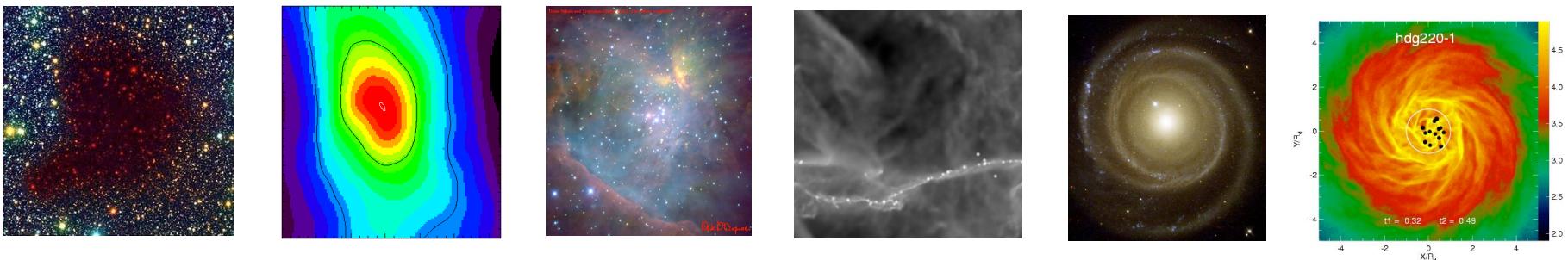


# ISM Turbulence



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# Agenda

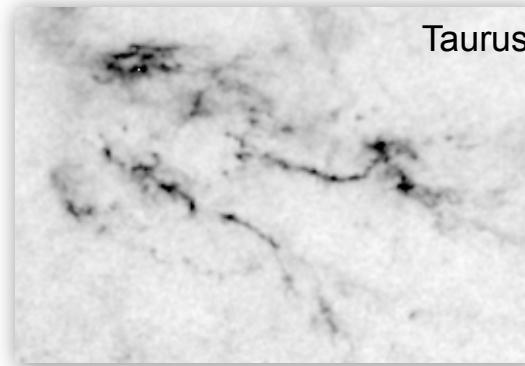
- some phenomenology

- what we know
- what we need to explain

- turbulence

- some basic properties
- formation of molecular clouds in galactic disks  
( $H_2$  & CO chemistry)

- summary: basic idea of gravoturbulent SF

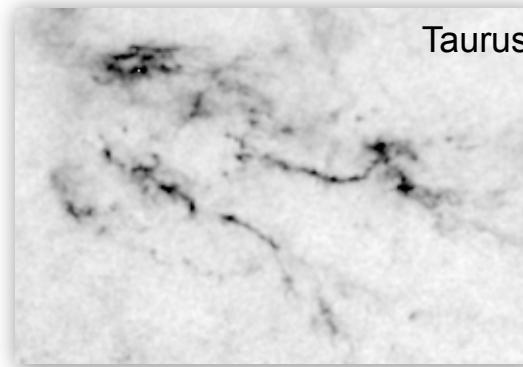




# Interstellar Matter: ISM

Abundances, scaled to 1.000.000 H atoms

element	atomic number	abundance
Wasserstoff	H	1
Deuterium	$^1\text{H}^2$	1
Helium	He	2
Kohlenstoff	C	6
Stickstoff	N	7
Sauerstoff	O	8
Neon	Ne	10
Natrium	Na	11
Magnesium	Mg	12
Aluminium	Al	13
Silicium	Si	14
Schwefel	S	16
Calcium	Ca	20
Eisen	Fe	26
Nickel	Ni	28

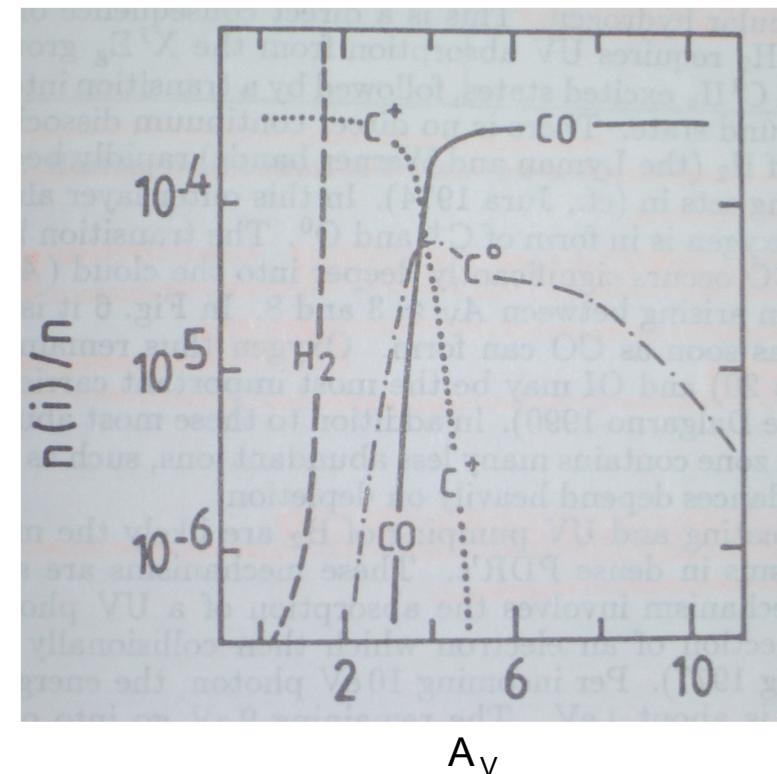
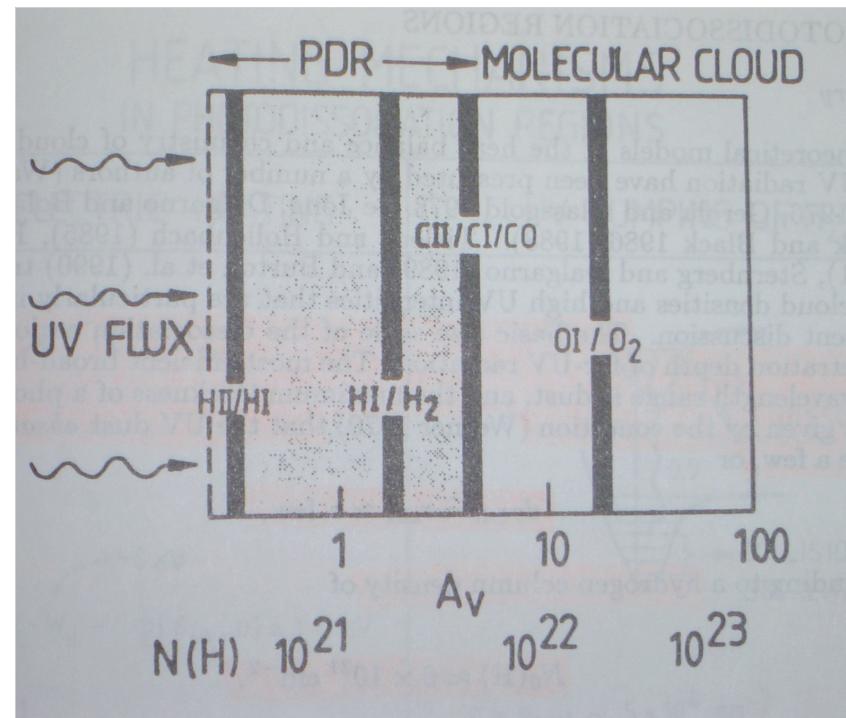


Taurus

Hydrogen is by far the most abundant element (more than 90% in number).



# Phases of the ISM



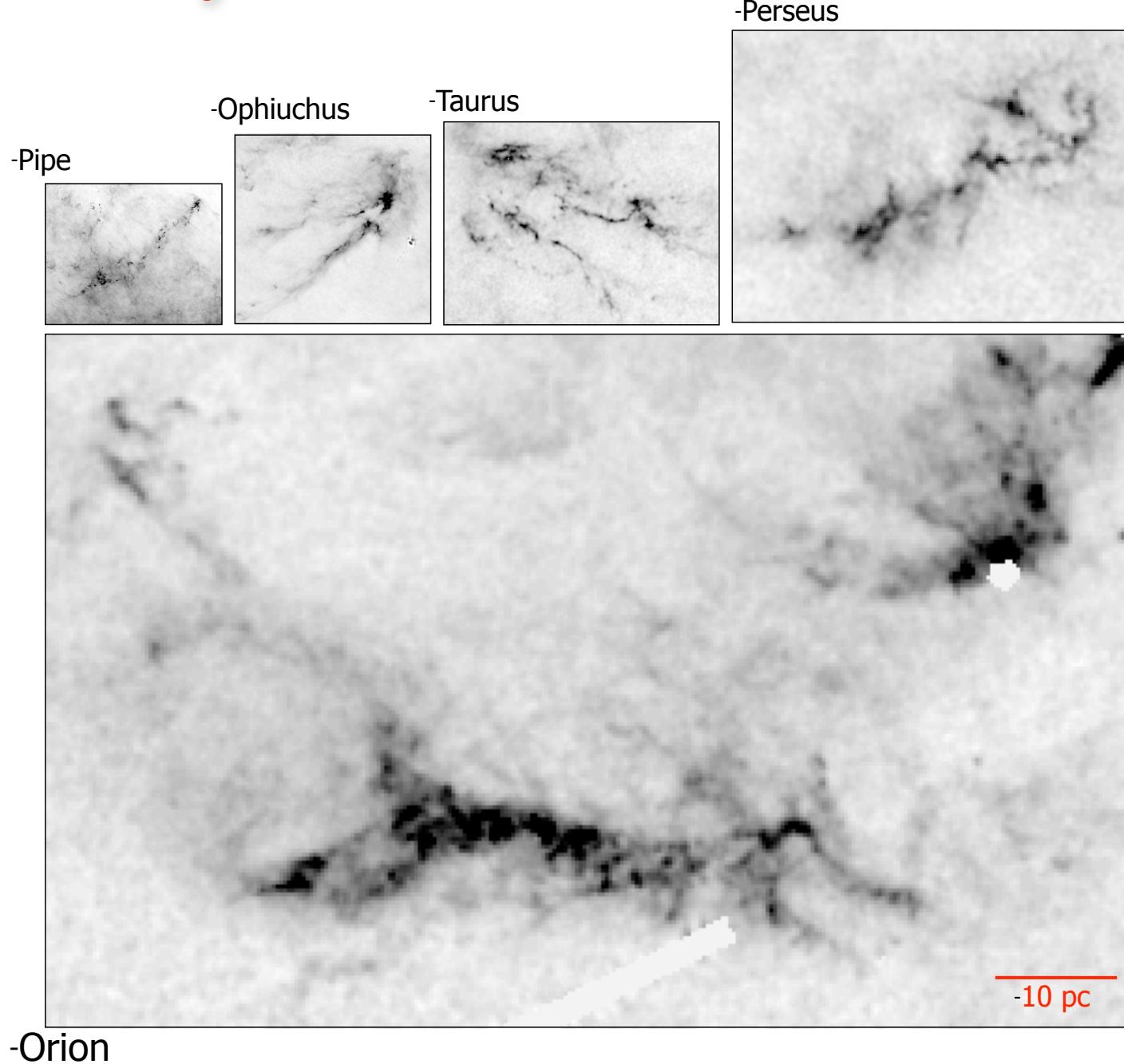
$A_V$  bezeichnet die Extinktion, dh. die Abschwächung der einfallenden Strahlung.



# nearby molecular clouds



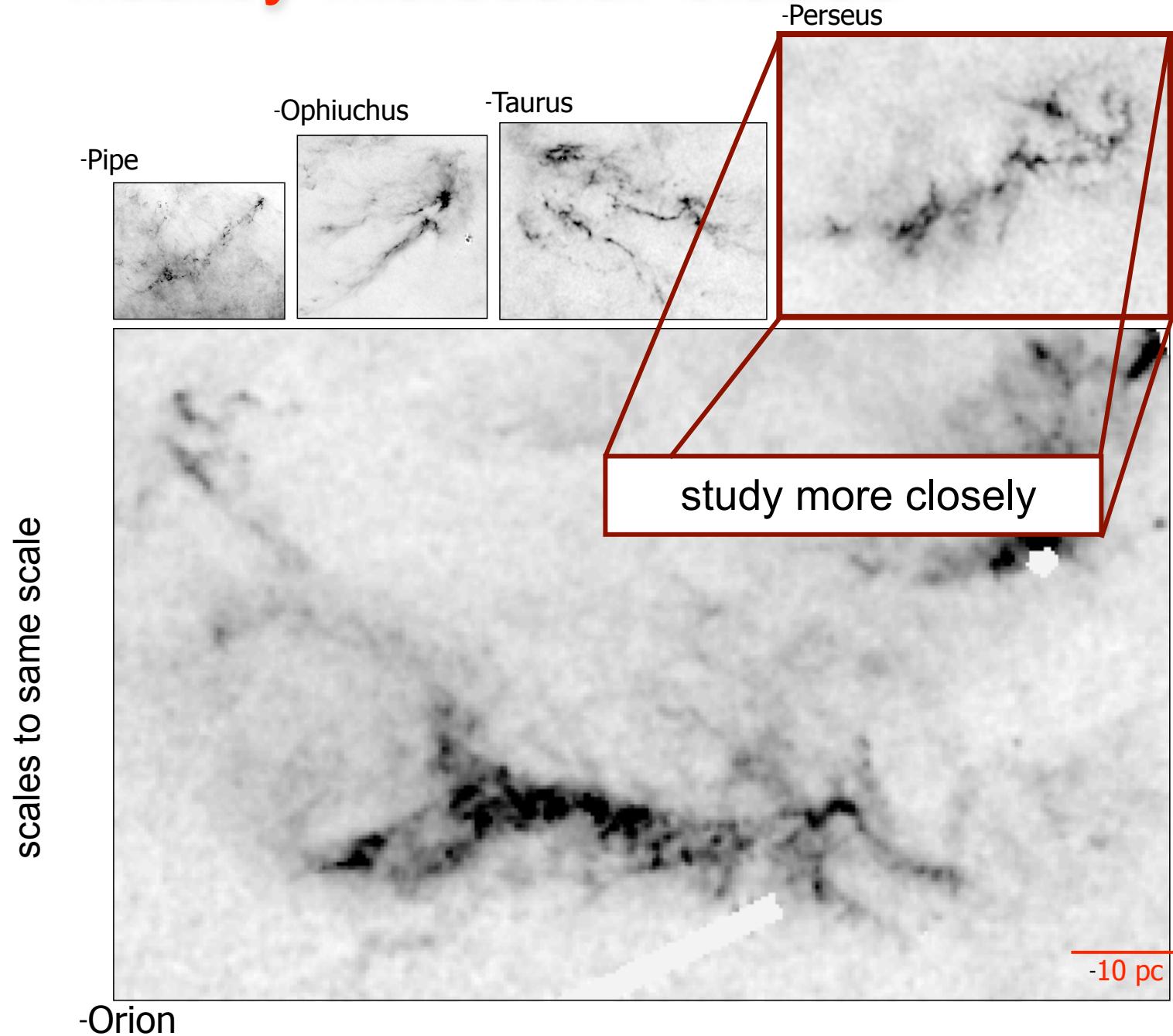
scales to same scale

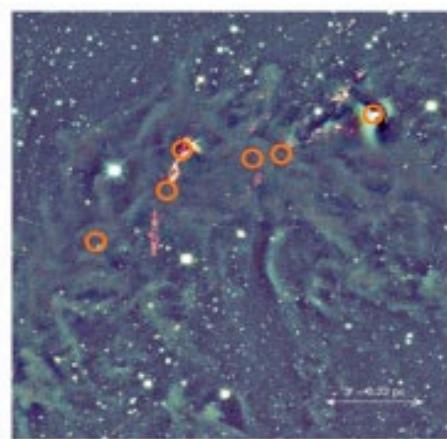


(from A. Goodman)

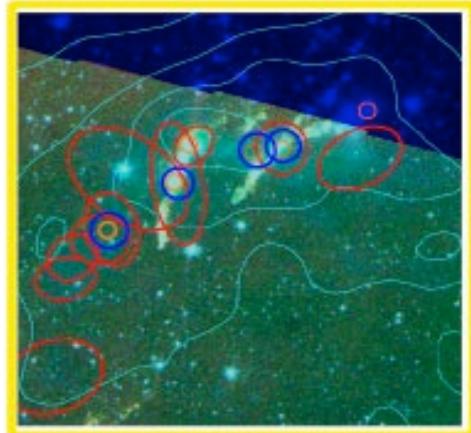


# nearby molecular clouds

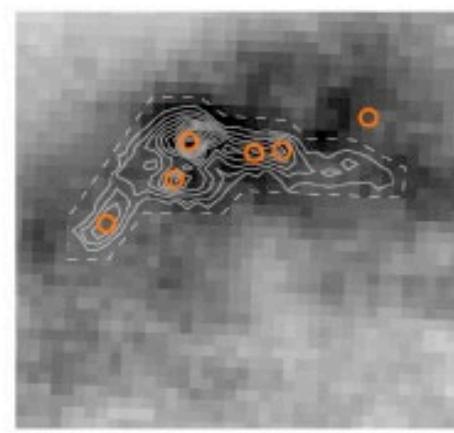




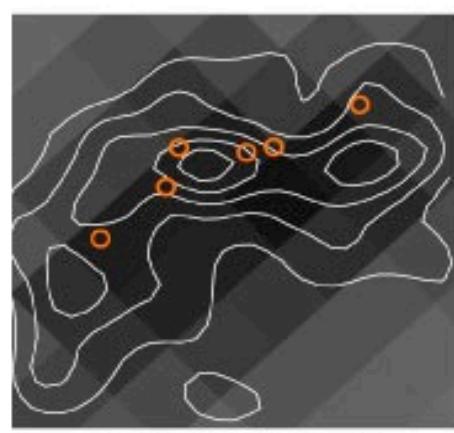
J,H,K Near-IR image  
of Cloudshine



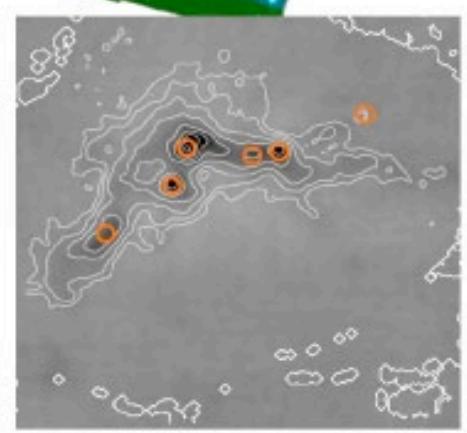
 850 micron and 1.1 mm  
clumps on a c2d IRAC  
3-color image



MPL       $\text{N}_2\text{H}^+$  on  $^{13}\text{CO}$   
integrated intensity



E      Deep NIR Extinction on  
2MASS Extinction



TE      1.2 mm (IRAM) on 850  
micron (SCUBA)  
continuum

images from Alyssa Goodman

Ralf Klessen: Santa Cruz, 21.04.2010

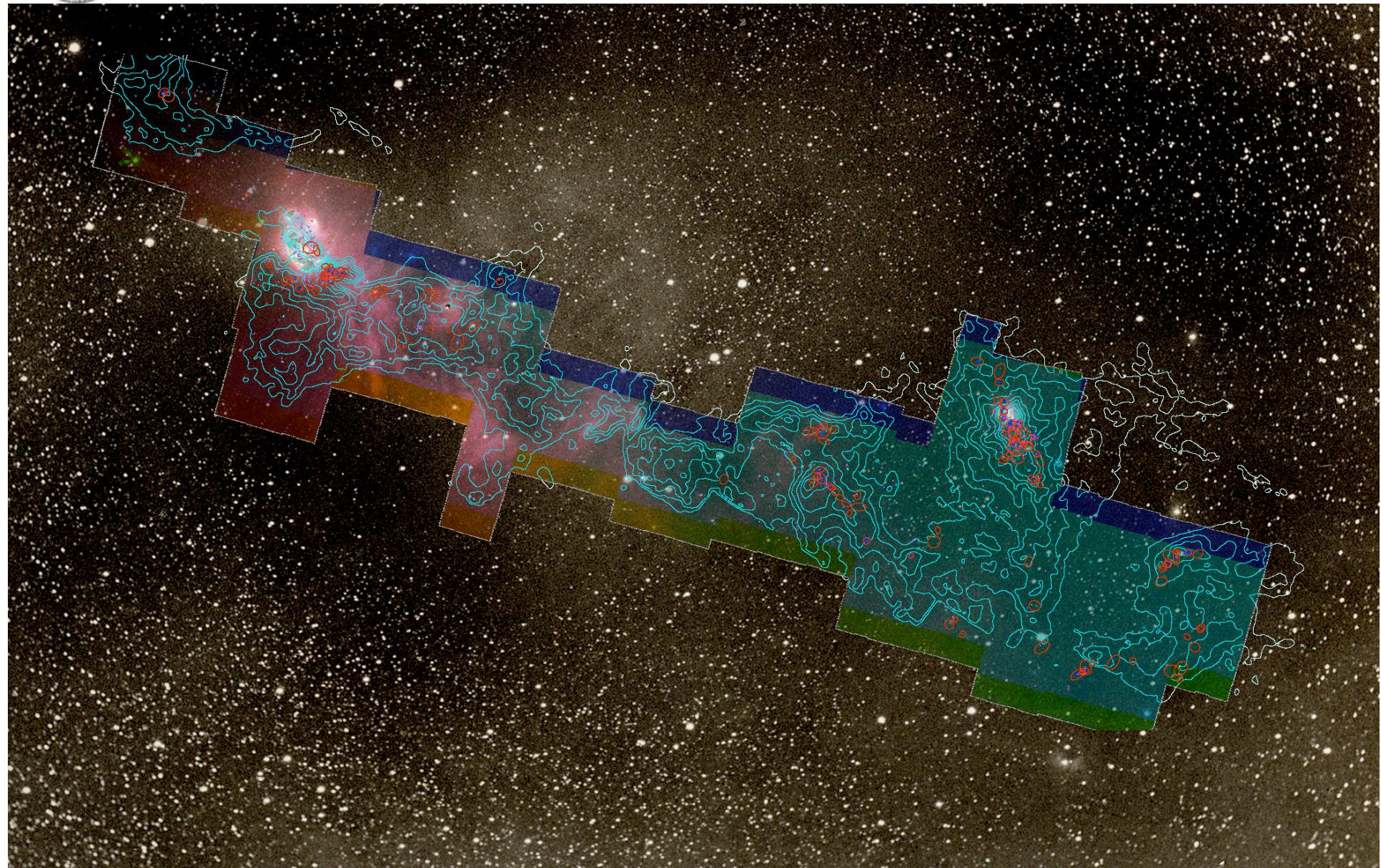
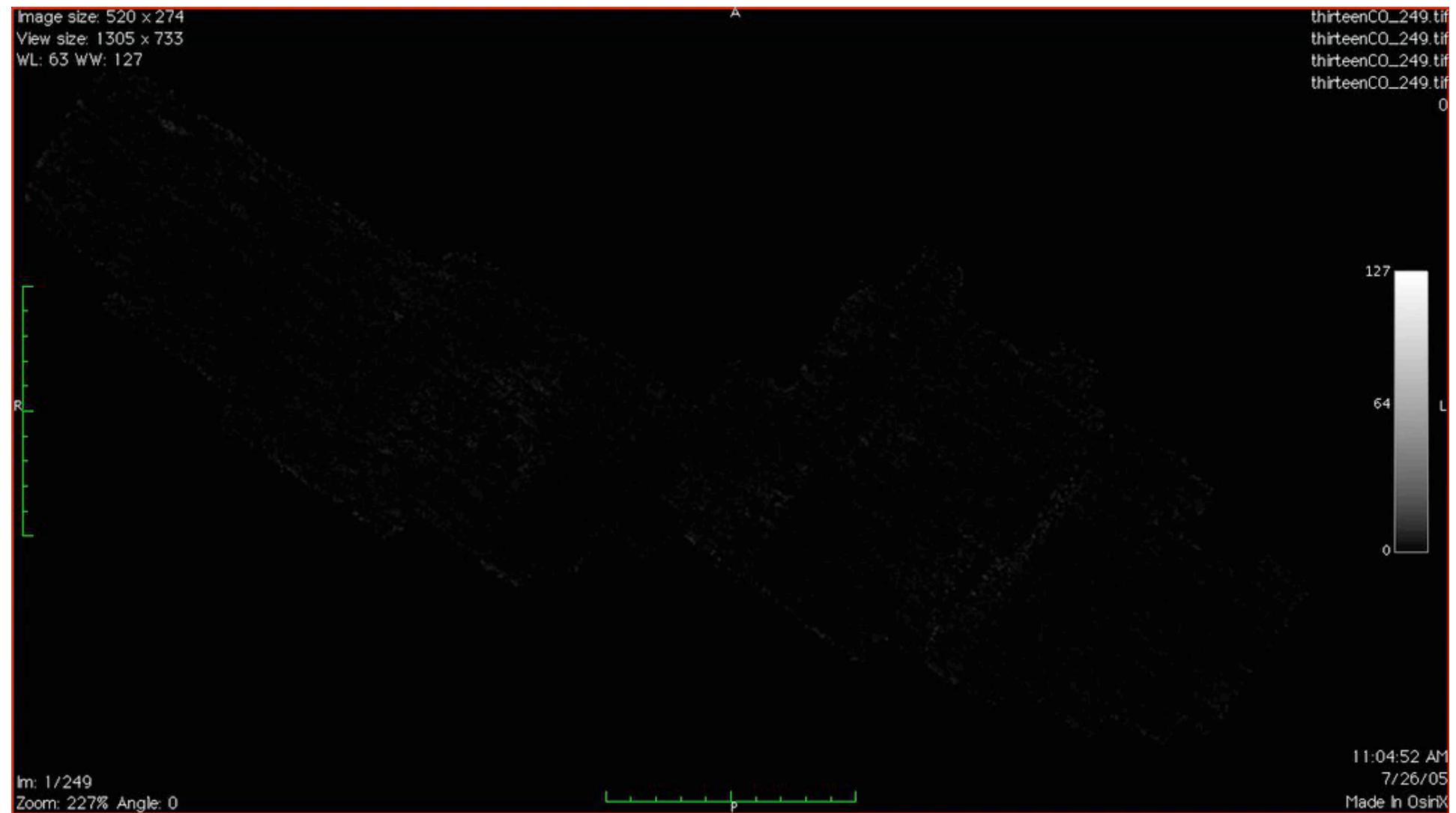


