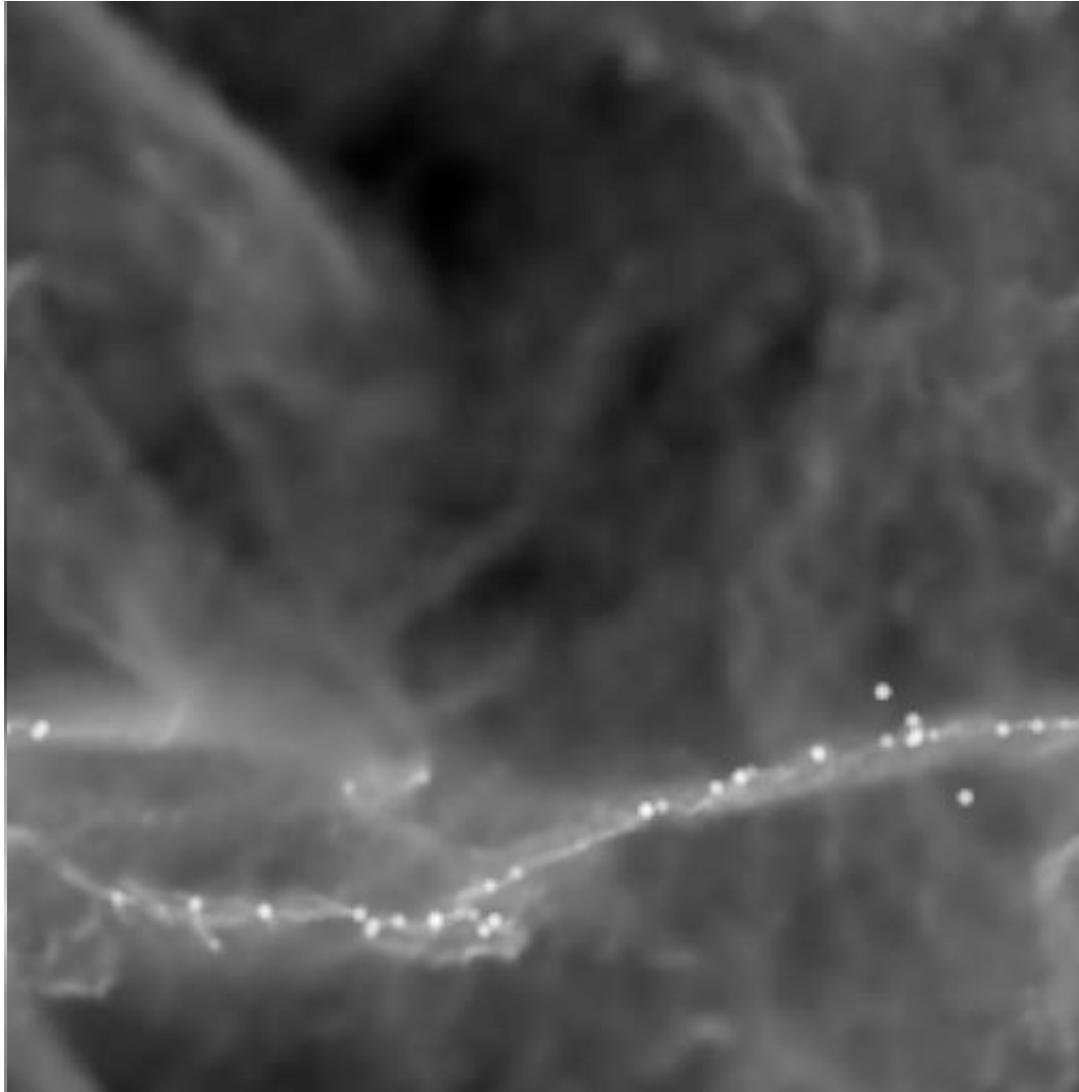


Model of gravoturbulent fragmentation

- SPH model with 1.6×10^6 particles
- large-scale driven turbulence
- Mach number $\mathcal{M} = 6$
- periodic boundaries
- physical scaling:

(from Klessen & Ballesteros, in preparation)

Gravoturbulent fragmentation



Gravoturbulent fragmentation in molecular clouds:

- SPH model with 1.6×10^6 particles
- large-scale driven turbulence
- Mach number $\mathcal{M} = 6$
- periodic boundaries
- physical scaling:

“Taurus”:

→ density $n(\text{H}_2) \approx 10^2 \text{ cm}^{-3}$:

→ $L = 6 \text{ pc}$,

$M = 5000 M_\odot$

NEXT STEPS: *differential rotation, chemical network (proper cooling function & $\text{H} \rightarrow \text{H}_2$), physical driving source*

What can we learn from that?

- *global properties* (statistical properties)
 - SF efficiency
 - SF time scale
 - IMF
 - description of self-gravitating turbulent systems (pdf's, Δ -var.)
 - chemical mixing properties
- *local properties* (properties of individual objects)
 - properties of individual clumps (e.g. shape, radial profile)
 - accretion history of individual protostars (dM/dt vs. t , j vs. t)
 - binary (proto)stars (eccentricity, mass ratio, etc.)
 - SED's of individual protostars
 - dynamic PMS tracks: $T_{\text{bol}}-L_{\text{bol}}$ evolution

What can we learn from that?

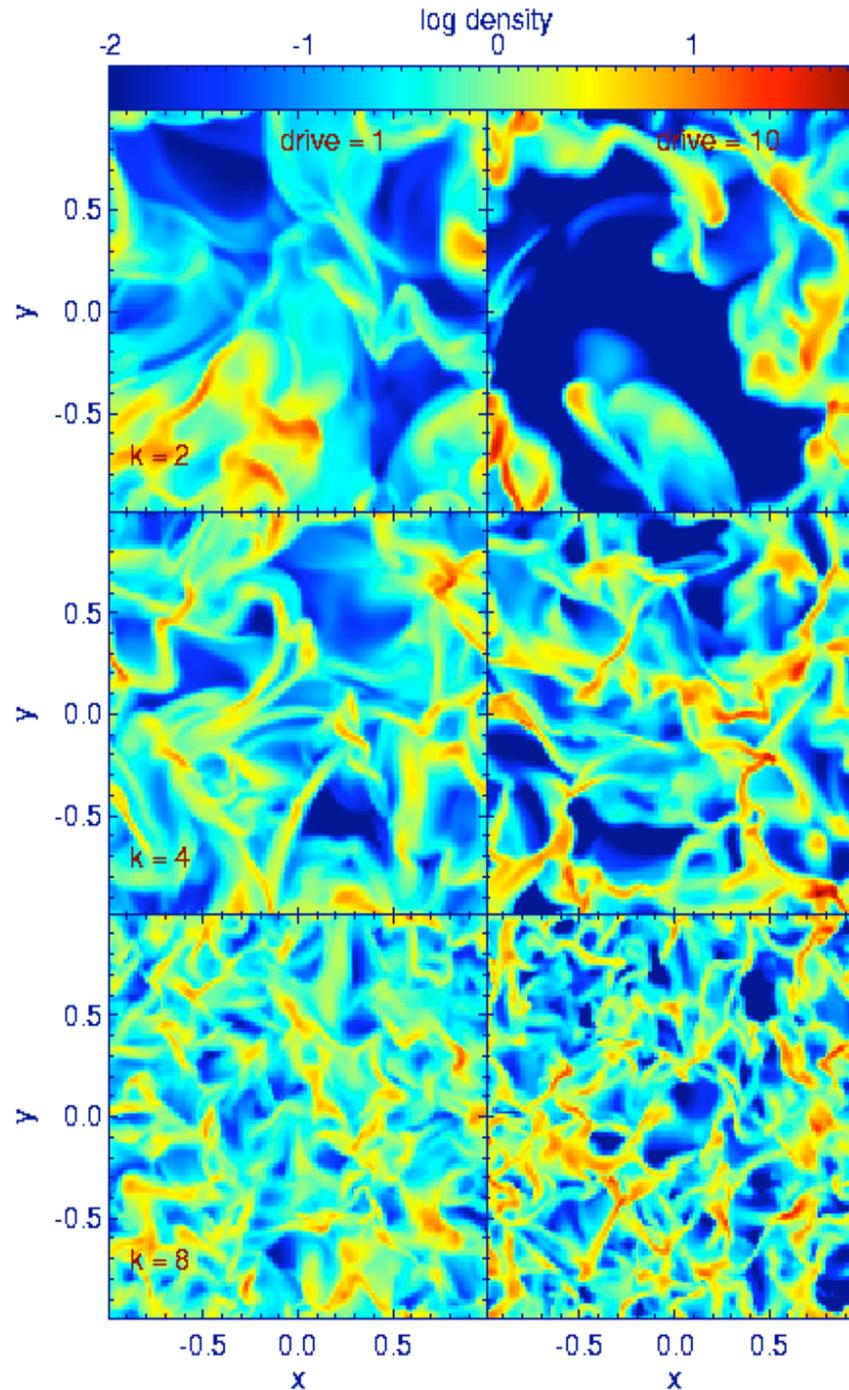
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weak driving

