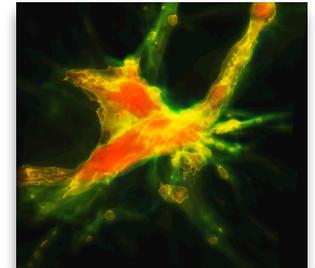
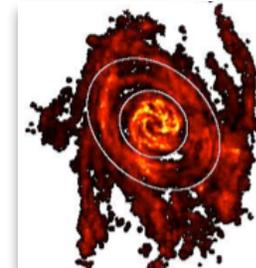
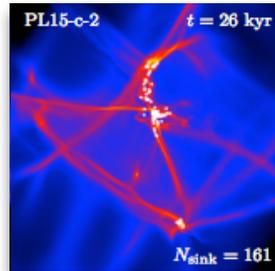
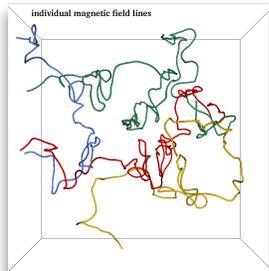


# ISM Dynamics and Star Formation



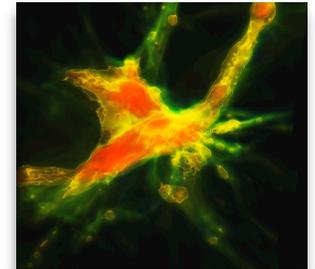
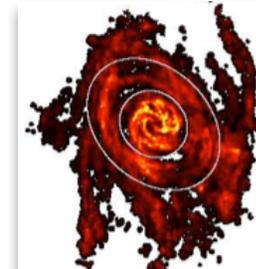
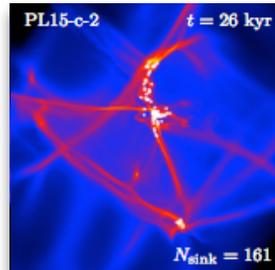
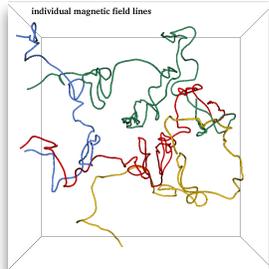
**Ralf Klessen**



Zentrum für Astronomie der Universität Heidelberg  
Institut für Theoretische Astrophysik



# Some Open Issues in Star Formation



**Ralf Klessen**

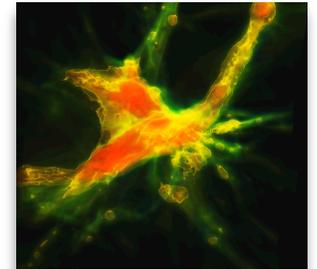
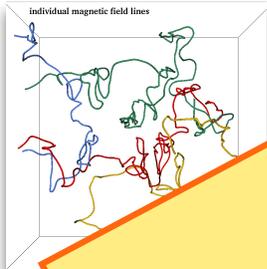


Zentrum für Astronomie der Universität Heidelberg  
Institut für Theoretische Astrophysik



# Some Open Issues in Star Formation

DISCLAIMER



**Ralf Klessen**

Zentrum für Astronomie der Universität Heidelberg  
Institut für Theoretische Astrophysik



# thanks to ...



... people in the group in Heidelberg:

Christian Baczynski, Erik Bertram, Frank Bigiel, Rachel Chicharro, Roxana Chira, Paul Clark, Gustavo Dopcke, Jayanta Dutta, Volker Gaibler, Simon Glover, Lukas Konstandin, Faviola Molina, Mei Sasaki, Jennifer Schober, Rahul Shetty, Rowan Smith, László Szűcs, Svitlana Zhukovska

... former group members:

Robi Banerjee, Ingo Berentzen, Christoph Federrath, Philipp Girichidis, Thomas Greif, Milica Micic, Thomas Peters, Dominik Schleicher, Stefan Schmeja, Sharanya Sur

... many collaborators abroad!



Deutsche  
Forschungsgemeinschaft  
**DFG**

**BADEN-  
WÜRTTEMBERG**  
STIFTUNG  
Wir stiften Zukunft



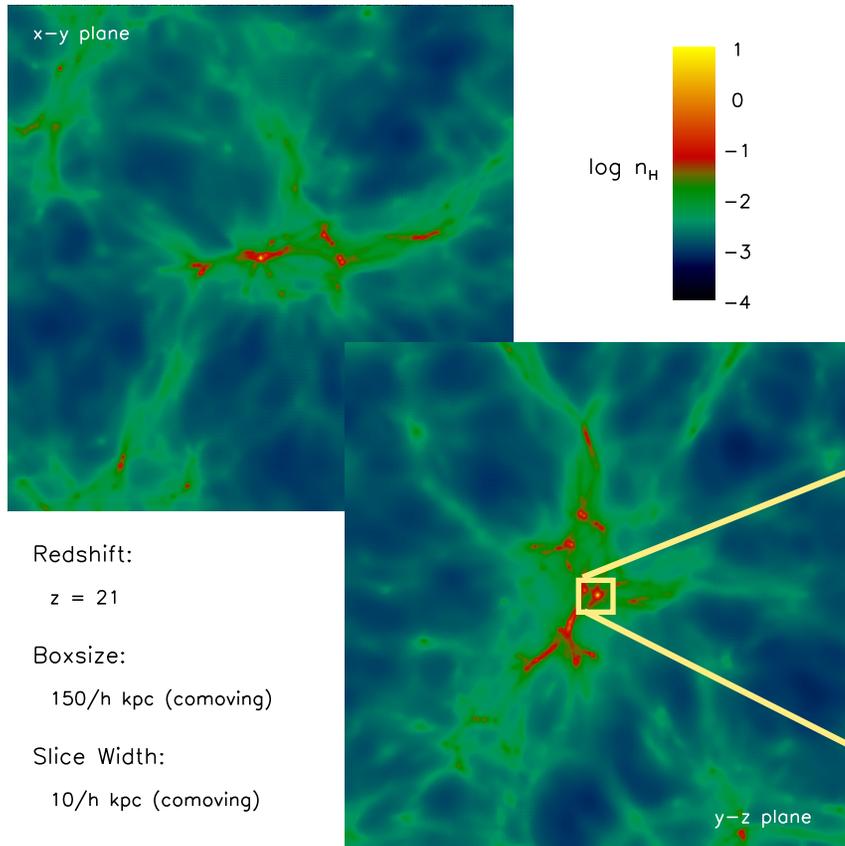
# agenda

- first star formation
  - influence of magnetic fields
  - influence of dark matter annihilation
- global star formation
  - non-universal and sub-linear Kennicutt-Schmidt relation



...following up on  
Volker's talk ...

# model the formation of the first stars



Redshift:

$z = 21$

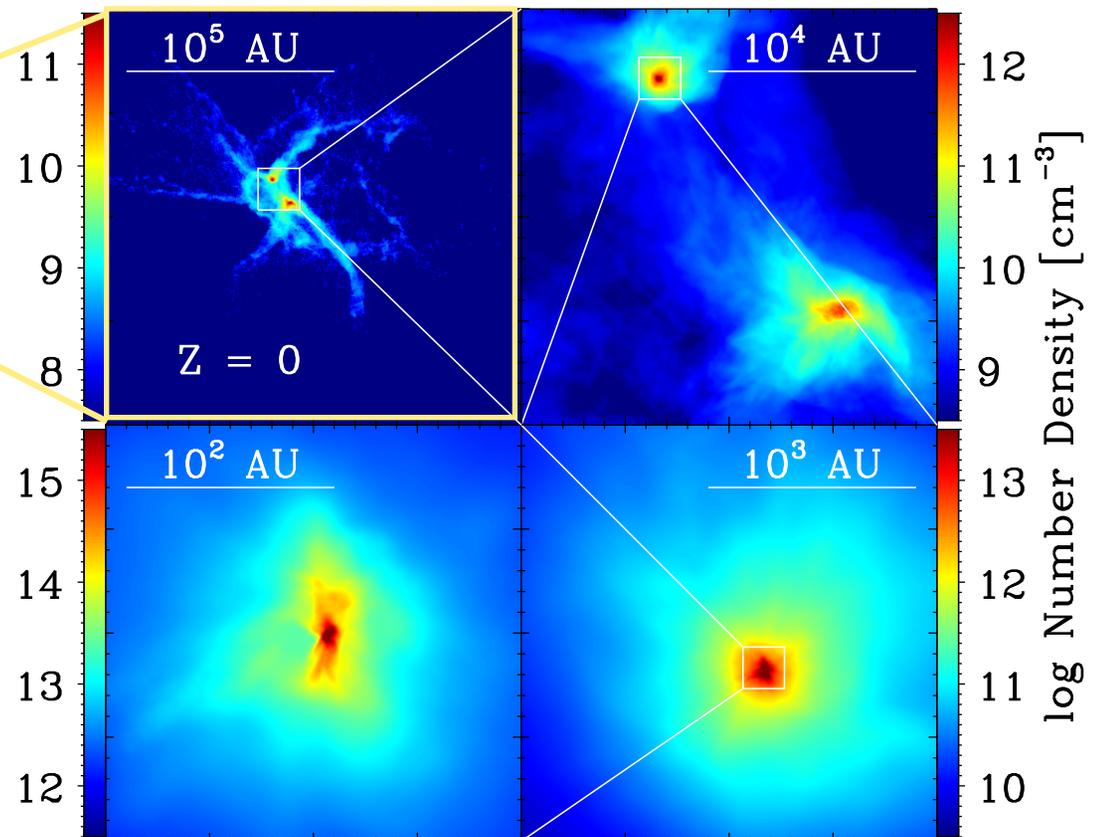
Boxsize:

$150/h$  kpc (comoving)

Slice Width:

$10/h$  kpc (comoving)

successive zoom-in calculation from cosmological initial conditions (using SPH and new grid-code AREPO)

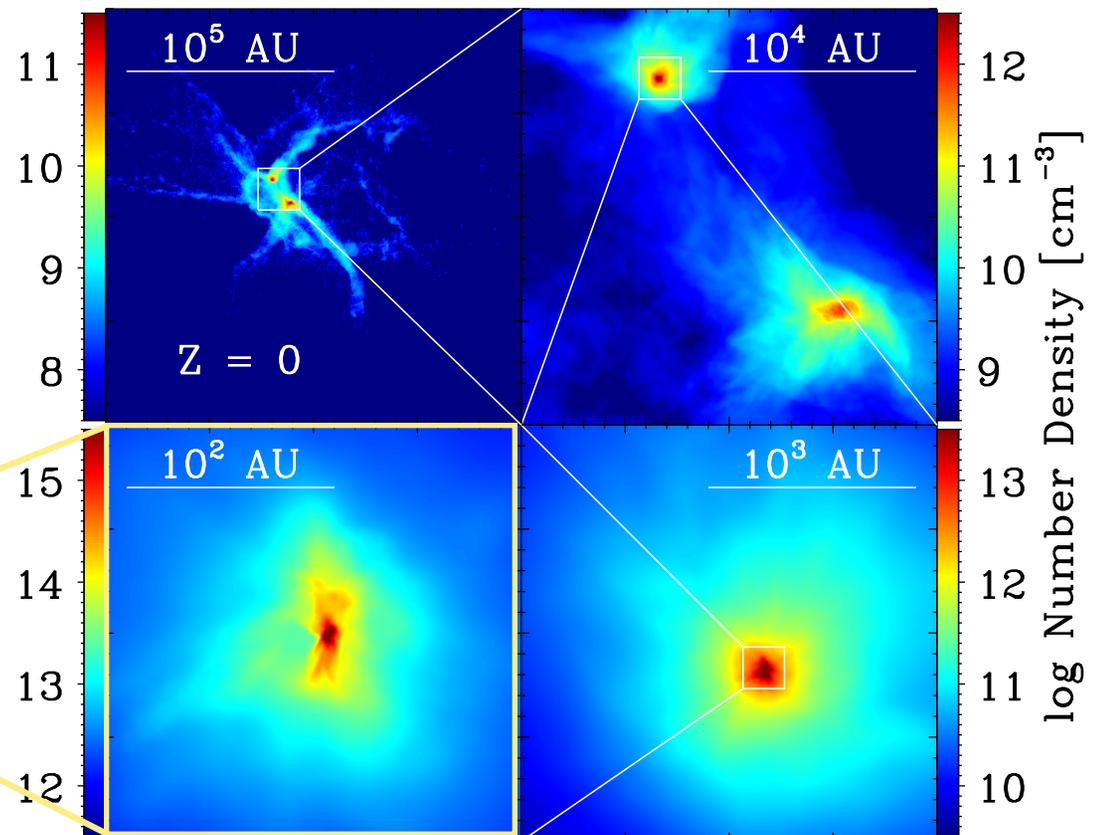


(Greif et al., 2007, ApJ, 670, 1)

(Greif et al. 2011, ApJ, 737, 75, Greif et al. 2012, MNRAS, 424, 399, Dopcke et al. 2013, ApJ, 776, 103)

# detailed look at accretion disk around first star

successive zoom-in calculation from cosmological initial conditions (using SPH and new grid-code AREPO)



(Greif et al. 2011, ApJ, 737, 75, Greif et al. 2012, MNRAS, 424, 399, Dopcke et al. 2012, ApJ submitted, arXiv 1203.6842)

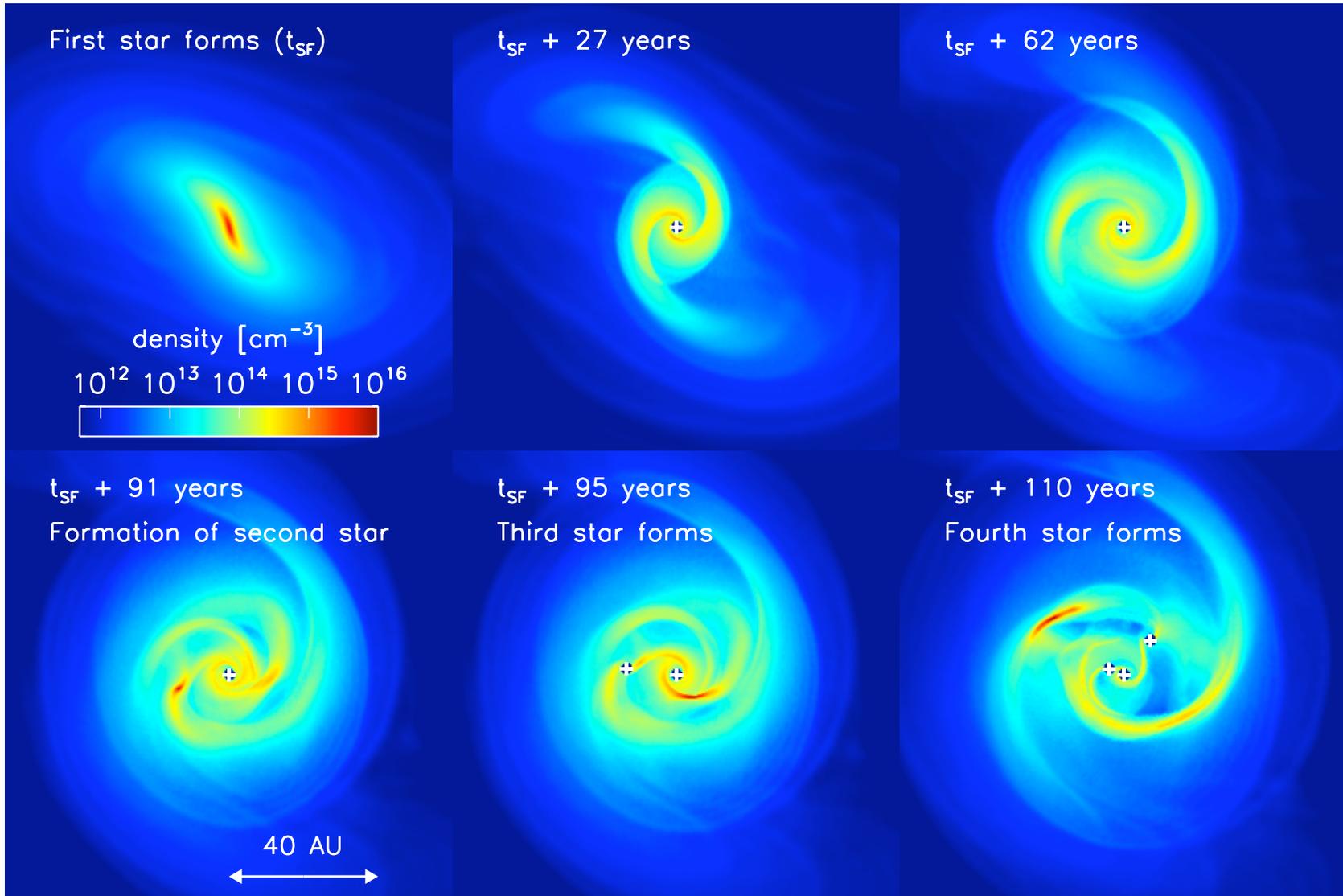
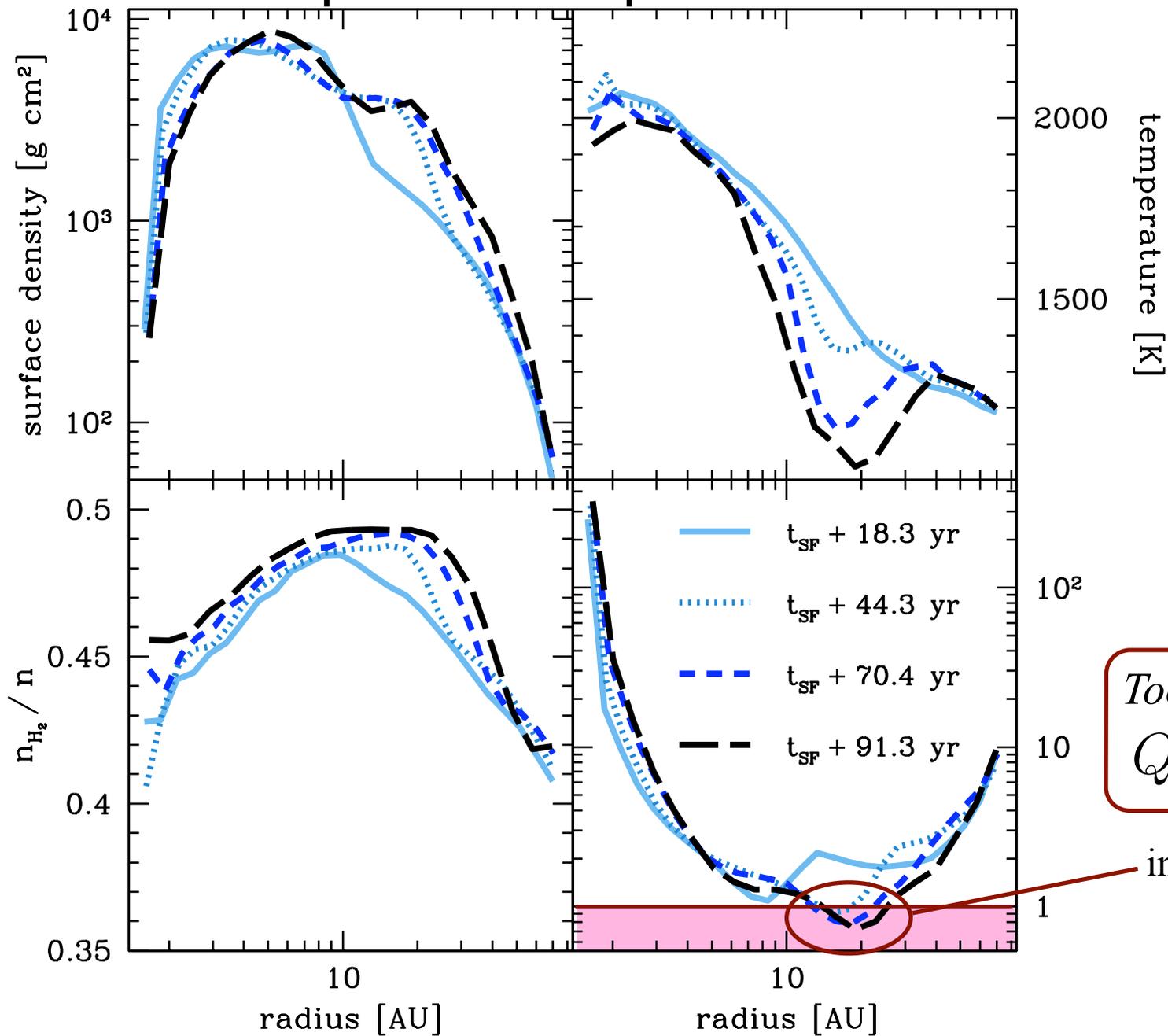
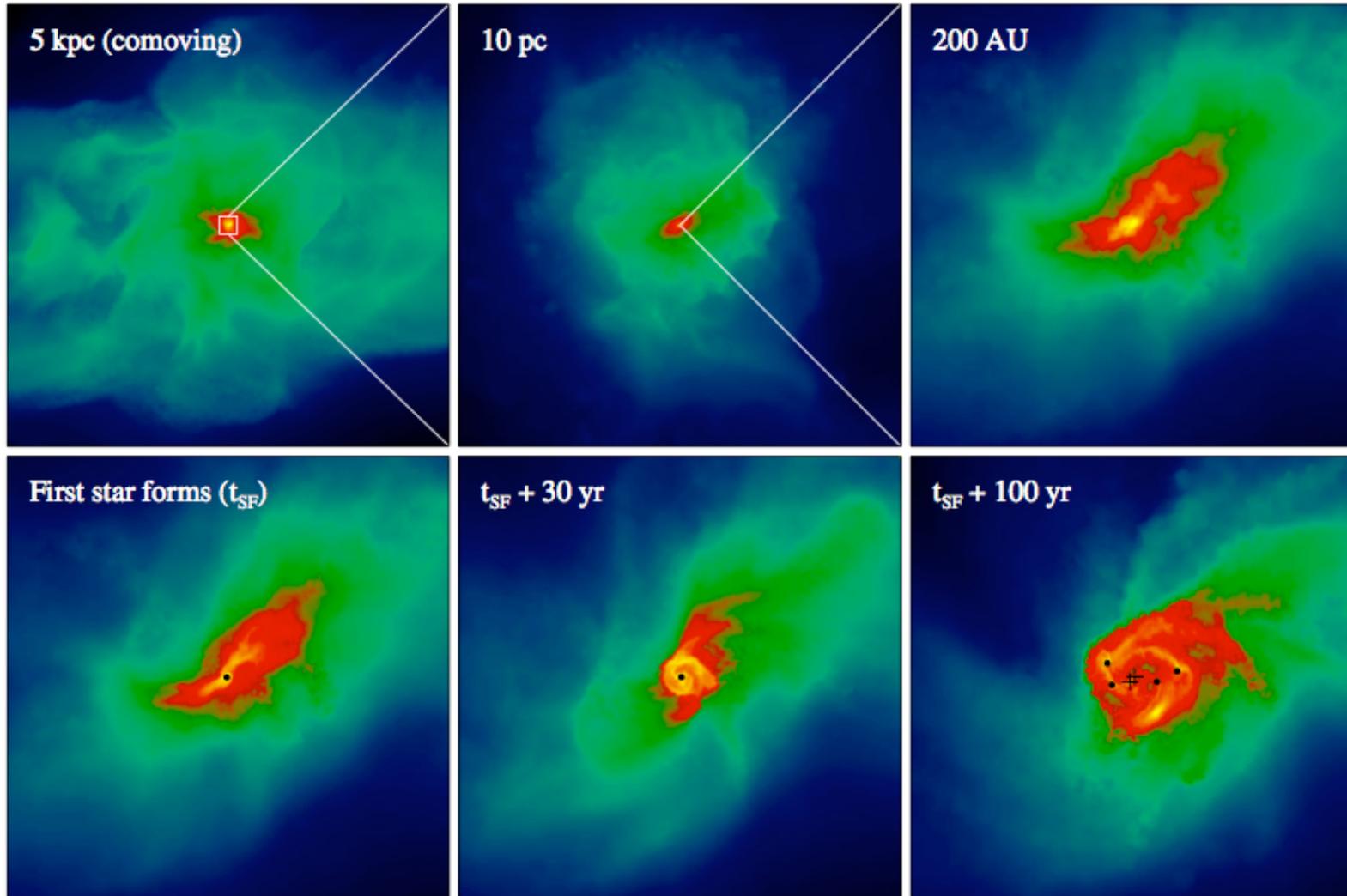


