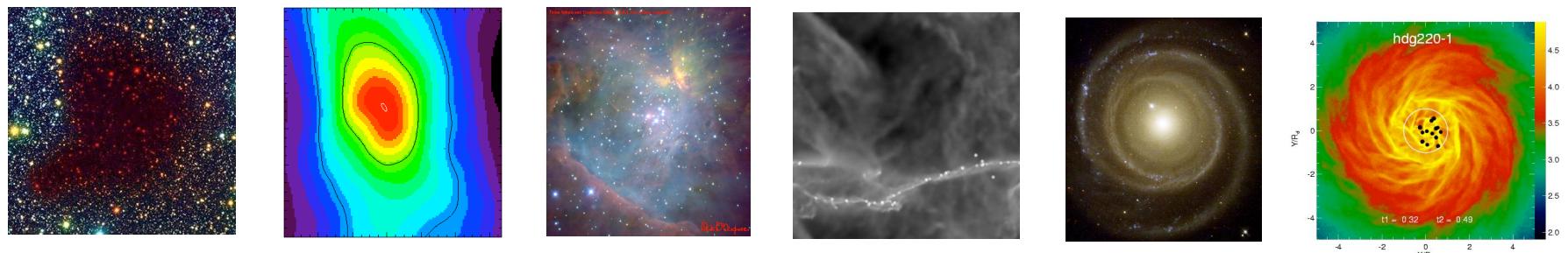


# Star Formation



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Institut für Theoretische Astrophysik



# Agenda

- phenomenology
  - Orion
  - Taurus
- interplay between gravity and turbulence
- examples and predictions
  - star cluster formation: dynamics
  - star cluster formation: thermodynamics
  - > stellar initial mass function

phenomenology

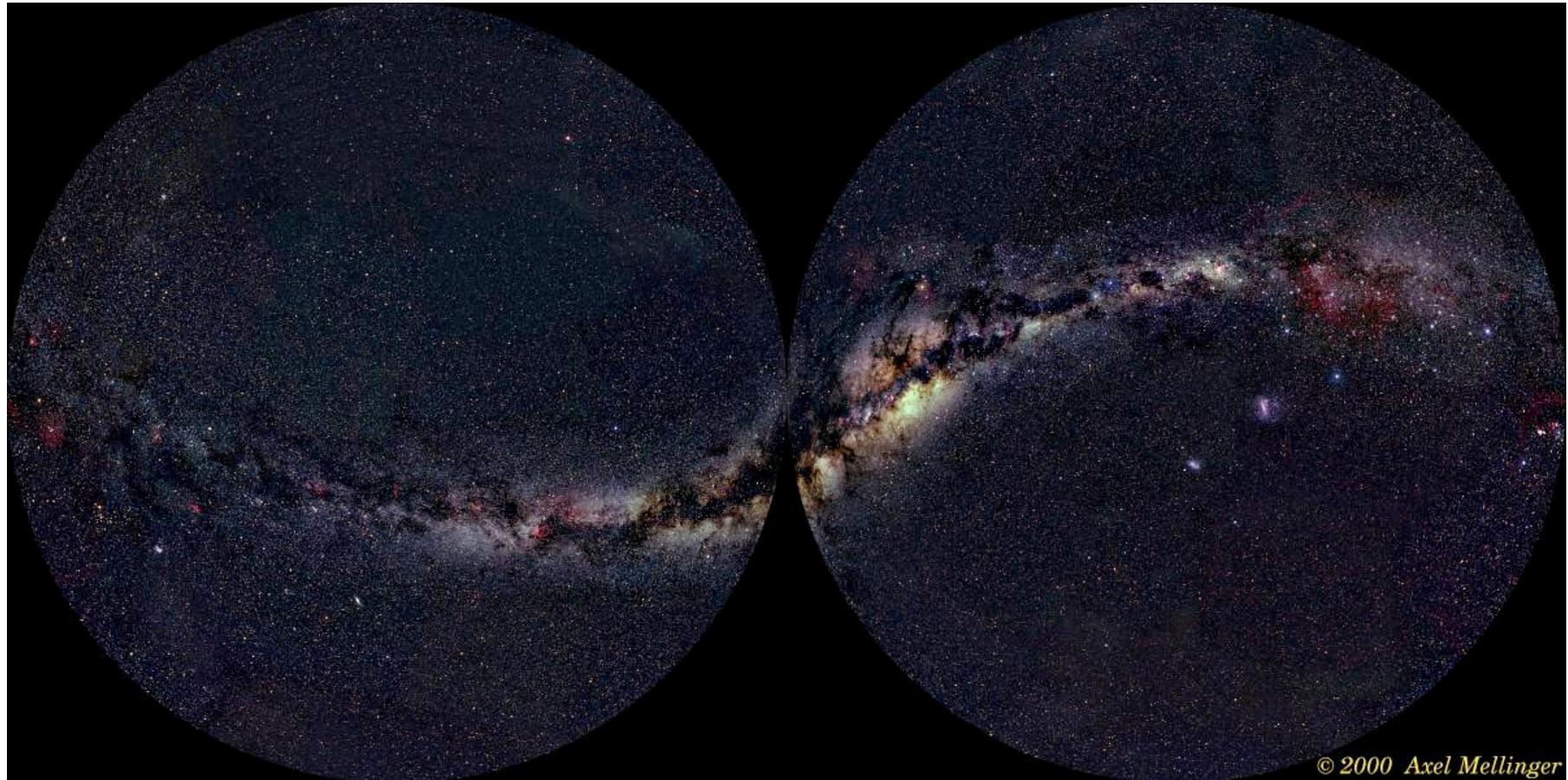
# young stars in spiral galaxies



(NGC 4622 from the Hubble Heritage Team)

- Star formation *always* is associated with *clouds of gas and dust.*
- Star formation is essentially a *local phenomenon* (on ~pc scale)
- **HOW** is star formation influenced by *global* properties of the galaxy?

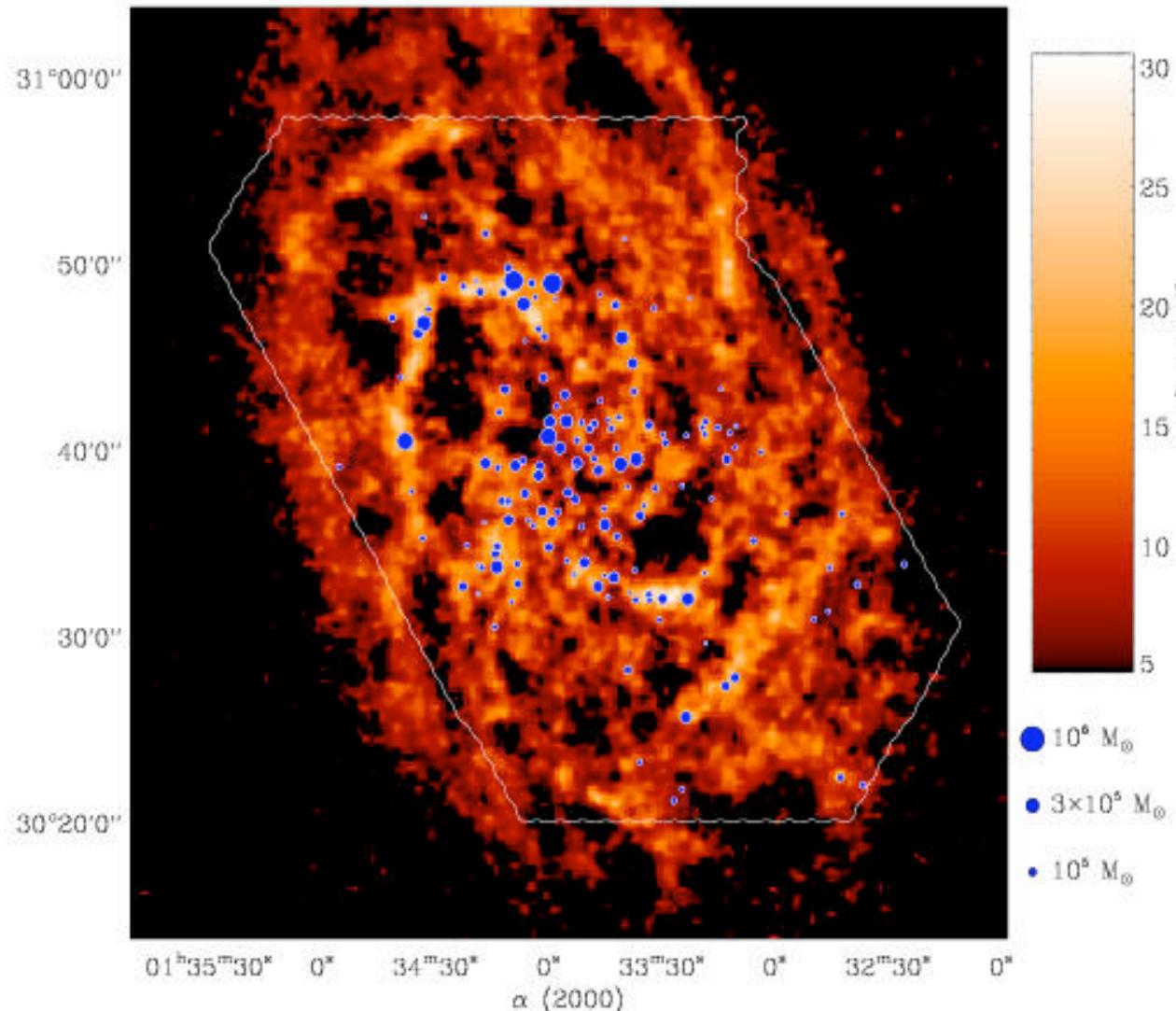
# young stars in the Milky Way



© 2000 Axel Mellinger

On the night sky, you see **stars** and **dark clouds**:  
The brightest stars are massive and therefore young.  
→ Star formation is important for understanding the structure of our Galaxy

# correlation between H<sub>2</sub> and HI

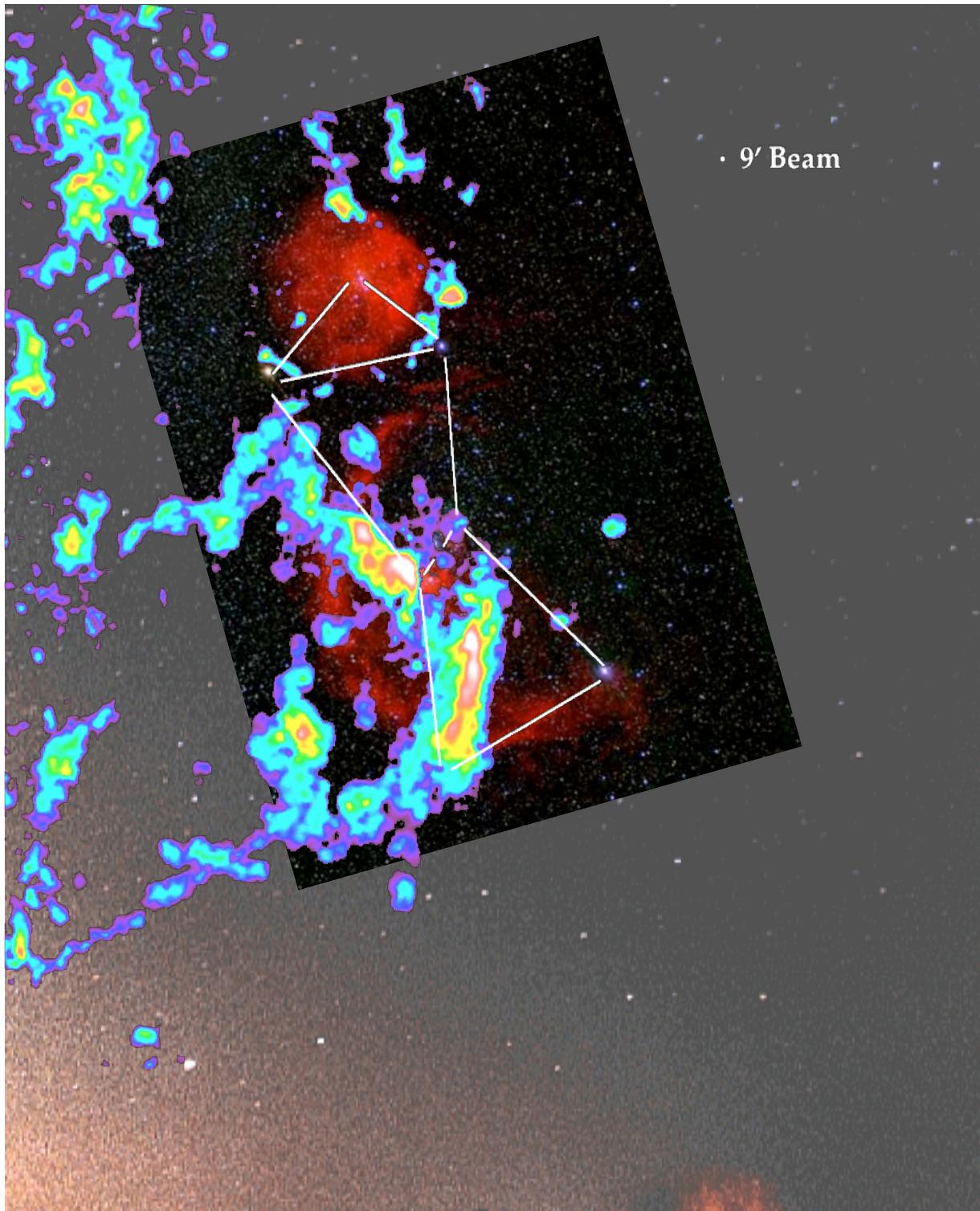


Compare H<sub>2</sub> - HI  
in M33:

- H<sub>2</sub>: BIMA-SONG Survey, see Blitz et al.
- HI: Observations with Westerbork Radio T.

H<sub>2</sub> clouds are seen in regions of high HI density  
(in spiral arms and filaments)

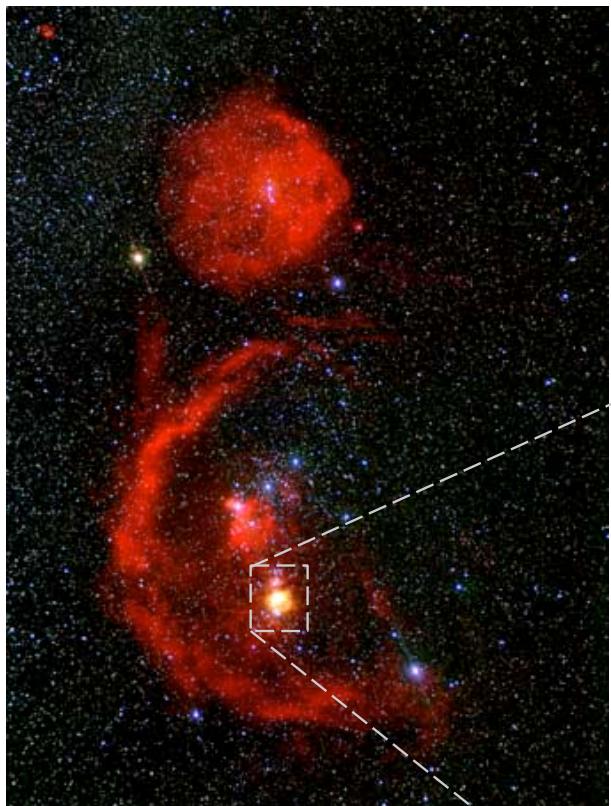
# Star formation in Orion



We see

- Stars (in visible light)
- Atomic hydrogen (in  $\text{H}\alpha$  -- red)
- Molecular hydrogen  $\text{H}_2$  (radio emission -- color coded)

# Local star forming region: The Trapezium Cluster in Orion



Orion molecular cloud

The Orion molecular cloud is the birth- place of several young embedded star clusters.

The Trapezium cluster is only visible in the IR and contains about 2000 newly born stars.



Trapezium  
cluster

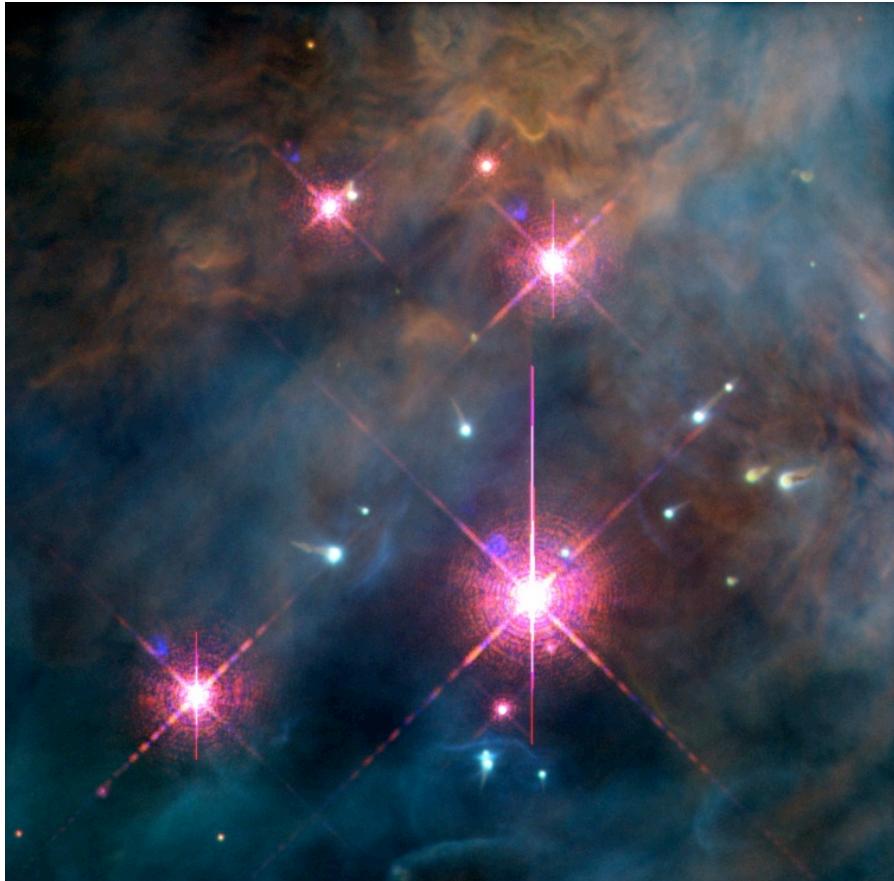


## Trapezium Cluster (detail)

- stars form in **clusters**
- stars form in **molecular clouds**
- (proto)stellar **feedback** is important

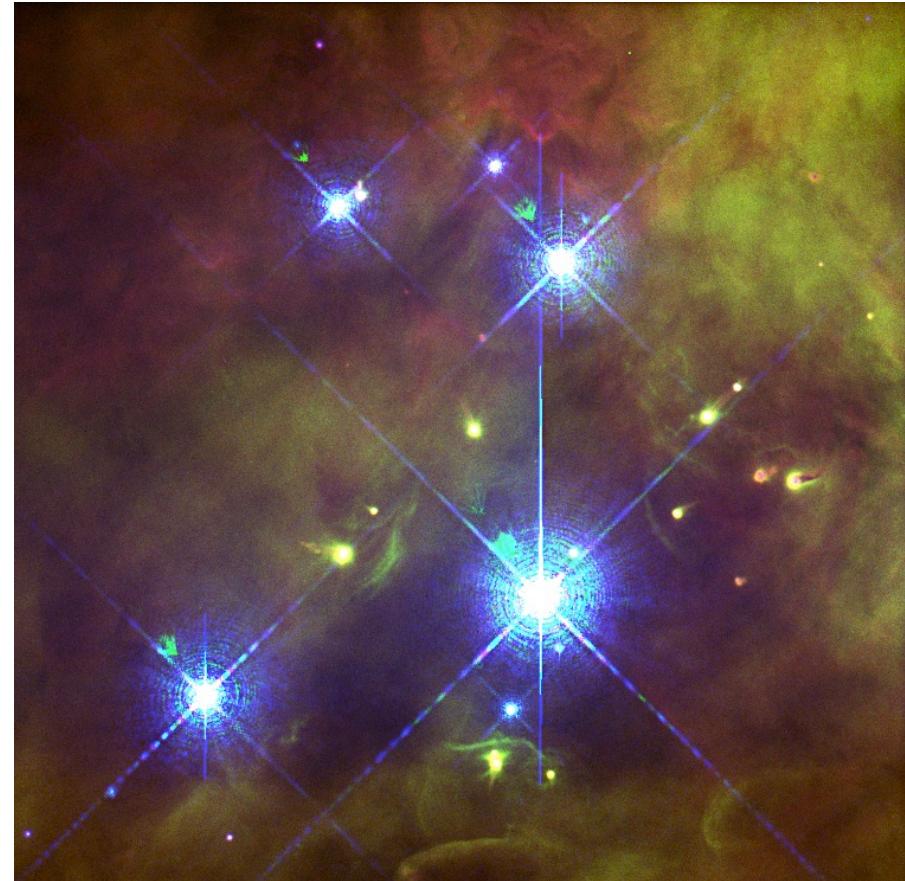
(color composite J,H,K  
by M. McCaughean,  
VLT, Paranal, Chile)

# Trapezium Cluster: Central Region



Ionizing radiation from central star  
**Θ1C Orionis**

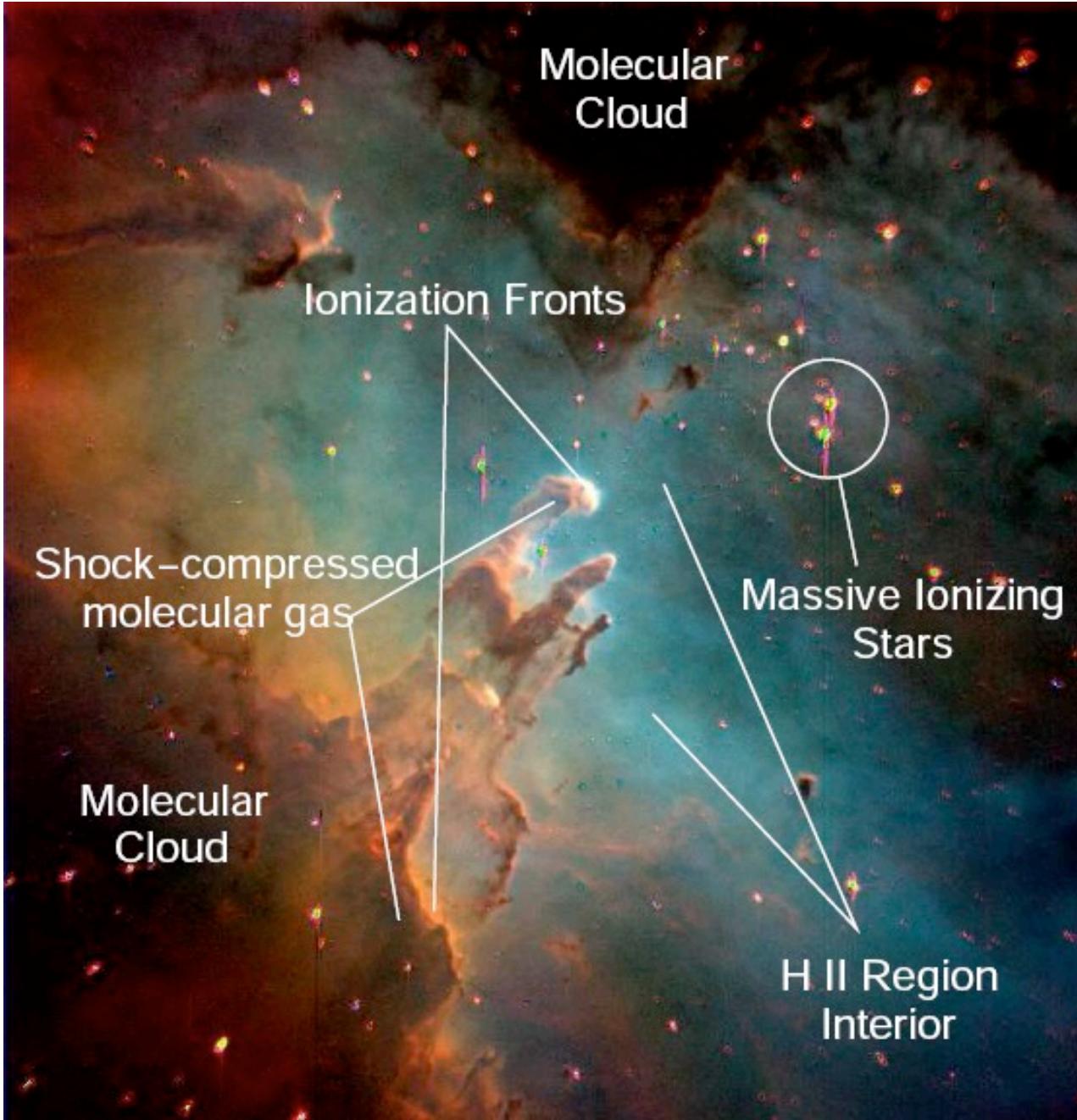
(images: Doug Johnstone et al.)

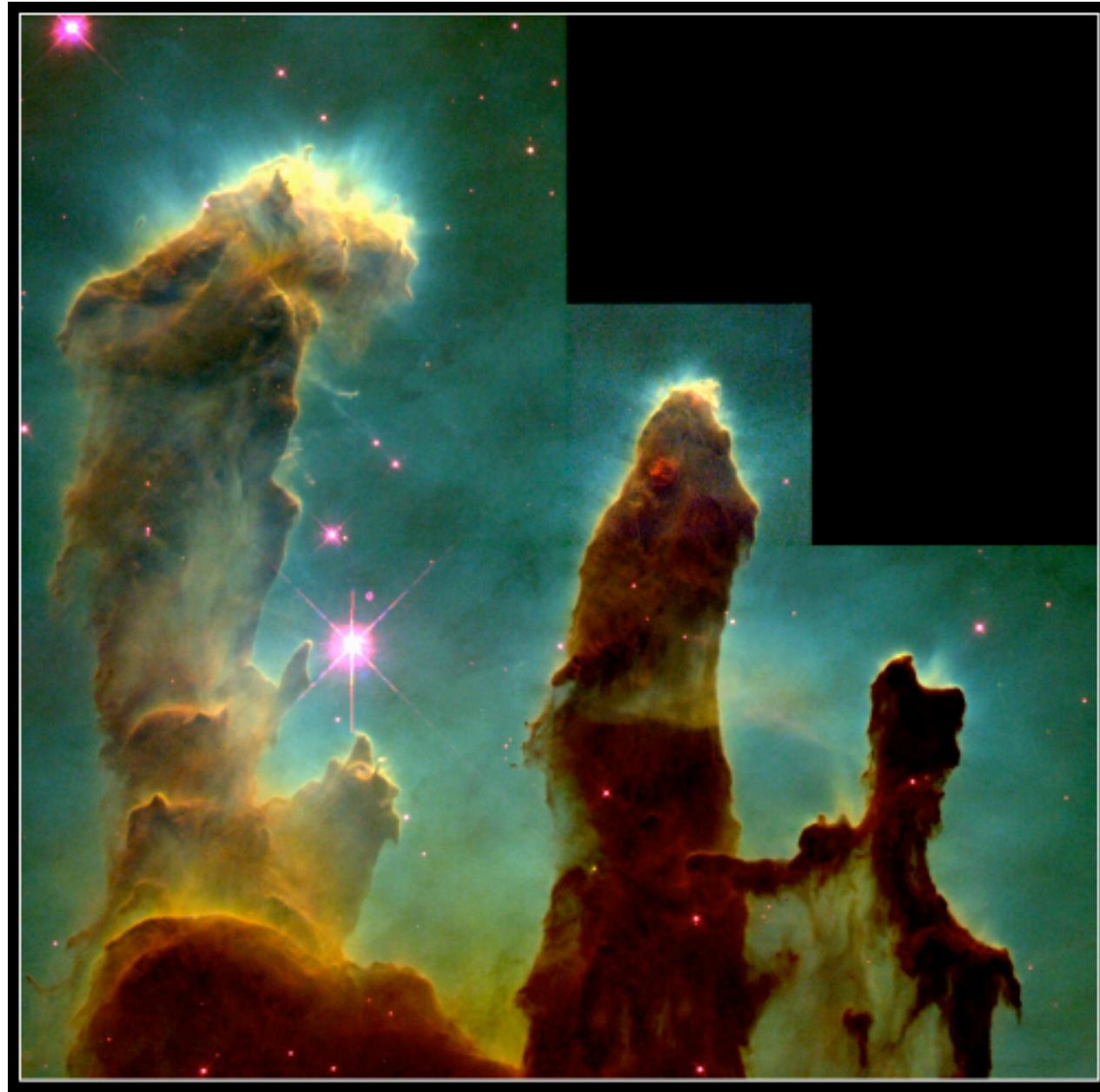


**Proplyds:** Evaporating ``protoplanetary'' disks  
around young low-mass protostars

Ralf Klessen: Cardiff, 25.02.2008

alles in einem Bild



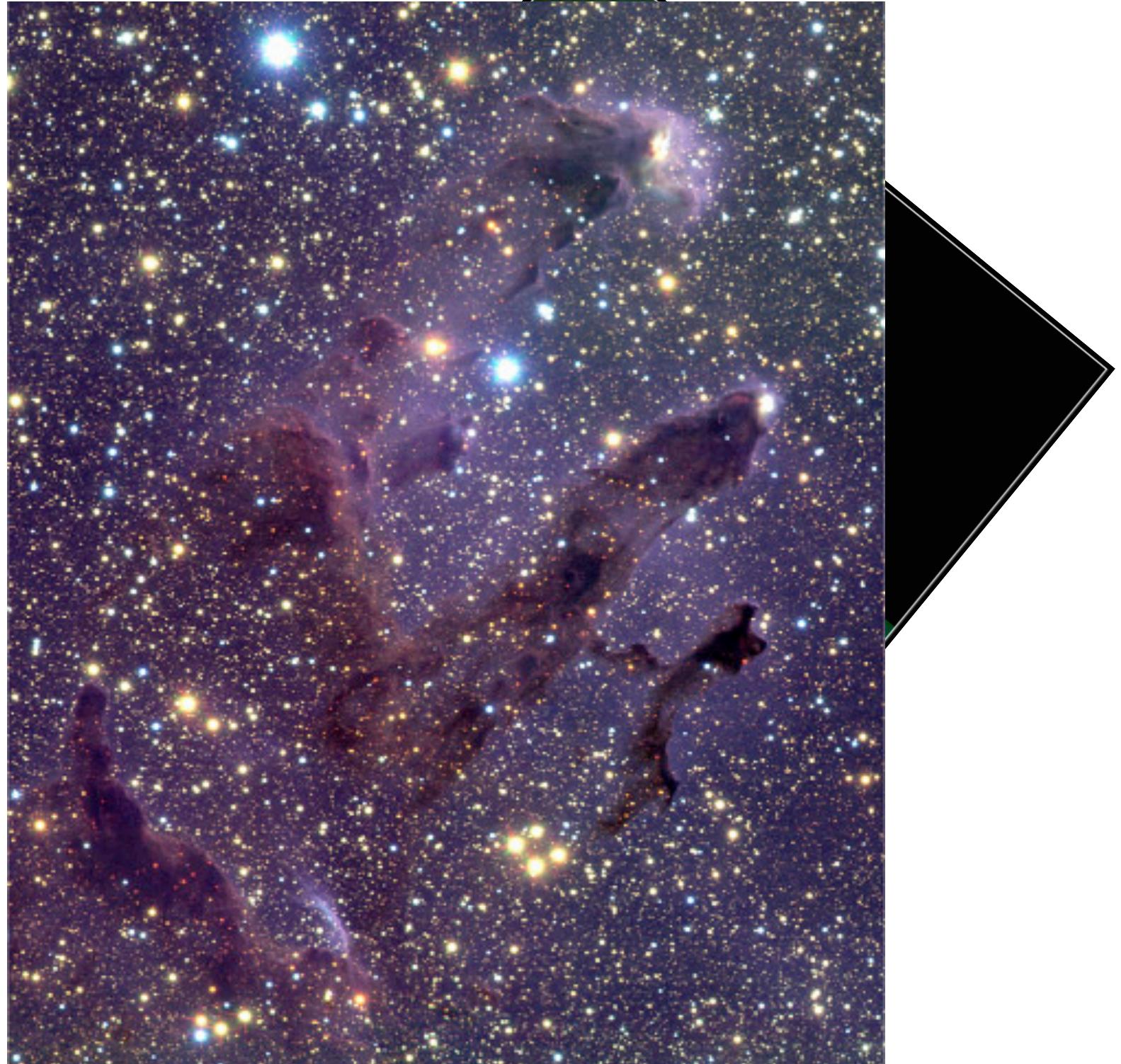


HST Aufnahme

*Pillars of God* (in Eagle Nebula): Formation of small groups of young stars in the tips of the columns of gas and dust ....

Ralf Klessen: Cardiff, 25.02.2008

Infrared  
observation





*Pillars of God* (in Eagle Nebula): Formation of small groups of young stars in the tips of the columns of gas and dust ....

IR observation with ESO-VLT



Head of Column No.2 in Eagle Nebula (IR-View)  
(VLT ANTU + ISAAC)

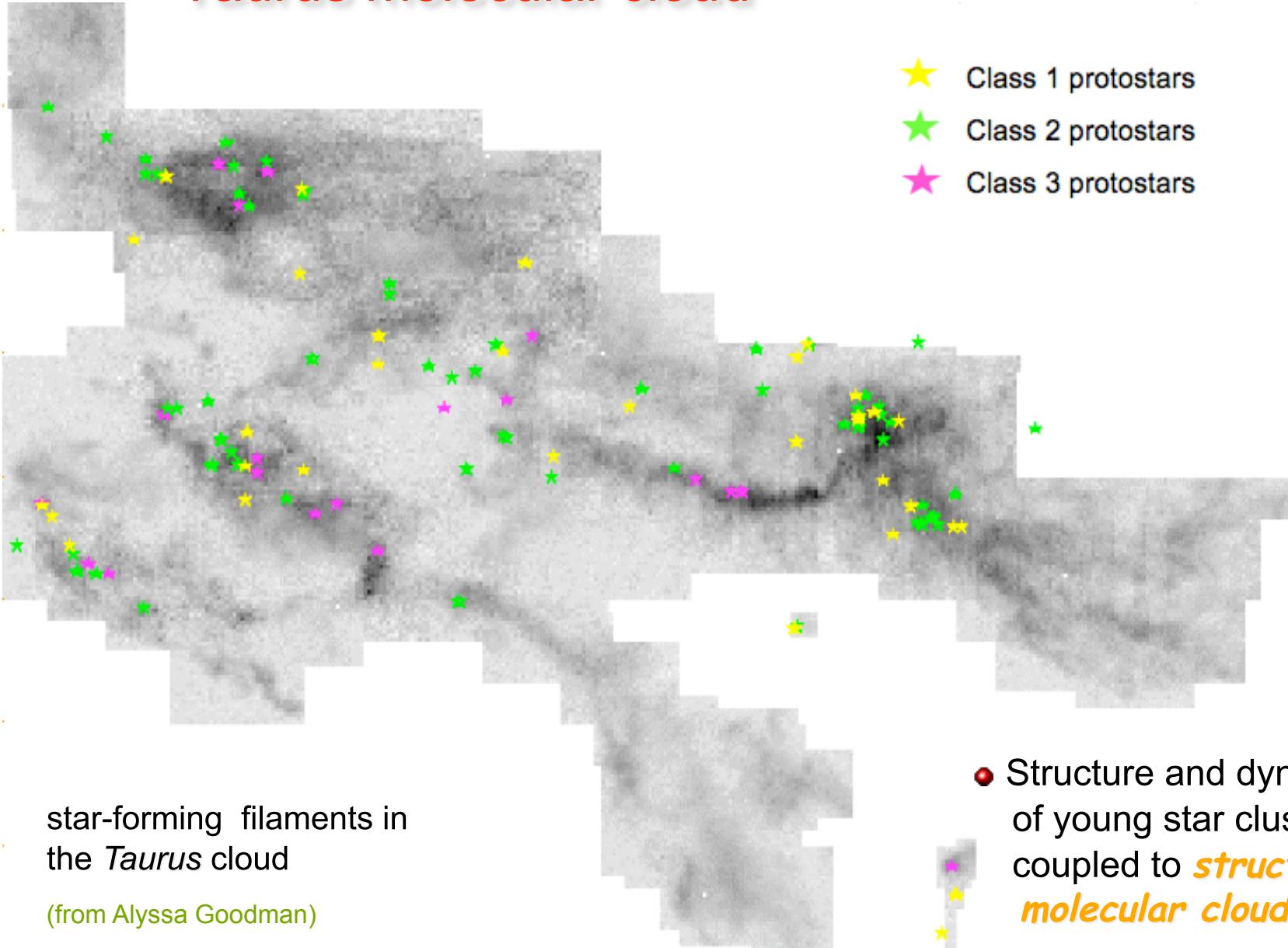
ESO PR Photo 37d/01 (30 December 2001)

© European Southern Observatory

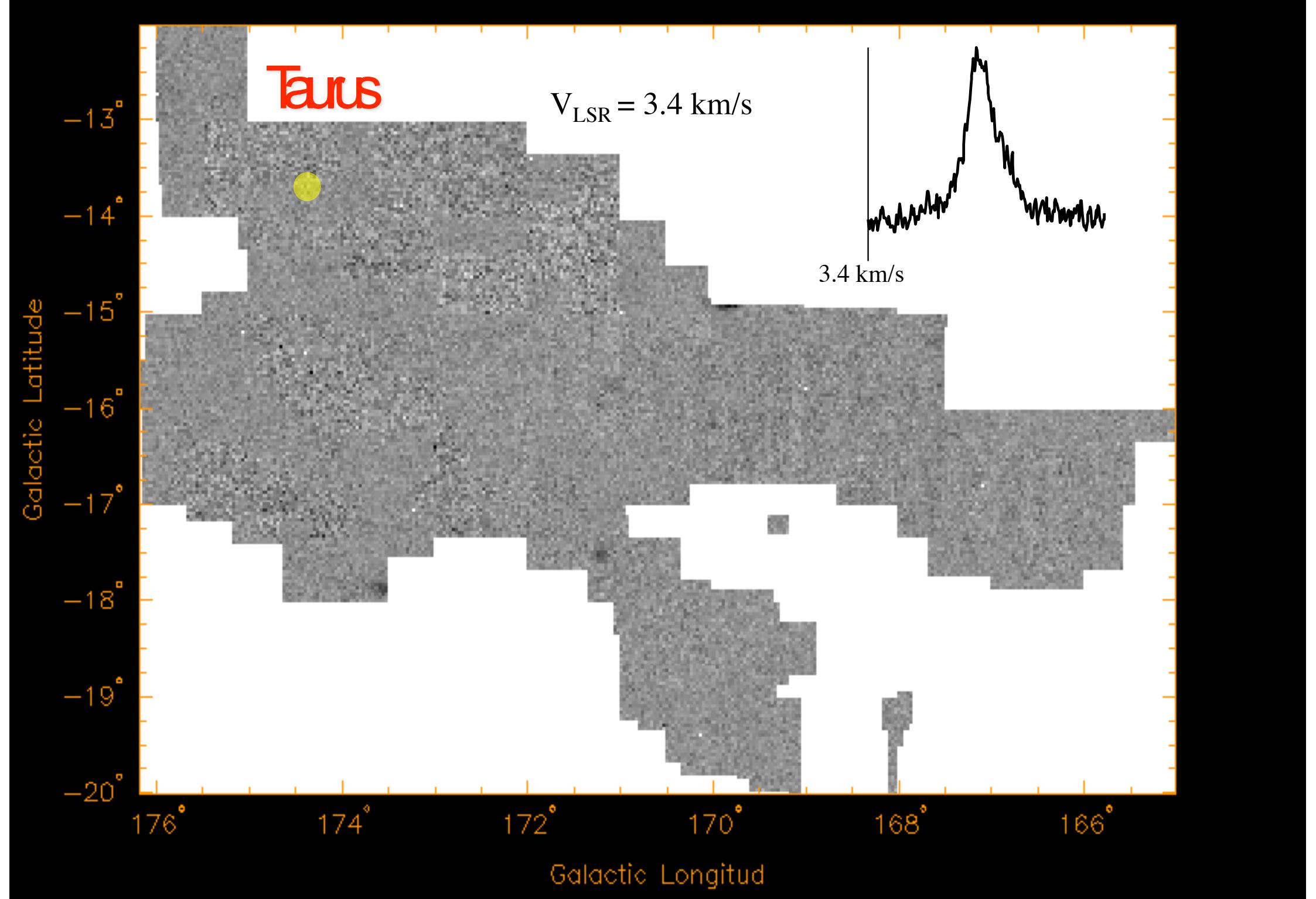


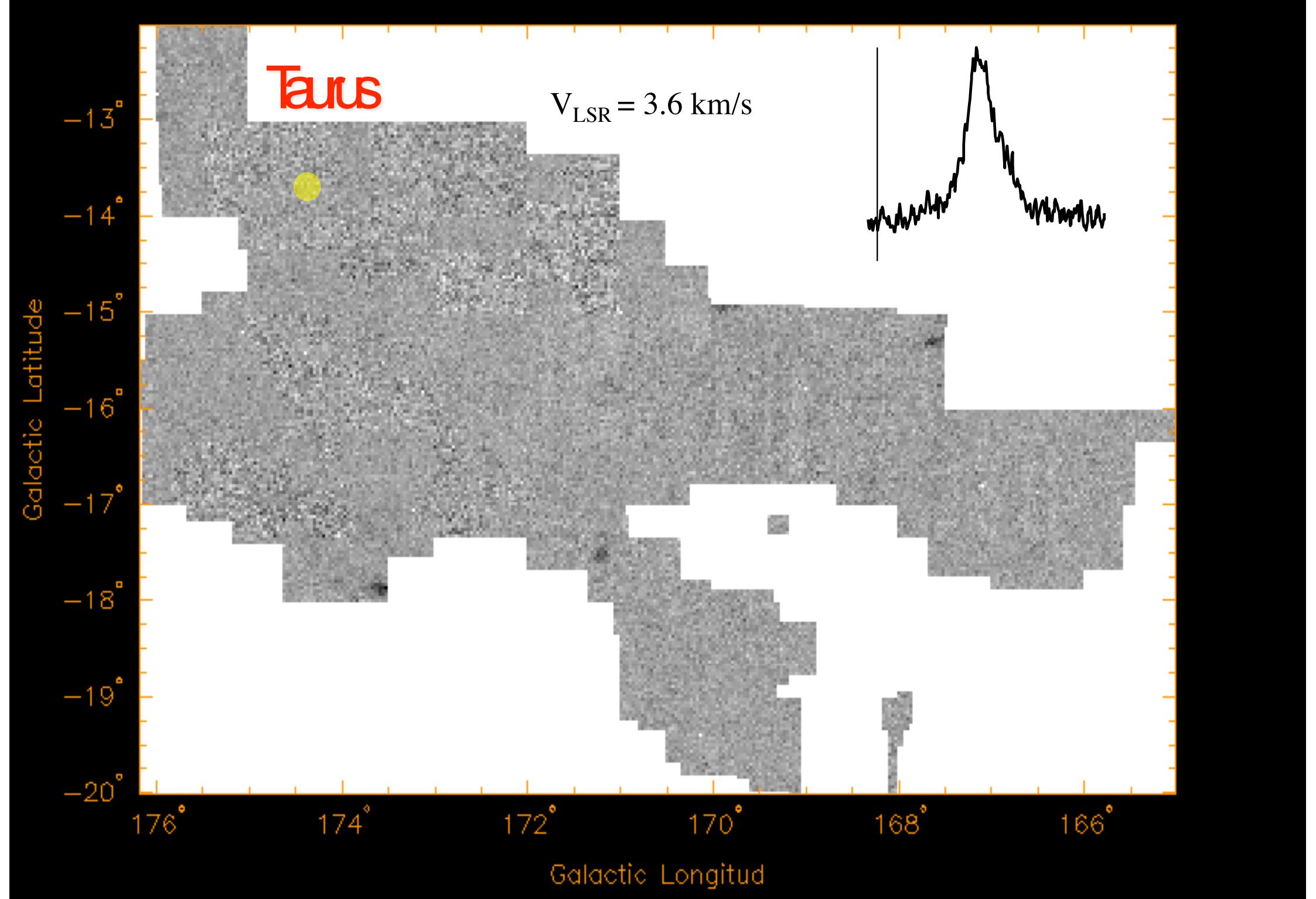
*Pillars of God (in Eagle Nebula): Formation of small groups of young stars in the tips of the columns of gas and dust ....*

