

*Julian Merten*

# *An advanced method to recover mass profiles through gravitational lensing*

Institut für Theoretische Astrophysik

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Universität Heidelberg

INAF - Osservatorio Astronomico di Bologna

June 1<sup>st</sup>, 2010

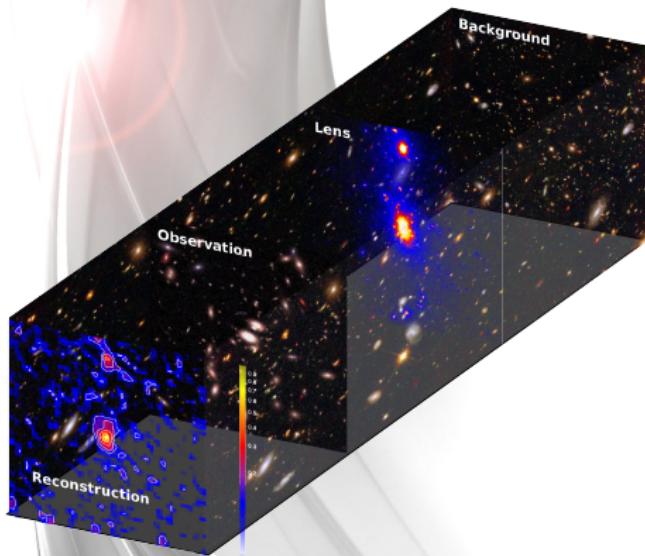
with: Massimo Meneghetti (OABO)  
& Matthias Bartelmann (ITA)



AIfA Bonn



# Outline: A joint lensing reconstruction method



(Figure to appear in  
625 yrs of Heidelberg University)

## 1 Reconstruction method

- A grid based “nonparametric” approach
- A problem of scales and a solution

## 2 Implementation

- The basic concept of GPUs
- GPUs in practice

## 3 Applications

- Realistic simulations
- Real data

## 4 Great things to come

- CLASH (HST/MCT)
- Solving some puzzles

# The basic idea of an “inverse” method (Bartelmann96)

## Spin fields

$$\beta = \theta - \alpha(\theta)$$

$$\partial = \partial_1 + i\partial_2$$

$$\psi$$

$$2\gamma = \partial\partial\psi$$

$$2F = \partial^*\partial\partial\psi$$

$$\partial^* = \partial_1 - i\partial_2$$

$$\alpha = \partial\psi$$

$$2\kappa = \partial^*\partial\psi$$

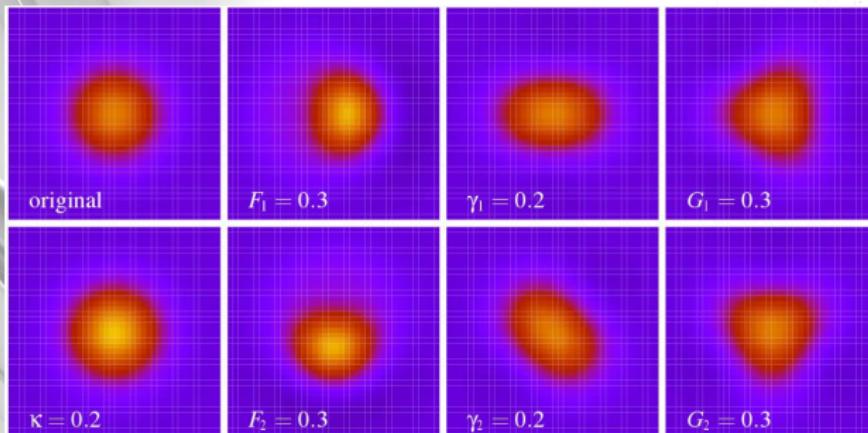
$$2G = \partial\partial\partial\psi$$

## Statistical approach

$$\chi^2(\psi) = \chi_1^2 + \chi_2^2 + \chi_3^2 + \dots$$

Possible constraints:

- Ellipticities of background sources
- Flexion (JM10 in prep.)
- Multiple image systems (Bradač05+)
- Critical curve estimates (JM09+)



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## Other possible constraints

- Optical
  - ▶ Magnification
  - ▶ Member dynamics
- X-ray
- SZ

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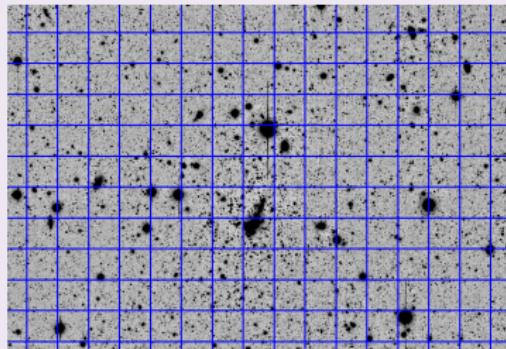
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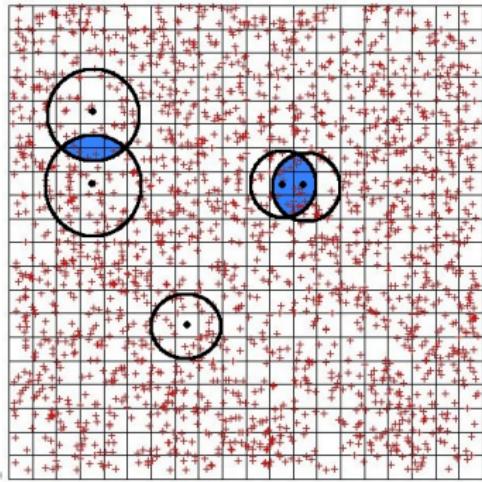
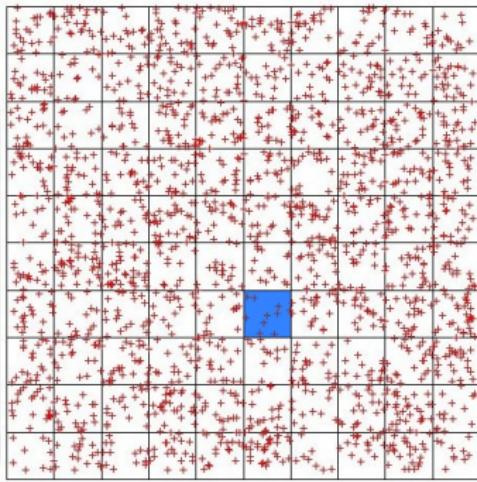
## The trick