Figure 1: Density evolution in a 120 AU region around the first protostar, showing the build-up of the protostellar disk and its eventual fragmentation. We also see ‘wakes’ in the low-density regions, produced by the previous passage of the spiral arms.

# important disk parameters



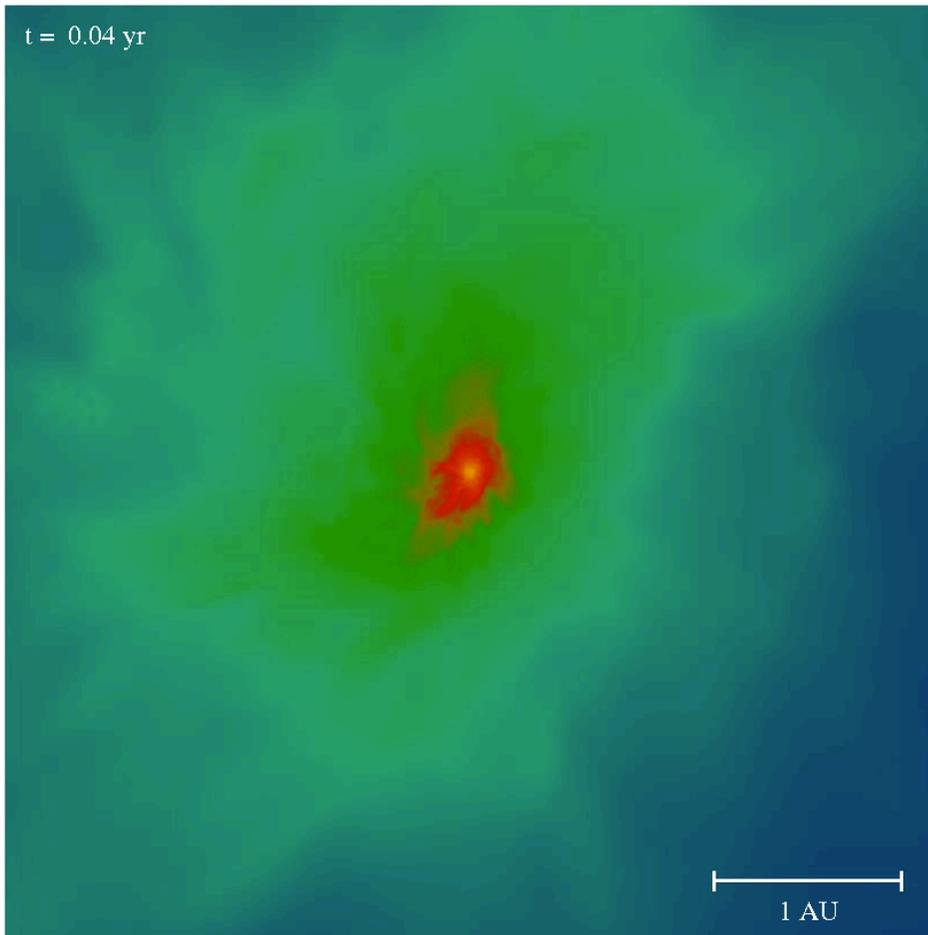
similar study with very different numerical method (AREPO)



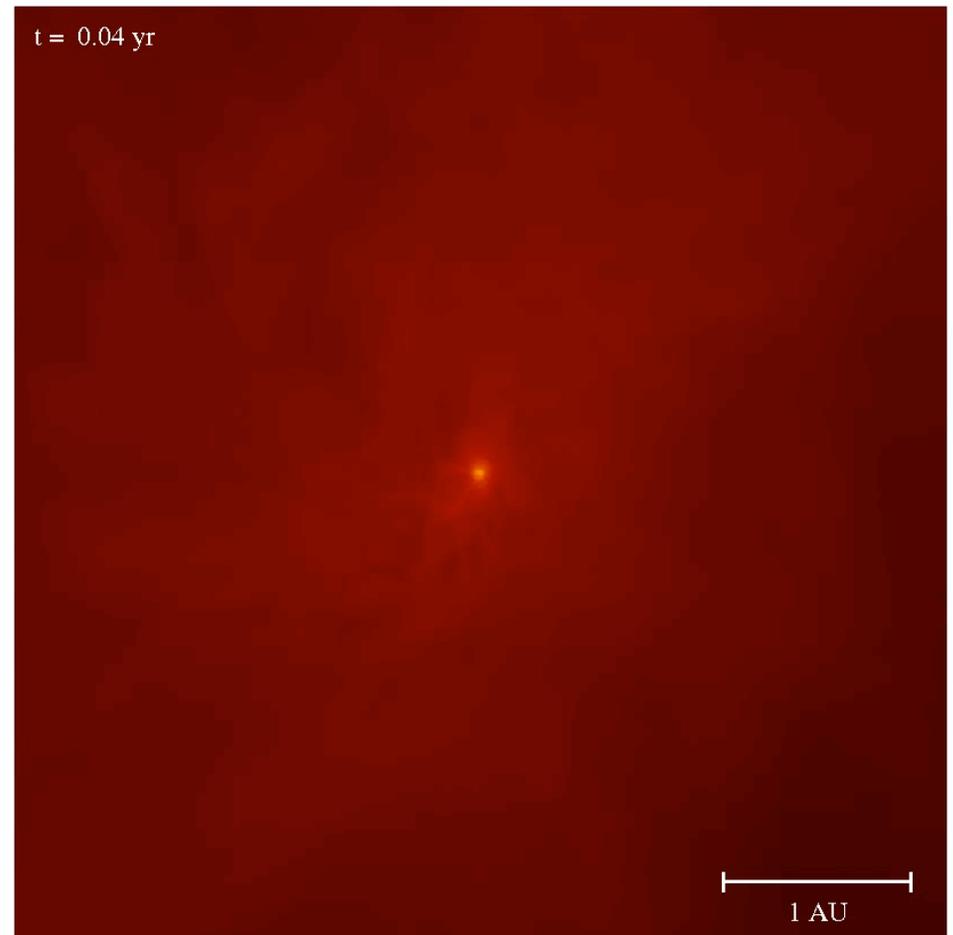
one out of five halos

Most recent calculations:

*fully sink-less simulations, following the disk build-up over  $\sim 10$  years  
(resolving the protostars - first cores - down to  $10^5$  km  $\sim 0.01 R_{\odot}$ )*



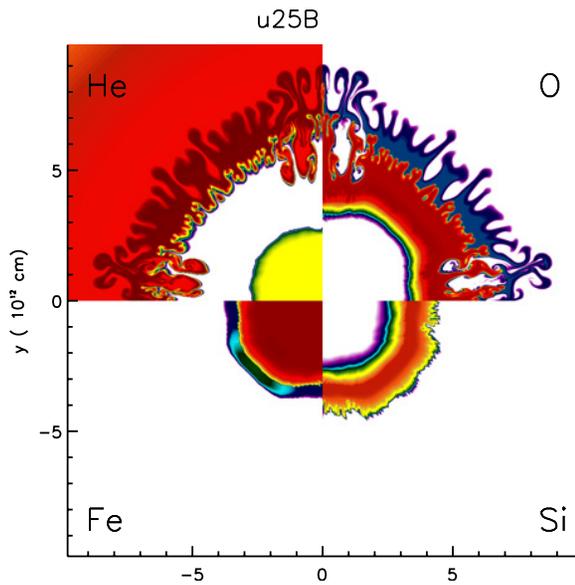
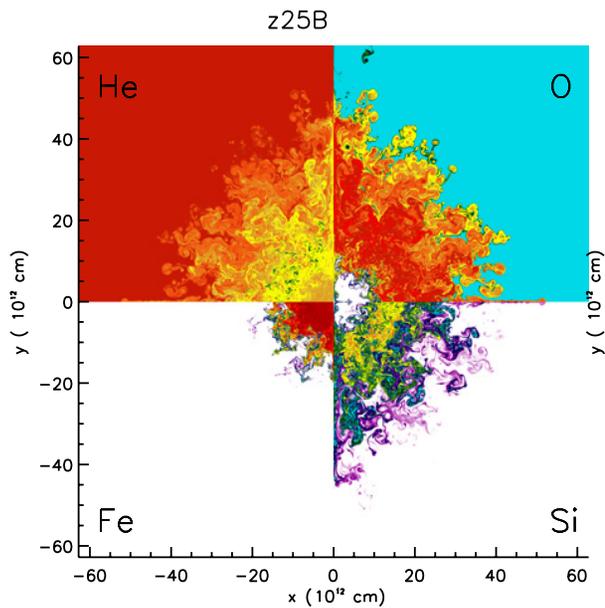
density



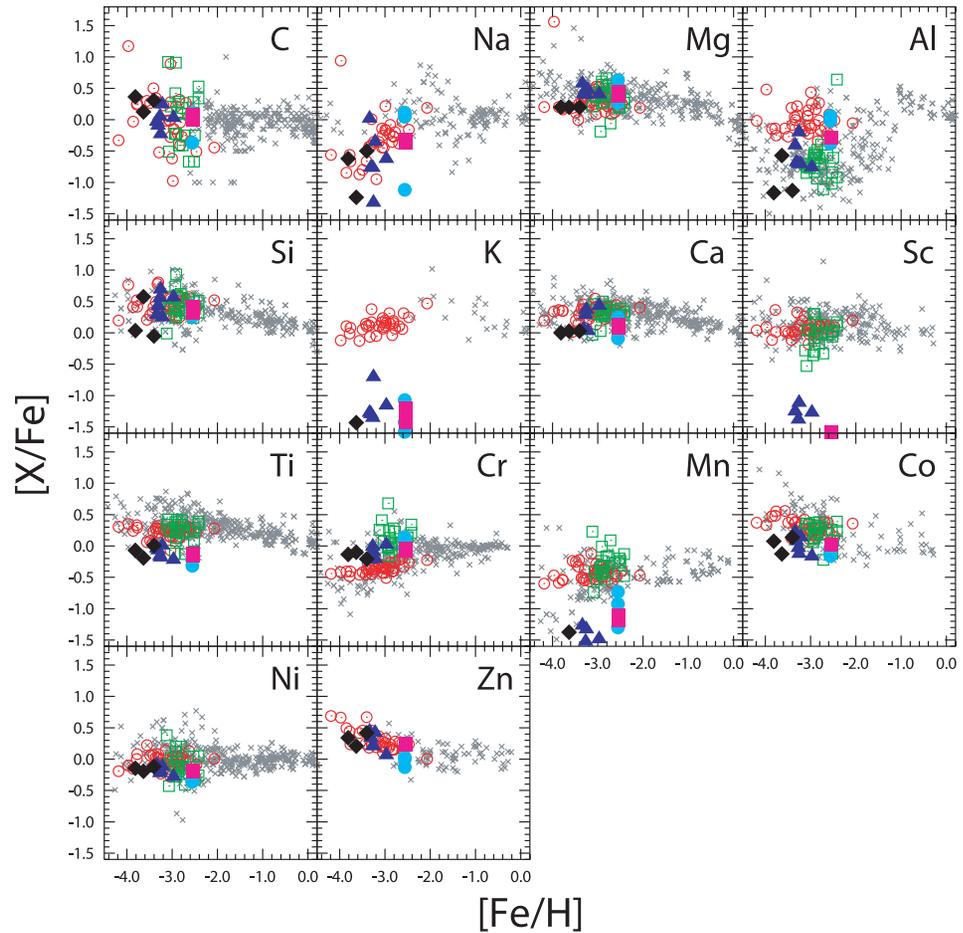
temperature

# expected mass spectrum

- *expected IMF is flat* and covers a wide range of masses
- implications
  - because slope  $> -2$ , most *mass is in massive objects* as predicted by most previous calculations
  - most high-mass Pop III stars should be in *binary systems* --> source of *high-redshift gamma-ray bursts*
  - because of ejection, some *low-mass objects* ( $< 0.8 M_{\odot}$ ) might have *survived* until today and could potentially be found in the Milky Way
- consistent with abundance patterns found in second generation stars



(Joggerst et al. 2009, 2010)



(Tominaga et al. 2007)

The metallicities of extremely metal-poor stars in the halo are consistent with the yields of core-collapse supernovae, i.e. progenitor stars with 20 - 40  $M_{\odot}$

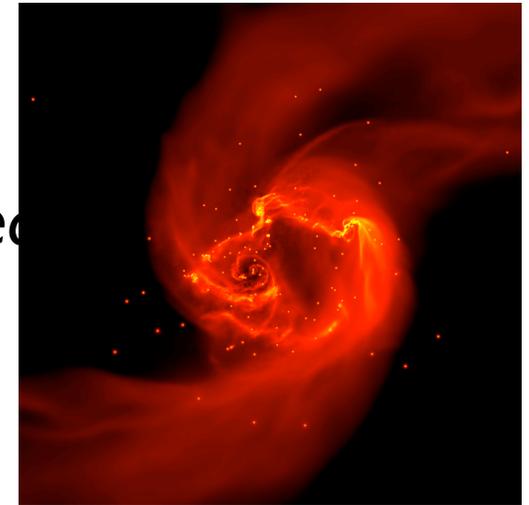
(e.g. Tominaga et al. 2007, Izutani et al. 2009, Joggerst et al. 2009, 2010)

# primordial star formation

- just like in present-day SF, we expect
  - *turbulence*
  - *thermodynamics (i.e. balance between heating and cooling)*
  - *feedback*
  - *magnetic fields*

to influence first star formation.