image from Alyssa Goodman: COMPLETE survey

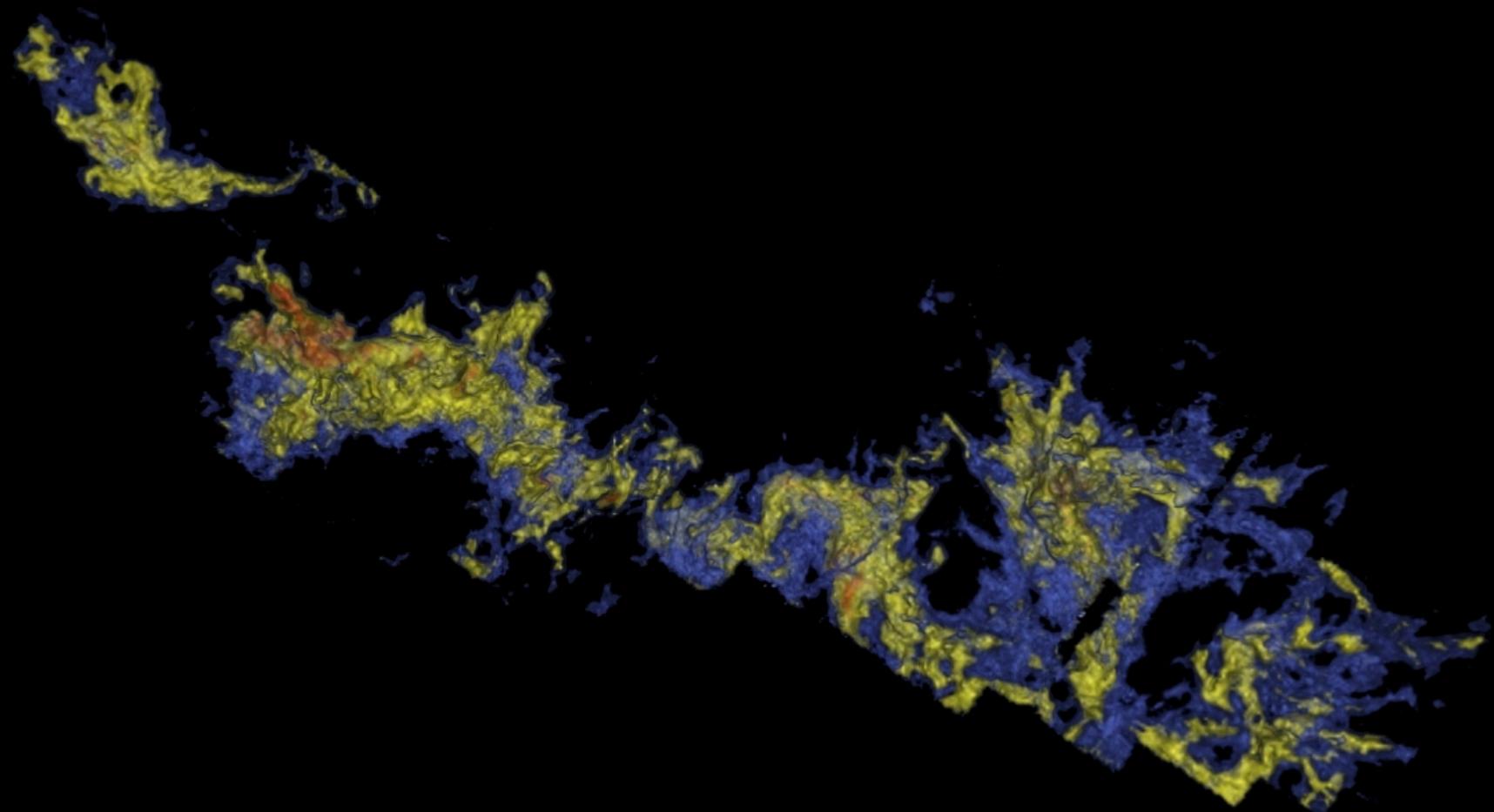
Ralf Klessen: Santa Cruz, 21.04.2010



velocity distribution in Perseus

velocity cube from Alyssa Goodman: COMPLETE survey

Ralf Klessen: Santa Cruz, 21.04.2010



velocity distribution in Perseus

image from Alyssa Goodman: COMPLETE survey

Ralf Klessen: Santa Cruz, 21.04.2010

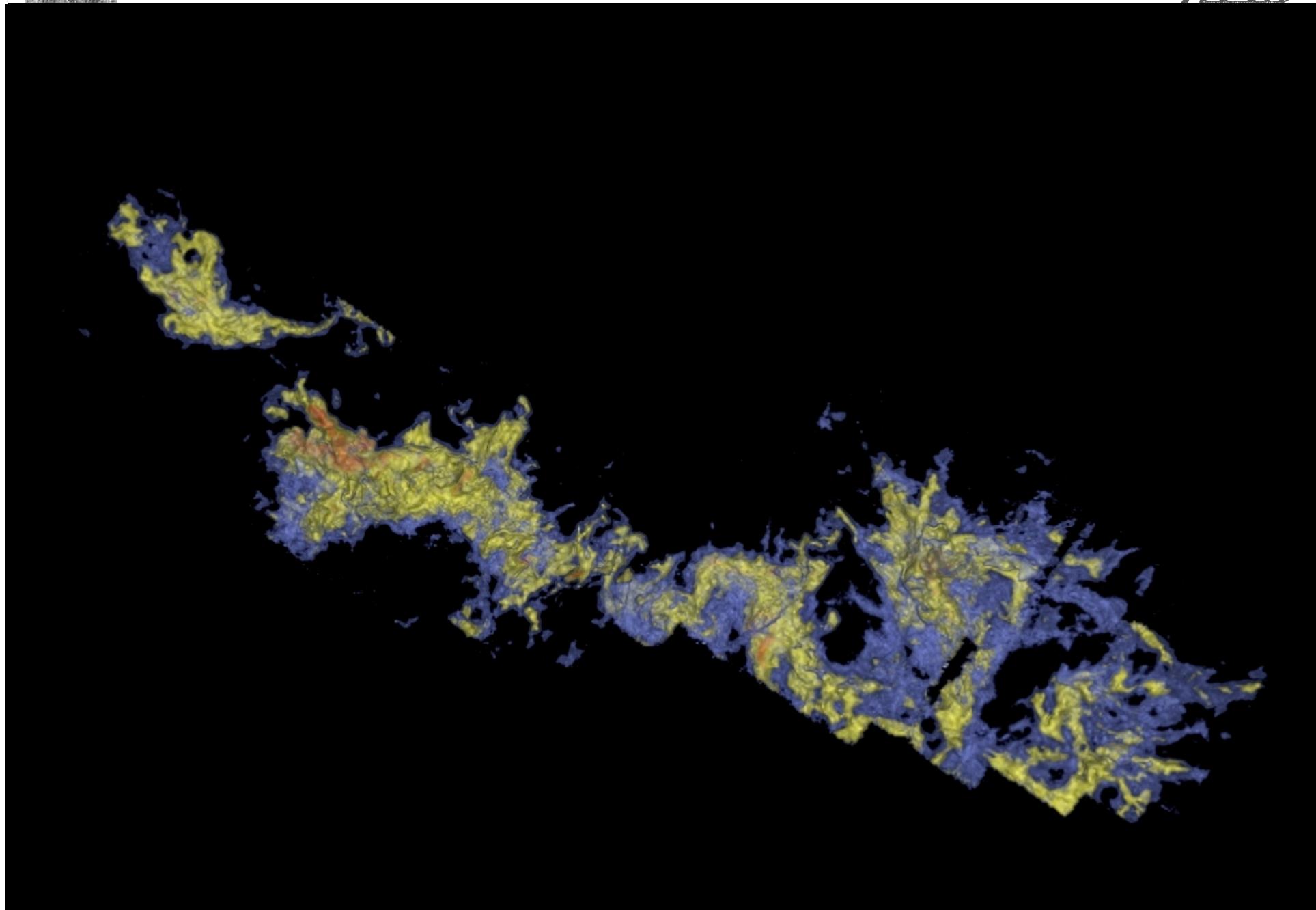
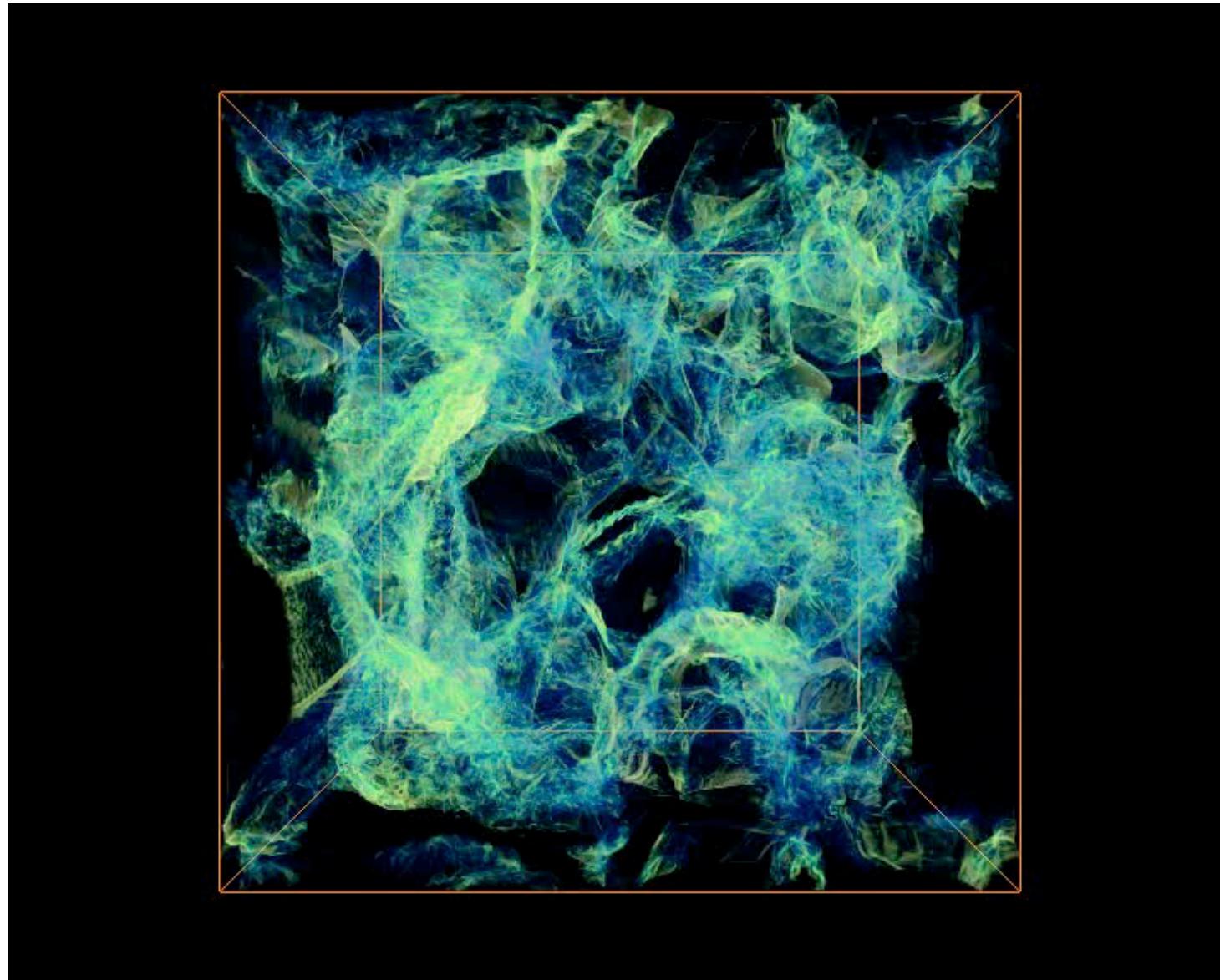


image from Alyssa Goodman: COMPLETE survey

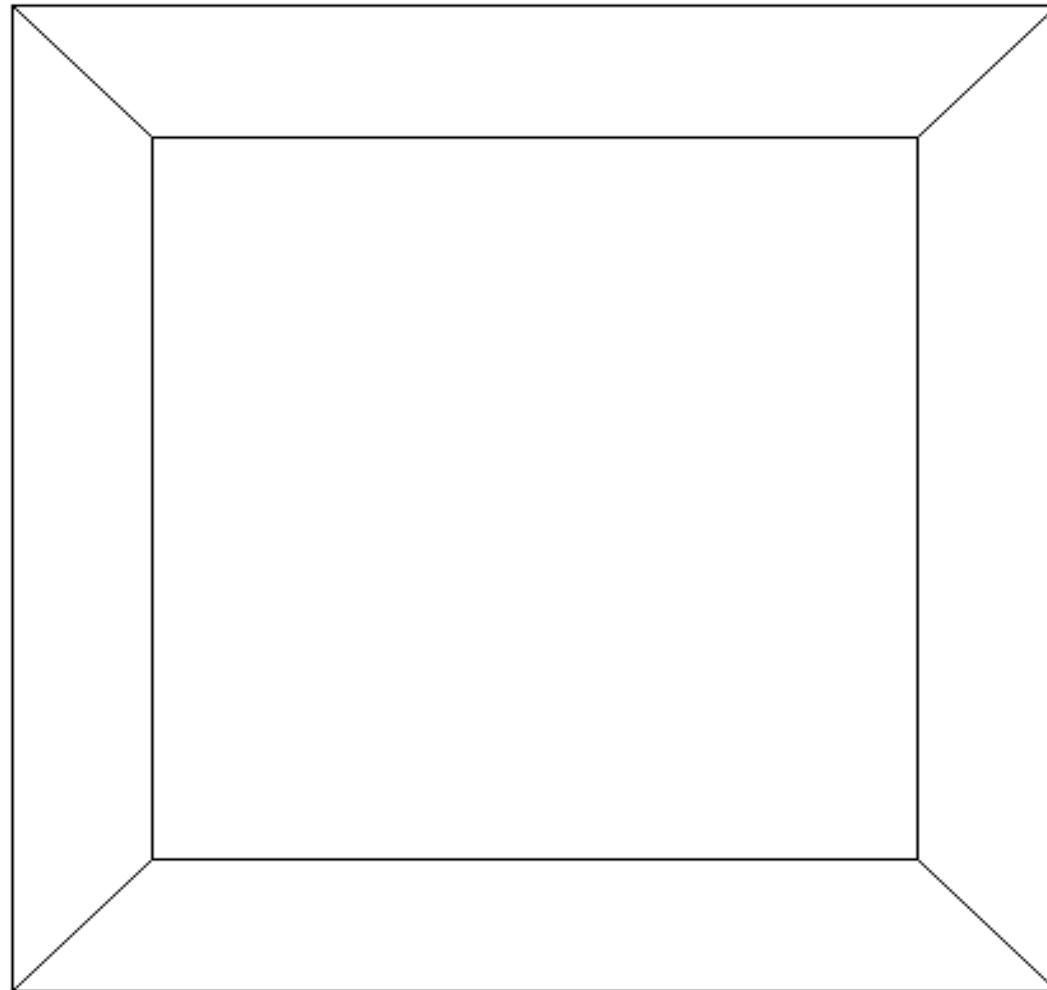
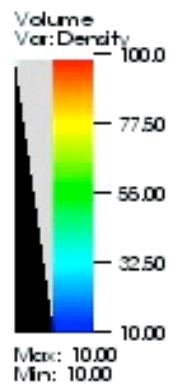
Ralf Klessen: Santa Cruz, 21.04.2010



(movie from Christoph Federrath)

Ralf Klessen: Santa Cruz, 21.04.2010

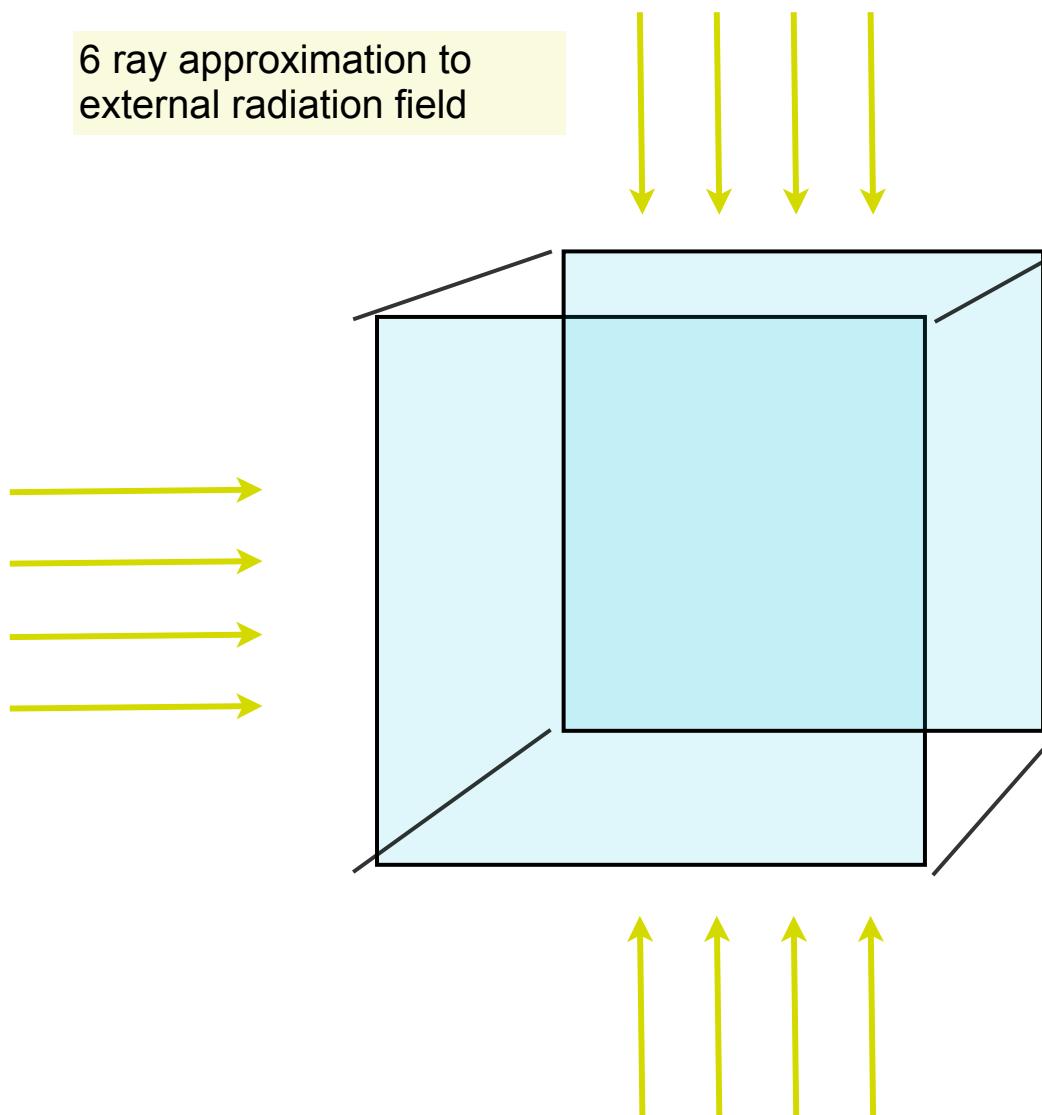
Mesh  
Var: tracer\_particles



user: chfeder  
Sun Oct 15 20:24:29 2006



# experimental set-up



- AMR MHD ( $B = 2 \mu\text{G}$ )
- stochastic forcing  
(Ornstein-Uhlenbeck)
- self-gravity
- time-dependent chemistry
- cooling & heating processes
- > thermodynamics done right!
  
- gives you mathematically well defined boundary conditions
- > good for statistical studies



# chemical model 0

- 32 chemical species

- 17 in instantaneous equilibrium:

$\text{H}^-$ ,  $\text{H}_2^+$ ,  $\text{H}_3^+$ ,  $\text{CH}^+$ ,  $\text{CH}_2^+$ ,  $\text{OH}^+$ ,  $\text{H}_2\text{O}^+$ ,  $\text{H}_3\text{O}^+$ ,  $\text{CO}^+$ ,  $\text{HOC}^+$ ,  $\text{O}^-$ ,  $\text{C}^-$  and  $\text{O}_2^+$

- 19 full non-equilibrium evolution

$\text{e}^-$ ,  $\text{H}^+$ ,  $\text{H}$ ,  $\text{H}_2$ ,  $\text{He}$ ,  $\text{He}^+$ ,  $\text{C}$ ,  $\text{C}^+$ ,  $\text{O}$ ,  $\text{O}^+$ ,  $\text{OH}$ ,  $\text{H}_2\text{O}$ ,  $\text{CO}$ ,  
 $\text{C}_2$ ,  $\text{O}_2$ ,  $\text{HCO}^+$ ,  $\text{CH}$ ,  $\text{CH}_2$  and  $\text{CH}_3^+$

- 218 reactions

- various heating and cooling processes

(Glover, Federrath, Mac Low, Klessen, in prep)



# chemical model 1

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## Process

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### Cooling:

C fine structure lines

Atomic data – Silva & Viegas (2002)

Collisional rates (H) – Abrahamsson, Krems & Dalgarno (2007)

Collisional rates ( $H_2$ ) – Schroder et al. (1991)

Collisional rates ( $e^-$ ) – Johnson et al. (1987)

Collisional rates ( $H^+$ ) – Roueff & Le Bourlot (1990)

Atomic data – Silva & Viegas (2002)

Collisional rates ( $H_2$ ) – Flower & Launay (1977)

Collisional rates (H,  $T < 2000$  K) – Hollenbach & McKee (1989)

Collisional rates (H,  $T > 2000$  K) – Keenan et al. (1986)

Collisional rates ( $e^-$ ) – Wilson & Bell (2002)

$C^+$  fine structure lines

Atomic data – Silva & Viegas (2002)

O fine structure lines

Collisional rates (H) – Abrahamsson, Krems & Dalgarno (2007)

Collisional rates ( $H_2$ ) – see Glover & Jappsen (2007)

Collisional rates ( $e^-$ ) – Bell, Berrington & Thomas (1998)

Collisional rates ( $H^+$ ) – Pequignot (1990, 1996)

Le Bourlot, Pineau des Forêts & Flower (1999)

$H_2$  rovibrational lines

Neufeld & Kaufman (1993); Neufeld, Lepp & Melnick (1995)

CO and  $H_2O$  rovibrational lines

Pavlovski et al. (2002)

OH rotational lines

Hollenbach & McKee (1989)

Gas-grain energy transfer

Wolfire et al. (2003)

Recombination on grains

Sutherland & Dopita (1993)

Atomic resonance lines

Abel et al. (1997)

H collisional ionization

See Table B1

$H_2$  collisional dissociation

Cen (1992)

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### Heating:

Photoelectric effect

Bakes & Tielens (1994); Wolfire et al. (2003)

$H_2$  photodissociation

Black & Dalgarno (1977)

UV pumping of  $H_2$

Burton, Hollenbach & Tielens (1990)

$H_2$  formation on dust grains

Hollenbach & McKee (1989)

Cosmic ray ionization

Goldsmith & Langer (1978)

**Table B1.** List of collisional gas-phase reactions included in our chemical model

No.	Reaction	Rate coefficient ( $\text{cm}^3 \text{s}^{-1}$ )	Note	Ref.
1	$\text{H} + \text{e}^- \rightarrow \text{H}^- + \gamma$	$= \text{dex}[-16.420 + 0.1098(\log T)^2 - 5.447 \times 10^{-3}(\log T)^4 + 4.0415 \times 10^{-5}(\log T)^6]$		
2	$\text{H}^- + \text{H} \rightarrow \text{H}_2 + \text{e}^-$	$k_2 = 1.5 \times 10^{-9}$ $= 4.0 \times 10^{-9} T^{-0.17}$	$T > 6000 \text{ K}$ $T \leq 300 \text{ K}$	2
3	$\text{H} + \text{H}^+ \rightarrow \text{H}_2^+ + \gamma$	$k_3 = \text{dex}[-19.38 - 1.523 \log T + 1.118(\log T)^2 - 0.1269(\log T)^3]$		3
4	$\text{H} + \text{H}_2^+ \rightarrow \text{H}_2 + \text{H}^+$	$k_4 = 6.4 \times 10^{-10}$		4
5	$\text{H}^- + \text{H}^+ \rightarrow \text{H} + \text{H}$	$k_5 = 2.4 \times 10^{-6} T^{-1/2} (1.0 + T/20000)$		5
6	$\text{H}_2^+ + \text{e}^- \rightarrow \text{H} + \text{H}$	$k_6 = 1.0 \times 10^{-8}$ $= 1.32 \times 10^{-6} T^{-0.76}$	$T \leq 617 \text{ K}$ $T > 617 \text{ K}$	6
7	$\text{H}_2 + \text{H}^+ \rightarrow \text{H}_2^+ + \text{H}$	$k_7 = [-3.3232183 \times 10^{-7}$ $+ 3.3735382 \times 10^{-7} \ln T$ $- 1.4491368 \times 10^{-8} (\ln T)^2$ $+ 3.4172805 \times 10^{-8} (\ln T)^3$ $- 4.7813720 \times 10^{-9} (\ln T)^4$ $+ 3.9731542 \times 10^{-10} (\ln T)^5$ $- 1.8171411 \times 10^{-11} (\ln T)^6$ $+ 3.5311932 \times 10^{-13} (\ln T)^7]$ $\times \exp\left(\frac{-21237.15}{T}\right)$		7
8	$\text{H}_2 + \text{e}^- \rightarrow \text{H} + \text{H} + \text{e}^-$	$k_8 = 3.73 \times 10^{-9} T^{0.1121} \exp\left(\frac{-99430}{T}\right)$		8
9	$\text{H}_2 + \text{H} \rightarrow \text{H} + \text{H} + \text{H}$	$k_{9,\text{l}} = 6.67 \times 10^{-12} T^{1/2} \exp\left[-(1 + \frac{63590}{T})\right]$ $k_{9,\text{h}} = 3.52 \times 10^{-9} \exp\left(-\frac{43900}{T}\right)$ $n_{\text{cr},\text{H}} = \text{dex}\left[3.0 - 0.416 \log\left(\frac{T}{10000}\right) - 0.327 \left\{\log\left(\frac{T}{10000}\right)\right\}^2\right]$		9
10	$\text{H}_2 + \text{H}_2 \rightarrow \text{H}_2 + \text{H} + \text{H}$	$k_{10,\text{l}} = \frac{5.996 \times 10^{-30} T^{4.1881}}{(1.0 + 6.761 \times 10^{-6} T)^{5.6881}} \exp\left(-\frac{54657.4}{T}\right)$ $k_{10,\text{h}} = 1.3 \times 10^{-9} \exp\left(-\frac{53300}{T}\right)$ $n_{\text{cr},\text{H}_2} = \text{dex}\left[4.845 - 1.3 \log\left(\frac{T}{10000}\right) + 1.62 \left\{\log\left(\frac{T}{10000}\right)\right\}^2\right]$		10
11	$\text{H} + \text{e}^- \rightarrow \text{H}^+ + \text{e}^- + \text{e}^-$	$k_{11} = \exp[-3.271396786 \times 10^1$ $+ 1.35365560 \times 10^1 \ln T_e$ $- 5.73932875 \times 10^0 (\ln T_e)^2$ $+ 1.56315498 \times 10^0 (\ln T_e)^3$ $- 2.87705600 \times 10^{-1} (\ln T_e)^4$ $+ 3.482255977 \times 10^{-2} (\ln T_e)^5$ $- 2.63197617 \times 10^{-3} (\ln T_e)^6$ $+ 1.11954395 \times 10^{-4} (\ln T_e)^7$ $- 2.03914985 \times 10^{-6} (\ln T_e)^8]$		11
12	$\text{H}^+ + \text{e}^- \rightarrow \text{H} + \gamma$	$k_{12,\text{A}} = 1.269 \times 10^{-13} \left(\frac{315614}{T}\right)^{1.503}$ $\times [1.0 + \left(\frac{604625}{T}\right)^{0.470}]^{-1.923}$ $k_{12,\text{B}} = 2.753 \times 10^{-14} \left(\frac{315614}{T}\right)^{1.500}$ $\times [1.0 + \left(\frac{115188}{T}\right)^{0.407}]^{-2.242}$	Case A Case B	12
13	$\text{H}^- + \text{e}^- \rightarrow \text{H} + \text{e}^- + \text{e}^-$	$k_{13} = \exp[-1.801849334 \times 10^1$ $+ 2.36085220 \times 10^0 \ln T_e$ $- 2.82744300 \times 10^{-1} (\ln T_e)^2$ $+ 1.62331664 \times 10^{-2} (\ln T_e)^3$ $- 3.36501203 \times 10^{-2} (\ln T_e)^4$ $+ 1.17832978 \times 10^{-2} (\ln T_e)^5$ $- 1.65619470 \times 10^{-3} (\ln T_e)^6$ $+ 1.06827520 \times 10^{-4} (\ln T_e)^7$ $- 2.63128581 \times 10^{-6} (\ln T_e)^8]$		13



Table B1.1

		14	$H^- + H \rightarrow H + H + e^-$	$k_{14} = 2.5634 \times 10^{-9} T_e^{1.78186}$ $= \exp[-2.0372609 \times 10^1$ $+ 1.13944933 \times 10^0 \ln T_e$ $- 1.4210135 \times 10^{-1} (\ln T_e)^2$ $+ 8.4644554 \times 10^{-3} (\ln T_e)^3$ $- 1.4327641 \times 10^{-5} (\ln T_e)^4$ $+ 2.125988 \times 10^{-6} (\ln T_e)^5$ $+ 8.551632 \times 10^{-8} (\ln T_e)^6$ $- 2.5850057 \times 10^{-5} (\ln T_e)^7$ $+ 2.4555012 \times 10^{-6} (\ln T_e)^8$ $- 8.0683825 \times 10^{-8} (\ln T_e)^9]$	$T_e \leq 0.1 \text{ eV}$	13
1	$H^+$	15	$H^- + H^+ \rightarrow H_2^+ + e^-$	$k_{15} = 6.9 \times 10^{-9} T^{-0.35}$ $= 9.6 \times 10^{-7} T^{-0.90}$	$T_e > 0.1 \text{ eV}$ $T \leq 8000 \text{ K}$ $T > 8000 \text{ K}$	15
2	$H^-$	16	$He + e^- \rightarrow He^+ + e^- + e^-$	$k_{16} = \exp[-4.409864886 \times 10^1$ $+ 2.391596563 \times 10^1 \ln T_e$ $- 1.07532302 \times 10^1 (\ln T_e)^2$ $+ 3.05803875 \times 10^0 (\ln T_e)^3$ $- 5.6851189 \times 10^{-1} (\ln T_e)^4$ $+ 6.79539123 \times 10^{-2} (\ln T_e)^5$ $- 5.0090561 \times 10^{-3} (\ln T_e)^6$ $+ 2.06723616 \times 10^{-4} (\ln T_e)^7$ $- 3.64916141 \times 10^{-6} (\ln T_e)^8]$		13
3	$H^+$	17	$He^+ + e^- \rightarrow He + \gamma$	$k_{17,tr,A} = 10^{-11} T^{-0.5} [12.72 - 1.615 \log T$ $- 0.3162(\log T)^2 + 0.0493(\log T)^3]$ $k_{17,tr,B} = 10^{-11} T^{-0.5} [11.19 - 1.676 \log T$ $- 0.2852(\log T)^2 + 0.04433(\log T)^3]$ $k_{17,di} = 1.9 \times 10^{-3} T^{-1.5} \exp\left(-\frac{473421}{T}\right)$ $\times [1.0 + 0.3 \exp\left(-\frac{946841}{T}\right)]^{0.25}$	Case A Case B 17	16
4	$H^+$	18	$He^+ + H \rightarrow He + H^+$	$k_{18} = 1.25 \times 10^{-15} \left(\frac{T}{300}\right)^{-0.6}$		18
5	$H^-$	19	$He + H^+ \rightarrow He^+ + H$	$k_{19} = 1.26 \times 10^{-9} T^{-0.75} \exp\left(-\frac{127500}{T}\right)$ $= 4.0 \times 10^{-37} T^{4.74}$	$T \leq 10000 \text{ K}$ $T > 10000 \text{ K}$	19
6	$H_2^+$	20	$C^+ + e^- \rightarrow C + \gamma$	$k_{20} = 4.67 \times 10^{-12} \left(\frac{T}{300}\right)^{-0.6}$ $= 1.23 \times 10^{-17} \left(\frac{T}{300}\right)^{2.49} \exp\left(\frac{21845.6}{T}\right)$ $= 9.62 \times 10^{-8} \left(\frac{T}{300}\right)^{-1.37} \exp\left(\frac{-115786.2}{T}\right)$	$T \leq 7950 \text{ K}$ $7950 \text{ K} < T \leq 21140 \text{ K}$ $T > 21140 \text{ K}$	20
7	$H_2$	21	$O^+ + e^- \rightarrow O + \gamma$	$k_{21} = 1.30 \times 10^{-10} T^{-0.64}$ $= 1.41 \times 10^{-10} T^{-0.66} + 7.4 \times 10^{-4} T^{-1.5}$ $\times \exp\left(-\frac{175000}{T}\right) [1.0 + 0.062 \times \exp\left(-\frac{145000}{T}\right)]$	$T \leq 400 \text{ K}$ $T > 400 \text{ K}$	21
8	$H_2$	22	$C + e^- \rightarrow C^+ + e^- + e^-$	$k_{22} = 6.85 \times 10^{-8} (0.193 + u)^{-1} u^{0.25} e^{-u}$	$u = 11.26/T_e$	22
9	$H_2$	23	$O + e^- \rightarrow O^+ + e^- + e^-$	$k_{23} = 3.59 \times 10^{-8} (0.073 + u)^{-1} u^{0.34} e^{-u}$	$u = 13.6/T_e$	22
		24	$O^+ + H \rightarrow O + H^+$	$k_{24} = 4.99 \times 10^{-11} T^{0.405} + 7.54 \times 10^{-10} T^{-0.458}$		23
		25	$O + H^+ \rightarrow O^+ + H$	$k_{25} = [1.08 \times 10^{-11} T^{0.517}$ $+ 4.00 \times 10^{-10} T^{0.00669}] \exp\left(-\frac{227}{T}\right)$		24
		26	$O + He^+ \rightarrow O^+ + He$	$k_{26} = 4.991 \times 10^{-15} \left(\frac{T}{10000}\right)^{0.3794} \exp\left(-\frac{T}{1121000}\right)$ $+ 2.780 \times 10^{-15} \left(\frac{T}{10000}\right)^{-0.2163} \exp\left(\frac{T}{815800}\right)$		25
11	$H^+$	27	$C + H^+ \rightarrow C^+ + H$	$k_{27} = 3.9 \times 10^{-16} T^{0.213}$		24
12	$H^+$	28	$C^+ + H \rightarrow C + H^+$	$k_{28} = 6.08 \times 10^{-14} \left(\frac{T}{10000}\right)^{1.96} \exp\left(-\frac{170000}{T}\right)$		24
		29	$C + He^+ \rightarrow C^+ + He$	$k_{29} = 8.58 \times 10^{-17} T^{0.357}$ $= 3.25 \times 10^{-17} T^{0.968}$ $= 2.77 \times 10^{-19} T^{1.597}$	$T \leq 200 \text{ K}$ $200 < T \leq 2000 \text{ K}$ $T > 2000 \text{ K}$	26
13	$H^-$	30	$H_2 + He \rightarrow H + H + He$	$k_{30,1} = \text{dex} [-27.029 + 3.801 \log(T) - 29487/T]$ $k_{30,2} = \text{dex} [-2.729 - 1.75 \log(T) - 23474/T]$ $n_{cr,He} = \text{dex} [5.0792(1.0 - 1.23 \times 10^{-5}(T - 2000))]$		27
		31	$OH + H \rightarrow O + H + H$	$k_{31} = 6.0 \times 10^{-9} \exp\left(-\frac{50900}{T}\right)$		28
		32	$HOC^+ + H_2 \rightarrow HCO^+ + H_2$	$k_{32} = 3.8 \times 10^{-10}$		29
		33	$HOC^+ + CO \rightarrow HCO^+ + CO$	$k_{33} = 4.0 \times 10^{-10}$		30
		34	$C + H_2 \rightarrow CH + H$	$k_{34} = 6.64 \times 10^{-10} \exp\left(-\frac{11700}{T}\right)$		31
		35	$CH + H \rightarrow C + H_2$	$k_{35} = 1.31 \times 10^{-10} \exp\left(-\frac{80}{T}\right)$		32