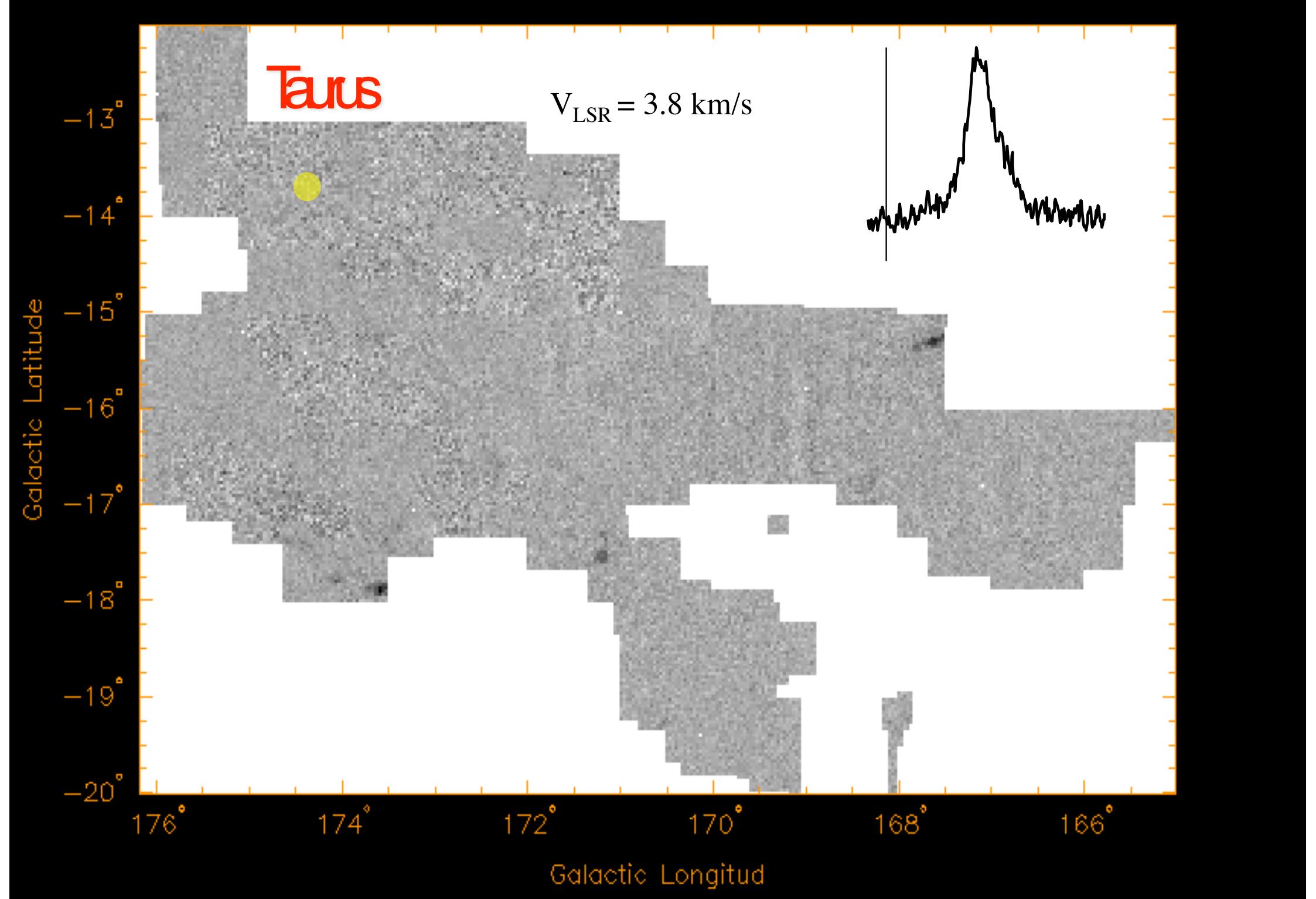
# Taurus molecular cloud

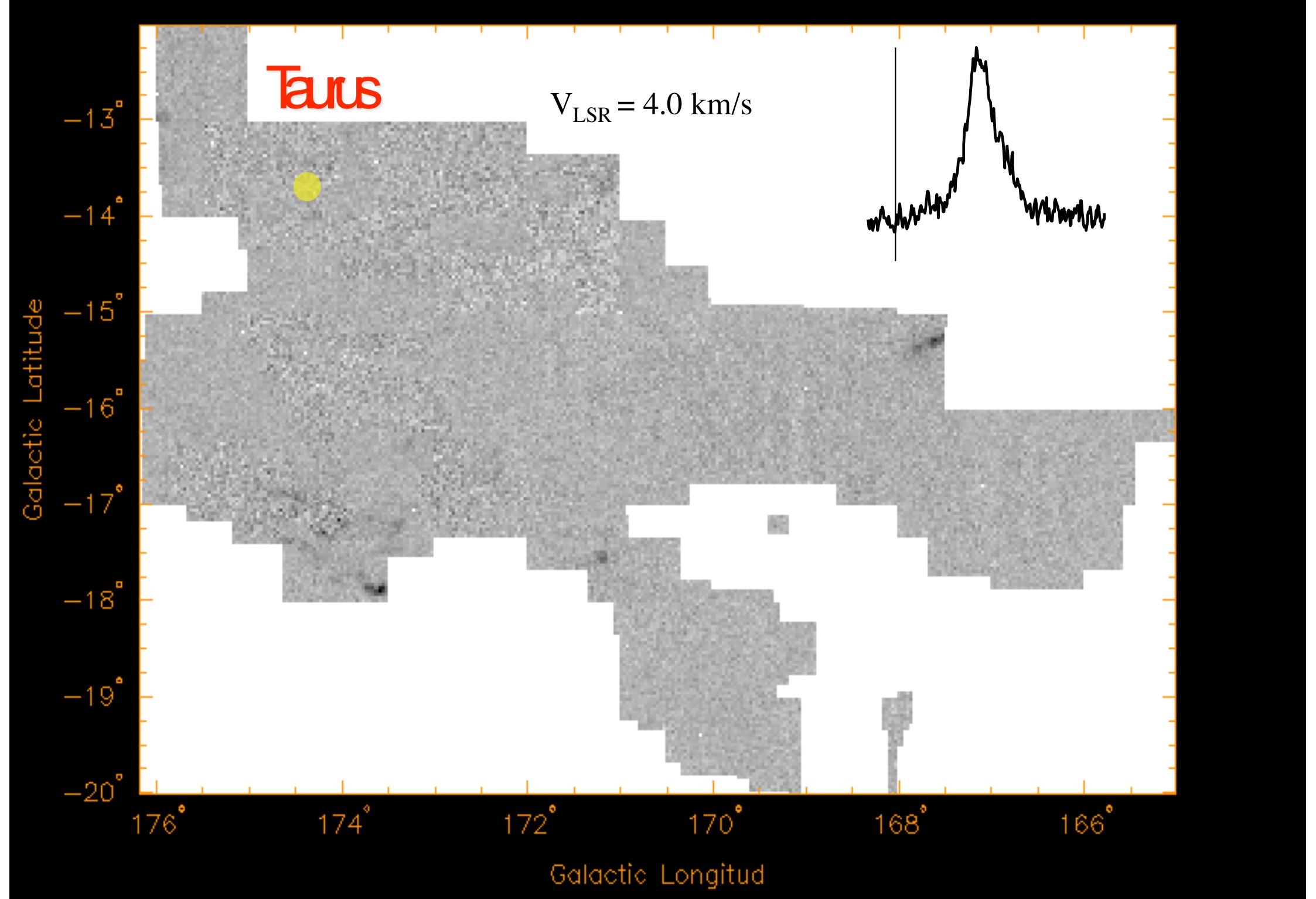


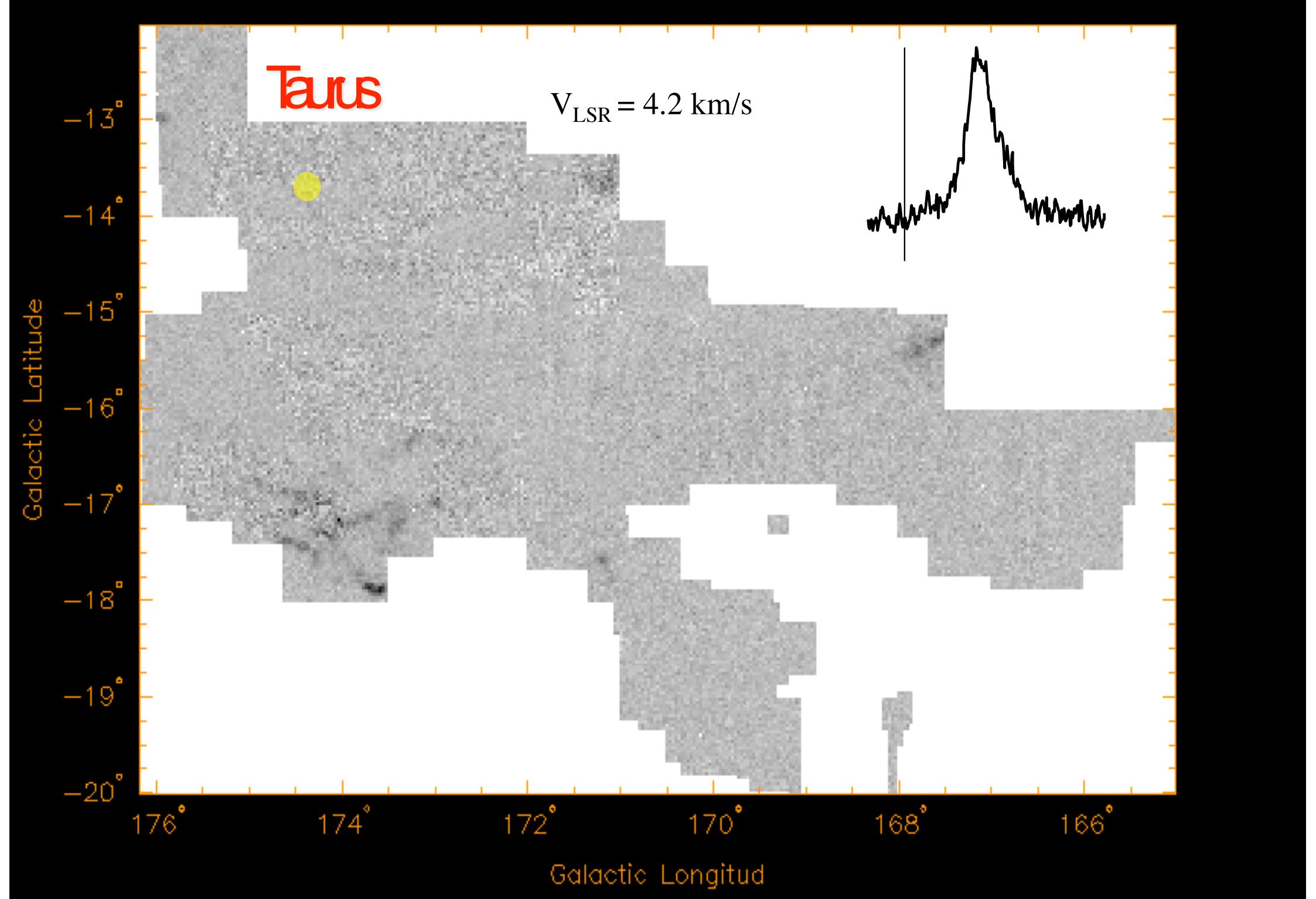
- Structure and dynamics of young star clusters is coupled to *structure of molecular cloud*