$$\frac{\partial \chi^2(\psi_k)}{\partial \psi_l} \stackrel{!}{=} 0 \\ \Rightarrow \mathcal{B}_{lk}\psi_k = \mathcal{V}_l$$

## Example: Weak lensing

$$\chi_w^2(\psi) = \sum_{i,j} \left( \varepsilon - \frac{Z(z)\gamma(\psi)}{1 - Z(z)\kappa(\psi)} \right)_i \mathcal{C}_{ij}^{-1} \left( \varepsilon - \frac{Z(z)\gamma(\psi)}{1 - Z(z)\kappa(\psi)} \right)_j$$



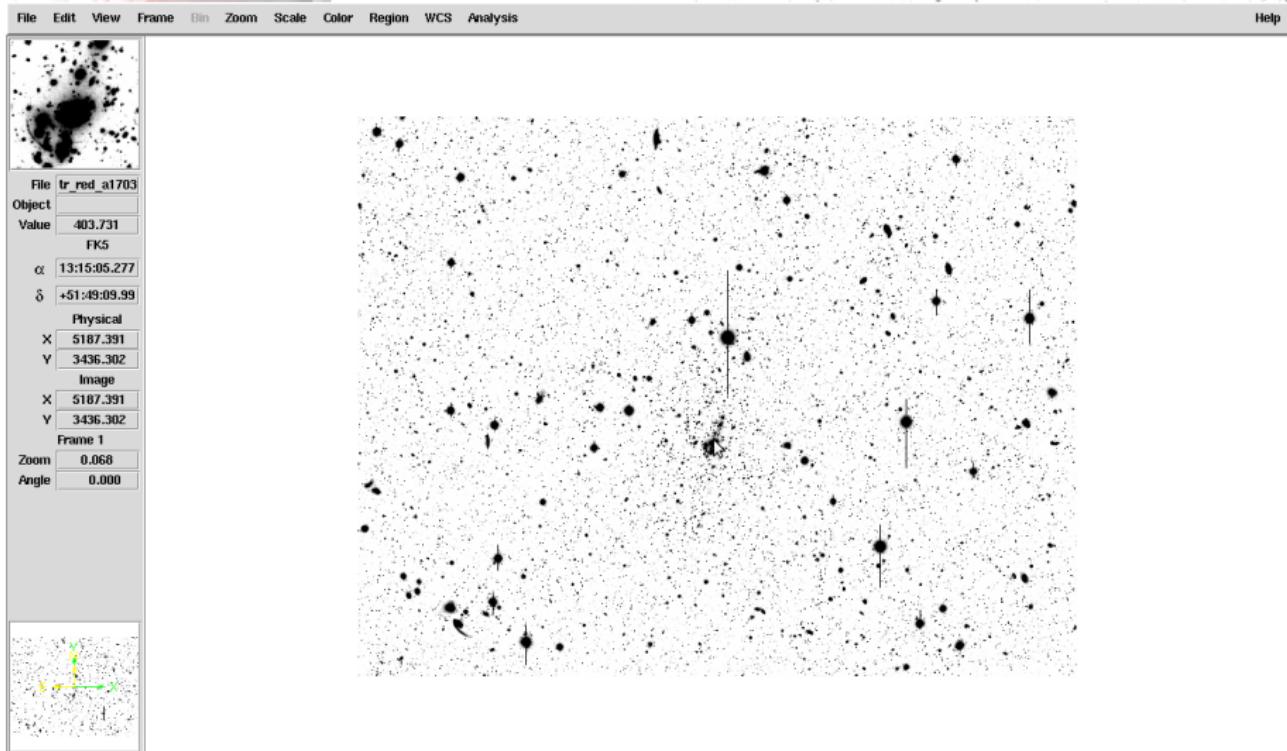
## Example: Strong lensing

$$\chi_s^2(\psi) = \sum_i \frac{\left( (1 - Z(z)\kappa(\psi))^2 - (Z(z)\gamma(\psi))^2 \right)_i^2}{\sigma_i^2}$$