# chemical model 2



Table B1.1

No.	Reac.	$H^- + H \rightarrow H + H + e^-$	$k_{14} = 2.5634 \times 10^{-9} T_e^{1.78186}$	$T_e \leq 0.1 \text{ eV}$	13
14	$H^- + H \rightarrow H + H + e^-$	$k_{14} = 2.5634 \times 10^{-9} T_e^{1.78186}$			
36	$CH + H_2 \rightarrow CH_2 + H$	$k_{36} = 5.46 \times 10^{-10} \exp\left(-\frac{1943}{T}\right)$		33	
37	$CH + C \rightarrow C_2 + H$	$k_{37} = 6.59 \times 10^{-11}$		34	
38	$CH + O \rightarrow CO + H$	$k_{38} = 6.6 \times 10^{-11}$		35	
		$= 1.02 \times 10^{-10} \exp\left(-\frac{914}{T}\right)$	$T \leq 2000 \text{ K}$	36	
39	$CH_2^{+} + H \rightarrow CH_2 + H$	$k_{39} = 1.0 \times 10^{-10} \times 10^{-11}$	$T > 2000 \text{ K}$	37	
40	$CH_2 + O \rightarrow CO + H_2$	$k_{40} = 3.5 \times 10^{-10}$		38	
41	$CH_2 + O \rightarrow CO + H_2$	$k_{41} = 8.0 \times 10^{-11}$		39	
42	$C_2 + O \rightarrow CO + C$	$k_{42} = 5.0 \times 10^{-11} \left(\frac{T}{300}\right)^{0.5}$ $= 5.0 \times 10^{-11} \left(\frac{T}{300}\right)^{0.757}$	$T \leq 300 \text{ K}$	40	
2	$H^-$	15	$H^-$		
43	$O + H_2 \rightarrow OH + H$	$k_{43} = 3.14 \times 10^{-13} \left(\frac{T}{300}\right)^{2.7} \exp\left(-\frac{3150}{T}\right)$		42	
3	$H^+$	16	$He$		
44	$OH + H \rightarrow O + H_2$	$k_{44} = 6.99 \times 10^{-14} \left(\frac{T}{300}\right)^{2.8} \exp\left(-\frac{1950}{T}\right)$		43	
45	$OH + H_2 \rightarrow H_2O + H$	$k_{45} = 2.05 \times 10^{-12} \left(\frac{T}{300}\right)^{1.52} \exp\left(-\frac{1736}{T}\right)$		44	
46	$OH + C \rightarrow CO + H$	$k_{46} = 1.0 \times 10^{-10}$		34	
5	$H^-$	47	$OH + O \rightarrow O_2 + H$	$k_{47} = 3.50 \times 10^{-11}$	45
6	$H_2^+$			$= 1.77 \times 10^{-11} \exp\left(\frac{178}{T}\right)$	33
7	$H_2$	48	$OH + OH \rightarrow H_2O + H$	$k_{48} = 1.65 \times 10^{-12} \left(\frac{T}{300}\right)^{1.14} \exp\left(-\frac{50}{T}\right)$	34
		49	$H_2O + H \rightarrow H_2 + OH$	$k_{49} = 1.59 \times 10^{-11} \left(\frac{T}{300}\right)^{1.2} \exp\left(-\frac{9610}{T}\right)$	46
8	$H_2$	50	$O_2 + H \rightarrow OH + O$	$k_{50} = 2.61 \times 10^{-10} \exp\left(-\frac{8156}{T}\right)$	33
9	$H_2$	51	$O_2 + H_2 \rightarrow OH + OH$	$k_{51} = 3.16 \times 10^{-10} \exp\left(-\frac{21890}{T}\right)$	47
		52	$O_2 + C \rightarrow CO + O$	$k_{52} = 4.7 \times 10^{-11} \left(\frac{T}{300}\right)^{-0.34}$	34
		53	$CO + H \rightarrow C + OH$	$k_{53} = 1.1 \times 10^{-10} \left(\frac{T}{300}\right)^{0.5} \exp\left(-\frac{7700}{T}\right)$	28
		54	$H_2^+ + H_2 \rightarrow H_3^+ + H$	$k_{54} = 2.24 \times 10^{-9} \left(\frac{T}{300}\right)^{0.042} \exp\left(-\frac{T}{46600}\right)$	48
		55	$H_3^+ + H \rightarrow H_2^+ + H_2$	$k_{55} = 7.7 \times 10^{-9} \exp\left(-\frac{17560}{T}\right)$	49
		56	$C + H_2^+ \rightarrow CH^+ + H$	$k_{56} = 2.4 \times 10^{-9}$	28
		57	$C + H_3^+ \rightarrow CH^+ + H_2$	$k_{57} = 2.0 \times 10^{-9}$	28
		58	$C^+ + H_2 \rightarrow CH^+ + H$	$k_{58} = 1.0 \times 10^{-10} \exp\left(-\frac{4640}{T}\right)$	50
		59	$CH^+ + H \rightarrow C^+ + H_2$	$k_{59} = 7.5 \times 10^{-10}$	51
10	$H_2$	60	$CH^+ + H_2 \rightarrow CH_2^+ + H$	$k_{60} = 1.2 \times 10^{-9}$	51
		61	$CH^+ + O \rightarrow CO^+ + H$	$k_{61} = 3.5 \times 10^{-10}$	52
		62	$CH_2 + H^+ \rightarrow CH^+ + H_2$	$k_{62} = 1.4 \times 10^{-9}$	28
		63	$CH_2^+ + H \rightarrow CH^+ + H_2$	$k_{63} = 1.0 \times 10^{-9} \exp\left(-\frac{7080}{T}\right)$	28
		64	$CH_2^+ + H_2 \rightarrow CH_3^+ + H$	$k_{64} = 1.6 \times 10^{-9}$	53
		65	$CH_2^+ + O \rightarrow HCO^+ + H$	$k_{65} = 7.5 \times 10^{-10}$	28
		66	$CH_3^+ + H \rightarrow CH_2^+ + H_2$	$k_{66} = 7.0 \times 10^{-10} \exp\left(-\frac{10560}{T}\right)$	28
		67	$CH_3^+ + O \rightarrow HCO^+ + H_2$	$k_{67} = 4.0 \times 10^{-10}$	54
		68	$C_2 + O^+ \rightarrow CO^+ + C$	$k_{68} = 4.8 \times 10^{-10}$	28
		69	$O^+ + H_2 \rightarrow OH^+ + H$	$k_{69} = 1.7 \times 10^{-9}$	55
		70	$O + H_2^+ \rightarrow OH^+ + H$	$k_{70} = 1.5 \times 10^{-9}$	28
		71	$O + H_3^+ \rightarrow OH^+ + H_2$	$k_{71} = 8.4 \times 10^{-10}$	56
		72	$OH + H_3^+ \rightarrow H_2O^+ + H_2$	$k_{72} = 1.3 \times 10^{-9}$	28
		73	$OH + C^+ \rightarrow CO^+ + H$	$k_{73} = 7.7 \times 10^{-10}$	28
		74	$OH^+ + H_2 \rightarrow H_2O^+ + H$	$k_{74} = 1.01 \times 10^{-9}$	57
		75	$H_2O^+ + H_2 \rightarrow H_3O^+ + H$	$k_{75} = 6.4 \times 10^{-10}$	58
		76	$H_2O + H_3^+ \rightarrow H_3O^+ + H_2$	$k_{76} = 5.9 \times 10^{-9}$	59
		77	$H_2O + C^+ \rightarrow HCO^+ + H$	$k_{77} = 9.0 \times 10^{-10}$	60
		78	$H_2O + C^+ \rightarrow HOC^+ + H$	$k_{78} = 1.8 \times 10^{-9}$	60
		79	$H_3O^+ + C \rightarrow HCO^+ + H_2$	$k_{79} = 1.0 \times 10^{-11}$	28
		80	$O_2 + C^+ \rightarrow CO^+ + O$	$k_{80} = 3.8 \times 10^{-10}$	53
		81	$O_2 + C^+ \rightarrow CO + O^+$	$k_{81} = 6.2 \times 10^{-10}$	53
		82	$O_2 + CH_2^+ \rightarrow HCO^+ + OH$	$k_{82} = 9.1 \times 10^{-10}$	53
		83	$O_2^+ + C \rightarrow CO^+ + O$	$k_{83} = 5.2 \times 10^{-11}$	28
		84	$CO + H_3^+ \rightarrow HOC^+ + H_2$	$k_{84} = 2.7 \times 10^{-11}$	61
		85	$CO + H_3^+ \rightarrow HCO^+ + H_2$	$k_{85} = 1.7 \times 10^{-9}$	61
		86	$HCO^+ + C \rightarrow CO + CH^+$	$k_{86} = 1.1 \times 10^{-9}$	28
		87	$HCO^+ + H_2O \rightarrow CO + H_3O^+$	$k_{87} = 2.5 \times 10^{-9}$	62



## chemical model 2

Table B1.1

No.	Reac.				
14	$H^- + H \rightarrow H + H + e^-$	88	$H_2 + He^+ \rightarrow He + H_2^+$	$k_{88} = 7.2 \times 10^{-15}$	63
		36	$CH + H_2 \rightarrow$	89 $H_2 + He^+ \rightarrow He + H + H^+$ $k_{89} = 3.7 \times 10^{-14} \exp\left(\frac{35}{T}\right)$	63
		37	$CH + C \rightarrow$	90 $CH + H^+ \rightarrow CH^+ + H$ $k_{90} = 1.9 \times 10^{-9}$	28
		38	$CH + O \rightarrow$	91 $CH_2 + H^+ \rightarrow CH_2^+ + H$ $k_{91} = 1.4 \times 10^{-9}$	28
				92 $CH_2 + H_2^+ \rightarrow C^+ + He + H_2$ $k_{92} = 7.5 \times 10^{-10}$	28
		39	$C_2^{+/-} + e^- \rightarrow C_2^{+/-} + e^-$	$k_{93} = 1.0 \times 10^{-9}$	28
		40	$C_2H_2^+ + e^- \rightarrow OH + H_2^+$	$k_{94} = 1.1 \times 10^{-9}$	28
		41	$CH_2^+ + O \rightarrow$	95 $OH + H_2^+ \rightarrow OH + H_2$ $k_{95} = 1.1 \times 10^{-9}$	28
		42	$C_2 + O \rightarrow$	96 $H_2O + H^+ \rightarrow H_2O^+ + H$ $k_{96} = 6.9 \times 10^{-9}$	64
2	$H^-$	15	$H^-$	97 $H_2O + He^+ \rightarrow OH + He + H^+$ $k_{97} = 2.04 \times 10^{-10}$	65
		16	$He$	98 $H_2O + He^+ \rightarrow OH^+ + He + H$ $k_{98} = 2.86 \times 10^{-10}$	65
3	$H^+$	43	$O + H_2 \rightarrow$	99 $H_2O + He^+ \rightarrow H_2O^+ + He$ $k_{99} = 6.05 \times 10^{-11}$	65
		44	$OH + H \rightarrow$	100 $O_2 + H^+ \rightarrow O_2^+ + H$ $k_{100} = 2.0 \times 10^{-9}$	64
		45	$OH + H_2 \rightarrow$	101 $O_2 + He^+ \rightarrow O_2^+ + He$ $k_{101} = 3.3 \times 10^{-11}$	66
		46	$OH + C \rightarrow$	102 $O_2 + He^+ \rightarrow O^+ + O + He$ $k_{102} = 1.1 \times 10^{-9}$	66
		47	$OH + O \rightarrow$	103 $O_2^+ + C \rightarrow O_2 + C^+$ $k_{103} = 5.2 \times 10^{-11}$	28
		48	$OH + OH \rightarrow$	104 $CO + He^+ \rightarrow C^+ + O + He$ $k_{104} = 1.4 \times 10^{-9} \left(\frac{T}{300}\right)^{-0.5}$	67
		49	$H_2O + H \rightarrow$	105 $CO + He^+ \rightarrow C + O^+ + He$ $k_{105} = 1.4 \times 10^{-16} \left(\frac{T}{300}\right)^{-0.5}$	67
7	$H_2$	17	$He$	106 $CO^+ + H \rightarrow CO + H^+$ $k_{106} = 7.5 \times 10^{-10}$	68
		50	$O_2 + H \rightarrow$	107 $C^- + H^+ \rightarrow C + H$ $k_{107} = 2.3 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.5}$	28
		51	$O_2 + H_2 \rightarrow$	108 $O^- + H^+ \rightarrow O + H$ $k_{108} = 2.3 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.5}$	28
		52	$O_2 + C \rightarrow$	109 $He^+ + H^- \rightarrow He + H$ $k_{109} = 2.32 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.52} \exp\left(-\frac{T}{22400}\right)$	69
				110 $H_3^+ + e^- \rightarrow H_2 + H$ $k_{110} = 2.34 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.52}$	70
				111 $H_3^+ + e^- \rightarrow H + H + H$ $k_{111} = 4.36 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.52}$	70
				112 $CH^+ + e^- \rightarrow C + H$ $k_{112} = 7.0 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.5}$	71
8	$H_2$	18	$He^+$	113 $CH_2^+ + e^- \rightarrow CH + H$ $k_{113} = 1.6 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.6}$	72
9	$H_2$	19	$He$	114 $CH_2^+ + e^- \rightarrow C + H + H$ $k_{114} = 4.03 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.6}$	72
		20	$C^+$	115 $CH_2^+ + e^- \rightarrow C + H_2$ $k_{115} = 7.68 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.6}$	72
		57	$C^+ + H_3^+ \rightarrow$	116 $CH_3^+ + e^- \rightarrow CH_2 + H$ $k_{116} = 7.75 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.5}$	73
10	$H_2$	59	$CH^+ + H \rightarrow$	117 $CH_3^+ + e^- \rightarrow CH + H_2$ $k_{117} = 1.95 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.5}$	73
		60	$CH^+ + H_2 \rightarrow$	118 $CH_3^+ + e^- \rightarrow CH + H + H$ $k_{118} = 2.0 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.4}$	28
		61	$CH^+ + O \rightarrow$	119 $OH^+ + e^- \rightarrow O + H$ $k_{119} = 6.3 \times 10^{-9} \left(\frac{T}{300}\right)^{-0.48}$	74
		62	$CH_2 + H^+ \rightarrow$	120 $H_2O^+ + e^- \rightarrow O + H + H$ $k_{120} = 3.05 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.5}$	75
		63	$CH_2^+ + H \rightarrow$	121 $H_2O^+ + e^- \rightarrow O + H_2$ $k_{121} = 3.9 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.5}$	75
11	$H^+$	22	$C +$	122 $H_2O^+ + e^- \rightarrow OH + H$ $k_{122} = 8.6 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.5}$	75
		23	$O +$	123 $H_3O^+ + e^- \rightarrow H + H_2O$ $k_{123} = 1.08 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.5}$	76
		24	$O^+$	124 $H_3O^+ + e^- \rightarrow OH + H_2$ $k_{124} = 6.02 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.5}$	76
		25	$O^- +$	125 $H_3O^+ + e^- \rightarrow OH + H + H$ $k_{125} = 2.58 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.5}$	76
		26	$O^- + H_2 \rightarrow$	126 $H_3O^+ + e^- \rightarrow O + H + H_2$ $k_{126} = 5.6 \times 10^{-9} \left(\frac{T}{300}\right)^{-0.5}$	76
		70	$O + H_2^+ \rightarrow$	127 $O_2^+ + e^- \rightarrow O + O$ $k_{127} = 1.95 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.7}$	77
		71	$O + H_3^+ \rightarrow$	128 $CO^+ + e^- \rightarrow C + O$ $k_{128} = 2.75 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.55}$	78
12	$H^+$	72	$OH + H_3^+ \rightarrow$	129 $HCO^+ + e^- \rightarrow CO + H$ $k_{129} = 2.76 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.64}$	79
		73	$OH + C^+ \rightarrow$	130 $HCO^+ + e^- \rightarrow OH + C$ $k_{130} = 2.4 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.64}$	79
		74	$OH^+ + H_2 \rightarrow$	131 $HOC^+ + e^- \rightarrow CO + H$ $k_{131} = 1.1 \times 10^{-7} \left(\frac{T}{300}\right)^{-1.0}$	28
		75	$H_2O^+ + H \rightarrow$	132 $H^- + C \rightarrow CH + e^-$ $k_{132} = 1.0 \times 10^{-9}$	28
		76	$H_2O + H_3^+ \rightarrow$	133 $H^- + O \rightarrow OH + e^-$ $k_{133} = 1.0 \times 10^{-9}$	28
13	$H^-$	77	$H_2O + C^+ \rightarrow$	134 $H^- + OH \rightarrow H_2O + e^-$ $k_{134} = 1.0 \times 10^{-10}$	28
		78	$H_2O^+ + C \rightarrow$	135 $C^- + H \rightarrow CH + e^-$ $k_{135} = 5.0 \times 10^{-10}$	28
		79	$H_3O^+ + C \rightarrow$	136 $C^- + H_2 \rightarrow CH_2 + e^-$ $k_{136} = 1.0 \times 10^{-13}$	28
		80	$O_2 + C^+ \rightarrow$	137 $C^- + O \rightarrow CO + e^-$ $k_{137} = 5.0 \times 10^{-10}$	28
		81	$O_2 + C^+ \rightarrow$	138 $O^- + H \rightarrow OH + e^-$ $k_{138} = 5.0 \times 10^{-10}$	28
		82	$O_2 + CH_2^+ \rightarrow$	139 $O^- + H_2 \rightarrow H_2O + e^-$ $k_{139} = 7.0 \times 10^{-10}$	28
		83	$O_2^+ + C \rightarrow$	140 $O^- + C \rightarrow CO + e^-$ $k_{140} = 5.0 \times 10^{-10}$	28
		84	$CO + H_3^+ \rightarrow$	87 $HCO^+ + H_2O \rightarrow CO + H_3O^+$ $k_{87} = 2.5 \times 10^{-9}$	28
		85	$CO + H_3^+ \rightarrow$		
		86	$HCO^+ + C \rightarrow$		
		87	$HCO^+ + H_2O \rightarrow CO + H_3O^+$		



Table B1.1

No.	Reac.							
14	$H^- + H \rightarrow H + H + e^-$	88	$H_2 + He^+ \rightarrow He + H_2^+$	$k_{88} = 7.2 \times 10^{-15}$	63			
		36	$CH + H_2 \rightarrow$	$k_{89} = 3.7 \times 10^{-14} \exp\left(\frac{35}{T}\right)$	63			
		37	$CH + C \rightarrow$	$k_{90} = 1.9 \times 10^{-9}$	28			
		38	$CH + O \rightarrow$	$k_{91} = 1.4 \times 10^{-9}$	28			
		39	$C_2^+ + H \rightarrow C + H + e^-$	$k_{92} = 7.5 \times 10^{-10}$	28			
		40	$C_2^+ + O \rightarrow C + OH + e^-$	$k_{93} = 1.0 \times 10^{-9}$	28			
		41	$CH_2 + O \rightarrow OH + H + e^-$	$k_{94} = 1.1 \times 10^{-9}$	28			
		42	$C_2 + O \rightarrow$	$k_{95} = 1.1 \times 10^{-9}$	28			
		96	$H_2O + H^+ \rightarrow H_2O^+ + H$	$k_{96} = 6.9 \times 10^{-9}$	64			
		97	$H_2O + He^+ \rightarrow OH + He + H^+$	$k_{97} = 2.04 \times 10^{-10}$	65			
		98	$O + H_2 \rightarrow OH + H + e^-$	$k_{98} = 1.0 \times 10^{-10}$	28			
2	$H^-$	15	$H^-$					
		43	$O + H_2 \rightarrow$	99				
		16	$He$	142	$C + e^- \rightarrow C^- + \gamma$	$k_{142} = 2.25 \times 10^{-15}$	81	
		44	$OH + H \rightarrow$	143	$C + H \rightarrow CH + \gamma$	$k_{143} = 1.0 \times 10^{-17}$	82	
		45	$OH + H_2 \rightarrow$	144	$C + H_2 \rightarrow CH_2 + \gamma$	$k_{144} = 1.0 \times 10^{-17}$	82	
		46	$OH + C \rightarrow$	145	$C + C \rightarrow C_2 + \gamma$	$k_{145} = 4.36 \times 10^{-18} \left(\frac{T}{300}\right)^{0.35} \exp\left(-\frac{161.3}{T}\right)$	83	
		47	$OH + O \rightarrow$	146	$C + O \rightarrow CO + \gamma$	$k_{146} = 2.1 \times 10^{-19}$ $= 3.09 \times 10^{-17} \left(\frac{T}{300}\right)^{0.33} \exp\left(-\frac{1629}{T}\right)$	$T \leq 300 \text{ K}$ $T > 300 \text{ K}$	84
		48	$OH + OH \rightarrow$	147	$C^+ + H \rightarrow CH^+ + \gamma$	$k_{147} = 4.46 \times 10^{-16} T^{-0.5} \exp\left(-\frac{4.93}{T^{2/3}}\right)$	85	
		49	$H_2O + H \rightarrow$	148	$C^+ + H_2 \rightarrow CH_2^+ + \gamma$	$k_{148} = 4.0 \times 10^{-16} \left(\frac{T}{300}\right)^{-0.2}$	86	
		50	$O_2 + H \rightarrow$	149	$C^+ + O \rightarrow CO^+ + \gamma$	$k_{149} = 2.5 \times 10^{-18}$ $= 3.14 \times 10^{-18} \left(\frac{T}{300}\right)^{-0.15} \exp\left(\frac{68}{T}\right)$	$T \leq 300 \text{ K}$ $T > 300 \text{ K}$	87
		51	$O_2 + H_2 \rightarrow$					
		52	$O_2 + C \rightarrow$	150	$O + e^- \rightarrow O^- + \gamma$	$k_{150} = 1.5 \times 10^{-15}$	28	
		53	$CO + H \rightarrow$	151	$O + H \rightarrow OH + \gamma$	$k_{151} = 9.9 \times 10^{-19} \left(\frac{T}{300}\right)^{-0.38}$	28	
		54	$H_2^+ + H_2 \rightarrow$	152	$O + O \rightarrow O_2 + \gamma$	$k_{152} = 4.9 \times 10^{-20} \left(\frac{T}{300}\right)^{1.58}$	82	
		55	$H_3^+ + H \rightarrow$	153	$OH + H \rightarrow H_2O + \gamma$	$k_{153} = 5.26 \times 10^{-18} \left(\frac{T}{300}\right)^{-5.22} \exp\left(-\frac{90}{T}\right)$	88	
		56	$C + H_2^+ \rightarrow$	154	$H + H + H \rightarrow H_2 + H$	$k_{154} = 1.32 \times 10^{-32} \left(\frac{T}{300}\right)^{-0.38}$ $= 1.32 \times 10^{-32} \left(\frac{T}{300}\right)^{-1.0}$	$T \leq 300 \text{ K}$ $T > 300 \text{ K}$	89
		57	$C + H_3^+ \rightarrow$	155	$H + H + H_2 \rightarrow H_2 + H_2$	$k_{155} = 2.8 \times 10^{-31} T^{-0.6}$	91	
		58	$C^+ + H_2 \rightarrow$	156	$H + H + He \rightarrow H_2 + He$	$k_{156} = 6.9 \times 10^{-32} T^{-0.4}$	92	
		59	$CH^+ + H \rightarrow$	157	$C + C + M \rightarrow C_2 + M$	$k_{157} = 5.99 \times 10^{-33} \left(\frac{T}{5000}\right)^{-1.6}$ $= 5.99 \times 10^{-33} \left(\frac{T}{5000}\right)^{-0.64} \exp\left(\frac{5255}{T}\right)$	$T \leq 5000 \text{ K}$ $T > 5000 \text{ K}$	93
		60	$CH^+ + H_2 \rightarrow$					
		61	$CH^+ + O \rightarrow$	158	$C + O + M \rightarrow CO + M$	$k_{158} = 6.16 \times 10^{-29} \left(\frac{T}{300}\right)^{-3.08}$ $= 2.14 \times 10^{-29} \left(\frac{T}{300}\right)^{-3.08} \exp\left(\frac{2114}{T}\right)$	$T \leq 2000 \text{ K}$ $T > 2000 \text{ K}$	35
		62	$CH_2 + H^+ \rightarrow$					
		63	$CH_2^+ + H \rightarrow$	159	$C^+ + O + M \rightarrow CO^+ + M$	$k_{159} = 100 \times k_{210}$	67	
		64	$CH_2^+ + H_2 \rightarrow$	160	$C + O^+ + M \rightarrow CO^+ + M$	$k_{160} = 100 \times k_{210}$	67	
		65	$CH_2^+ + O \rightarrow$	161	$O + H + M \rightarrow OH + M$	$k_{161} = 4.33 \times 10^{-32} \left(\frac{T}{300}\right)^{-1.0}$	43	
		66	$CH_3^+ + H \rightarrow$	162	$OH + H + M \rightarrow H_2O + M$	$k_{162} = 2.56 \times 10^{-31} \left(\frac{T}{300}\right)^{-2.0}$	35	
		67	$CH_3^+ + O \rightarrow$	163	$O + O + M \rightarrow O_2 + M$	$k_{163} = 9.2 \times 10^{-34} \left(\frac{T}{300}\right)^{-1.0}$	37	
		68	$C_2 + O^+ \rightarrow$	164	$O + CH \rightarrow HCO^+ + e^-$	$k_{164} = 2.0 \times 10^{-11} \left(\frac{T}{300}\right)^{0.44}$	95	
		69	$O^+ + H_2 \rightarrow$	165	$H + H(s) \rightarrow H_2$	$k_{165} = 3.0 \times 10^{-18} T^{0.5} f_A [1.0 + 0.04(T + T_d)^{0.5}]$ $+ 0.002 T + 8 \times 10^{-6} T^2]^{-1}$	$f_A = \left[1.0 + 10^4 \exp\left(-\frac{600}{T_d}\right)\right]^{-1}$	96
		70	$O + H_2^+ \rightarrow$					
		71	$O + H_3^+ \rightarrow$					
		72	$OH + H_3^+ \rightarrow$					
		73	$OH + C^+ \rightarrow$					
		74	$OH^+ + H_2 \rightarrow$	129	$HCO^+ + e^- \rightarrow CO + H$	$k_{129} = 2.76 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.64}$	79	
		75	$H_2O^+ + H \rightarrow$	130	$HCO^+ + e^- \rightarrow OH + C$	$k_{130} = 2.4 \times 10^{-8} \left(\frac{T}{300}\right)^{-0.64}$	79	
		76	$H_2O + H_3^+ \rightarrow$	131	$HOC^+ + e^- \rightarrow CO + H$	$k_{131} = 1.1 \times 10^{-7} \left(\frac{T}{300}\right)^{-1.0}$	28	
		77	$H_2O + C^+ \rightarrow$	132	$H^- + C \rightarrow CH + e^-$	$k_{132} = 1.0 \times 10^{-9}$	28	
		78	$H_2O + C^- \rightarrow$	133	$H^- + O \rightarrow OH + e^-$	$k_{133} = 1.0 \times 10^{-9}$	28	
		79	$H_3O^+ + C \rightarrow$	134	$H^- + OH \rightarrow H_2O + e^-$	$k_{134} = 1.0 \times 10^{-10}$	28	
		80	$O_2 + C^+ \rightarrow$	135	$C^- + H \rightarrow CH + e^-$	$k_{135} = 5.0 \times 10^{-10}$	28	
		81	$O_2 + C^- \rightarrow$	136	$C^- + H_2 \rightarrow CH_2 + e^-$	$k_{136} = 1.0 \times 10^{-13}$	28	
		82	$O_2 + CH_2 \rightarrow$	137	$C^- + O \rightarrow CO + e^-$	$k_{137} = 5.0 \times 10^{-10}$	28	
		83	$O_2^+ + C \rightarrow$	138	$O^- + H \rightarrow OH + e^-$	$k_{138} = 5.0 \times 10^{-10}$	28	
		84	$CO + H_3^+ \rightarrow$	139	$O^- + H_2 \rightarrow H_2O + e^-$	$k_{139} = 7.0 \times 10^{-10}$	28	
		85	$CO + H_3^- \rightarrow$	140	$O^- + C \rightarrow CO + e^-$	$k_{140} = 5.0 \times 10^{-10}$	28	
		86	$HCO^+ + C \rightarrow$					
		87	$HCO^+ + H_2O \rightarrow CO + H_3O^+$			$k_{87} = 2.5 \times 10^{-9}$	28	