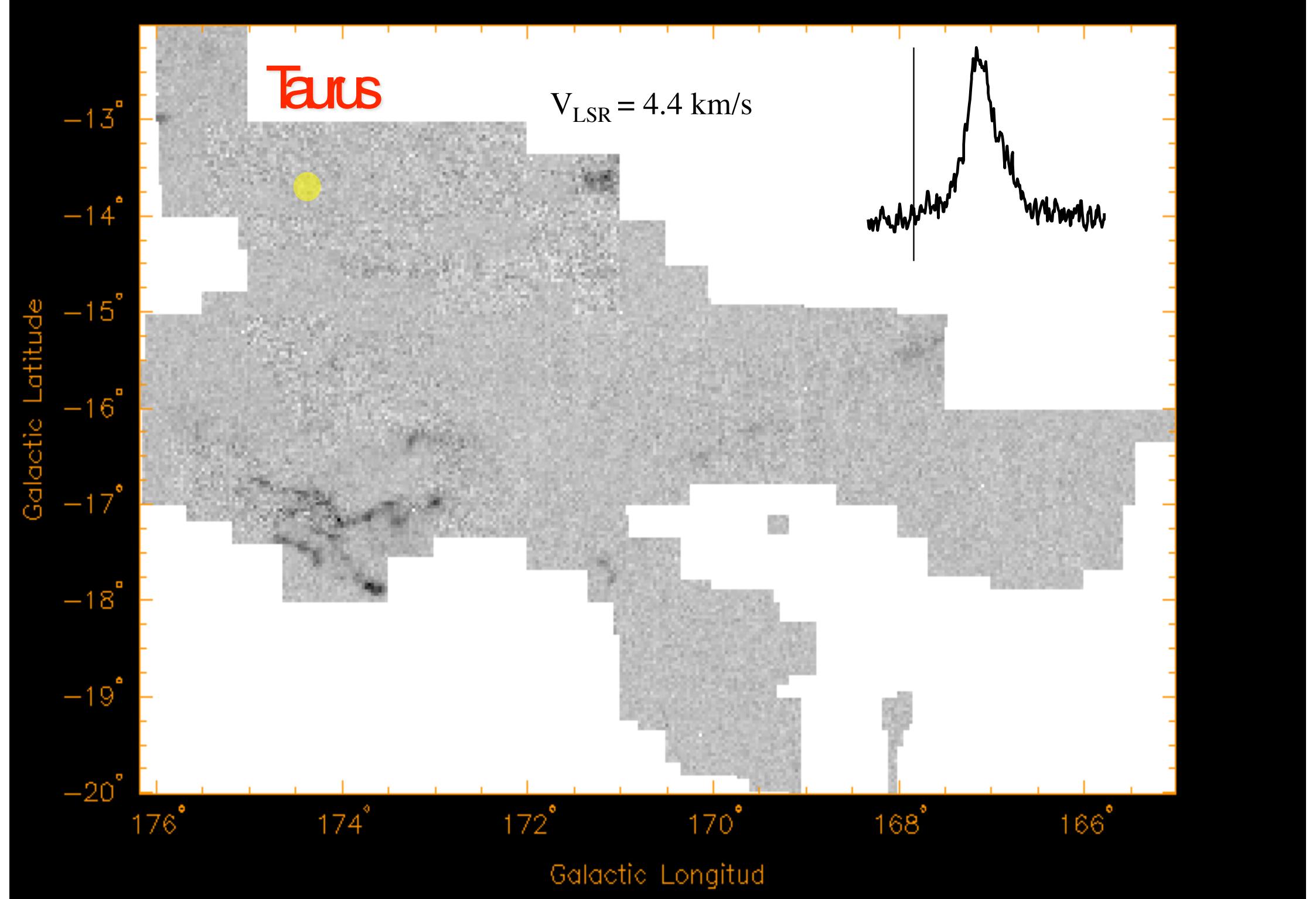


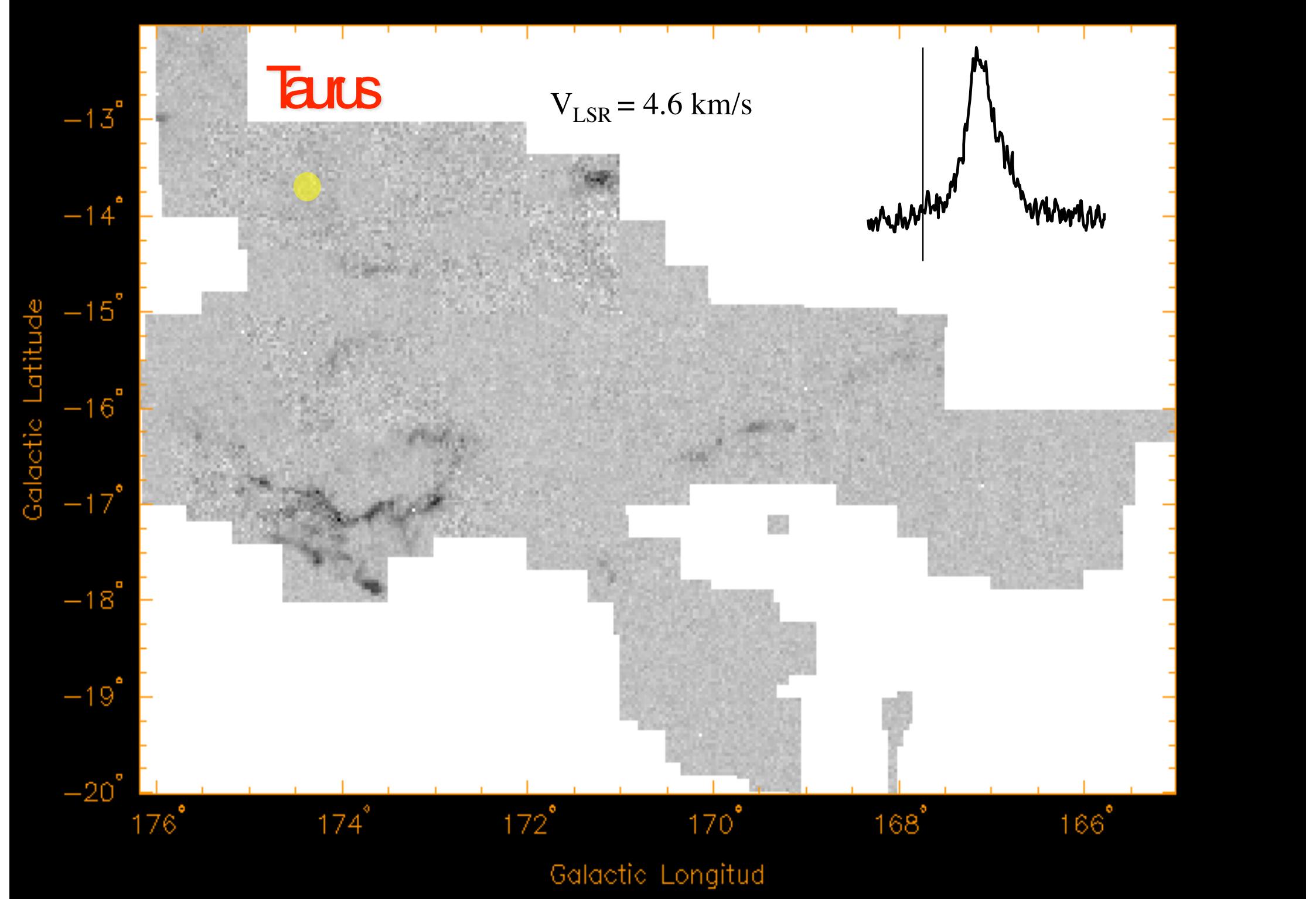


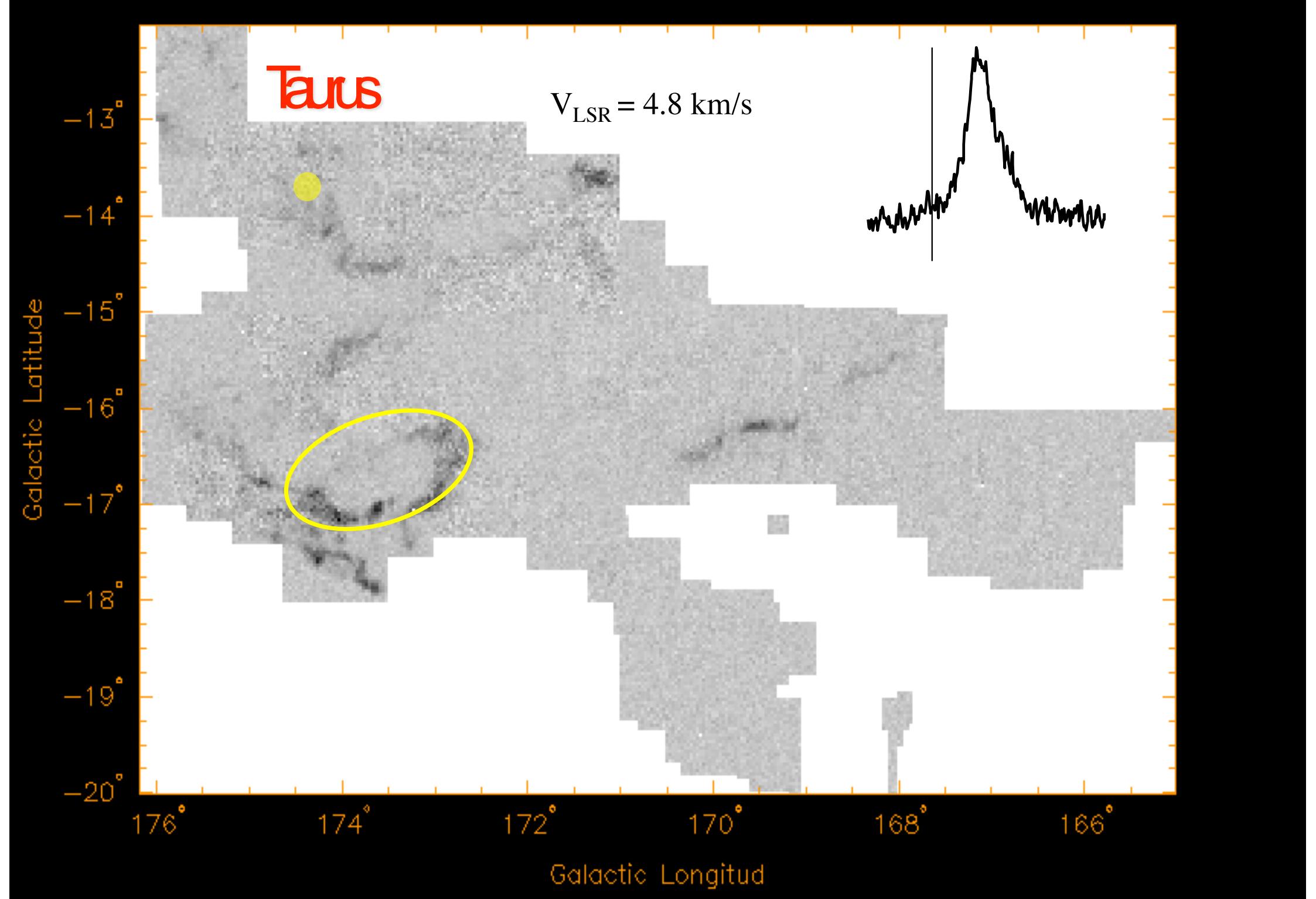


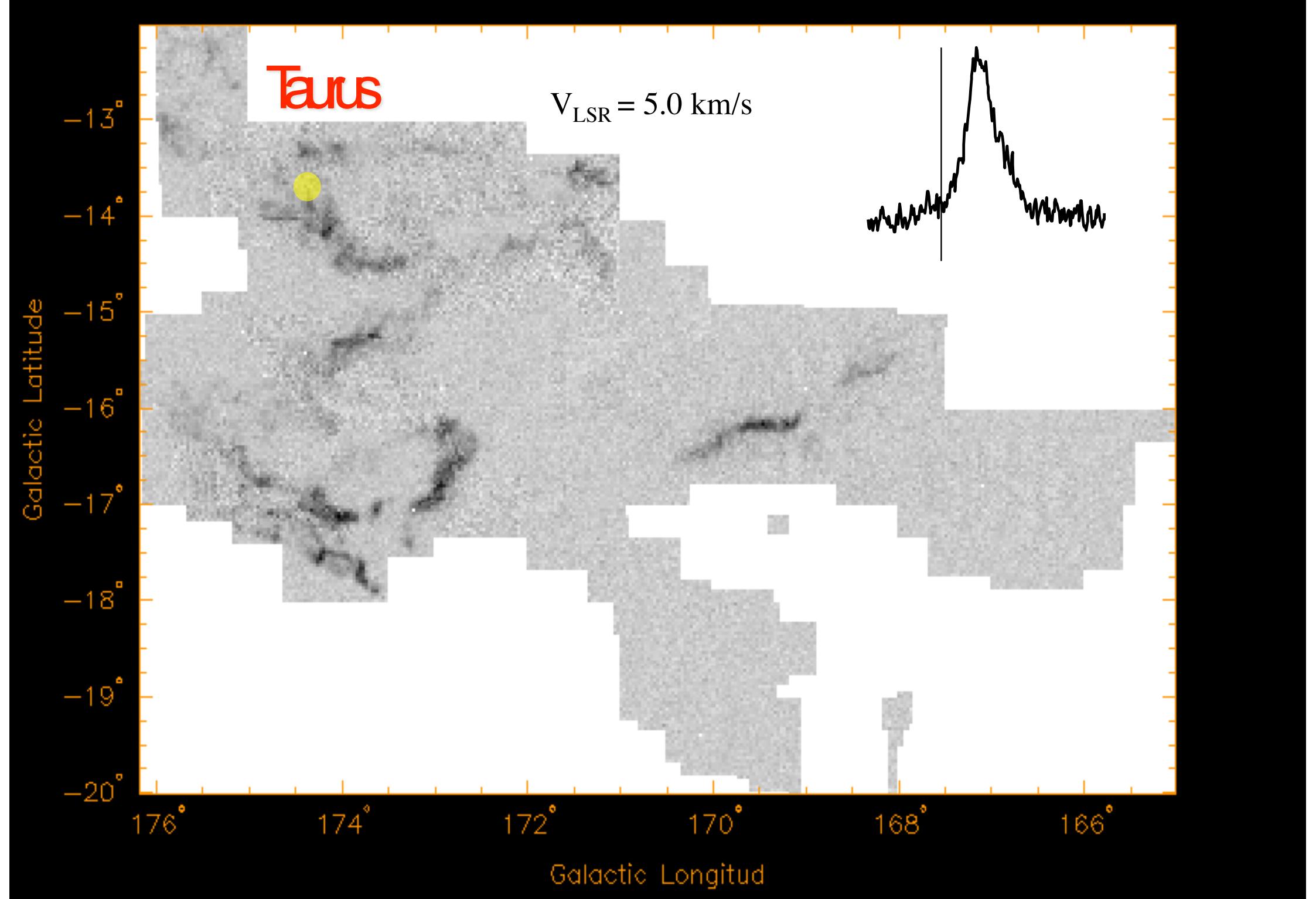


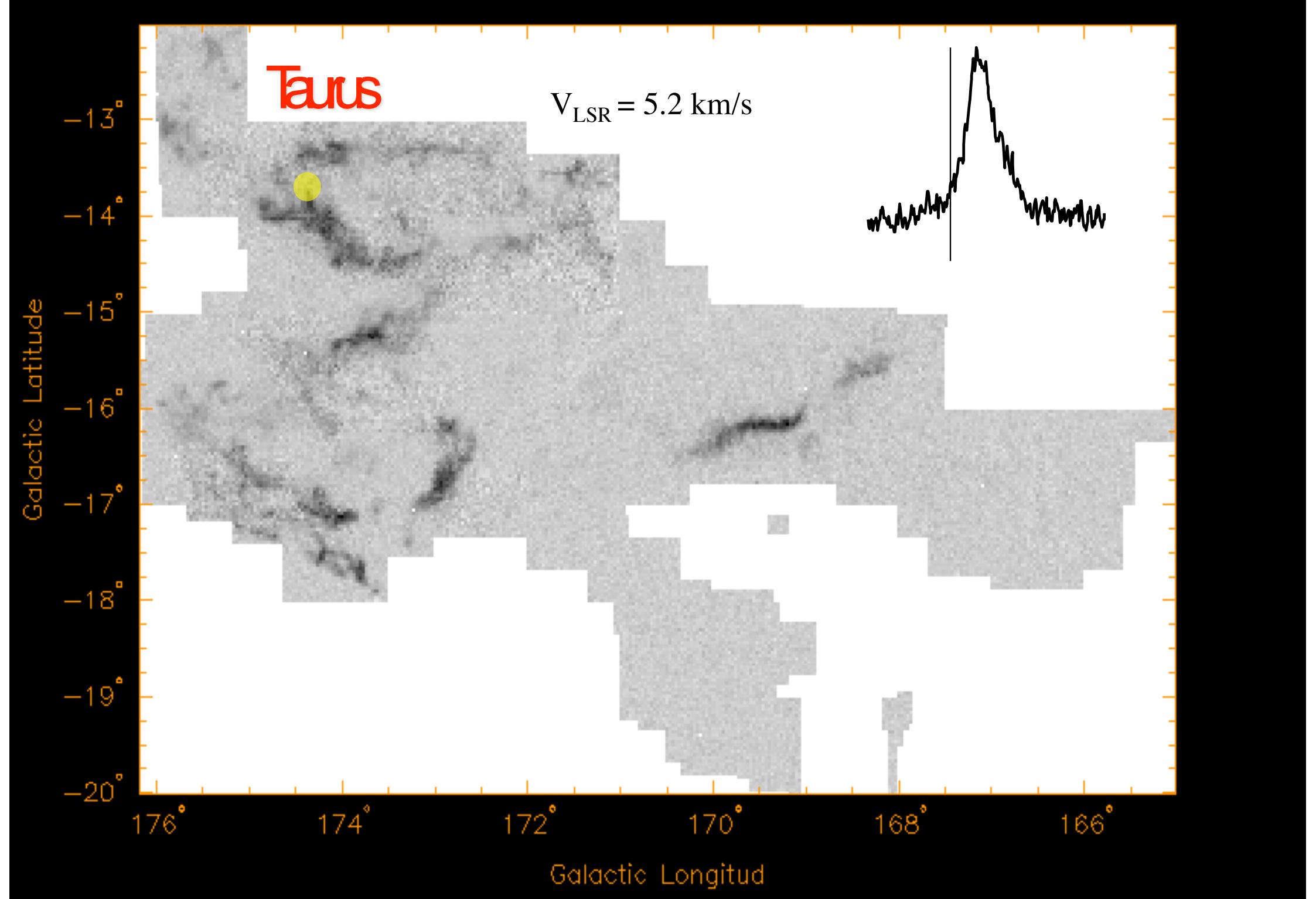


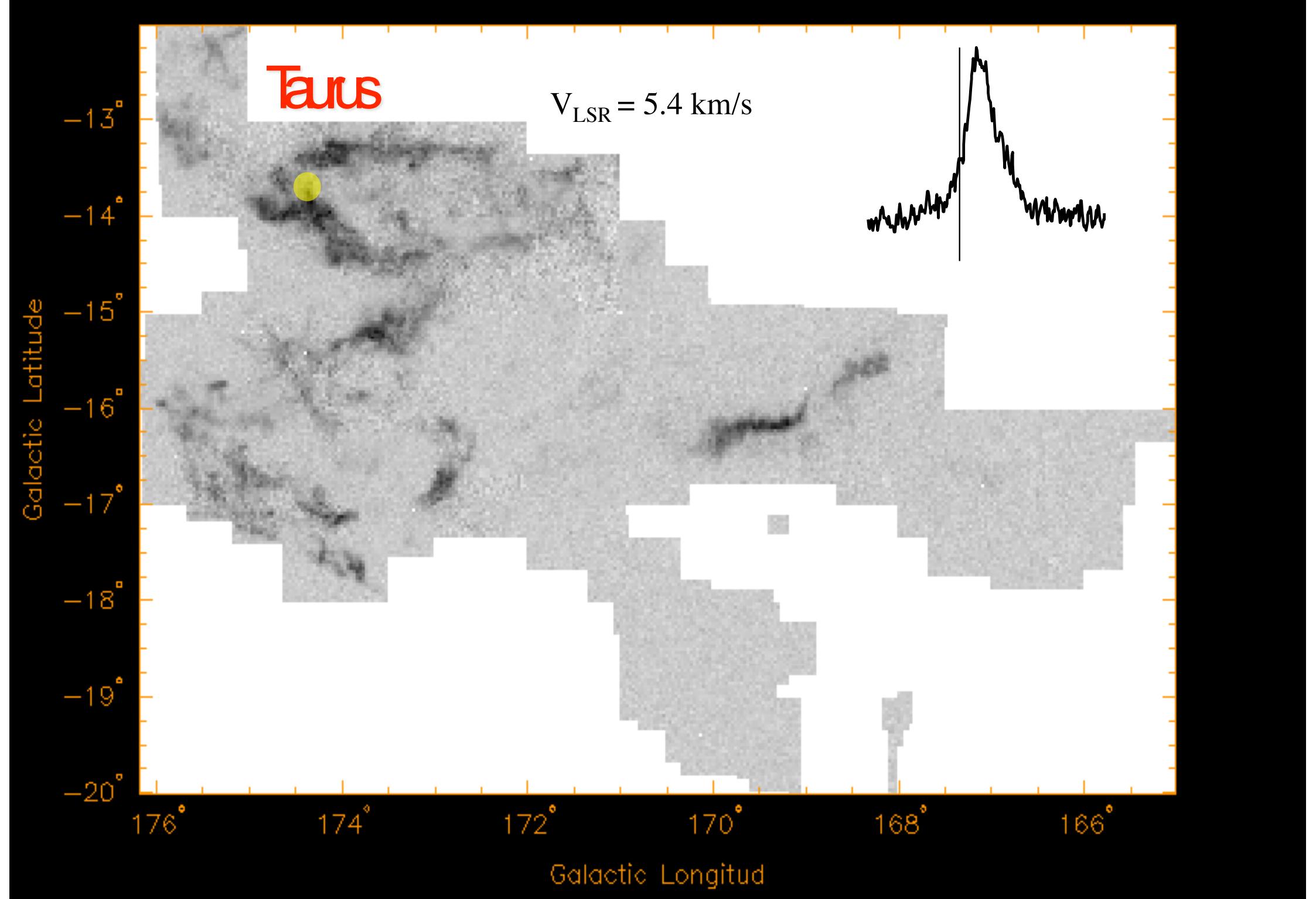


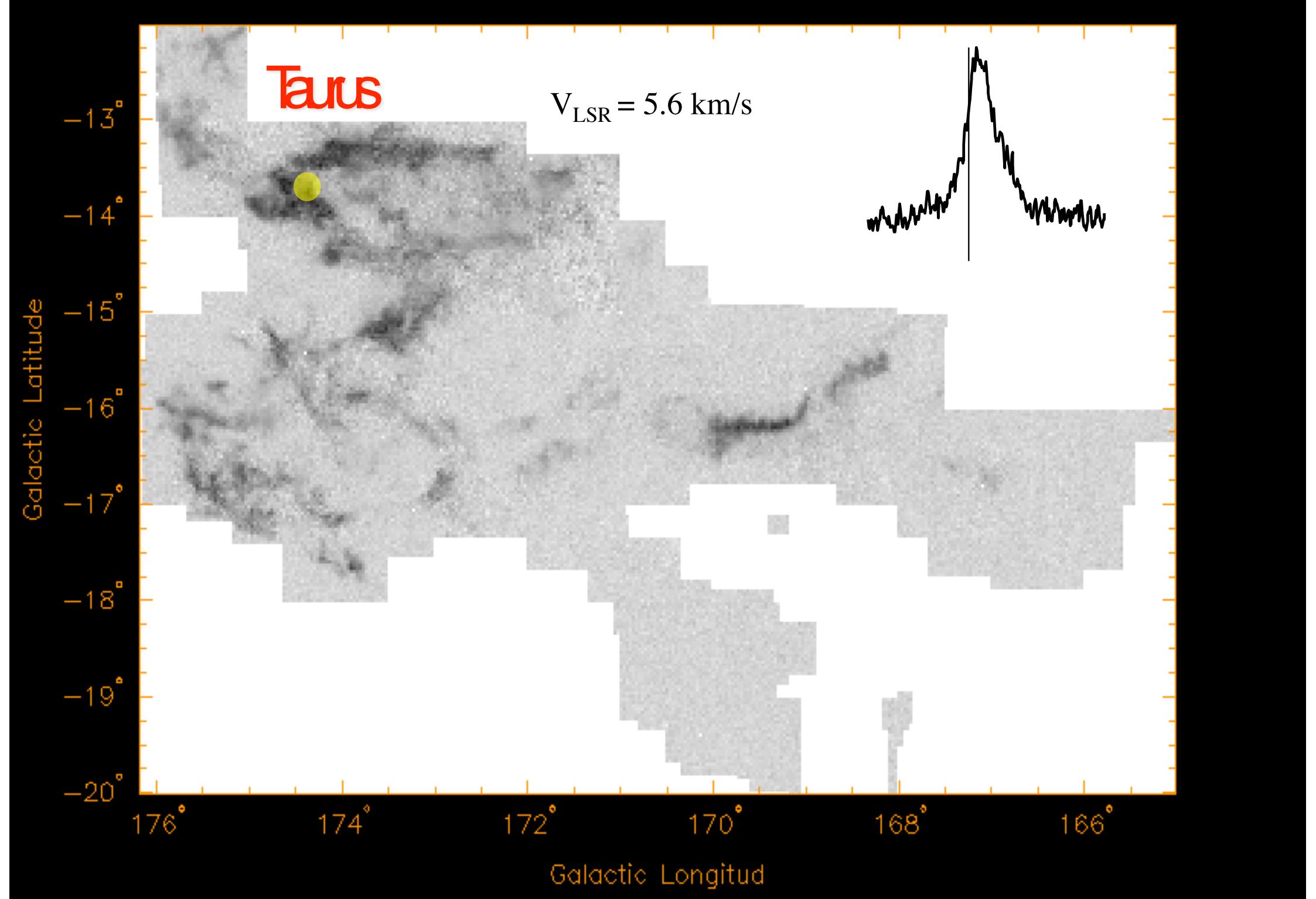


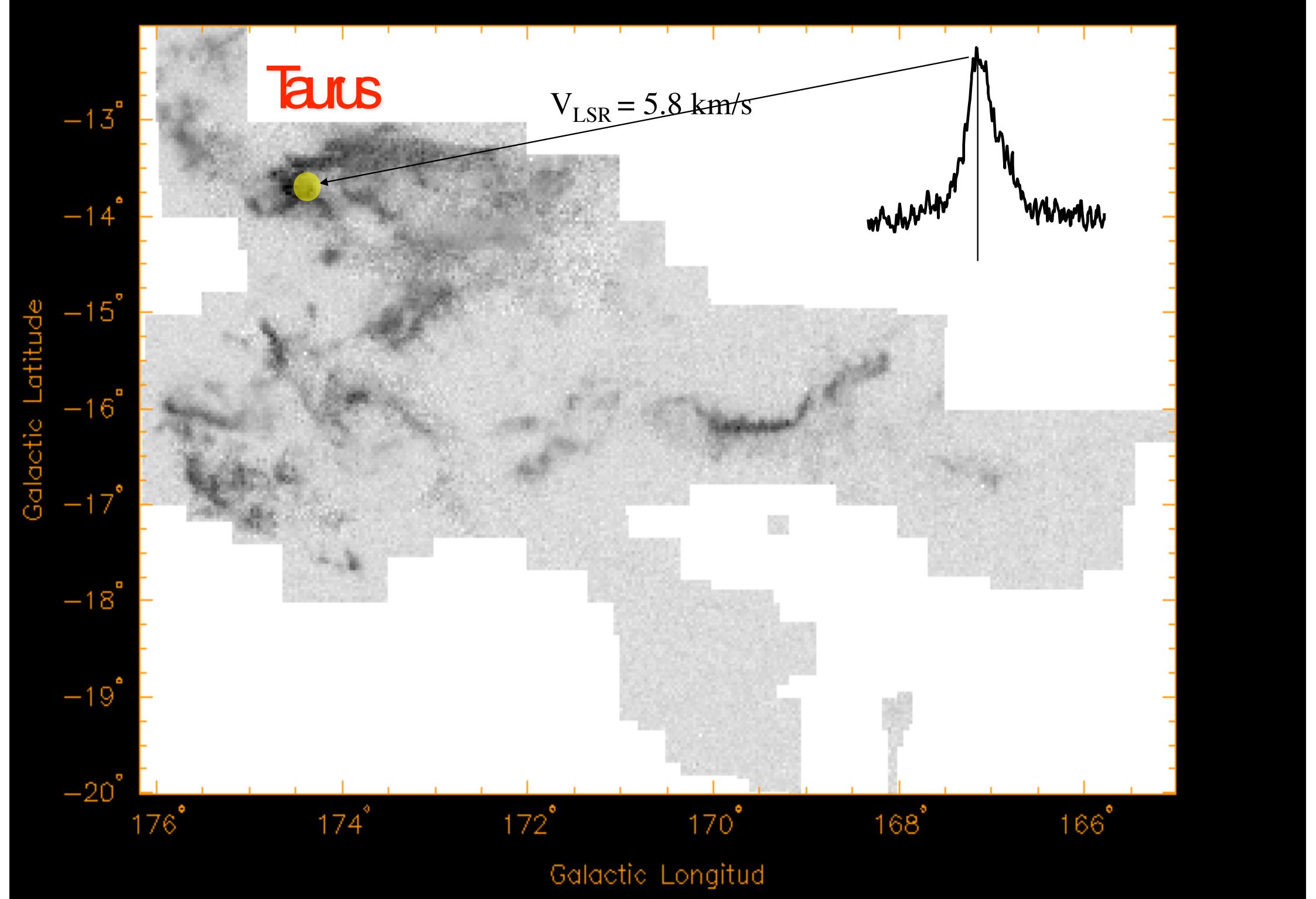


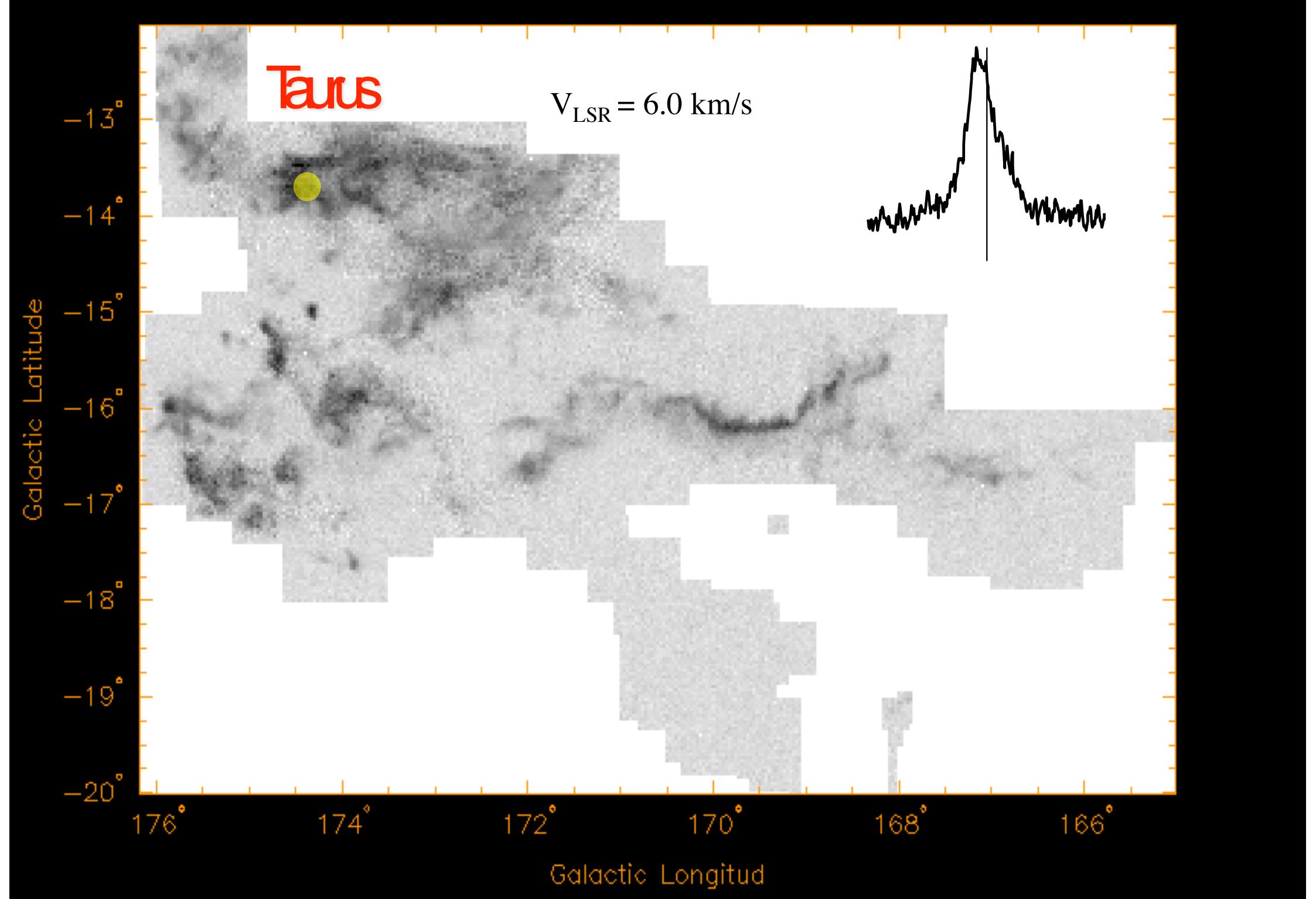


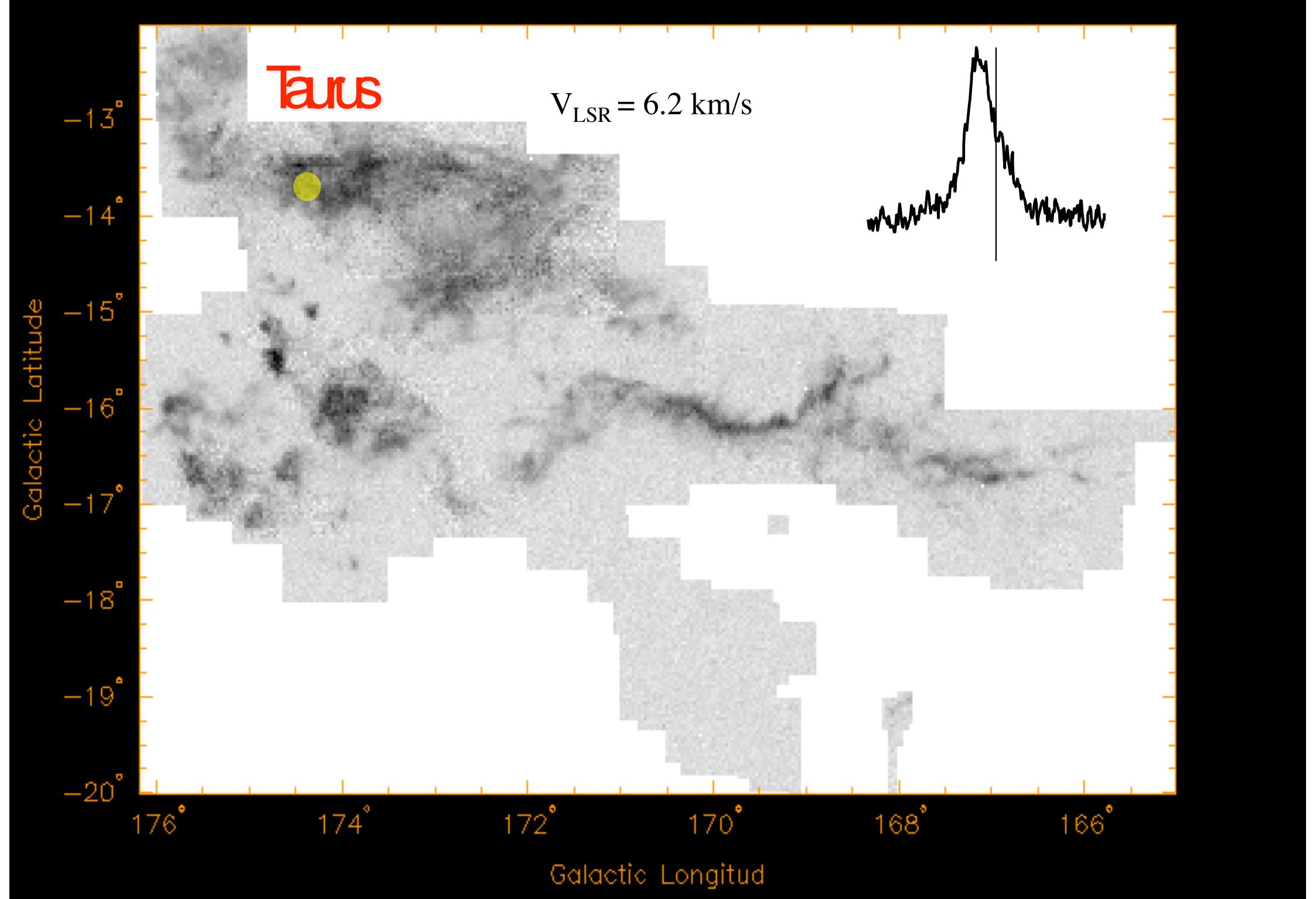


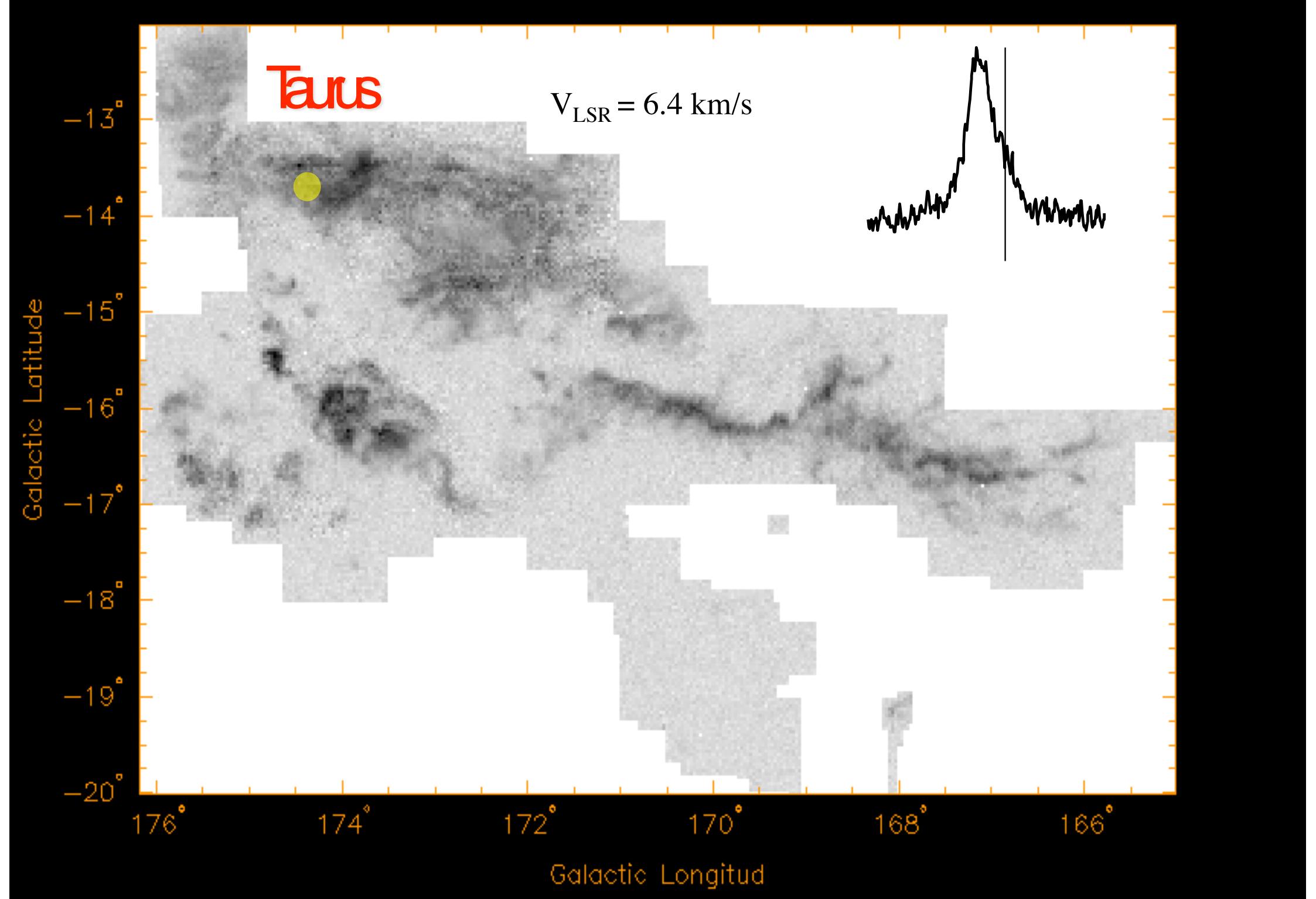


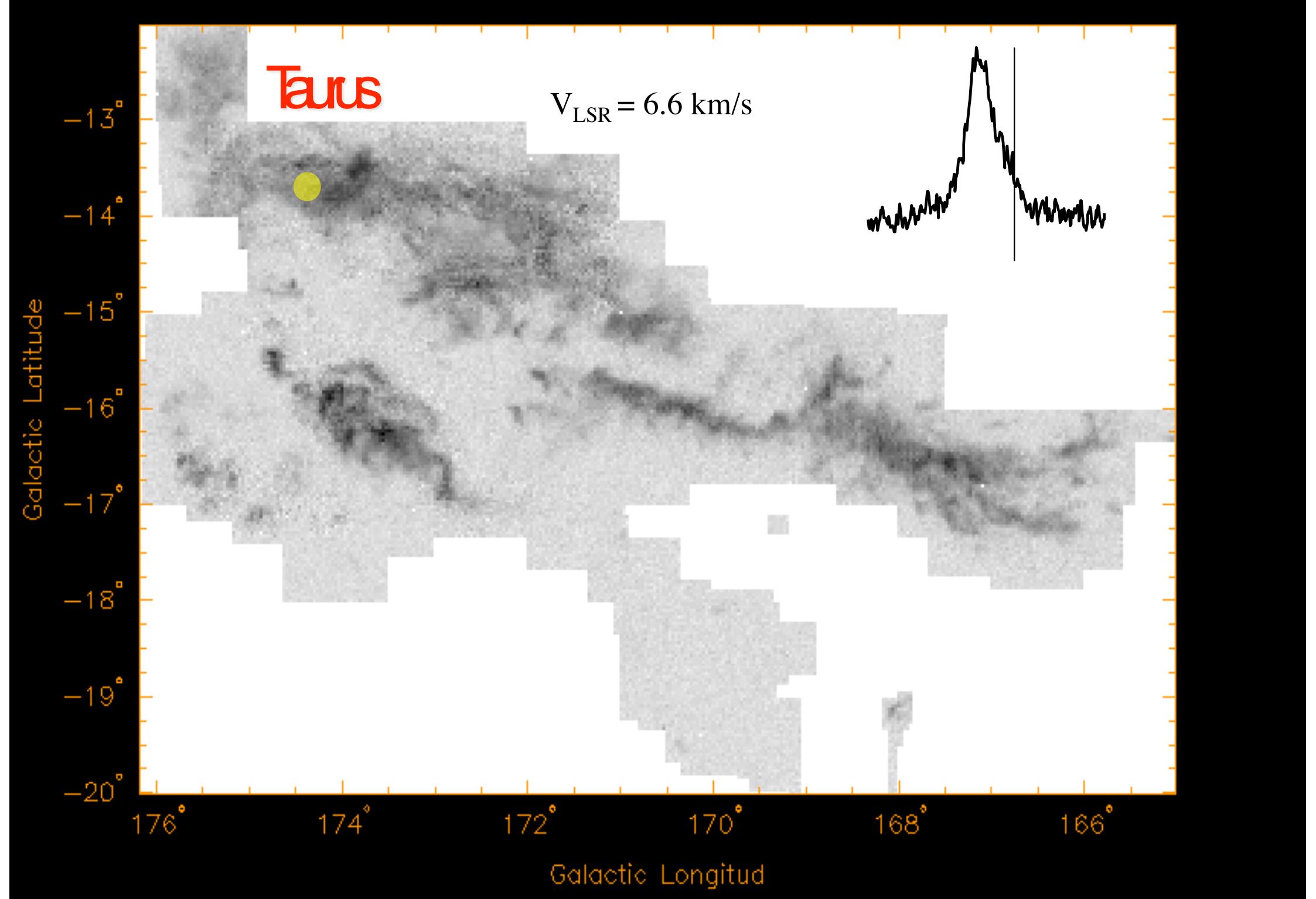


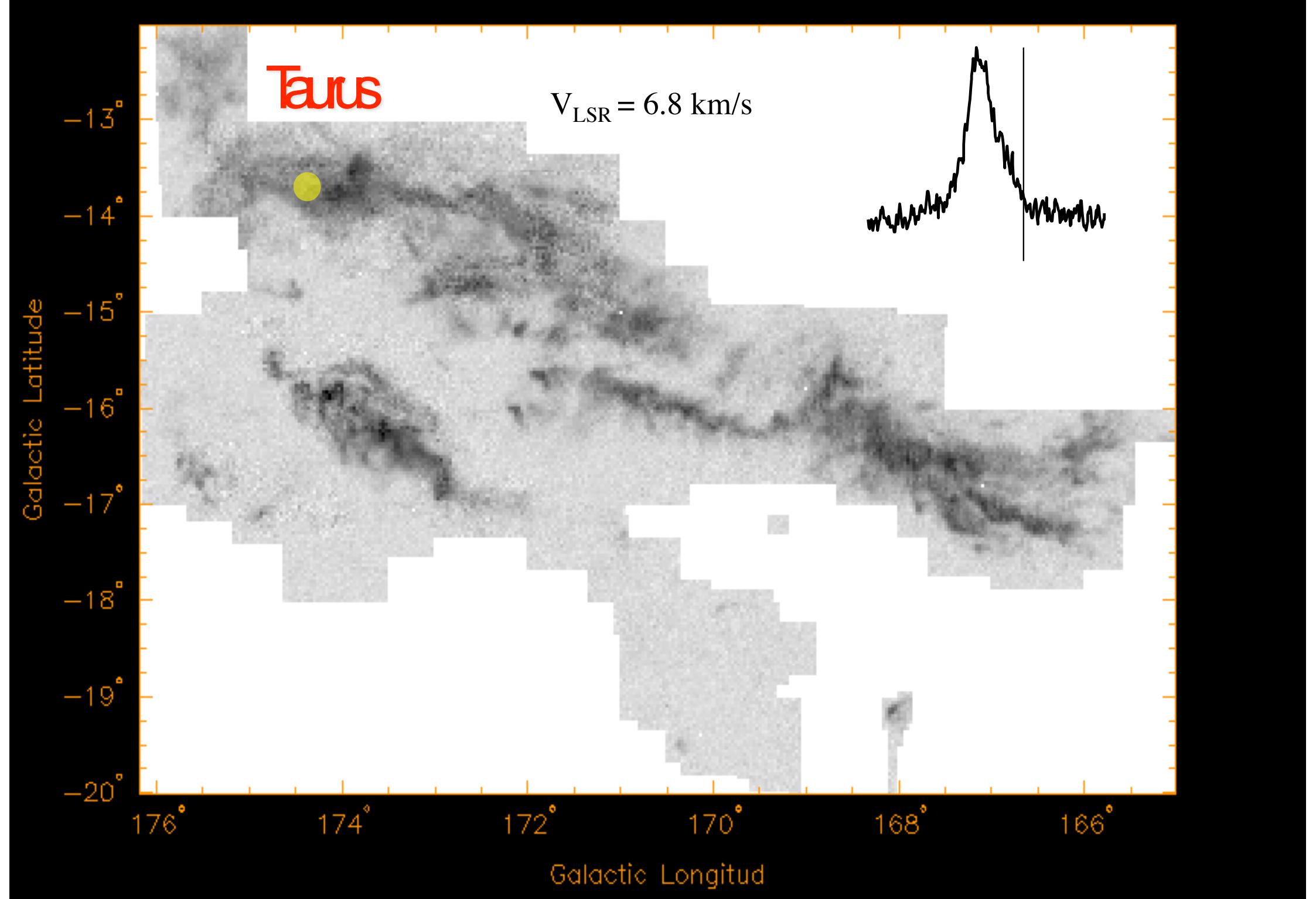


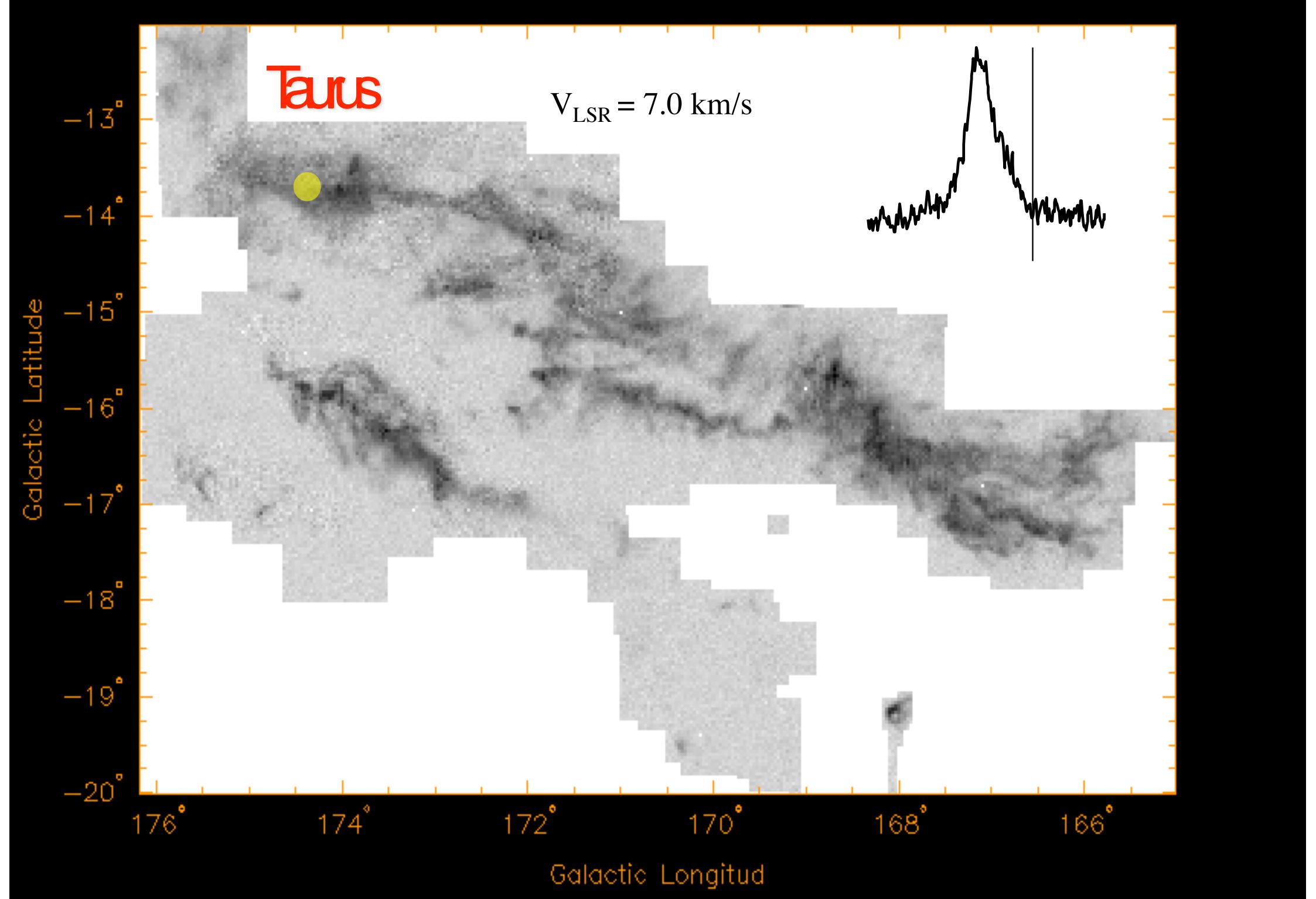


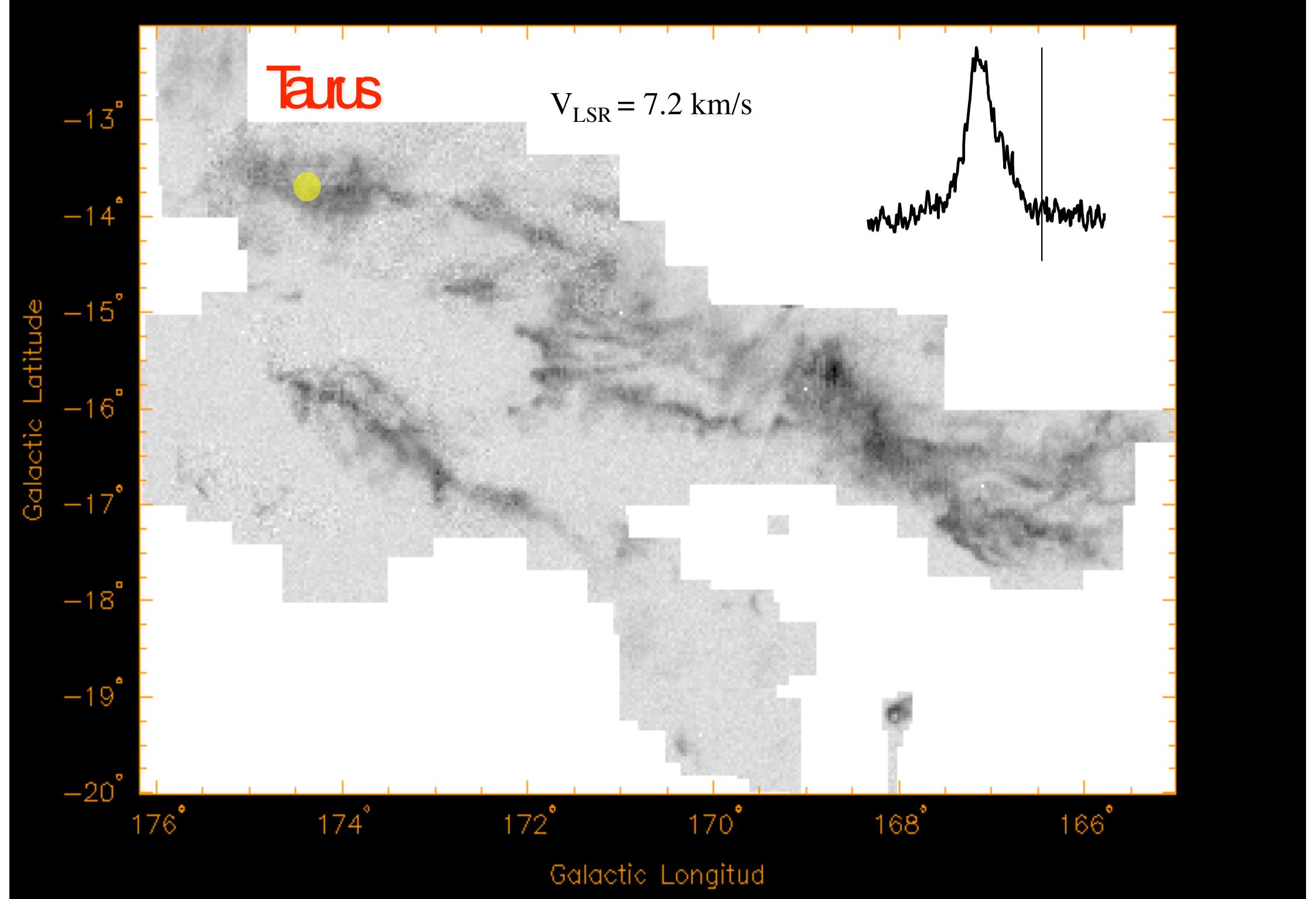


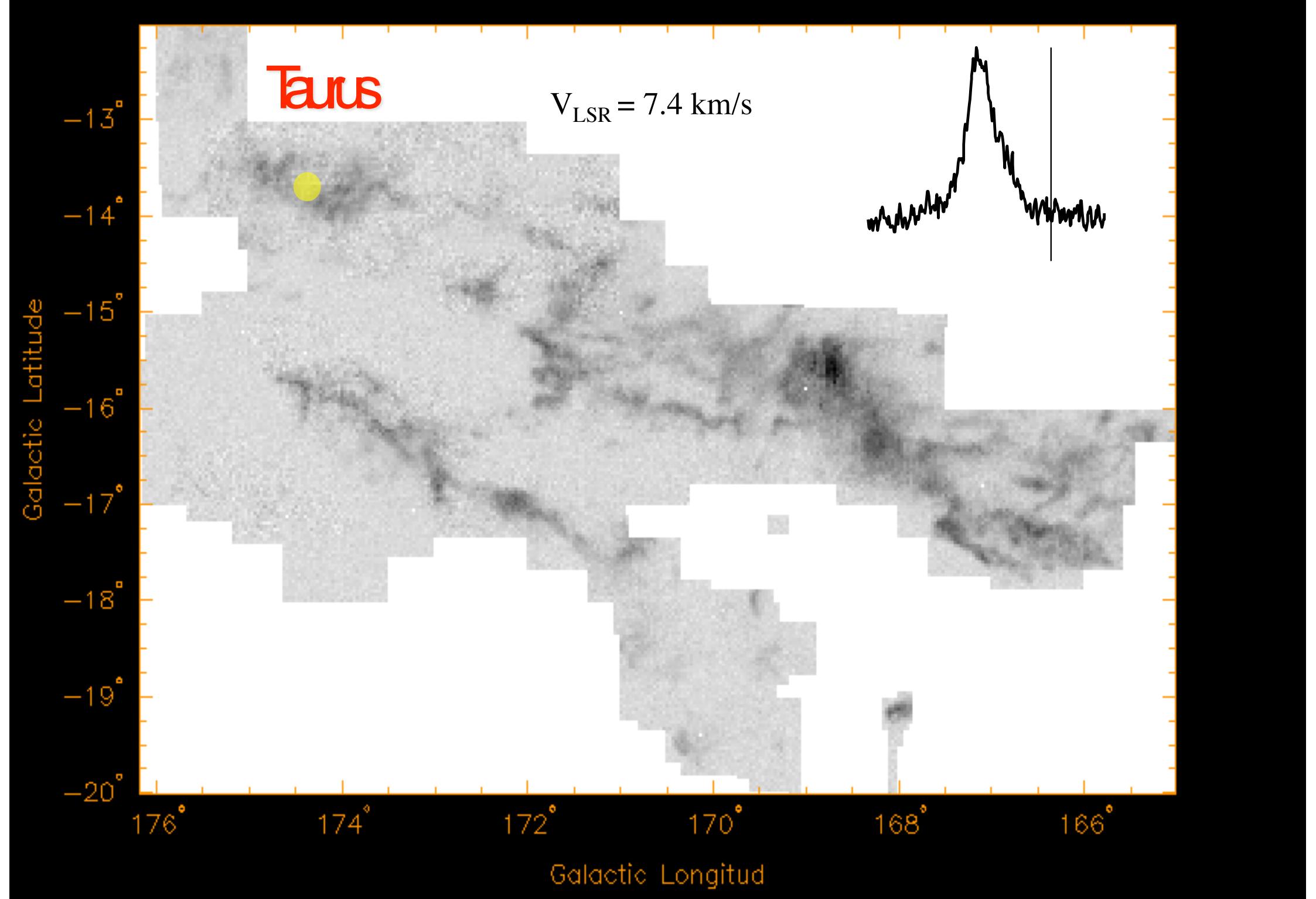


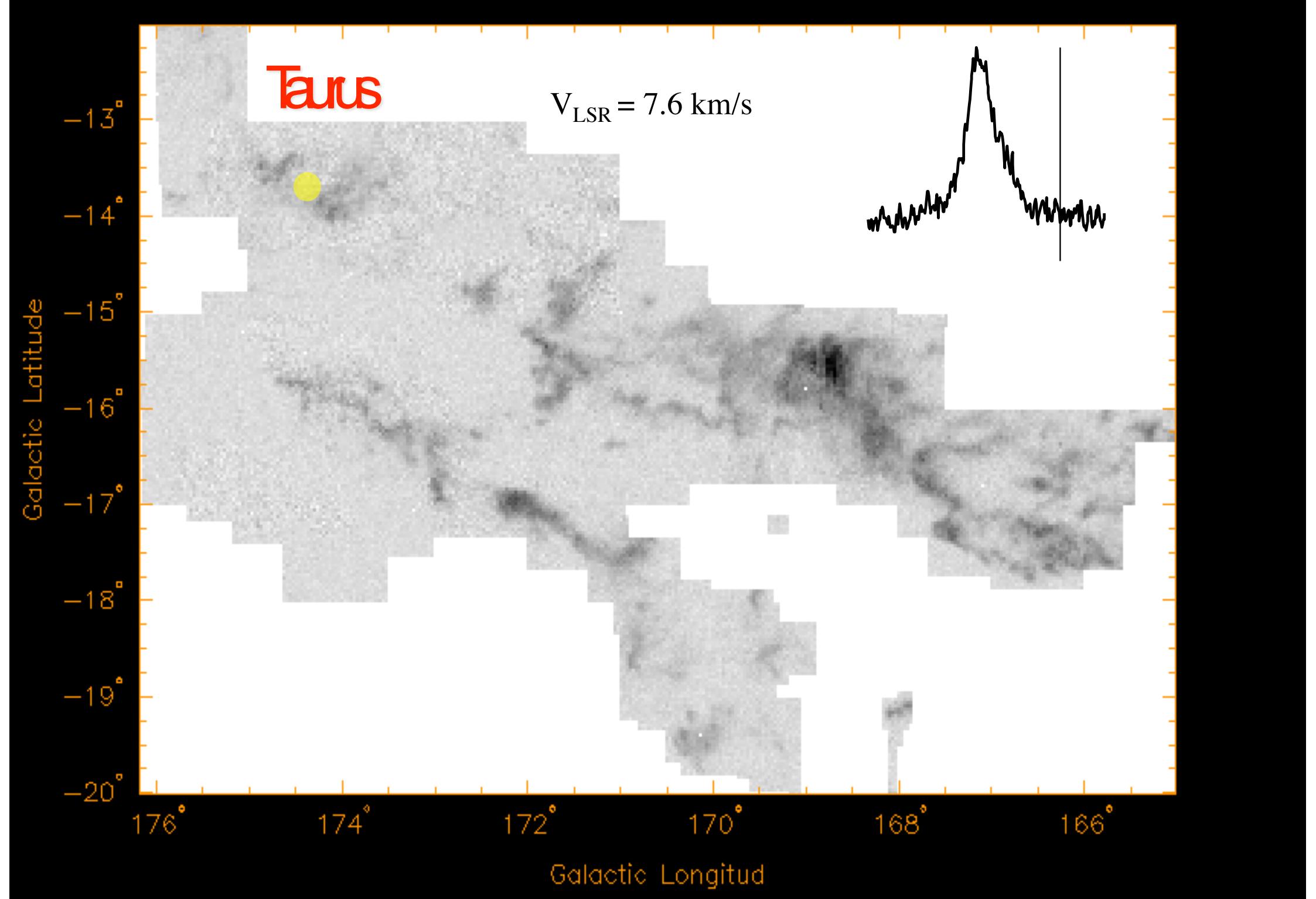


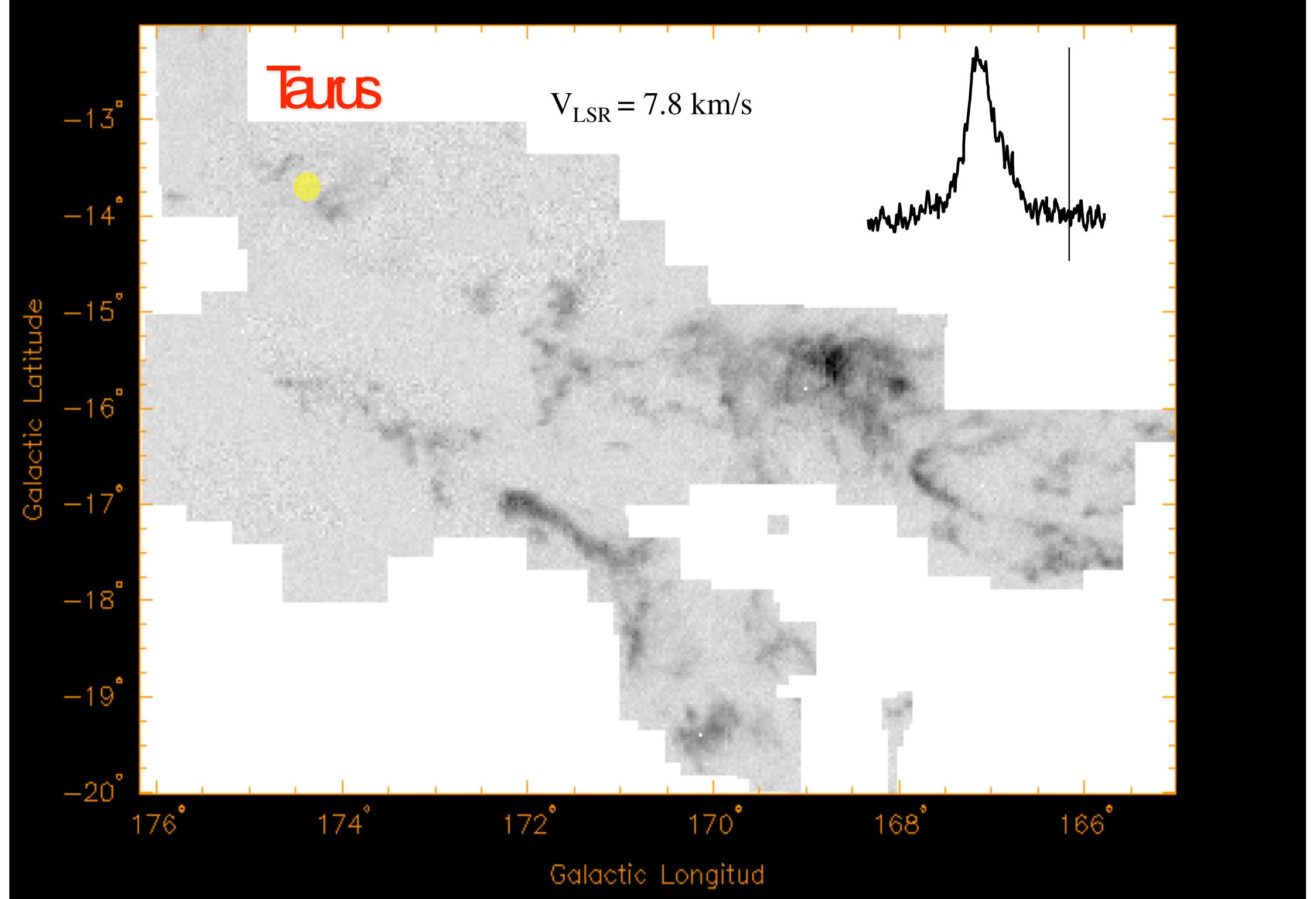


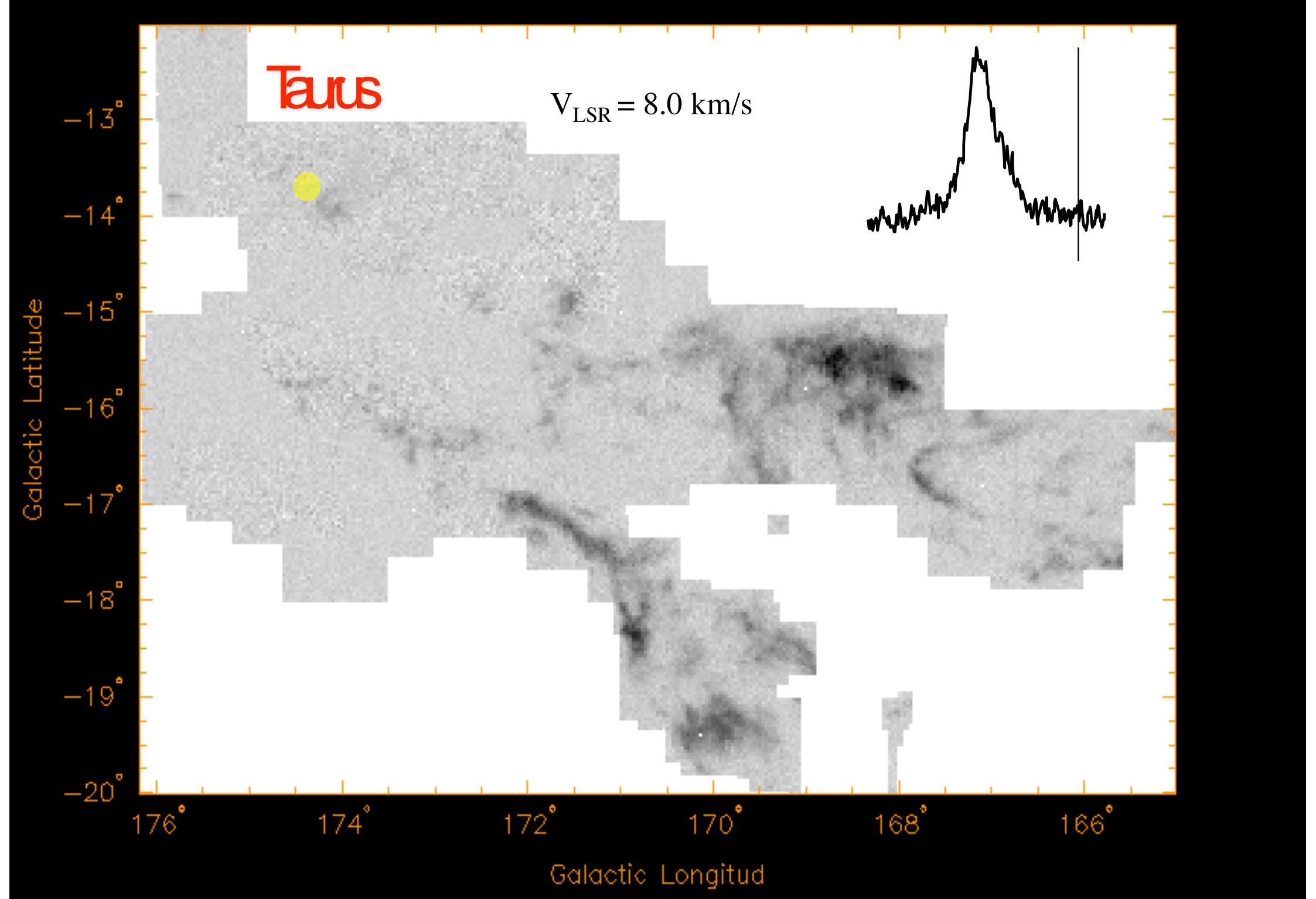


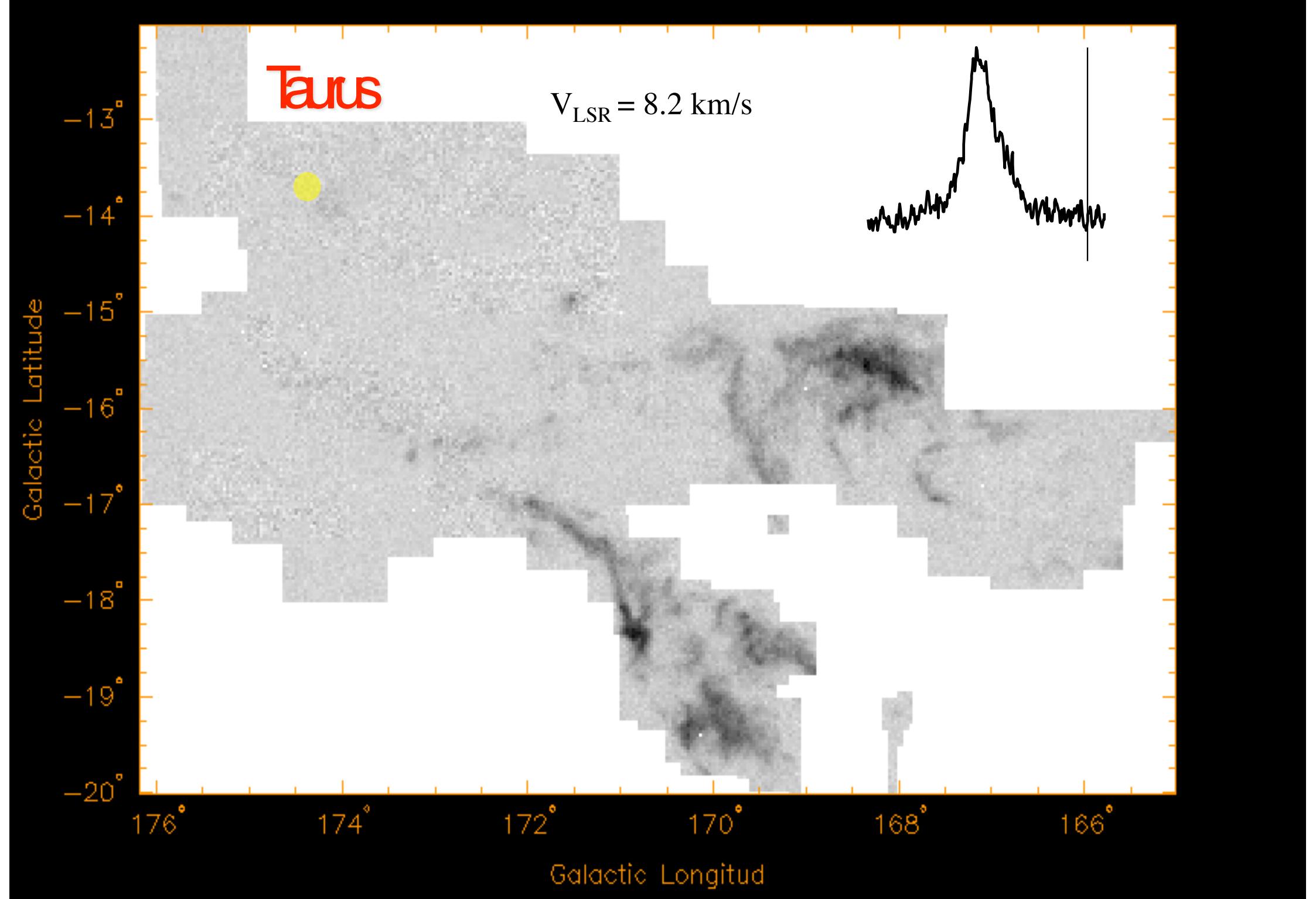


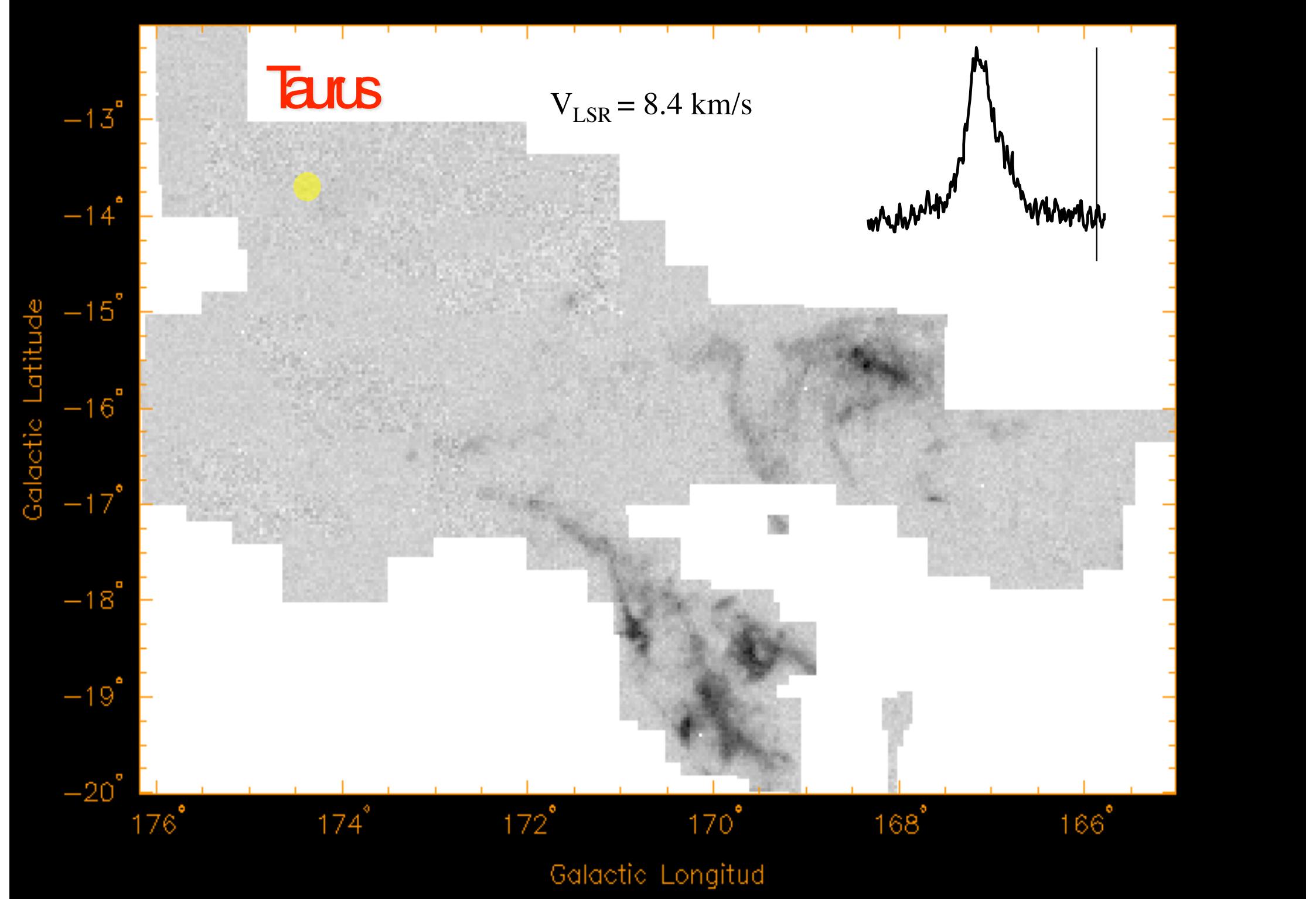


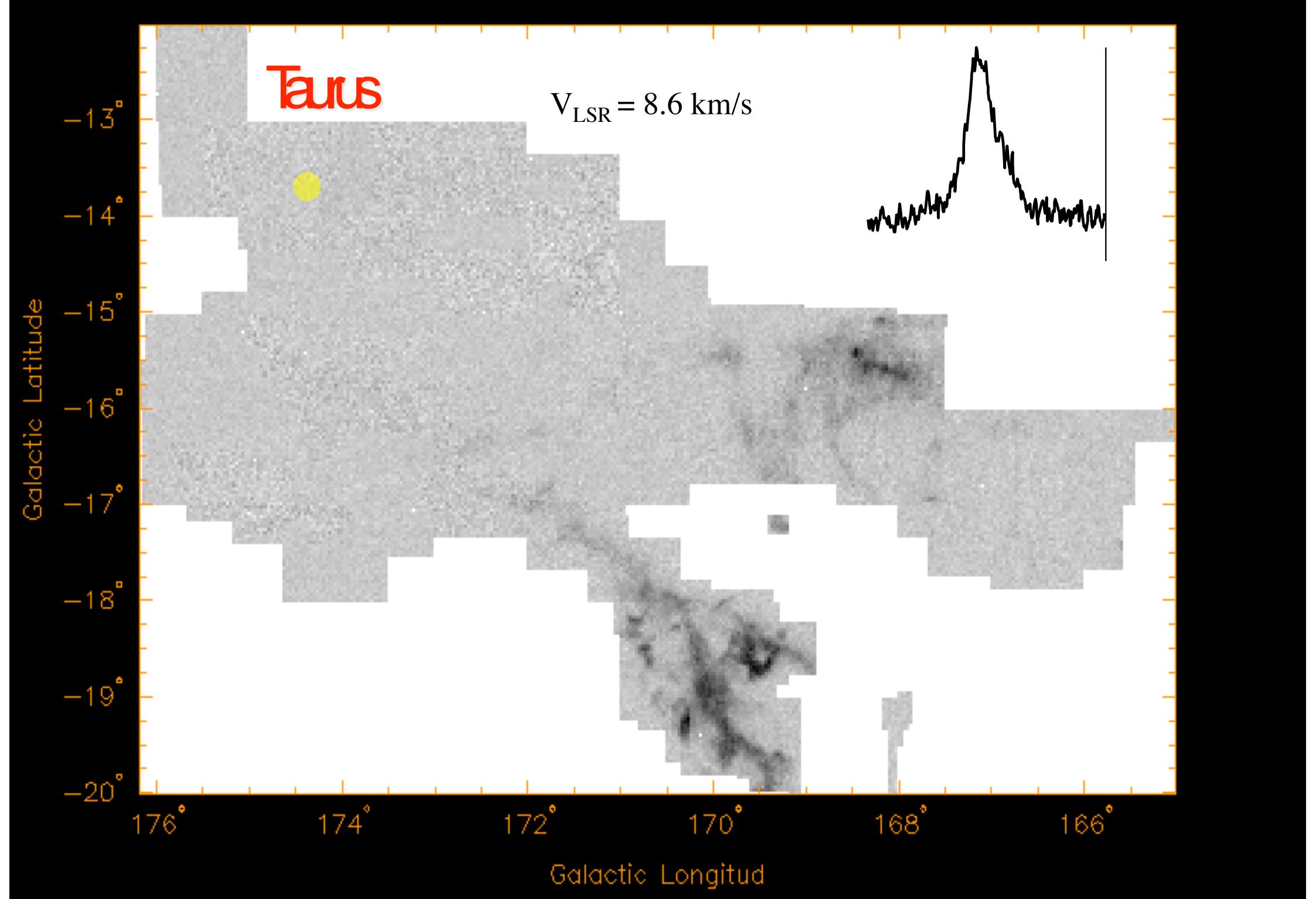


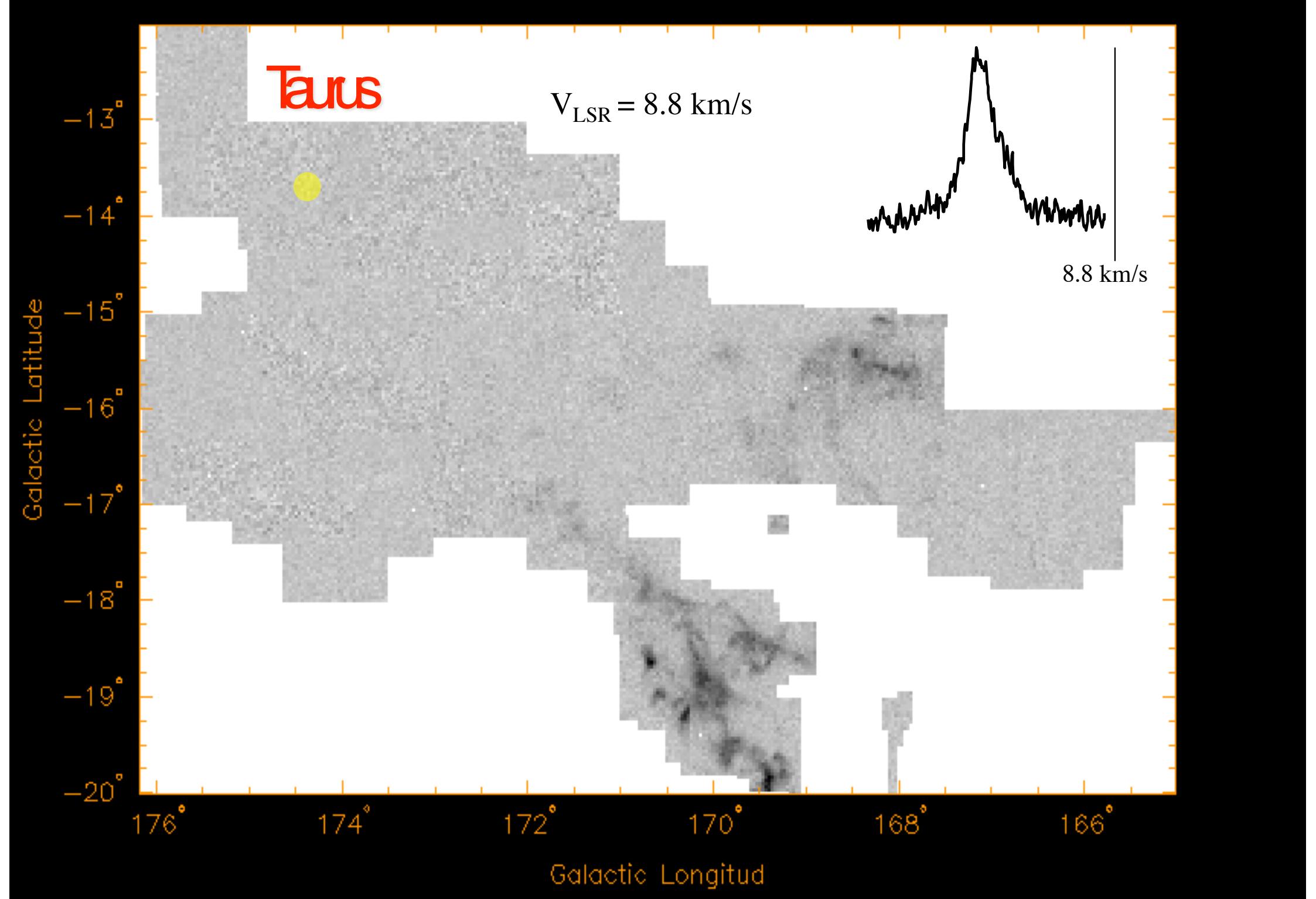


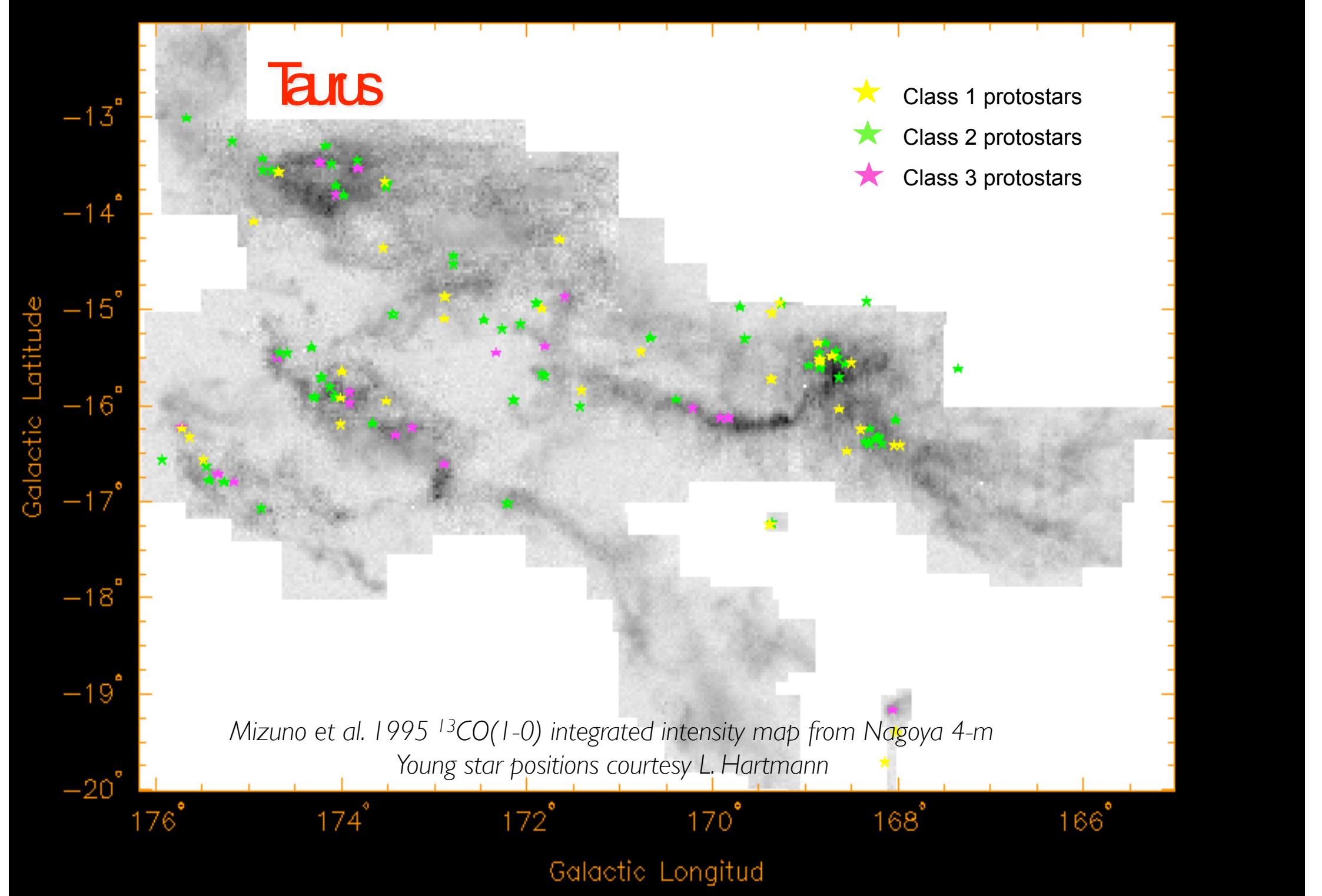












# theoretical approach

# Gravoturbulent star formation

- Idea:

*Star formation is controlled  
by interplay between  
gravity and  
supersonic turbulence!*

- Dual role of turbulence:
  - *stability on large scales*
  - *initiating collapse on small scales*

(e.g., Larson, 2003, Rep. Prog. Phys., 66, 1651;  
or Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125)

Ralf Klessen: Cardiff, 25.02.2008

# Gravoturbulent star formation

- Idea:

*Star formation is controlled  
by interplay between  
gravity and  
supersonic turbulence!*

- Validity:

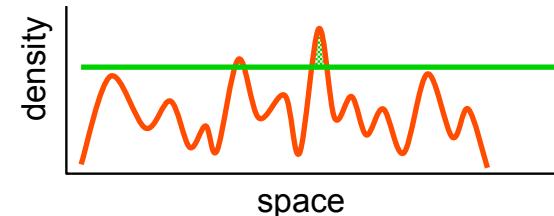
This hold on *all* scales and applies to build-up of stars and star clusters within molecular clouds as well as to the formation of molecular clouds in galactic disk.

(e.g., Larson, 2003, Rep. Prog. Phys, 66, 1651;  
or Mac Low & Klessen, 2004, Rev. Mod. Phys., 76, 125)

Ralf Klessen: Cardiff, 25.02.2008

# Graviturbulent star formation

- interstellar gas is highly *inhomogeneous*
  - *thermal instability*
  - *gravitational instability*
  - *turbulent compression* (in shocks  $\delta\rho/\rho \propto M^2$ ; in atomic gas:  $M \approx 1\dots3$ )
- cold *molecular clouds* can form rapidly in high-density regions at *stagnation points* of convergent large-scale flows
  - chemical *phase transition*: atomic  $\rightarrow$  molecular
  - process is *modulated* by large-scale *dynamics* in the galaxy

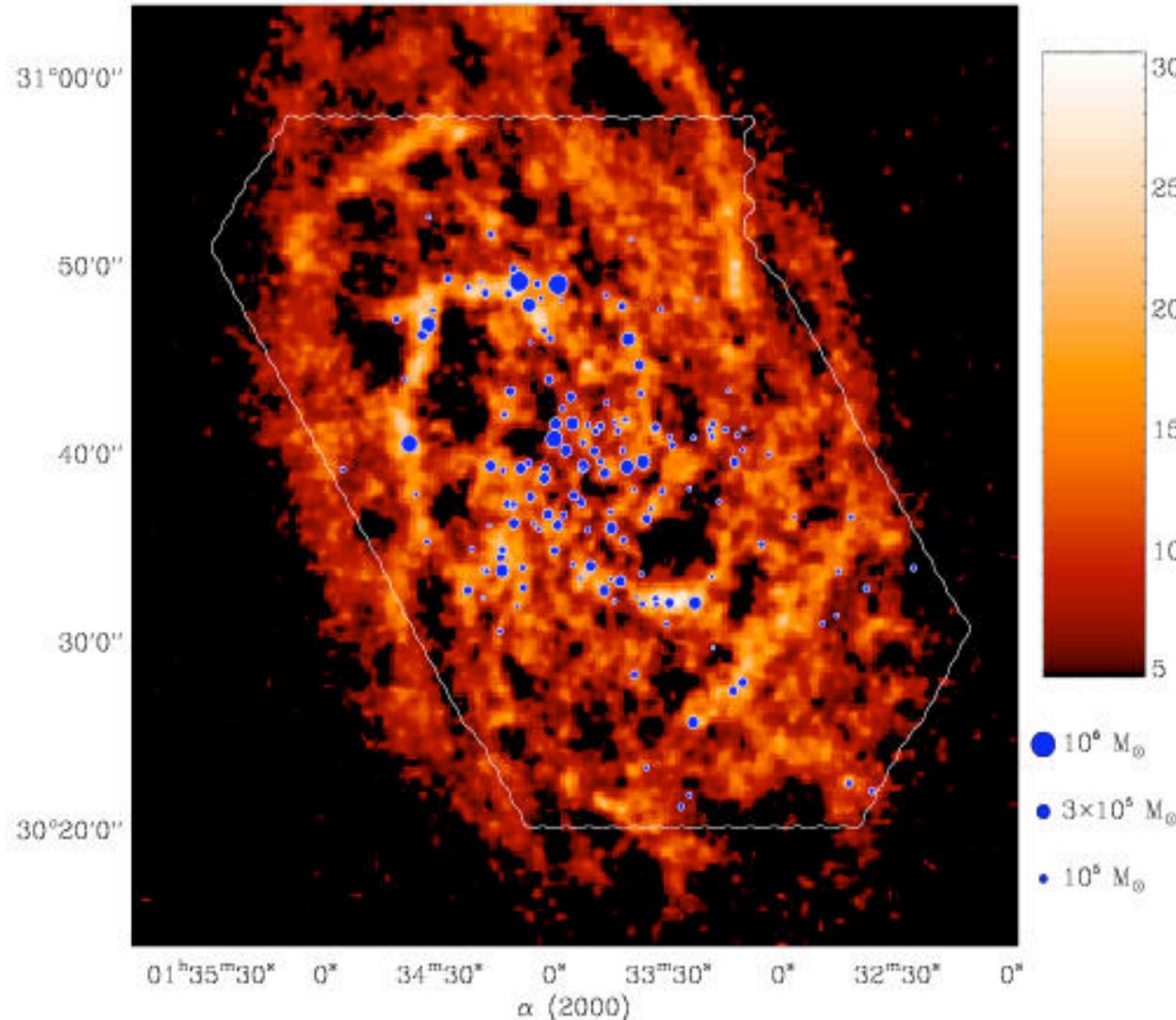


- inside *cold clouds*: turbulence is highly supersonic ( $M \approx 1\dots20$ )  
→ *turbulence* creates large density contrast,  
*gravity* selects for collapse