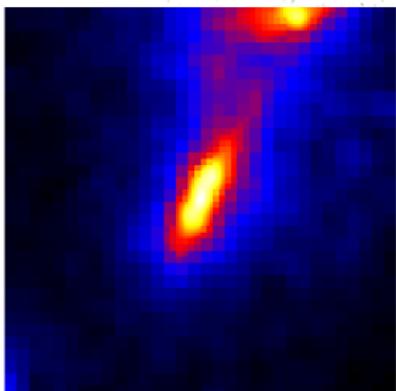
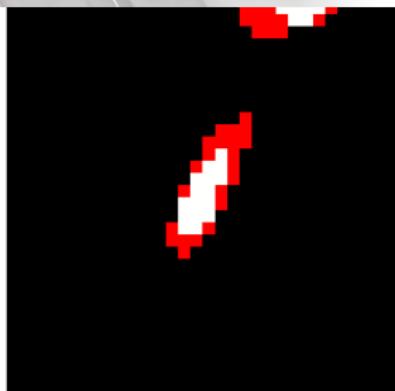
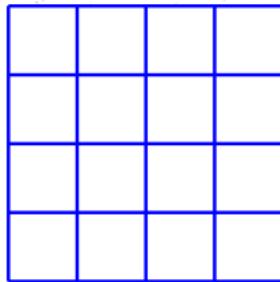
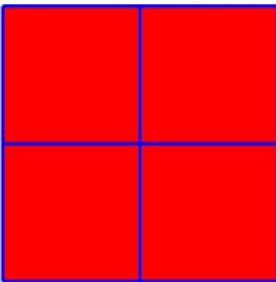
(Figure from Jullo07)

# *A problem of different scales*



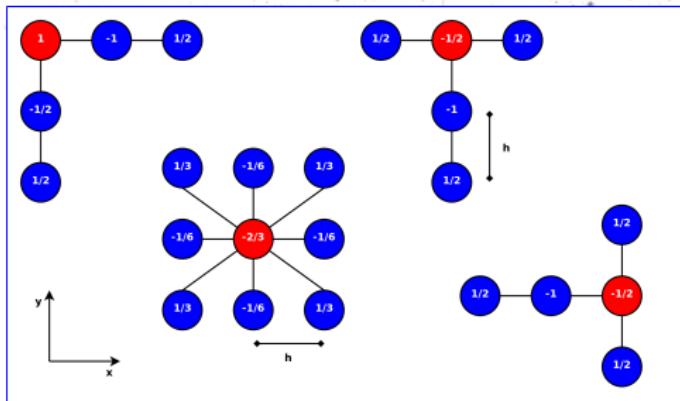
(Abell 1703 in SUBARU r-band)

# Clever merging: AMR (*Bradač09, JM10*)



# Making it all work: Numerics

- $\alpha, \gamma, \kappa, F$  and  $G$  can be expressed by derivatives of  $\psi$  via finite differences.
- Linearisation of the problem.
- 2-level iteration scheme with simple regularisation (Bradač05).



## Problem Runtime

$$\mathcal{B}_{lk}\psi_k = \mathcal{V}_l$$

$$\mathcal{B}_{lk} \sim a_i b_j C_{ij} D_{il} E_{jk}$$

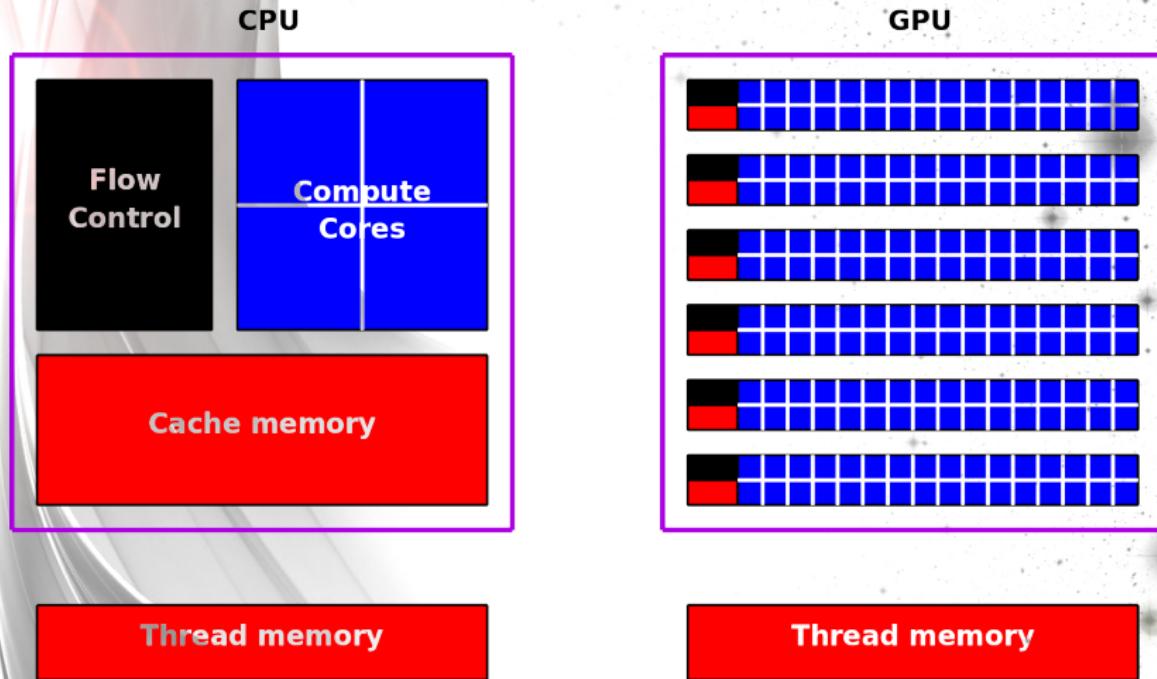
$$\mathcal{V}_l \sim a_i b_j C_{ij} E_{il}$$