Table B1.1

14	H <sup>-</sup> + H → H + H + e <sup>-</sup>	88	H <sub>2</sub> + He <sup>+</sup> → He + H <sub>2</sub> <sup>+</sup>	$k_{88} = 7.2 \times 10^{-15}$	63
36	CH + H <sub>2</sub> →	89	H <sub>2</sub> + He <sup>+</sup> → He + H + H <sup>+</sup>	$k_{89} = 3.7 \times 10^{-14} \exp\left(\frac{35}{T}\right)$	63
37	CH + C →	90	CH + H <sup>+</sup> → CH <sup>+</sup> + H	$k_{90} = 1.9 \times 10^{-9}$	28
38	CH + O →	91	CH <sub>2</sub> + H <sup>+</sup> → CH <sub>2</sub> <sup>+</sup> + H	$k_{91} = 1.4 \times 10^{-9}$	28
		92	CH <sub>2</sub> + H <sup>+</sup> → C <sup>+</sup> + He + H <sub>2</sub>	$k_{92} = 7.5 \times 10^{-10}$	28
39	C <sub>2</sub> <sup>+</sup> + e <sup>-</sup> →	93	OH + OH <sup>+</sup> → H <sub>2</sub> O + e <sup>-</sup>	$k_{93} = 1.1 \times 10^{-9}$	28
40	C <sub>2</sub> <sup>+</sup> + O →	94	OH <sup>+</sup> + H <sub>2</sub> → H <sub>2</sub> O + H	$k_{94} = 1.1 \times 10^{-9}$	28
41	CH <sub>2</sub> + O →	95	H <sub>2</sub> O + H <sup>+</sup> → H <sub>2</sub> O <sup>+</sup> + H	$k_{95} = 1.1 \times 10^{-9}$	28
		96	H <sub>2</sub> O + H <sup>+</sup> → OH + He + H <sup>+</sup>	$k_{96} = 6.9 \times 10^{-9}$	64
42	C <sub>2</sub> + O →	97	H <sub>2</sub> O + He <sup>+</sup> → OH + He + H <sup>+</sup>	$k_{97} = 2.04 \times 10^{-10}$	65
		98	H <sub>2</sub> O + H <sup>+</sup> → OH + He + H <sup>+</sup>	$k_{98} = 2.04 \times 10^{-10}$	65

Table B2. List of photochemical reactions included in our chemical model

No.	Reaction	Optically thin rate ( $s^{-1}$ )	$\gamma$	Ref.	
166	H <sup>-</sup> + $\gamma$ → H + e <sup>-</sup>	$R_{166} = 7.1 \times 10^{-7}$	0.5	1	
167	H <sub>2</sub> <sup>+</sup> + $\gamma$ → H + H <sup>+</sup>	$R_{167} = 1.1 \times 10^{-9}$	1.9	2	
168	H <sub>2</sub> + $\gamma$ → H + H	$R_{168} = 5.6 \times 10^{-11}$	See §2.2	3	
169	H <sub>3</sub> <sup>+</sup> + $\gamma$ → H <sub>2</sub> + H <sup>+</sup>	$R_{169} = 4.9 \times 10^{-13}$	1.8	4	
170	H <sub>3</sub> <sup>+</sup> + $\gamma$ → H <sub>2</sub> <sup>+</sup> + H	$R_{170} = 4.9 \times 10^{-13}$	2.3	4	
171	C + $\gamma$ → C <sup>+</sup> + e <sup>-</sup>	$R_{171} = 3.1 \times 10^{-10}$	3.0	5	
172	C <sup>-</sup> + $\gamma$ → C + e <sup>-</sup>	$R_{172} = 2.4 \times 10^{-7}$	0.9	6	
173	CH + $\gamma$ → C + H	$R_{173} = 8.7 \times 10^{-10}$	1.2	7	
174	CH + $\gamma$ → CH <sup>+</sup> + e <sup>-</sup>	$R_{174} = 7.7 \times 10^{-10}$	2.8	8	
175	CH <sup>+</sup> + $\gamma$ → C + H <sup>+</sup>	$R_{175} = 2.6 \times 10^{-10}$	2.5	7	
176	CH <sub>2</sub> + $\gamma$ → CH + H	$R_{176} = 7.1 \times 10^{-10}$	1.7	7	
177	CH <sub>2</sub> + $\gamma$ → CH <sub>2</sub> <sup>+</sup> + e <sup>-</sup>	$R_{177} = 5.9 \times 10^{-10}$	2.3	6	
178	CH <sub>2</sub> <sup>+</sup> + $\gamma$ → CH <sup>+</sup> + H	$R_{178} = 4.6 \times 10^{-10}$	1.7	9	
179	CH <sub>3</sub> <sup>+</sup> + $\gamma$ → CH <sub>2</sub> <sup>+</sup> + H	$R_{179} = 1.0 \times 10^{-9}$	1.7	6	
180	CH <sub>3</sub> <sup>+</sup> + $\gamma$ → CH <sup>+</sup> + H <sub>2</sub>	$R_{180} = 1.0 \times 10^{-9}$	1.7	6	
181	C <sub>2</sub> + $\gamma$ → C + C	$R_{181} = 1.5 \times 10^{-10}$	2.1	7	
182	O <sup>-</sup> + $\gamma$ → O + e <sup>-</sup>	$R_{182} = 2.4 \times 10^{-7}$	0.5	6	
183	OH + $\gamma$ → O + H	$R_{183} = 3.7 \times 10^{-10}$	1.7	10	
184	OH + $\gamma$ → OH <sup>+</sup> + e <sup>-</sup>	$R_{184} = 1.6 \times 10^{-12}$	3.1	6	
185	OH <sup>+</sup> + $\gamma$ → O + H <sup>+</sup>	$R_{185} = 1.0 \times 10^{-12}$	1.8	4	
186	H <sub>2</sub> O + $\gamma$ → OH + H	$R_{186} = 6.0 \times 10^{-10}$	1.7	11	
187	H <sub>2</sub> O + $\gamma$ → H <sub>2</sub> O <sup>+</sup> + e <sup>-</sup>	$R_{187} = 3.2 \times 10^{-11}$	3.9	8	
188	H <sub>2</sub> O <sup>+</sup> + $\gamma$ → H <sub>2</sub> <sup>+</sup> + O	See §2.2	12		
189	H <sub>2</sub> O <sup>+</sup> + $\gamma$ → H <sup>+</sup> + OH	See §2.2	12		
190	H <sub>2</sub> O <sup>+</sup> + $\gamma$ → O <sup>+</sup> + H <sub>2</sub>	$R_{190} = 5.0 \times 10^{-11}$	See §2.2	12	
191	H <sub>2</sub> O <sup>+</sup> + $\gamma$ → OH <sup>+</sup> + H	See §2.2	12		
192	H <sub>3</sub> O <sup>+</sup> + $\gamma$ → H <sup>+</sup> + H <sub>2</sub> O	See §2.2	12		
193	H <sub>3</sub> O <sup>+</sup> + $\gamma$ → H <sub>2</sub> <sup>+</sup> + OH	See §2.2	12		
194	H <sub>3</sub> O <sup>+</sup> + $\gamma$ → H <sub>2</sub> O <sup>+</sup> + H	See §2.2	12		
195	H <sub>3</sub> O <sup>+</sup> + $\gamma$ → OH <sup>+</sup> + H <sub>2</sub>	See §2.2	12		
196	O <sub>2</sub> + $\gamma$ → O <sub>2</sub> <sup>+</sup> + e <sup>-</sup>	$R_{196} = 5.6 \times 10^{-11}$	3.7	7	
197	O <sub>2</sub> + $\gamma$ → O + O	$R_{197} = 7.0 \times 10^{-10}$	1.8	7	
198	CO + $\gamma$ → C + O	$R_{198} = 2.0 \times 10^{-10}$	See §2.2	13	
86	HCO <sup>+</sup> + C → CO + e <sup>-</sup>	$k_{140} = 5.0 \times 10^{-10}$			28
87	HCO <sup>+</sup> + H <sub>2</sub> O → CO + H <sub>3</sub> O <sup>+</sup>	$k_{87} = 2.5 \times 10^{-9}$			28



# chemical model 2

Table B1.1

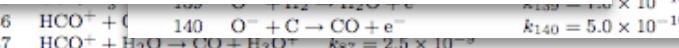
14	H <sup>-</sup> + H → H + H + e <sup>-</sup>	88	H <sub>2</sub> + He <sup>+</sup> → He + H <sub>2</sub> <sup>+</sup>	$k_{88} = 7.2 \times 10^{-15}$	63
36	CH + H <sub>2</sub>	89	H <sub>2</sub> + He <sup>+</sup> → He + H + H <sup>+</sup>	$k_{89} = 3.7 \times 10^{-14} \exp\left(\frac{35}{T}\right)$	63
37	CH + C	90	CH + H <sup>+</sup> → CH <sup>+</sup> + H	$k_{90} = 1.9 \times 10^{-9}$	28
38	CH + O	91	CH <sub>2</sub> + H <sup>+</sup> → CH <sub>2</sub> <sup>+</sup> + H	$k_{91} = 1.4 \times 10^{-9}$	28
		92	CH <sub>2</sub> + H <sup>+</sup> → C <sup>+</sup> + He + H <sub>2</sub>	$k_{92} = 7.5 \times 10^{-10}$	28
39	C <sub>2</sub> <sup>+</sup> + e <sup>-</sup>	93	OH + OH <sup>+</sup> → H <sub>2</sub> O <sup>+</sup> + e <sup>-</sup>	$k_{93} = 1.1 \times 10^{-9}$	28
40	C <sub>2</sub> <sup>+</sup> + e <sup>-</sup>	94	OH <sub>2</sub> <sup>+</sup> + H → OH + H <sub>2</sub>	$k_{94} = 1.1 \times 10^{-9}$	28
41	CH <sub>2</sub> <sup>+</sup> + O	95	H <sub>2</sub> O + H <sup>+</sup> → H <sub>2</sub> O <sup>+</sup> + H	$k_{95} = 1.1 \times 10^{-9}$	28
		96	H <sub>2</sub> O + H <sup>+</sup> → OH + He + H <sup>+</sup>	$k_{96} = 6.9 \times 10^{-9}$	64
42	C <sub>2</sub> + O →	97	H <sub>2</sub> O + He <sup>+</sup> → OH + He + H <sup>+</sup>	$k_{97} = 2.04 \times 10^{-10}$	65
		98	H <sub>2</sub> O + H <sup>+</sup> → OH + He + H <sup>+</sup>	$k_{98} = 2.04 \times 10^{-10}$	65

Table B2. List of photochemical reactions included in our chemical model

No.	Reaction	Optically thin rate ( $s^{-1}$ )	$\gamma$	Ref.
166	H <sup>-</sup> + $\gamma$ → H + e <sup>-</sup>	$R_{166} = 7.1 \times 10^{-7}$	0.5	1
167	H <sub>2</sub> <sup>+</sup> + $\gamma$ → H + H <sup>+</sup>	$R_{167} = 1.1 \times 10^{-9}$	1.9	2
168	H <sub>2</sub> + $\gamma$ → H + H	$R_{168} = 5.6 \times 10^{-11}$	See §2.2	3
169	H <sub>3</sub> <sup>+</sup> + $\gamma$ → H <sub>2</sub> + H <sup>+</sup>	$R_{169} = 4.9 \times 10^{-13}$	1.8	4
170	H <sub>3</sub> <sup>+</sup> + $\gamma$ → H <sub>2</sub> <sup>+</sup> + H	$R_{170} = 4.9 \times 10^{-13}$	2.3	4
171	C + $\gamma$ → C <sup>+</sup> + e <sup>-</sup>	$R_{171} = 2.1 \times 10^{-10}$	—	—

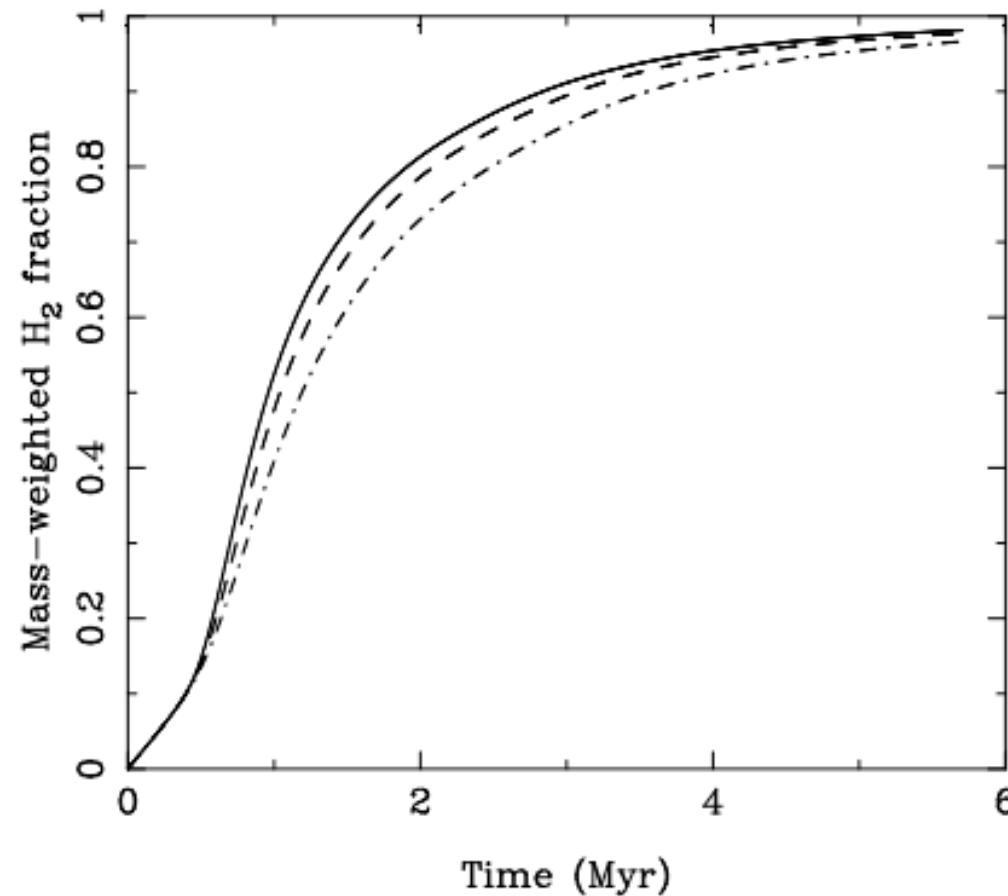
Table B3. List of reactions included in our chemical model that involve cosmic rays or cosmic-ray induced UV emission

No.	Reaction	Rate ( $s^{-1} \zeta_H^{-1}$ )	Ref.
176	CH <sub>2</sub> + $\gamma$	199 H + c.r. → H <sup>+</sup> + e <sup>-</sup>	$R_{199} = 1.0$
177	CH <sub>2</sub> + $\gamma$	200 He + c.r. → He <sup>+</sup> + e <sup>-</sup>	$R_{200} = 1.1$
178	CH <sub>2</sub> <sup>+</sup> + $\gamma$	201 H <sub>2</sub> + c.r. → H <sup>+</sup> + H + e <sup>-</sup>	$R_{201} = 0.037$
179	CH <sub>3</sub> <sup>+</sup> + $\gamma$	202 H <sub>2</sub> + c.r. → H + H	$R_{202} = 0.22$
180	CH <sub>3</sub> <sup>+</sup> + $\gamma$	203 H <sub>2</sub> + c.r. → H <sup>+</sup> + H <sup>-</sup>	$R_{203} = 6.5 \times 10^{-4}$
181	C <sub>2</sub> + $\gamma$	204 H <sub>2</sub> + c.r. → H <sub>2</sub> <sup>+</sup> + e <sup>-</sup>	$R_{204} = 2.0$
182	O <sup>-</sup> + $\gamma$	205 C + c.r. → C <sup>+</sup> + e <sup>-</sup>	$R_{205} = 3.8$
183	OH + $\gamma$	206 O + c.r. → O <sup>+</sup> + e <sup>-</sup>	$R_{206} = 5.7$
184	OH + $\gamma$	207 CO + c.r. → CO <sup>+</sup> + e <sup>-</sup>	$R_{207} = 6.5$
185	OH <sup>+</sup> + $\gamma$	208 C + $\gamma$ c.r. → C <sup>+</sup> + e <sup>-</sup>	$R_{208} = 2800$
186	H <sub>2</sub> O + $\gamma$	209 CH + $\gamma$ c.r. → C + H	$R_{209} = 4000$
187	H <sub>2</sub> O + $\gamma$	210 CH <sup>+</sup> + $\gamma$ c.r. → C <sup>+</sup> + H	$R_{210} = 960$
188	H <sub>2</sub> O <sup>+</sup> + $\gamma$	211 CH <sub>2</sub> + $\gamma$ c.r. → CH <sub>2</sub> <sup>+</sup> + e <sup>-</sup>	$R_{211} = 2700$
189	H <sub>2</sub> O <sup>+</sup> + $\gamma$	212 CH <sub>2</sub> + $\gamma$ c.r. → CH + H	$R_{212} = 2700$
190	H <sub>2</sub> O <sup>+</sup> + $\gamma$	213 C <sub>2</sub> + $\gamma$ c.r. → C + C	$R_{213} = 1300$
191	H <sub>2</sub> O <sup>+</sup> + $\gamma$	214 OH + $\gamma$ c.r. → O + H	$R_{214} = 2800$
192	H <sub>3</sub> O <sup>+</sup> + $\gamma$	215 H <sub>2</sub> O + $\gamma$ c.r. → OH + H	$R_{215} = 5300$
193	H <sub>3</sub> O <sup>+</sup> + $\gamma$	216 O <sub>2</sub> + $\gamma$ c.r. → O + O	$R_{216} = 4100$
194	H <sub>3</sub> O <sup>+</sup> + $\gamma$	217 O <sub>2</sub> + $\gamma$ c.r. → O <sub>2</sub> <sup>+</sup> + e <sup>-</sup>	$R_{217} = 640$
195	H <sub>3</sub> O <sup>+</sup> + $\gamma$	218 CO + $\gamma$ c.r. → C + O	$R_{218} = 0.21 T^{1/2} x_{H_2} x_{CO}^{-1/2}$
196	O <sub>2</sub> + $\gamma$		4
197	O <sub>2</sub> + $\gamma$ → O + O	$R_{197} = 7.0 \times 10^{-10}$	1.8
198	CO + $\gamma$ → C + O	$R_{198} = 2.0 \times 10^{-10}$	See §2.2





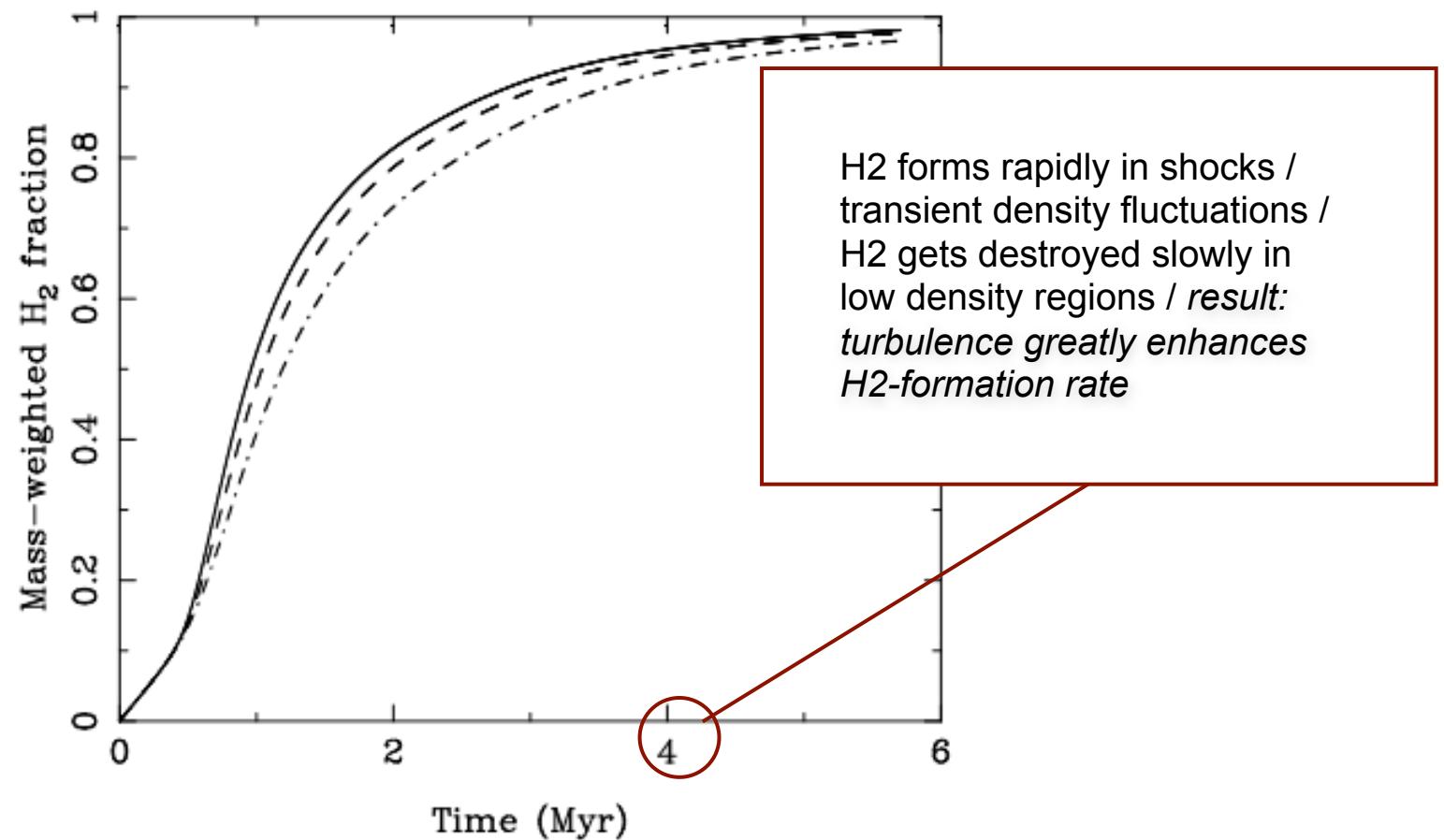
# HI to H<sub>2</sub> conversion rate



**Figure 4.** Time evolution of the mass-weighted H<sub>2</sub> abundance in simulations R1, R2 and R3, which have numerical resolutions of 64<sup>3</sup> zones (dot-dashed), 128<sup>3</sup> zones (dashed) and 256<sup>3</sup> zones (solid), respectively.



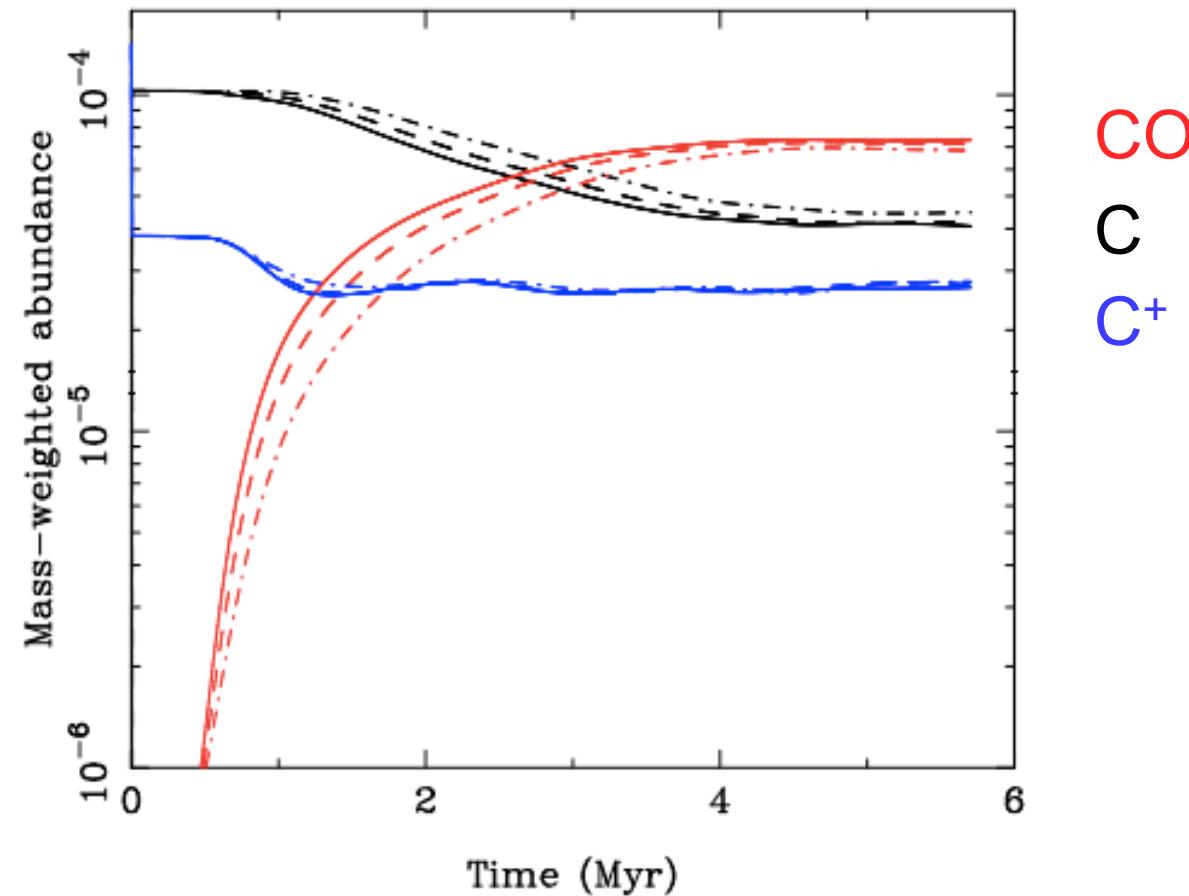
# HI to H<sub>2</sub> conversion rate



**Figure 4.** Time evolution of the mass-weighted H<sub>2</sub> abundance in simulations R1, R2 and R3, which have numerical resolutions of 64<sup>3</sup> zones (dot-dashed), 128<sup>3</sup> zones (dashed) and 256<sup>3</sup> zones (solid), respectively.