$$k = 2$$

$$k = 4$$

$$k = 8$$



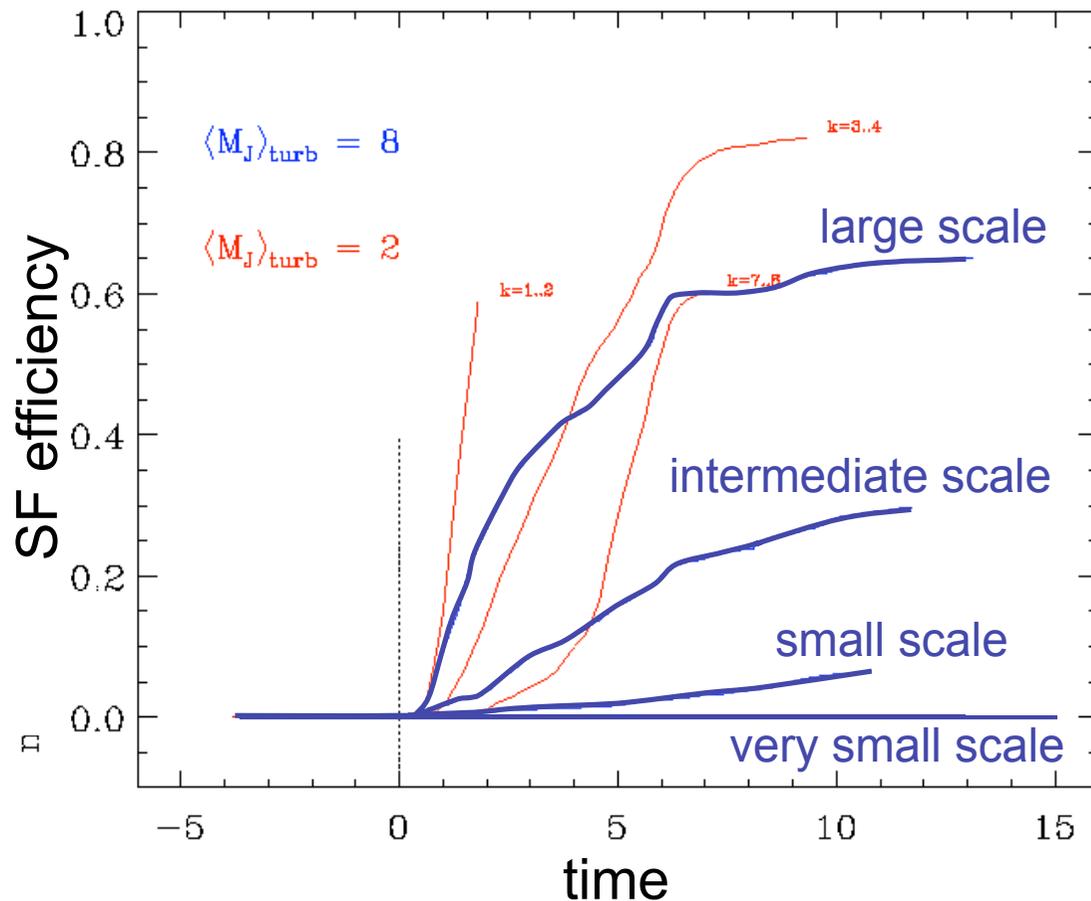
strong driving

large-scale
turbulence

intermediate-
scale turbulence

small-scale
turbulence

Efficiency of star formation



Star formation efficiency is **high** for *large-scale turbulence* and **low** if most energy resides on *small scales*.

Efficiency *decreases* with *increasing* turbulent kinetic energy.

Local collapse can only be *prevented* completely if turbulence is driven on scales *below* the Jeans length. ← **this is unrealistic**

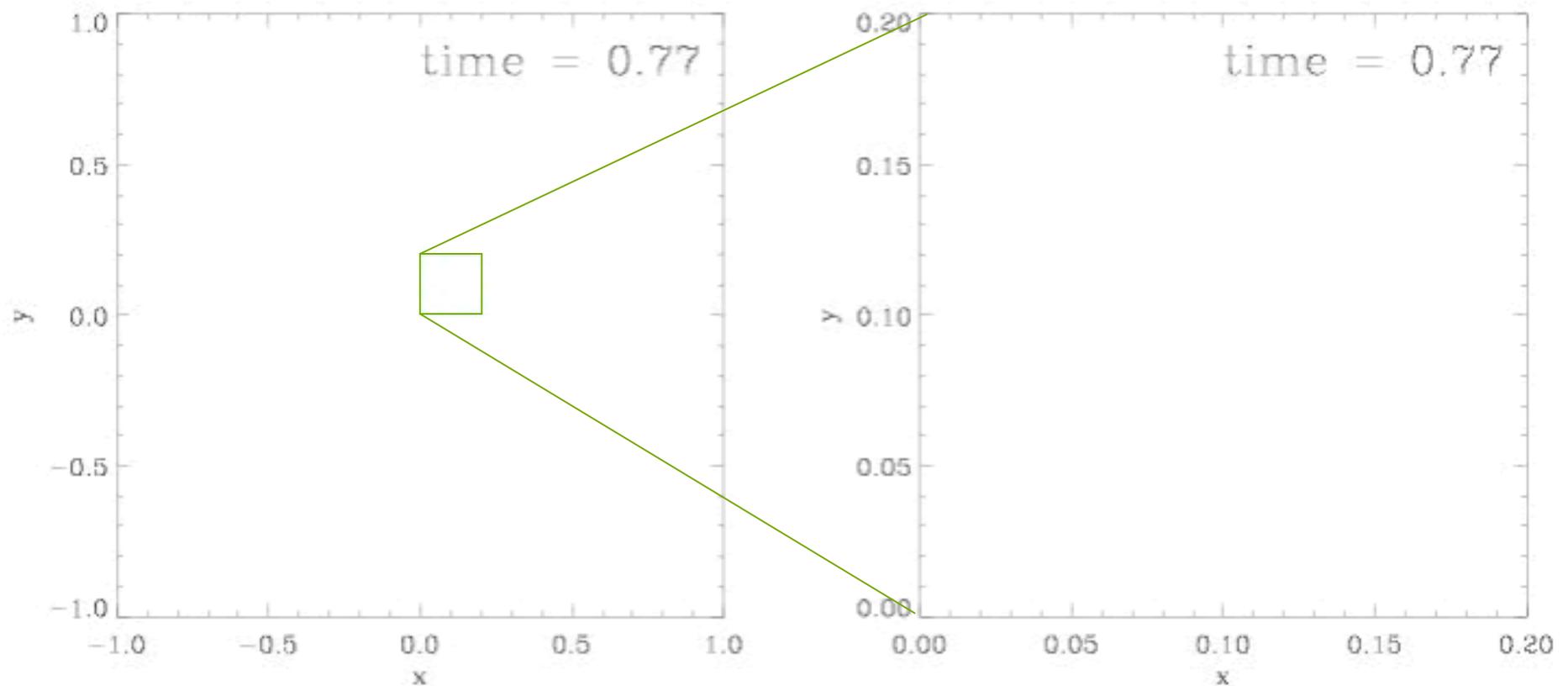
→ It is very difficult prevent star formation in molecular clouds.

What can we learn from that?

- *global properties* (statistical properties)
 - SF efficiency
 - SF time scale
 - IMF – formation of stellar clusters
 - description of self-gravitating turbulent systems (pdf's, Δ -var.)
 - chemical mixing properties
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Star cluster formation

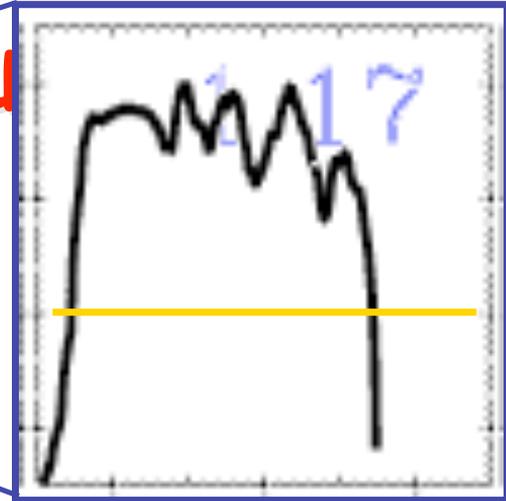
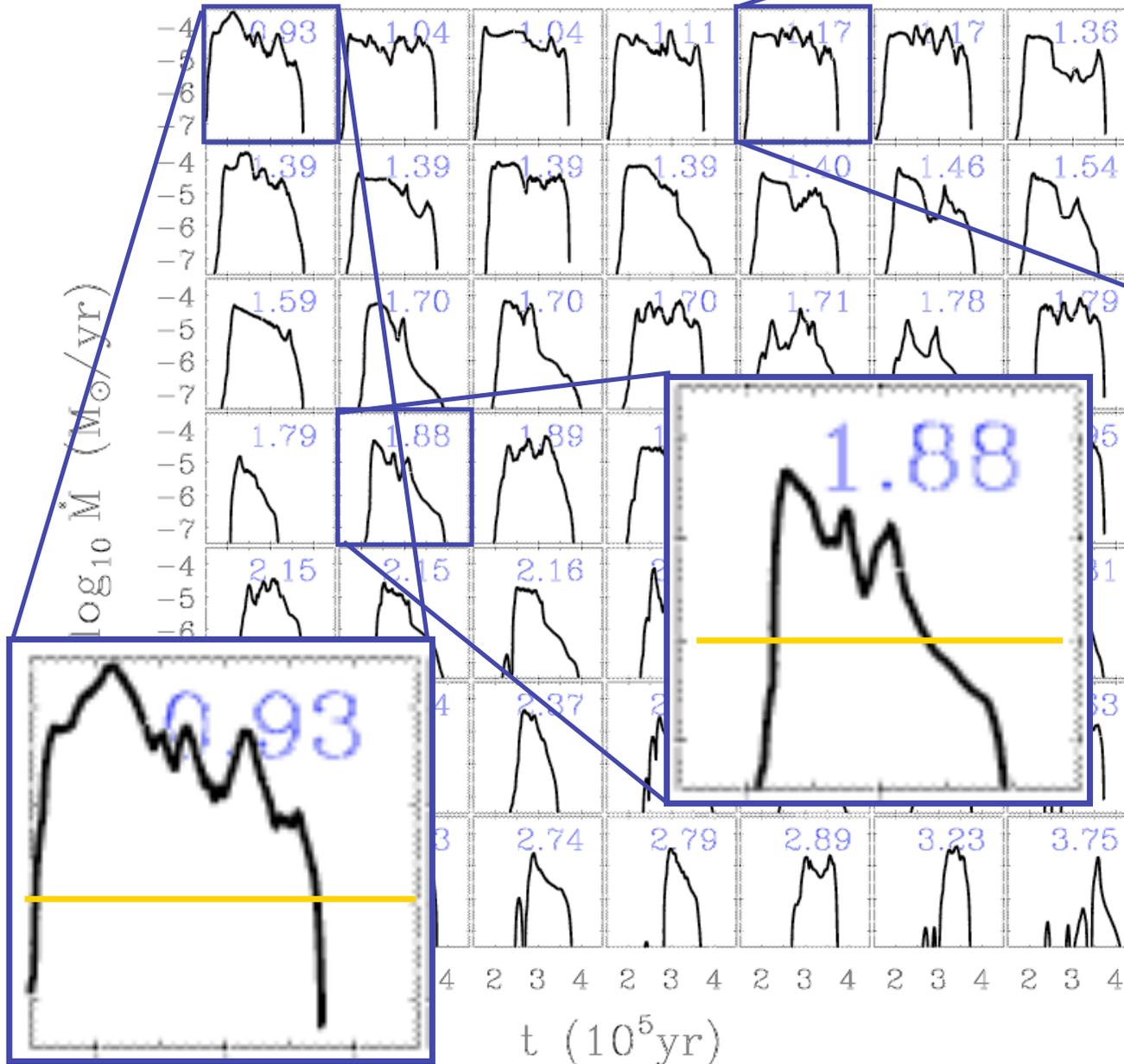
Most stars form in clusters → *star formation = cluster formation*