- masses of first stars still *uncertain*, but we expect a wide *mass range* with *typical masses* of several *10s of  $M_{\odot}$*
- disks unstable: first stars in *binaries* or *part of small clusters*
- current frontier: include *feedback* and *magnetic fields* and possibly *dark matter annihilation...*

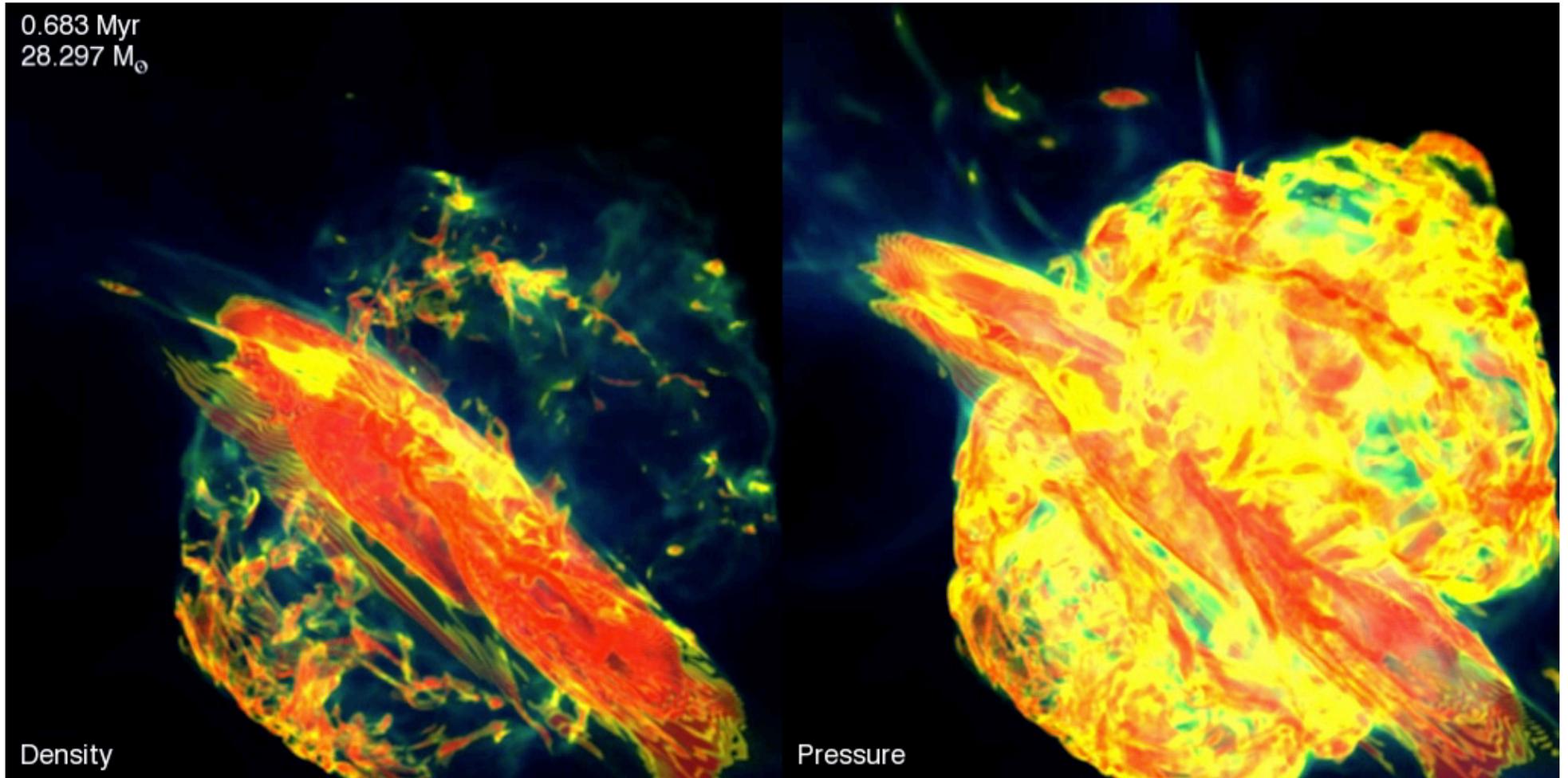


# reducing fragmentation

- from present-day star formation theory we know, that
  - magnetic fields: Peters et al. 2011, Seifried et al. 2012, Hennebelle et al. 2011
  - accretion heating: Peters et al. 2010, Krumholz et al. 2009, Kuipers et al. 2011can influence the fragmentation behavior.
- in the context of Pop III
  - radiation: Hosokawa et al. 2012, Stacy et al. 2012a
  - magnetic fields: Turk et al. 2012, but see also Bovino et al. 2013  
Schleicher et al. 2010, Sur et al. 2010, Federrath et al. 2011, Schober et al. 2012ab, 2013
- all these will reduce degree of fragmentation  
(but not by much, see Rowan Smith et al. 2011, 2012, at least for accretion heating)
- DM annihilation might become important for disk dynamics and fragmentation (Ripamonti et al. 2011, Stacy et al. 2012b, Rowan Smith et al. 2012)

magnetic fields

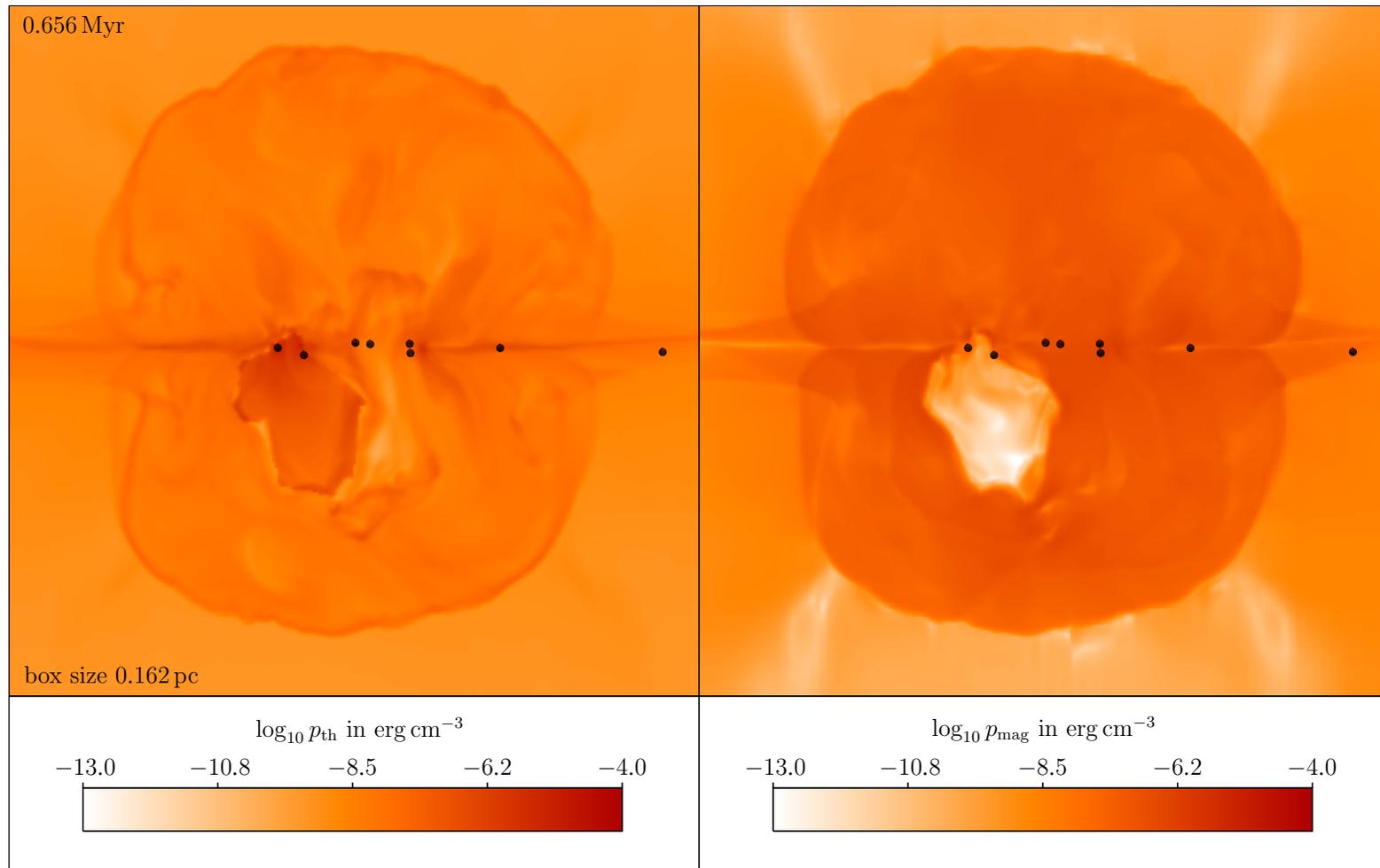
# influence of B on disk evolution



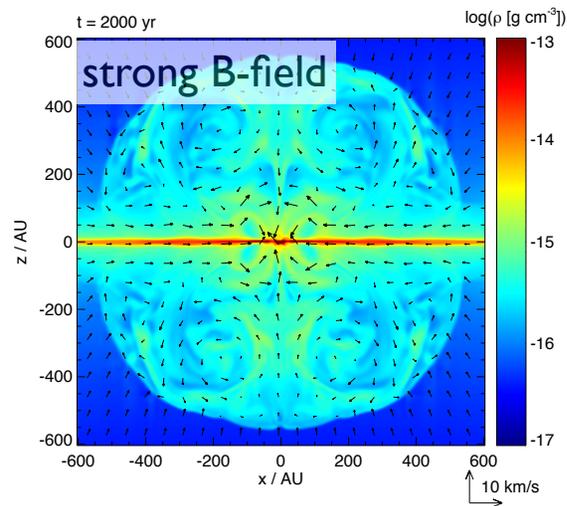
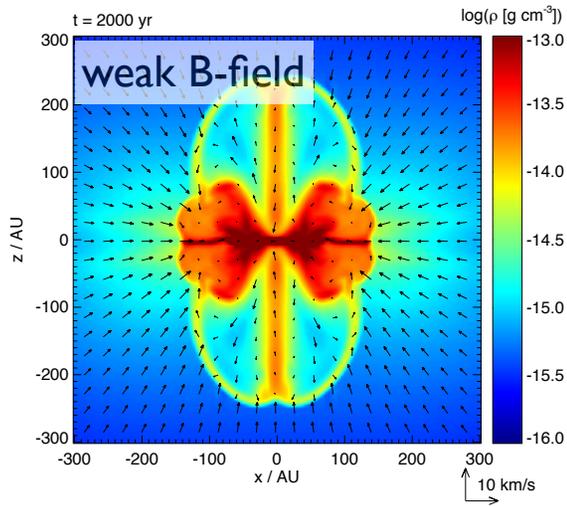
Peters et al. (2011)

in disk around high-mass stars, fragmentation is reduced but rarely fully suppressed  
see Peters et al. (2011), Hennebelle et al. (2011), Seifried et al. (2011)

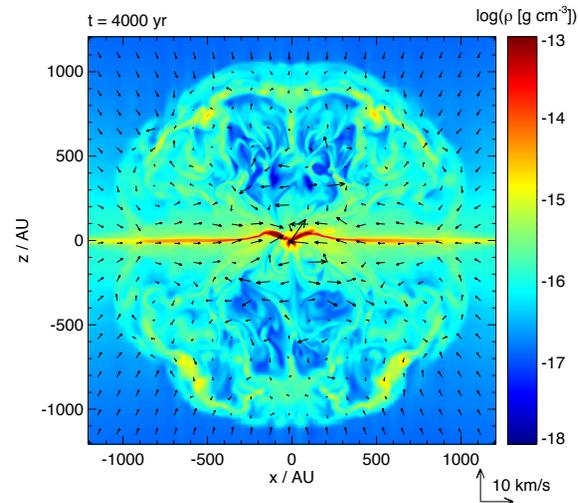
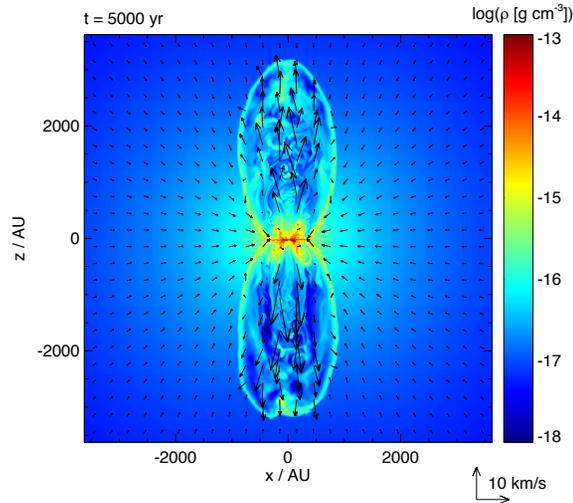
# interplay of ionization and B-field



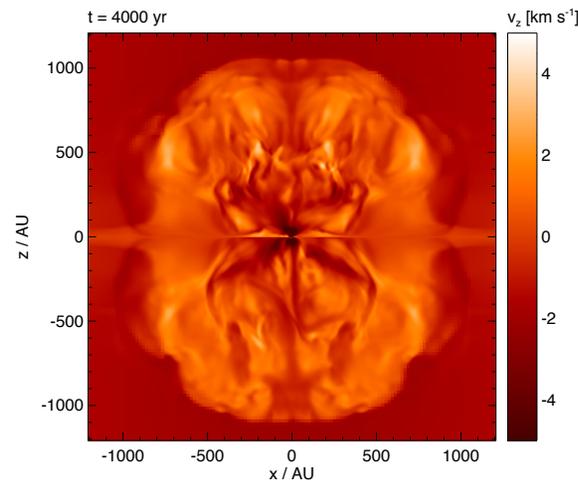
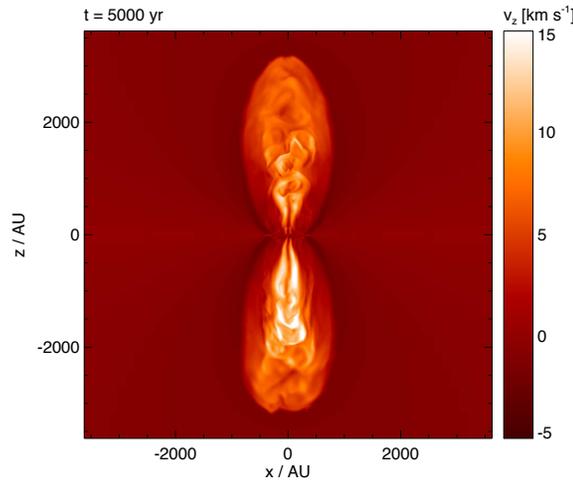
**Figure 10.** Comparison of thermal and magnetic pressure for the data from the lefthand panels in Figure 5. The thermal pressure  $p_{\text{th}}$  inside the H II region (left) is of comparable magnitude to the magnetic pressure  $p_{\text{mag}}$  outside the H II region (right). Thus, magnetic pressure plays a significant role in constraining the size of expanding H II regions. The black dots represent sink particles.



density in inner region  
and early times



density on larger scales  
and later times



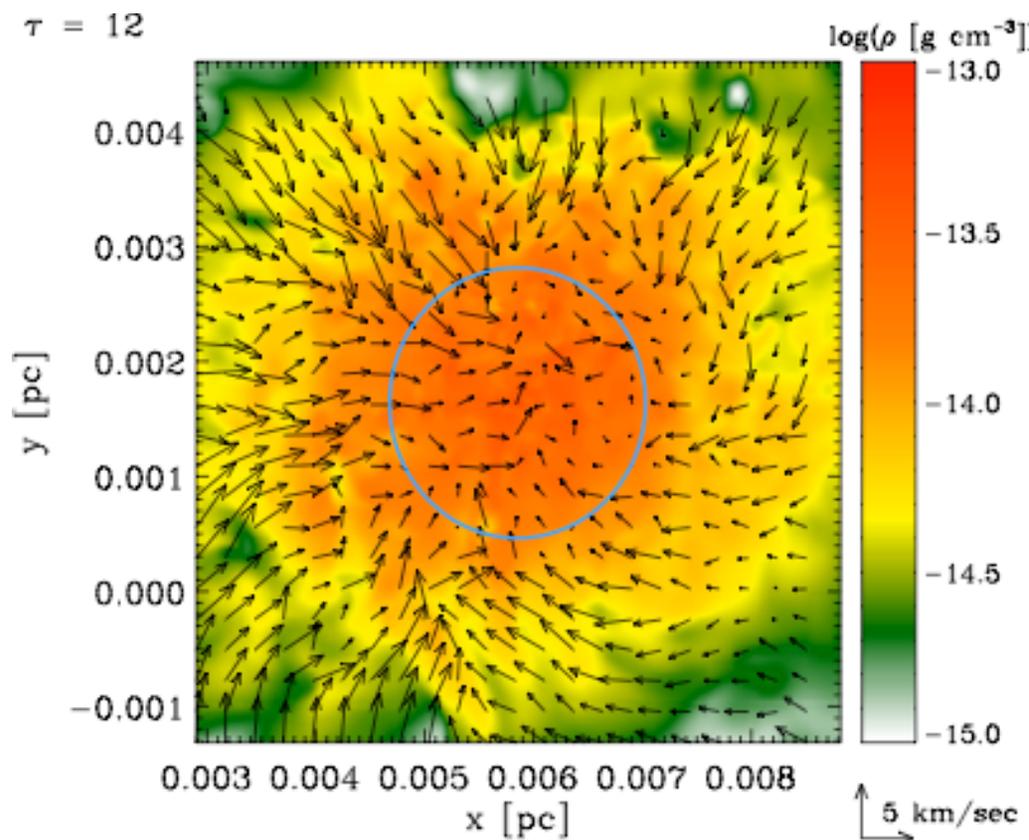
velocity on larger scales  
and later times

# B fields in the early universe?

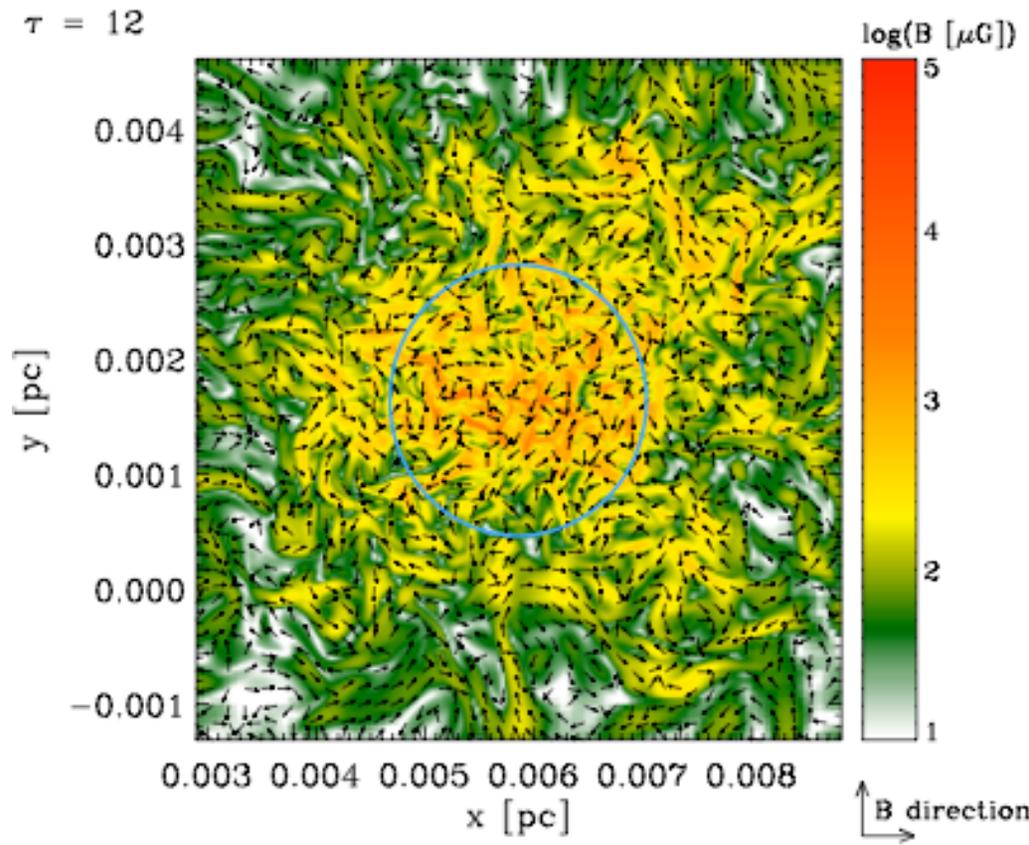
- we know the universe is magnetized (now)
- knowledge about B-fields in the high-redshift universe is extremely uncertain
  - inflation / QCD phase transition / Biermann battery / Weibel instability
- they are thought to be extremely small
- however, *THIS MAY BE WRONG!*