$$l, k, i, j \sim \mathcal{O}(\text{grid\_dim}^2)$$

## Geeky implementation facts

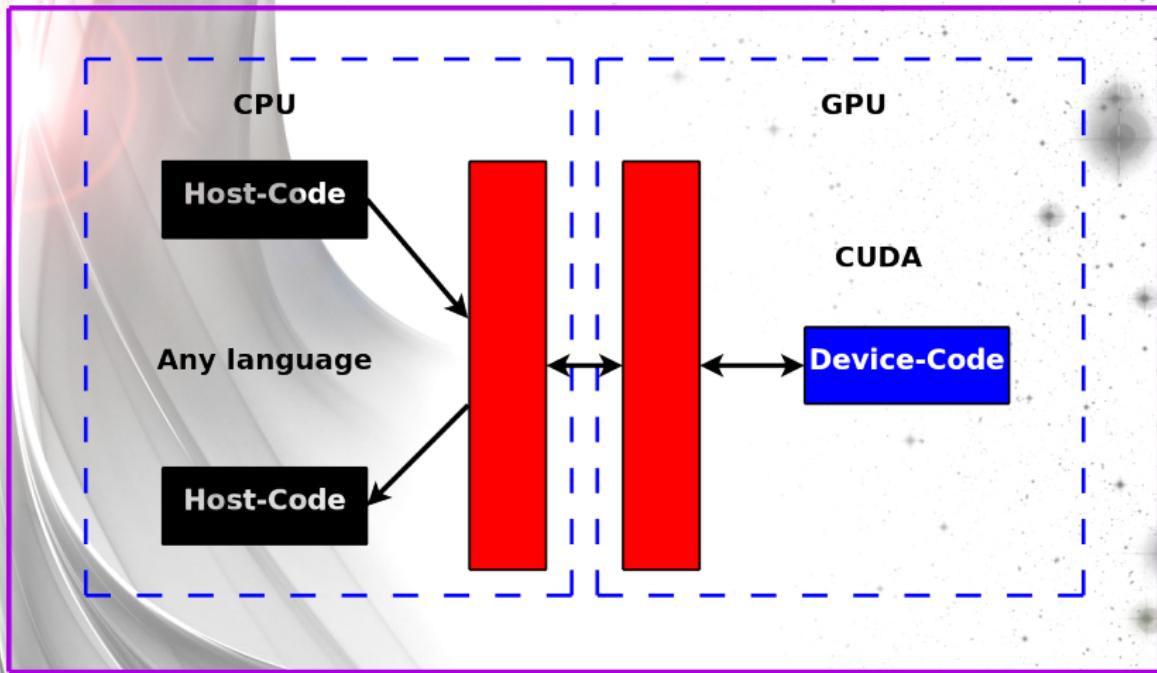
- Parallel C++ code
- medium sized  $\sim 12000$  lines
- Uses GSL, LAPACK, ATLAS, MPI
- Fully documented, including user manual
- and...CUDA...

# *Single node GPU Parallelisation*



- One single GPU allows for massive parallelisation at  $\sim 1/1000$  of the cost, if problem is suited for  $\Rightarrow$  **Data-parallel**.

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# GPUs in practice (JM10 in prep.)

## NVIDIA Tesla C1060

- 240 streaming cores
- 4 GB DDR3 GPU memory
- 933 GFLOPS peak performance
- Upcoming Fermi cards



## Speed-up

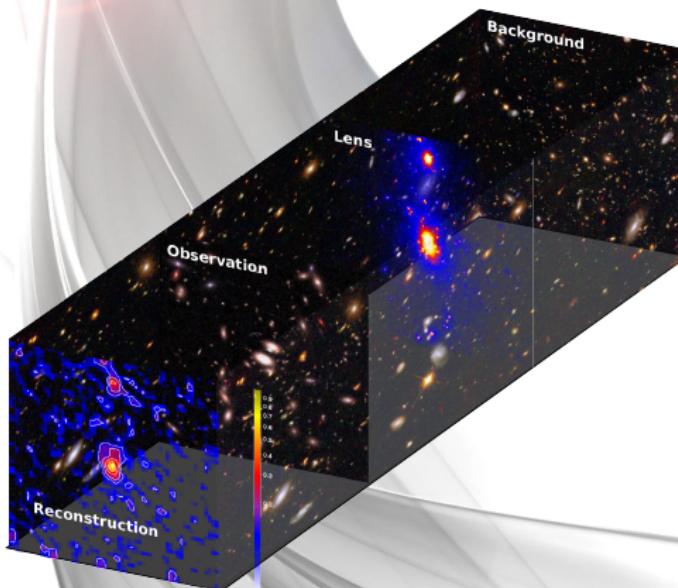
- Calculate:

$$\mathcal{B}_{lk} = a_i b_j \mathcal{C}_{ij} \mathcal{D}_{ik} \mathcal{E}_{jl}$$