Trajectories of protostars in a nascent dense cluster created by gravoturbulent fragmentation

(from Klessen & Burkert 2000, ApJS, 128, 287)

Accretion rates in clu

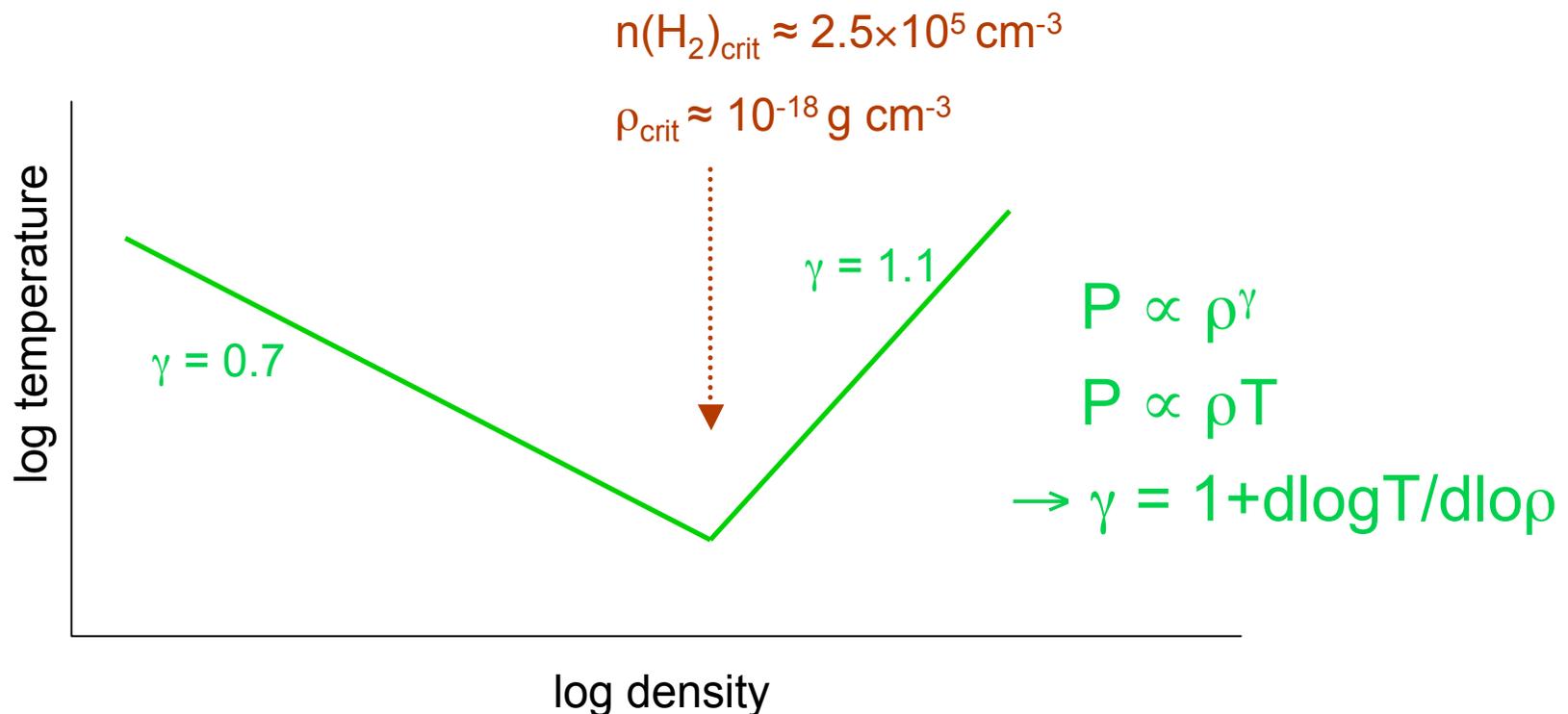


Mass accretion rates *vary with time* and are strongly *influenced* by the *cluster environment*.

(Klessen 2001, ApJ, 550, L77;
also Schmeja & Klessen,
2004, A&A, 419, 405)

Influence of EOS

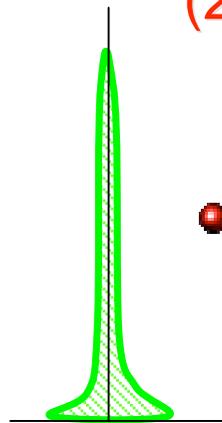
- But EOS depends on *chemical state*, on *balance* between *heating* and *cooling*



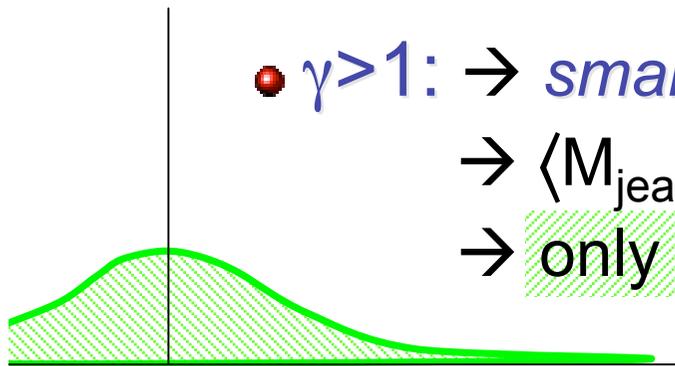
Influence of EOS

$$(1) \quad p \propto \rho^\gamma \quad \rightarrow \quad \rho \propto p^{1/\gamma}$$

$$(2) \quad M_{\text{jeans}} \propto \gamma^{3/2} \rho^{(3\gamma-4)/2}$$



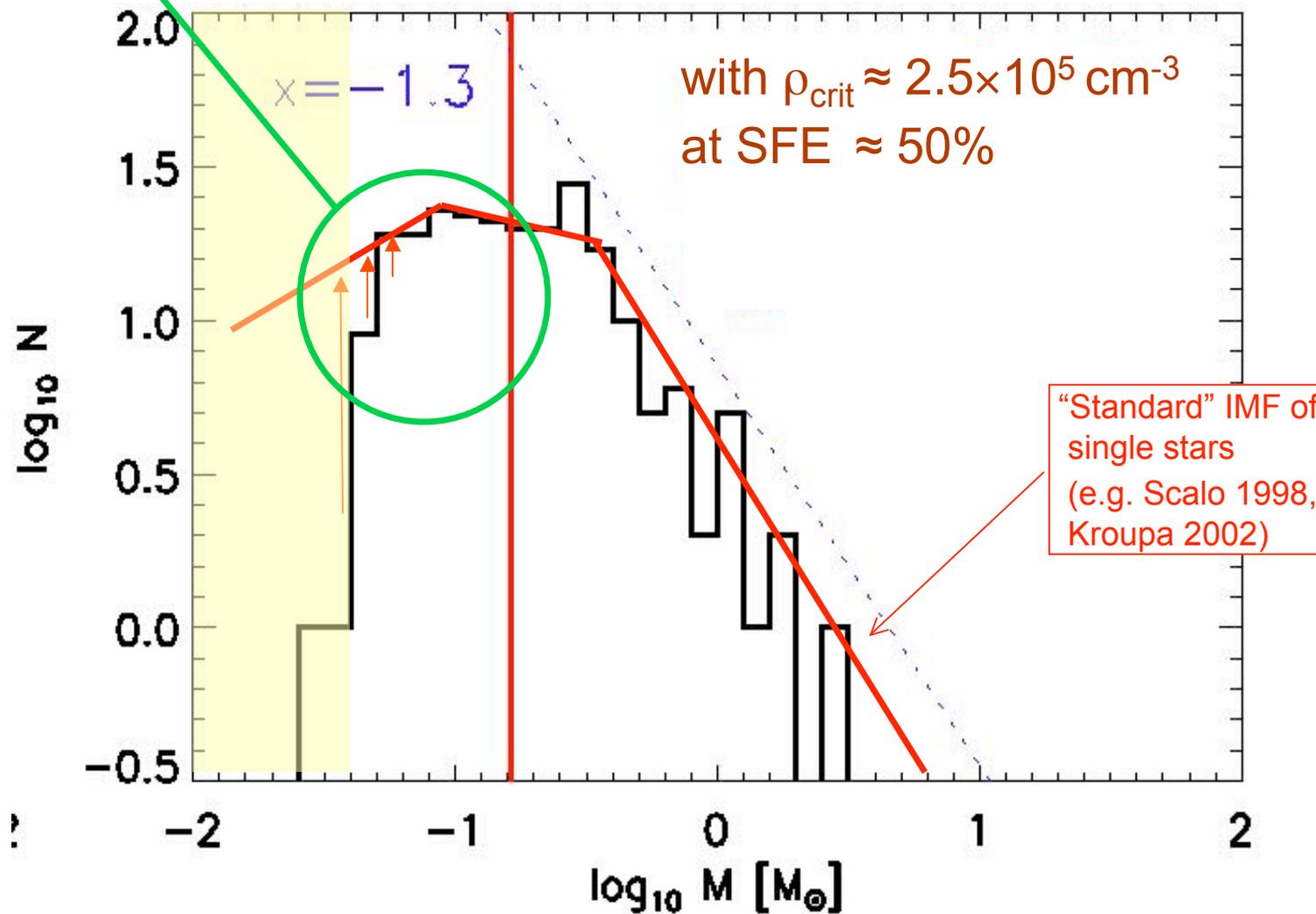
- $\gamma < 1$: \rightarrow *large* density excursion for given pressure
 \rightarrow $\langle M_{\text{jeans}} \rangle$ becomes small
 \rightarrow number of fluctuations with $M > M_{\text{jeans}}$ is large