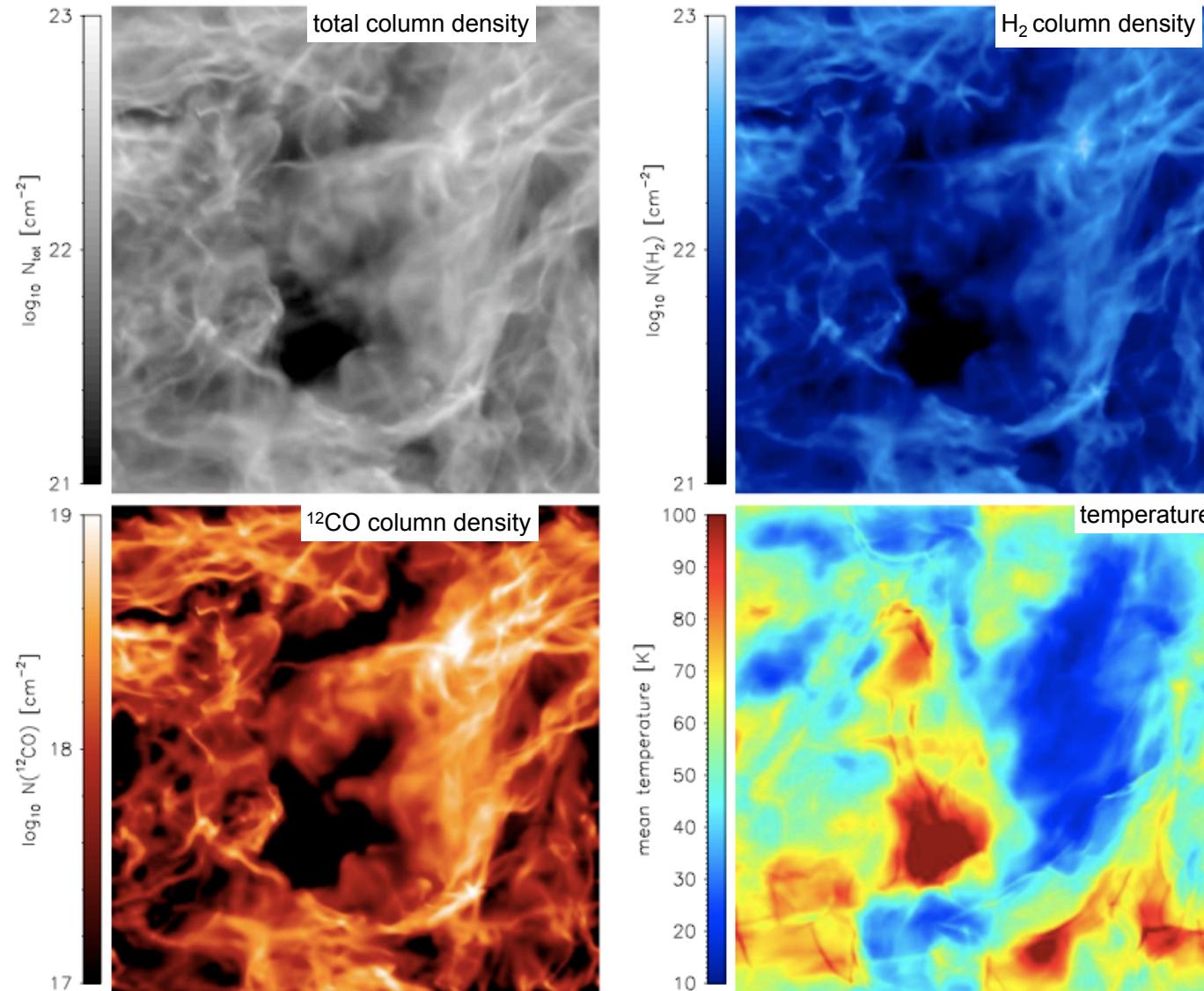
# CO, C<sup>+</sup> formation rates



**Figure 5.** Time evolution of the mass-weighted abundances of atomic carbon (black lines), CO (red lines), and C<sup>+</sup> (blue lines) in simulations with numerical resolutions of  $64^3$  zones (dot-dashed),  $128^3$  zones (dashed) and  $256^3$  zones (solid).



# effects of chemistry 1

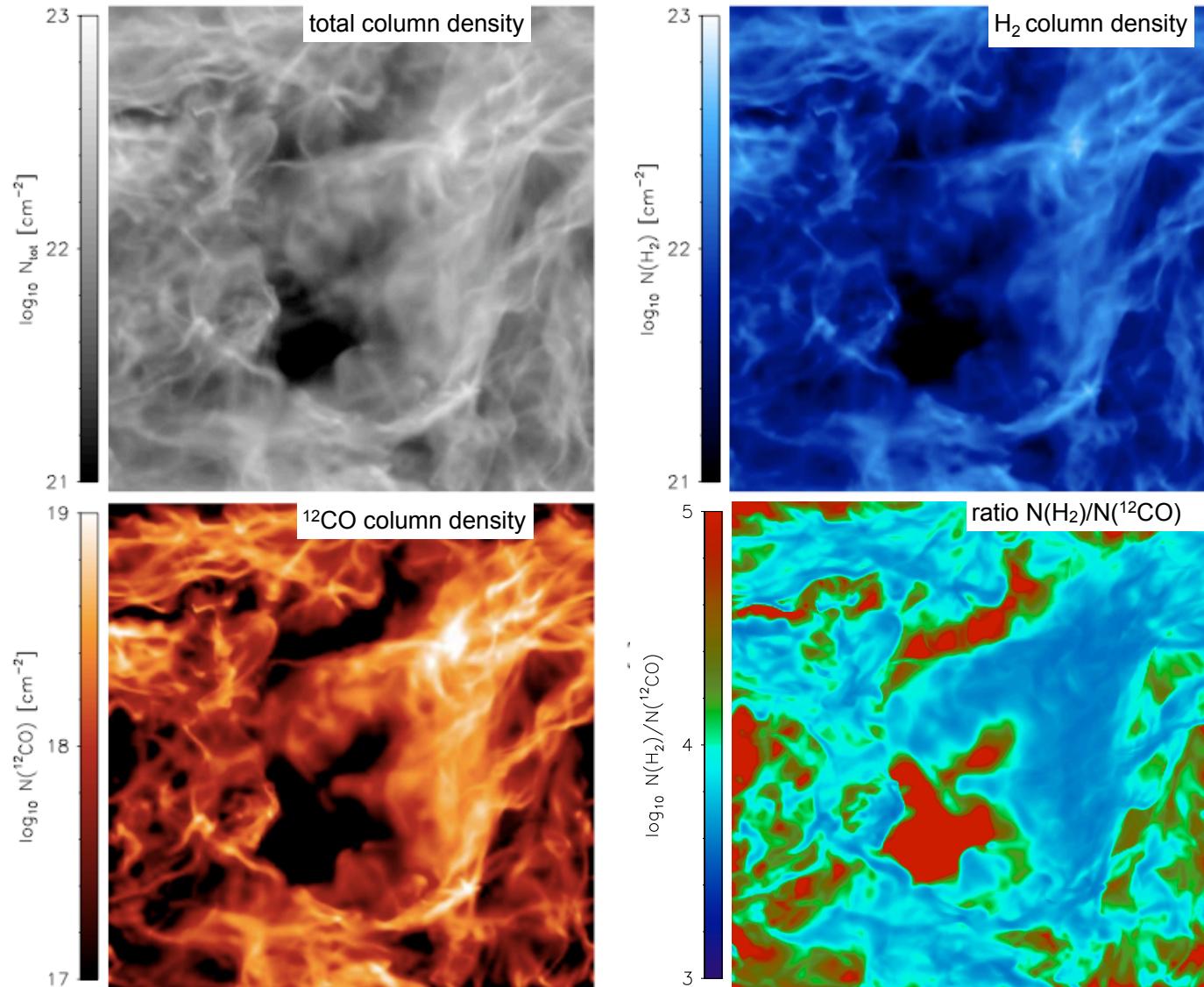


(Glover, Federrath, Mac Low, Klessen, in prep)

Ralf Klessen: Spineto 09.07.09



# effects of chemistry 2

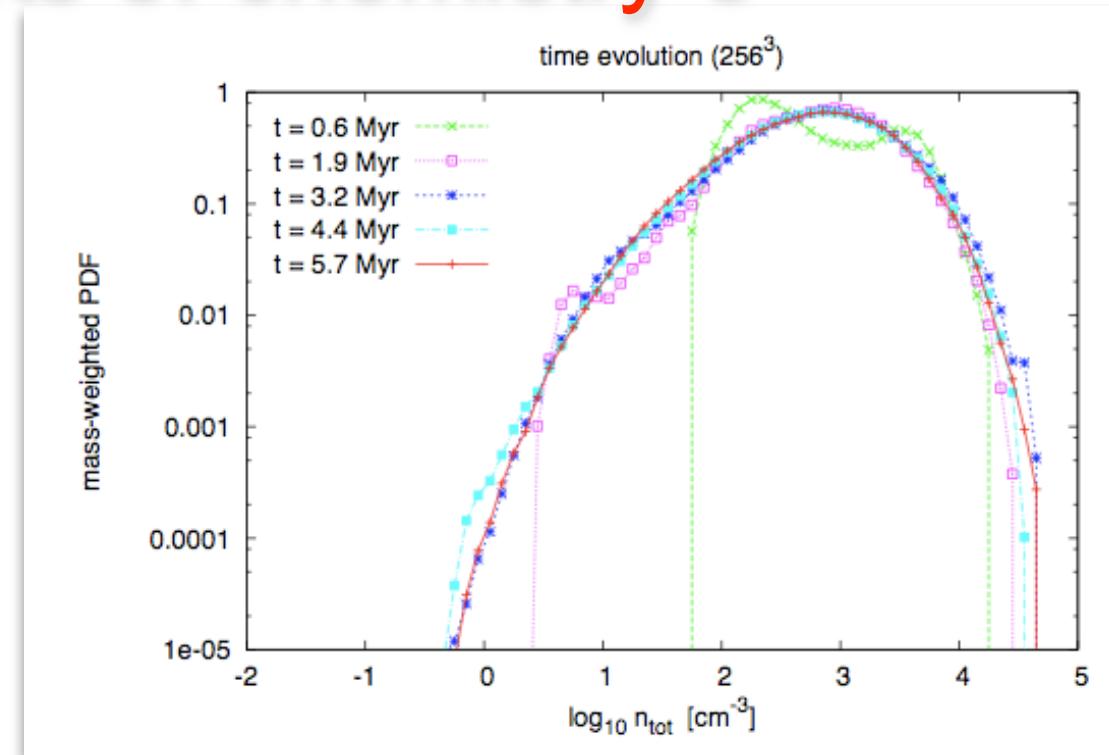


(Glover, Federrath, Mac Low, Klessen, in prep)

Ralf Klessen: Spineto 09.07.09

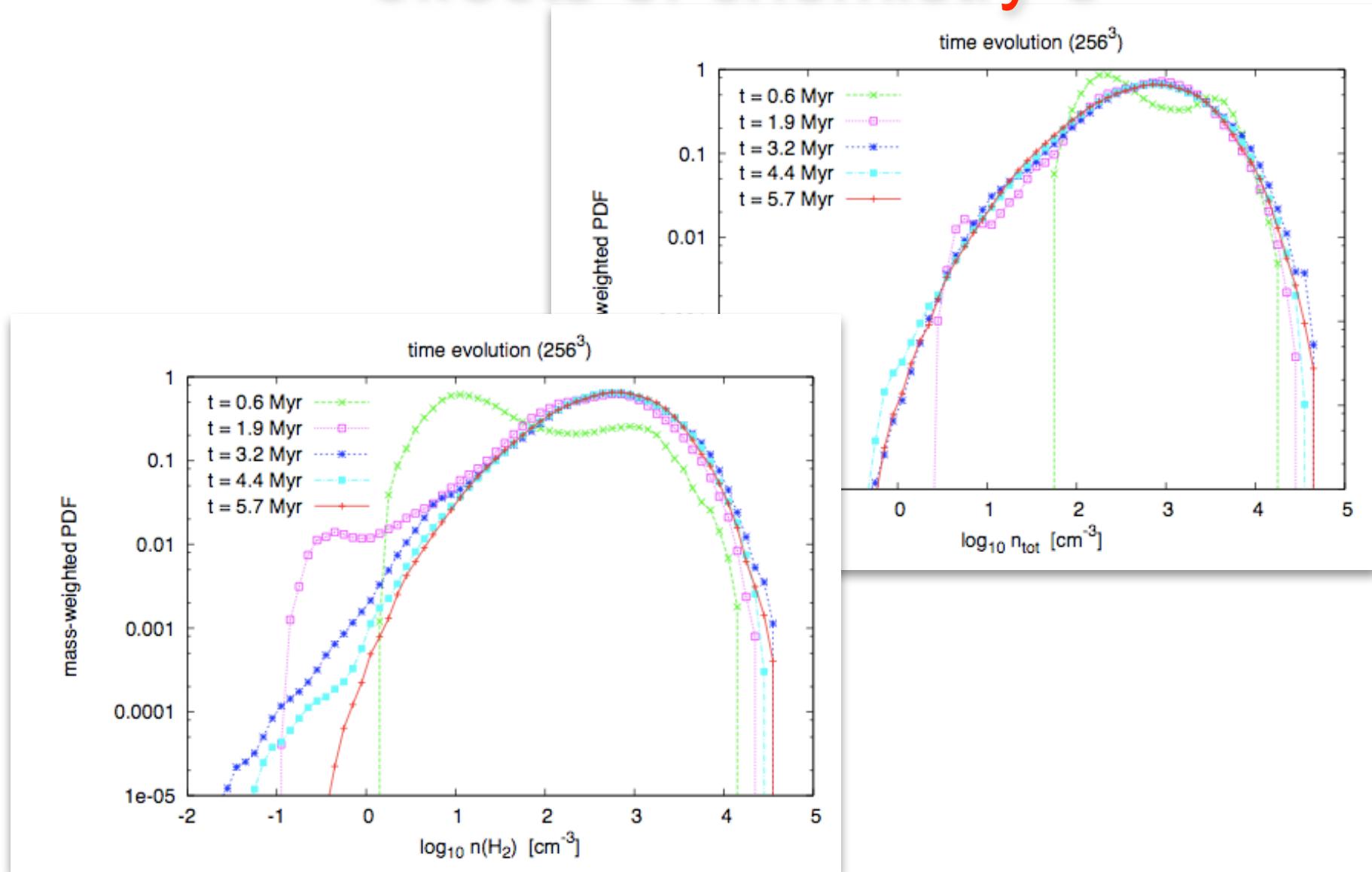


# effects of chemistry 3



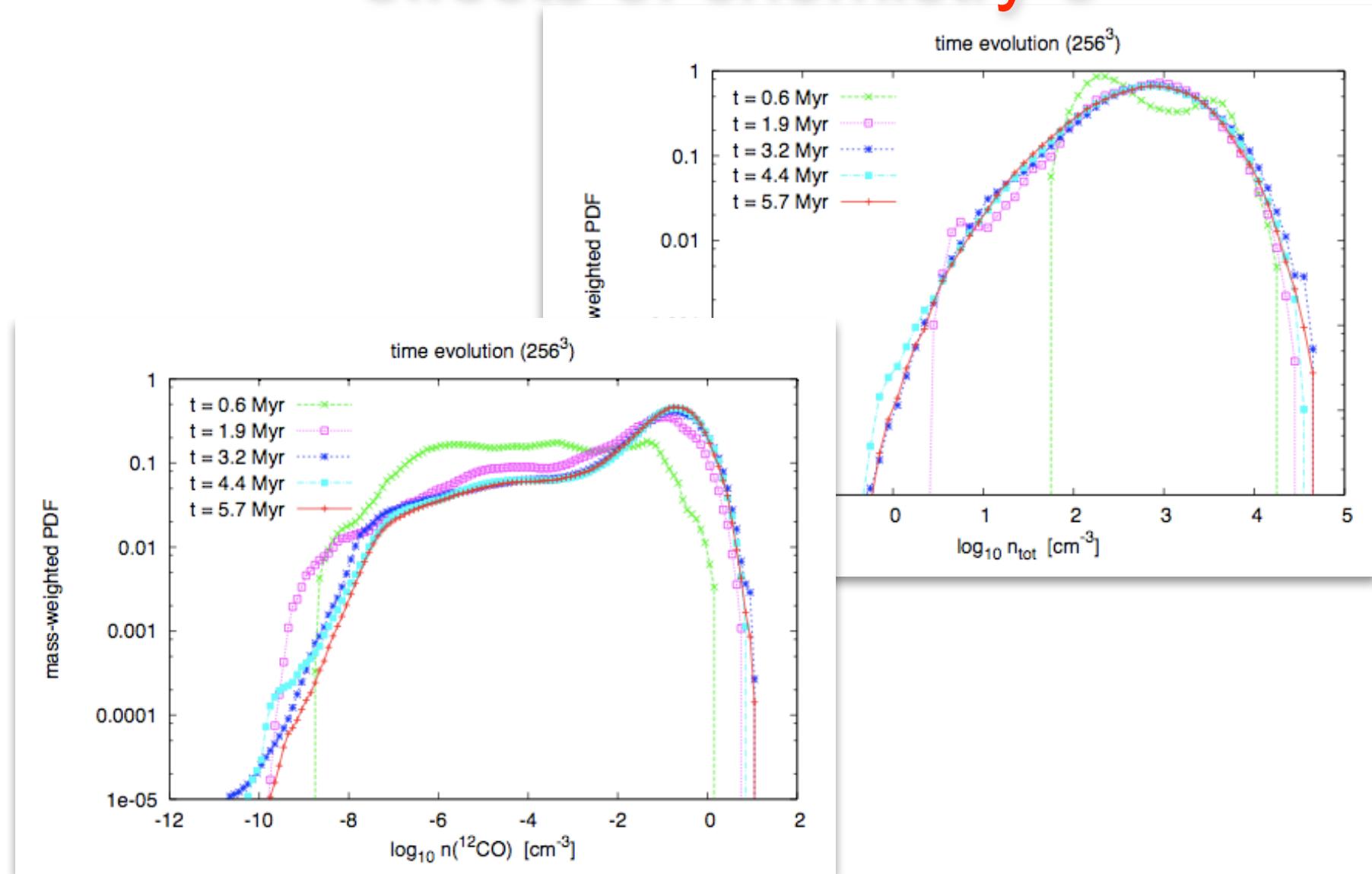


# effects of chemistry 3



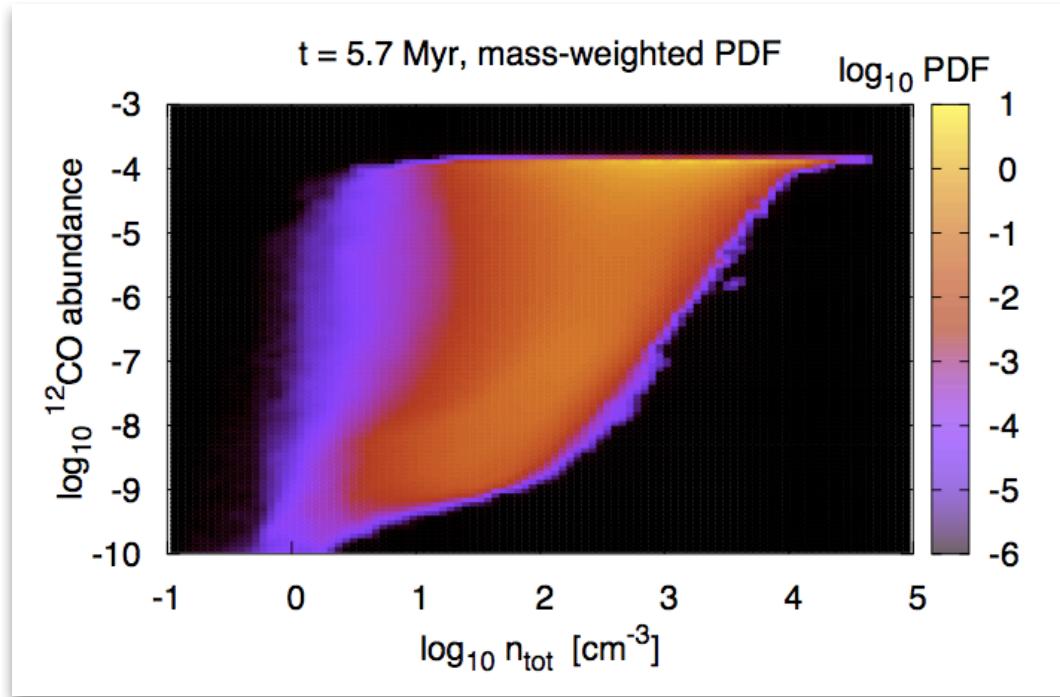


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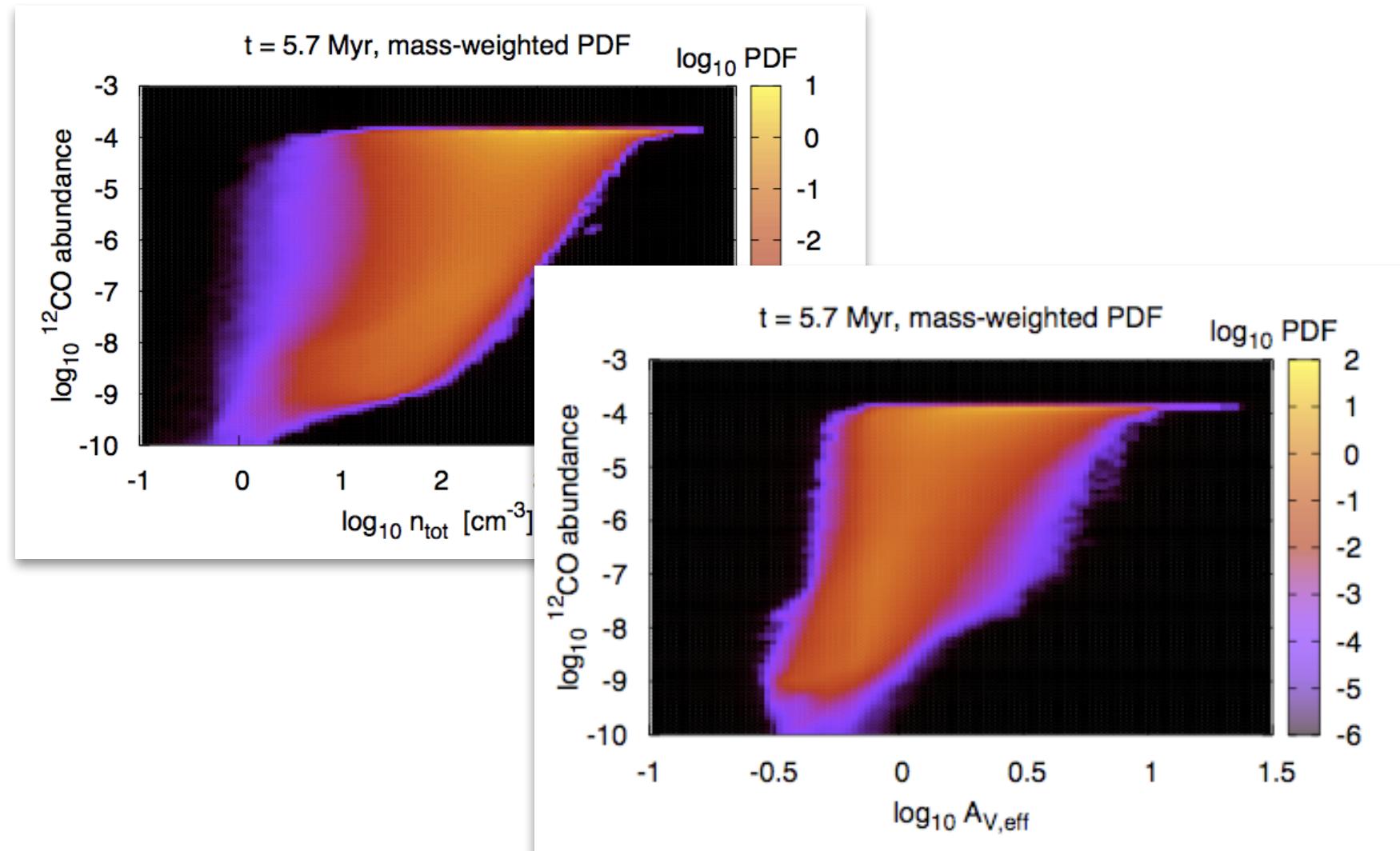


# effects of chemistry 3





# effects of chemistry 3





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turbulence



# Properties of turbulence

- laminar flows turn *turbulent* at *high* Reynolds numbers

$$Re = \frac{\text{advection}}{\text{dissipation}} = \frac{VL}{\nu}$$

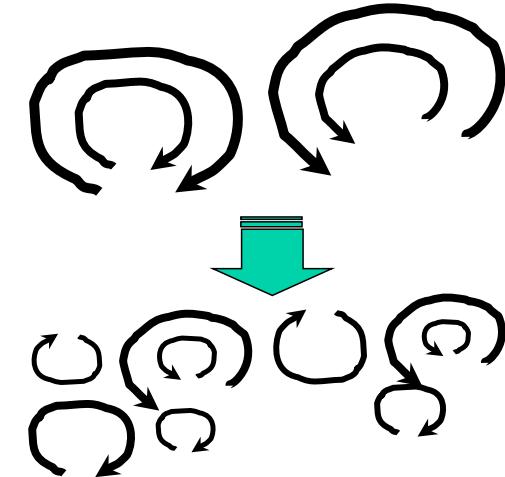
$V$ = typical velocity on scale  $L$ ,  $\nu$  = viscosity,  $Re > 1000$

- *vortex stretching* --> turbulence

is *intrinsically anisotropic*

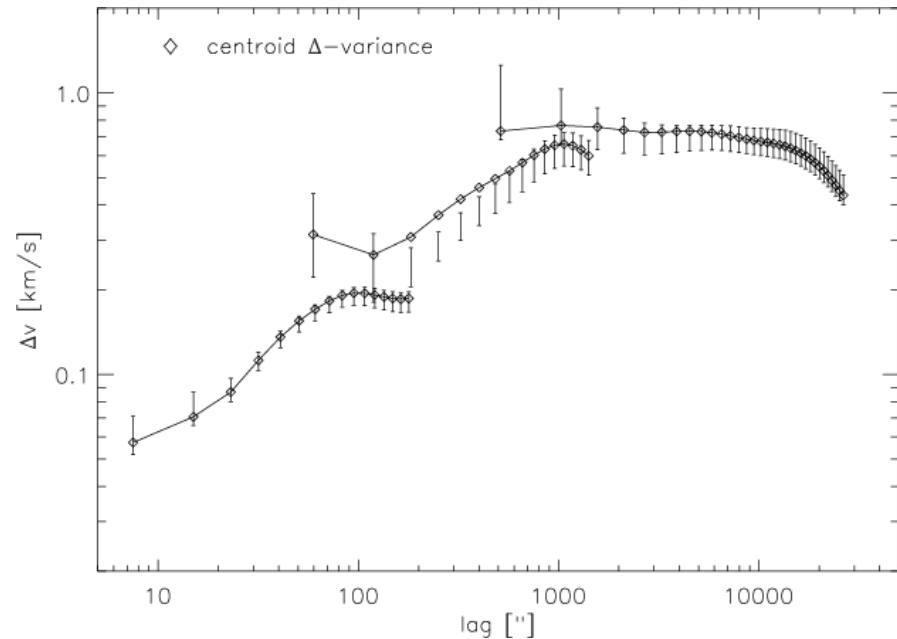
(only on large scales you *may* get homogeneity & isotropy in a statistical sense;  
see Landau & Lifschitz, Chandrasekhar, Taylor, etc.)

(ISM turbulence: shocks & B-field cause additional inhomogeneity)





# what drives turbulence?

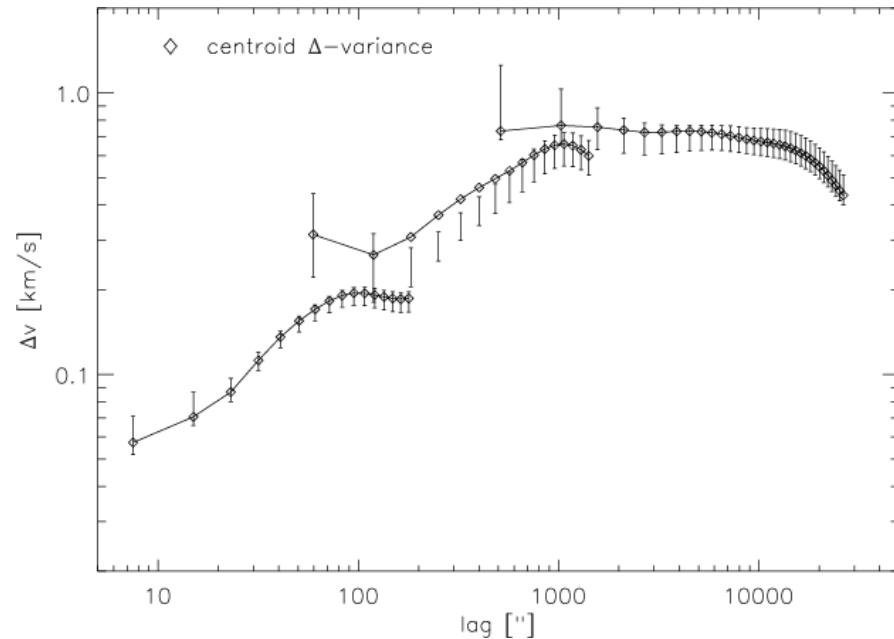


Polaris flare (from Ossenkopf & Mac Low 2002)

- turbulence characteristics
  - molecular cloud turbulence seems to be dominated by large-scale models
  - consistent with external driving
  - convergent flows?  
→ the same process that creates the cloud supplies internal turbulence ...
- alternative mechanisms:
  - gravity (spiral shocks), supernovae, HII regions?
  - internal sources: jets, outflows?



# what drives turbulence?



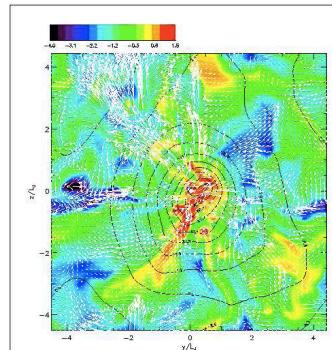
Polaris flare (from Ossenkopf & Mac Low 2002)

- turbulence characteristics
  - molecular cloud turbulence seems to be dominated by large-scale models
  - consistent with external driving
  - *convergent flows?*
    - the same process that creates the cloud supplies internal turbulence ..
    - caused by
      - *gravity (spiral shocks), supernovae, HII regions?*
  - alternative mechanisms:
    - internal sources: jets, outflows?