# small-scale turbulent dynamo

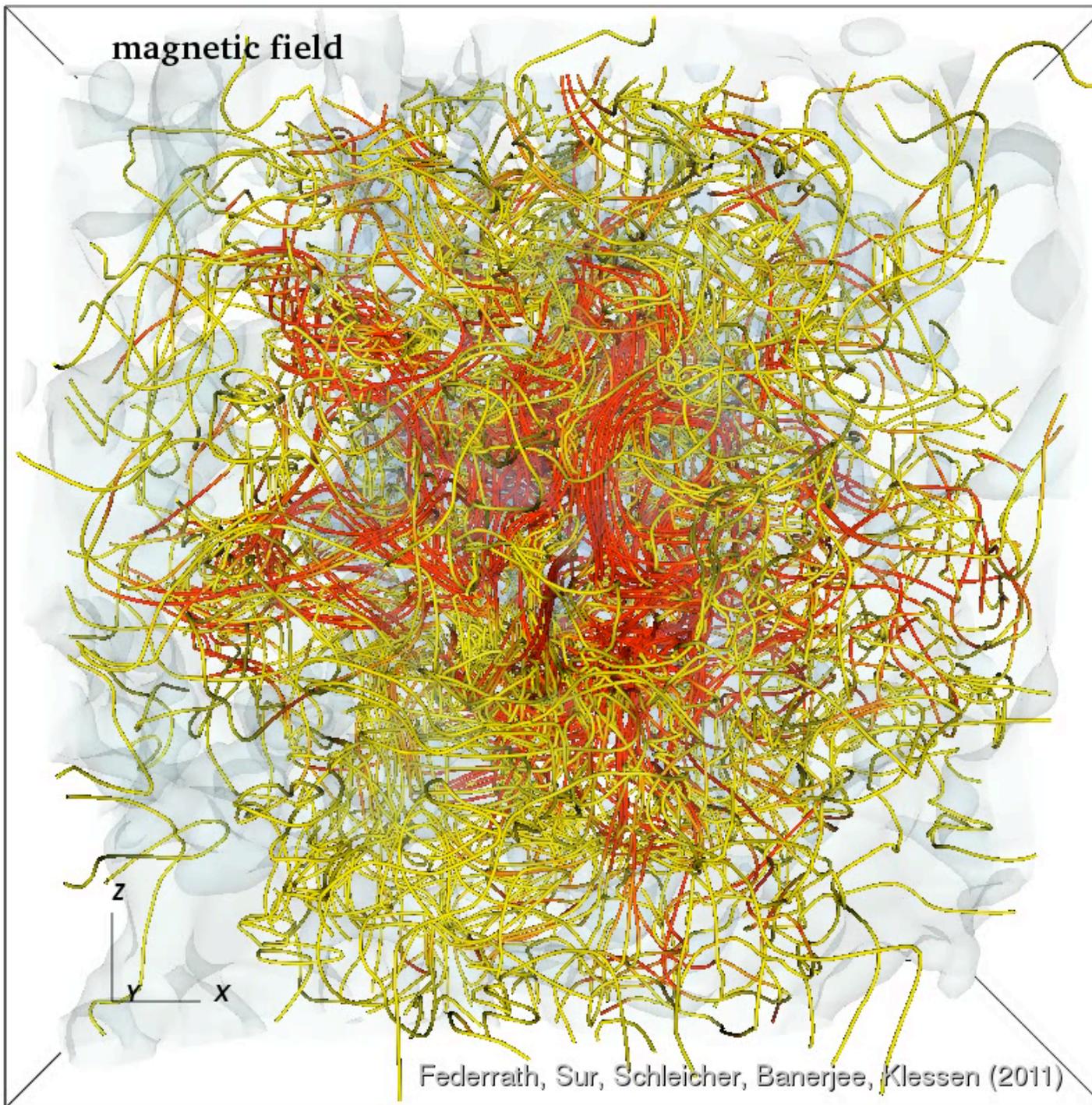
- *idea*: the small-scale turbulent dynamo can generate strong magnetic fields from very small seed fields
- *approach*: model collapse of primordial gas ---> formation of the first stars in low-mass halo
- *method*: solve ideal MHD with very high resolution
  - grid-based AMR code FLASH
  - polytropic EOS with  $\gamma = 1.1$
  - resolution up to  $128^3$  cells per Jeans volume (effective resolution  $65536^3$  cells)
  - see: Schleicher et al. 2010, A&A, 522, A115, Sur et al. 2010, ApJ, 721, L734, Federrath et al., 2011, ApJ, 731, 62, Schober 2012, PRE, 85, 026303, Schober et al. 2012, ApJ, 754, 99



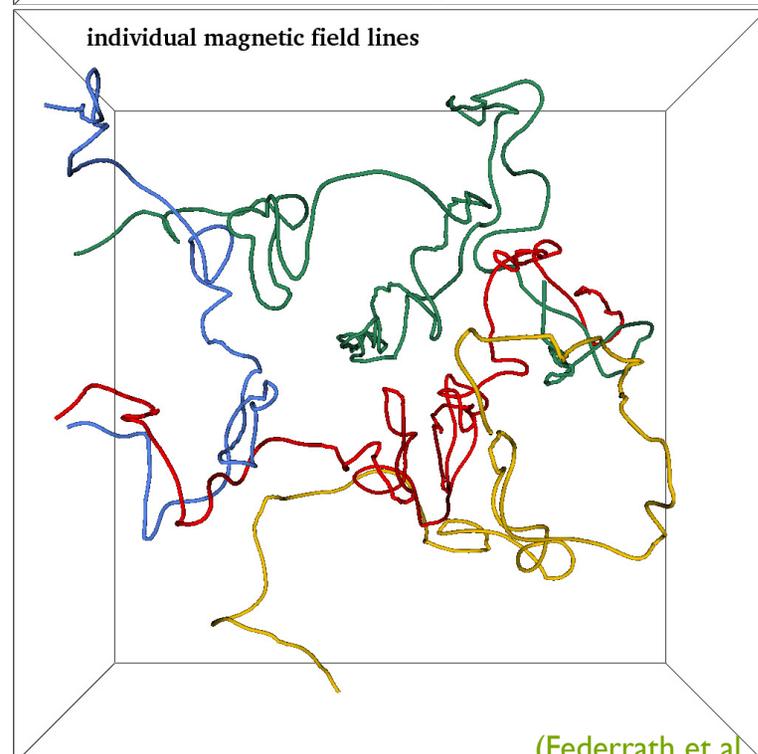
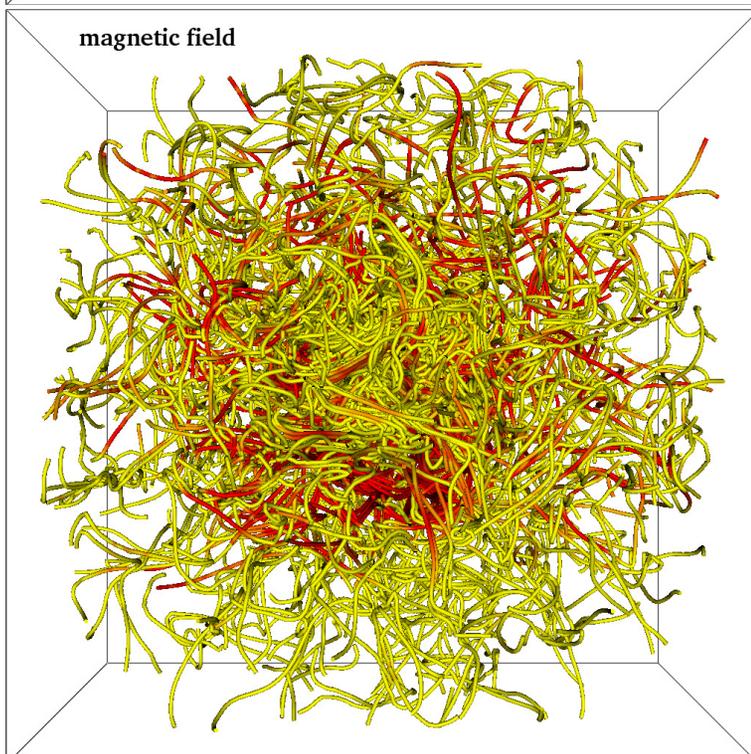
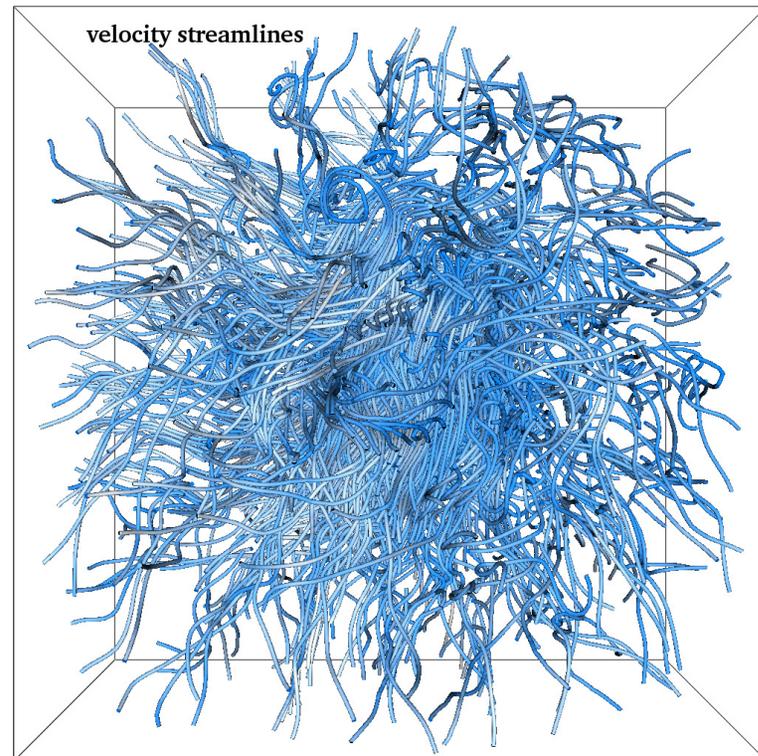
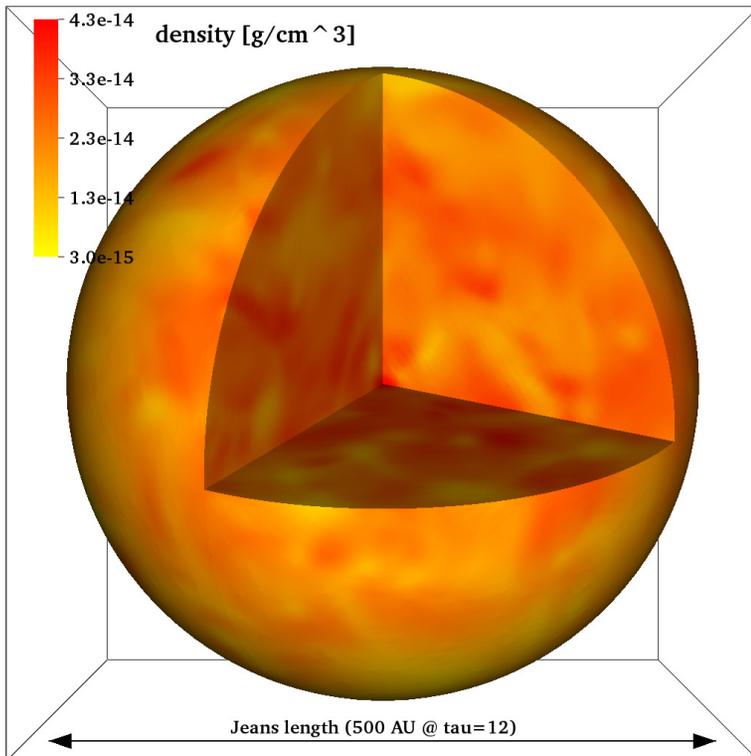
magnetic field structure

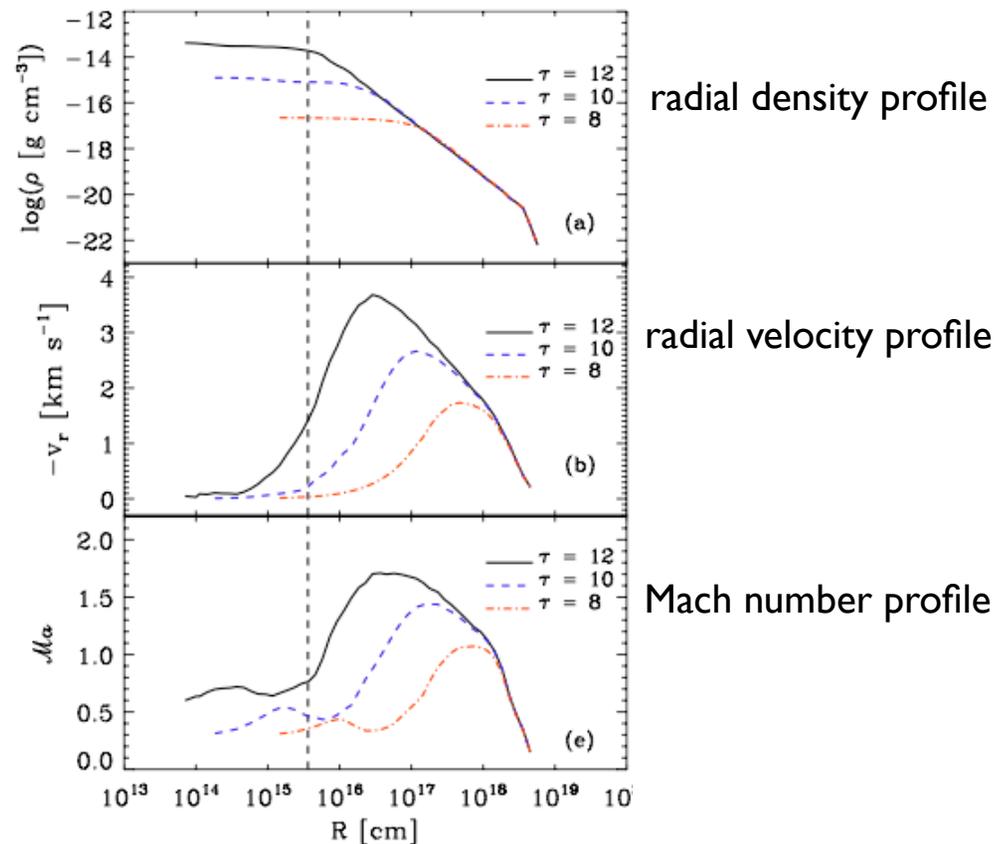
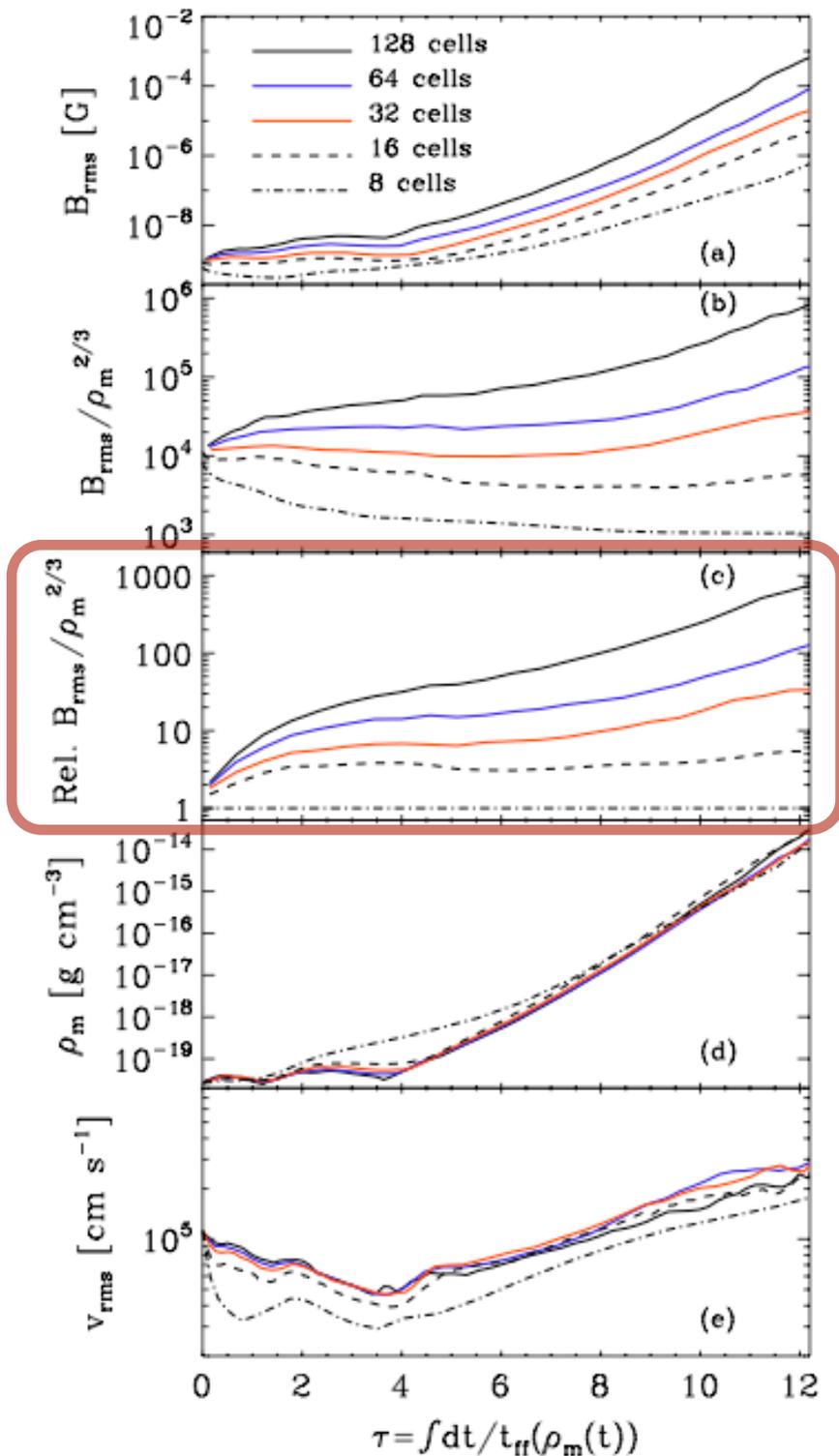


density structure



(Schleicher et al. 2010, A&A, 522, A115, Sur et al. 2010, ApJ, 721, L734, Federrath et al., 2011, ApJ, 731, 62)

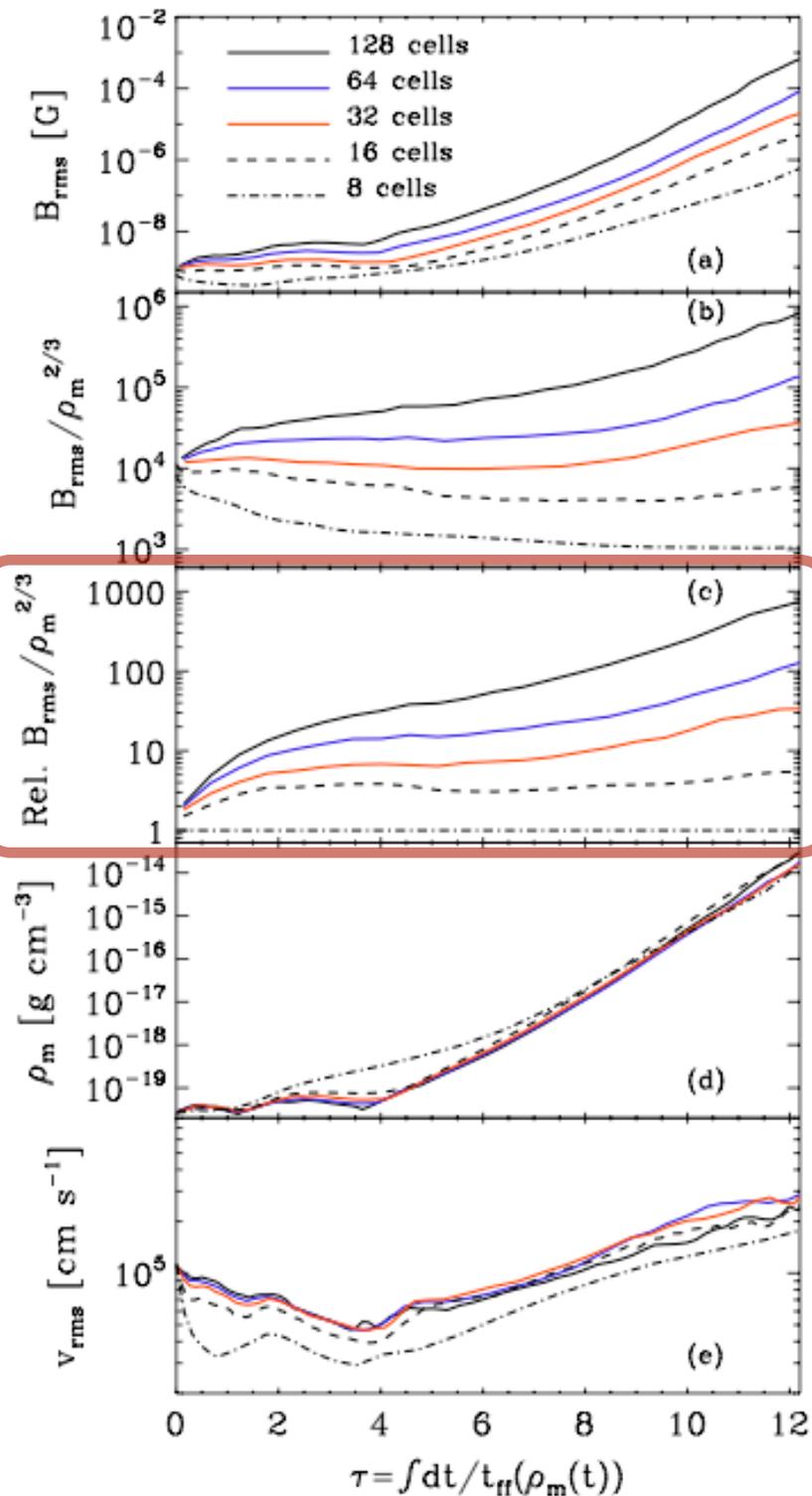




Field amplification during first collapse seems unavoidable.