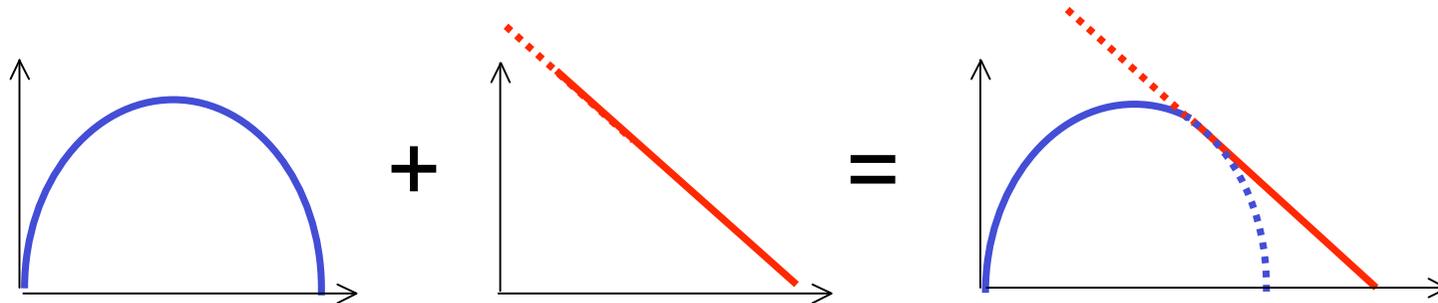
- $\gamma > 1$: \rightarrow *small* density excursion for given pressure
 \rightarrow $\langle M_{\text{jeans}} \rangle$ is large
 \rightarrow only few and massive clumps exceed M_{jeans}

Mass spectrum

sufficient # of brown dwarfs



Plausibility argument for shape



- Supersonic turbulence is scale free process

→ *POWER LAW BEHAVIOR*

- *But also:* turbulence and fragmentation are highly stochastic processes → central limit theorem

→ *GAUSSIAN DISTRIBUTION*

What can we learn from that?

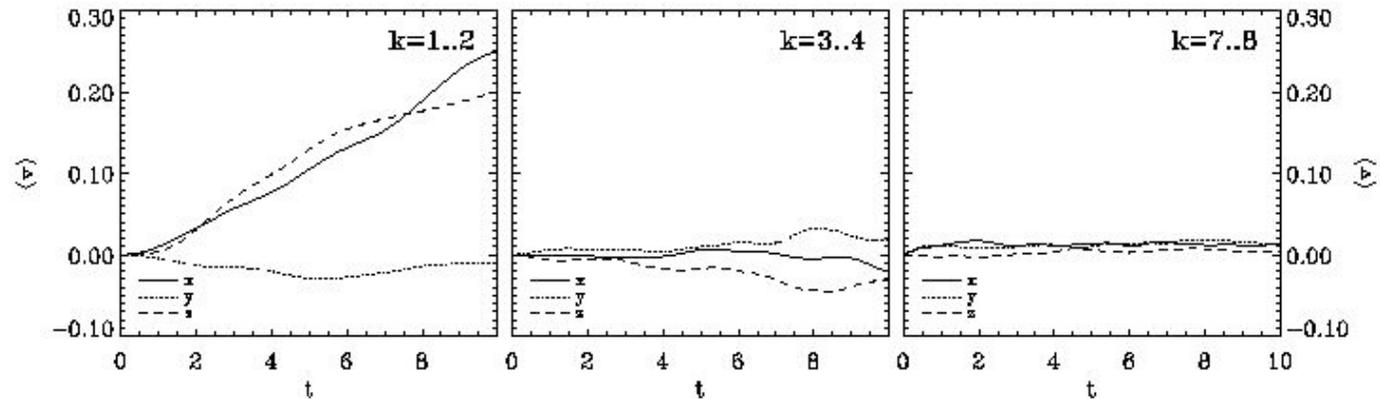
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 - SED's of individual protostars
 - dynamic PMS tracks: $T_{\text{bol}}-L_{\text{bol}}$ evolution

Turbulent diffusion I

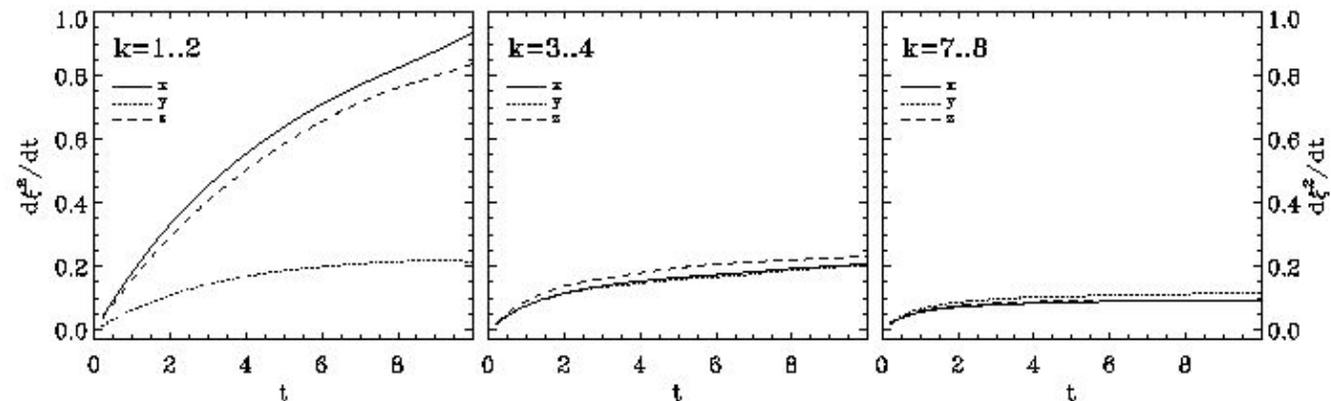
- Observations of young star clusters exhibit an enormous degree of *chemical homogeneity* (e.g. in the Pleiades: Wilden et al. 2002)
- Star-forming gas must be *well mixed*.
- How does this constrain models of interstellar turbulence?
- → Study mixing in supersonic compressible turbulence.....

Turbulent diffusion II

- Large-scale turbulence associated with bulk motion.

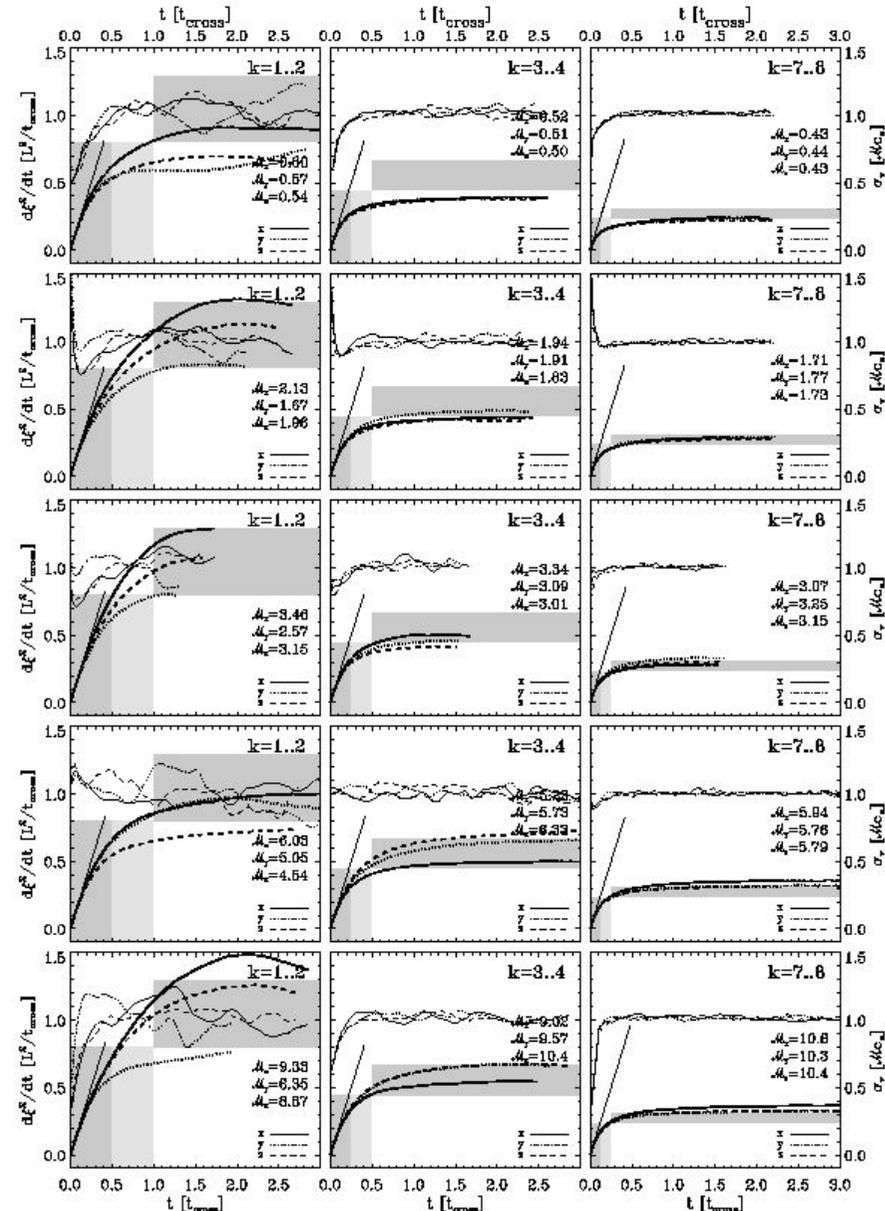


- Super-diffusive behavior.



Turbulent diffusion III

- Mean-motion corrected diffusion
- Simple mixing-length approach:
 - $D(t) \approx v_{\text{rms}}^2 t \quad t < \tau$
 - $D(t) \approx v_{\text{rms}}^2 \tau = v_{\text{rms}} \ell \quad t > \tau$
 - With v_{rms} = rms velocity and $\ell = L/k =$ shock sep.