—————> **GRAVOTUBULENT FRAGMENTATION**

- *turbulent cascade*: local compression *within* a cloud provokes collapse  
→ formation of individual *stars* and *star clusters*

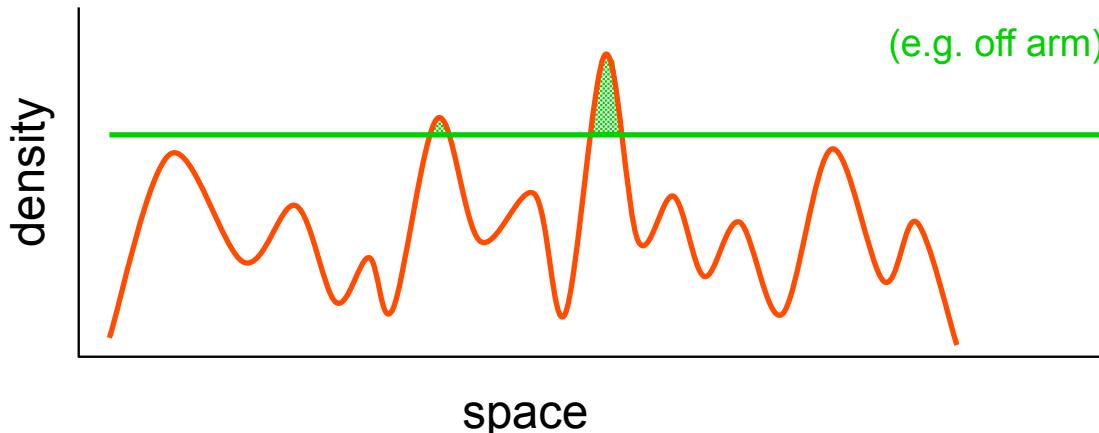
# molecular cloud formation



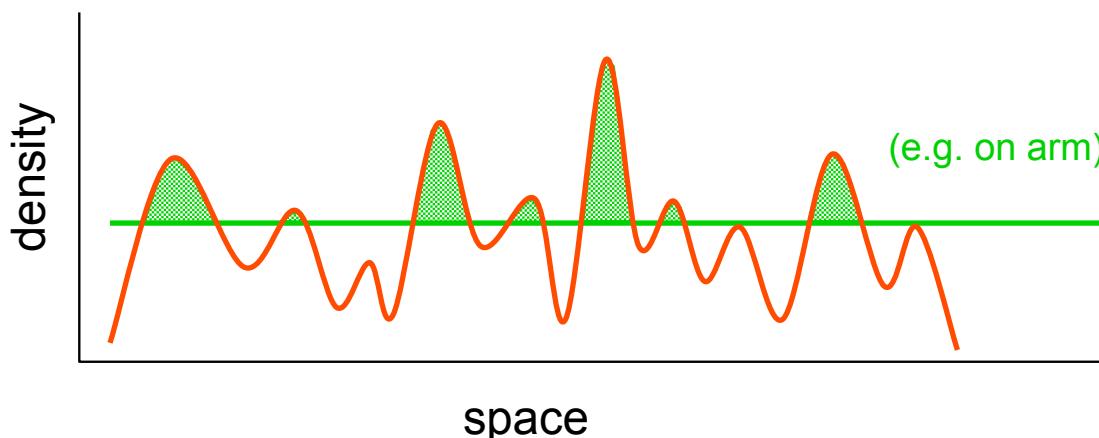
Thesis:

Molecular clouds form at *stagnation points* of large-scale convergent flows, mostly triggered by global (or external) perturbations.

# correlation with large-scale perturbations



*density/temperature fluctuations* in warm atomar ISM are caused by *thermal/gravitational instability* and/or *supersonic turbulence*



some fluctuations are *dense* enough to *form H<sub>2</sub>* within “reasonable time”

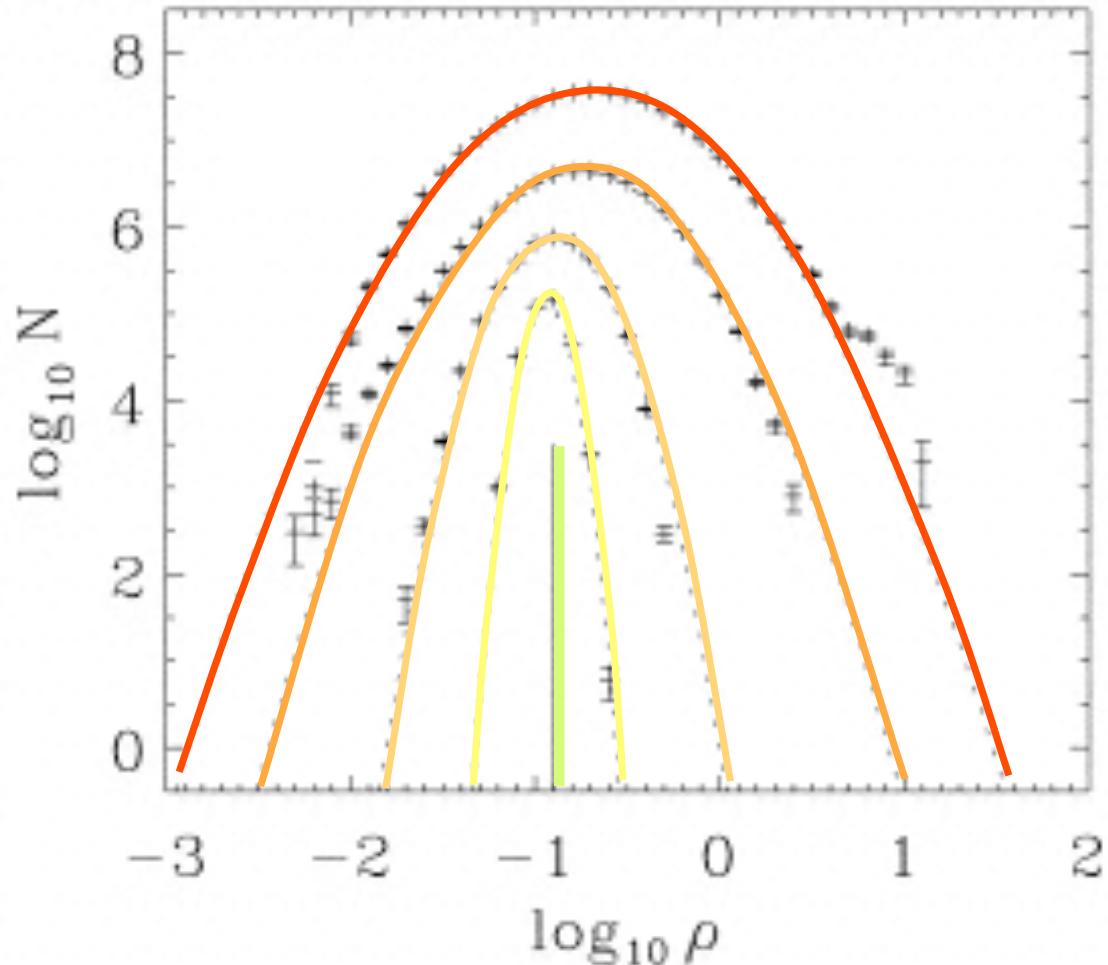
→ **molecular cloud**

(Glover & Mac Low 2007a,b)

*external perturbations* (i.e. potential changes) *increase* likelihood

(Dobbs & Bonnell 2006)

# star formation on *global* scales



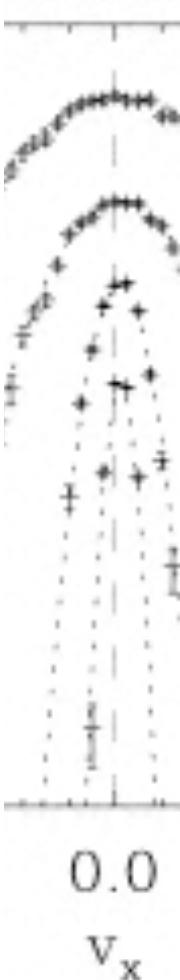
mass weighted  $\rho$ -pdf, each shifted by  $\Delta \log N = 1$

(from Klessen, 2001; also Gazol et al. 2005, Mac Low et al. 2005)

probability distribution  
function of the density  
( $\rho$ -pdf)

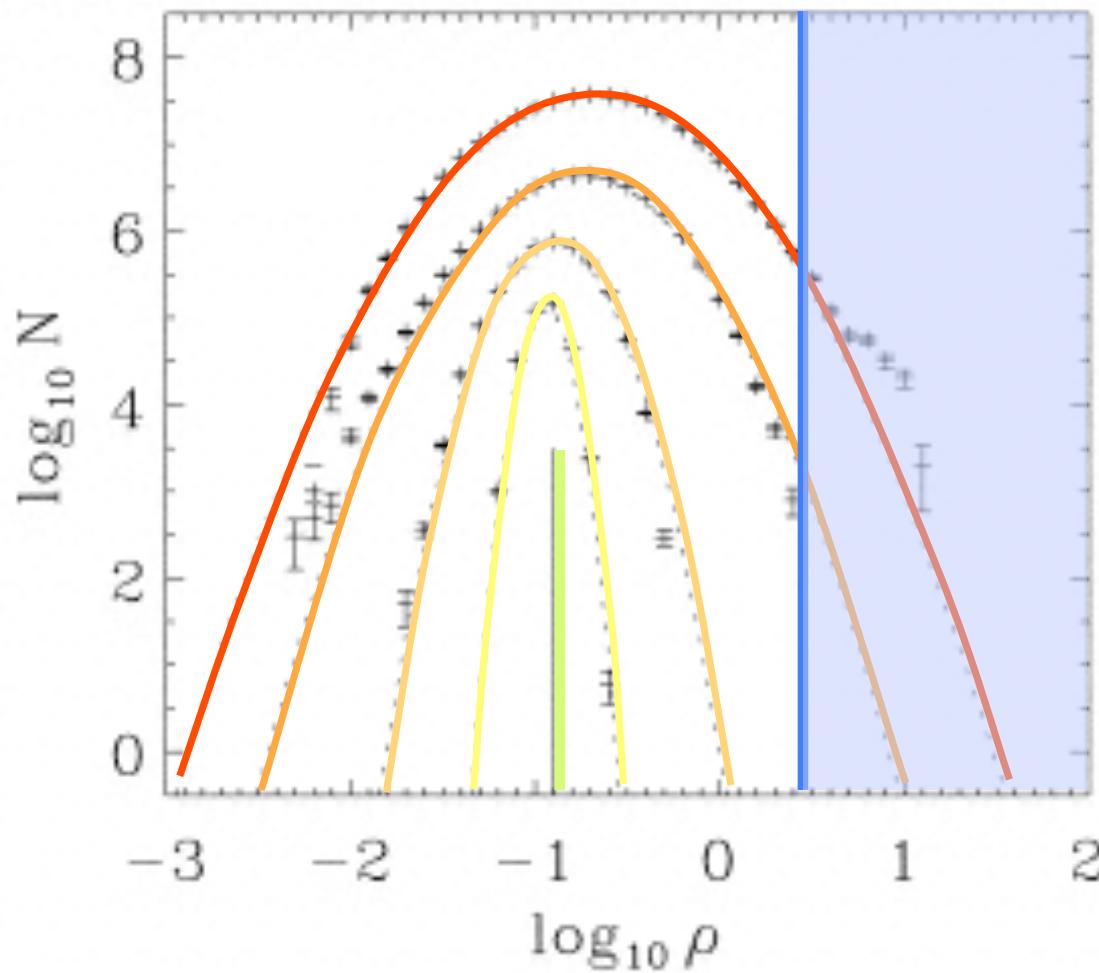
varying rms Mach  
numbers:

**M1 > M2 >**  
**M3 > M4 > 0**



Ralf Klessen: Cardiff, 25.02.2008

# star formation on *global* scales



mass weighted  $\rho$ -pdf, each shifted by  $\Delta \log N = 1$

(rate from Hollenback, Werner, & Salpeter 1971)

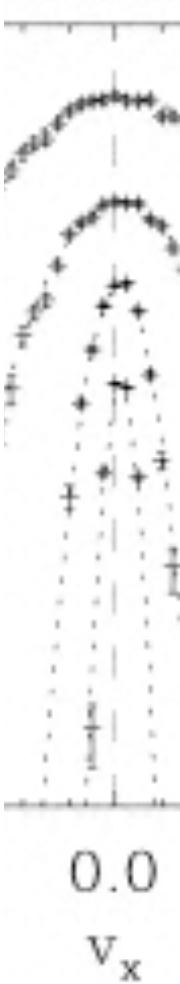
$H_2$  formation rate:

$$\tau_{H_2} \approx \frac{1.5 \text{ Gyr}}{n_H / 1 \text{ cm}^{-3}}$$

for  $n_H \geq 100 \text{ cm}^{-3}$ ,  $H_2$  forms within 10 Myr, this is about the lifetime of typical MC's.

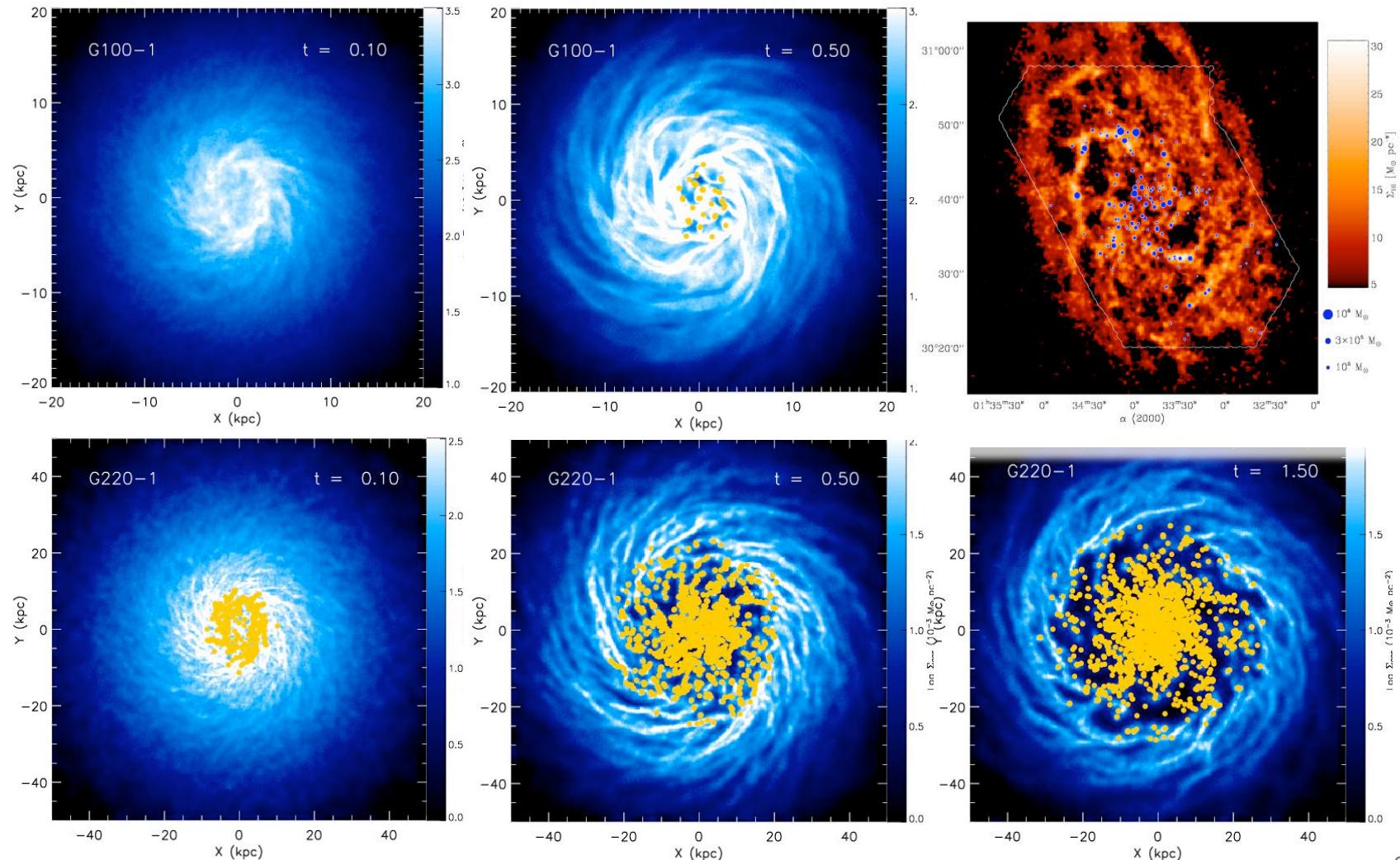
in turbulent gas, the  $H_2$  fraction can become very high on short timescale

(for models with coupling between cloud dynamics and time-dependent chemistry, see Glover & Mac Low 2007a,b)

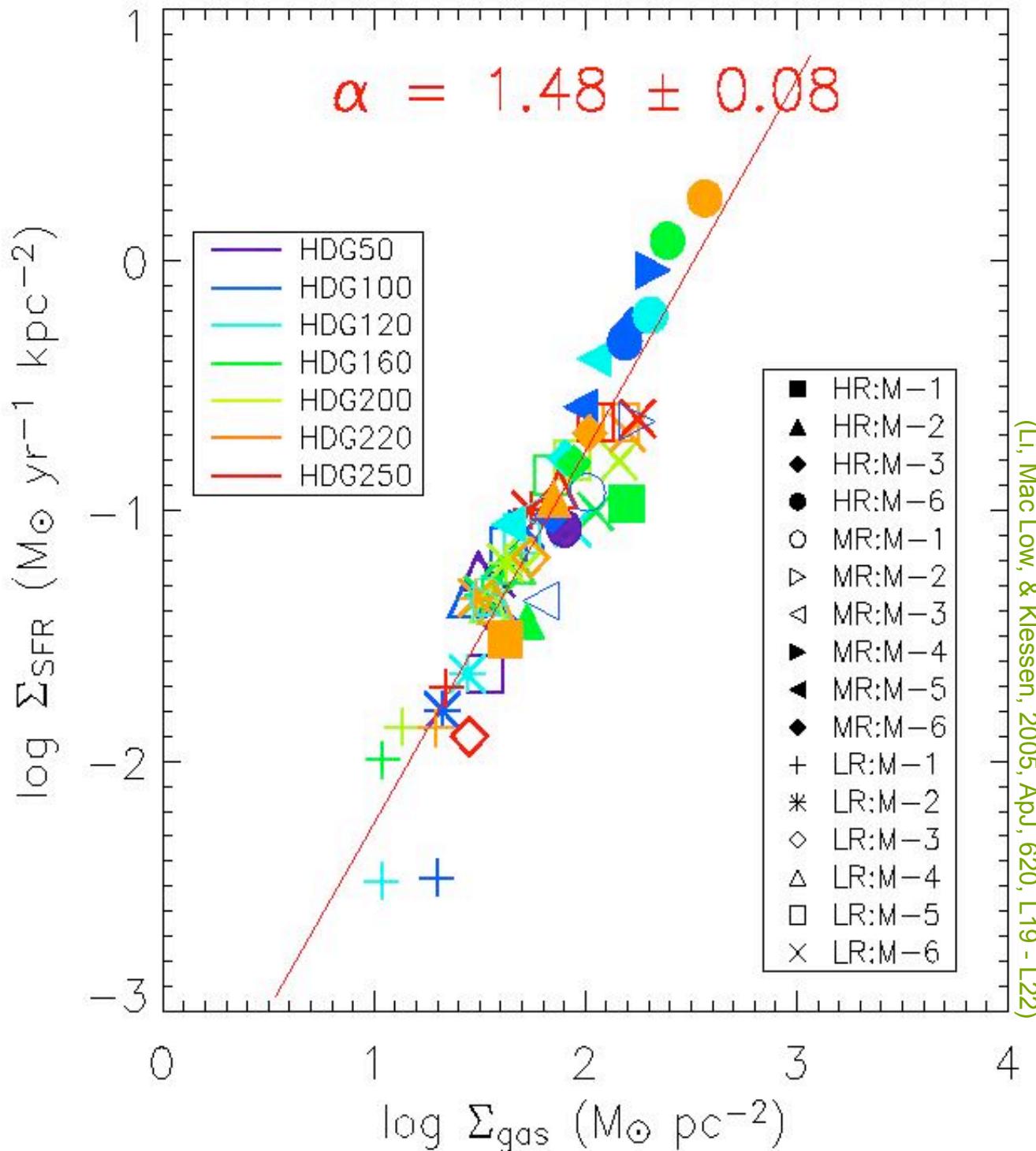


# modeling galactic SF

SPH calculations of self-gravitating disks of stars and (isothermal) gas in dark-matter potential, sink particles measure local collapse  $\rightarrow$  star formation



(Li, Mac Low, & Klessen, 2005, ApJ, 620,L19 - L22)

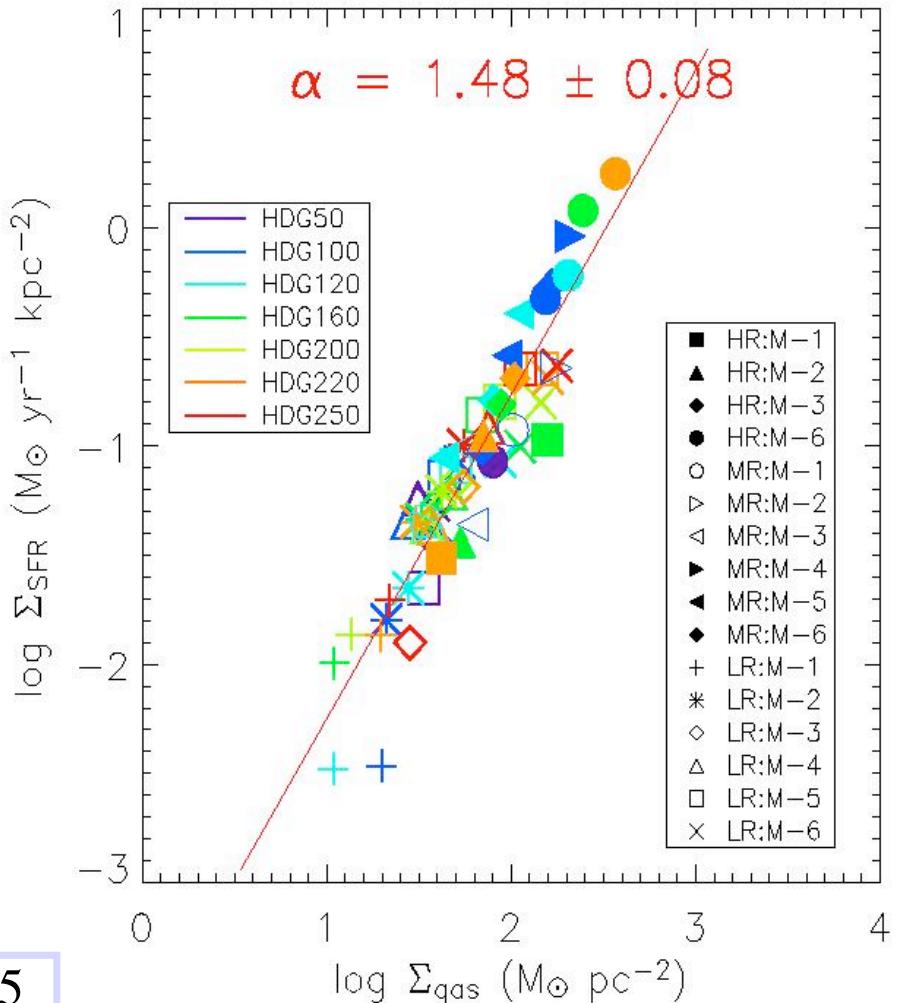
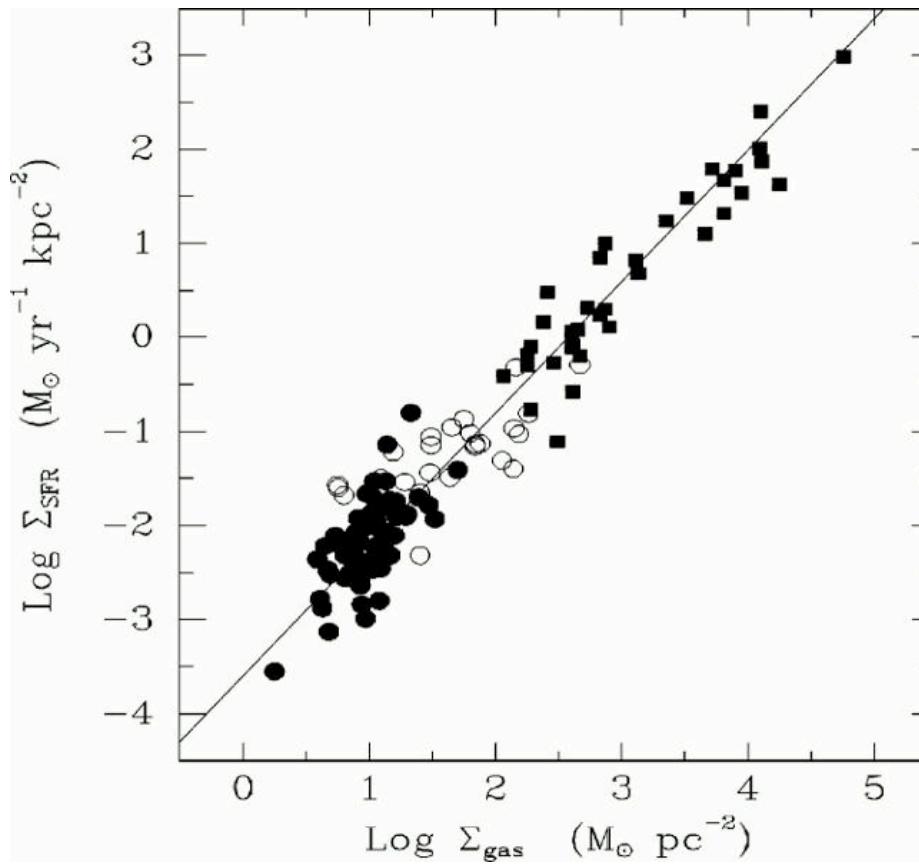


We find correlation between *star formation rate* and *gas surface density*:

$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^{1.5}$$

*global Schmidt law*

# observed Schmidt law



in both cases:

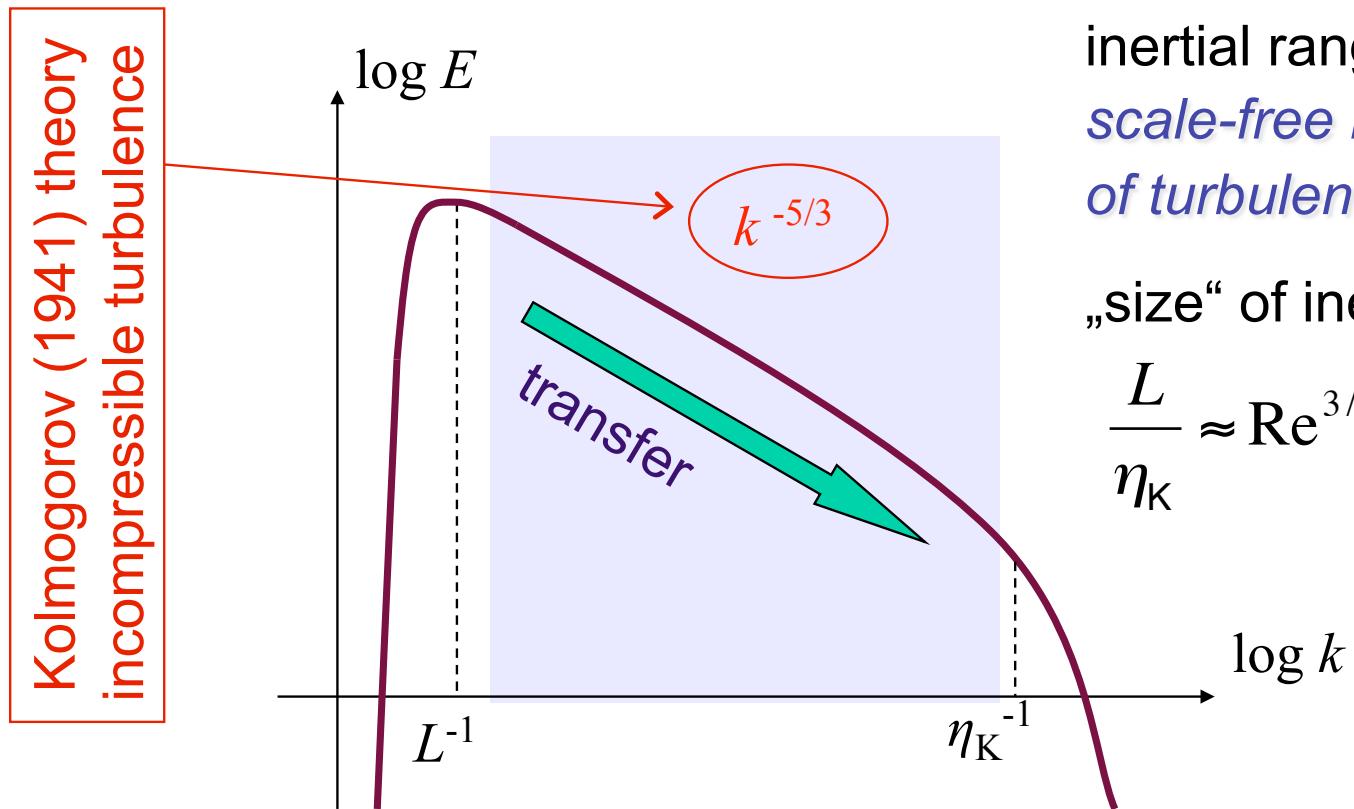
$$\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^{1.5}$$