QUESTIONS:

- Is it really the small scale dynamo?
  - What is the saturation value?
- Can the field reach dynamically important strength?



Field amplification during first collapse seems unavoidable.

QUESTIONS:

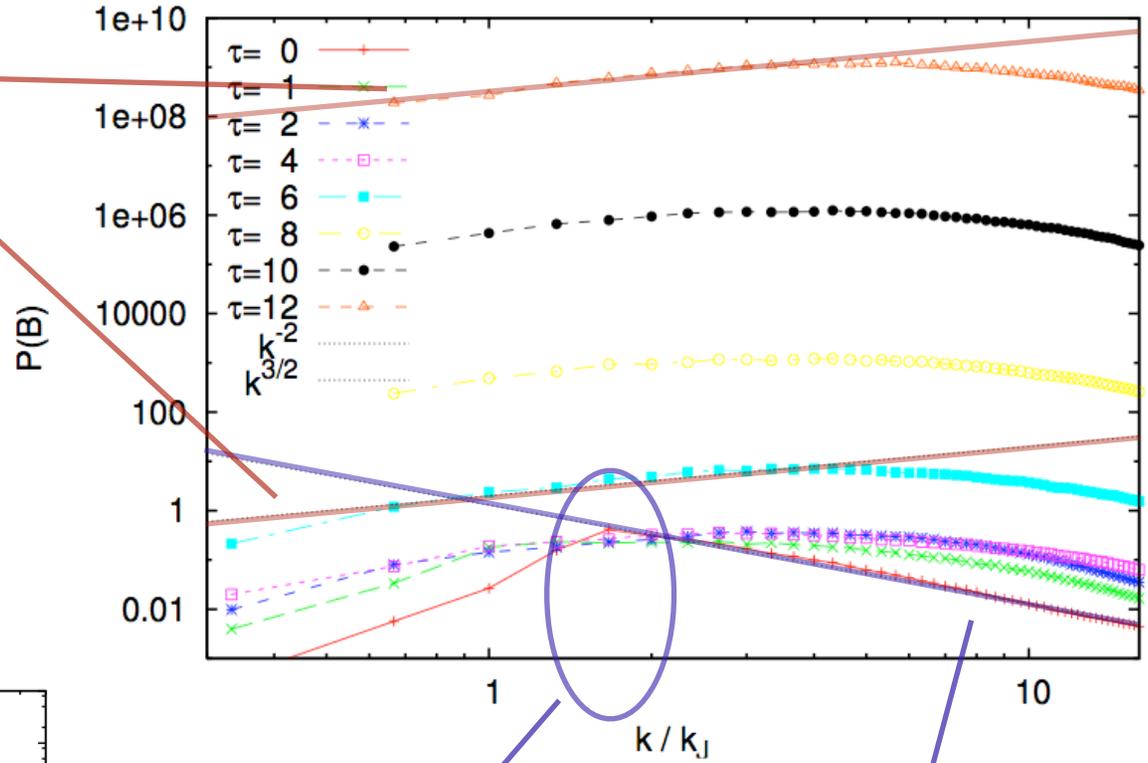
- Is it really the small scale dynamo?
- What is the saturation value?  
Can the field reach dynamically important strength?
- How does it depend on the thermodynamics of the gas (i.e. on the EOS)?

# Kazantsev behavior

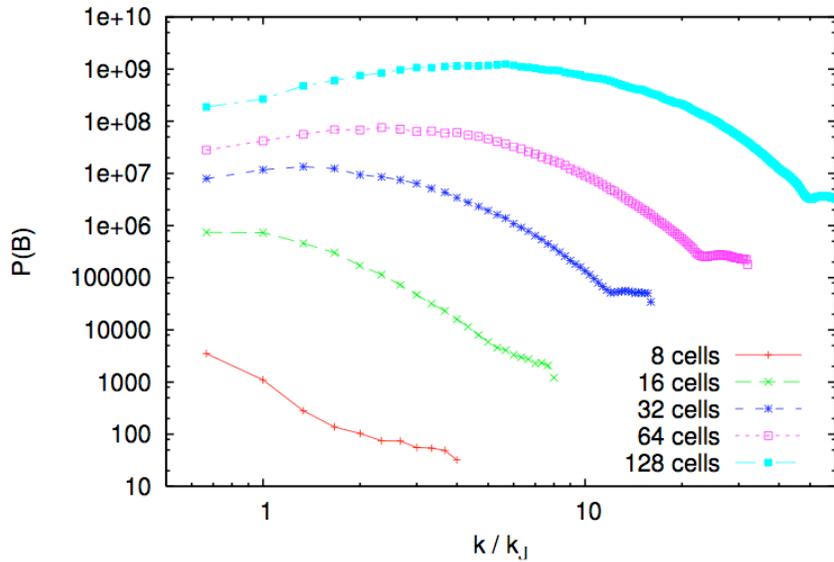
Slope +3/2 of Kazantsev theory

(e.g. Brandenburg & Subramanian, 2005, Phys. Rep., 417, 1)

time evolution of magnetic field spectra (128 cell run)



resolution dependence ( $\tau=12$ )

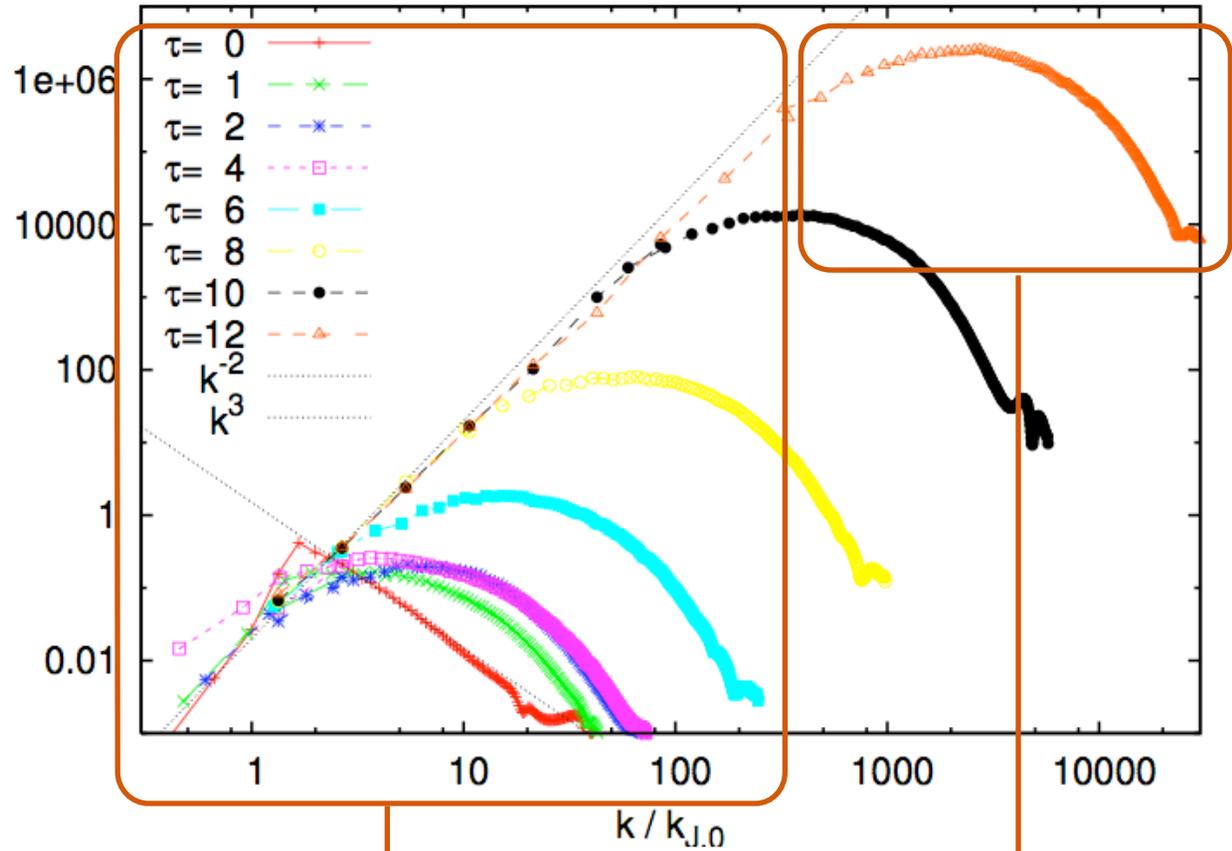


initial peak of B fluctuation spectrum

initial slope of B fluctuations

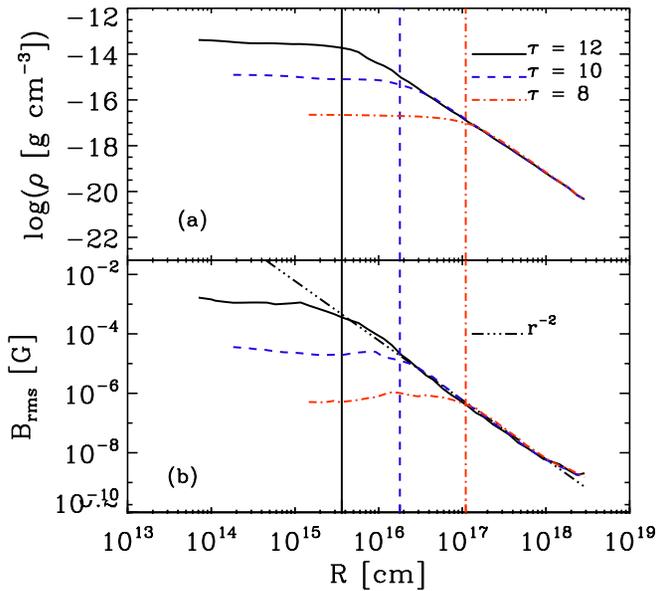
# analysis of magnetic field spectra

time evolution of magnetic field spectra (128 cell run)



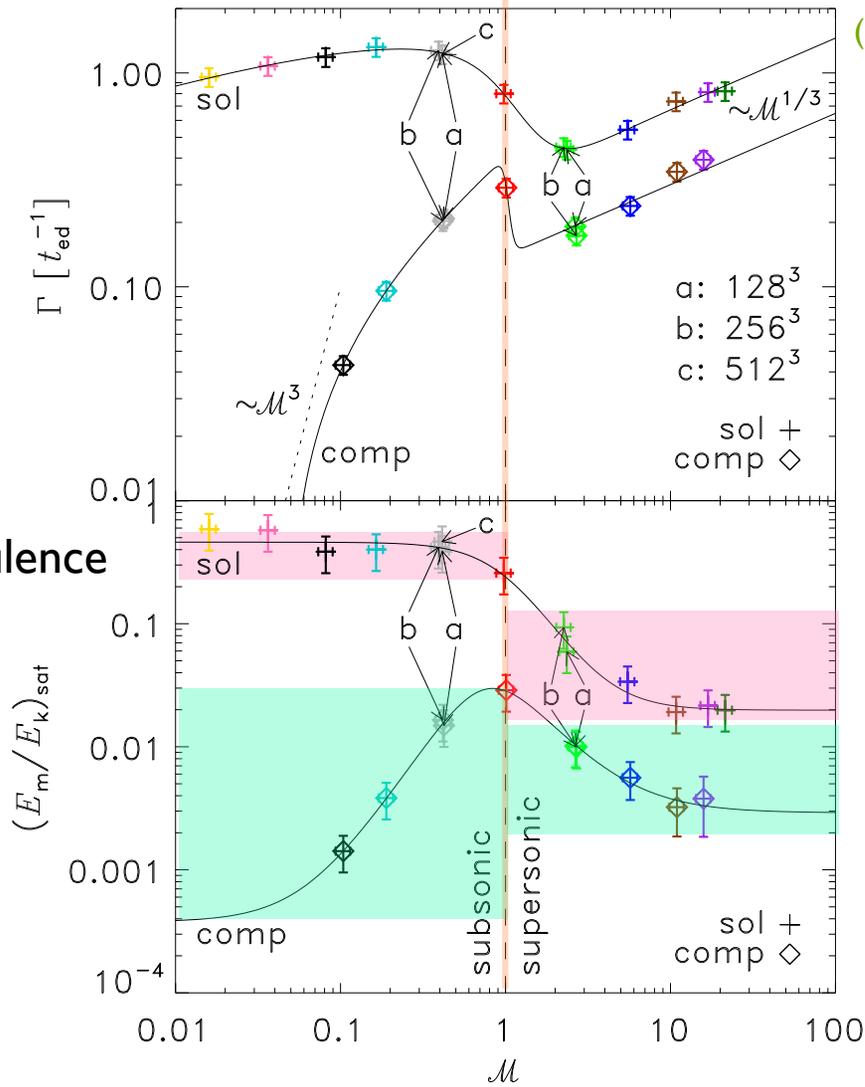
B fluctuation spectrum in  $1/r^2$  fall-off

B fluctuation spectrum in flat inner core



# Saturation level

(Federrath et al., 2011, PRL, 107, 114505)



subsonic, solenoidal turbulence

subsonic,  
compressive turbulence

saturation level for supersonic,  
solenoidal turbulence

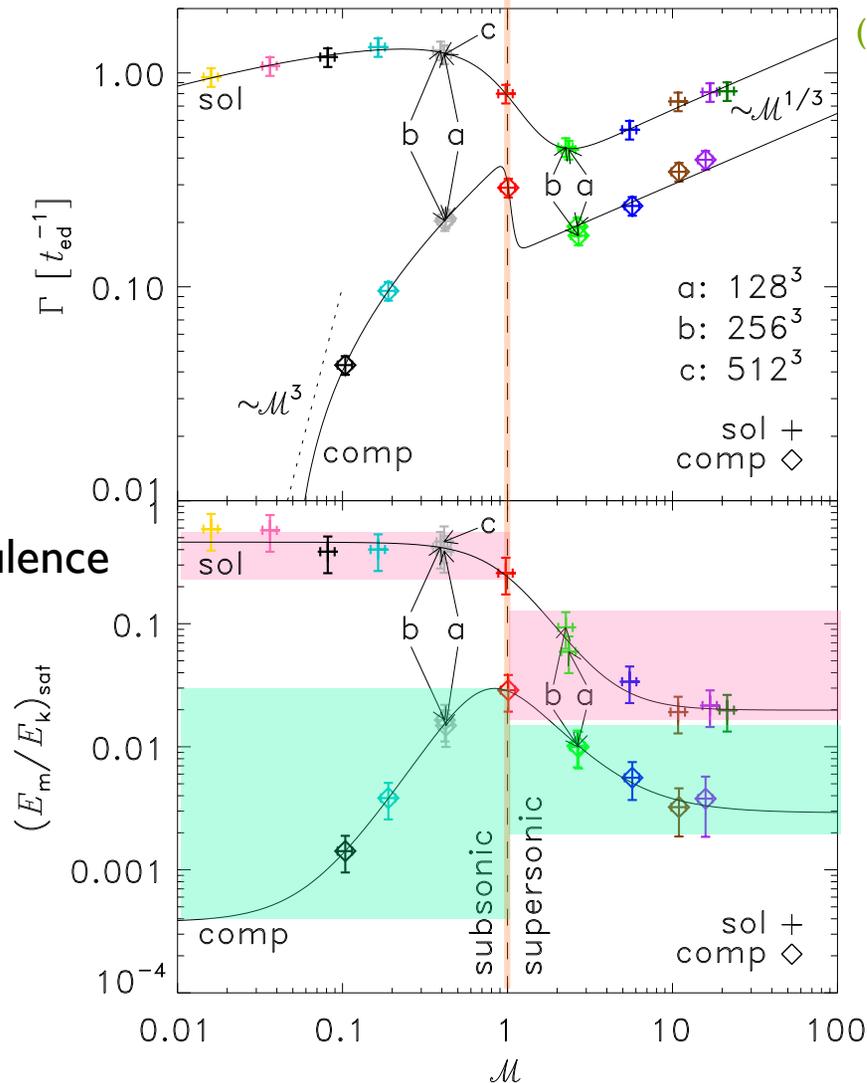
saturation level for supersonic,  
compressive turbulence

# Saturation level

(Federrath et al., 2011, PRL, 107, 114505)

subsonic, solenoidal turbulence

subsonic, compressive turbulence



saturation level for supersonic, solenoidal turbulence

saturation level for supersonic, compressive turbulence

This behavior is reproduced *analytically* using the *Kazantsev* formalism for very large and very small Prandtl numbers, and for the range from Kolmogorov to Burgers turbulence.