- one-core CPU: 82.3 s
- 240 core GPU: 1.03 s

# Realistic lensing simulations: *SkyLens* (Meneghetti, JM 08/09)

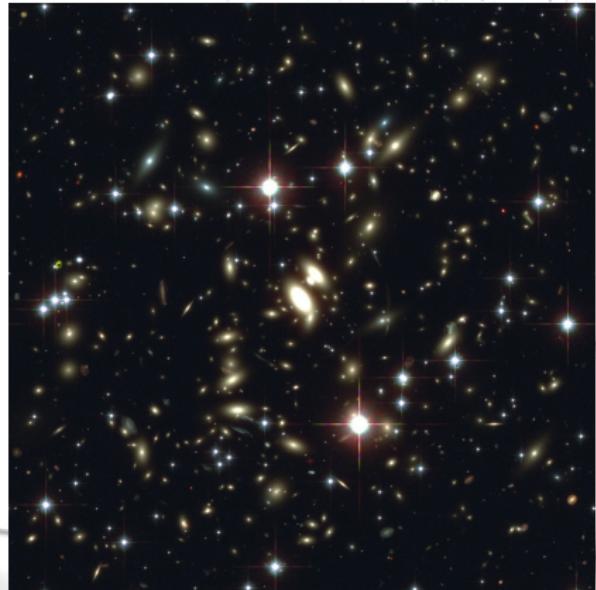
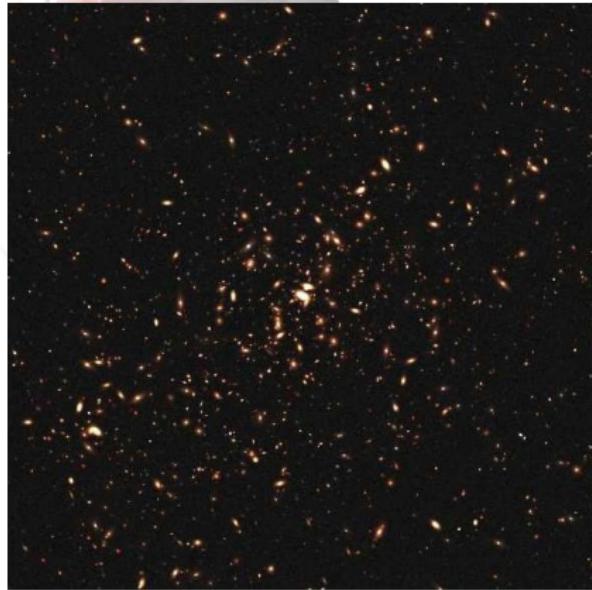
Developers: Massimo Meneghetti, Peter Melchior, Fabio Bellagamba, JM



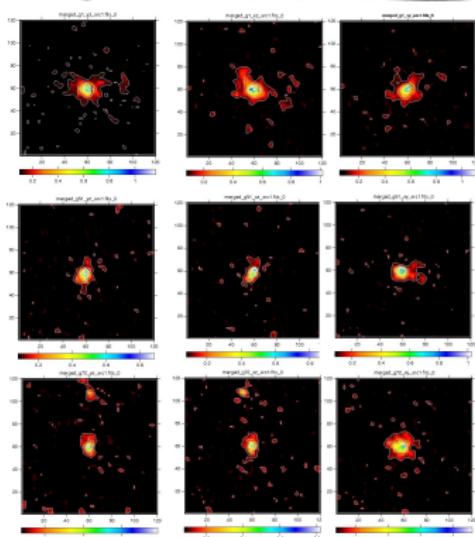
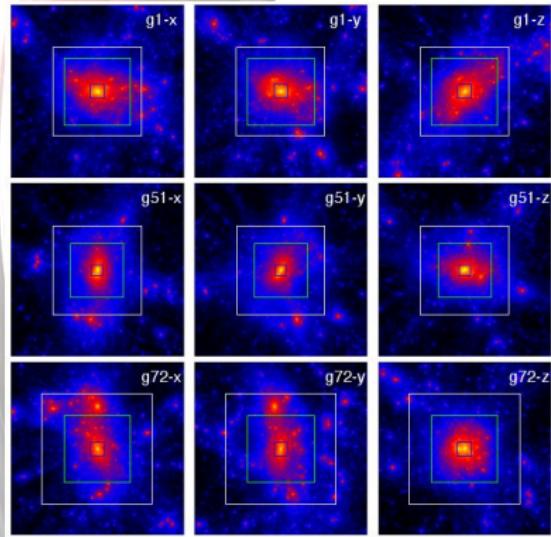
Name	Description
$D$	aperture diameter
$g$	detector gain
$A_{\text{pix}}$	pixel area
$F(\lambda)$	used filter
$M(\lambda)$	mirror filter curve
$O(\lambda)$	optics filter curve
$C(\lambda)$	CCD filter curve
FoV	total field-of-view
RON	detector readout-noise
$f$	flat-field accuracy
$a$	residual flat-field error
PSF	PSF model
$t_{\text{exp}}$	exposure time
$A(\lambda)$	atmospheric extinction
$m_a$	airmass
$\text{SED}_{\text{sky}}$	sky-background emission
$\text{SED}_{\text{gal}}$	background population
$\alpha$	deflection angle map