(from Kennicutt 1998)

Ralf Klessen: Cardiff, 25.02.2008

turbulence

# Turbulent cascade



energy  
input  
scale

energy  
dissipation  
scale

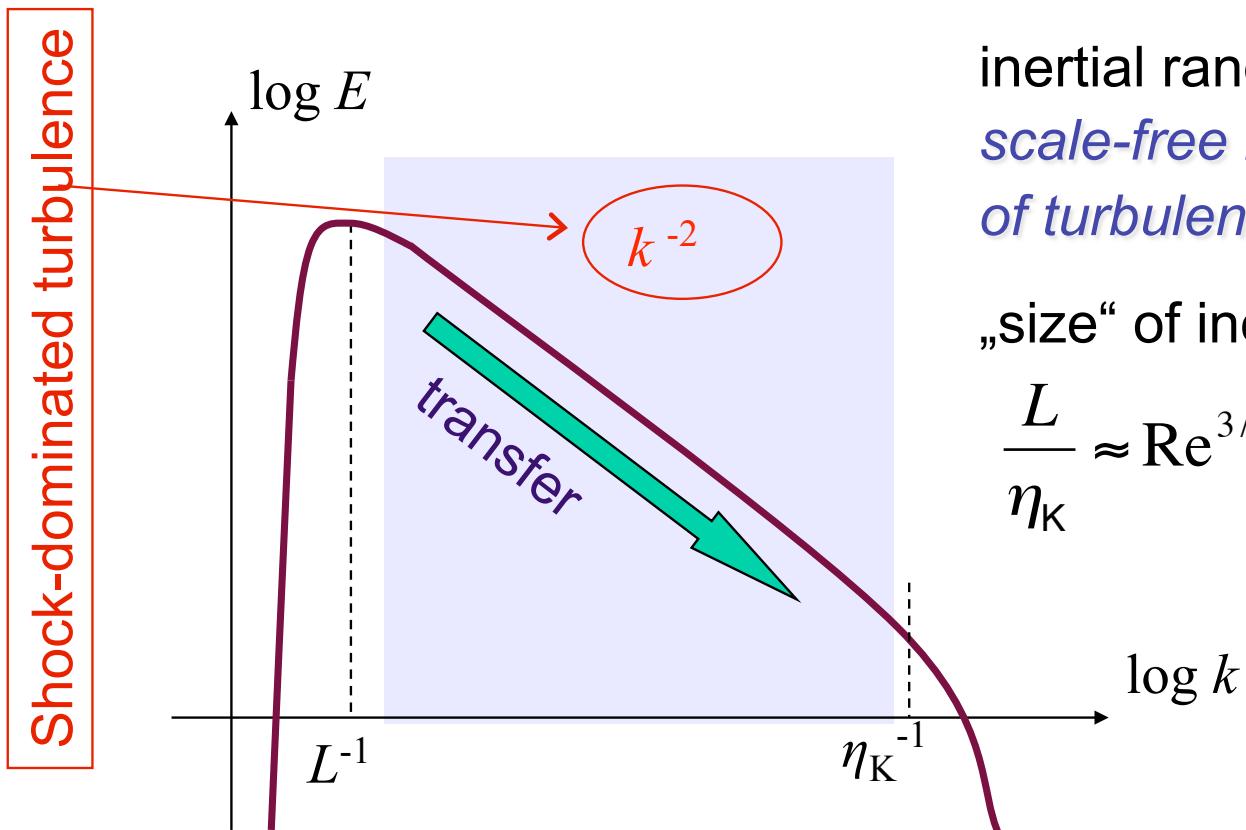
inertial range:  
*scale-free behavior  
of turbulence*

„size“ of inertial range:

$$\frac{L}{\eta_k} \approx \text{Re}^{3/4}$$

log  $k$

# Turbulent cascade



inertial range:  
*scale-free behavior  
of turbulence*

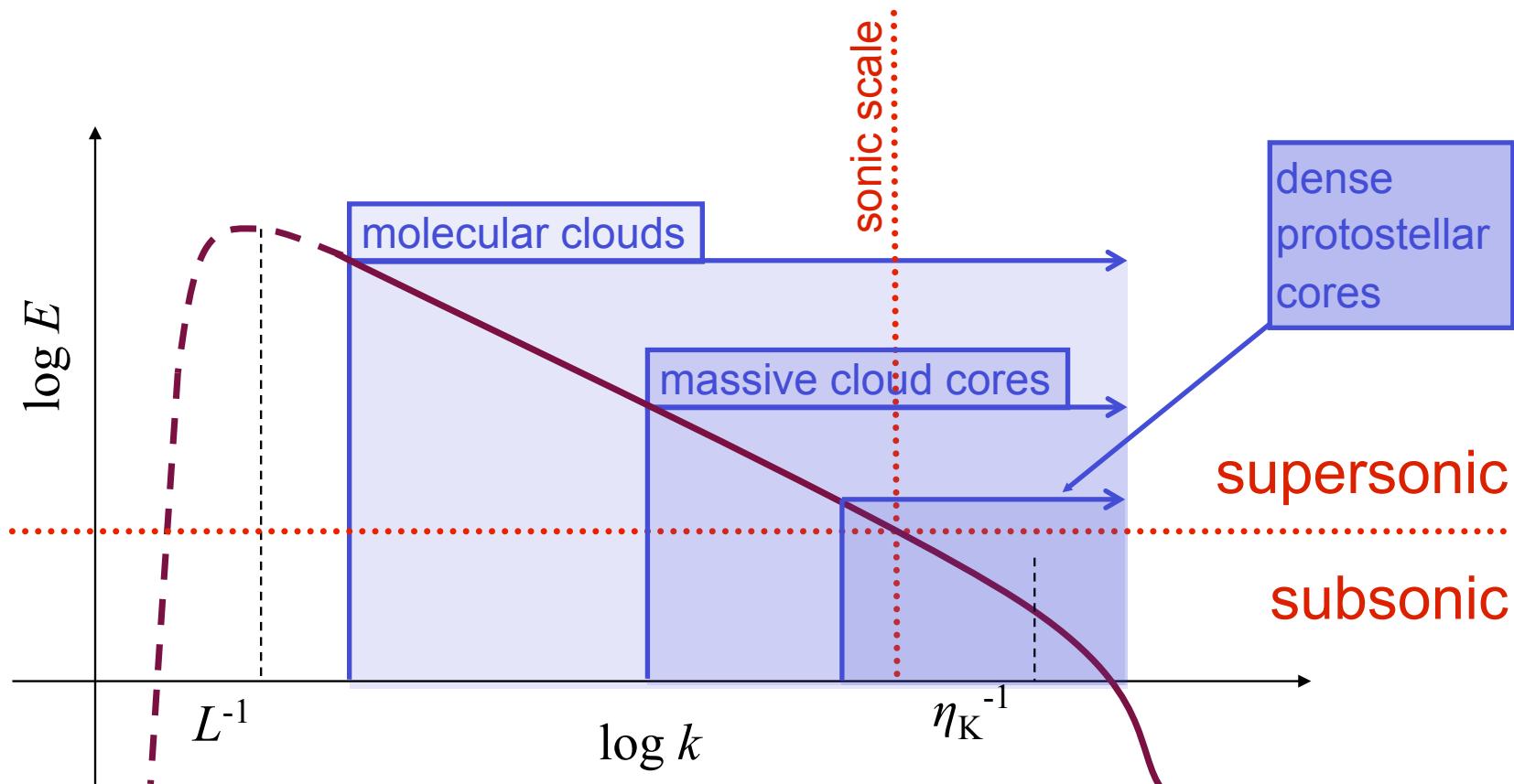
„size“ of inertial range:

$$\frac{L}{\eta_k} \approx \text{Re}^{3/4}$$

energy  
input  
scale

energy  
dissipation  
scale

# Turbulent cascade in ISM

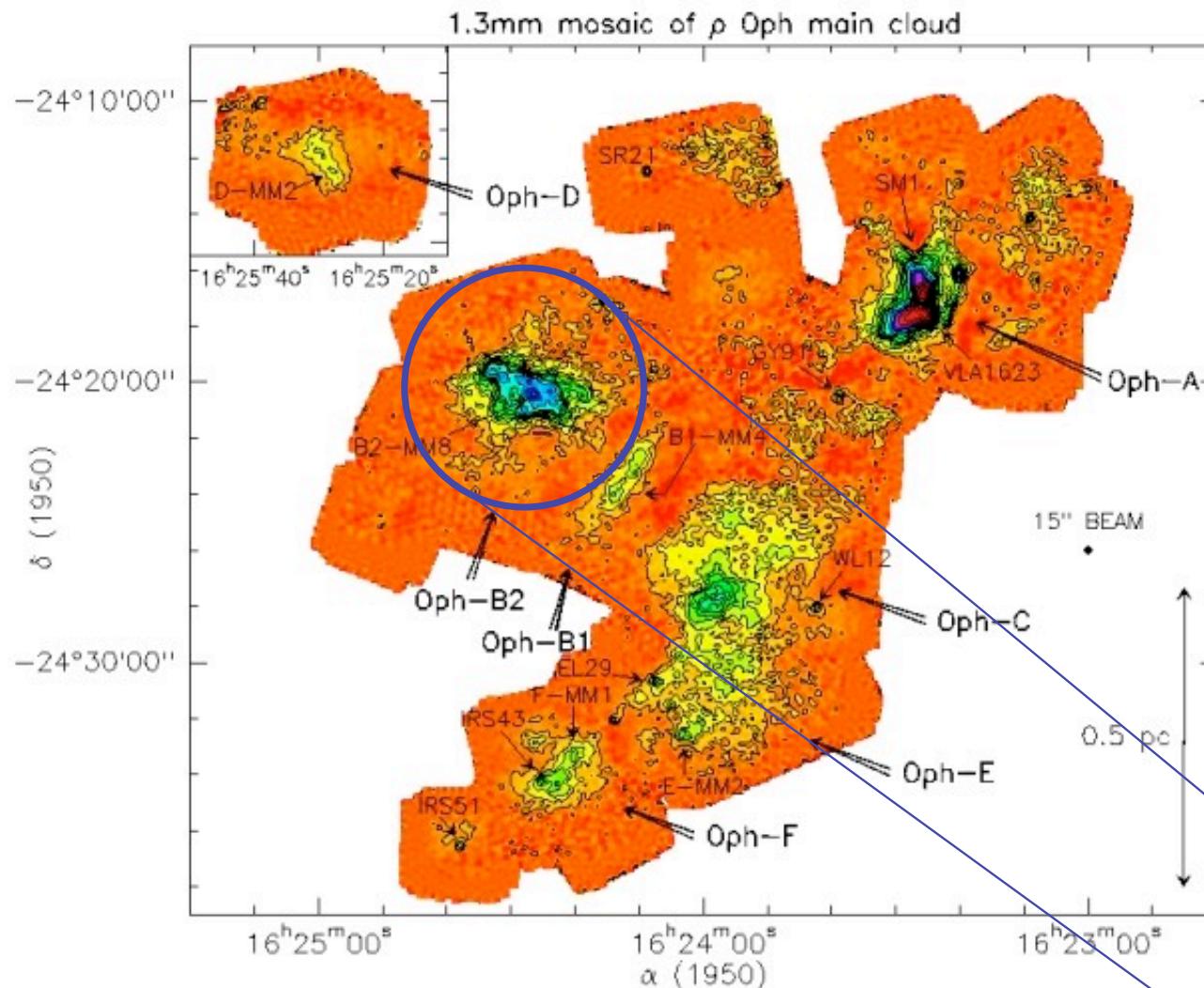


energy source & scale  
NOT known  
(supernovae, winds,  
spiral density waves?)

$\sigma_{\text{rms}} \ll 1 \text{ km/s}$   
 $M_{\text{rms}} \leq 1$   
 $L \approx 0.1 \text{ pc}$

dissipation scale not known  
(ambipolar diffusion,  
molecular diffusion?)

# Density structure of MC's



(Motte, André, & Neri 1998)

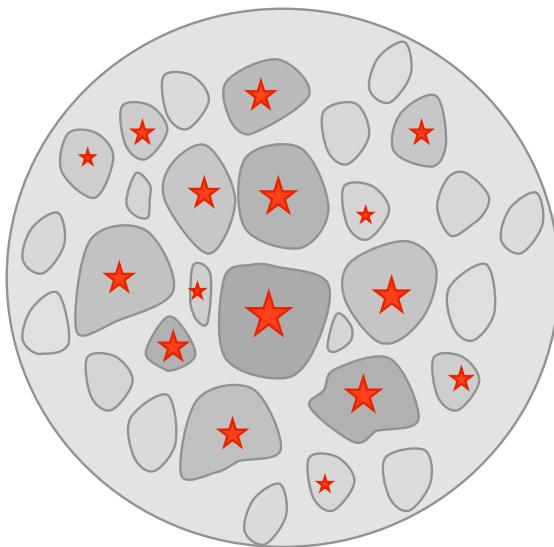
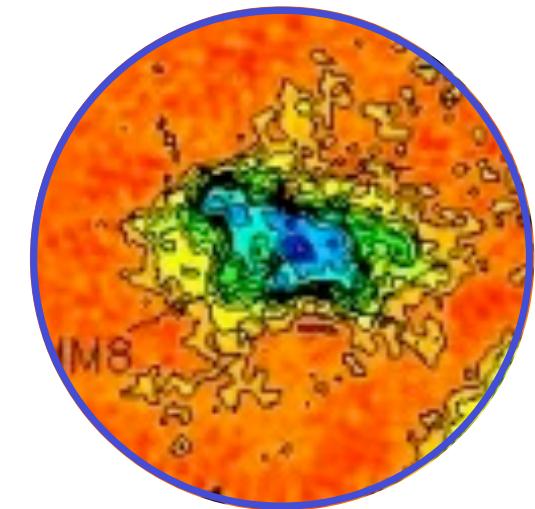
molecular clouds  
are highly  
inhomogeneous

stars form in the  
densest and  
coldest parts of  
the cloud

$\rho$ -Ophiuchus  
cloud seen in dust  
emission

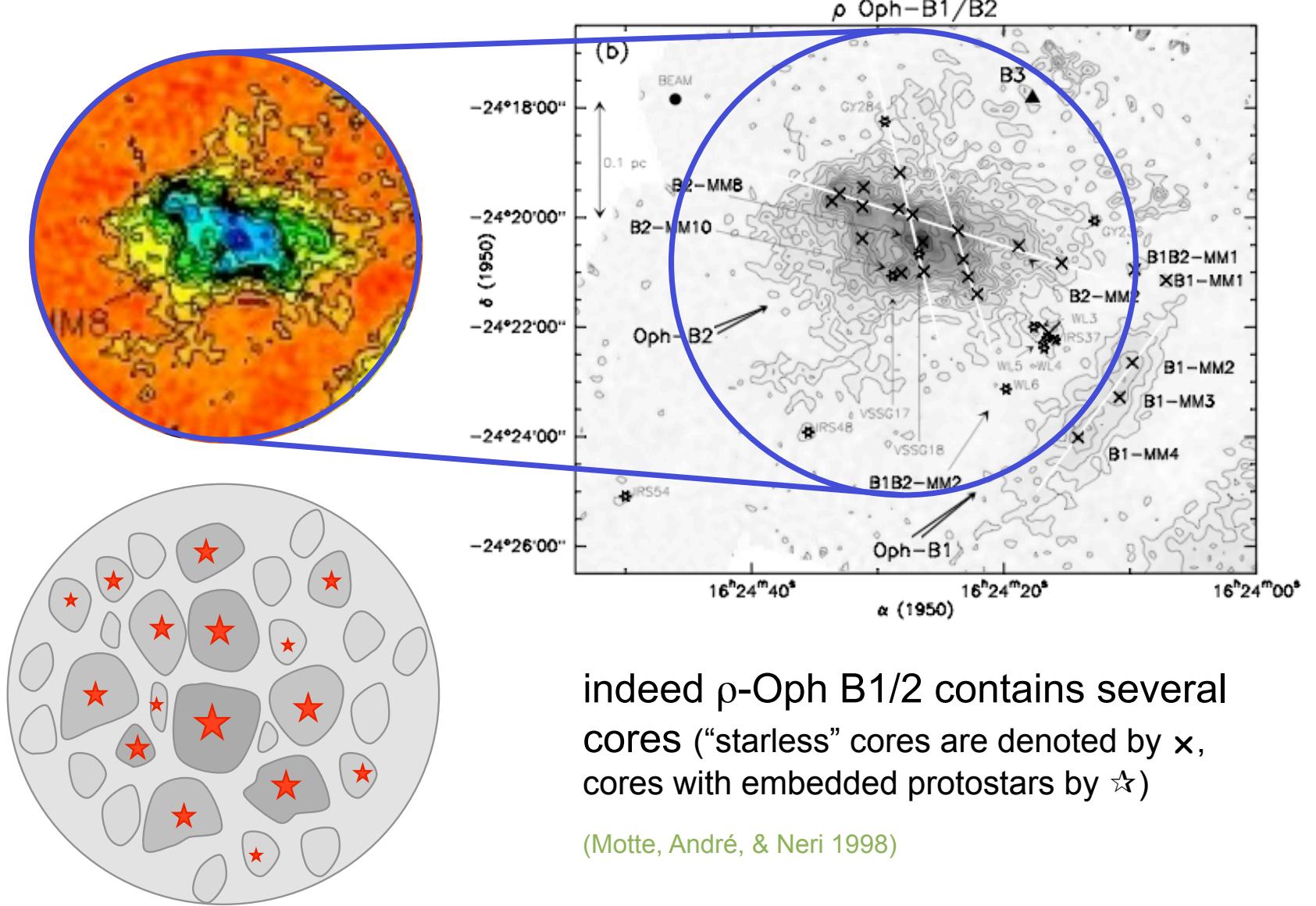
let's focus on  
a cloud core  
like this one

# Evolution of cloud cores



- How does this core evolve?  
Does it form one single massive star or cluster with mass distribution?
- Turbulent cascade „goes through“ cloud core
  - > NO scale separation possible
  - > NO effective sound speed
- Turbulence is supersonic!
  - > produces strong density contrasts:  
 $\delta\rho/\rho \approx M^2$
  - > with typical  $M \approx 10$  -->  $\delta\rho/\rho \approx 100!$
- many of the shock-generated fluctuations are Jeans unstable and go into collapse
- --> expectation: *core breaks up and forms a cluster of stars*

# Evolution of cloud cores

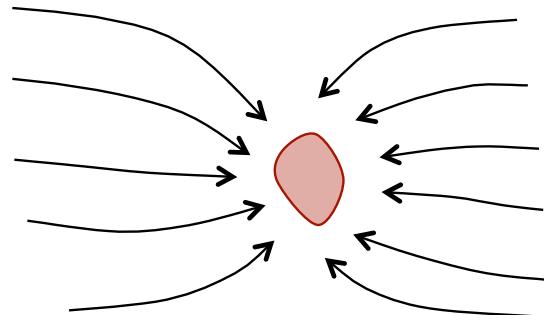


indeed  $\rho$ -Oph B1/2 contains several cores (“starless” cores are denoted by  $\times$ , cores with embedded protostars by  $\star$ )

(Motte, André, & Neri 1998)

# Formation and evolution of cores

- protostellar cloud cores form at *stagnation point* in *convergent turbulent flows*



- if  $M > M_{\text{crit}} \propto \rho^{-1/2} T^{3/2}$ :

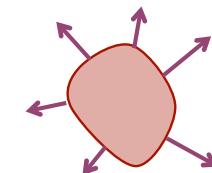
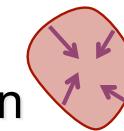
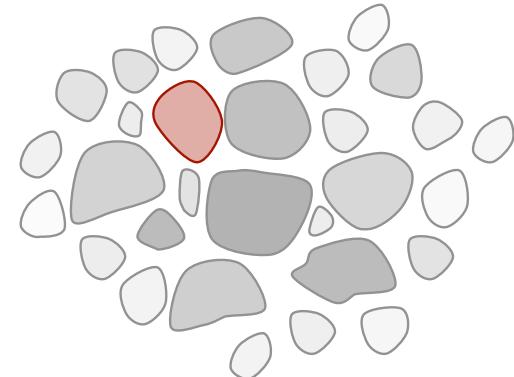
collapse & star formation

- if  $M < M_{\text{crit}} \propto \rho^{-1/2} T^{3/2}$ :

reexpansion after end of  
external compression

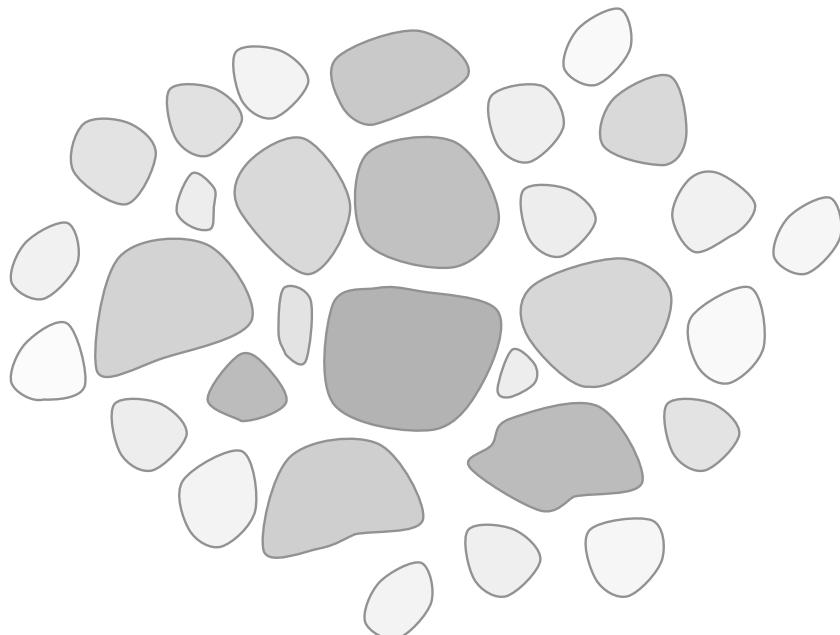
(e.g. Vazquez-Semadeni et al 2005)

- typical timescale:  $t \approx 10^4 \dots 10^5 \text{ yr}$



# Formation and evolution of cores

What happens to distribution  
of cloud cores?



Two extreme cases:

(1) turbulence dominates energy budget:

$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| > 1$$

--> individual cores do *not* interact

--> *collapse of individual cores*  
dominates *stellar mass growth*

--> *loose cluster of low-mass stars*

(2) turbulence decays, i.e. gravity

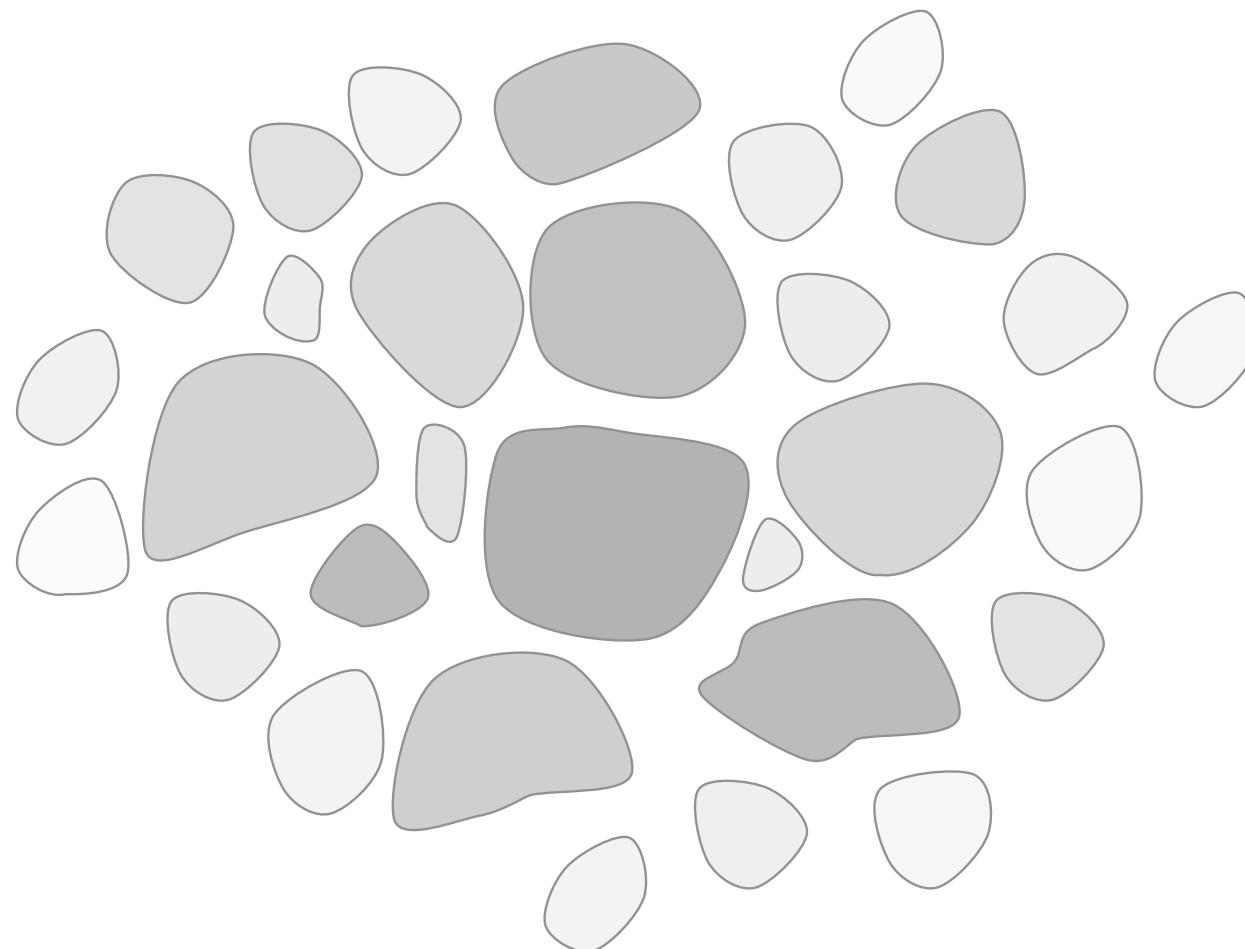
$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

--> *global contraction*

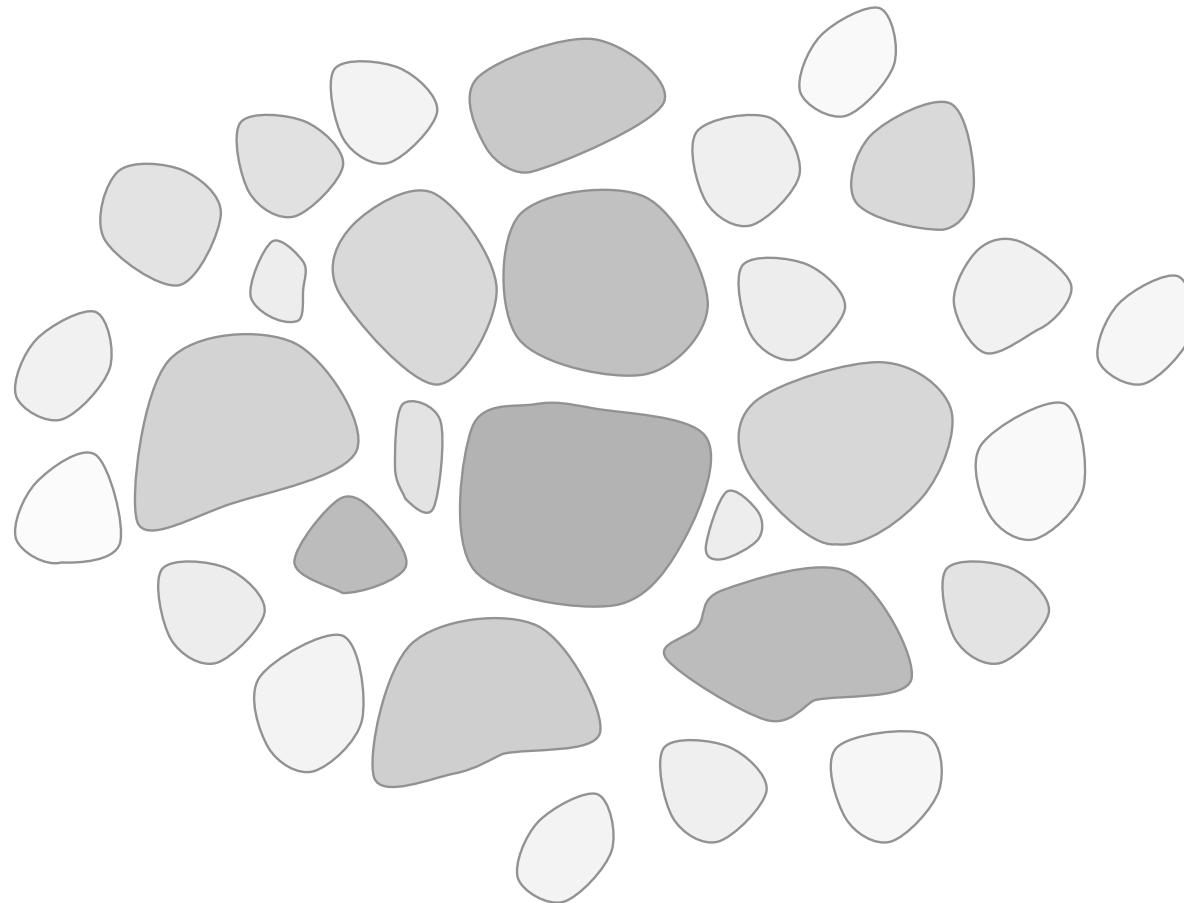
--> cores do *interact* while collapsing

--> *competition influences mass growth*

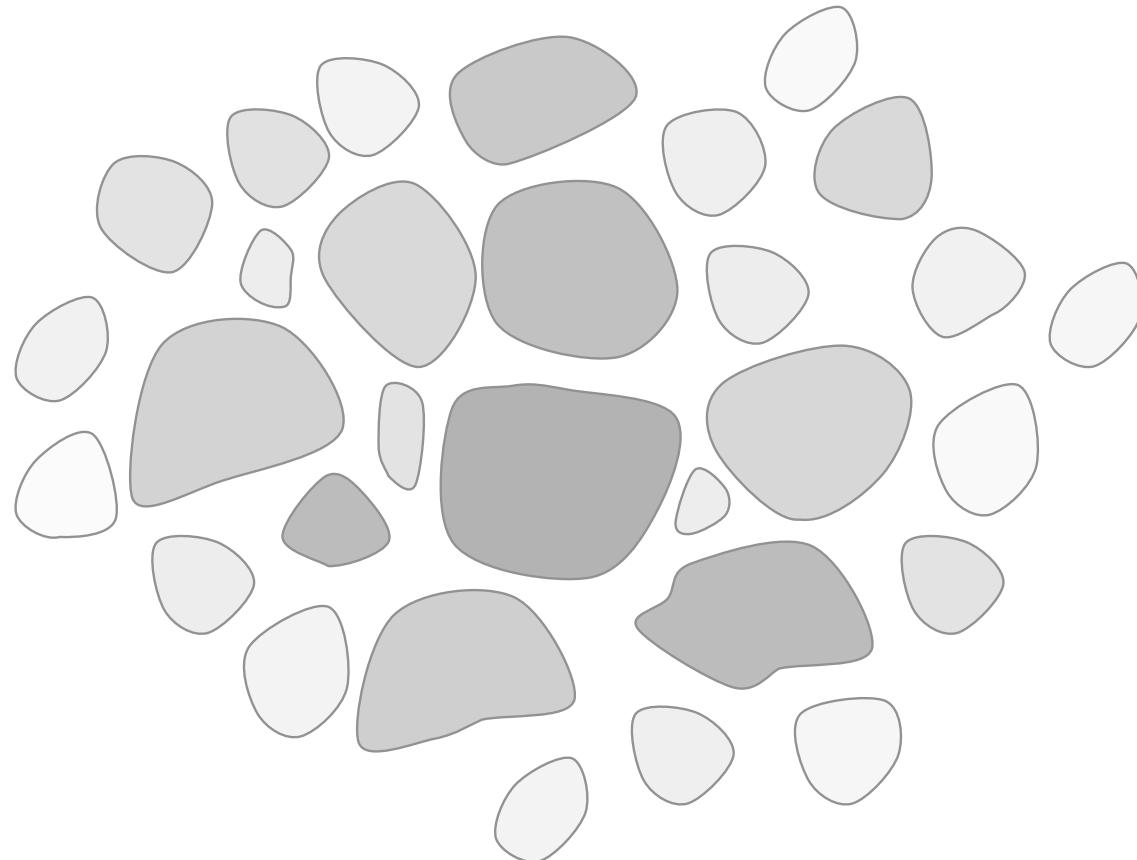
--> *dense cluster with high-mass stars*



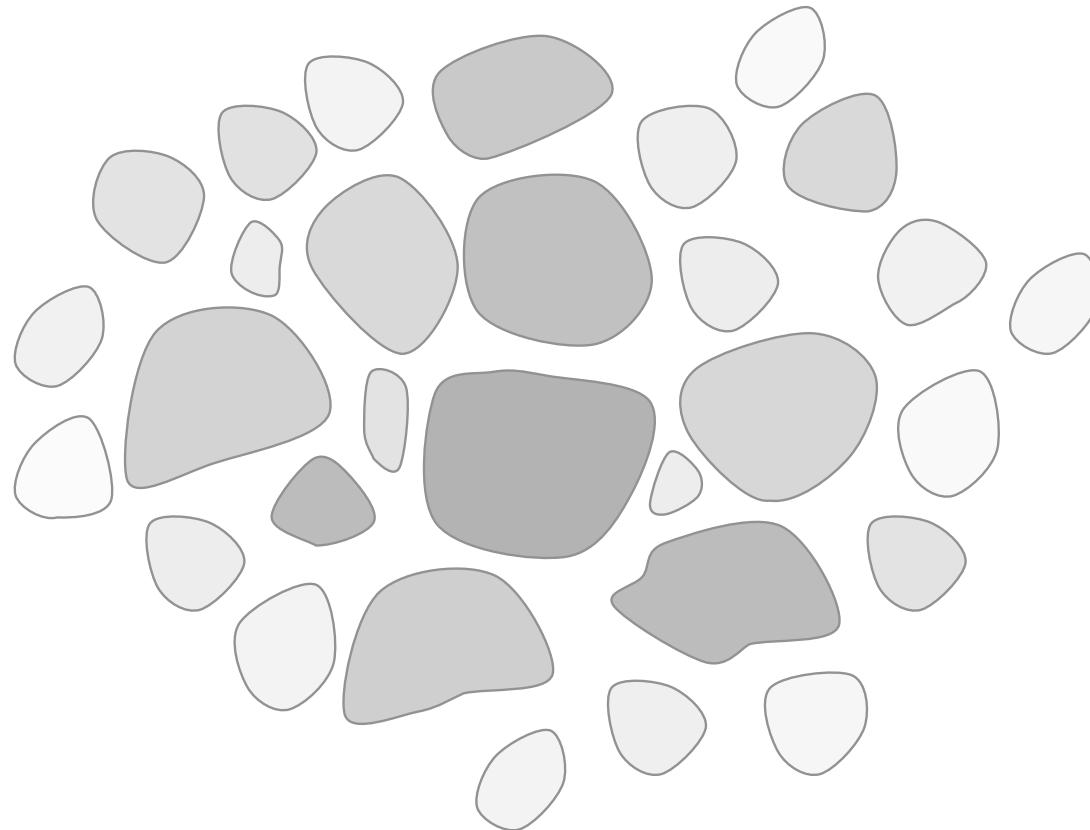
turbulence creates a hierarchy of clumps



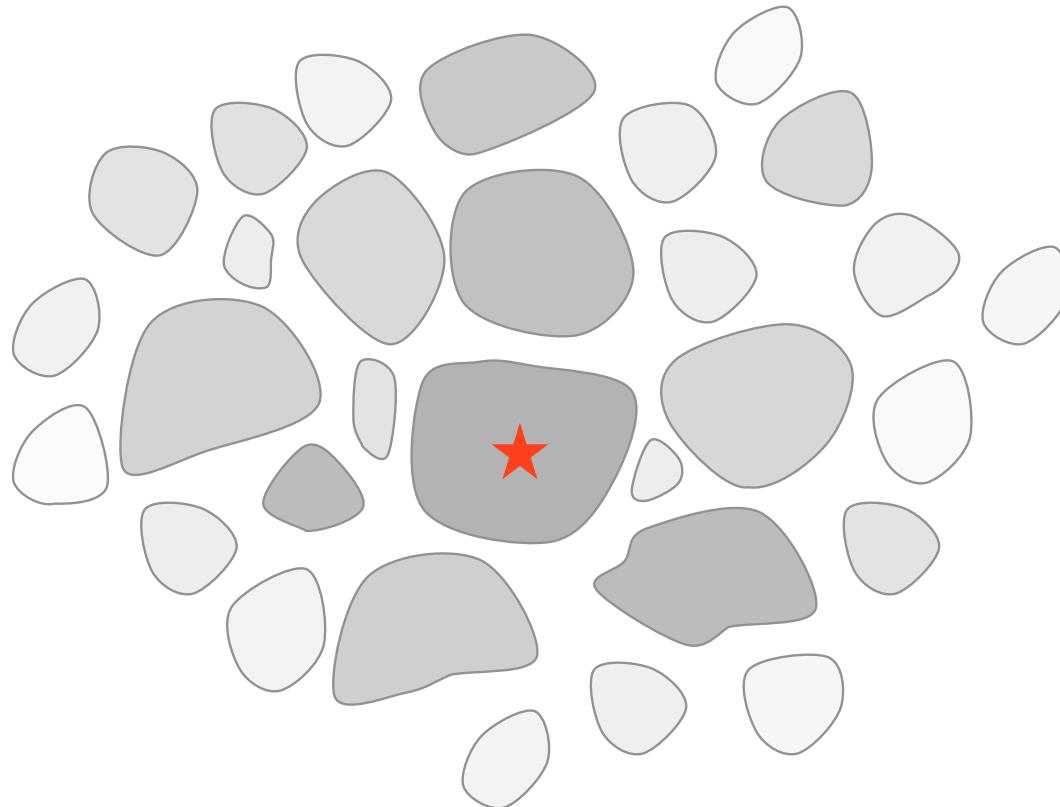
as turbulence decays locally, contraction sets in



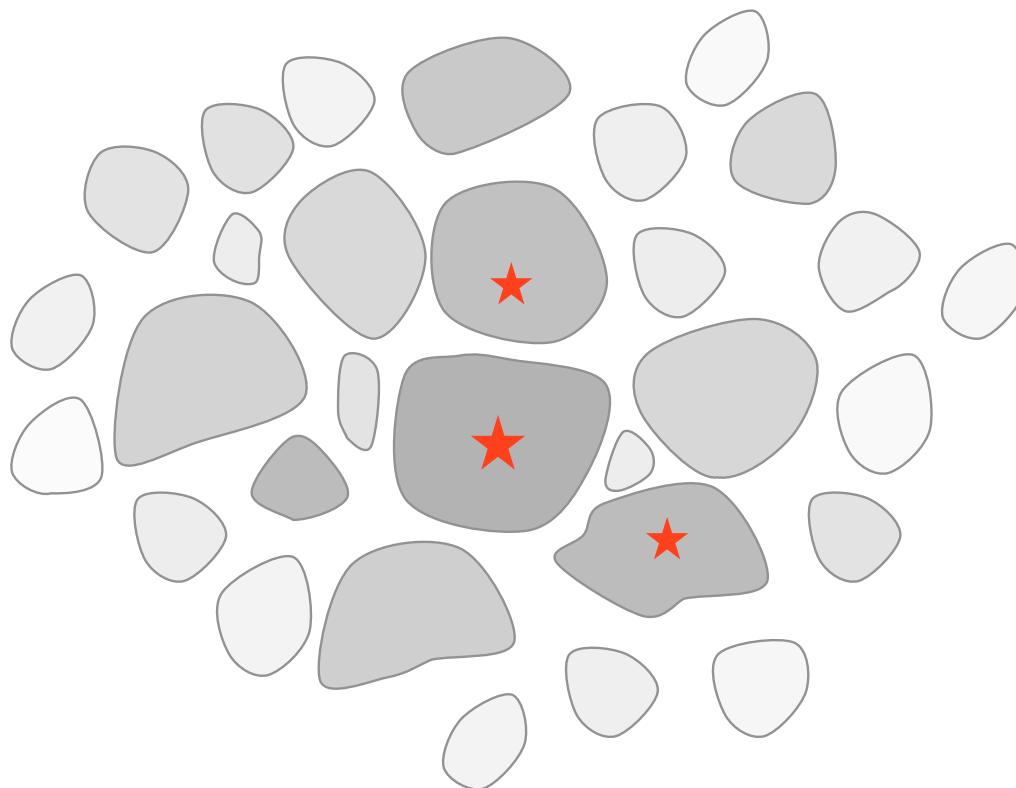
as turbulence decays locally, contraction sets in



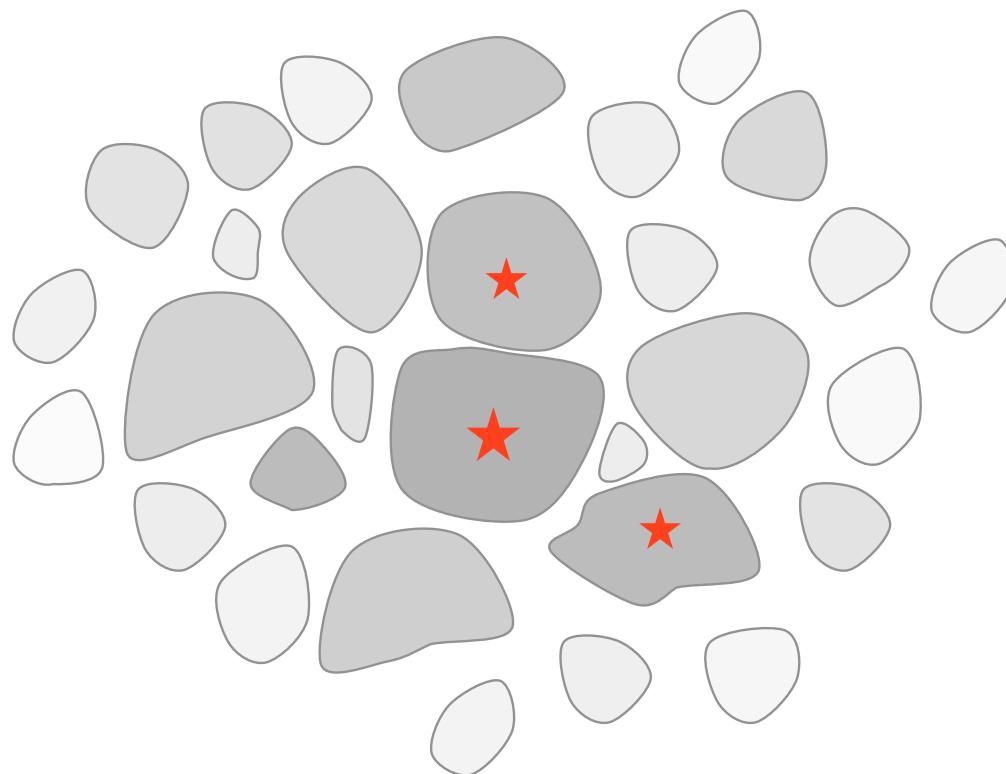
while region contracts, individual clumps collapse to form stars