(Schober et al., 2012, PRE, 85, 026303, Schober et al. 2012, ApJ, 754, 99, Schober et al. 2012, PRE, submitted, Bovino et al., PRL, submitted)

# turbulent velocity field

separation of smooth and turbulent component:

$$\vec{v} = \vec{v}_0 + \delta \vec{v}$$

properties of turbulent field  $\delta \vec{v}$  :

- isotropic and homogeneous
- Gaussian random field with zero mean
- delta-correlated in time

spatial two-point correlation of fluctuations:

$$\langle \delta v^i(\vec{x}, t) \delta v^j(\vec{y}, s) \rangle = T^{ij}(\mathbf{r}) \delta(t-s)$$

$$T^{ij}(\mathbf{r}) = \left( \delta^{ij} - \frac{r^i r^j}{r^2} \right) T_N(\mathbf{r}) + \frac{r^i r^j}{r^2} T_L(\mathbf{r})$$

# model for $T_L$

model for general turbulence:

$$T_L(r) \propto \begin{cases} (1 - Re^{(1-\vartheta)/(1+\vartheta)} (\frac{r}{L})^2) & , r < l_c \\ (1 - (\frac{r}{L})^{1+\vartheta}) & , l_c < r < L \\ 0 & , L < r \end{cases}$$

( $l_c$ : cut-off scale,  $L$ : scale of largest fluctuations,  
 $Re = VL/\nu$ : Reynolds number)

different turbulence models (in the inertial range):

$$\boxed{\nu(l) \propto l^\vartheta}$$

$$1/3 \text{ (Kolmogorov)} \leq \vartheta \leq 1/2 \text{ (Burgers)}$$

# MHD dynamo

idea: divide also magnetic field into mean and turbulent component

$$\vec{B} = \vec{B}_0 + \delta \vec{B}$$

put into induction equation:

$$\frac{\partial \vec{B}}{\partial t} = \nabla \times (\vec{v} \times \vec{B}) + \eta \nabla^2 \vec{B}$$

=> evolution equations for mean and turbulent field (large-scale dynamo and small-scale dynamo)

# Kazantsev theory

“Kazantsev Theory” (Kazantsev, 1968):  
theory of the small-scale dynamo

correlation function of magnetic fluctuation:

$$\langle \delta B^i(\vec{x}, t) \delta B^j(\vec{y}, t) \rangle = M^{ij}(r, t)$$

$$M^{ij} = \left( \delta^{ij} - \frac{r^i r^j}{r^2} \right) M_N + \frac{r^i r^j}{r^2} M_L$$

with  $\nabla \cdot \vec{B} = 0$  :

$$M_N = \frac{1}{2r} \frac{\partial}{\partial r} (r^2 M_L)$$

# Kazantsev theory

put magnetic correlation function into induction equation

=> Kazantsev equation:

$$M_L(r, t) \propto \Psi(r) e^{2\Gamma t}$$

$$-\kappa_T(r) \frac{\partial^2 \Psi(r)}{\partial^2 r} + U_0(r) \Psi(r) = -\Gamma \Psi(r)$$

$$\kappa_T(r) = \kappa_T(T_L(r), \eta) \quad \text{“mass”}$$

$$U_0(r) = U_0(T_L(r), T_N(r), \eta) \quad \text{“potential”}$$

can be solved with WKB-approximation for large magnetic Prandtl numbers ( $\nu/\eta$ )

# critical mag. Reynolds number

Reynolds number for minimal growth rate:  
set  $\Gamma = 0$  in Kazantsev equation  
and solve for  $Rm$  ( $Rm = VL/\eta$ )

result (for Kolmogorov turbulence):

$$Rm > 110$$

result (for Burgers turbulence):

$$Rm > 2700$$

=> need high resolution in order to see dynamo  
in simulations

# growth rate

growth rate for large magnetic Prandtl numbers:

$$\Gamma \propto Re^{(1-\vartheta)/(1+\vartheta)}$$

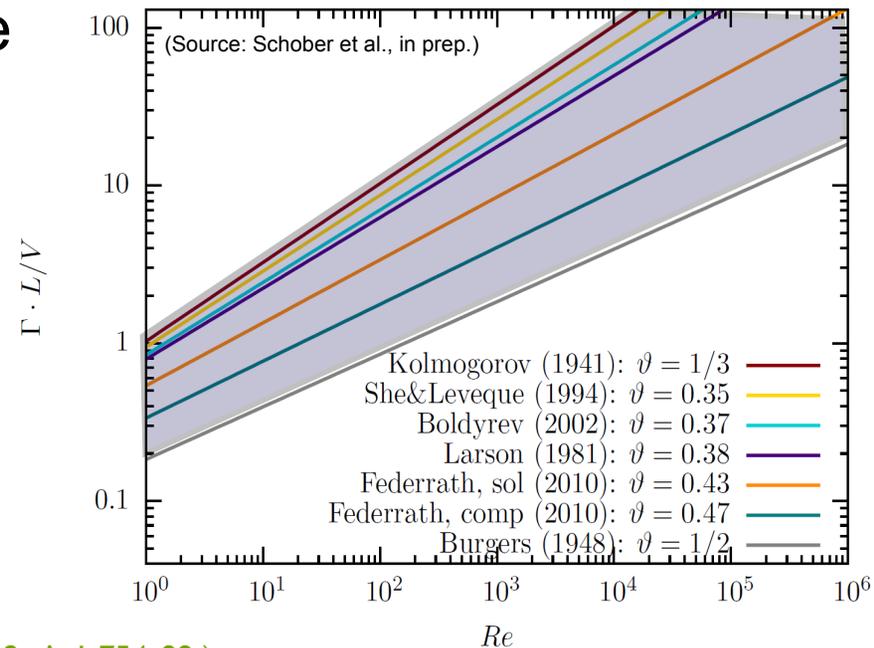
(with slope of the turbulent velocity spectrum  $v(l) \propto l^\vartheta$ )

example 1: Kolmogorov turbulence

$$\Gamma \propto Re^{1/2}$$

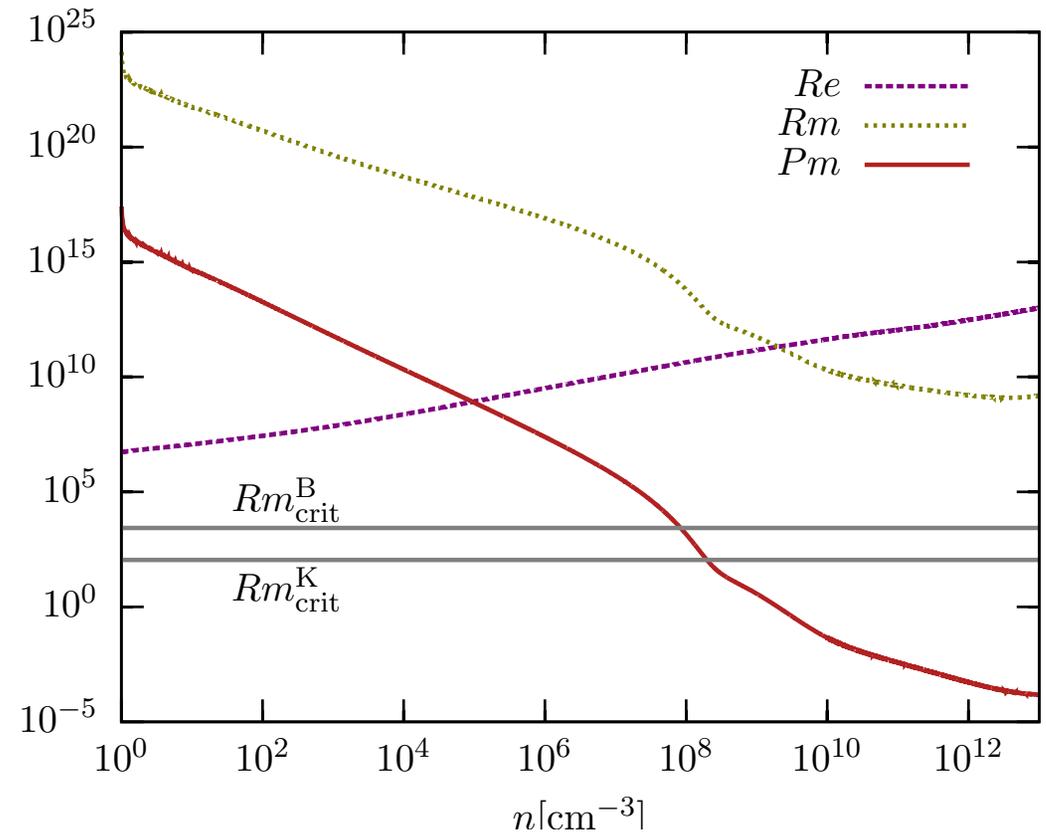
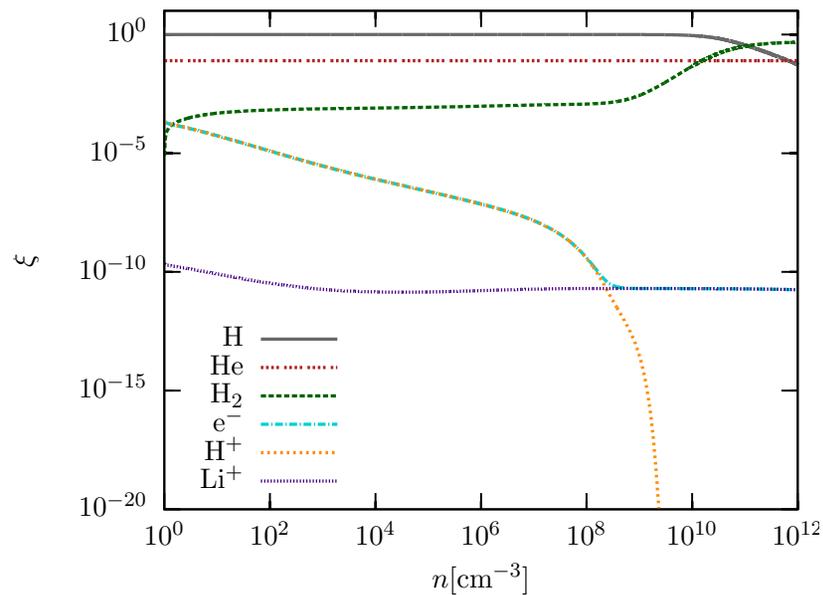
example 2: Burgers turbulence

$$\Gamma \propto Re^{1/3}$$



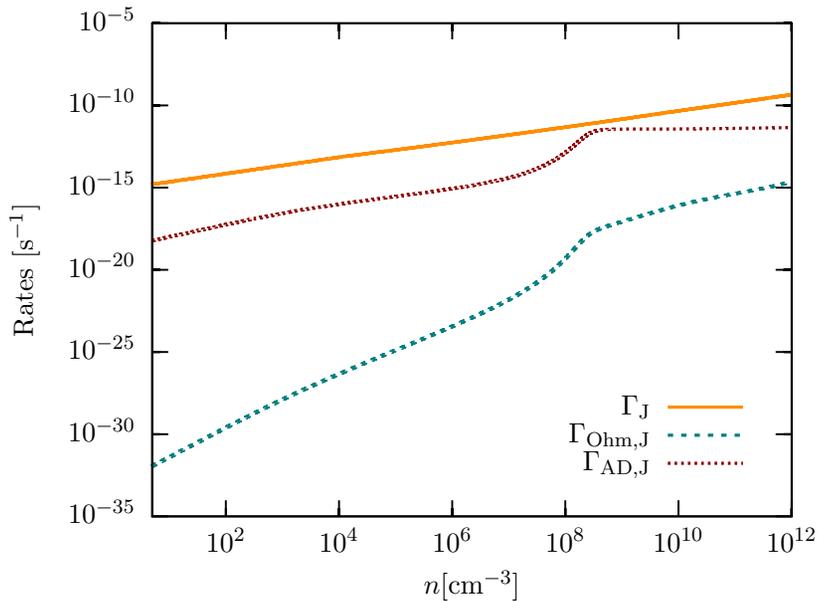
# dynamo in early universe

calculation of characteristic quantities in primordial gas with the chemistry code of Glover & Savin (2009)

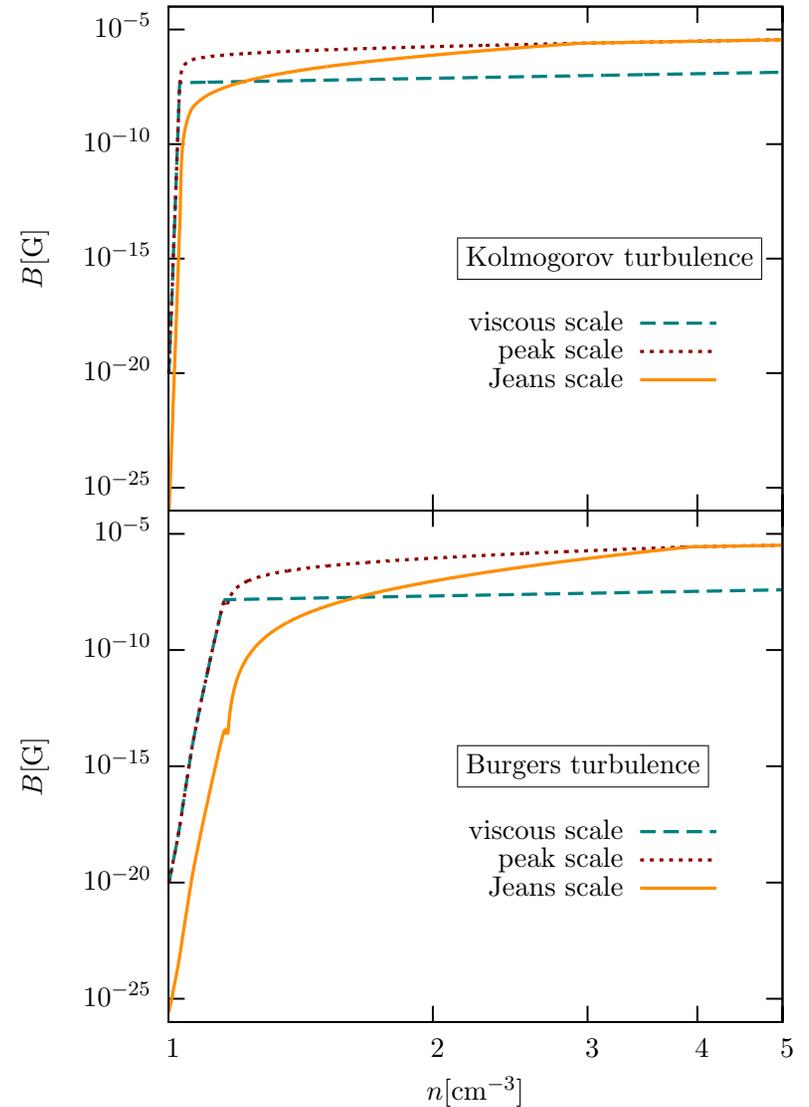


(Schober et al., 2012, PRE, 85, 026303, see also Schober et al. 2012, ApJ, 754, 99)

# in primordial minihalos



**Figure 8.** The growth rate on the Jeans scale  $\Gamma_J$  after the dynamo amplification compared to the diffusion rates as a function of the number density.  $\Gamma_{\text{Ohm},J}$  and  $\Gamma_{\text{AD},J}$  are the Ohmic and ambipolar diffusion rate, respectively.

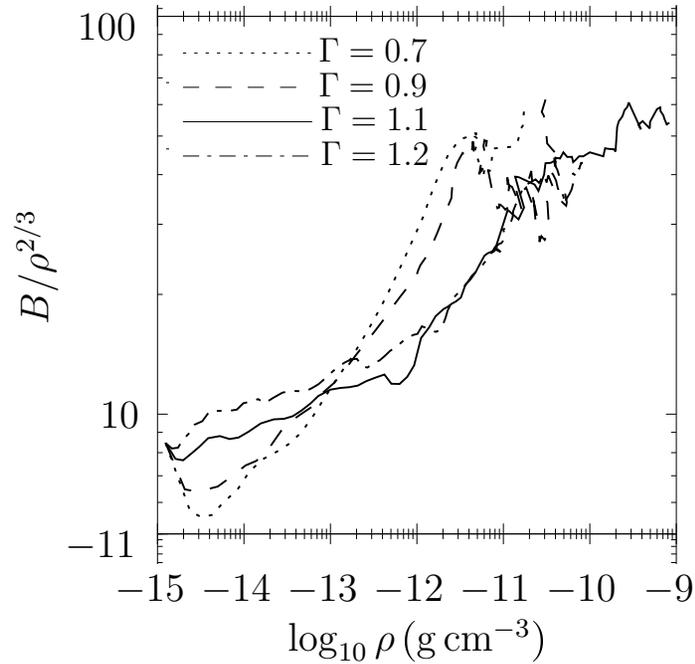


**Figure 7.** The magnetic field strength as a function of the number density on different scales. The dashed green line corresponds to the field evolution on the viscous scale, the dotted red line to the peak scale and the solid orange line to the Jeans scale. We show the results for Kolmogorov turbulence in the upper plot and the results for Burgers turbulence in the lower plot.

# questions

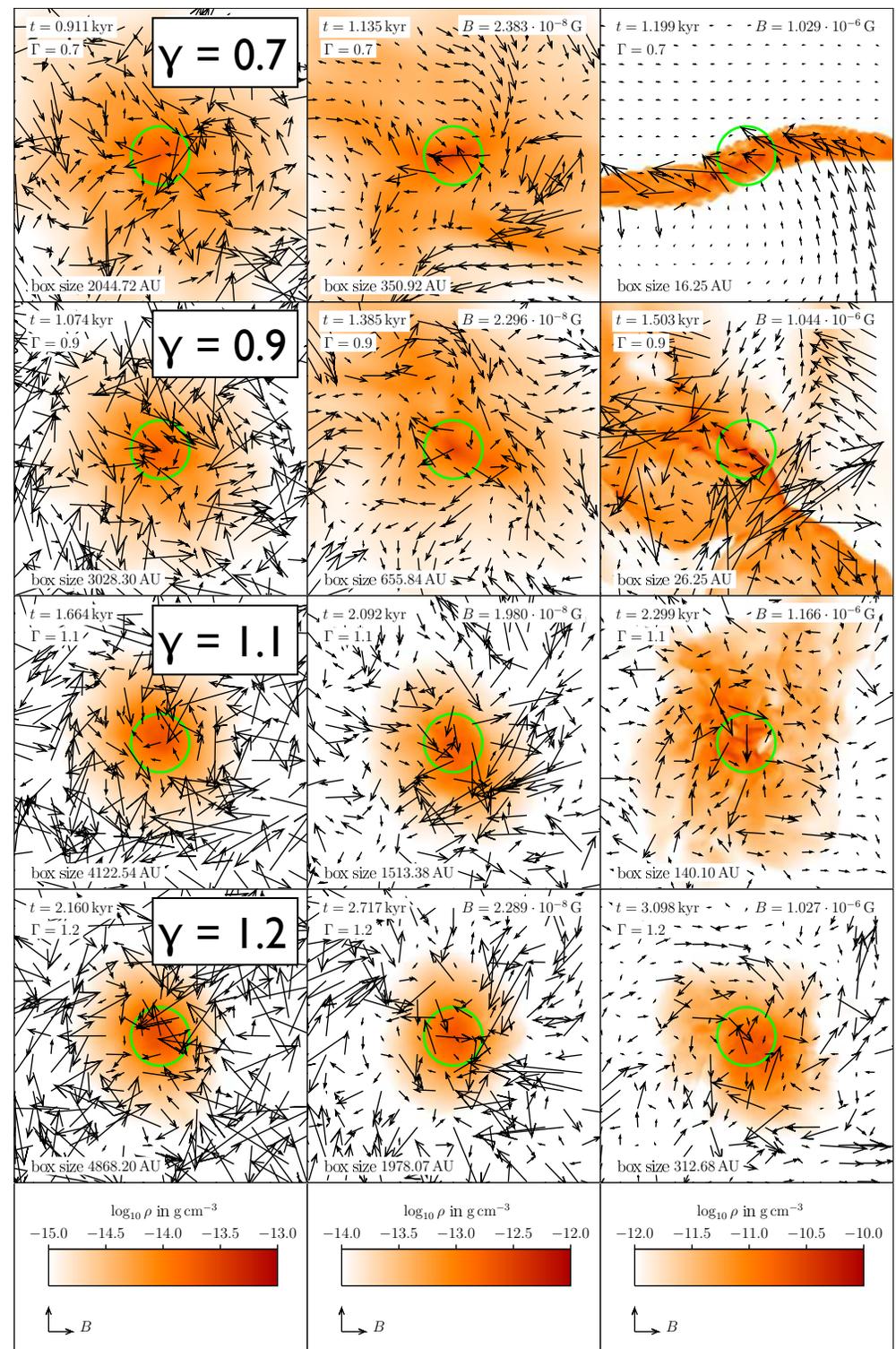
- *small-scale turbulent dynamo* is expected to operate during Pop III star formation
- process is *fast* ( $10^4 \times t_{\text{ff}}$ ), so primordial halos may collapse with B-field at *saturation level!*
- simple models indicate *saturation levels of  $\sim 10\%$*   
--> larger values via  $\alpha\Omega$  dynamo?
- **QUESTIONS:**
  - does this hold for “proper” halo calculations (with chemistry and cosmological context)?
  - what is the strength of the seed magnetic field?