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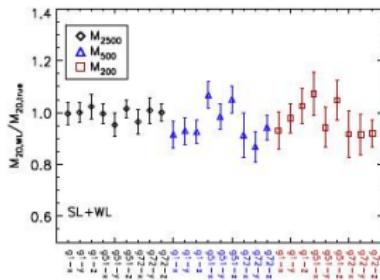
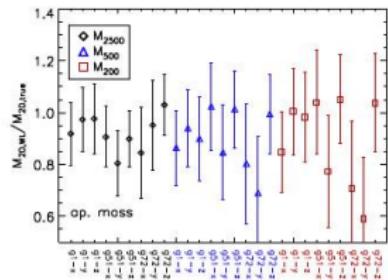
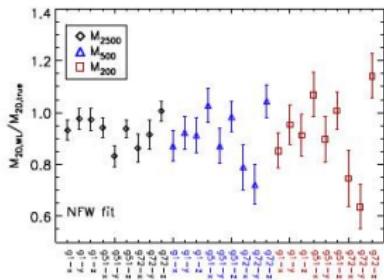
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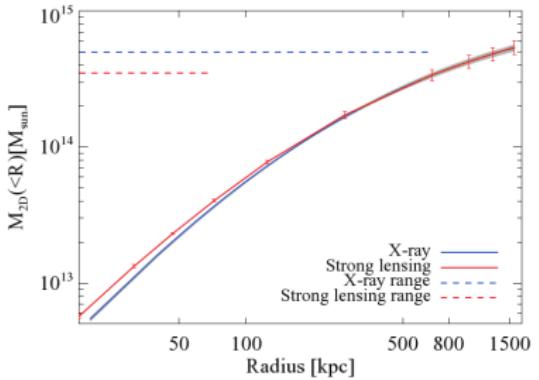
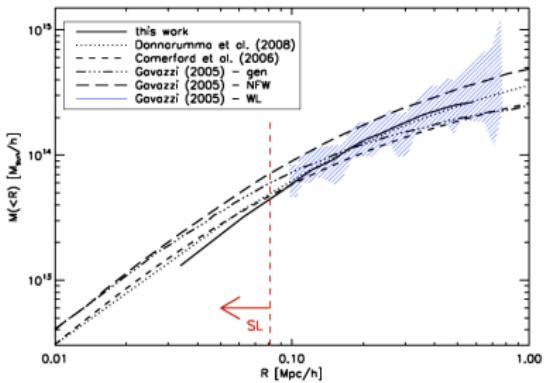
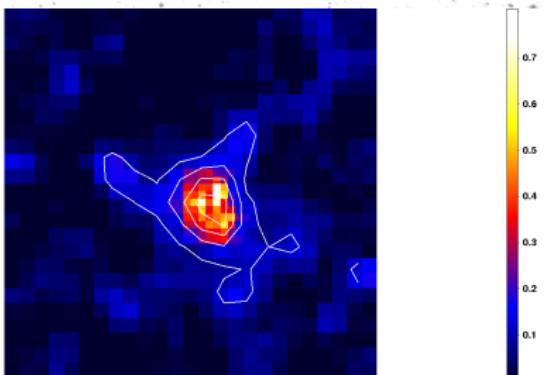
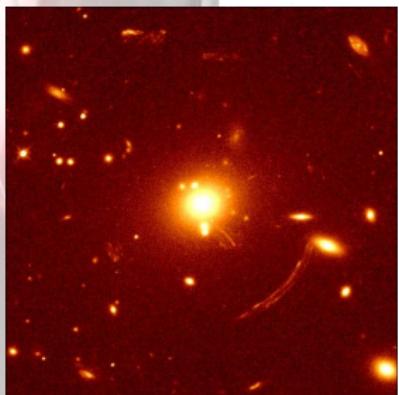
# Weighing simulated galaxy clusters (Meneghetti, JM09)



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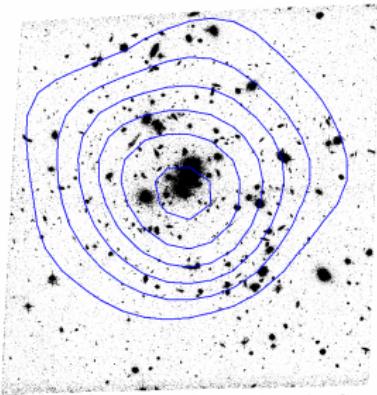
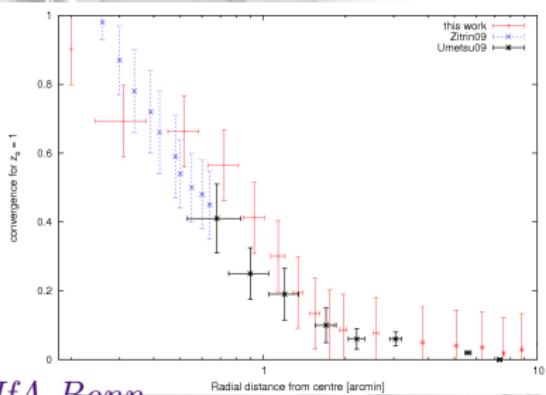
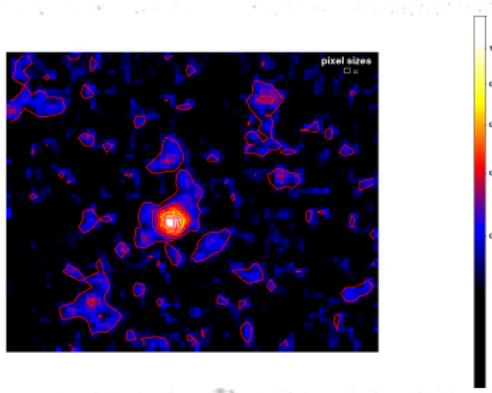
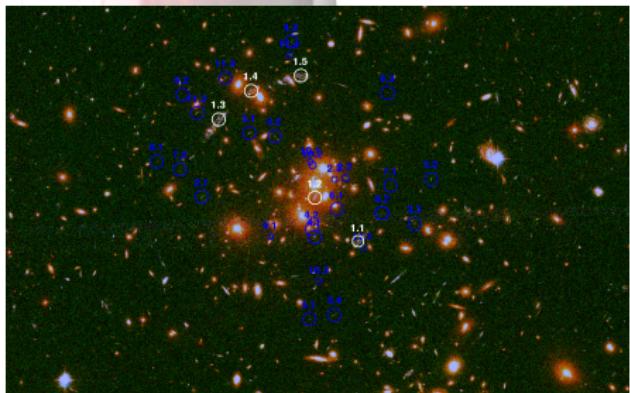