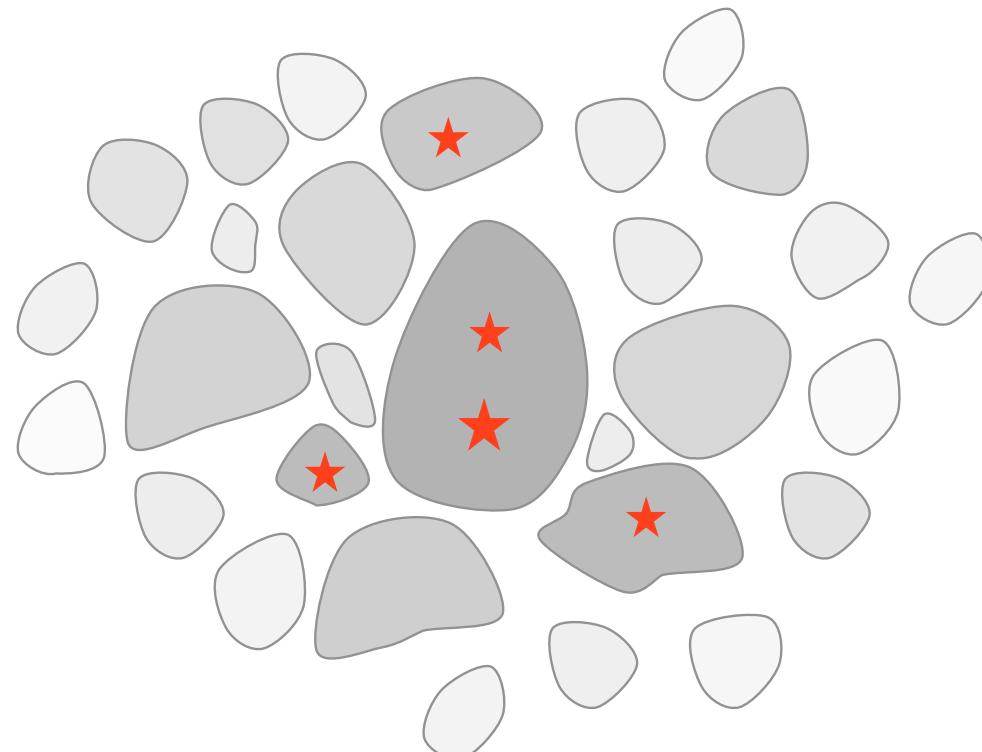
while region contracts, individual clumps collapse to form stars



individual clumps collapse to form stars

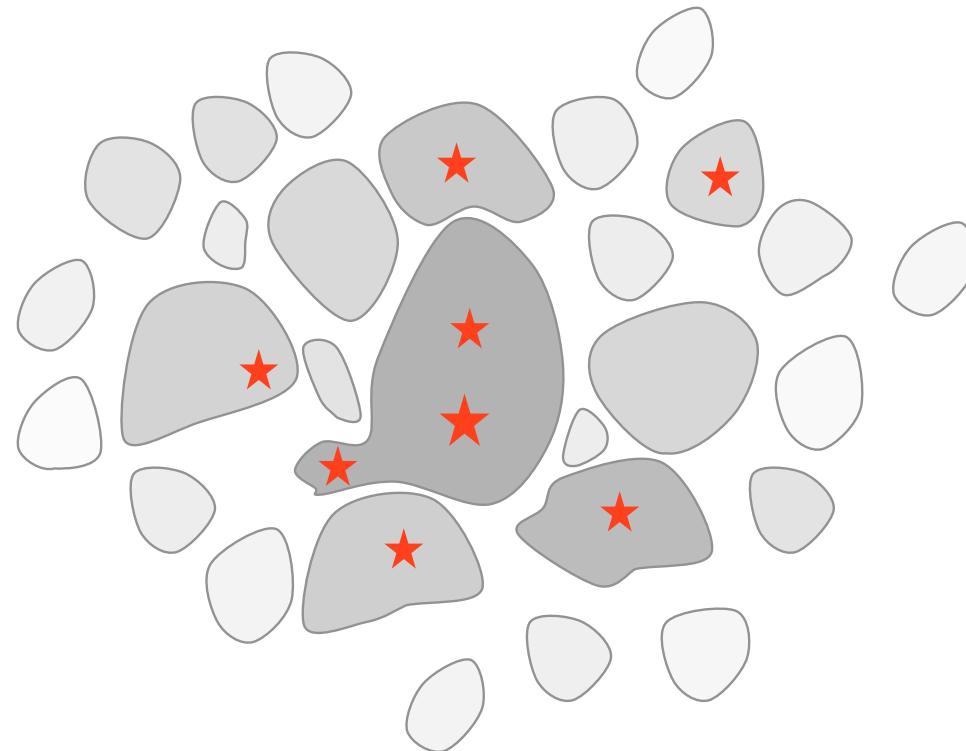


individual clumps collapse to form stars

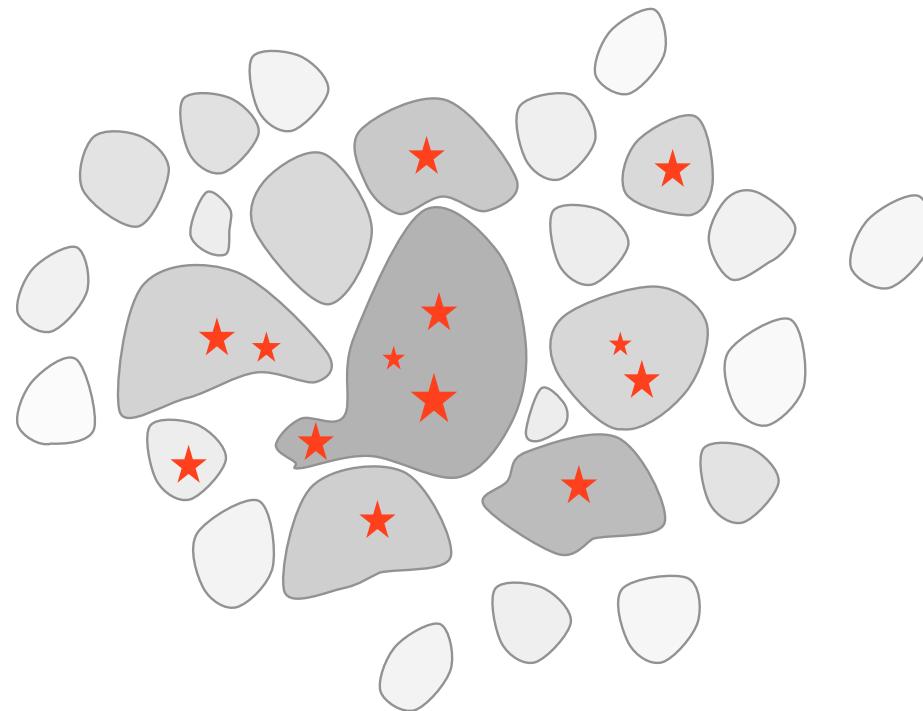


$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

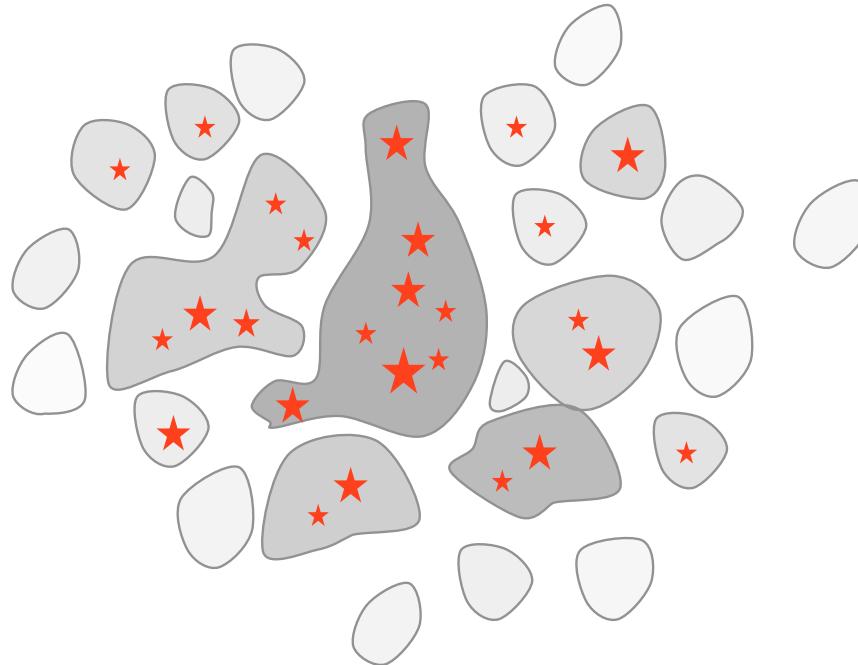
in *dense clusters*, clumps may merge while collapsing  
--> then contain multiple protostars



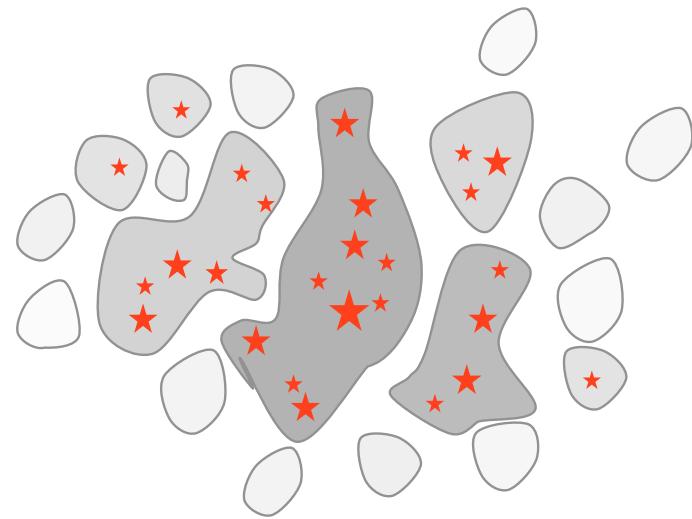
in *dense clusters*, clumps may merge while collapsing  
--> then contain multiple protostars



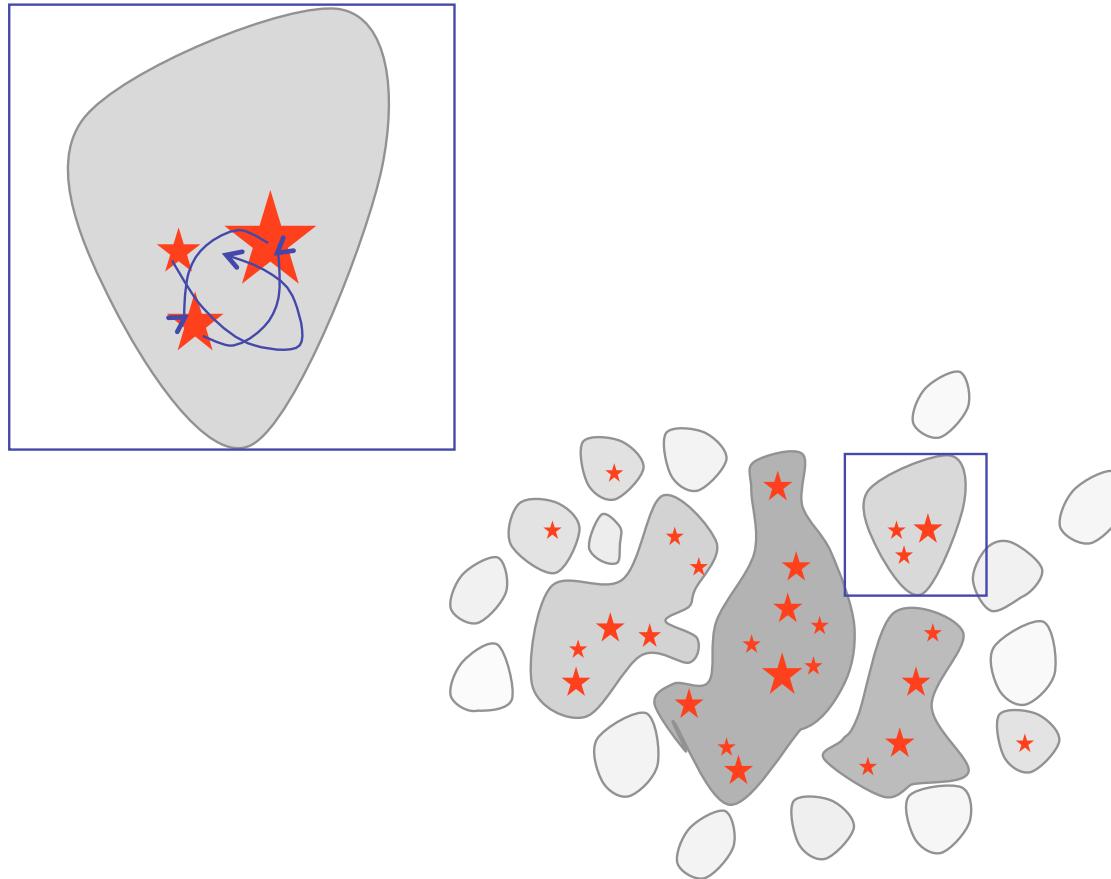
in *dense clusters*, clumps may merge while collapsing  
--> then contain multiple protostars



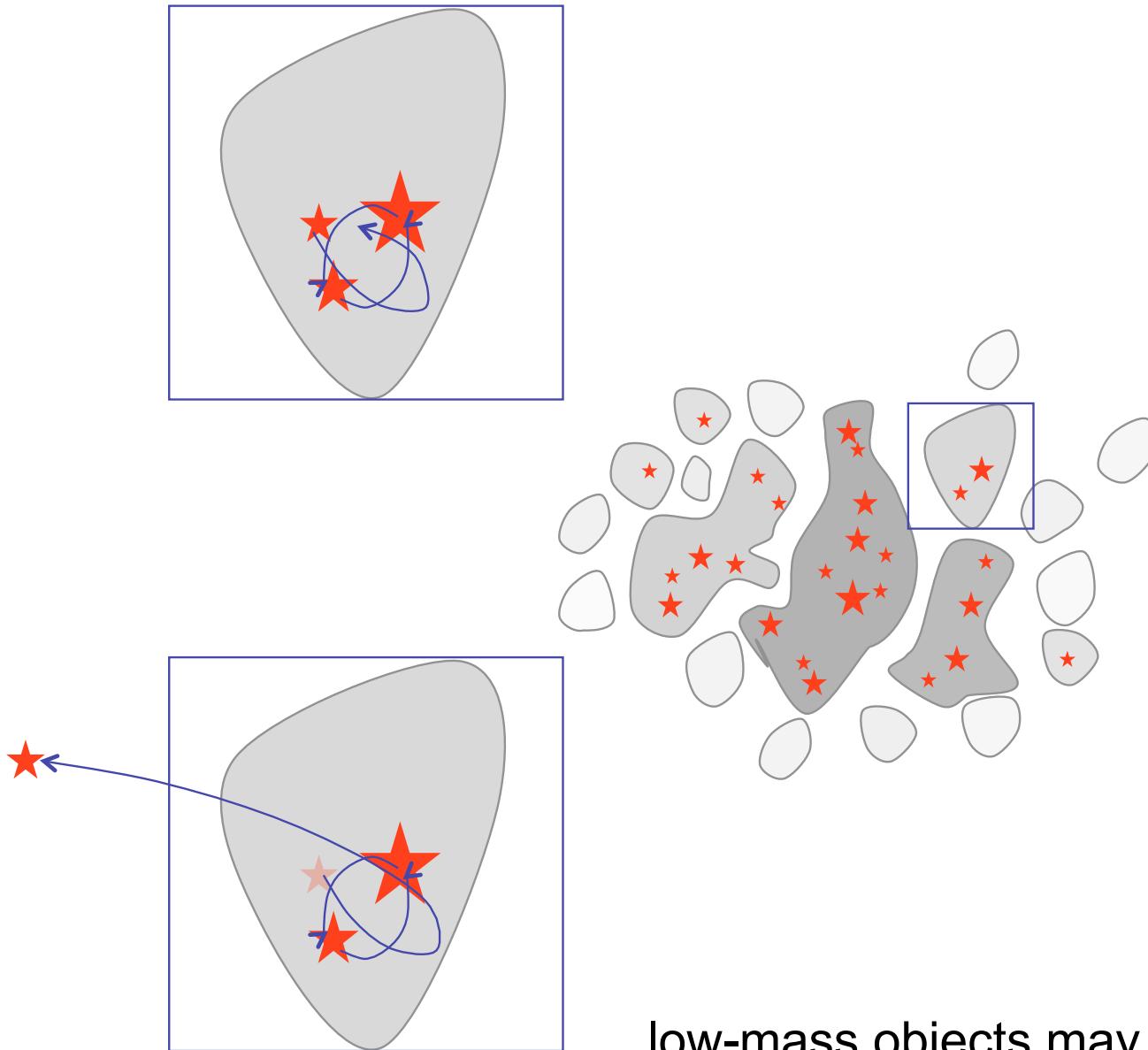
*in dense clusters, competitive mass growth becomes important*



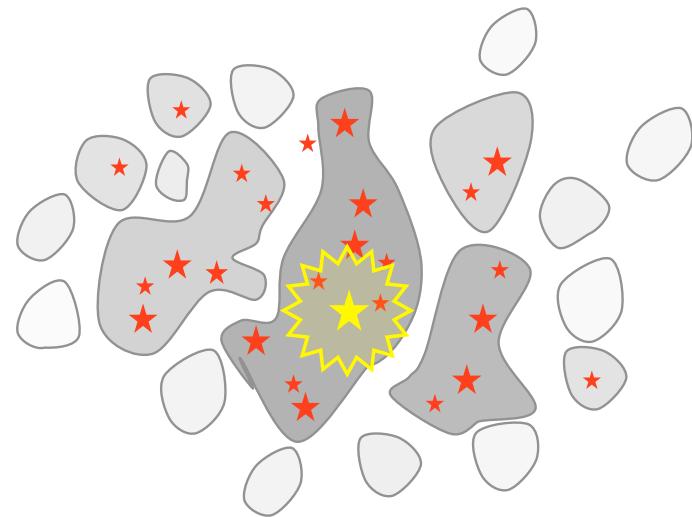
*in dense clusters, competitive mass growth becomes important*



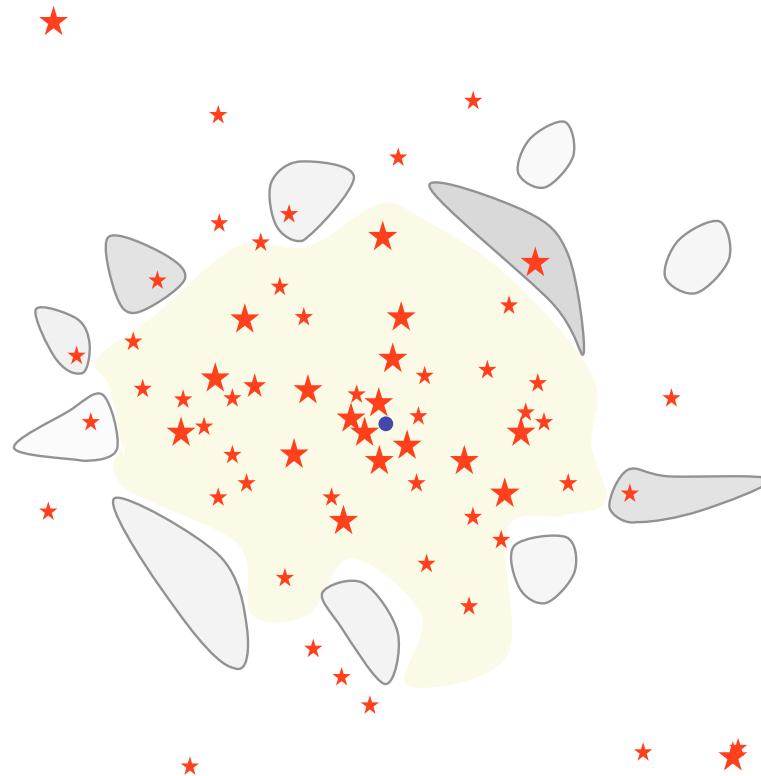
*in dense clusters, N-body effects influence mass growth*



low-mass objects may  
become ejected --> accretion stops



**feedback terminates star formation**



result: *star cluster*, possibly with H<sub>II</sub> region

predictions

# Predictions

- *global properties* (statistical properties)
  - SF efficiency and timescale
  - stellar mass function -- IMF
  - dynamics of young star clusters
  - description of self-gravitating turbulent systems (pdf's,  $\Delta$ -var.)
  - chemical mixing properties
- *local properties* (properties of individual objects)
  - properties of individual clumps (e.g. shape, radial profile, lifetimes)
  - accretion history of individual protostars ( $dM/dt$  vs.  $t$ ,  $j$  vs.  $t$ )
  - binary (proto)stars (eccentricity, mass ratio, etc.)
  - SED's of individual protostars
  - dynamic PMS tracks:  $T_{\text{bol}}\text{-}L_{\text{bol}}$  evolution

# Examples and predictions

*example 1:* star cluster formation: *dynamics*

*example 2:* star cluster formation: *thermodynamics*

--> speculations on the origin of the stellar  
mass spectrum (IMF)

example<sup>1</sup>

# Example: model of Orion cloud

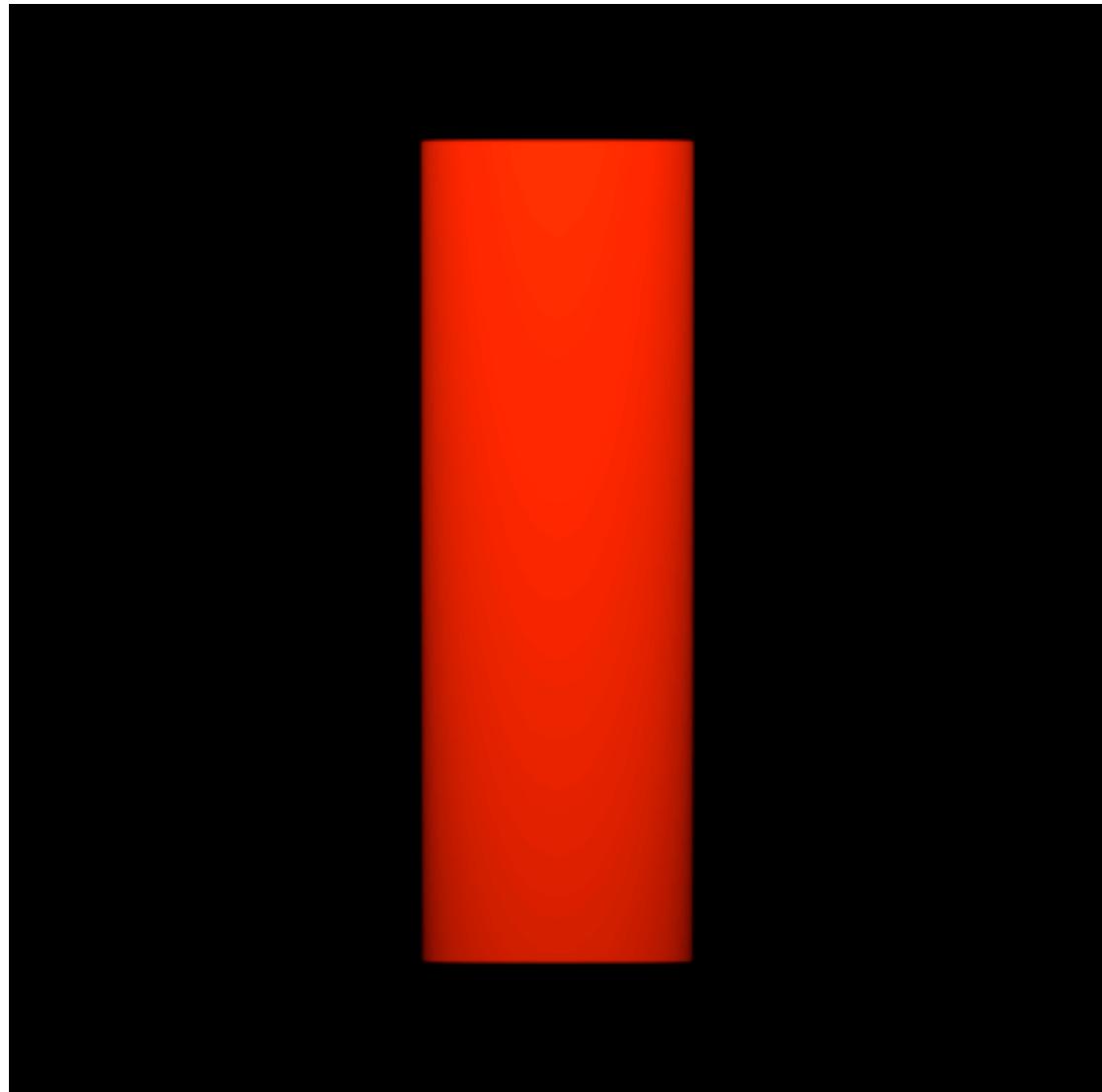
„model“ of Orion cloud:  
15.000.000 SPH particles,  
 $10^4 M_{\text{sun}}$  in 10 pc, mass  
resolution  $0,02 M_{\text{sun}}$ , forms  
 $\sim 2.500$  „stars“ (sink particles)

isothermal EOS, top bound,  
bottom unbound

has clustered as well as  
distributed „star“ formation

efficiency varies from 1% to  
20%

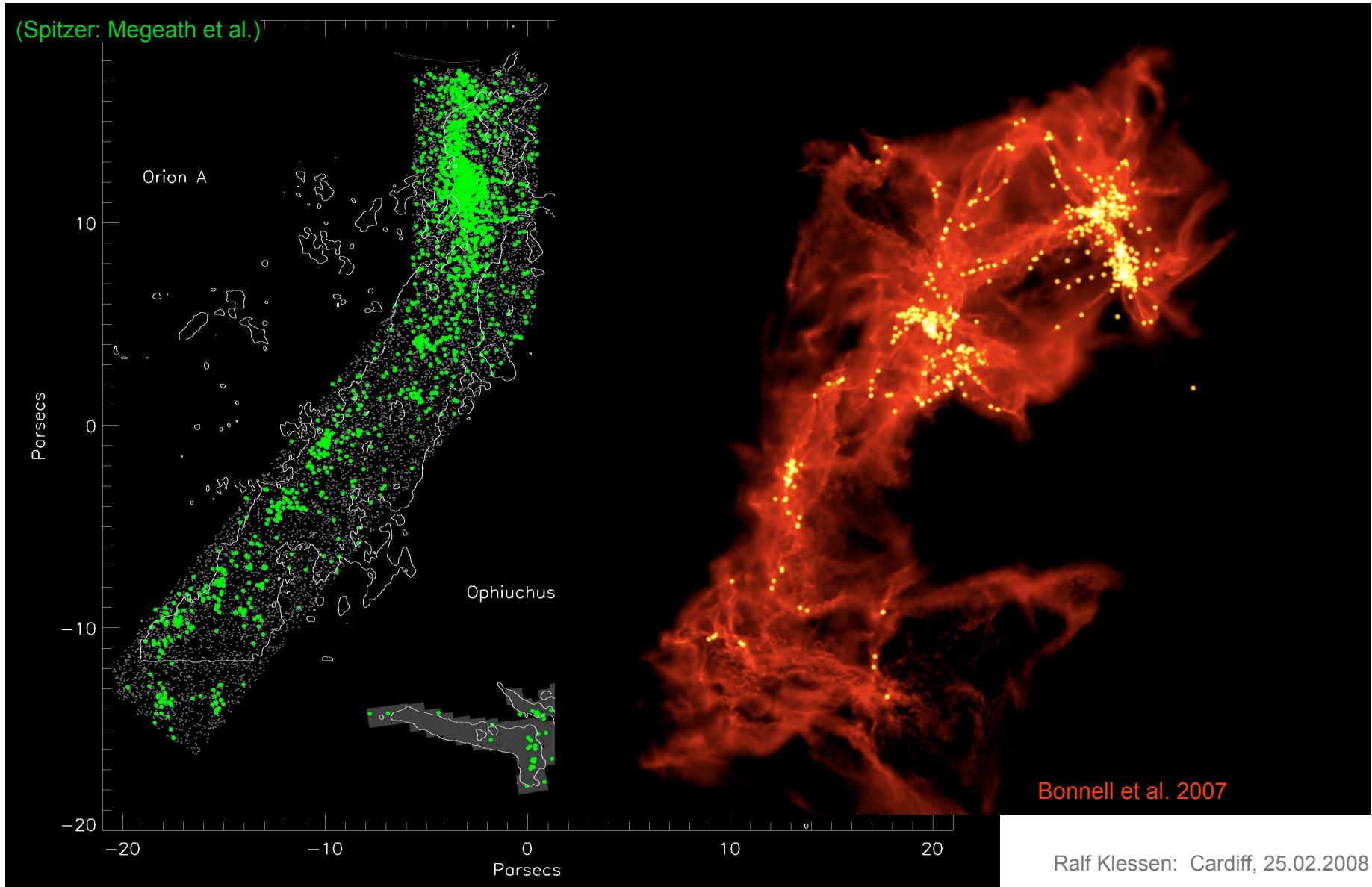
develops full IMF  
(distribution of sink particle masses)



(Bonnell et al. 2007)

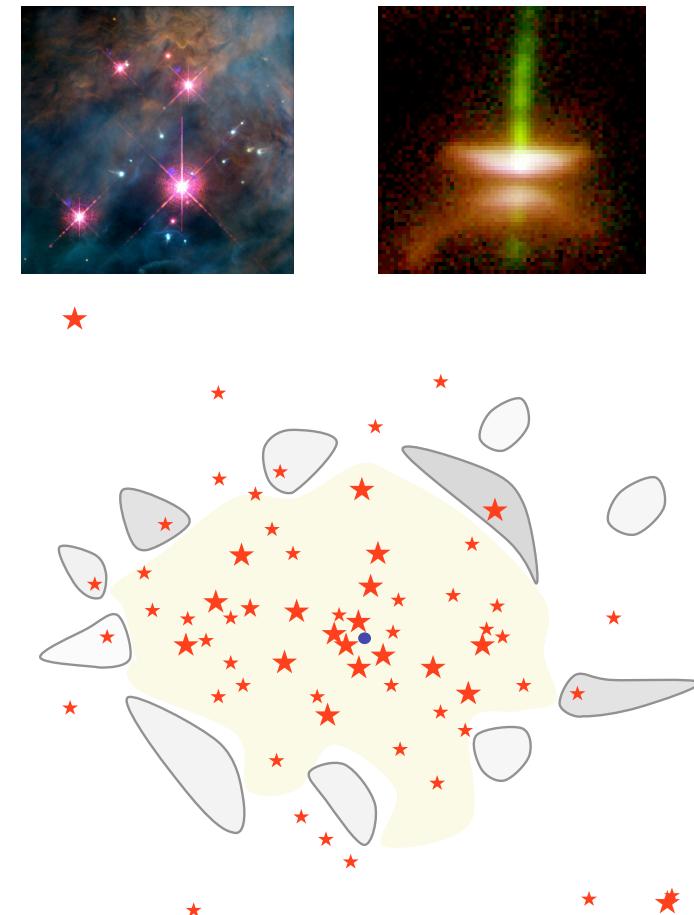
Ralf Klessen: Cardiff, 25.02.2008

# Example: model of Orion cloud



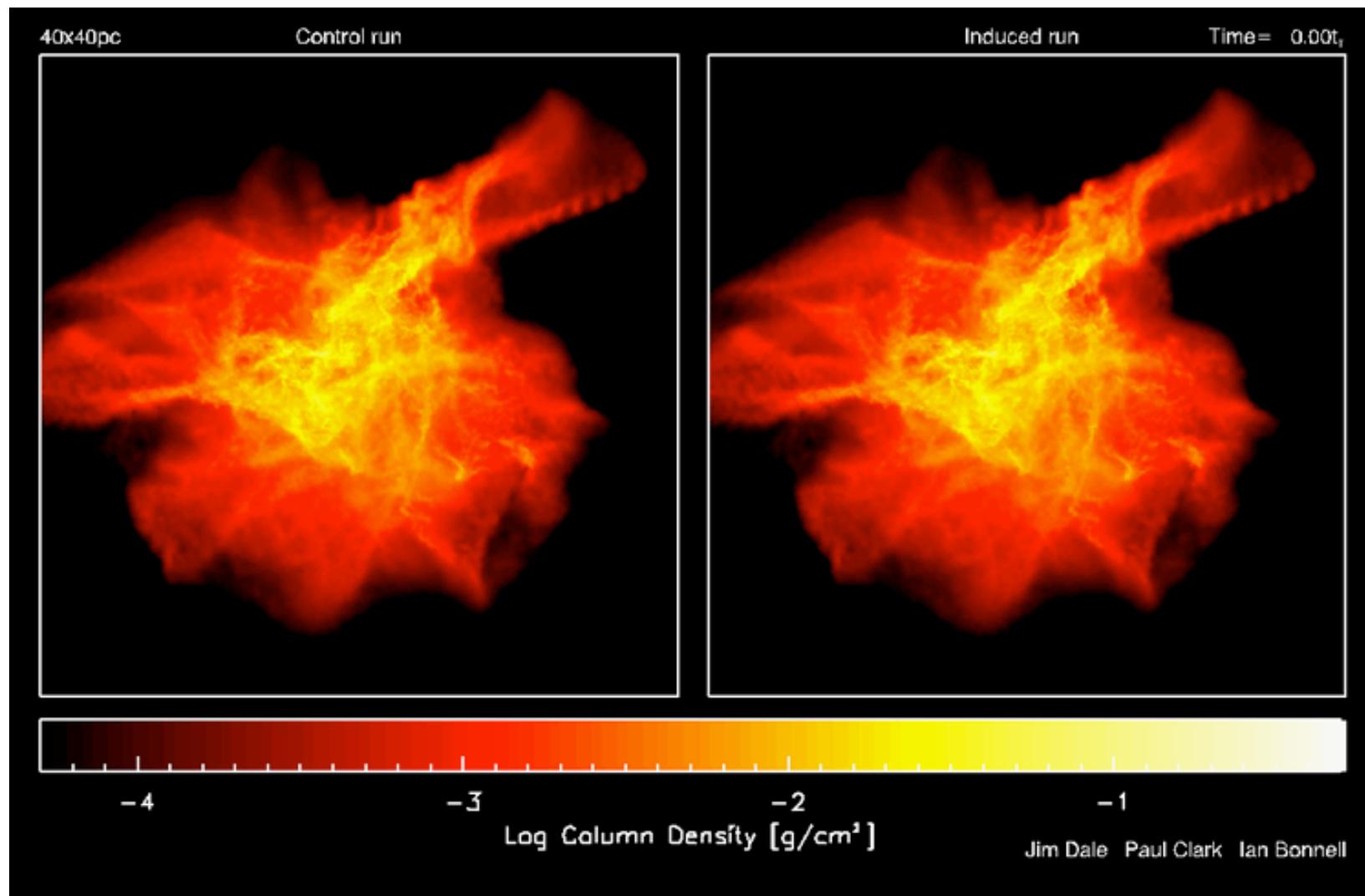
# Models of star cluster formation

- dynamics:  
basic properties are  
probably okay
- BUT: no feedback  
(outflows, radiation, etc.)
- *how much detail are  
we missing?*
  - how does that change  
properties like *IMF*,  
*boundedness, efficiency?*



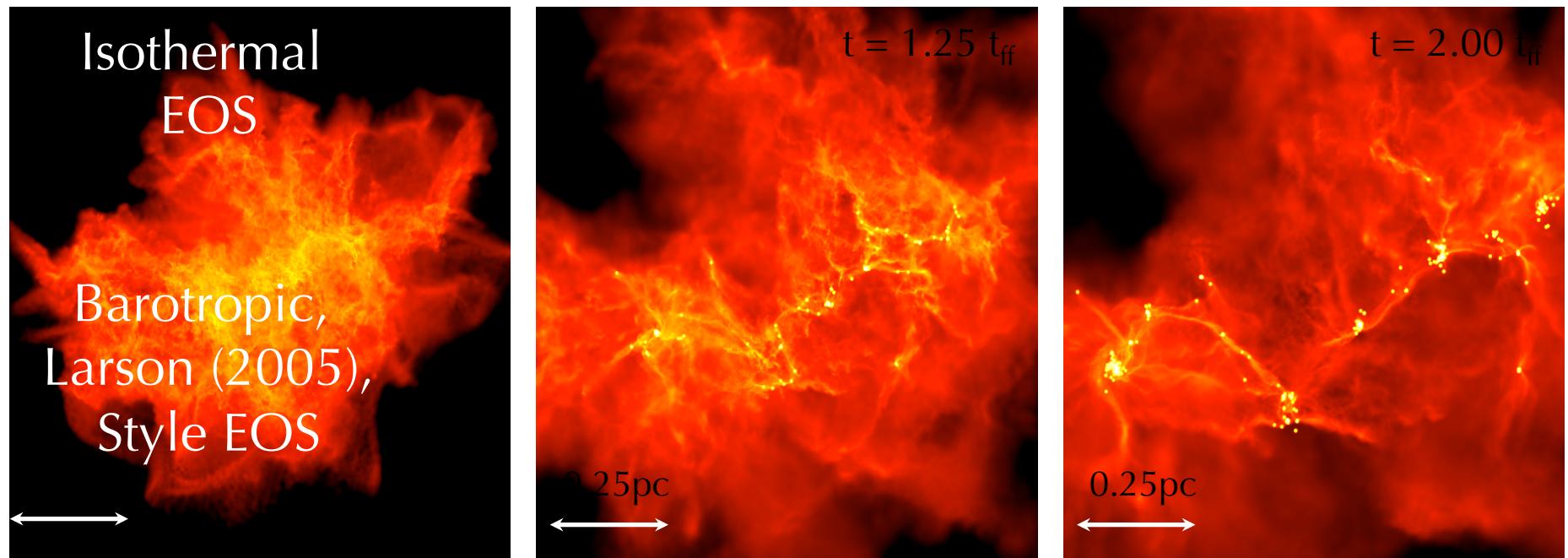
# Model with ionizing feedback

SPH with radiation feedback: first calculations of star-cluster formation with ionization



# Unbound clouds

KE = 2 x PE (initially), 1000 solar masses, 0.5pc



**No global collapse:**

local  $t_{\text{ff}} <$  global interaction time  
-scale

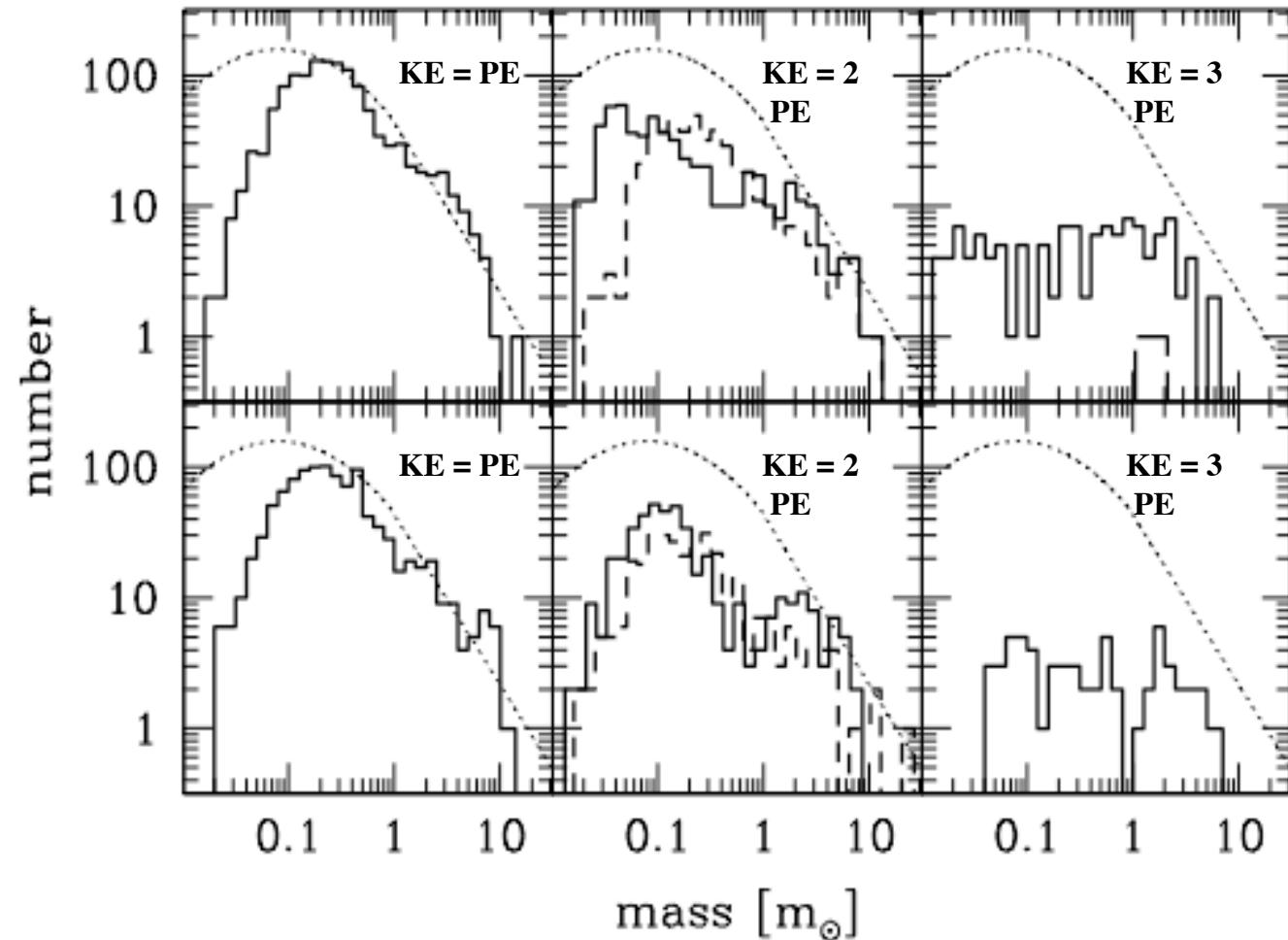
$$t_{\text{ff}} \sim 2 \times 10^5 \text{ years}$$

Clark, Bonnell & Klessen (2007)

# Mass functions

Isothermal  
EOS

Barotropic,  
Larson  
(2005), Style  
EOS



Clark, Bonnell & Klessen (2007)

example 2

# IMF

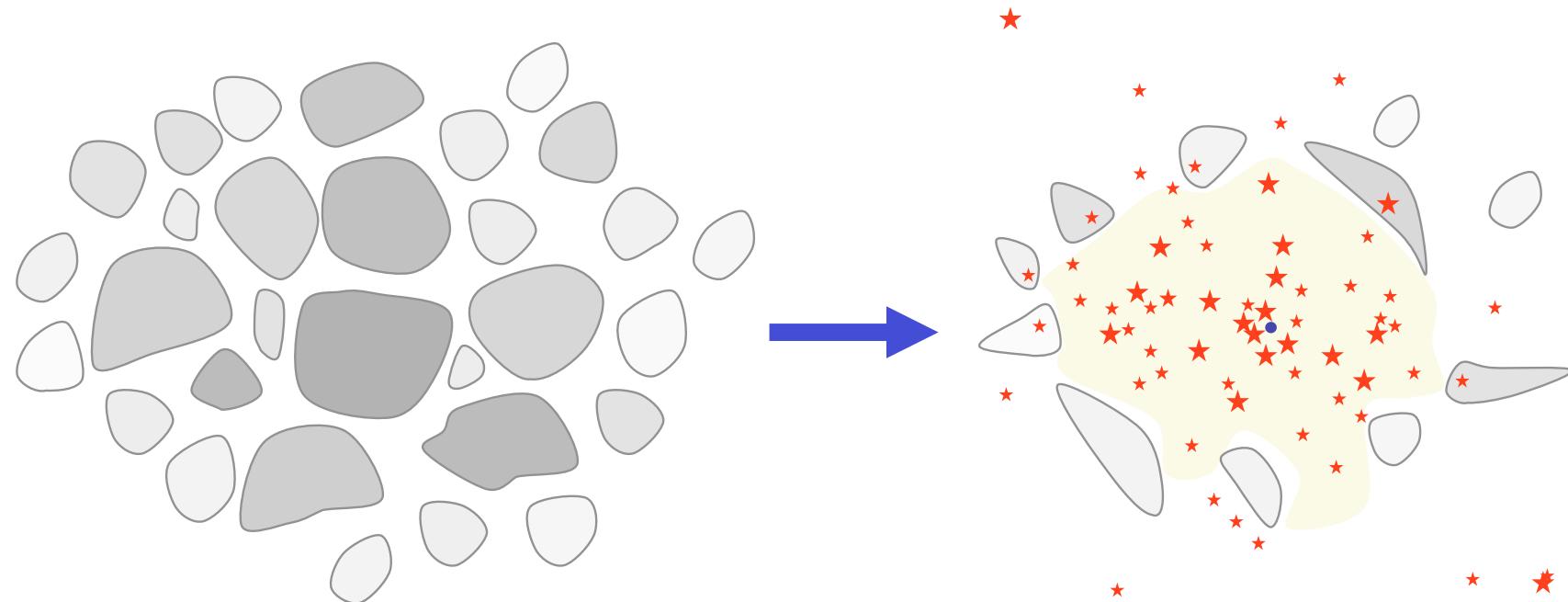
- distribution of stellar masses depends on
  - turbulent initial conditions  
--> mass spectrum of prestellar cloud cores
  - collapse and interaction of prestellar cores  
--> competitive accretion and  $N$ -body effects
  - thermodynamic properties of gas  
--> balance between heating and cooling  
--> EOS (determines which cores go into collapse)
  - (proto) stellar feedback terminates star formation  
ionizing radiation, bipolar outflows, winds, SN

(e.g. Larson 2003, Prog. Rep. Phys.; Mac Low & Klessen, 2004, Rev. Mod. Phys, 76, 125 - 194)

Ralf Klessen: Cardiff, 25.02.2008

# Star cluster formation

Most stars form in clusters → *star formation = cluster formation*



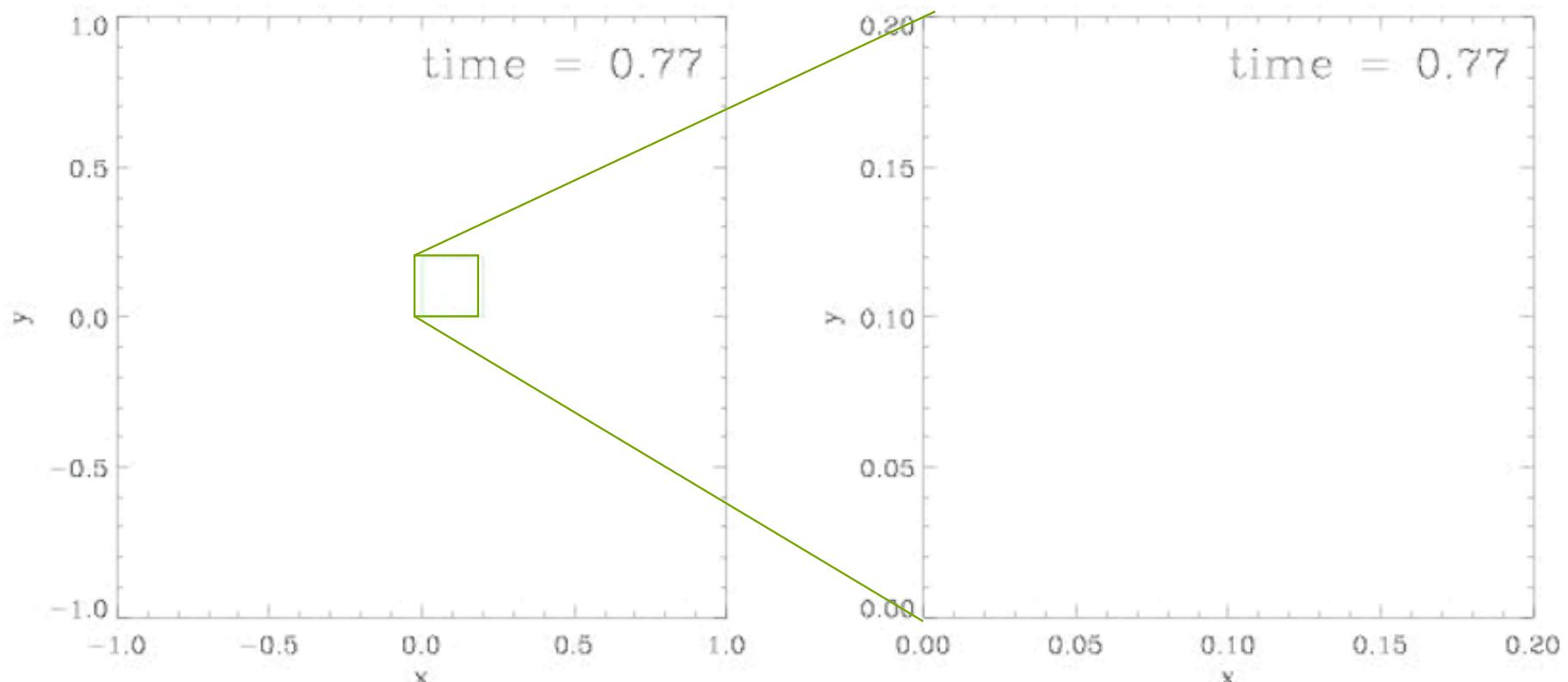
How to get from **cloud cores** to **star clusters**?  
How do the stars **acquire mass**?