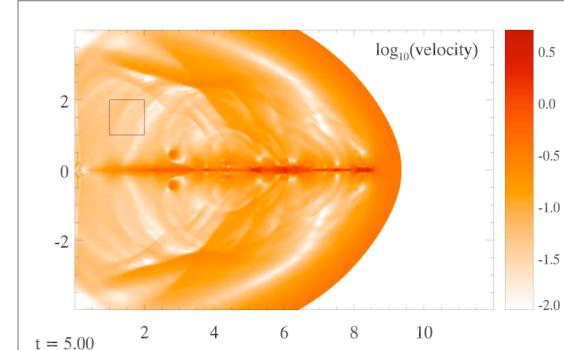


# what drives turbulence?

- molecular cloud turbulence is be dominated by *large-scale modes*
  - “*external*” sources such as supernovae, expanding HII regions, or large-scale gravitational process (spiral waves, accretion, etc)
- some words on “*internal*” sources
  - jets / outflow can only work after onset of star formation  
→ what about turbulence in non-star forming parts of clouds, or during initial phases?
  - debate on effectiveness of internal sources for driving supersonic turbulence (Li & Nakamura + Wang et al. vs. Banerjee, Klessen, Fendt)



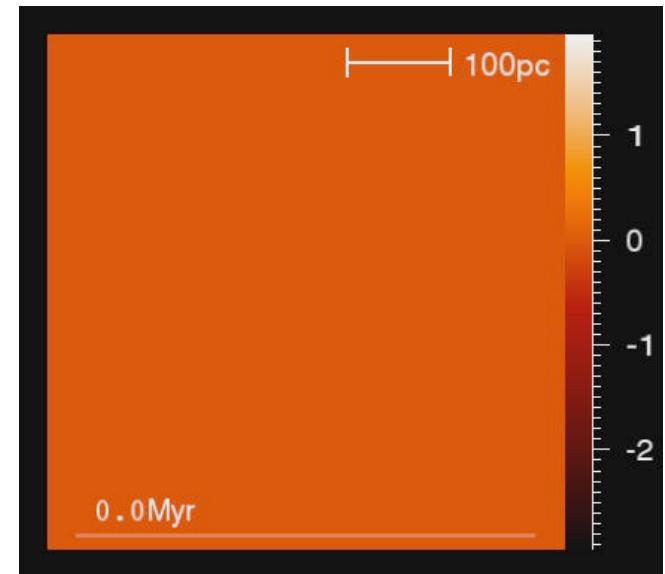
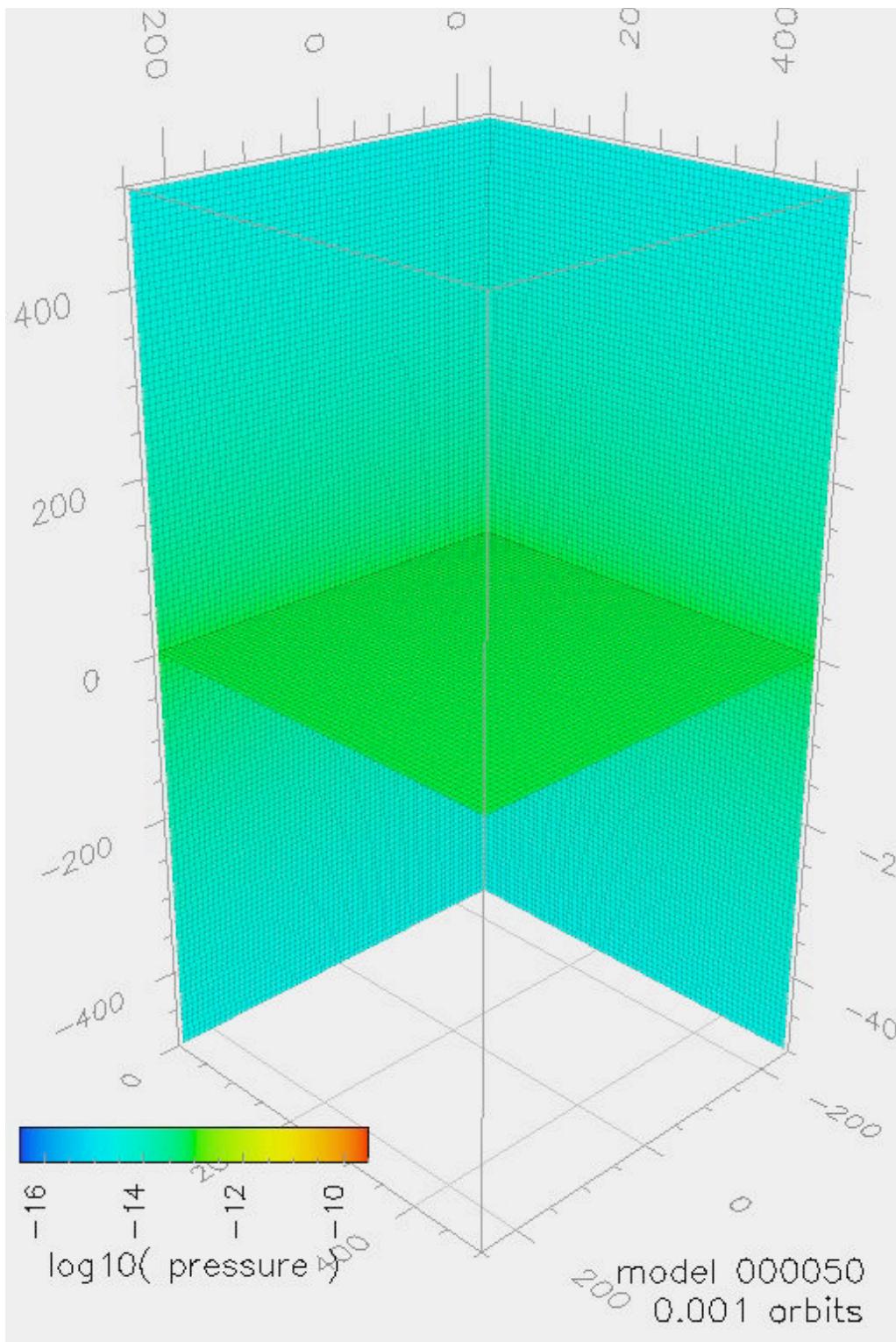
(Nakamura & Li 2007)



(Banerjee, Klessen, Fendt 2008)



from PhD thesis of Oliver Gressel (AIP)



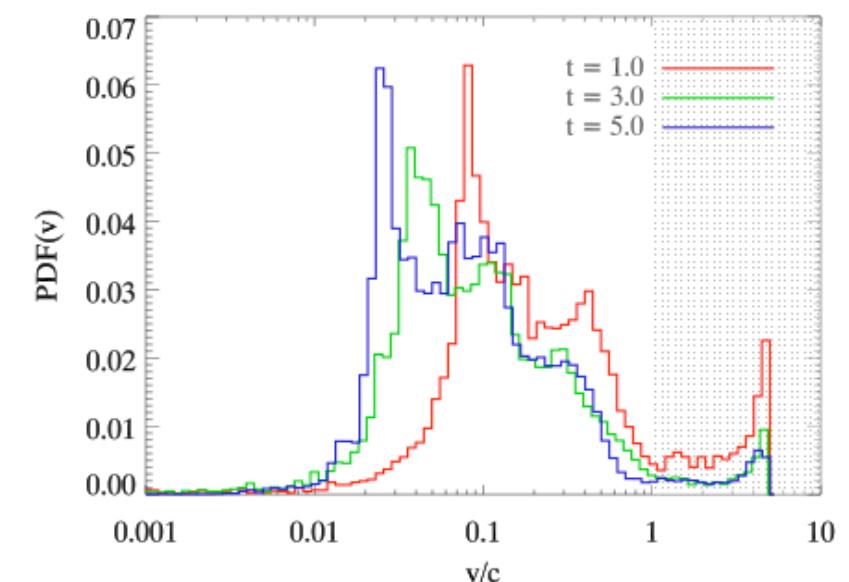
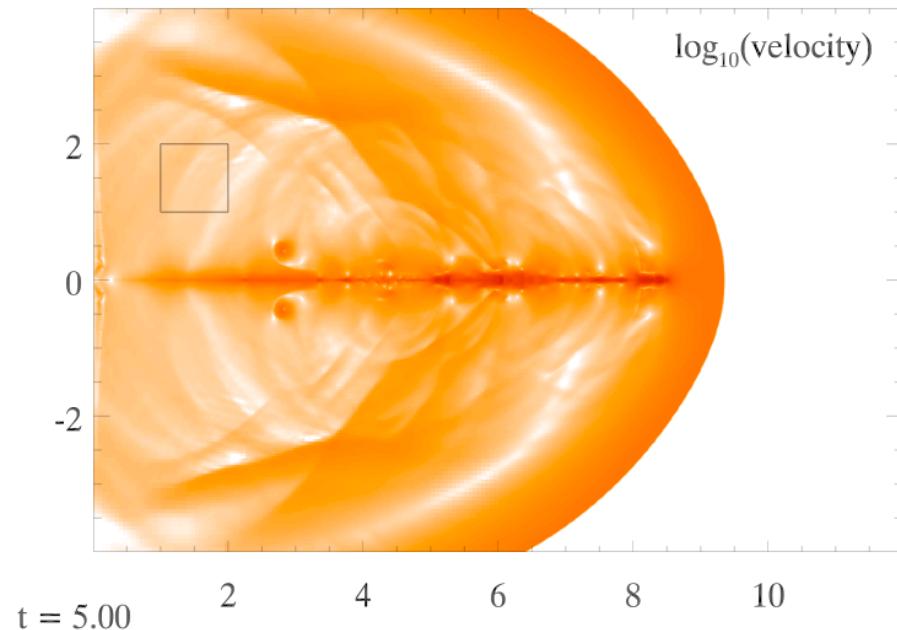
from PhD thesis of Oliver Gressel (AIP)

also work by  
deAvillez & Breitschwerdt  
Oishi & Mac Low  
Kim & Ostriker  
Shetty & Ostriker  
and many others...



# local feedback

- individual jets cannot drive supersonic turbulence in a space-filling way → need additional physics



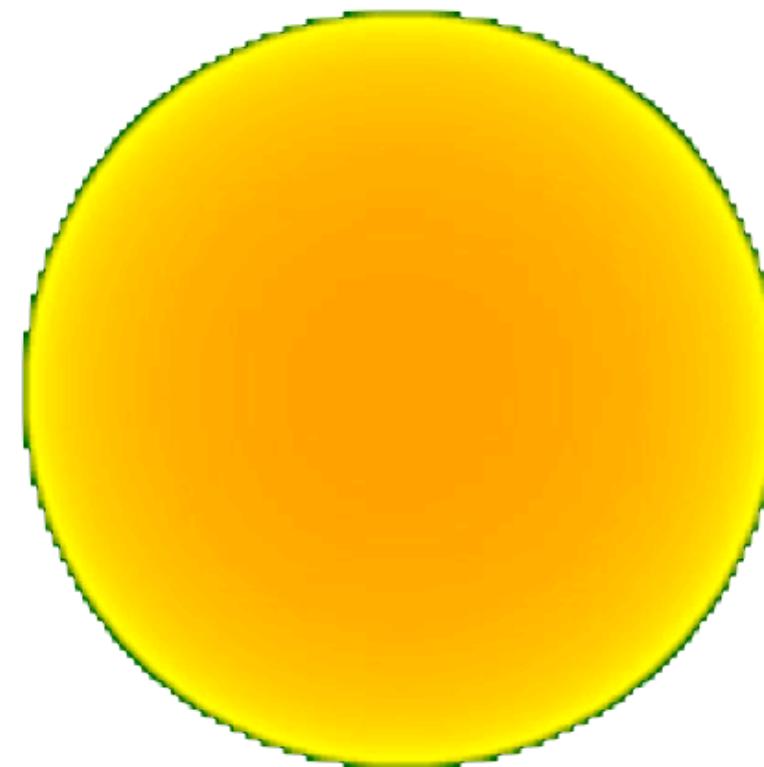
Banerjee, Klessen, & Fendt (2008)



# cluster forming cloud with jets

- jets from cluster with self-gravity  
with AMR code  
FLASH

0.0000e+00 yr



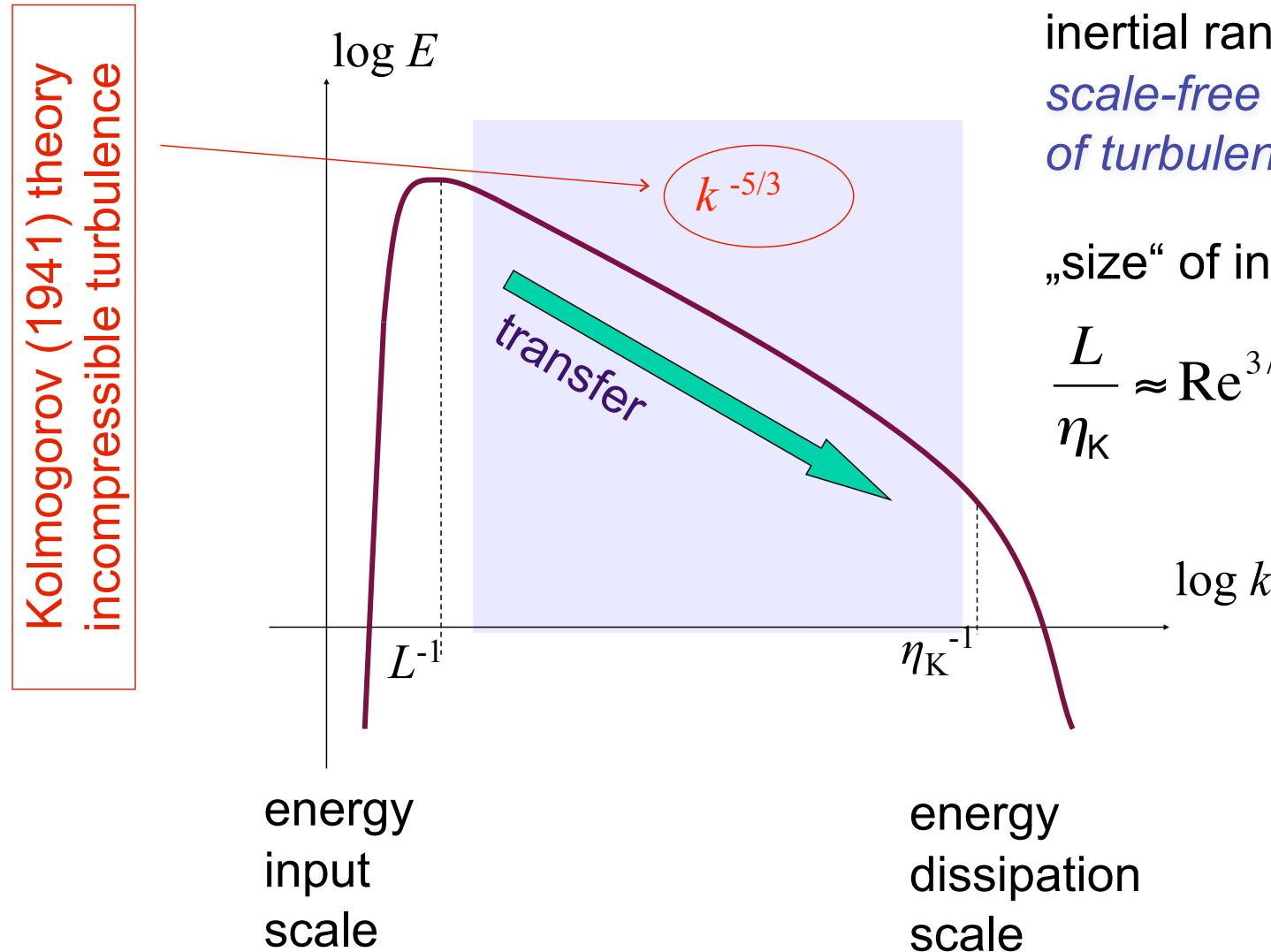
Boxsize 0.4 pc

Banerjee et al. (very preliminary study)

Ralf Klessen: Santa Cruz, 21.04.2010

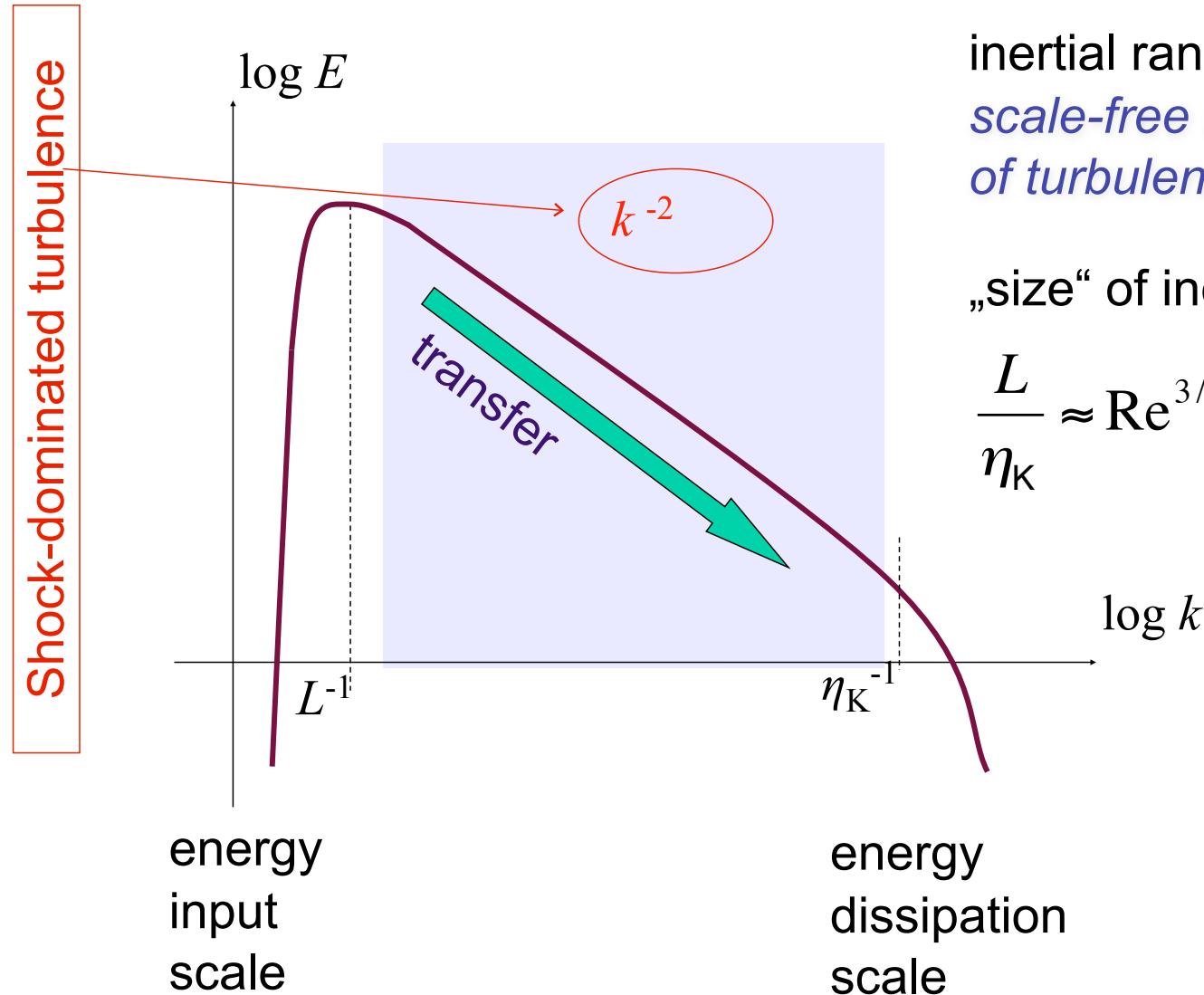


# Turbulent cascade





# Turbulent cascade



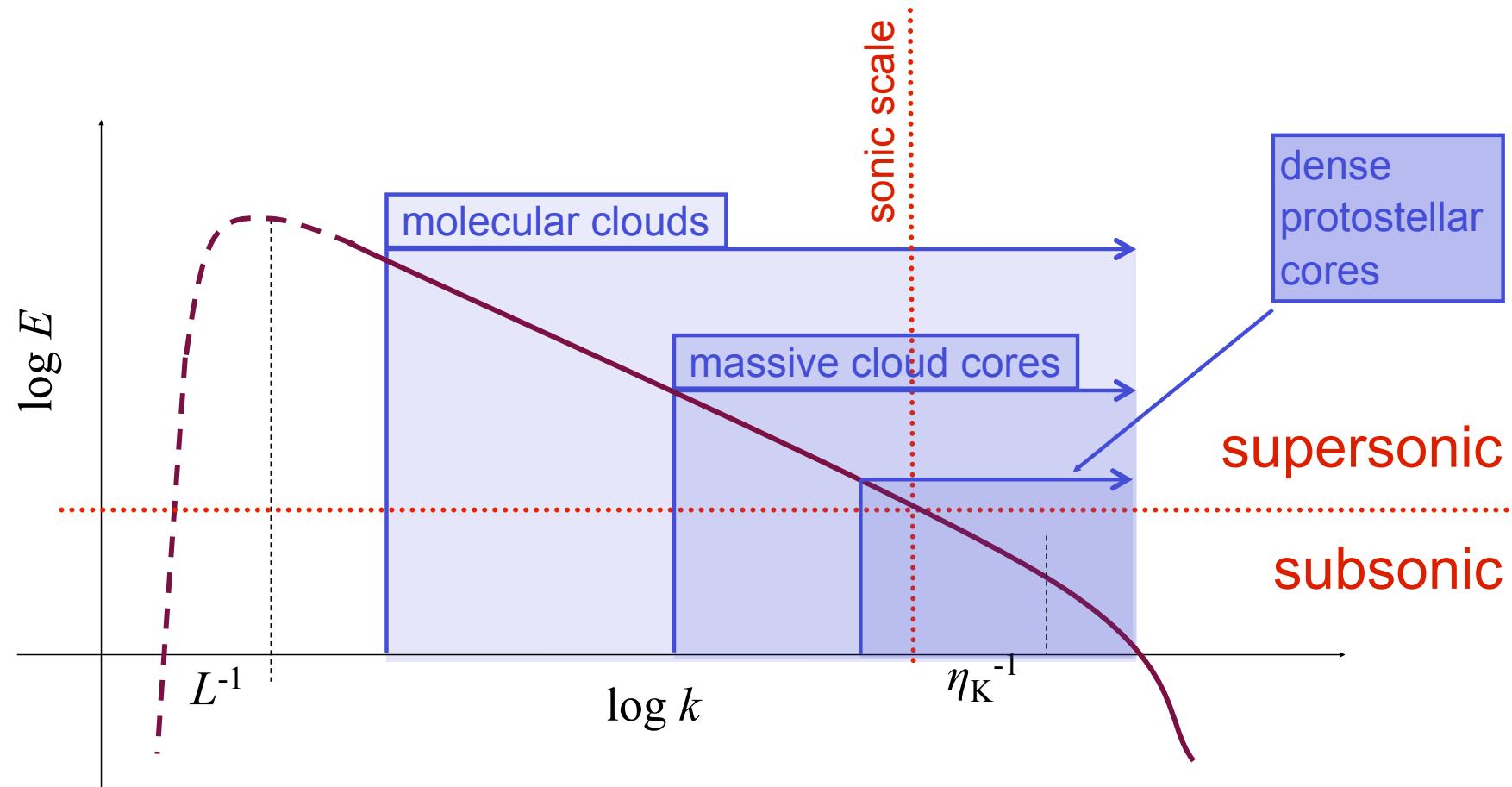
inertial range:  
*scale-free behavior  
of turbulence*

„size“ of inertial range:

$$\frac{L}{\eta_K} \approx \text{Re}^{3/4}$$



# Turbulent cascade in ISM



energy source & scale  
*NOT known*  
(supernovae, winds,  
spiral density waves?)

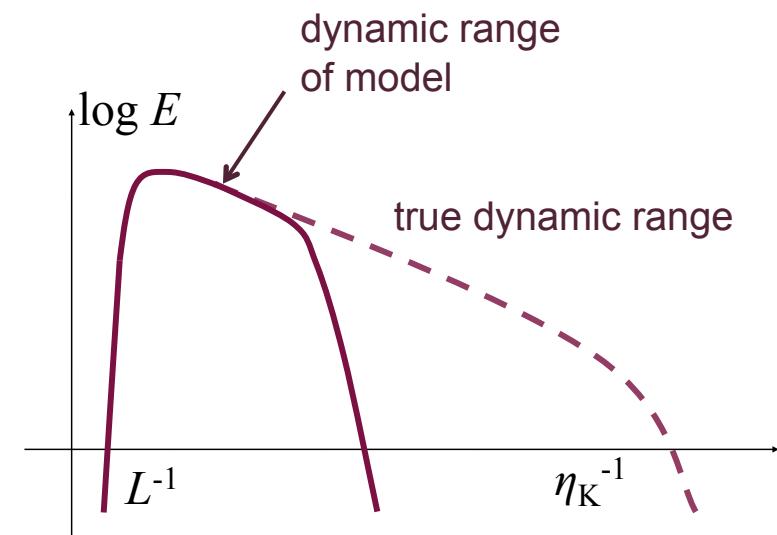
$\sigma_{\text{rms}} \ll 1 \text{ km/s}$   
 $M_{\text{rms}} \leq 1$   
 $L \approx 0.1 \text{ pc}$

dissipation scale not known  
(ambipolar diffusion,  
molecular diffusion?)



# Large-eddy simulations

- We use **LES** to model the large-scale dynamics
- Principal problem: only large scale flow properties
  - Reynolds number:  $\text{Re} = LV/\nu$  ( $\text{Re}_{\text{nature}} \gg \text{Re}_{\text{model}}$ )
  - dynamic range much smaller than true physical one
  - need *subgrid model* (in our case simple: only dissipation)
  - but what to do for more complex when processes on subgrid scale determine large-scale dynamics  
(chemical reactions, nuclear burning, etc)
  - Turbulence is “space filling” --> difficulty for AMR (don’t know what criterion to use for refinement)
- How *large* a Reynolds number do we need to catch basic dynamics right?





# compressive vs. rotational driving

- statistical characteristics of turbulence depend strongly on „type“ of driving
- example: dilatational vs. solenoidal driving
- question: what drives ISM turbulence on different scales?



# dilatational vs. solenoidal

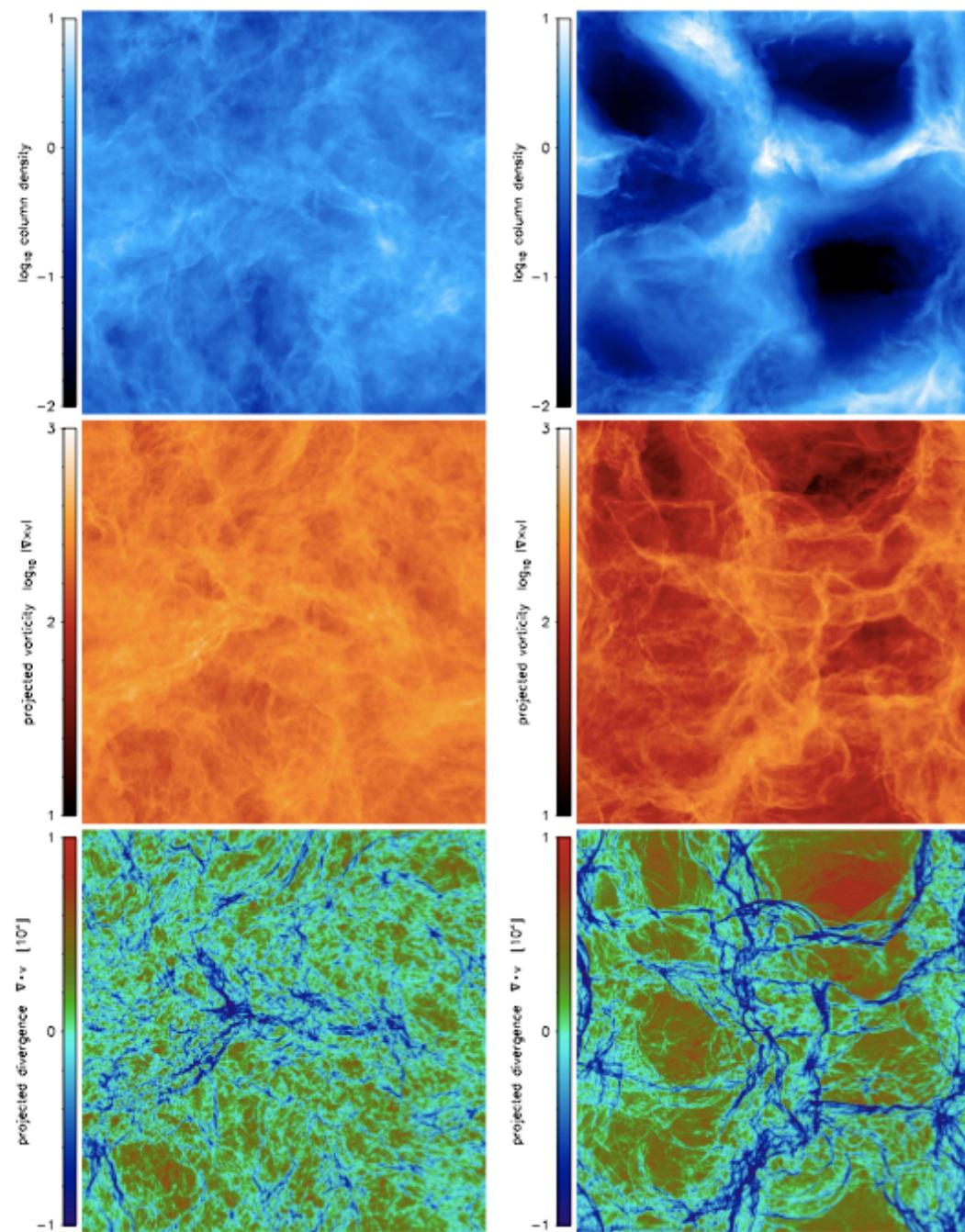
density as function of time / cut through  $1024^3$  cube simulation (FLASH)



compressive  
*larger structures, higher  $\rho$ -contrast*



rotational  
*smaller structures, small  $\rho$ -pdf*



column density

projected vorticity

projected divergence

Fig. 1. Maps showing density, vorticity and divergence in projection along the  $z$ -axis at time  $t = 2T$  as an example for the regime of statistically fully developed compressible turbulence for solenoidal forcing (left) and compressive forcing (right). Top panels: Column density fields in units of the mean column density. Both maps show three orders of magnitude in column density with the same scaling and magnitudes for direct comparison. Middle panels: Projections of the modulus of the vorticity  $|\nabla \times v|$ . Regions of intense vorticity appear to be elongated filamentary structures often coinciding with positions of intersecting shocks. Bottom panels: Projections of the divergence of the velocity field  $\nabla \cdot v$  showing the positions of shocks. Negative divergence corresponds to compression, while positive divergence corresponds to rarefaction.