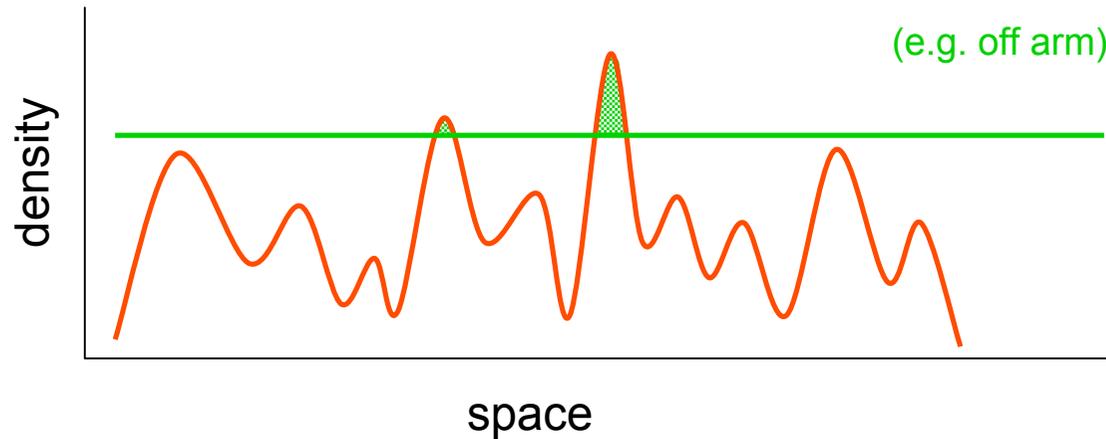
GALACTIC SCALE

Würzburg, January 20, 2005

Star formation on *global scales*

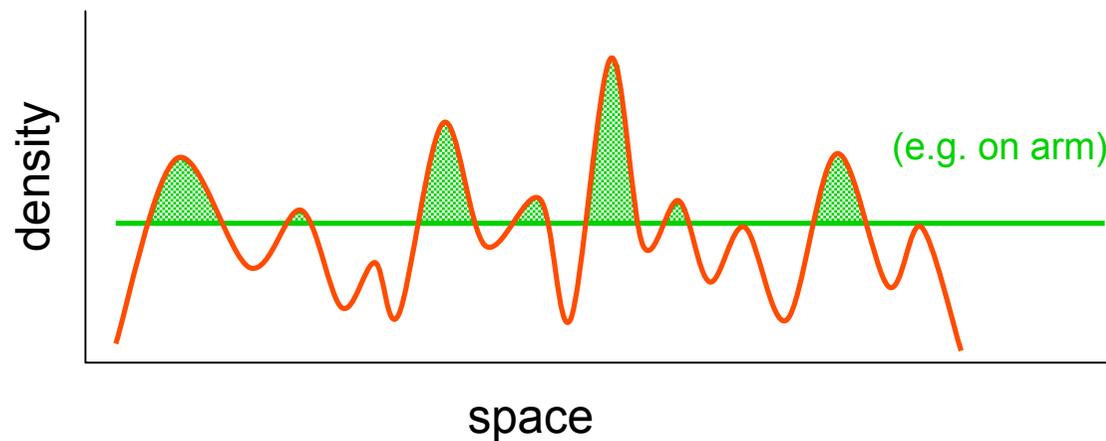
- *SF on global scales* = *formation of molecular clouds*
- MC's form at *stagnation points* of *convergent large-scale flows*
(need $\sim 0.5 \text{kpc}^3$ of gas) \rightarrow high density \rightarrow enhanced cooling \rightarrow fast H_2 formation & gravitational instability \rightarrow local collapse and star formation
- External perturbations *increase* the local likelihood of MC formation (e.g. in spiral density waves, galaxy interactions, etc.)

Star formation on *global scales*



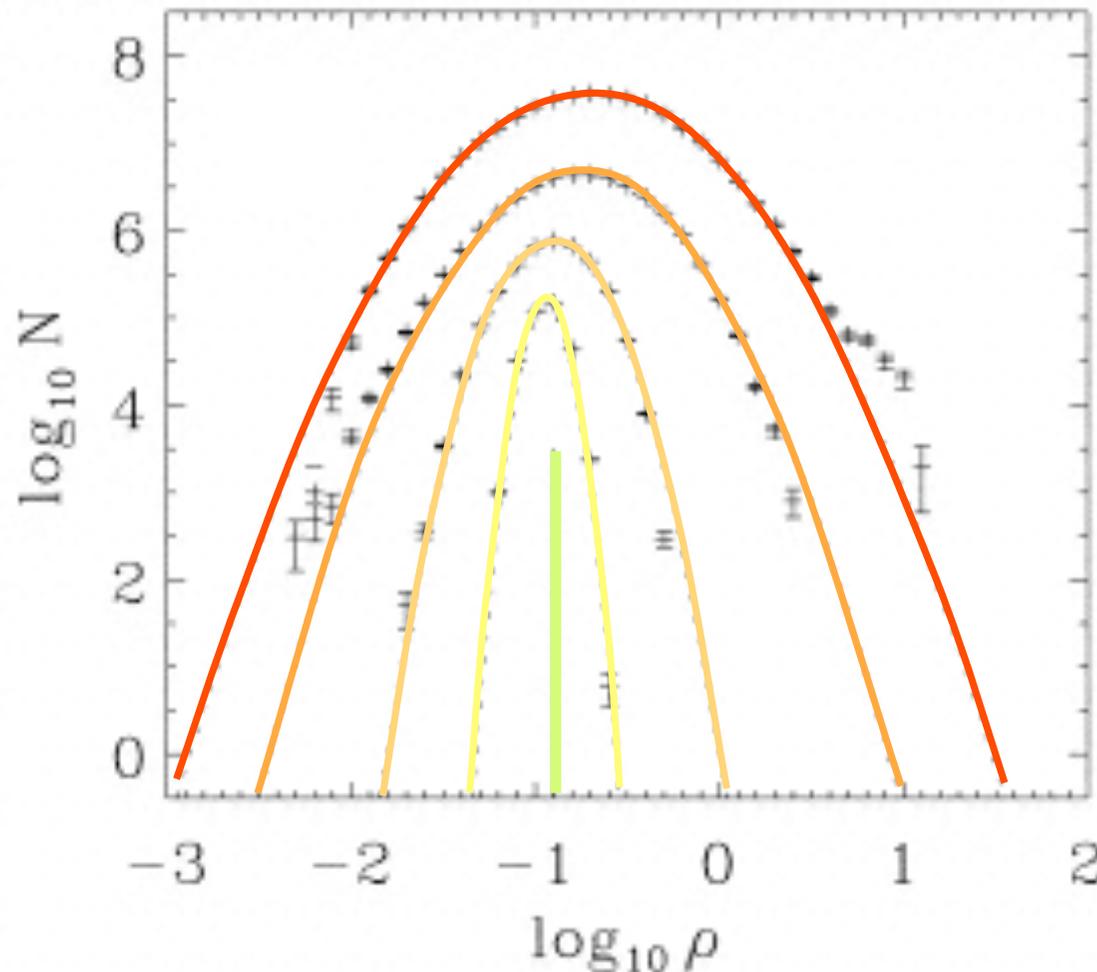
density fluctuations in warm atomic ISM caused by supersonic turbulence

some are dense enough to form H₂ within “reasonable timescale”
→ molecular clouds



external perturbations (i.e. potential changes) increase likelihood

Star formation on *global scales*



probability
distribution
function of
density
(ρ -pdf) for
decaying
supersonic
turbulence

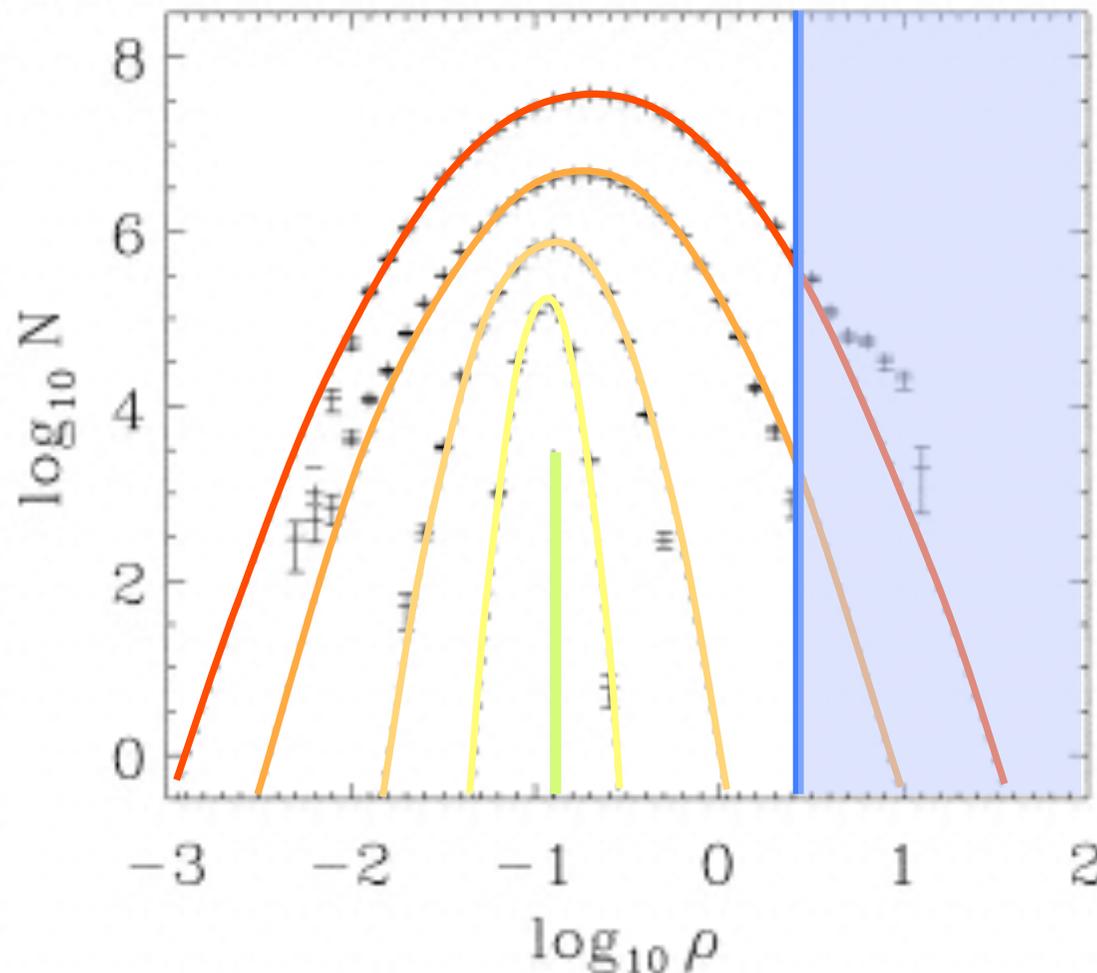
*varying rms Mach
numbers:*

M1 > **M2** >
M3 > **M4** > **0**

mass weighted ρ -pdf, each shifted by $\Delta \log N = 1$

(from Klessen, 2001)