# Dependence on EOS



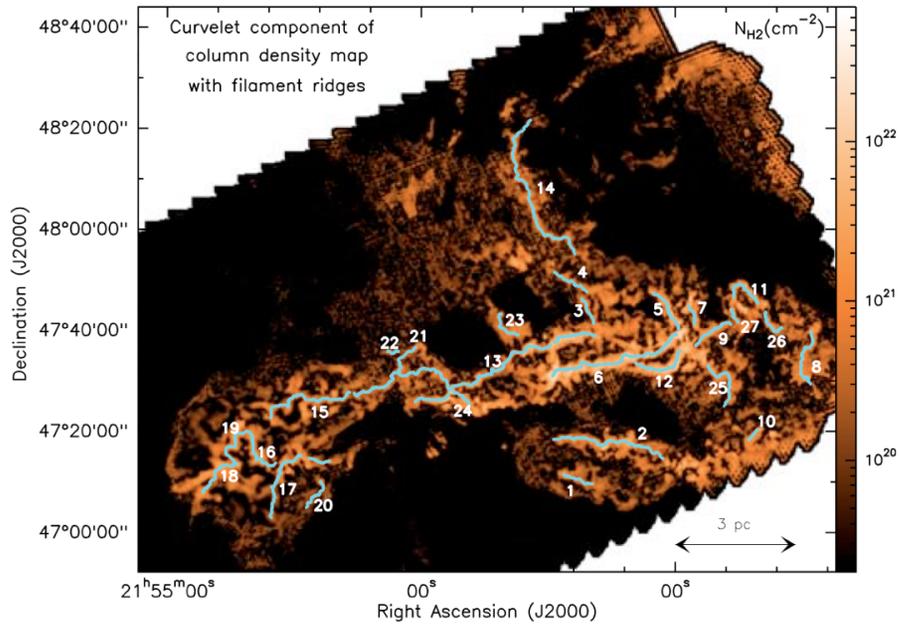
- magnetic field amplification for all gamma.
- *BUT*: very different morphology:
  - *filaments* for  $\gamma < 1$  and
  - *roundish structures* for  $\gamma > 1$
- implications for present-day molecular clouds?

Peters et al. (2012, ApJ, in press -- arXiv:1209.5861)



zooming in on collapsing core

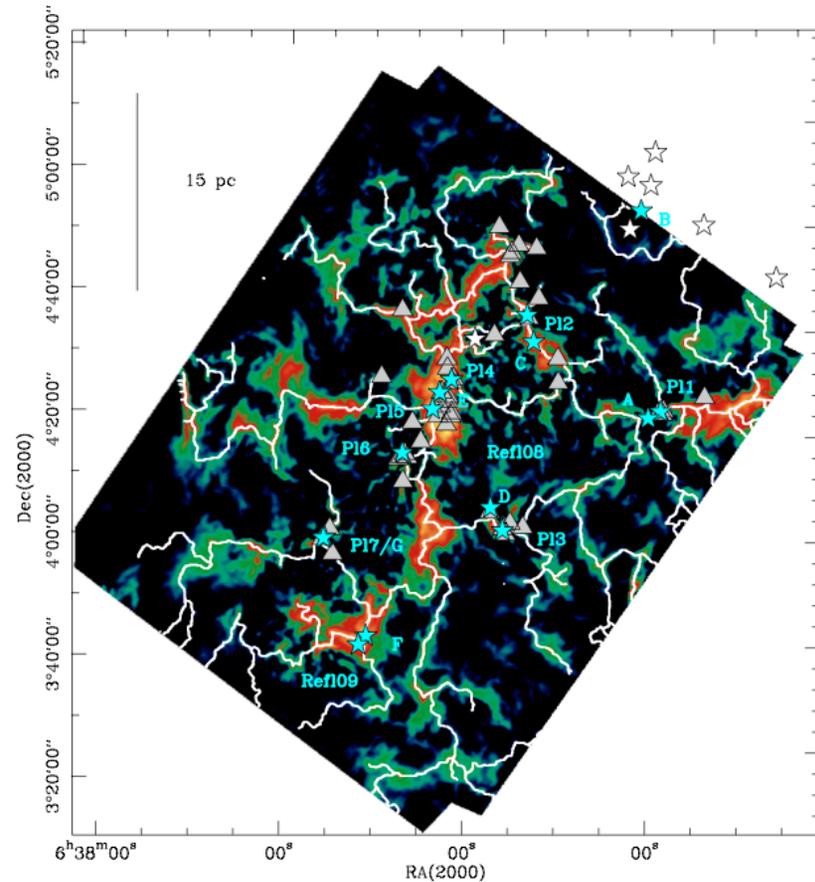
# Filaments in nearby molecular clouds



## IC 5146 as seen by Herschel

Arzoumanian et al. (2011, 529, L6)

- **QUESTION:** to what degree are the filaments seen in nearby molecular clouds caused by EOS effects.
- molecular clouds form in thermally unstable gas with  $\gamma \sim 0.7$  (i.e. they are in a cooling regime)



## Rosette as seen by Herschel

Schneider et al. (2012, A&A, 540, L11)

dark matter  
annihilation

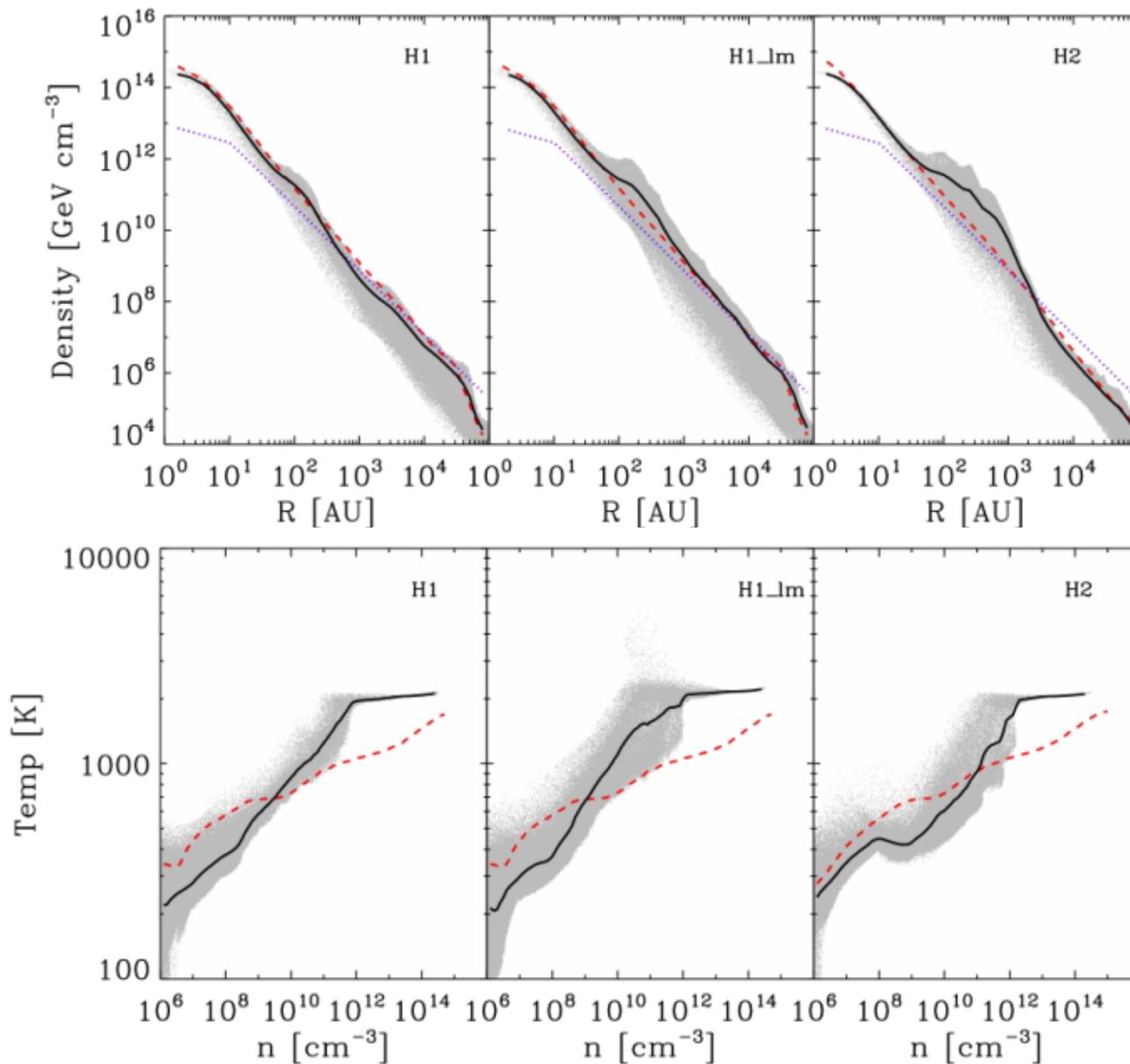
# DM annihilation and SF

- assume there is DM and that the DM particles can self-annihilate (e.g. lowest-mass SUSY particle)
- adiabatic contraction will drag in DM particles as the gas collapses in the center of primordial halo  
--> as  $\rho$  increases, the annihilation rate goes up
- is there an evolutionary phase, when heating by DM annihilation compensates all cooling processes?  
--> *YES* say Freese et al. (2008), Spolyar et al. (2009), Gondolo et al. (2013, arXiv)  
--> *MAYBE NOT* say Iocco et al. (2008), Ripamonti & Iocco (2010), Hirano et al. (2011), Stacy et al. (2012), Rowan Smith et al. (2013)

**Table 1**  
Overview of Simulations

Simulation	Annihilation	DM Particle Mass (GeV)
H1-ref	No	0
H1-lm	Yes	10
H1	Yes	100
H1-hm	Yes	1000
H2-ref	No	0
H2	Yes	100

Two different halo models with different assumptions of the DM particle mass.



— mean gas density / temperature  
with DM annihilation

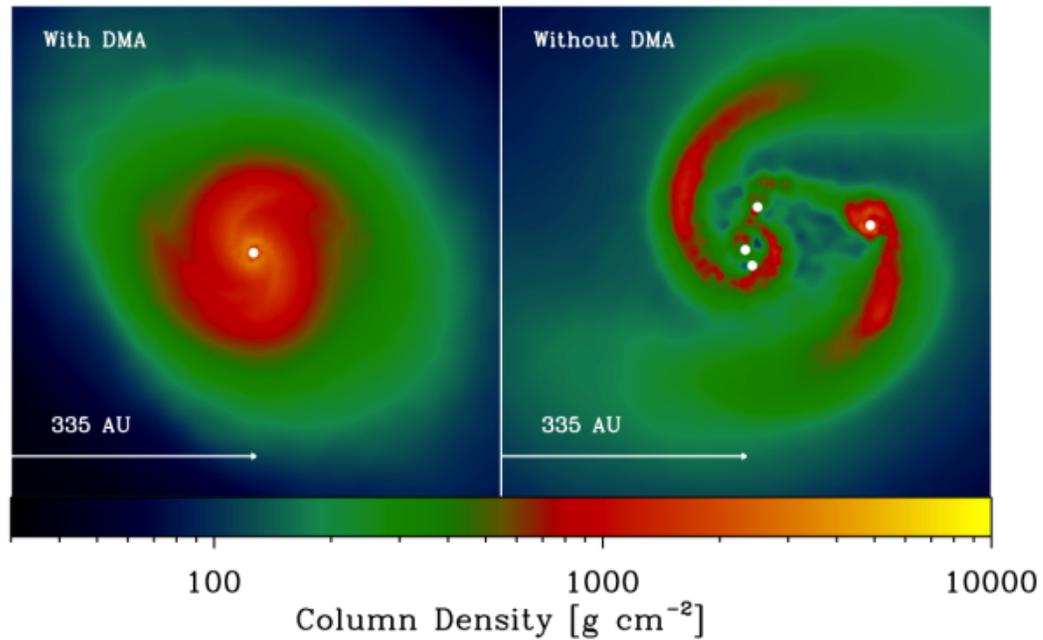
- - - reference case without DM annihilation

⋯ DM density

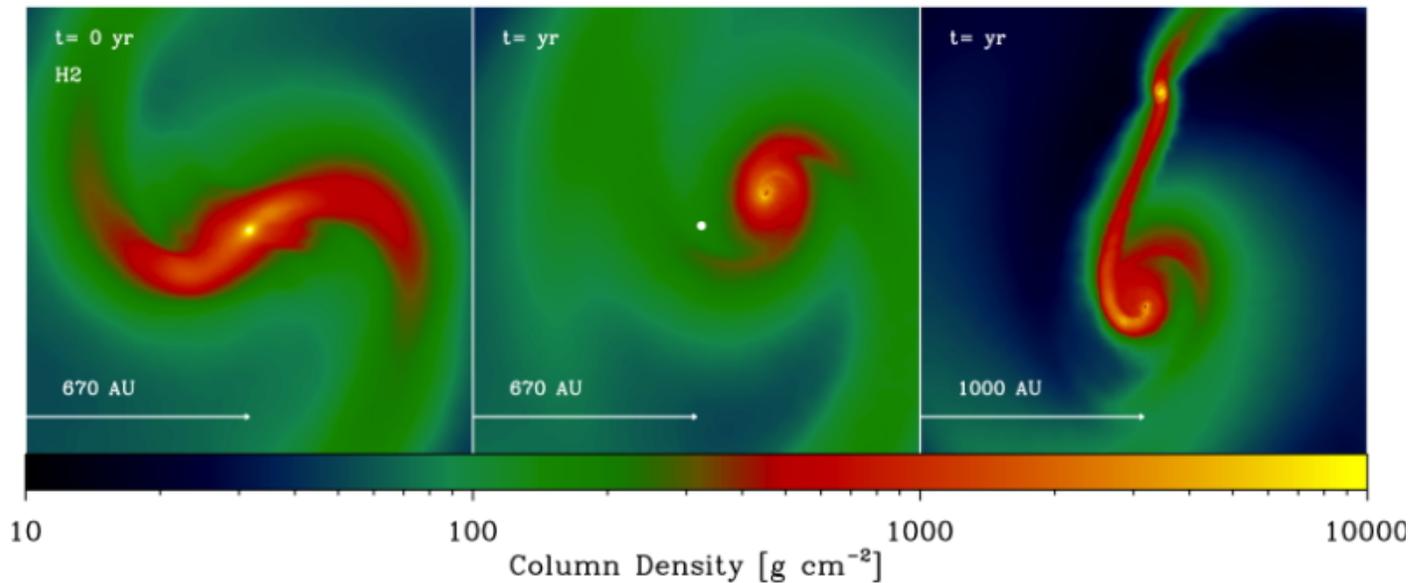


**DM annihilation leads  
to disk heating and  
reduced fragmentation**

**Fig 3:** The column density at the centre of H1 with and without DMA feedback 500 yr after the first sink forms. Without DMA three additional sink particles form, however with DMA the disk is stable and does not fragment.