# *MS2137* (*JM09, Donnarumma09*)



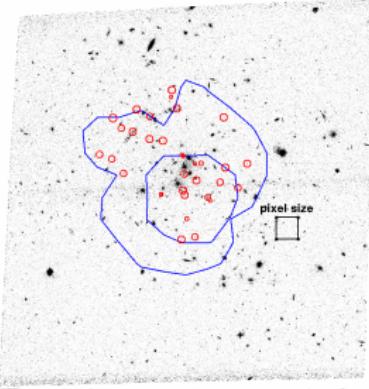
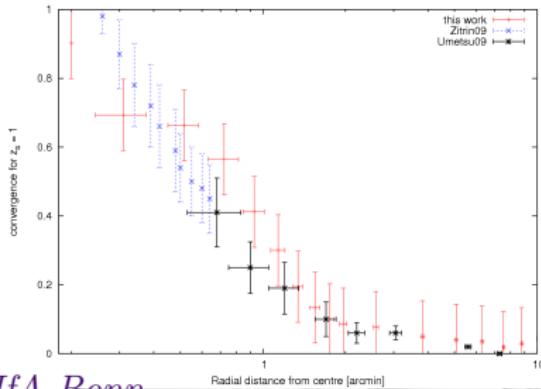
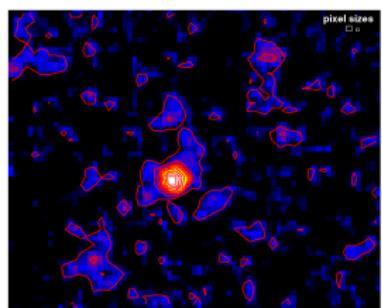
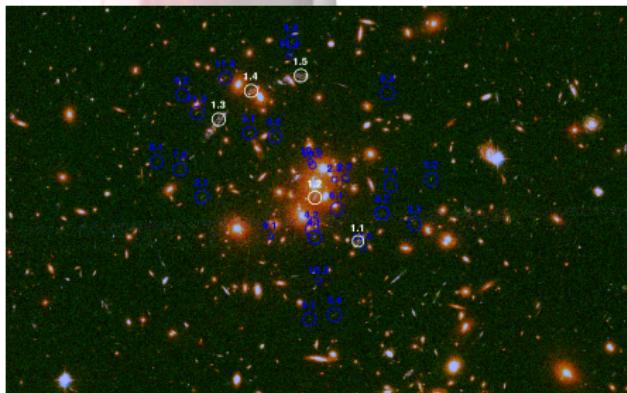
# *CL0024*

with: T. Broadhurst, A. Zitrin, K. Umetsu



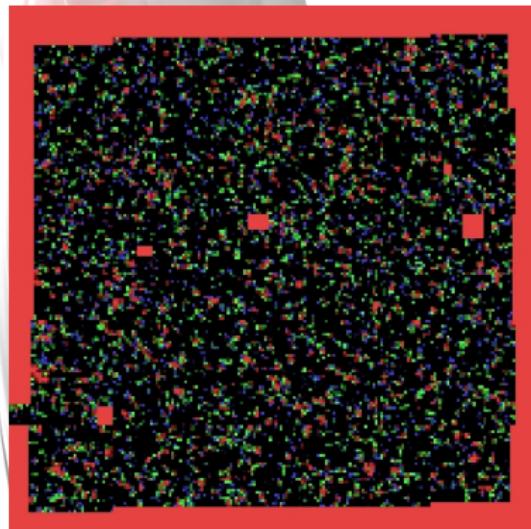
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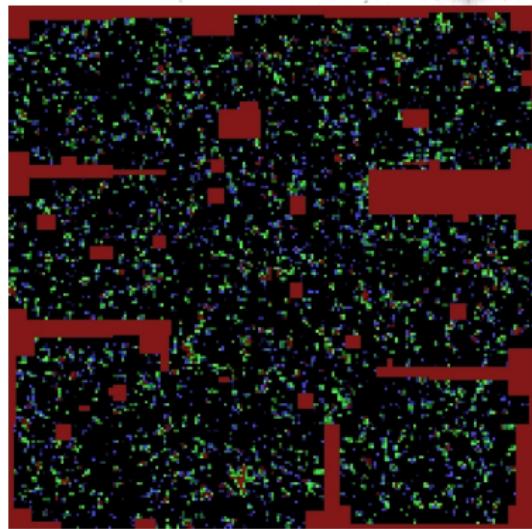