(e.g. Larson 2003, Prog. Rep. Phys.; Mac Low & Klessen, 2004, Rev. Mod. Phys, 76, 125 - 194)

Ralf Klessen: Cardiff, 25.02.2008

# Dynamics of nascent star cluster

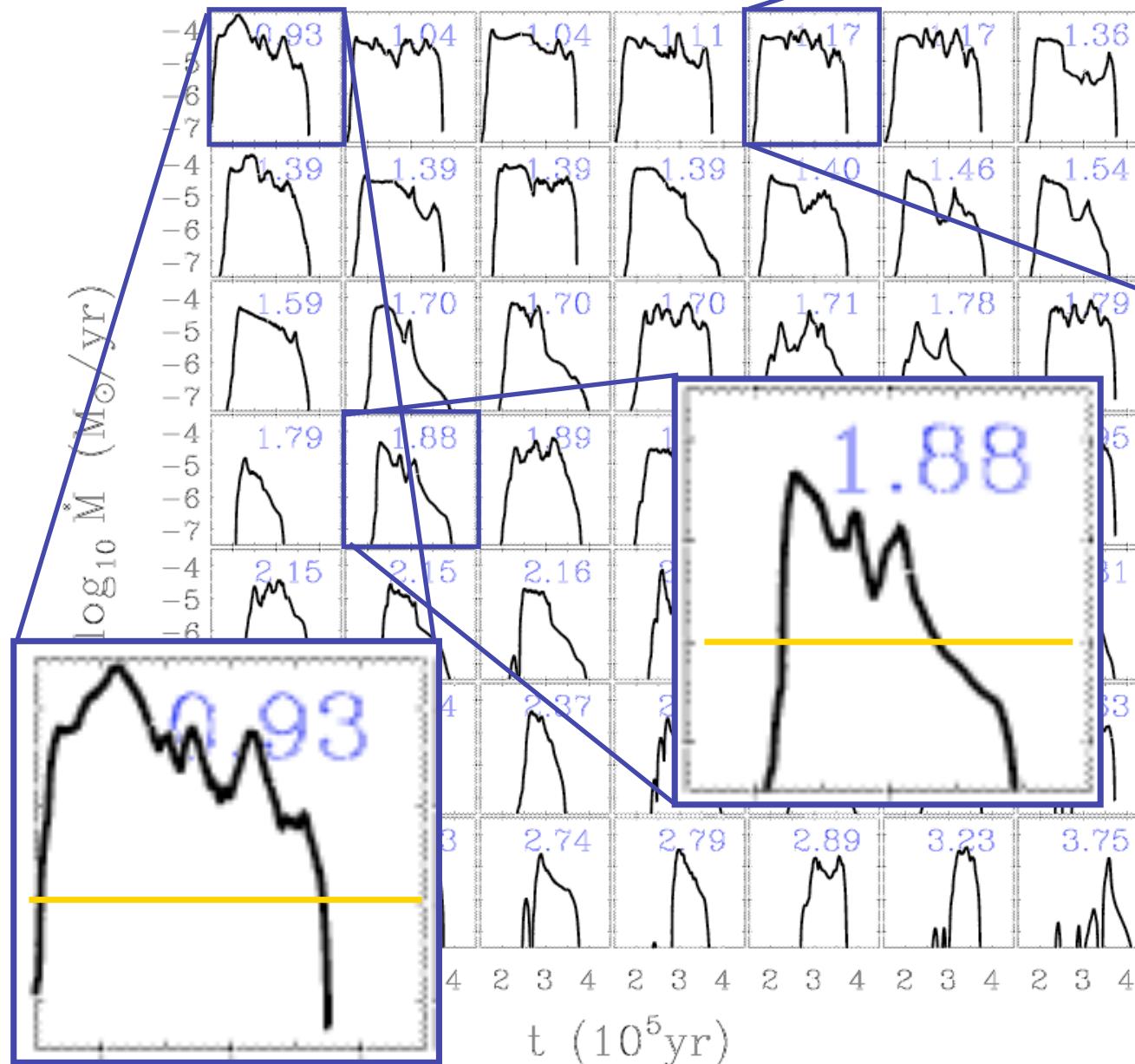
in dense clusters protostellar interaction may be come important!



Trajectories of protostars in a nascent dense cluster created by gravoturbulent fragmentation  
(from Klessen & Burkert 2000, ApJS, 128, 287)

Ralf Klessen: Cardiff, 25.02.2008

# Accretion rates in clusters



Mass accretion rates *vary with time* and are strongly *influenced* by the *cluster environment*.

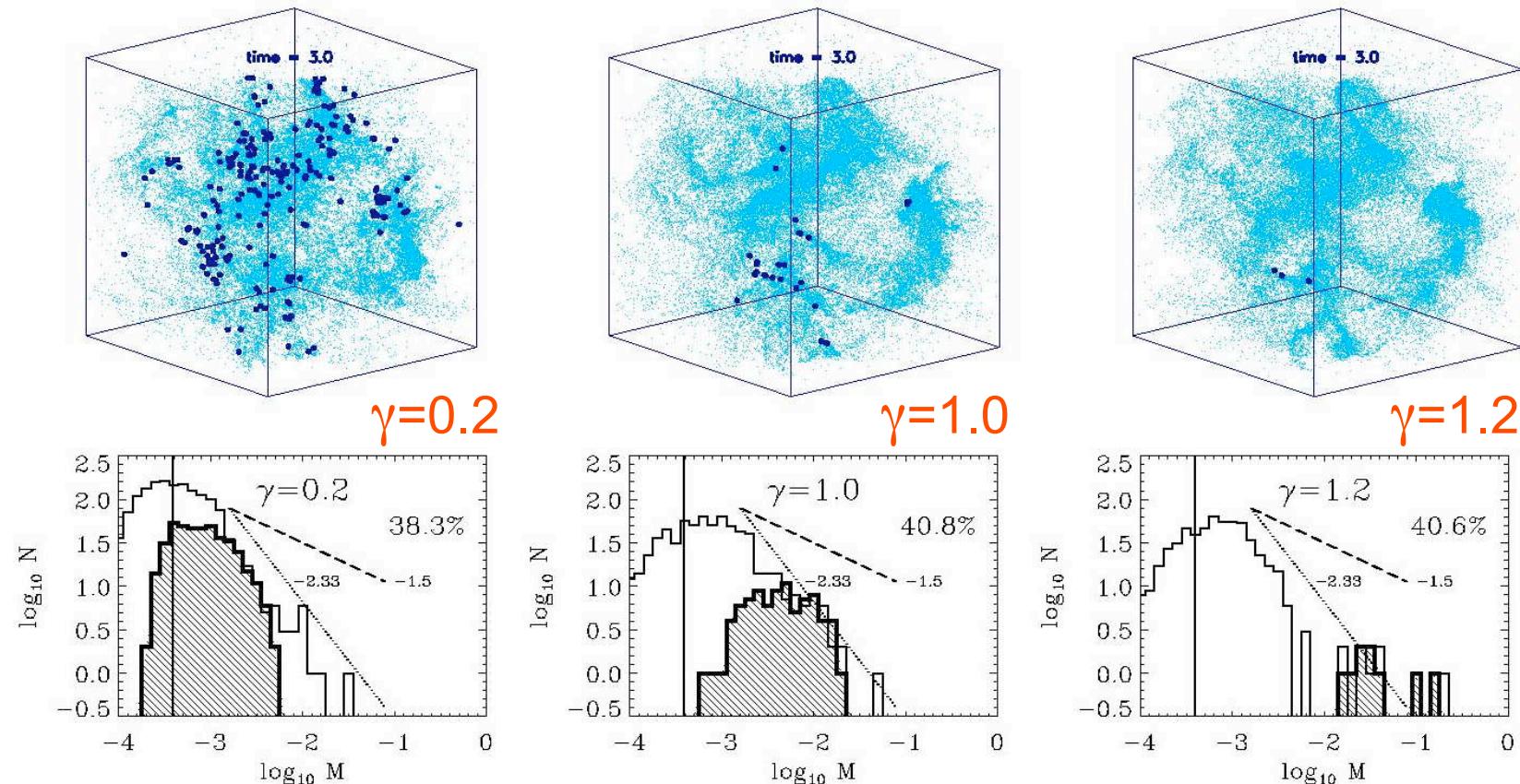
(Klessen 2001, ApJ, 550, L77;  
also Schmeja & Klessen,  
2004, A&A, 419, 405)

# Dependency on EOS

- degree of fragmentation depends on *EOS!*
- polytropic EOS:  $p \propto \rho^\gamma$
- $\gamma < 1$ : dense cluster of low-mass stars
- $\gamma > 1$ : isolated high-mass stars

(see Li, Klessen, & Mac Low 2003, ApJ, 592, 975; also Kawachi & Hanawa 1998, Larson 2003)

# Dependency on EOS



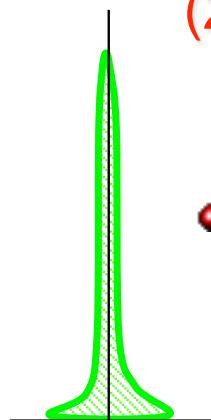
for  $\gamma < 1$  fragmentation is enhanced → *cluster of low-mass stars*  
for  $\gamma > 1$  it is suppressed → formation of *isolated massive stars*

(from Li, Klessen, & Mac Low 2003, ApJ, 592, 975)

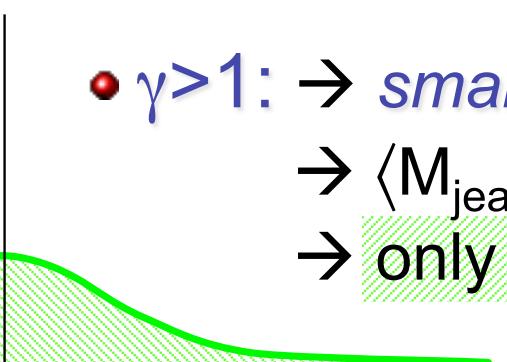
# How does that work?

$$(1) \ p \propto \rho^\gamma \rightarrow \rho \propto p^{1/\gamma}$$

$$(2) \ M_{\text{jeans}} \propto \gamma^{3/2} \rho^{(3\gamma-4)/2}$$



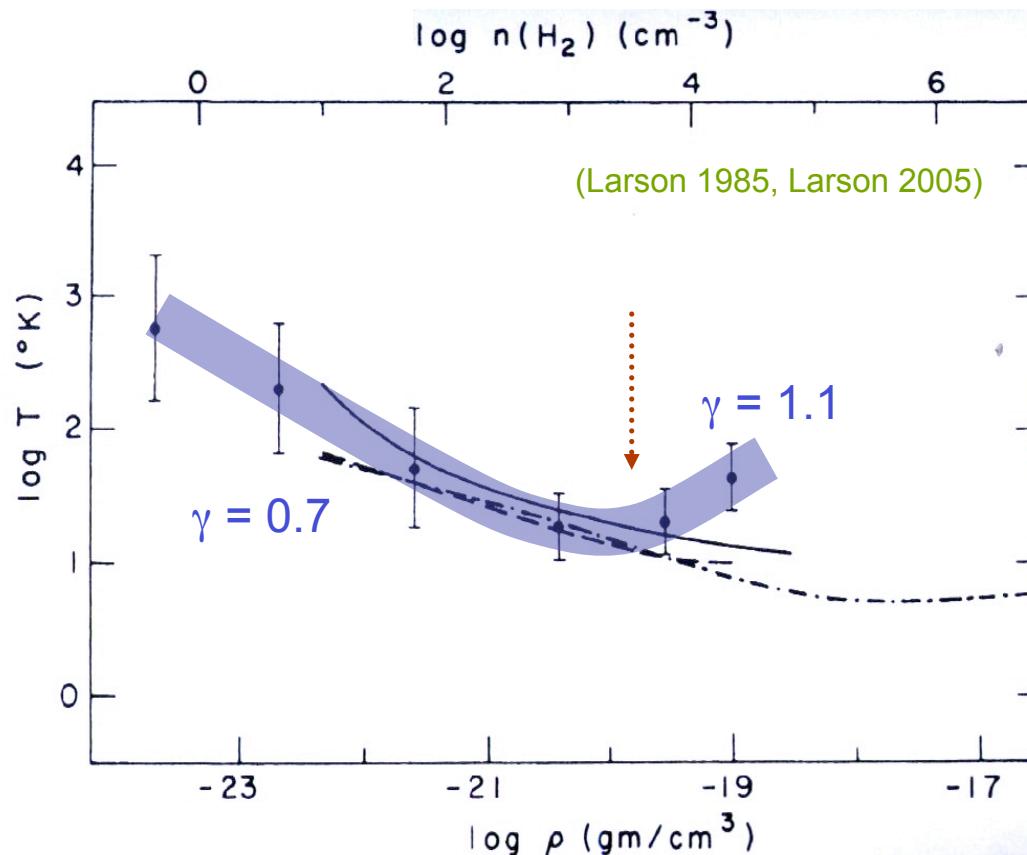
- $\gamma < 1$ : → *large* density excursion for given pressure  
→  $\langle M_{\text{jeans}} \rangle$  becomes small  
→ number of fluctuations with  $M > M_{\text{jeans}}$  is large



- $\gamma > 1$ : → *small* density excursion for given pressure  
→  $\langle M_{\text{jeans}} \rangle$  is large  
→ only few and massive clumps exceed  $M_{\text{jeans}}$

# EOS for solar neighborhood

below  $10^{-18} \text{ gcm}^{-3}$ :  $\rho \uparrow \longrightarrow T \downarrow$   
above  $10^{-18} \text{ gcm}^{-3}$ :  $\rho \uparrow \longrightarrow T \uparrow$



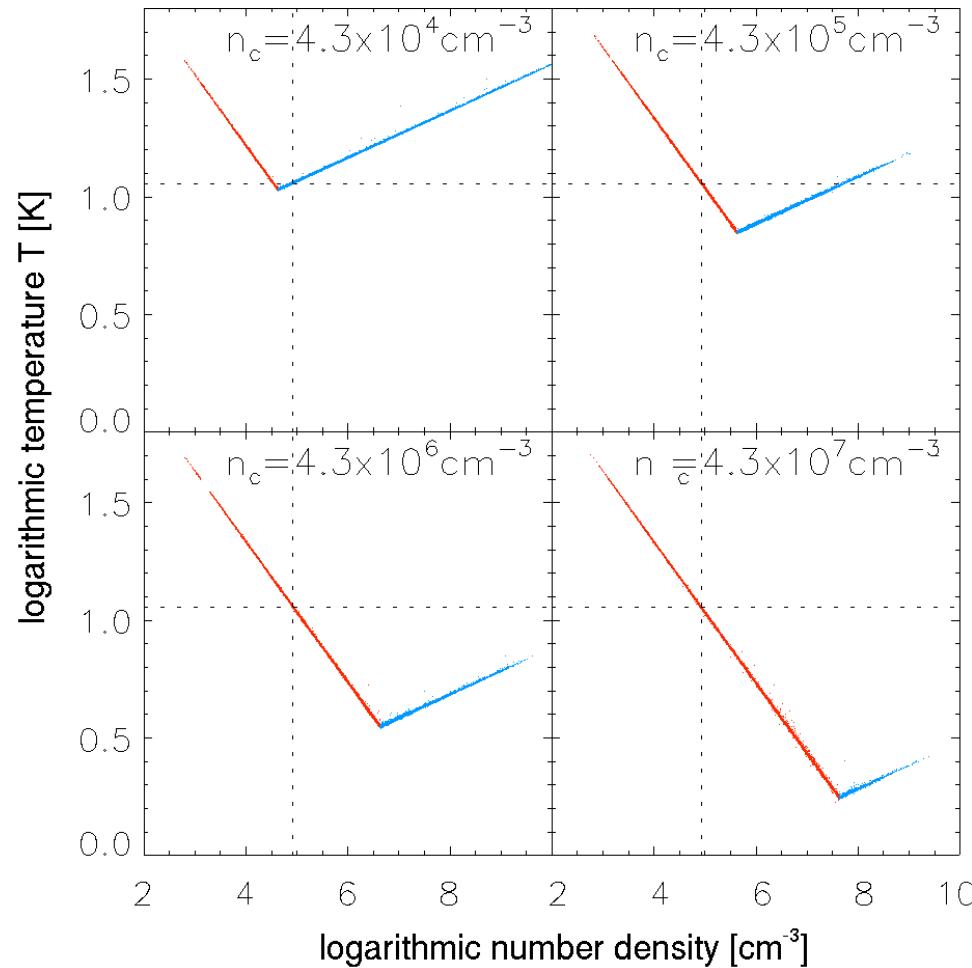
$$\begin{aligned} P &\propto \rho^\gamma \\ P &\propto \rho T \\ \rightarrow \gamma &= 1 + d \ln T / d \ln \rho \end{aligned}$$

# IMF from simple piece-wise polytropic EOS

$$\gamma_1 = 0.7$$

$$\gamma_2 = 1.1$$

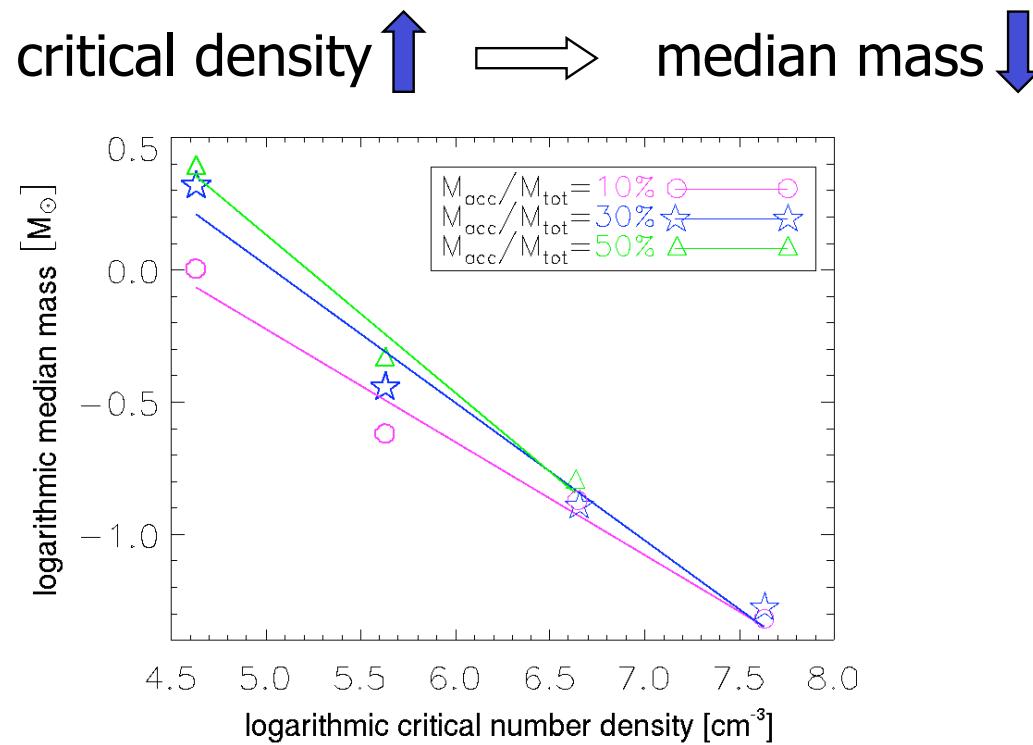
$$T \sim \rho^{\gamma-1}$$



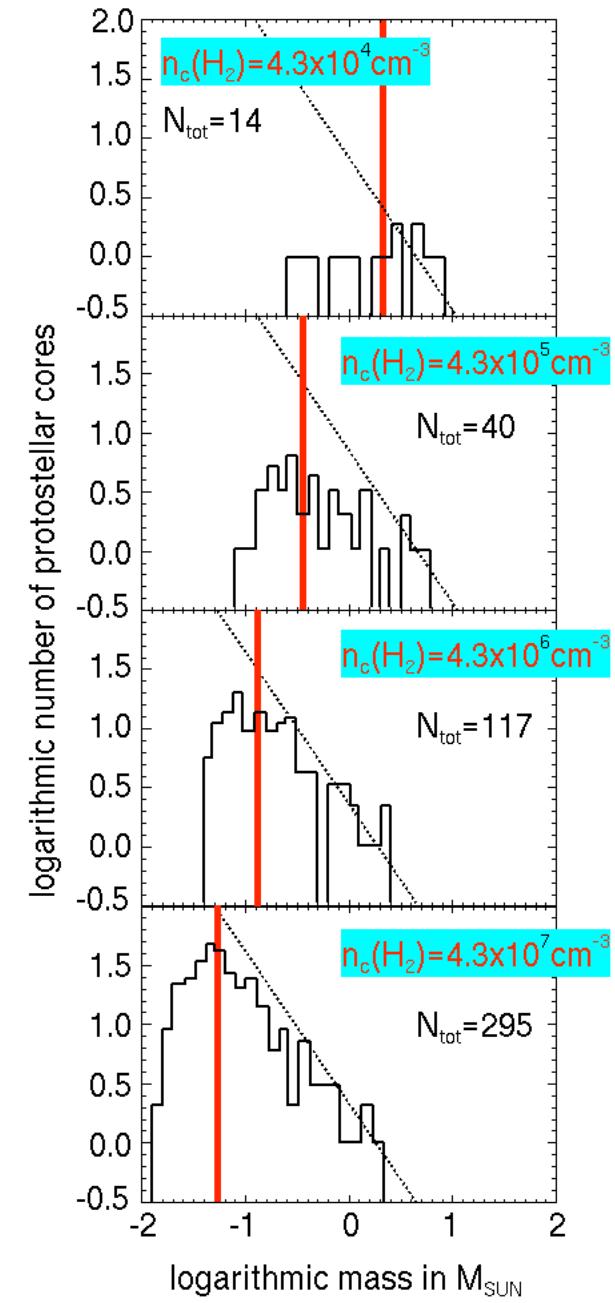
(Jappsen et al. 2005)

Ralf Klessen: Cardiff, 25.02.2008

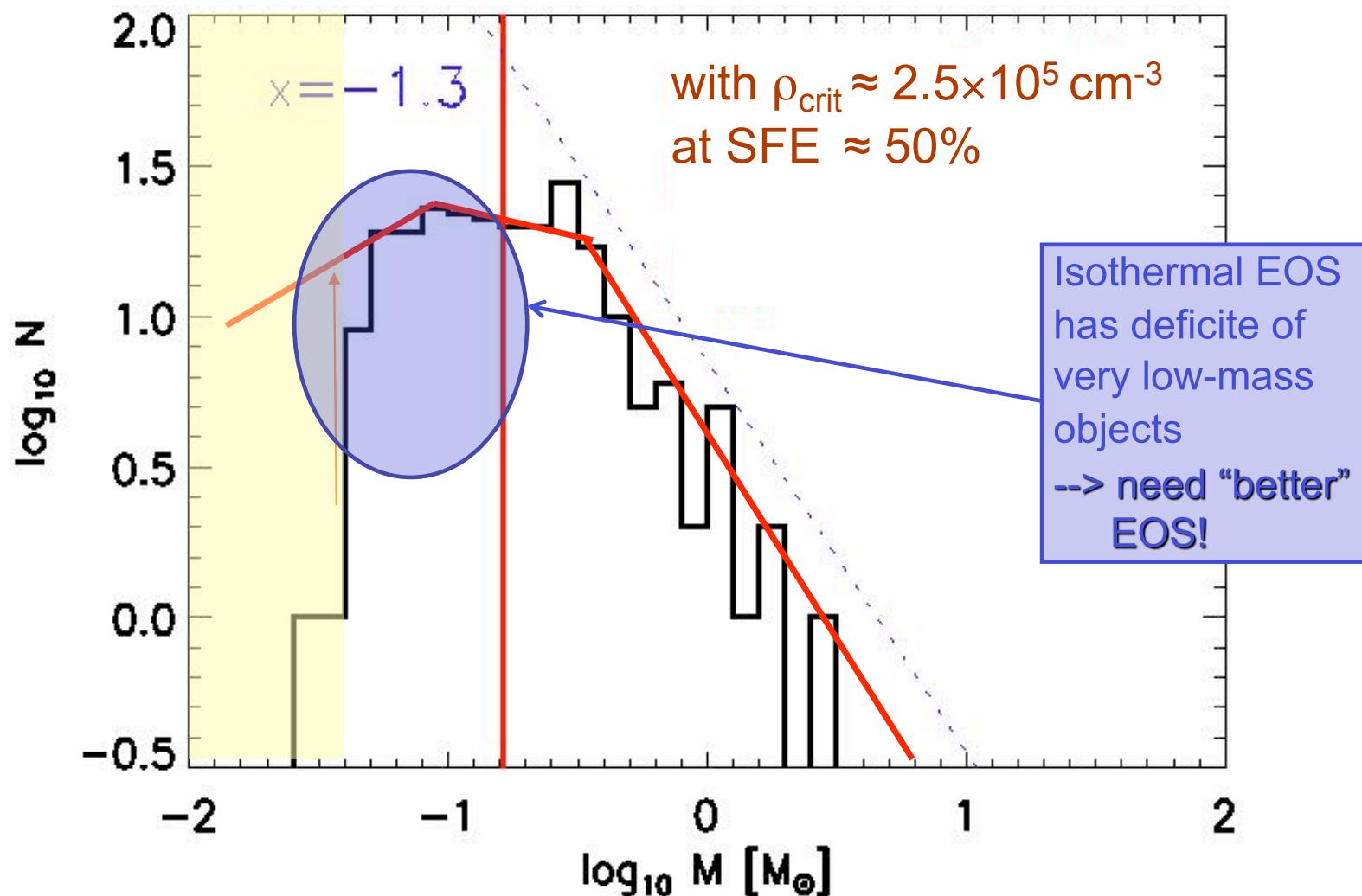
# IMF from simple piece-wise polytropic EOS



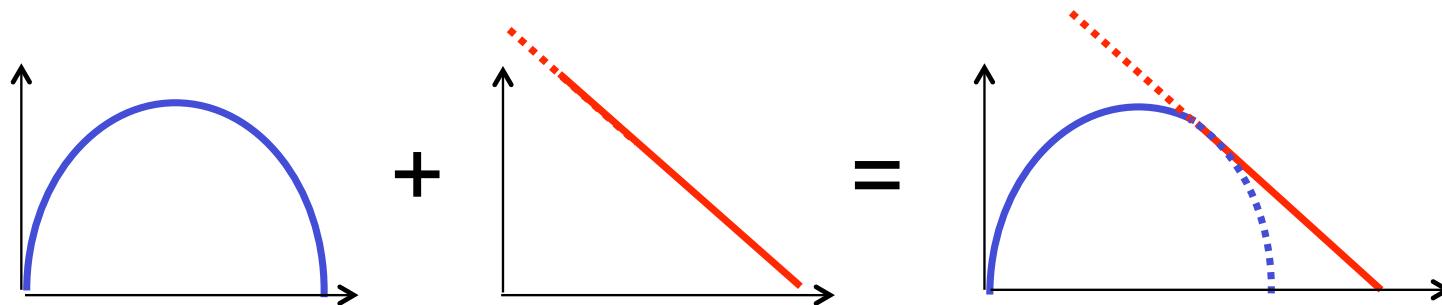
(Jappsen et al. 2005)



# IMF in nearby molecular clouds



# Plausibility argument for shape

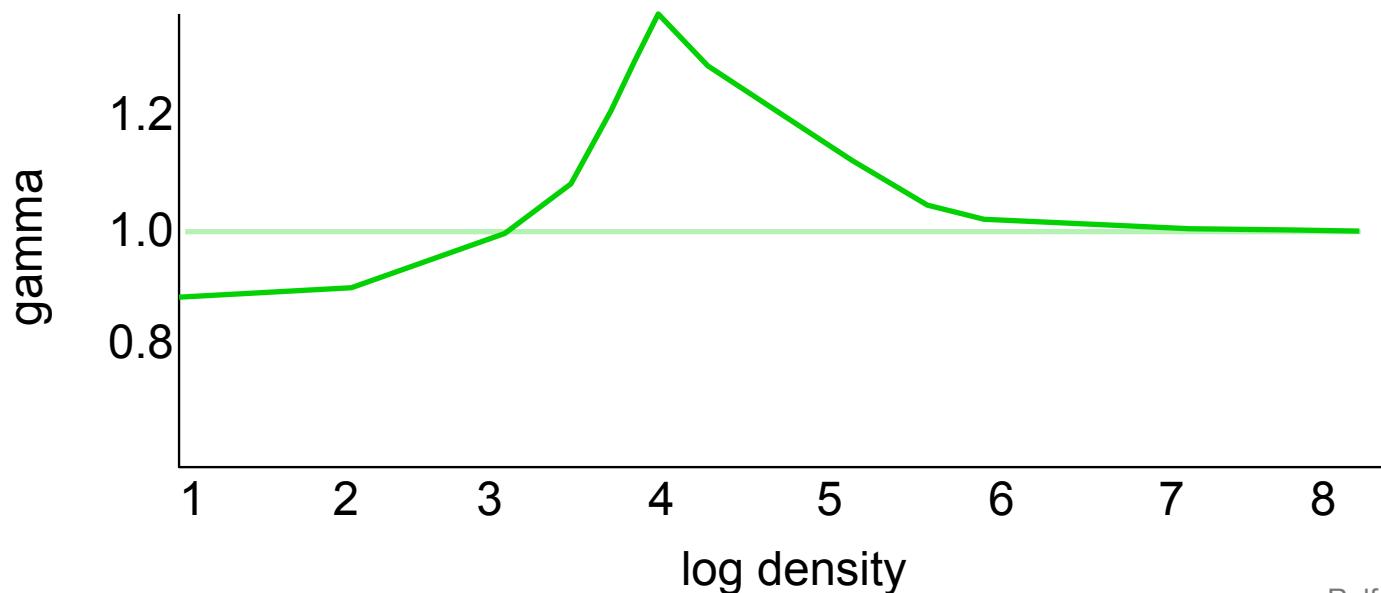


- Supersonic turbulence is scale free process  
→ *POWER LAW BEHAVIOR*
- *But also:* turbulence and fragmentation are highly stochastic processes → central limit theorem  
→ *GAUSSIAN DISTRIBUTION*

# IMF in starburst galaxies

- Nuclear regions of starburst galaxies are extreme:
  - hot dust, large densities, strong radiation, etc.
- Thermodynamic properties of star-forming gas differ from Milky Way --> Different EOS!

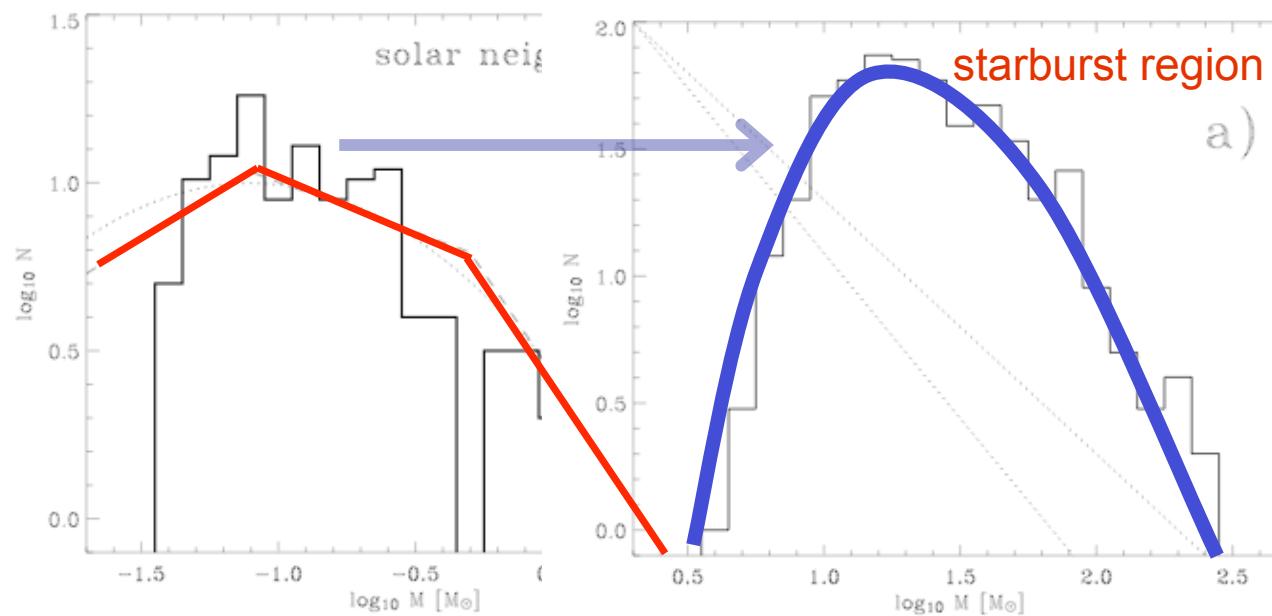
(see Spaans & Silk 2005)



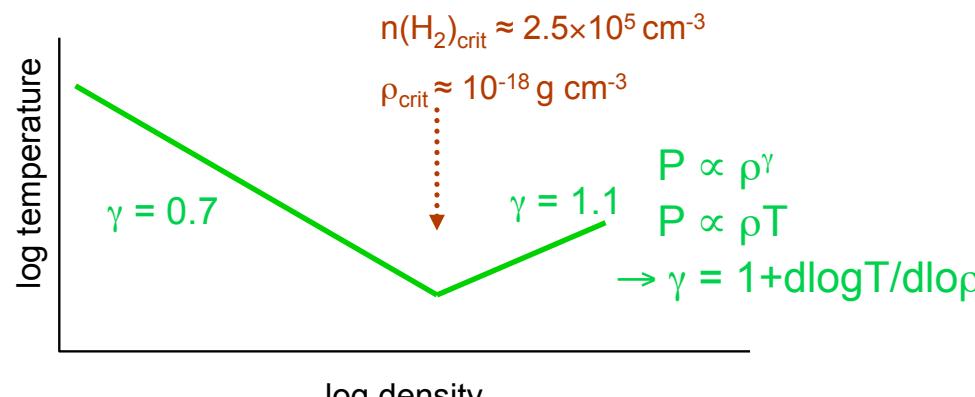
# IMF in starburst galaxies

- Starburst EOS --> top-heavy IMF

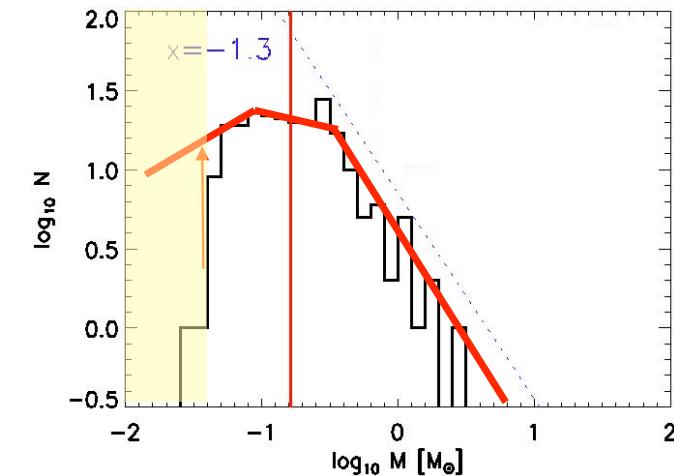
(Klessen, Spaans, Jappsen, 2007)



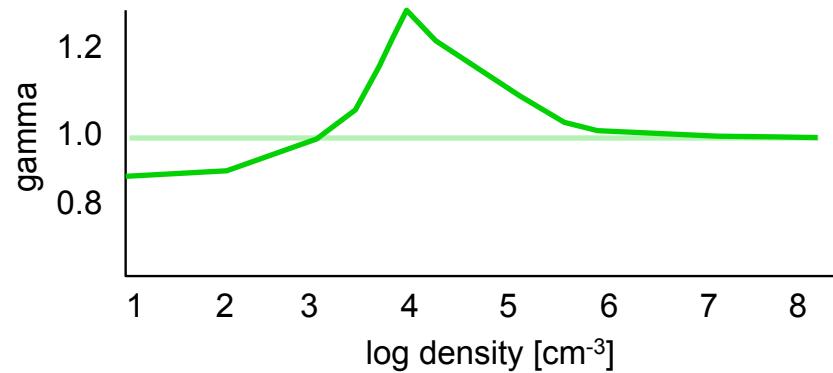
# fragmentation depends on EOS



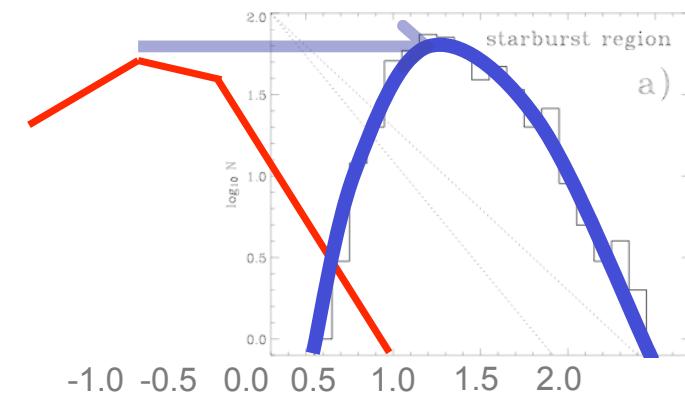
(Larson 2005)



(Jappsen et al. 2005)



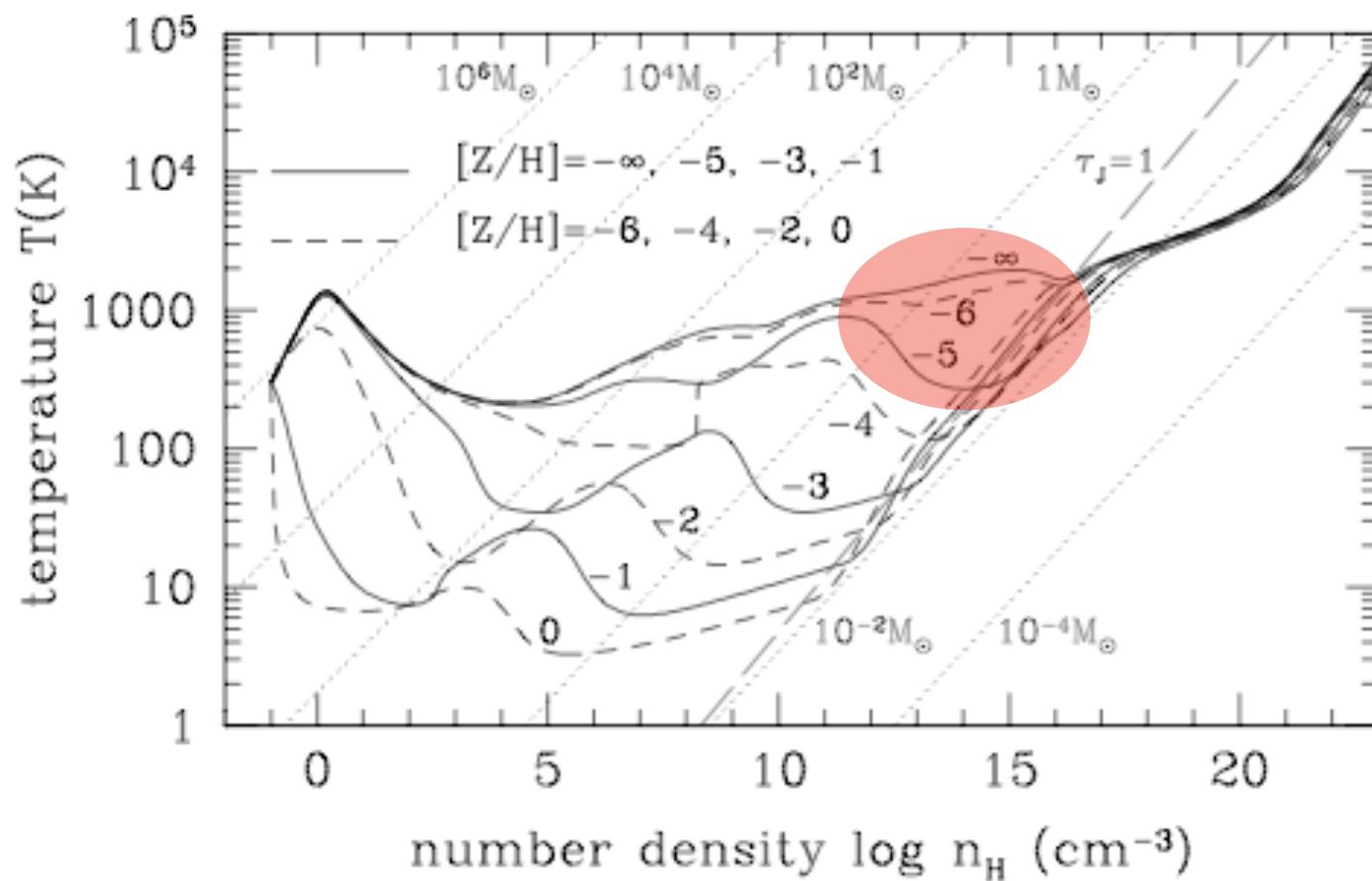
(Spaans & Silk 2005)



(Klessen et al. 2007)

# transition: Pop III to Pop II.5

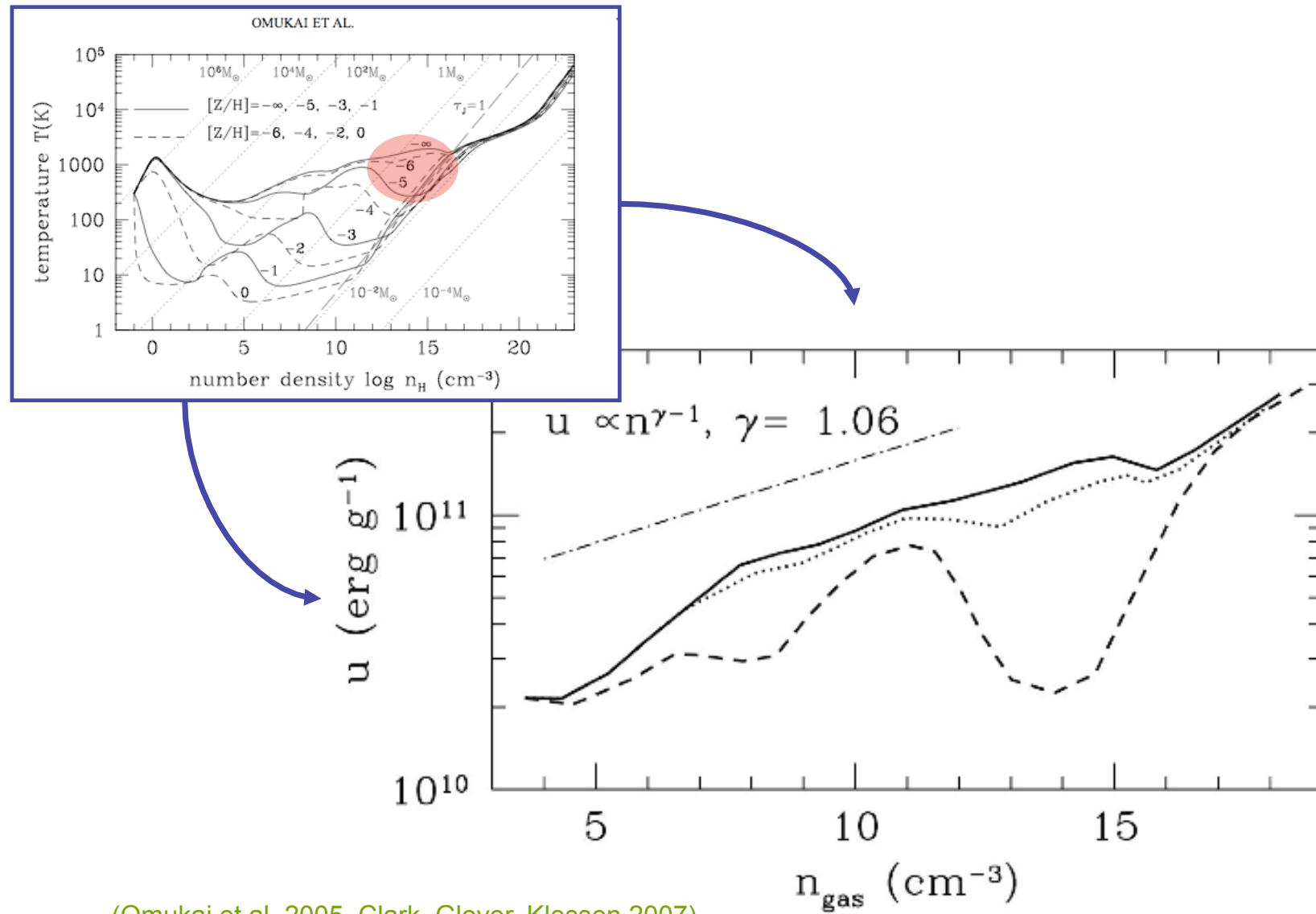
OMUKAI ET AL.