Star formation on *global scales*



mass weighted ρ -pdf, each shifted by $\Delta \log N = 1$

(from Klessen, 2001; rate from Hollenback, Werner, & Salpeter 1971)

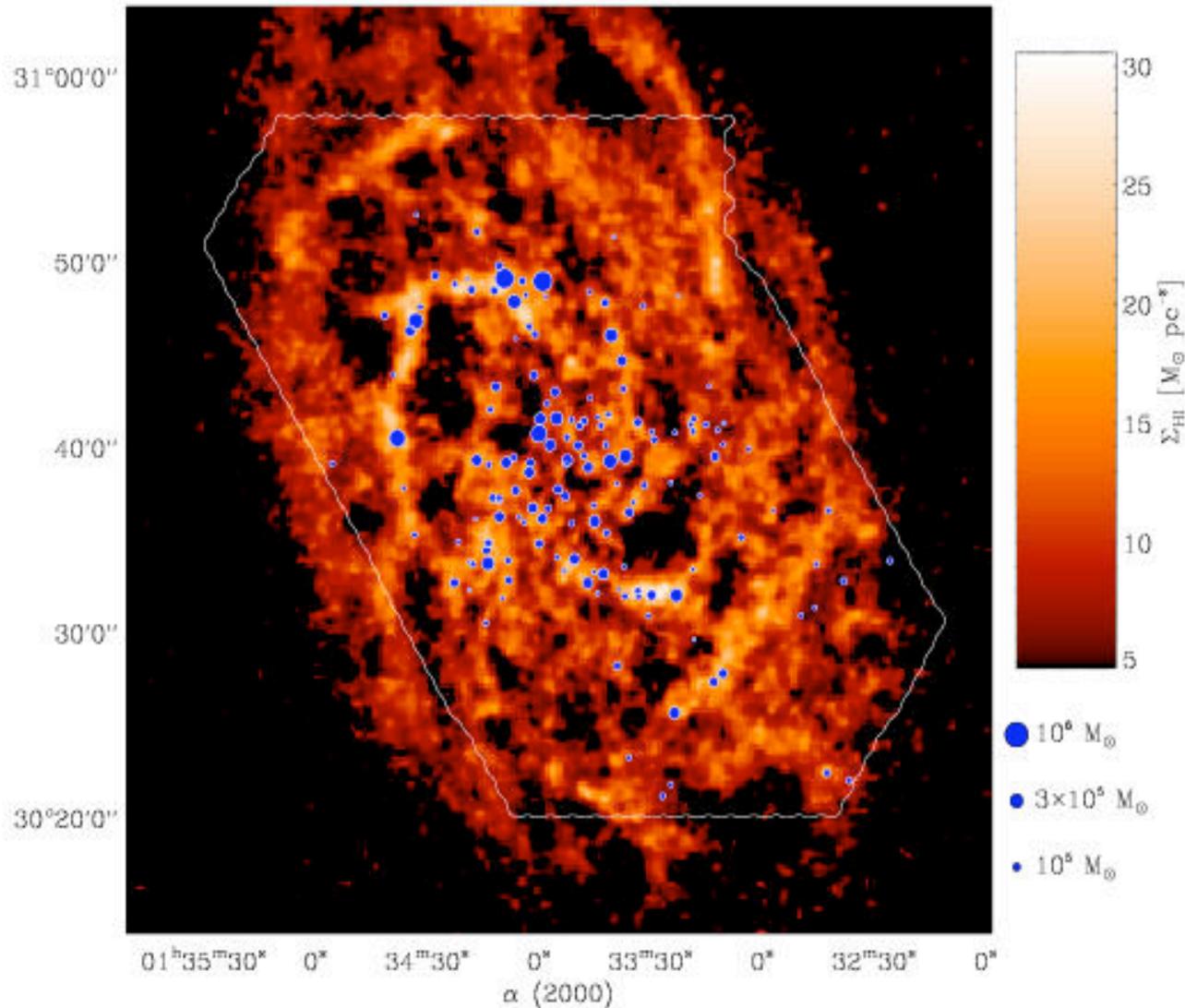
H₂ formation rate:

$$\tau_{\text{H}_2} \approx \frac{1.5 \text{ Gyr}}{n_{\text{H}} / 1 \text{ cm}^{-3}}$$

For $n_{\text{H}} \geq 100 \text{ cm}^{-3}$,
H₂ forms within
10 Myr, this is
about the lifetime
of typical MC's.

*What fraction of
the galactic ISM
reaches such
densities?*

Correlation between H₂ and HI



Compare H₂ - HI
in M33:

- H₂: BIMA-SONG Survey, see Blitz et al.
- HI: Observations with Westerbork Radio T.

H₂ clouds are seen
in regions of high
HI density
(in spiral arms and
filaments)

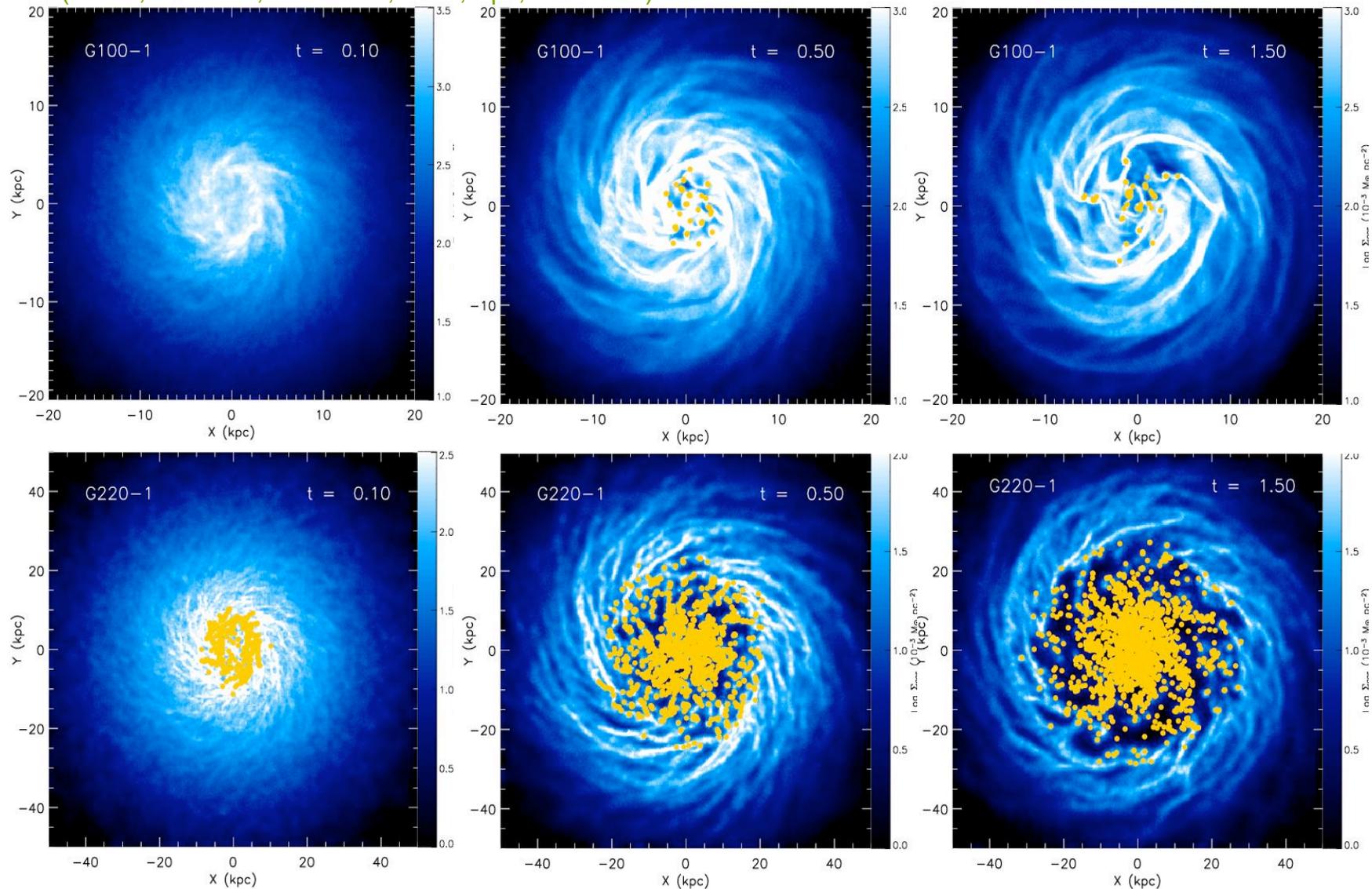
(Deul & van der Hulst 1987, Blitz et al. 2004)