# *Not really official yet: COSMOS*

with: M. Maturi, T.Schrabback



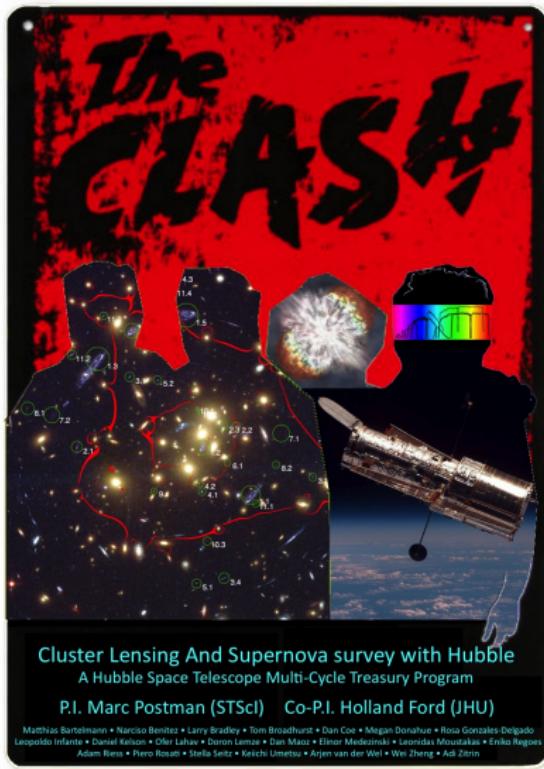
(HST/ACS, the old one)



(SUBARU)

# *Great things to come: The CLASH*

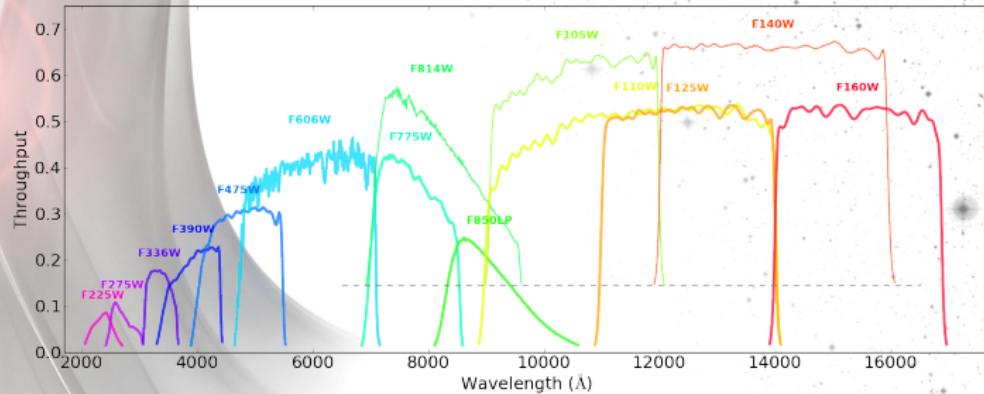
One of three HST/MCT programmes. Start September 2010 (3 cycles).



## Science Drivers

- To map the dark matter in galaxy clusters
- To detect SN out to redshifts  $z > 1.5$
- To detect and characterise  $z > 7$  galaxies
- To study the galaxies in and behind the clusters

# CLASH



## CLASH Facts

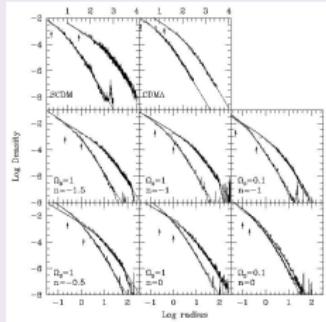
- 25 X-ray clusters
- 524 orbits
- ACS + WFC3 obs.
- 14 (16) wave bands
- wide follow-ups with SUBARU

## Our contribution

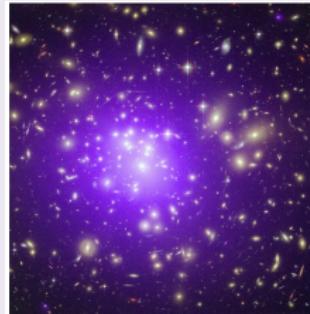
- Full pipeline calibration
- nonparametric DM profiles
- weak-lensing shapes + flexion
- magnification maps for the high-z guys

# Cluster puzzles / Puzzle clusters + c.c.

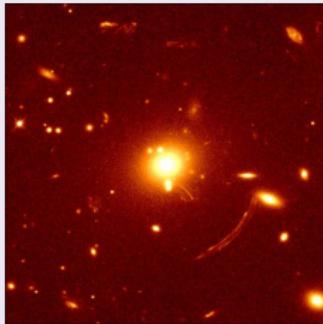
## Density profile



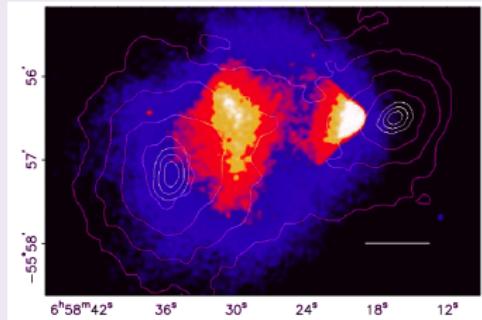
## Cool cores



## Strong lensing



## Extreme dynamics



# Are those puzzles at all?

## Simulations

- State-of-the-art N-body hydro-sims
- As much physics as possible
  - ▶ Cooling
  - ▶ Star formation
  - ▶ AGN/SN feedback
  - ▶ Chemical enrichment
  - ▶ ...
- Detailed sims of individual objects
- Cluster populations from cosmological volumes



## Observations

- State-of-the-art data
  - ▶ HST/ACS/WFPC3
  - ▶ SUBARU/LBT
  - ▶ KECK
  - ▶ CHANDRA / XMM / SUZAKU
- Joint reconstruction method: lensing, X-ray, dynamics, SZ (JM09+, Bradač05+, Puchwein06+)
- reliable error bars
- large cluster sample

Both sides have to be analysed with the **same** tools.