# dilatational vs. solenoidal

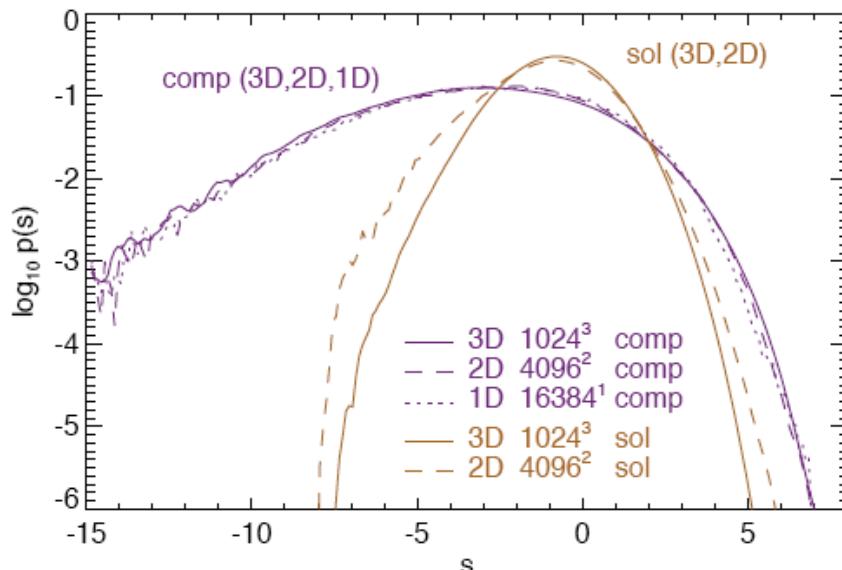


FIG. 3.— Volume-weighted density PDFs  $p(s)$  obtained from 3D, 2D and 1D simulations with compressive forcing and from 3D and 2D simulations using solenoidal forcing. Note that in 1D, only compressive forcing is possible as in the study by Passot & Vázquez-Semadeni (1998). As suggested by eq. (5), compressive forcing yields almost identical density PDFs in 1D, 2D and 3D with  $b \sim 1$ , whereas solenoidal forcing leads to a density PDF with  $b \sim 1/2$  in 2D and with  $b \sim 1/3$  in 3D.

Federrath, Klessen, Schmidt (2008a)

- density pdf depends on “dimensionality” of driving
  - relation between width of pdf and Mach number

$$\sigma_\rho / \rho_0 = b \mathcal{M}$$

- with  $b$  depending on  $\zeta$  via

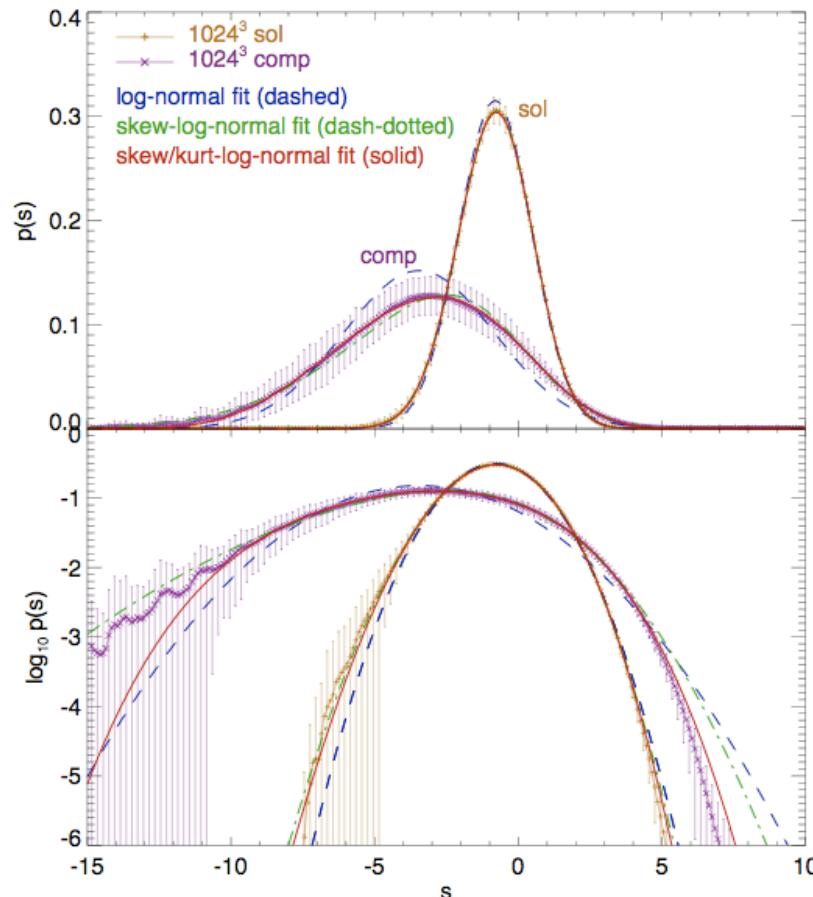
$$b = 1 + \left[ \frac{1}{D} - 1 \right] \zeta = \begin{cases} 1 - \frac{2}{3}\zeta & , \text{ for } D = 3 \\ 1 - \frac{1}{2}\zeta & , \text{ for } D = 2 \\ 1 & , \text{ for } D = 1 \end{cases}$$

- with  $\zeta$  being the ratio of dilatational vs. solenoidal modes:

$$\mathcal{P}_{ij}^\zeta = \zeta \mathcal{P}_{ij}^\perp + (1 - \zeta) \mathcal{P}_{ij}^\parallel = \zeta \delta_{ij} + (1 - 2\zeta) \frac{k_i k_j}{|k|^2}$$



# dilatational vs. solenoidal



good fit needs 3<sup>rd</sup> and 4<sup>th</sup> moment of distribution!

Federrath, Klessen, Schmidt (2008b)

- density pdf depends on “dimensionality” of driving  
→ is that a problem for the Krumholz & McKee model of the SF efficiency?
- density pdf of compressive driving is *NOT log-normal*  
→ is that a problem for the Padoan & Nordlund IMF model?
- most “physical” sources should be *compressive* (convergent flows from spiral shocks or SN)



# effects of chemistry 4

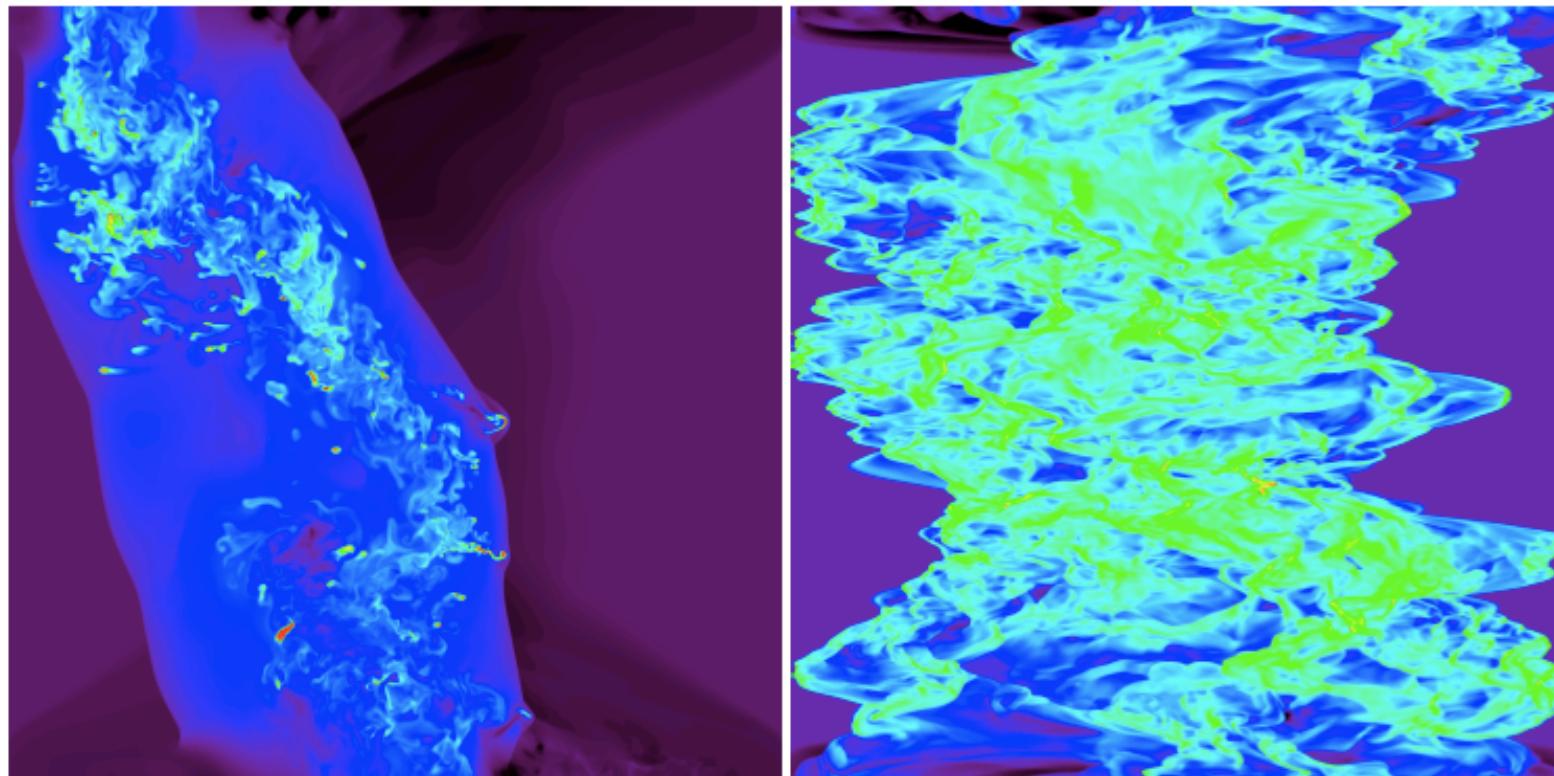
- deliverables / predictions:

- x-factor estimates (as function of environmental conditions)
- synthetic line emission maps (in combination with line transfer)
- pdf's of density, velocity, emissivity / structure functions (to directly connect to observational regime)
- **COMMENT:** density pdf is *NOT* lognormal!  
<-- gravity (poster by Kim), driving scheme (Federrath et al. 2008), EOS (Hennebelle & Audit 2009)



# density pdf

1200<sup>3</sup> hydrodynamic simulation



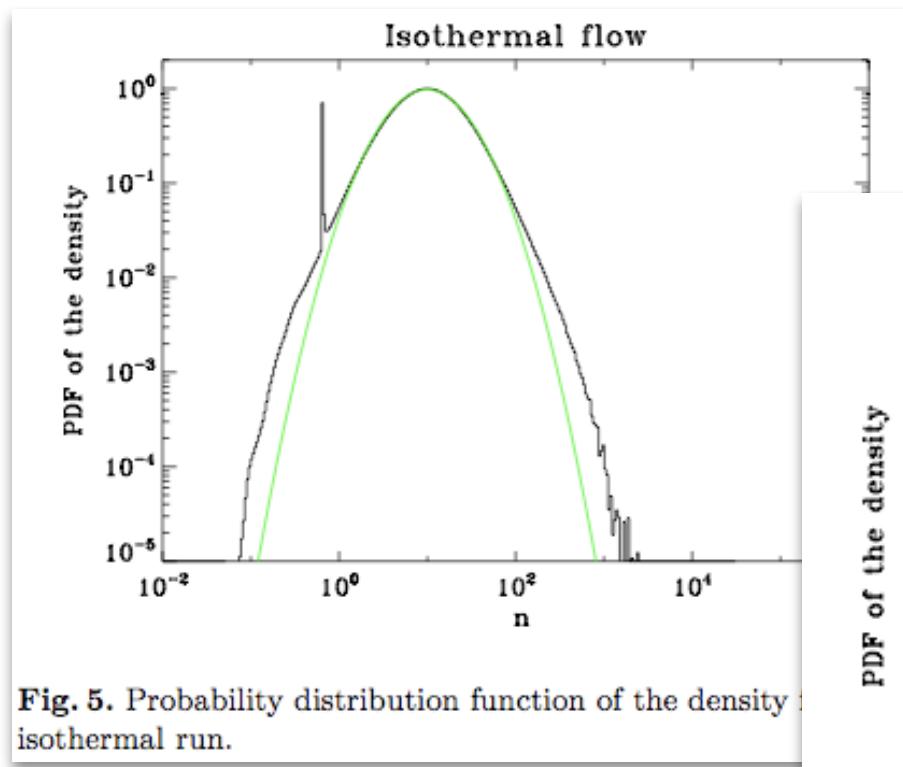
**Fig. 3.** Density cut through the simulations. The left plot corresponds to the 2-phase run and the right one to the isothermal run. Dark-blue, blue, green and red correspond respectively to densities of the order of  $1 \text{ cm}^{-3}$ ,  $3 \text{ cm}^{-3}$ ,  $20 \text{ cm}^{-3}$  and  $100 \text{ cm}^{-3}$ .

(Audit & Hennebelle, submitted)

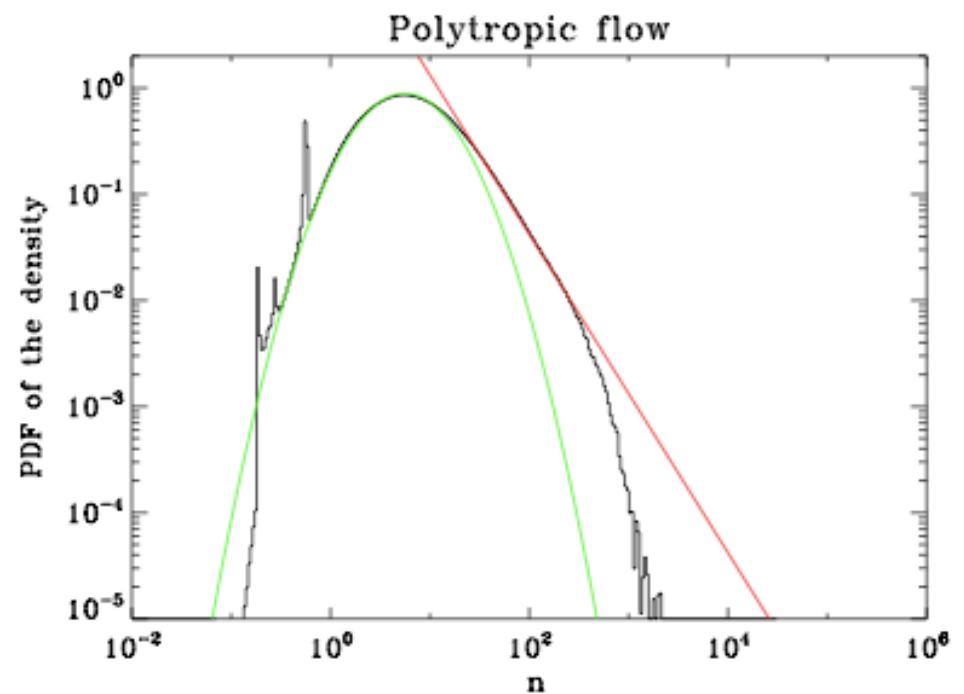
Ralf Klessen: Spineto 09.07.09



# density pdf



$1200^3$  hydrodynamic simulation



**Fig. 5.** Probability distribution function of the density for the isothermal run.

(Audit & Hennebelle, submitted)

**Fig. 6.** Probability distribution function of the density for the polytropic run.

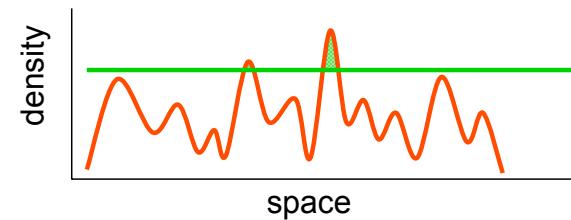


basic idea



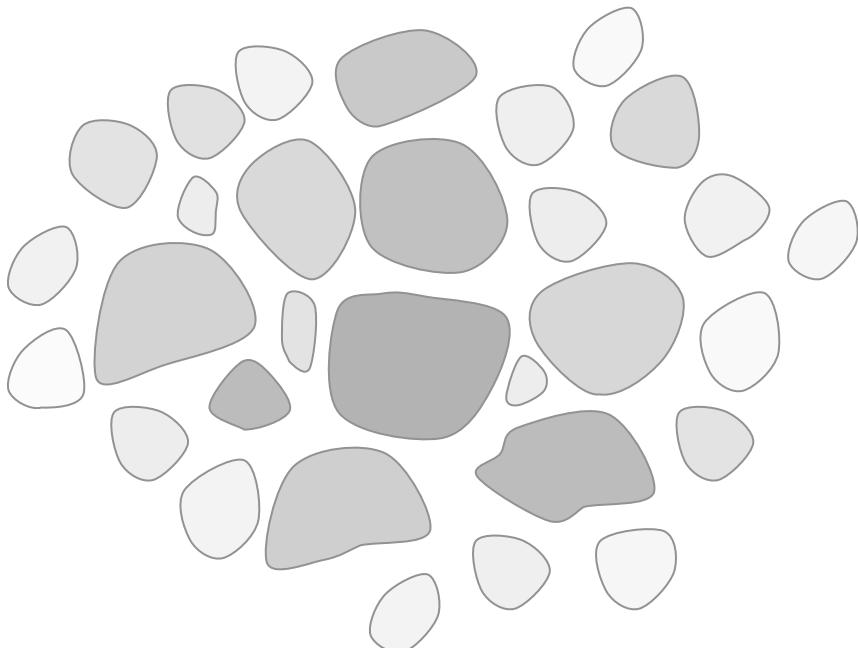
# dynamical SF in a nutshell

- interstellar gas is highly *inhomogeneous*
    - *gravitational instability*
    - *thermal instability*
    - *turbulent compression* (in shocks  $\delta\rho/\rho \propto M^2$ ; in atomic gas:  $M \approx 1\dots3$ )
  - cold *molecular clouds* can form rapidly in high-density regions at *stagnation points of convergent large-scale flows*
    - chemical *phase transition*: atomic  $\rightarrow$  molecular
    - process is *modulated* by large-scale *dynamics* in the galaxy
  - inside *cold clouds*: turbulence is highly supersonic ( $M \approx 1\dots20$ )  
 $\rightarrow$  *turbulence* creates large density contrast,  
*gravity* selects for collapse
- > **GRAVOTUBULENT FRAGMENTATION**
- *turbulent cascade*: local compression *within* a cloud provokes collapse  $\rightarrow$  formation of individual *stars* and *star clusters*



# Formation and evolution of cores

What happens to distribution of cloud cores?



Two extreme cases:

(1) turbulence dominates energy budget:

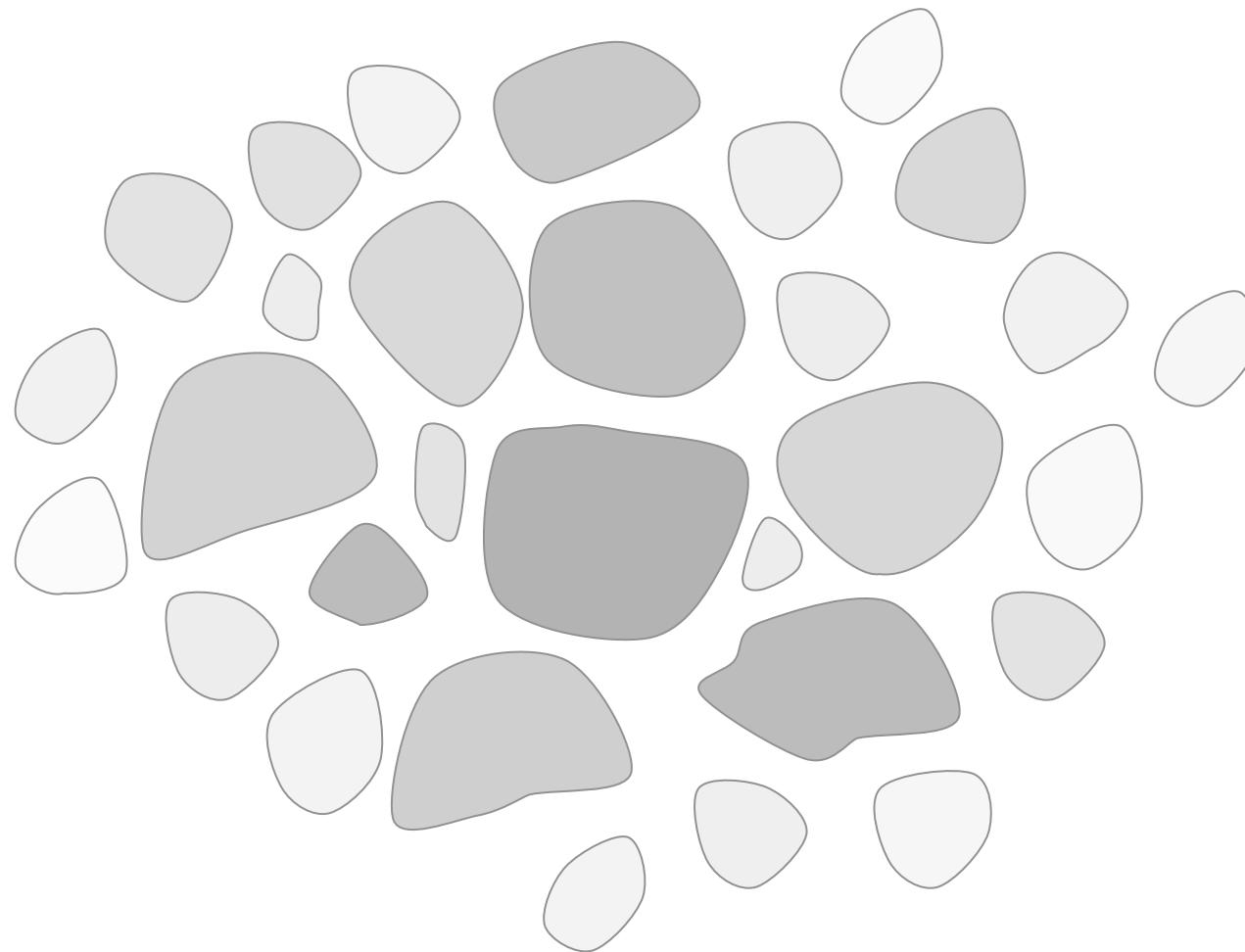
$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| > 1$$

- > individual cores do *not* interact
- > *collapse of individual cores* dominates *stellar mass growth*
- > *loose cluster of low-mass stars*

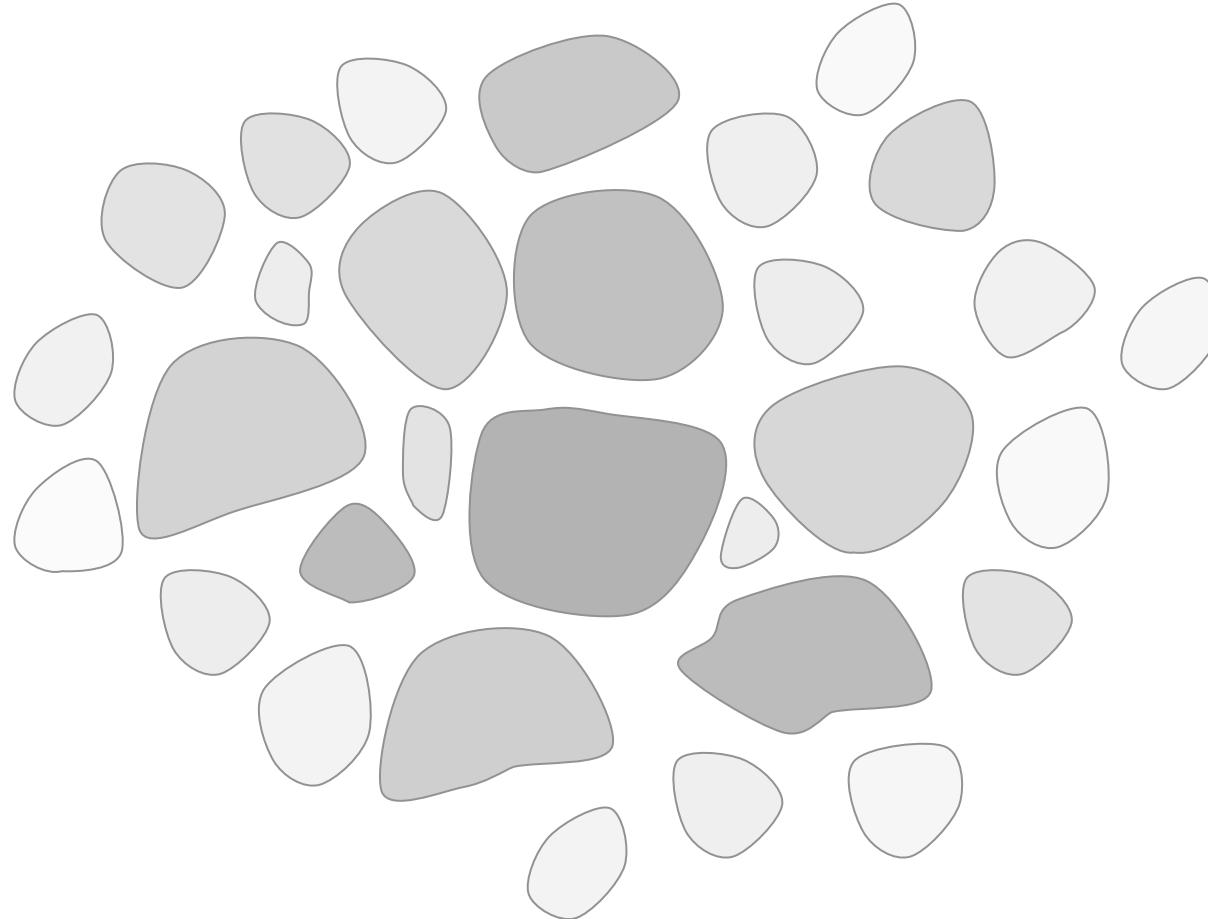
(2) turbulence decays, i.e. gravity dominates:

$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

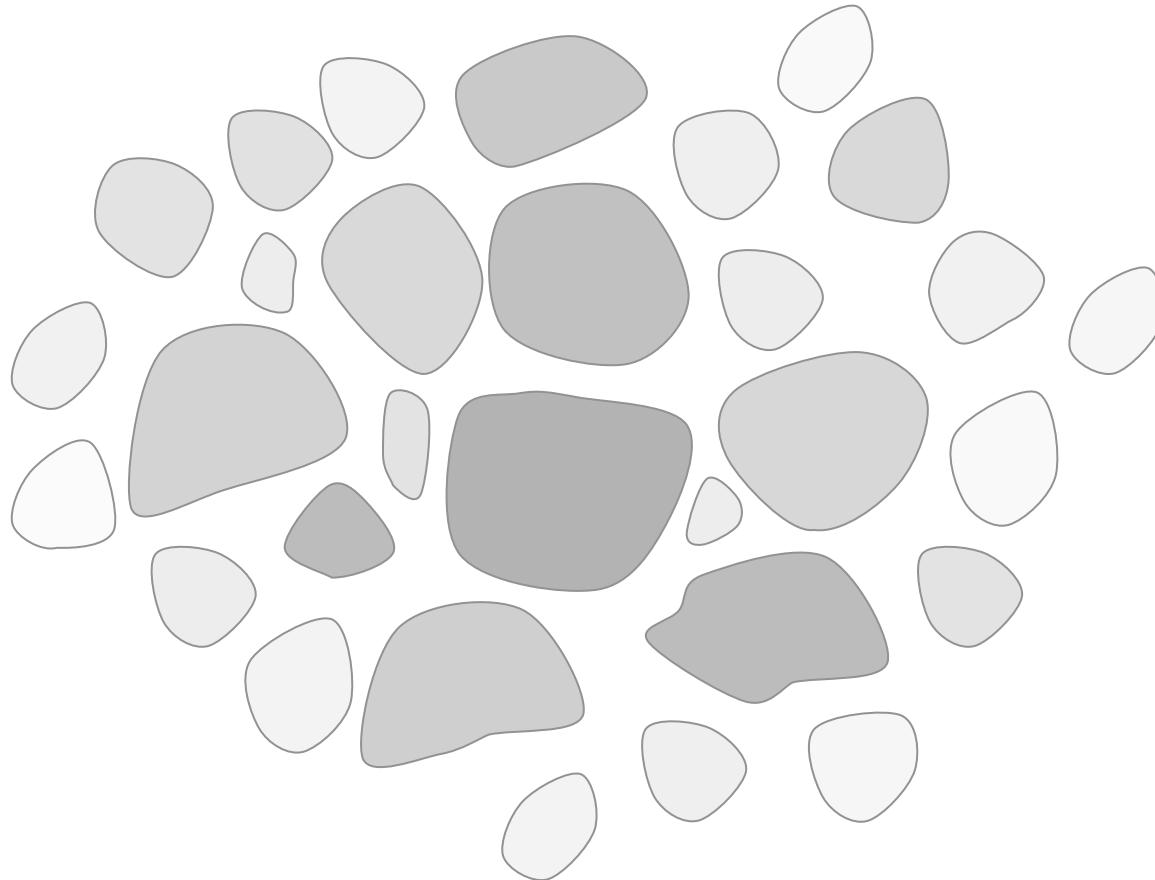
- > *global contraction*
- > cores do *interact* while collapsing
- > *competition influences mass growth*
- > *dense cluster with high-mass stars*