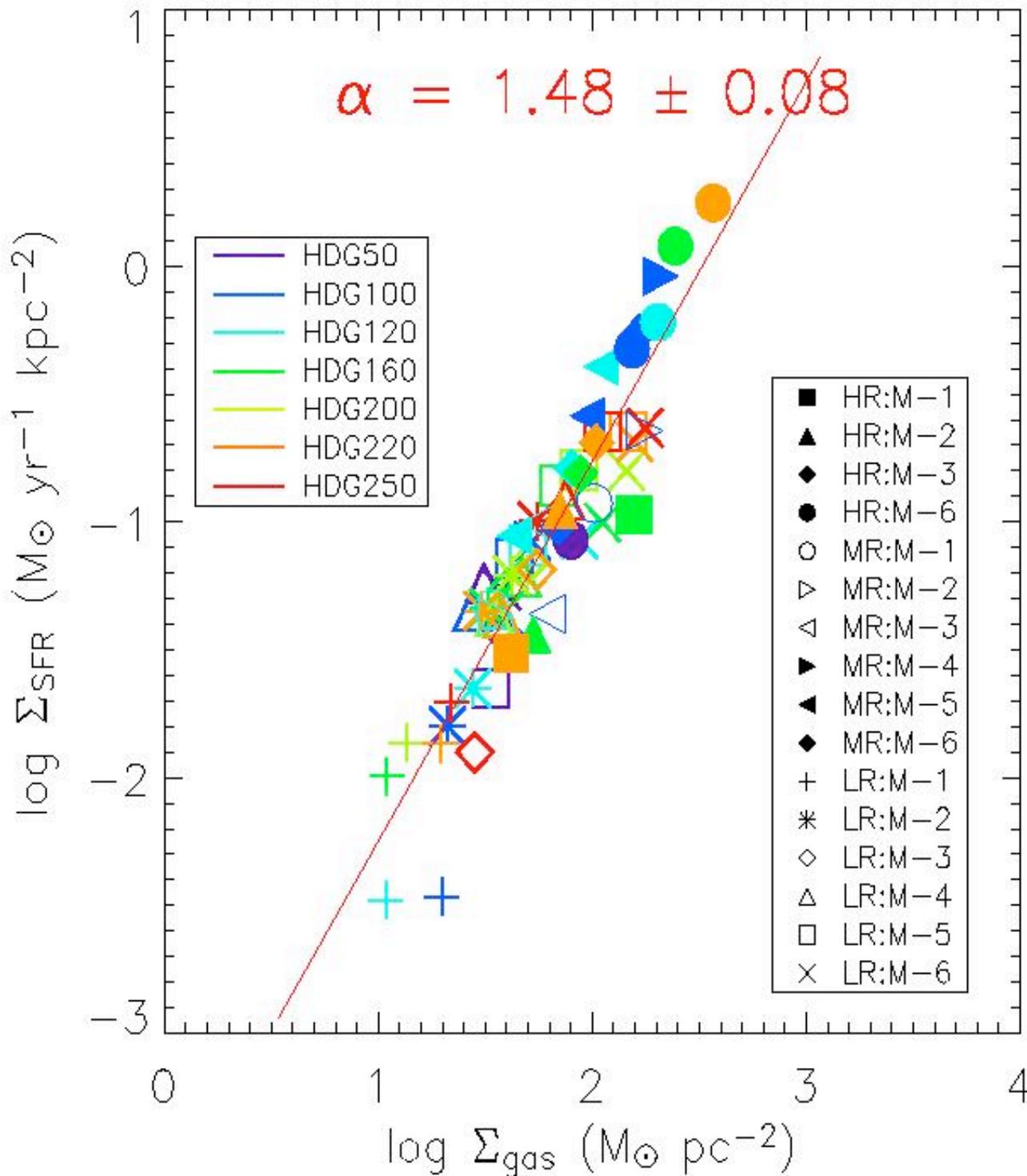
Modeling galactic SF

- Evolution of 42 isolated disk galaxies
 - DM halo, stellar disk & gas disk
 - SPH code GADGET with accretion particles
(resolution: 5×10^5 to 3×10^6 gas particles)
 - $50 \text{ km/s} \leq v_{\text{circ}} \leq 250 \text{ km/s}$
 - fraction of disk mass: $m_d = 5\% - 10\%$
 - gas fraction in disk: $f_d = 20\%, 50\%, \& 90\%$
 - total mass: $4.15 \times 10^{10} M_{\odot} \leq M_{200} \leq 357.14 \times 10^{10} M_{\odot}$
(corresponds to mass resolution of $138 M_{\odot} \leq M_{\text{SPH}} \leq 10^5 M_{\odot}$ in models with 3×10^6 gas particles)

Modeling galactic SF

(aus Li, Mac Low, & Klessen, 2004, ApJ, submitted)





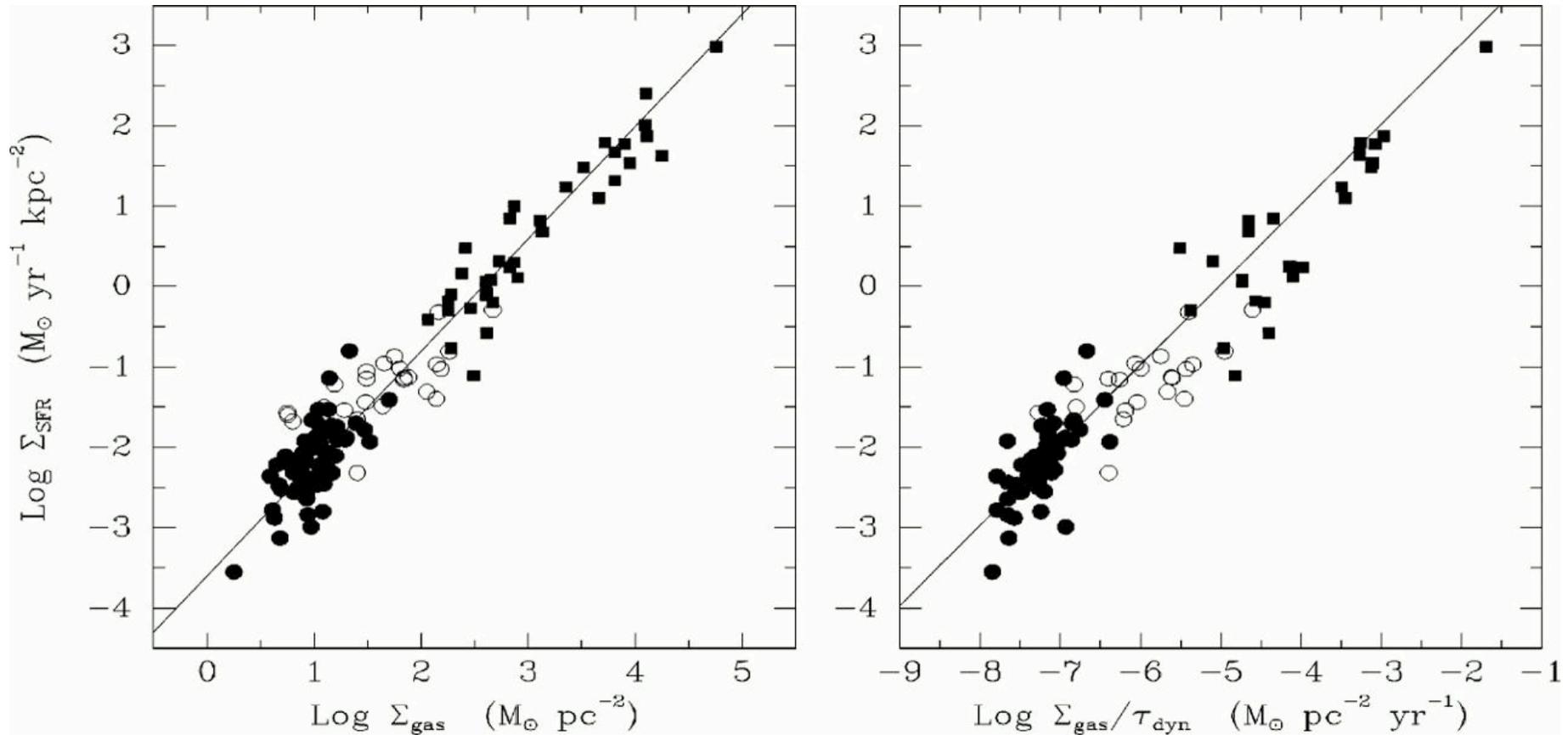
(Li, Mac Low, & Klessen, 2004, ApJ submitted)

We find correlation between *star formation rate* and *gas surface density*:

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^{1.5}$$

global Schmidt law

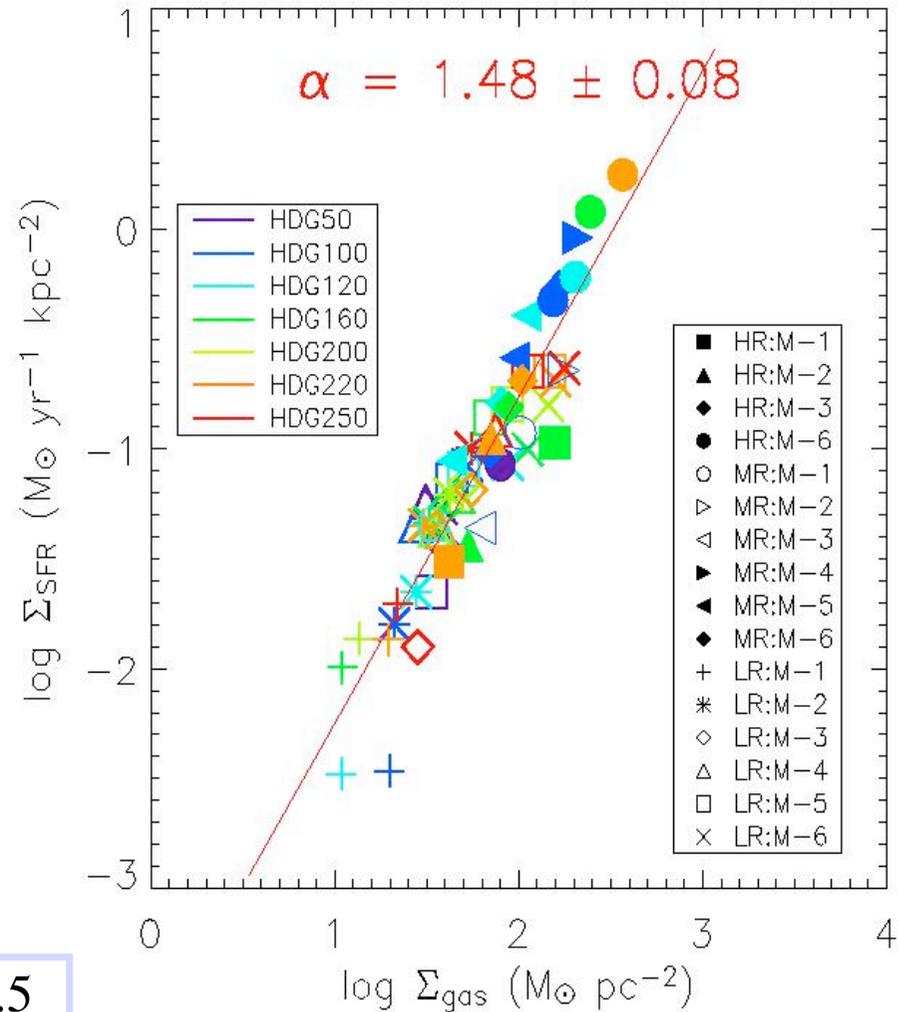
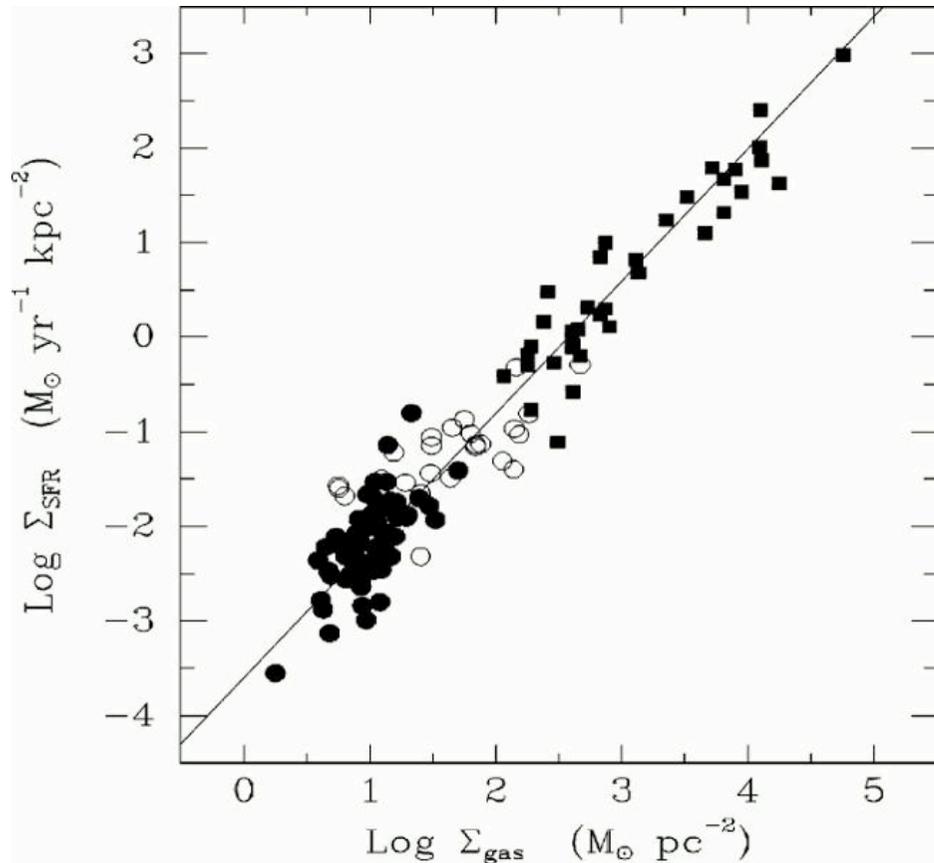
Observed Schmidt law



$$\Sigma_{\text{SFR}} = (2.5 \pm 0.7) \times 10^{-4} \left(\frac{\Sigma_{\text{gas}}}{1 M_{\odot} \text{ pc}^{-2}} \right)^{1.4 \pm 0.15} M_{\odot} \text{ year}^{-1} \text{ kpc}^{-2},$$

(from Kennicutt 1998)

Observed Schmidt law



in both cases:

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^{1.5}$$

(from Kennicutt 1998)

Summary

Summary

- Stars form from complex *interplay* between *gravity* and *supersonic turbulence*

→ GRAVOTURBULENT STAR FORMATION

- Supersonic turbulence plays a *dual role*:
 - on **large scales**: supersonic turbulence carries sufficient energy to prevent global collapse
 - on **small scales**: turbulence provokes collapse by creating high-density peaks
 - microturbulent approach is *not valid* in astrophysics

Summary

- *Gravoturbulent star formation* can explain
 - structure and evolution of molecular clouds (structure functions, pdf's, Δ -variance, PCA,...)
 - chemical mixing properties of the ISM
 - timescale and efficiency of star formation in molecular clouds and on galactic scales
 - structure and evolution of pre- and protostellar cores
 - protostellar accretion rates
 - binary properties and frequencies

Summary

- *Gravoturbulent star formation* can explain
 - the *IMF*:
 - turbulence together with EOS determines density structure
 - gravity then selects fluctuations to collapse → *characteristic mass*
 - this interplay determines *PEAK* and *WIDTH* of IMF

Summary: theory of SF

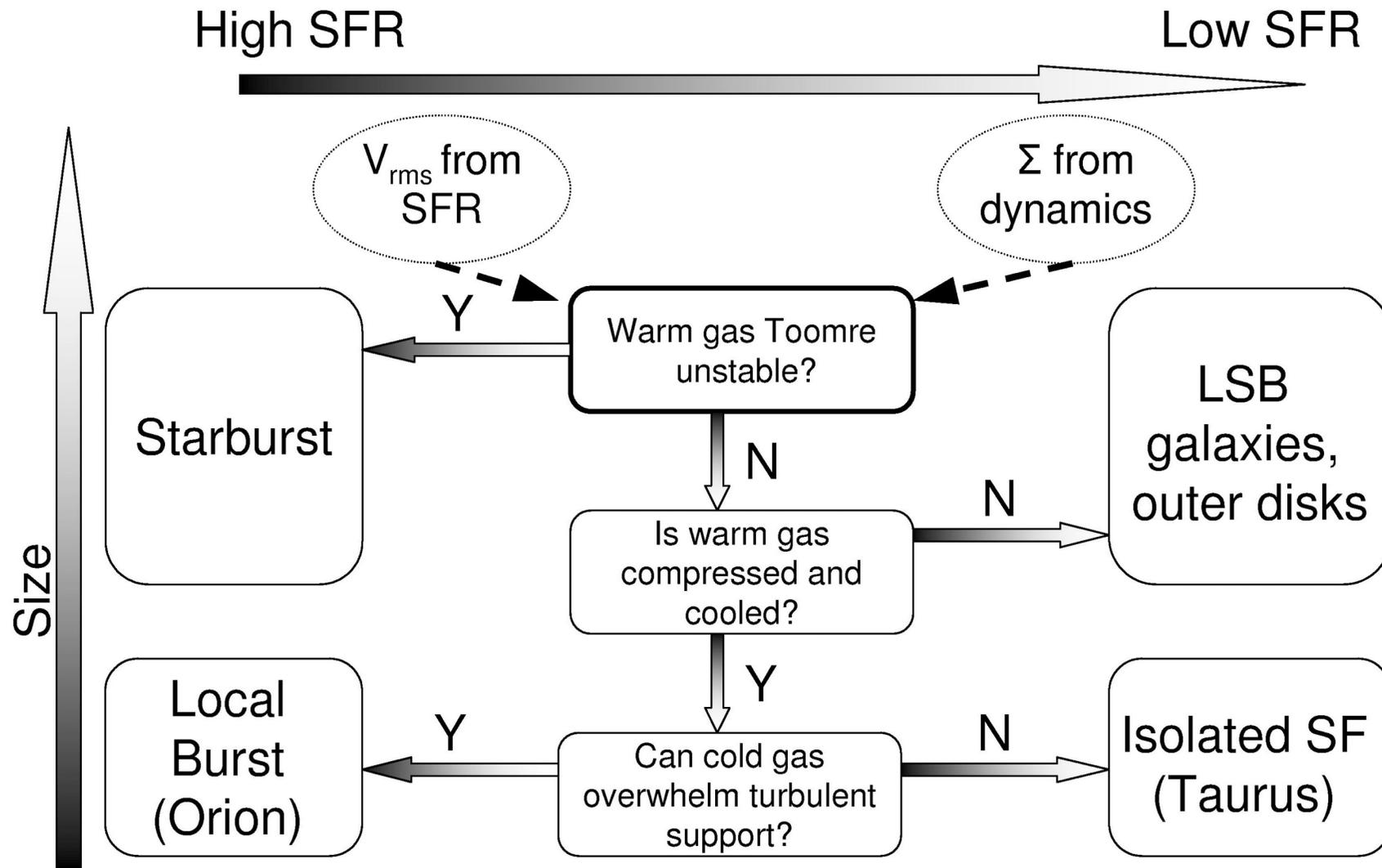
- *Gravoturbulent star formation* can explain
 - Gravity overwhelms turbulence: *Star burst*
(maybe triggered by interaction or global instability)
 - “Normal” *spiral galaxy*: approximate support by ISM turbulence, only local collapse
(with intermediate to low SF rate)
 - *LSB galaxy*: strong turbulent support
(turbulence generated by MRI or gas infall?)

Open questions

- What's next?
 - Understand *protostellar feedback*...
 - Understand *what drives turbulence*...
(and on what scales)
 - Understand *relation* between *large-scale dynamics* in the galaxy and *local build-up of stars*...
 - Understand *variations* of star formation with environmental conditions...
(e.g. Pop III stars, star burst galaxies, etc.)
 - Understand *planet formation* in turbulent cloud context...

Thanks!

Summary



Literature

- Quasi-static “standard theory” of SF:
 - Shu, Adams, & Lizano (1986, ARAA)
- Dynamical gravoturbulent theory:
 - Larson (2003, Prog. Rep. Phys.)
 - Mac Low & Klessen (2004, Rev. Mod. Phys.)
 - Elmegreen & Scalo (2005, ARAA)
 - Scalo & Elmegreen (2005, ARAA)