(Omukai et al. 2005)

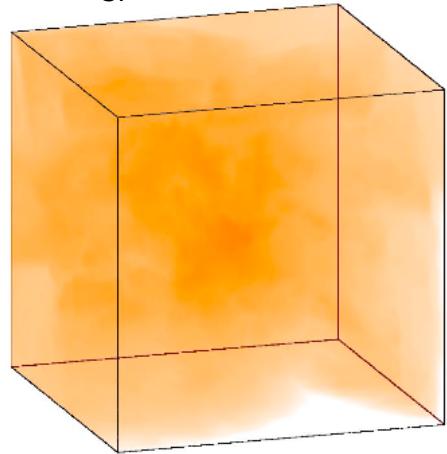
Ralf Klessen: Cardiff, 25.02.2008

# transition: Pop III to Pop II.5

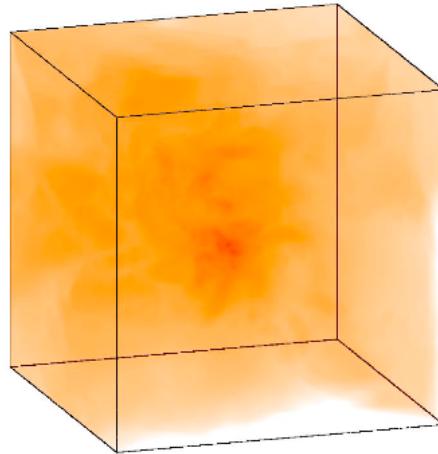


# dust induced fragmentation at $Z=10^{-5}$

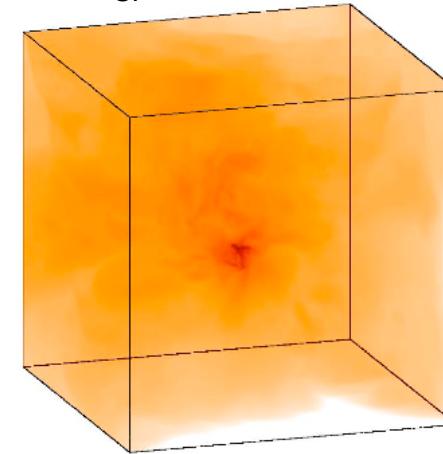
$t = t_{SF} - 67$  yr



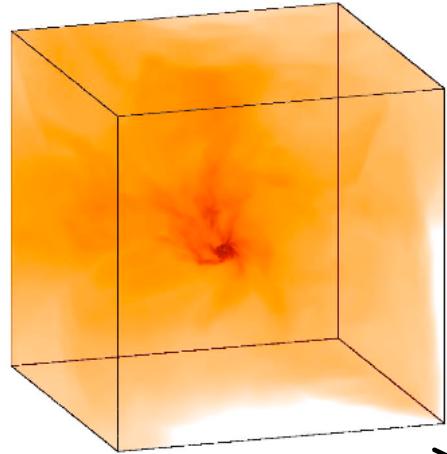
$t = t_{SF} - 20$  yr



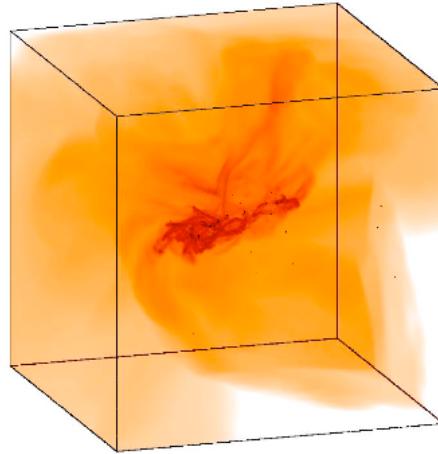
$t = t_{SF}$



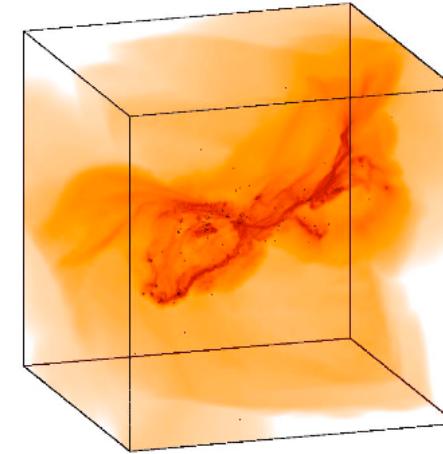
$t = t_{SF} + 53$  yr



$t = t_{SF} + 233$  yr



$t = t_{SF} + 420$  yr



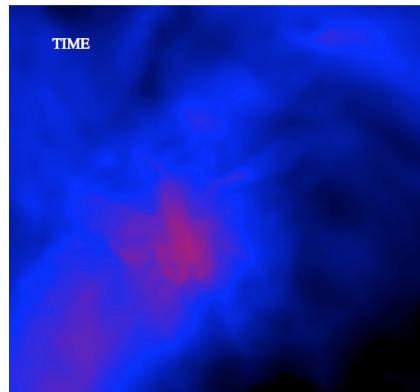
← 400 AU →

(Clark et al. 2007)

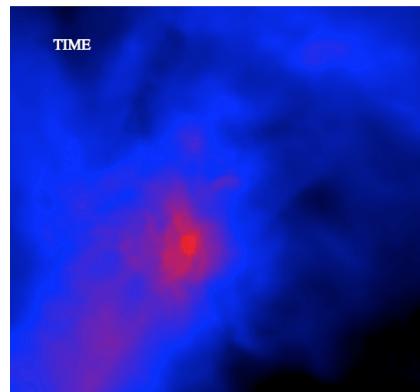
Ralf Klessen: Cardiff, 25.02.2008

# dust induced fragmentation at $Z=10^{-5}$

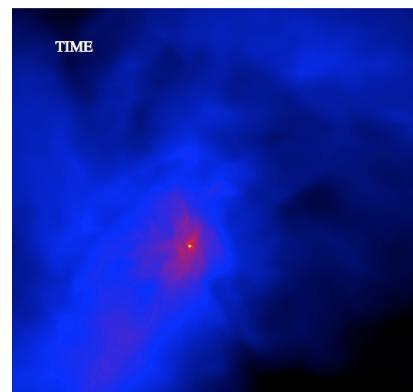
$t = t_{SF} - 67$  yr



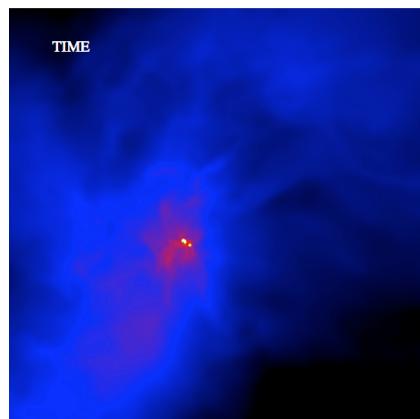
$t = t_{SF} - 20$  yr



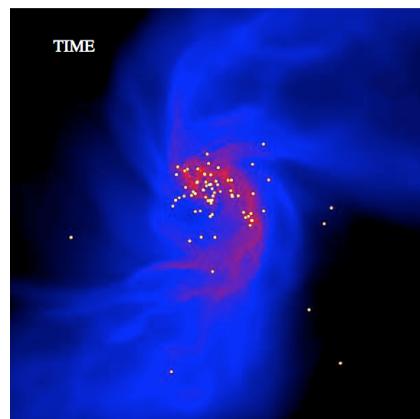
$t = t_{SF}$



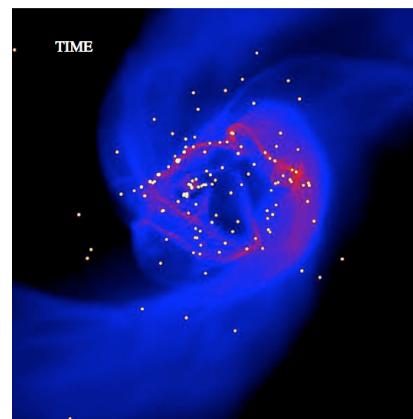
$t = t_{SF} + 53$  yr



$t = t_{SF} + 233$  yr



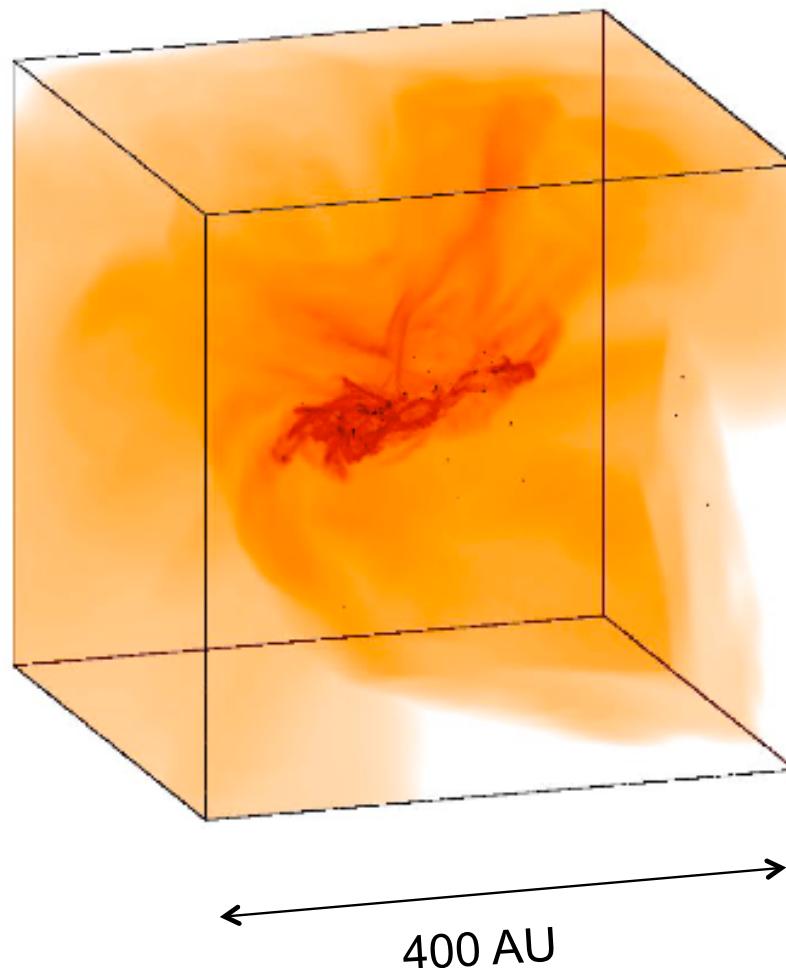
$t = t_{SF} + 420$  yr



(Clark et al. 2007)

Ralf Klessen: Cardiff, 25.02.2008

# dust induced fragmentation at $Z=10^{-5}$



dense cluster of low-mass protostars builds up:

- mass spectrum peaks below  $1 M_{\text{sun}}$
- cluster VERY dense
- $n_{\text{stars}} = 2.5 \times 10^9 \text{ pc}^{-3}$
- fragmentation at density
- $n_{\text{gas}} = 10^{12} - 10^{13} \text{ cm}^{-3}$

(Clark et al. 2007)

# cluster build-up

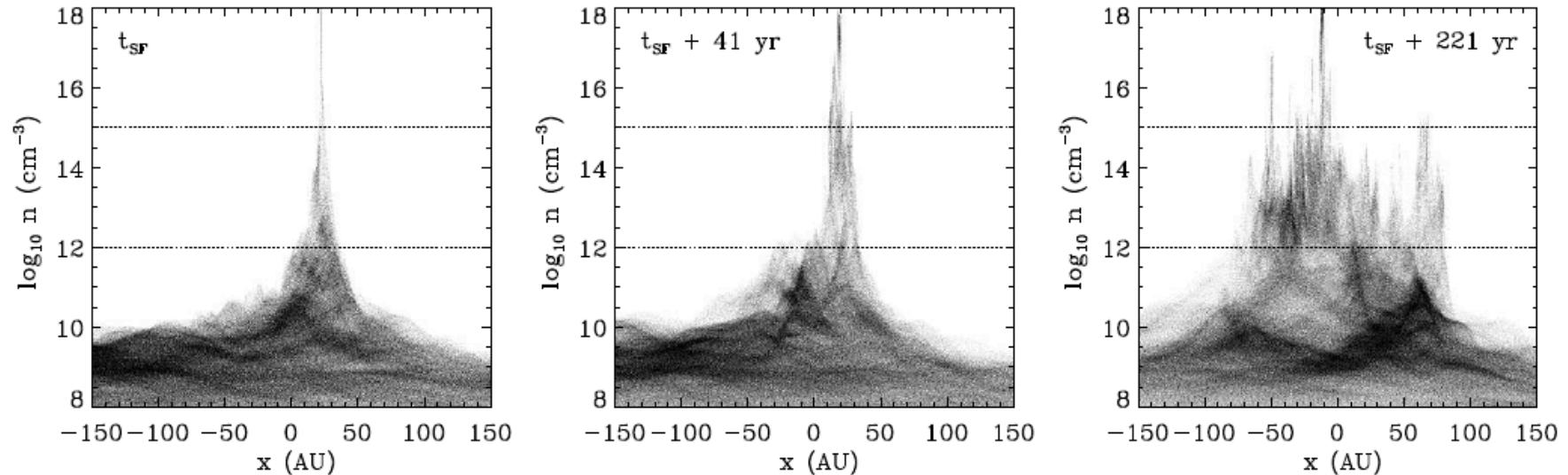
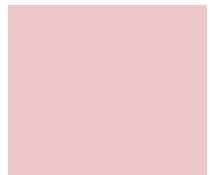
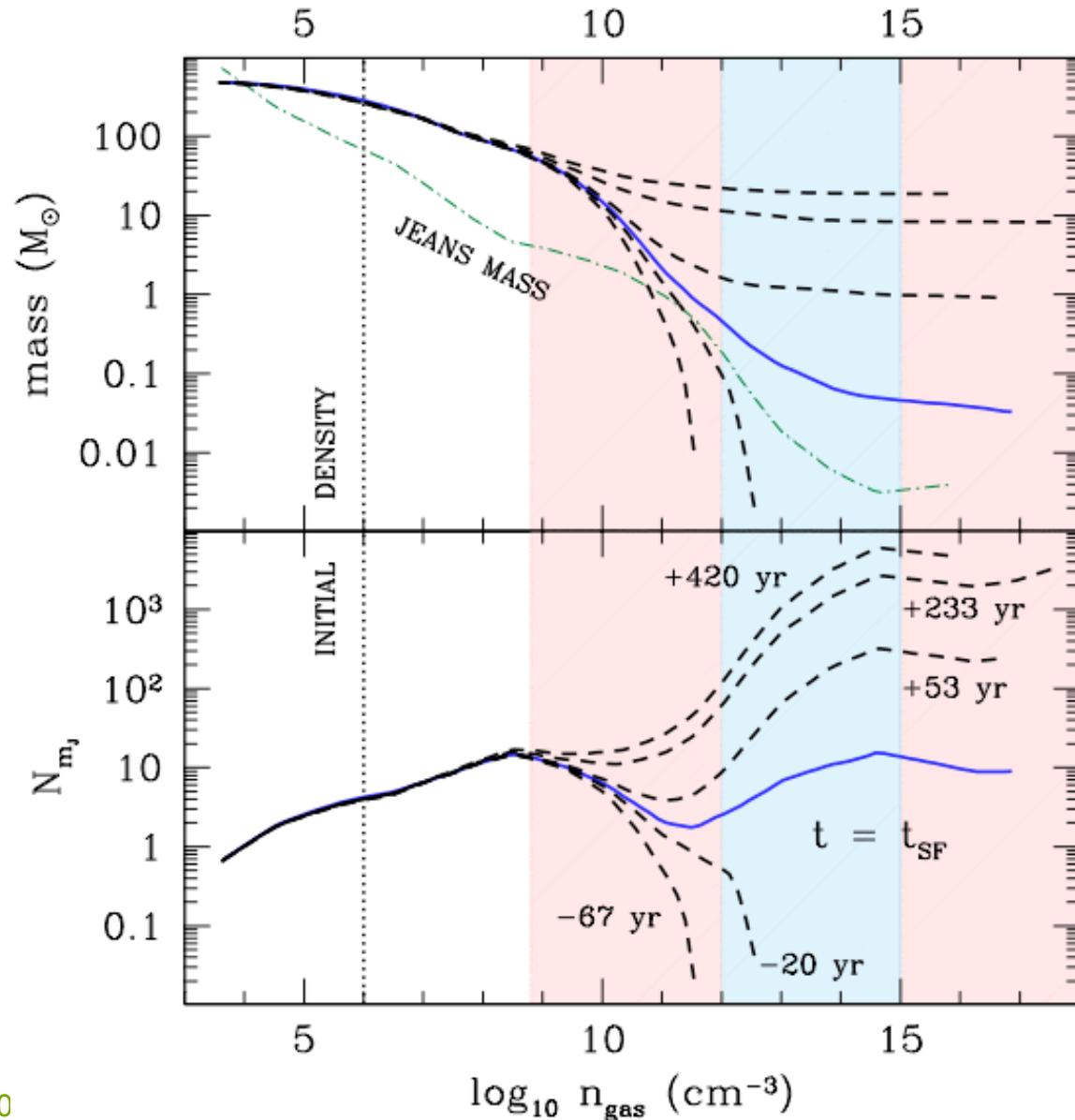


FIG. 3.— We illustrate the onset of the fragmentation process in the high resolution  $Z = 10^{-5} Z_{\odot}$  simulation. The graphs show the densities of the particles, plotted as a function of their x-position. Note that for each plot, the particle data has been centered on the region of interest. We show here results at three different output times, ranging from the time that the first star forms ( $t_{\text{sf}}$ ) to 221 years afterwards. The densities lying between the two horizontal dashed lines denote the range over which dust cooling lowers the gas temperature.

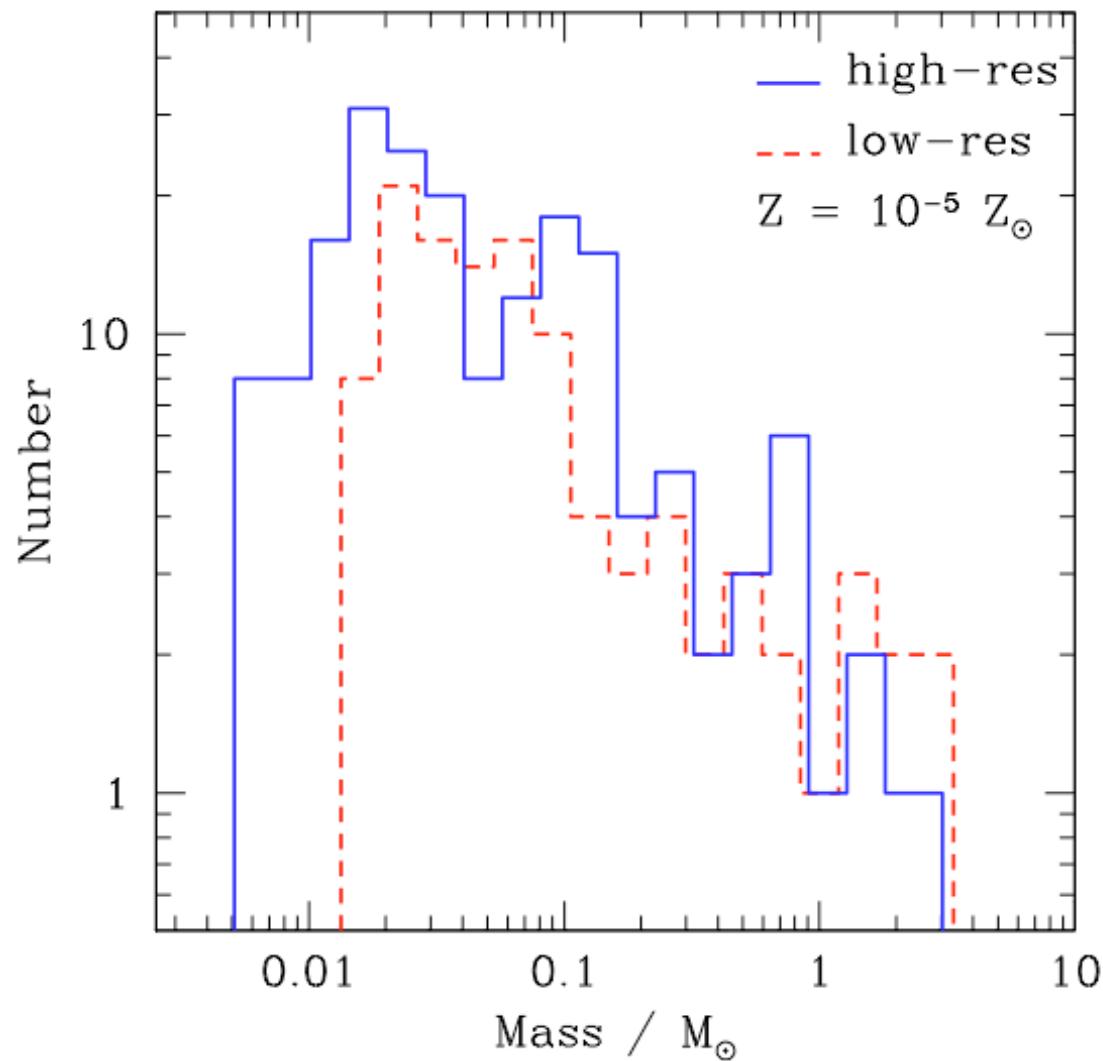
# cluster build-up



$\gamma > 1$   
(heating)

$\gamma < 1$   
(cooling)

# dust induced fragmentation at $Z=10^{-5}$



dense cluster of low-mass protostars builds up:

- mass spectrum
- peaks below  $1 M_{\odot}$
- cluster VERY dense
- $n_{\text{stars}} = 2.5 \times 10^9 \text{ pc}^{-3}$
- fragmentation
- at density
- $n_{\text{gas}} = 10^{12} - 10^{13} \text{ cm}^{-3}$

(Clark et al. 2007)

# comparison for different Z

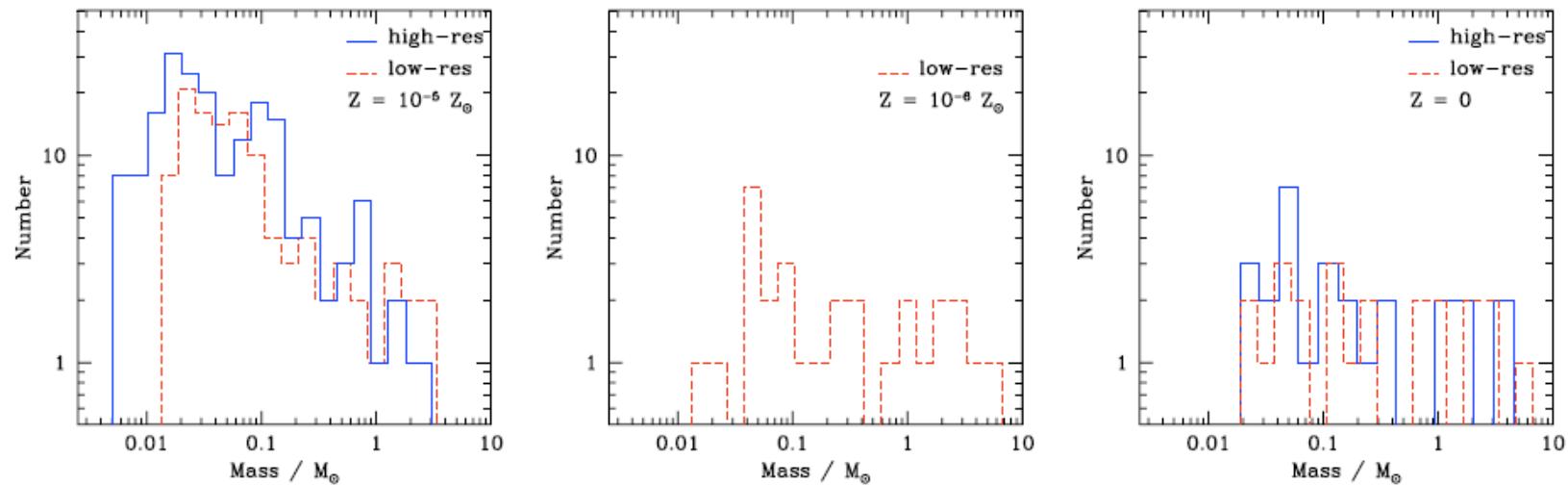
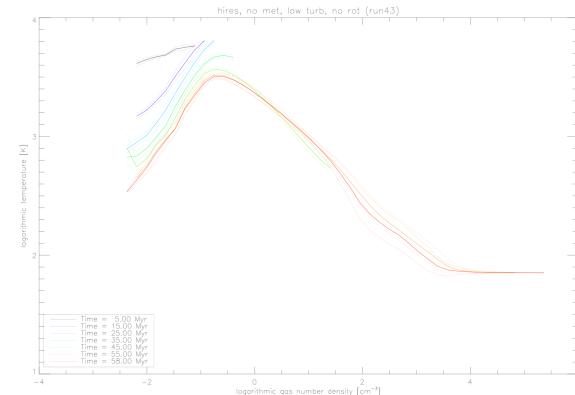


FIG. 4.— Mass functions resulting from simulations with metallicities  $Z = 10^{-5} Z_{\odot}$  (left-hand panel),  $Z = 10^{-6} Z_{\odot}$  (center panel), and  $Z = 0$  (right-hand panel). The plots refer to the point in each simulation at which  $19 M_{\odot}$  of material has been accreted (which occurs at a slightly different time in each simulation). The mass resolutions are  $0.002 M_{\odot}$  and  $0.025 M_{\odot}$  for the high and low resolution simulations, respectively. Note the similarity between the results of the low-resolution and high-resolution simulations. The onset of dust-cooling in the  $Z = 10^{-5} Z_{\odot}$  cloud results in a stellar cluster which has a mass function similar to that for present day stars, in that the majority of the mass resides in the lower-mass objects. This contrasts with the  $Z = 10^{-6} Z_{\odot}$  and primordial clouds, in which the bulk of the cluster mass is in high-mass stars.

even zero-metallicity case fragments  
(although much more weakly)

# Simple EOS vs. radiation transfer

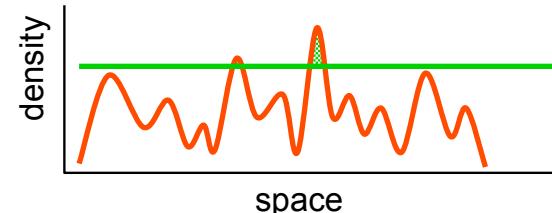
- how good is EOS approach?
  - time to reach chemical and thermal equilibrium shorter than dynamical time?
  - how does EOS depend on dynamics?  
(e.g. 1D collapse with large-gradient approx. versus complex 3D turbulent flows)
- how important is heating from stars?
  - accretion luminosity may heat gas and reduce degree of cloud fragmentation (cluster formation vs. high-mass SF)
- how can we model that best?
  - full radiation transfer vs. approximate schemes



# Summary

# Summary I

- interstellar gas is highly *inhomogeneous*
    - *thermal instability*
    - *gravitational instability*
    - *turbulent compression* (in shocks  $\delta\rho/\rho \propto M^2$ ; in atomic gas:  $M \approx 1\dots 3$ )
  - cold *molecular clouds* can form rapidly in high-density regions at *stagnation points of convergent large-scale flows*
    - chemical *phase transition*: atomic  $\rightarrow$  molecular
    - process is *modulated* by large-scale *dynamics* in the galaxy
  - inside *cold clouds*: turbulence is highly supersonic ( $M \approx 1\dots 20$ )  
→ *turbulence* creates density contrast, *gravity* selects for collapse
- > **GRAVOTUBULENT FRAGMENTATION**
- *turbulent cascade*: local compression *within* a cloud provokes collapse → formation of individual *stars* and *star clusters*
  - *star cluster*: gravity dominates in large region (→ competitive accretion)



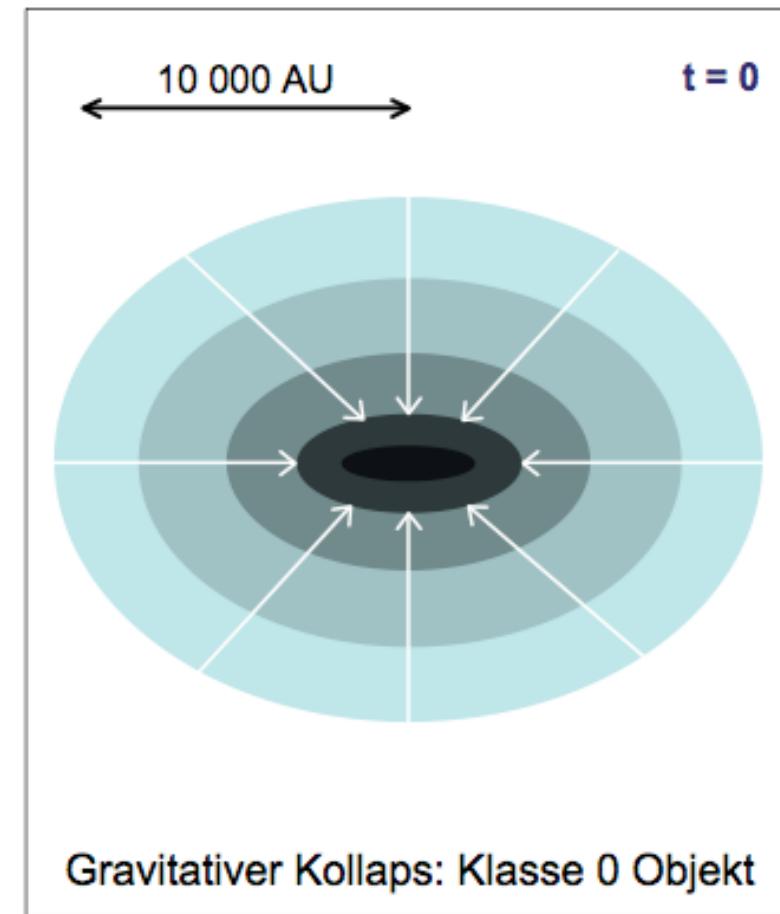
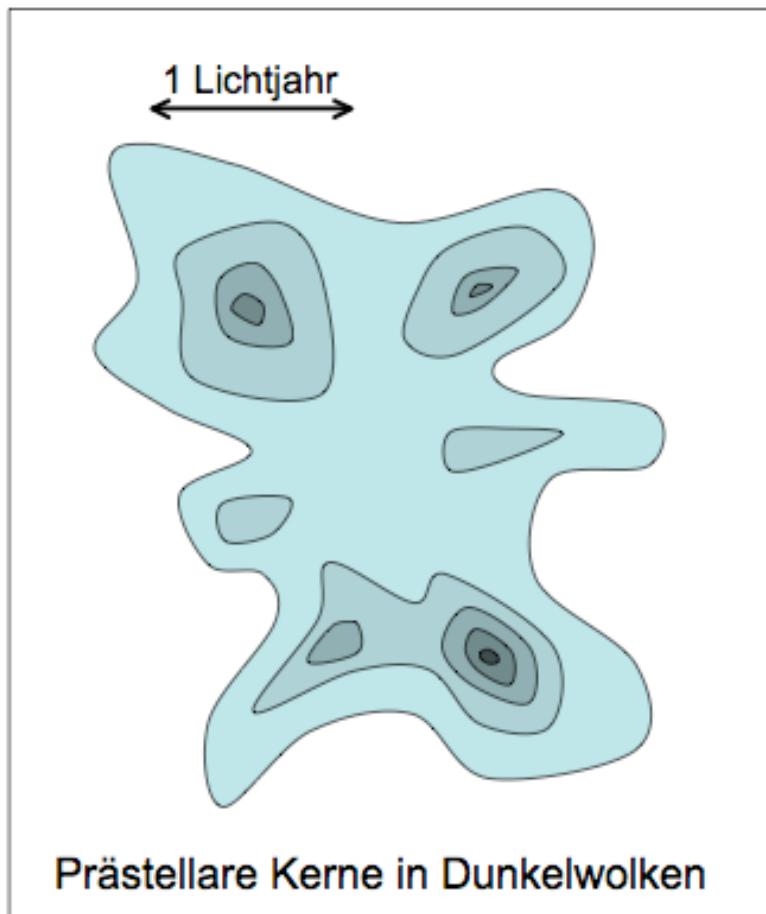
# Summary II

- *thermodynamic response* (EOS) determines fragmentation behavior
  - characteristic stellar mass from fundamental atomic and molecular parameters  
--> explanation for quasi-universal IMF?
- *stellar feedback* is important
  - accretion heating may reduce degree of fragmentation
  - ionizing radiation will set efficiency of star formation
- *CAVEATS:*
  - star formation is *multi-scale, multi-physics* problem --> VERY difficult to model
  - in simulations: very small turbulent inertial range ( $Re < 1000$ )
  - can we use EOS to describe thermodynamics of gas, or do we need time-dependent chemical network and radiative transport?
  - stellar feedback requires (at least approximative) radiative transport, most numerical calculations so far have neglected that aspect

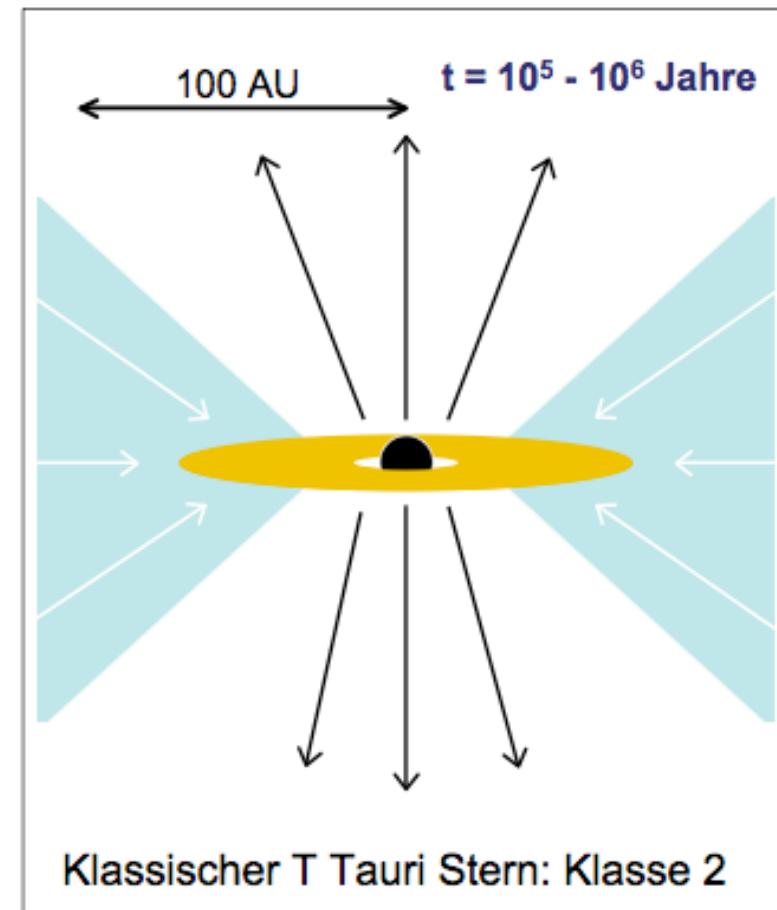
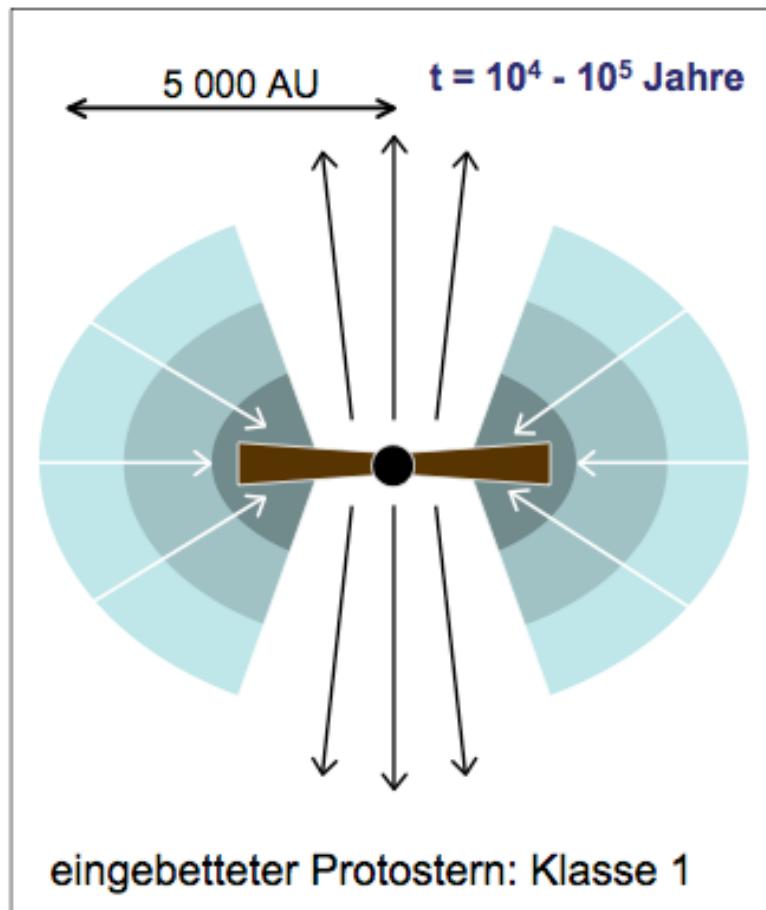


Thanks!

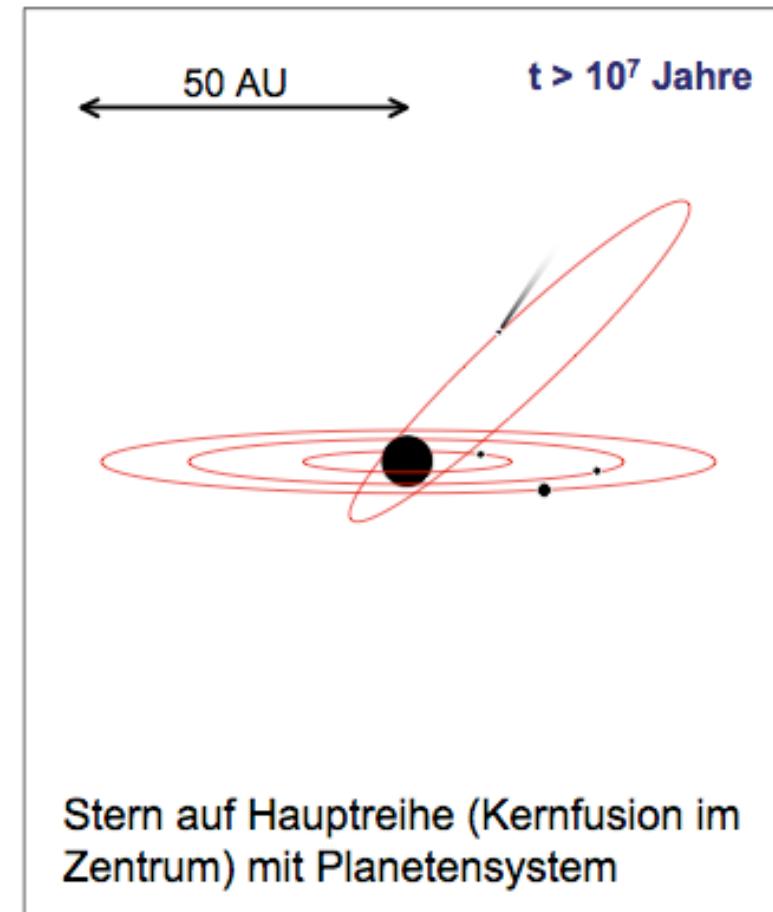
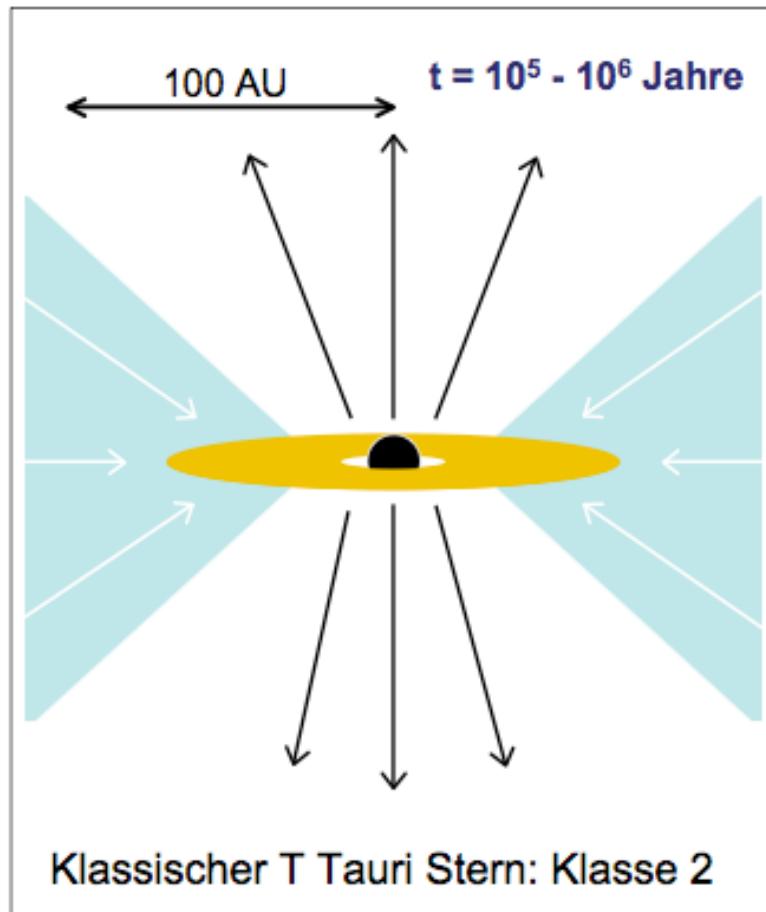
# Stadien der Sternbildung 1



# Stadien der Sternbildung 2



# Stadien der Sternbildung 3



hires, no met, low turb, no rot (run43)