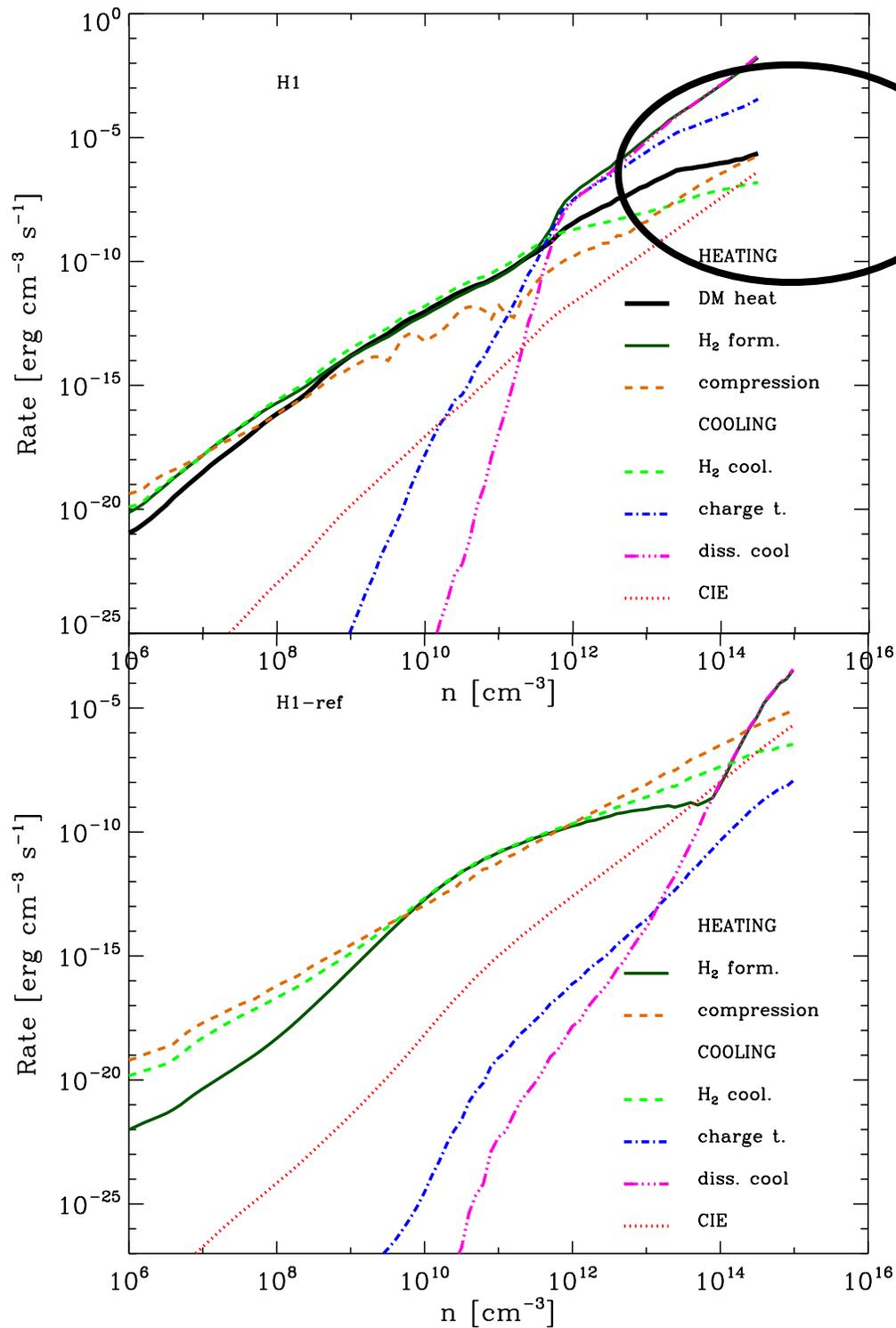


fragmentation  
without DM  
annihilation  
heating



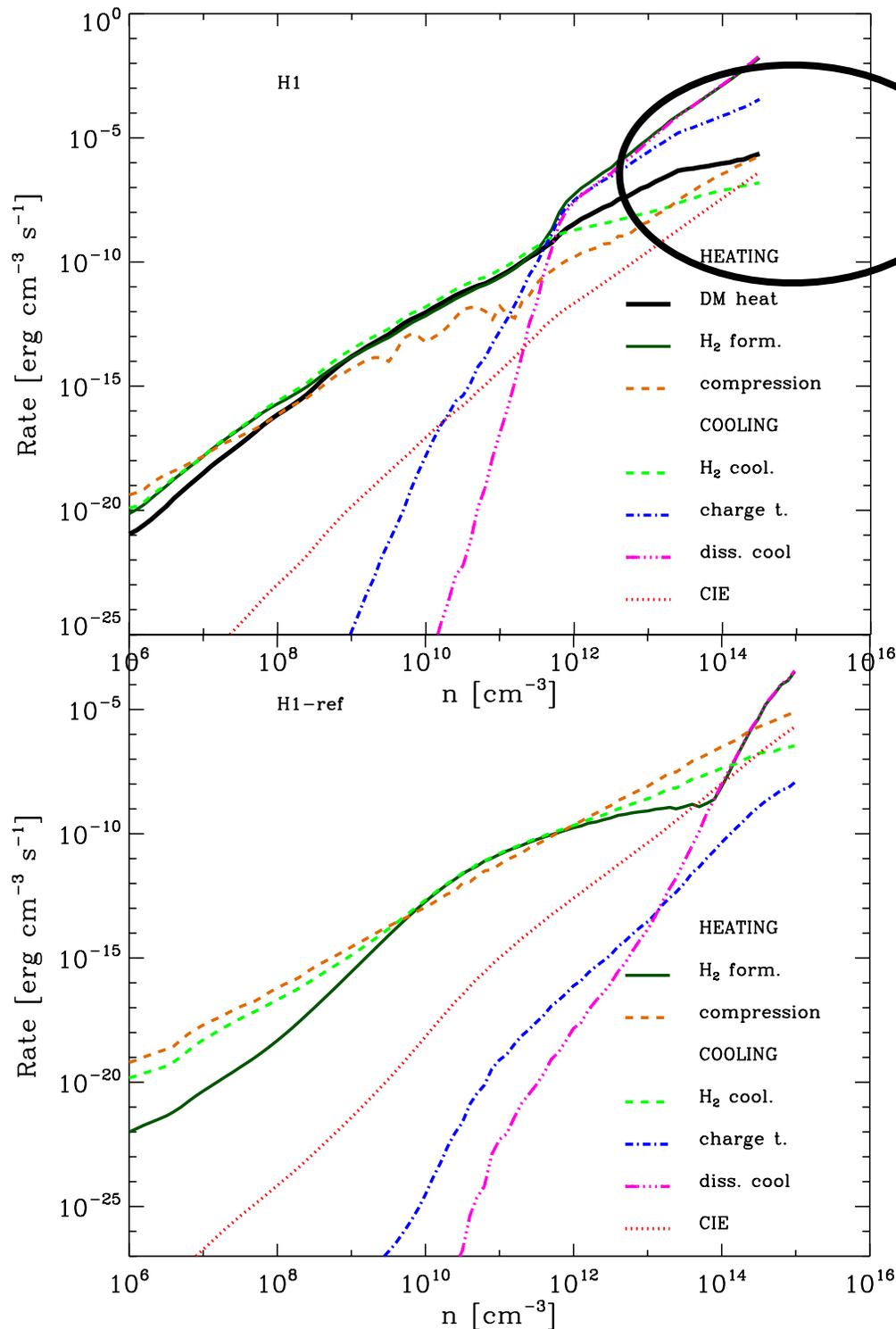
reduced  
fragmentation  
with DM  
annihilation  
heating

**Fig 4:** The column density at the centre of H2 at three times after the sink particle forms. A sink particle is formed at a separation of 1000 AU from the central object after a period of ? Interestingly the sink protostar has become displaced from its original position in panel 2 introducing the possibility that the baryons may eventually decouple from the DM peak.



net heating in  
density range up  
to few  $\times 10^{12} \text{ cm}^{-3}$

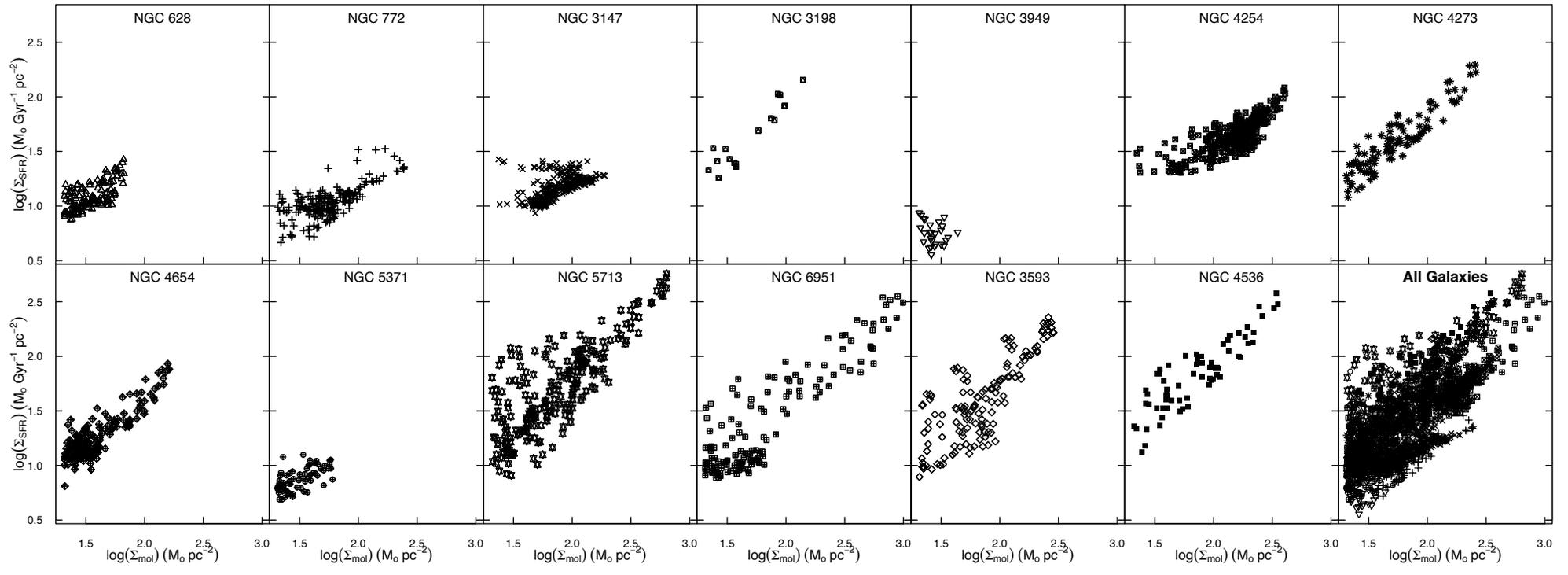
but at higher  $n$ ,  
cooling dominates

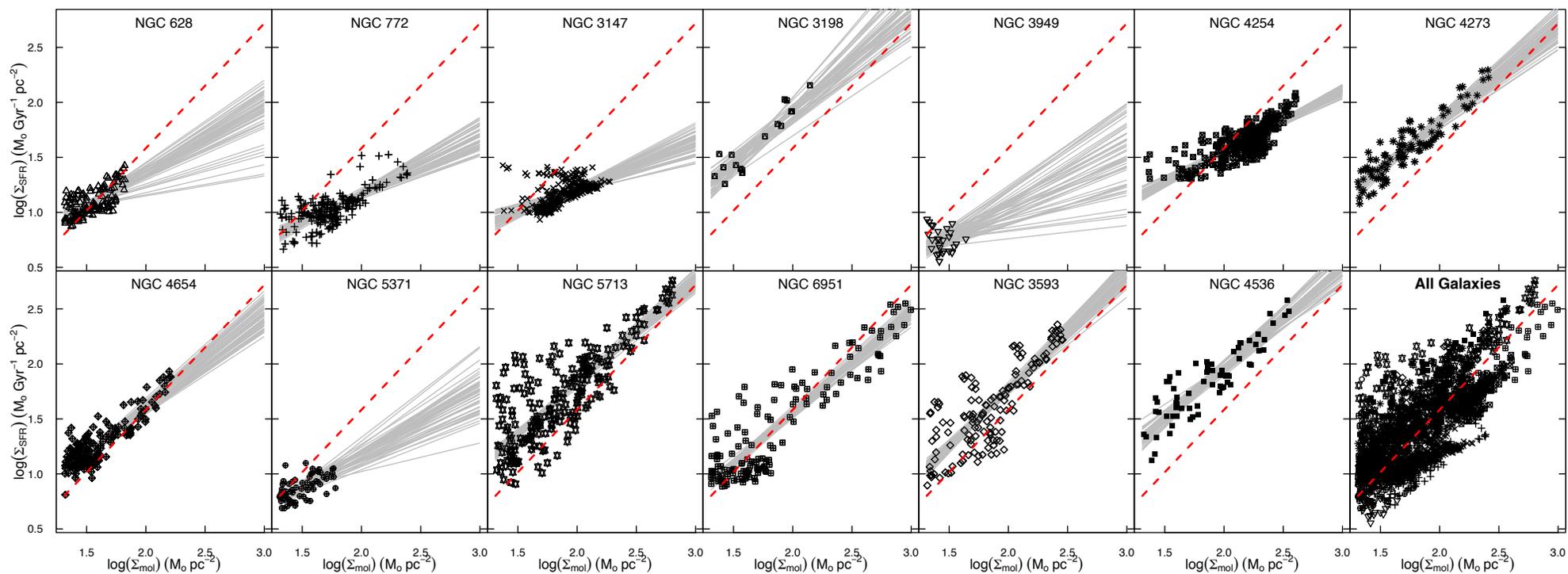


net heating in  
density range up  
to few  $\times 10^{12} \text{ cm}^{-3}$   
  
but at higher  $n$ ,  
cooling dominates

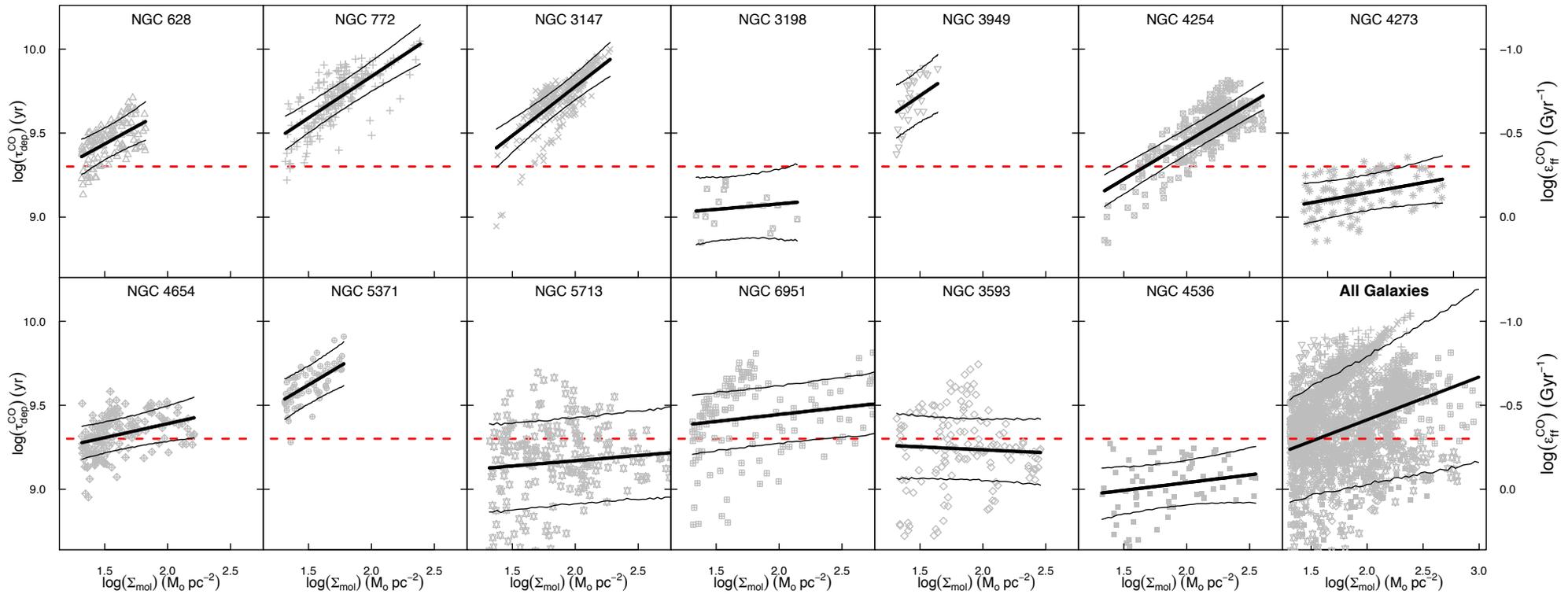
- DM annihilation does not stop collapse (see also Ripamonti & Iocco 2010)
- *BUT*: maybe we did not go to high enough densities (Gondolo et al. 2013)
- *STILL TO DO*: consistent calculation with live DM halo







Hierarchical Bayesian model for STING galaxies reveal large galaxy-to-galaxy *variations* and typically a *sublinear slope*.



Hierarchical Bayesian model for STING galaxies indicate *varying depleting times*.

**Table 1.** Bayesian estimated parameters for the STING galaxies

Subject	# Datapoints	$A$	$2\sigma_A$	$N$	$2\sigma_N$	$\sigma_{\text{scat}}$	$\tau_{\text{dep}}^{\text{CO}}(\Sigma_{\text{mol}}=50)^1$	$\tau_{\text{dep}}^{\text{CO}}(\Sigma_{\text{mol}}=100)^1$	$\tau_{\text{dep}}^{\text{CO}}(\Sigma_{\text{mol}}=150)^1$	$\tau_{\text{dep}}^{\text{CO}}(\Sigma_{\text{mol}}=200)^1$
1. NGC 0337	3	0.33	[−0.16, 0.91]	1.08	[0.68, 1.45]	0.09	0.1, 0.3, 0.9	0.1, 0.3, 1.1	0.1, 0.3, 1.2	0.1, 0.3, 1.2
2. NGC 0628	131	0.05	[−0.23, 0.38]	0.67	[0.46, 0.86]	0.04	2.6, 3.3, 4.1	3.2, 4.4, 6.2	3.5, 5.2, 7.8	3.8, 5.8, 9.3
3. NGC 0772	217	0.14	[−0.08, 0.34]	0.51	[0.40, 0.64]	0.04	4.0, 4.9, 6.0	5.6, 6.9, 8.4	6.7, 8.4, 10.5	7.6, 9.7, 12.5
4. NGC 1637	47	0.18	[−0.12, 0.59]	0.61	[0.34, 0.82]	0.05	2.2, 3.0, 4.2	2.6, 4.0, 6.3	2.8, 4.7, 8.5	2.9, 5.3, 10.1
5. NGC 3147	298	0.36	[ 0.10, 0.60]	0.43	[0.31, 0.57]	0.03	3.3, 4, 4.8	5.0, 6.0, 7.2	6.2, 7.6, 9.4	7.1, 8.9, 11.4
6. NGC 3198	18	0.05	[−0.39, 0.47]	0.93	[0.69, 1.20]	0.07	0.7, 1.2, 1.8	0.7, 1.2, 1.9	0.7, 1.2, 2.1	0.7, 1.3, 2.2
7. NGC 3593	141	−0.28	[−0.51, 0.07]	1.02	[0.91, 1.14]	0.08	1.1, 1.8, 2.7	1.1, 1.7, 2.6	1.1, 1.7, 2.6	1.1, 1.7, 2.6
8. NGC 3949	27	0.02	[−0.39, 0.53]	0.51	[0.14, 0.79]	0.06	4.4, 6.7, 10.0	5.3, 9.4, 17.2	5.9, 11.6, 24.1	6.2, 13.3, 30.4
9. NGC 4254	308	0.40	[ 0.20, 0.59]	0.57	[0.49, 0.67]	0.04	1.7, 2.1, 2.5	2.4, 2.8, 3.4	2.8, 3.4, 4.0	3.2, 3.8, 4.6
10. NGC 4273	103	0.06	[−0.17, 0.25]	0.89	[0.78, 1.02]	0.05	1.1, 1.4, 1.7	1.1, 1.5, 1.9	1.2, 1.6, 2.1	1.2, 1.6, 2.2
11. NGC 4536	67	0.15	[−0.13, 0.40]	0.90	[0.77, 1.05]	0.06	0.8, 1.0, 1.4	0.8, 1.1, 1.5	0.8, 1.1, 1.6	0.8, 1.2, 1.6
12. NGC 4654	168	−0.06	[−0.42, 0.16]	0.83	[0.70, 1.05]	0.04	1.8, 2.2, 2.7	1.9, 2.5, 3.2	2.0, 2.6, 3.4	2.1, 2.8, 3.8
13. NGC 5371	65	0.01	[−0.36, 0.45]	0.58	[0.28, 0.82]	0.05	3.9, 5.1, 6.8	4.8, 7.0, 10.1	5.4, 8.4, 13.0	5.8, 9.6, 15.5
14. NGC 5713	220	−0.04	[−0.20, 0.12]	0.94	[0.85, 1.01]	0.13	0.8, 1.4, 2.5	0.8, 1.5, 2.7	0.8, 1.5, 2.7	0.9, 1.6, 2.8
15. NGC 6951	135	−0.27	[−0.42, 0.11]	0.91	[0.83, 0.99]	0.08	1.8, 2.6, 3.9	1.9, 2.8, 4.1	1.9, 2.9, 4.3	2.0, 3.0, 4.4
<b>Group Parameters</b>	1948	<b>0.07</b>	<b>[−0.11, 0.27]</b>	<b>0.76</b>	<b>[0.60, 0.92]</b>	0.09	1.0, 2.2, 4.8	1.1, 2.6, 6.2	1.1, 2.9, 7.3	1.2, 3.1, 8.2

slope of KS relation

depletion times

# implications

- modern hierarchical Bayesian methods suggest the KS relation will vary from galaxy to galaxy and the slope of  $N_{\text{H}_2}$  vs.  $N_{\text{SFR}}$  is sublinear.
- that implies the depletion time is *larger* at higher (column) densities
- why?
  - maybe CO is not a good tracer of SF (see also the extended discussion in Leroy et al. 2013)
  - maybe there is  $\text{H}_2$  that is not traced by CO at low average densities (see Simon Glover's talk)
  - a large fraction of  $\text{H}_2$  may not be forming stars (low SFE)

summary

# summary

- magnetic fields will influence first star formation  
→ influence on mass spectrum still not understood
- dark matter annihilation will not lead to “dark stars”, but it could reduce the level of fragmentation in first disks and influence Pop III mass spectrum and multiplicity
- on global scales the relation between molecular gas surface density and star formation (Kennicutt-Schmidt relation) varies from galaxy to galaxy and it seem to be sublinear  
→ varying depletion timescales

thanks