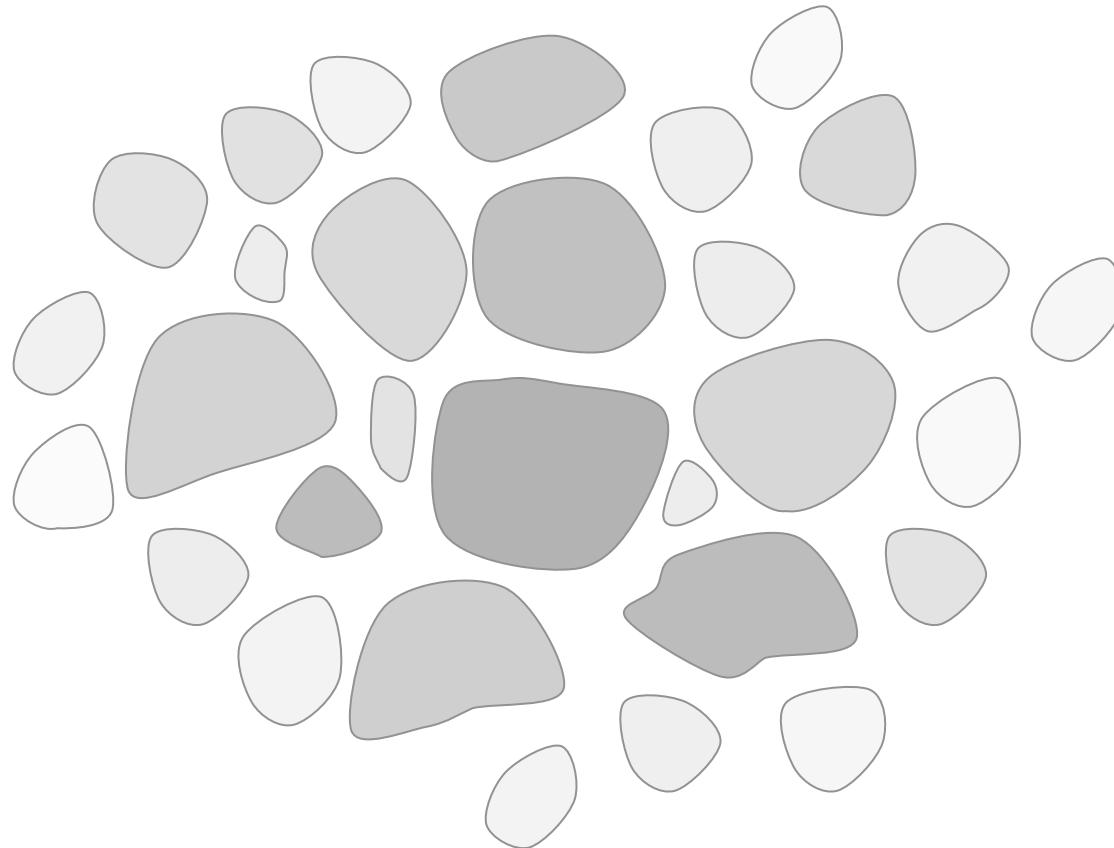
turbulence creates a hierarchy of clumps



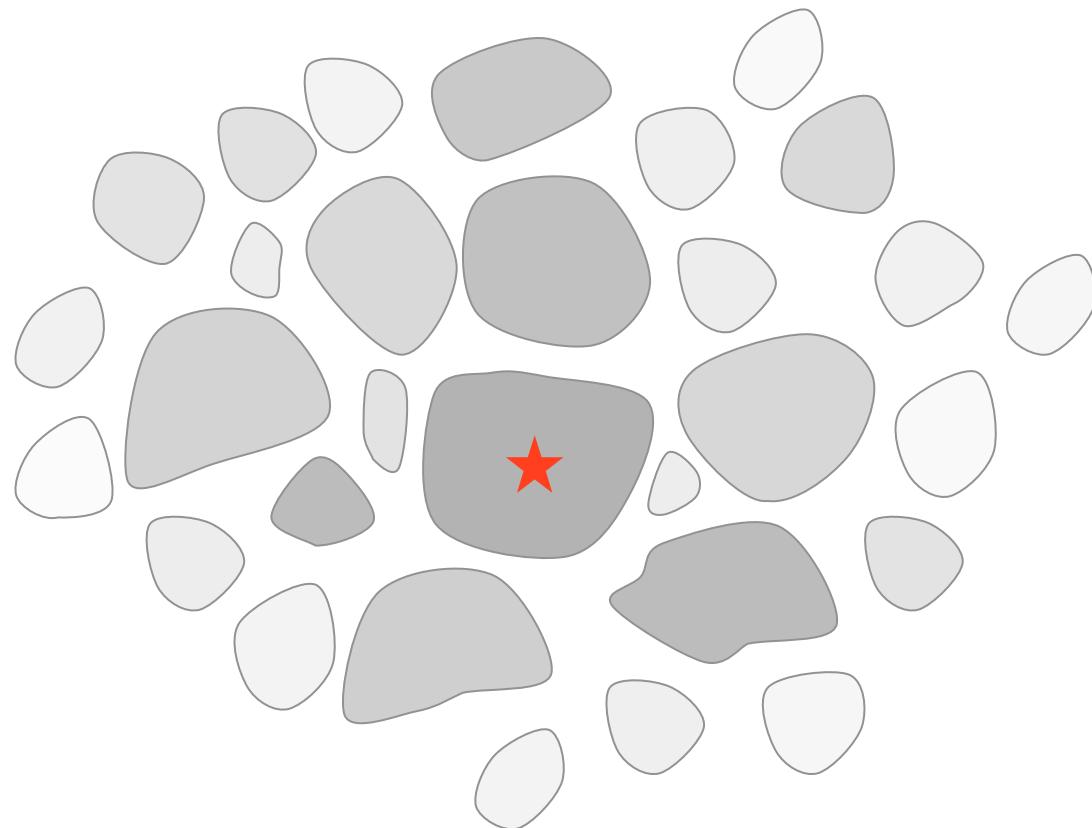
as turbulence decays locally, contraction sets in



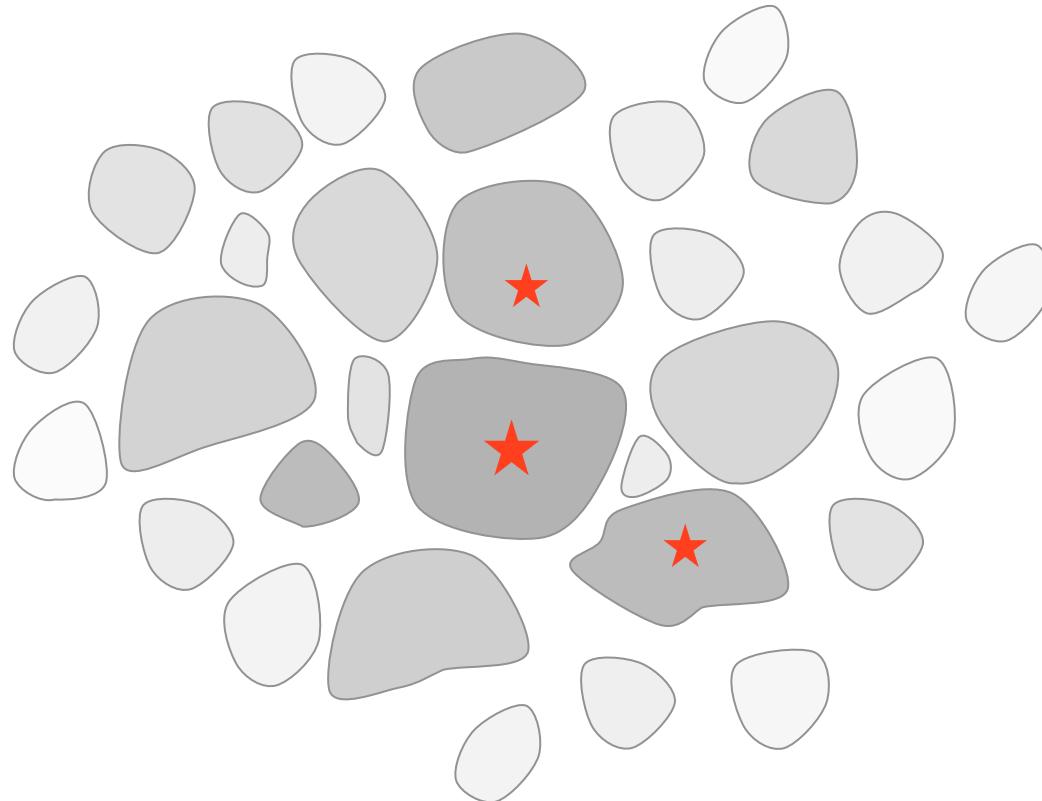
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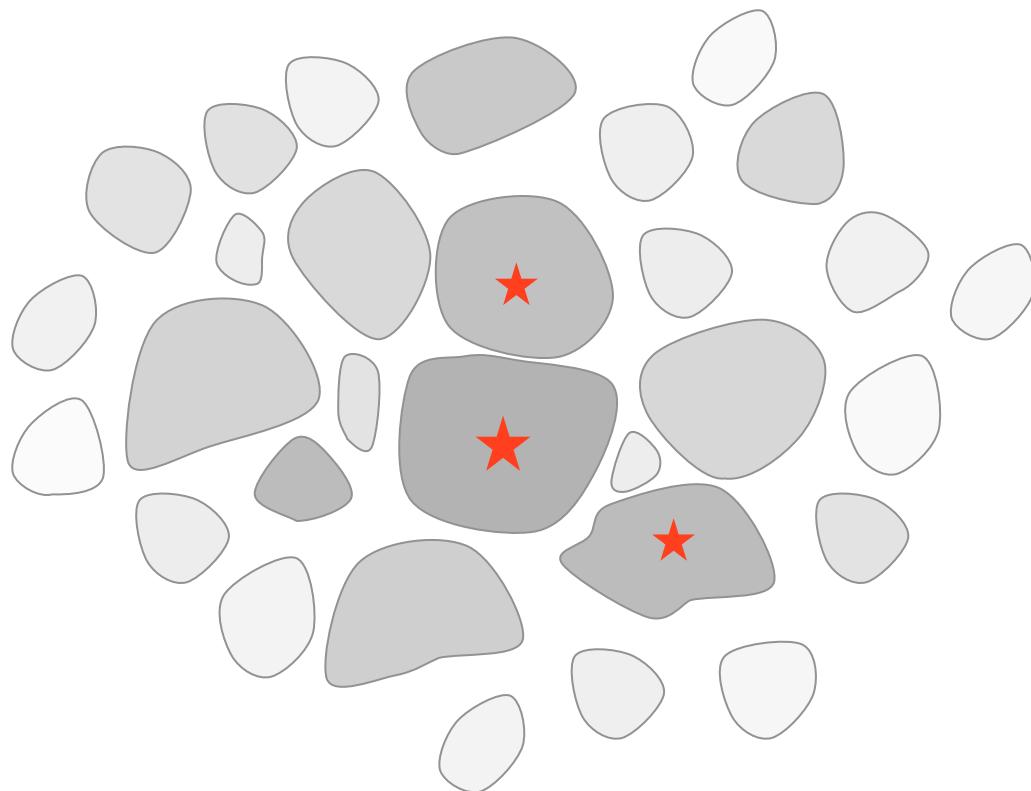
while region contracts, individual clumps collapse to form stars



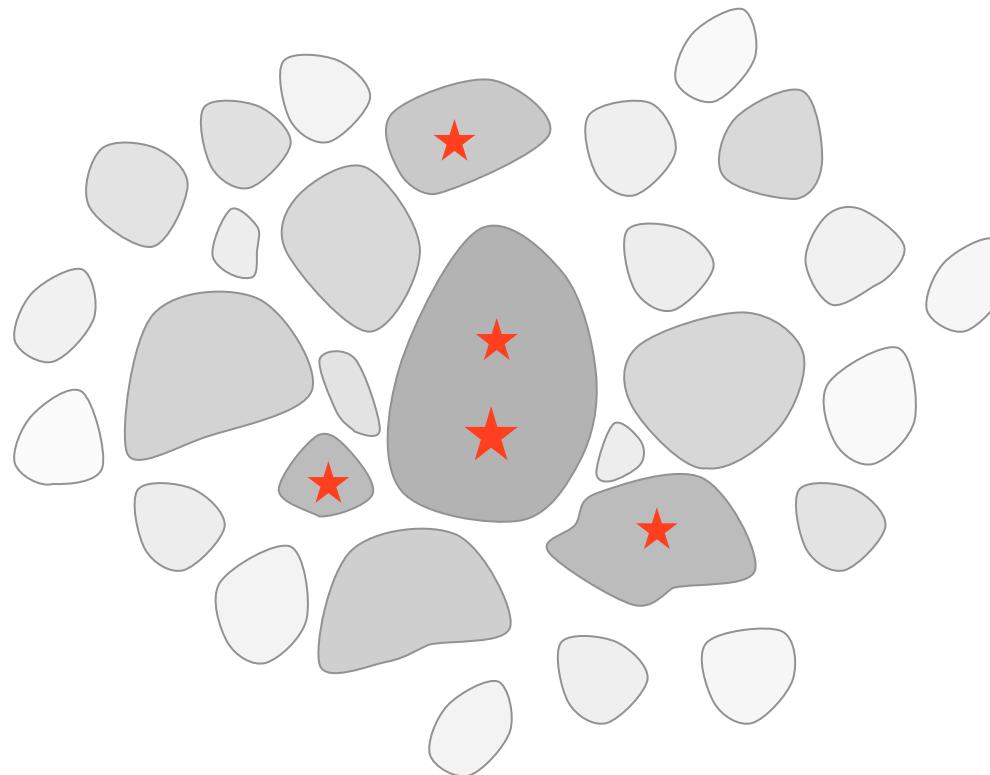
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individual clumps collapse to form stars

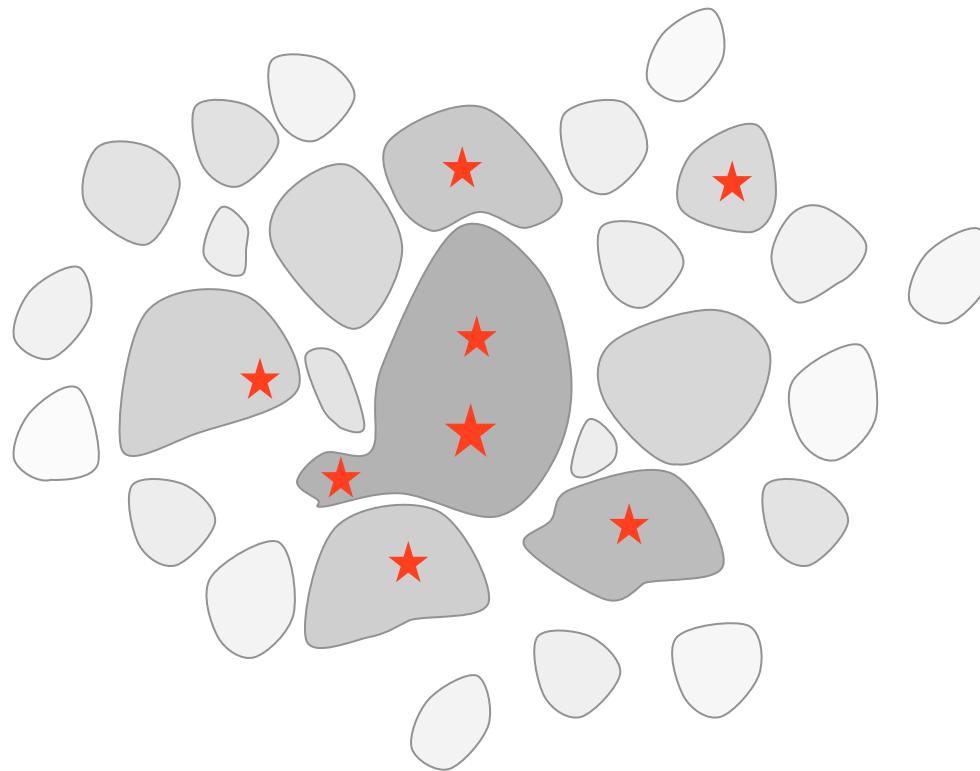


individual clumps collapse to form stars

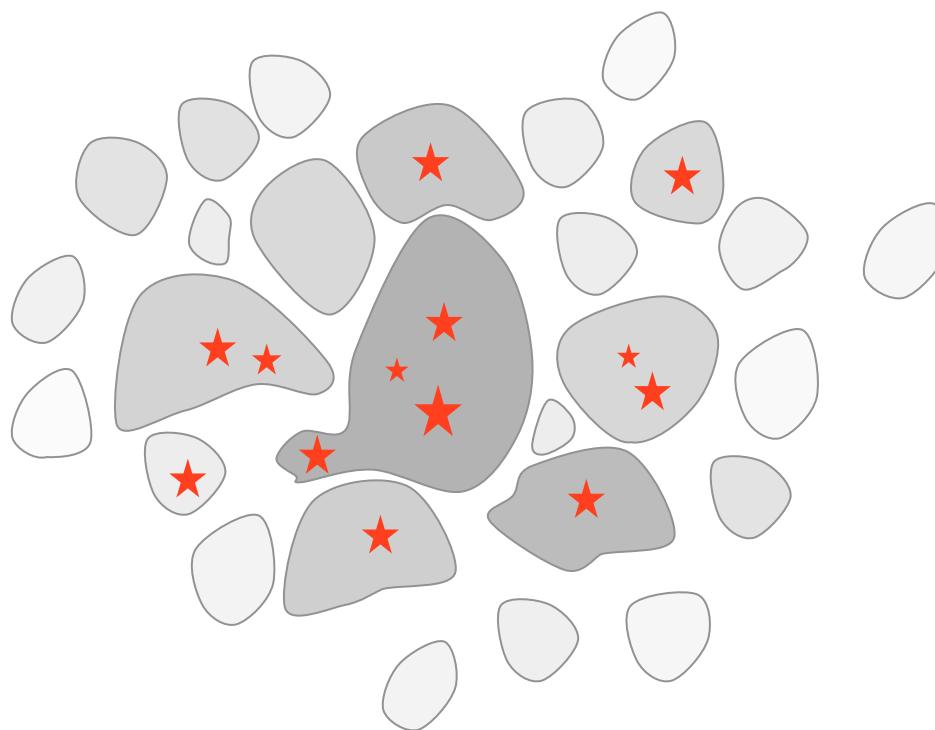


$$\alpha = E_{\text{kin}} / |E_{\text{pot}}| < 1$$

in *dense clusters*, clumps may merge while collapsing  
--> then contain multiple protostars



in *dense clusters*, clumps may merge while collapsing  
--> then contain multiple protostars



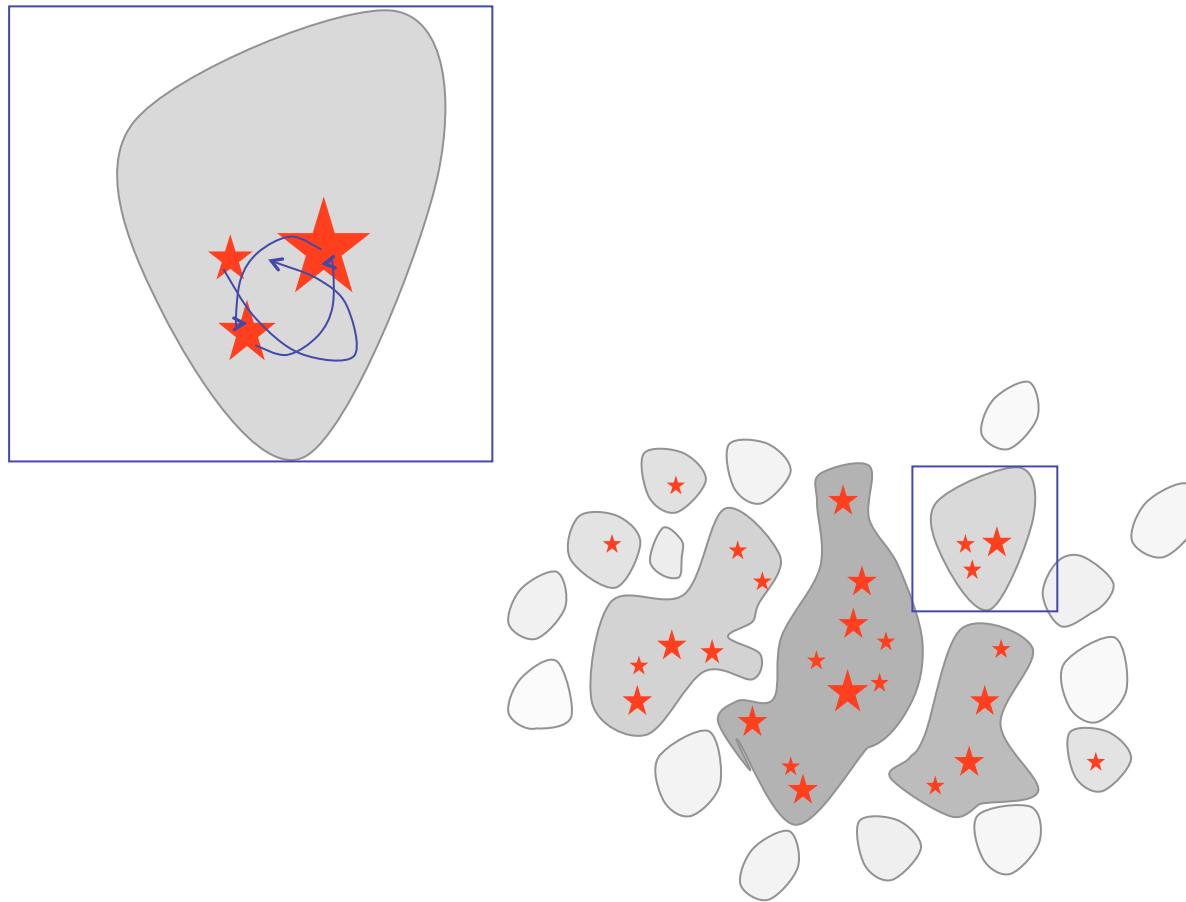
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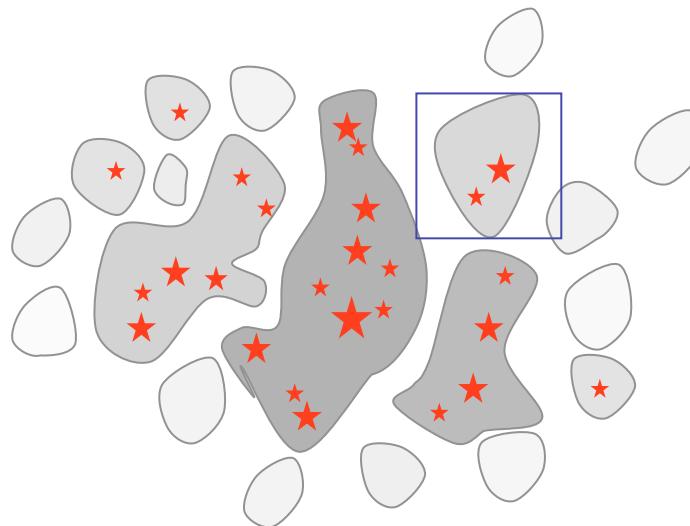
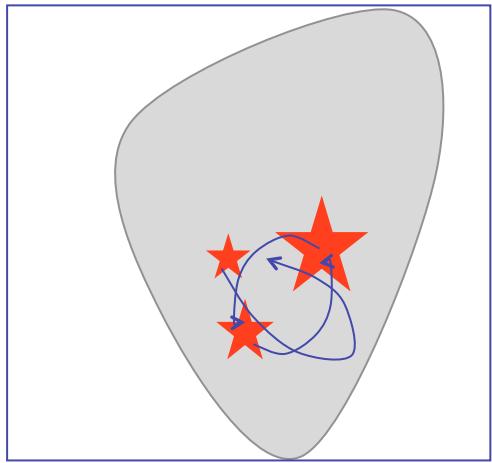
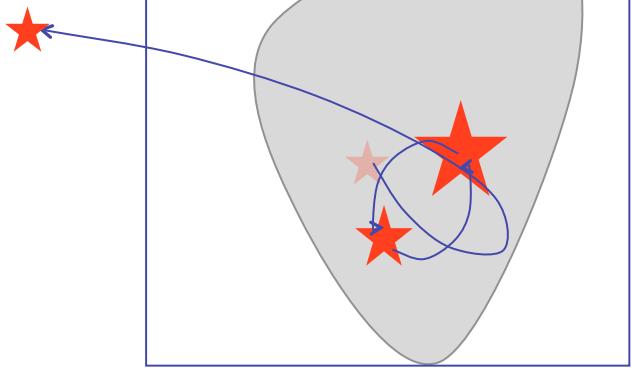
in *dense clusters*, competitive mass growth  
becomes important



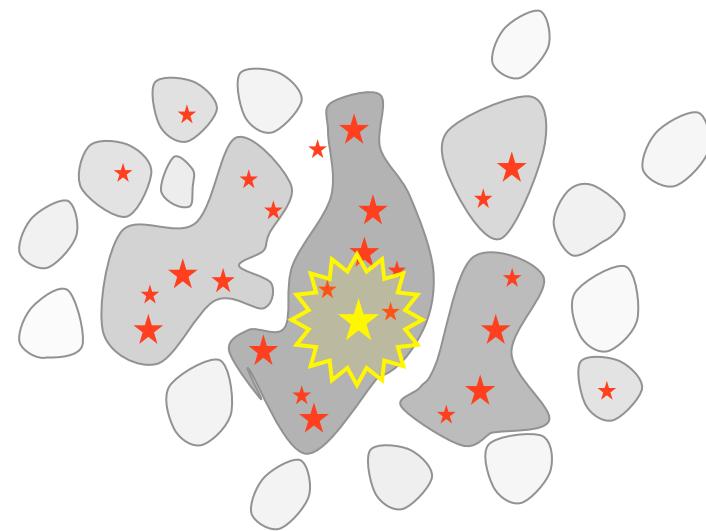
in *dense clusters*, competitive mass growth becomes important



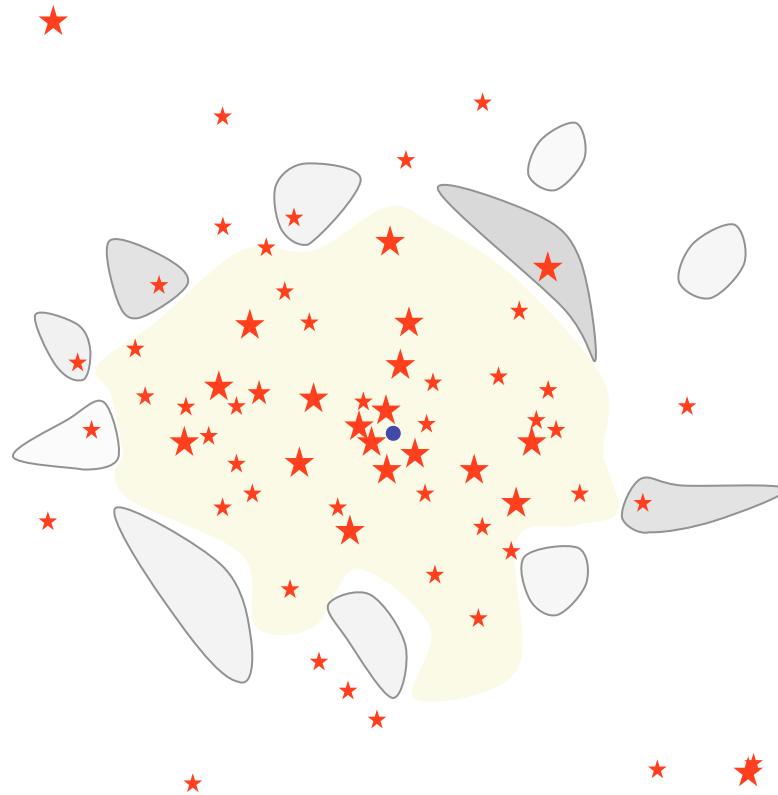
*in dense clusters, N-body effects influence mass growth*



low-mass objects may  
become ejected --> accretion stops



feedback terminates star formation



result: *star cluster*, possibly with H<sub>II</sub> region